Machine Learning Approaches for Automated Lesion Detection in Microwave Breast Imaging Clinical Data

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10 ABSTRACT

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Breast lesion detection employing state of the art microwave systems provide a safe, non-ionizing technique that can differentiate healthy and non-healthy tissues by exploiting their dielectric properties. In this paper, a microwave apparatus for breast lesion detection is used to accumulate clinical data from subjects undergoing breast examinations at the Department of Diagnostic Imaging, Perugia Hospital, Perugia, Italy. This paper presents the first ever clinical demonstration and comparison of a microwave ultra-wideband (UWB) device augmented by machine learning with subjects who are simultaneously undergoing parameters (S-parameter) are received via a dedicated moving transmitting and receiving antenna set-up. The output of a parallel radiologist study for the same subjects, performed using conventional techniques, is taken to pre-process microwave

data and create suitable data for the machine intelligence system. These data are used to train and investigate several suitable supervised machine learning algorithms nearest neighbour (NN), multi-layer perceptron (MLP) neural network, and support vector machine (SVM) to create an intelligent classification system towards supporting clinicians to recognise breasts with lesions. The results are rigorously analysed, validated through statistical measurements, and found the quadratic kernel of SVM can classify the breast data with 98% accuracy.

12 Introduction

Breast cancer is the most common cancer to affect women worldwide and the second most common cancer overall¹, with 13 nearly 1.7 million new cases diagnosed annually². Mammography, the gold screening standard, is not suggested for screening 14 women under 50 years old due to ionizing radiation exposure concerns. This means that 40% of all women in the EU (age 15 25-49 years old), representing 20% of breast cancer cases in Europe, cannot avail of the the most conventional breast cancer 16 screening modality³. Furthermore, X-ray mammography cannot be undergone frequently, i.e. no more than once every 2 years 17 in the EU, and it is prohibited for obvious reasons during pregnancy⁴. Breast cancer risk increases with further exposure to 18 ionizing radiation from repeated mammography examinations⁵. Women who have undergone such tests also state that the 19 exam is painful, particularly during their premenstrual period, or when the test is performed on women with smaller breasts⁶. 20 Lastly, conventional mammography has been shown to miss approximately 15% of cancer (false negative)^{7,8}. Bearing in 21 mind these limitations, new imaging approaches must be considered. Hitherto, microwave imaging has gained increased 22 attention for its potential in breast cancer detection scenarios, fortified by the measurable variations in the dielectric properties 23 of malignant and normal tissues at the microwave frequency ranges used. Explicitly, the work presented by Li, Xu, et al.⁹ and 24 Bond, Essex J., et al.¹⁰, demonstrated that a substantial contrast between malignant and healthy breast tissue is present; this 25 contrast was demonstrated to be up to a factor of five in conductivity and permittivity. More recent works propose that this 26 contrast is only between malignant and fatty breast tissues, with a lower contrast (lower than 10% in dielectric properties) is 27 found between healthy fibro glandular and malignant tissues¹¹⁻¹³. Moreover, Lazebnik, Mariya, et al., demonstrated that the 28 dielectric properties of benign lesions are similar to the properties of fibro glandular tissues by¹³. Current microwave breast 29 imaging research can be considered in two categories; microwave tomography and ultra-wideband (UWB) radar techniques¹⁴ 30 A small number of prototypes are at clinical trial stages, including developments by Dartmouth College¹⁵ and the University of 31 Bristol¹⁶. Specifically,¹⁵ employs microwave tomography and employs antennas with a matching liquid, while¹⁶ employs an 32 UWB radar approach and uses an array of 60 antennas with a matching liquid. 33

A UWB microwave prototype (Mammowave UBT etc) has been constructed, tested and validated previously¹⁷. The system 34 operates in air employing two antennas and displays maps of dielectric property changes in tissues. Artefact removal (a 35 matching liquid is not used here) is performed through appropriate mathematical procedures^{18,19}. A Huygens Principle (HP) 36 approach is used to capture differences in dielectric properties and discriminates tissues and tissue condition. Test on phantoms 37 have shown a resolution of 1 mm¹⁸, while a sensitivity of 90% has been achieved in the ongoing clinical trial¹⁹. 38

Recently, machine learning based approaches for breast lesion detection have enjoyed increased attention^{20–22}. Machine learning (ML) can be explicitly used to make decisions based on learned patterns (available datasets) and can automatically 40 create an analytical model for future predictions without direct human intervention. Various methods such as nearest neighbor, neural networks, naive bayes, decision trees, conventional ML algorithms, and some hybrid approaches have been used for classification purpose. Also, deep learning (DL) based methods for tumor classification has been investigated. However, limited to breast lesion microwave imaging, ML and DL for breast lesion detection have been applied hitherto only to microwave datasets obtained through numerical simulations or measurements in phantoms 23-27 and nor ever before to clinical data.

The authors present the first ever work on clinically trialed UWB data augmented by ML for automated safe breast lesion 46 detection. The clinical trial UWB data have been collected at Perugia Hospital, Italy, using the microwave apparatus named 47 "MammoWave", a non-ionizing and X-ray free mammogram invented by UBT Srl, Italy. In this research, we have investigated 48 the prospect of employing ML algorithms for computer-aided breast lesion detection to support clinicians, by reducing overhead 49 and increasing the speed in decision making between healthy and non-healthy lesion patterns from the clinically collected 50 data through the current microwave apparatus. Various ML algorithms have been applied in the field of pattern identification 51 and future prediction. Among them, three popular methods, k-nearest neighbor (kNN), multi-layer perceptron (MLP) neural 52 network, and support vector machine (SVM) are explored here to analyze the acquired labeled MammoWave data thoroughly. 53 These experiments have been performed to fit the labeled training data with the optimal model parameters for predicting the 54 presence of a lesion. The kNN uses a distance-based decision function for classifying lesions and MLP employs a nonlinear 55 activation function to distinguish lesions. The obtained accuracy from these two classifiers is less than 60%, thus more suitable 56 algorithms must be investigated to compare and establish the proposed work. Support vector machine has been investigated 57 using a linear and quadratic kernel, which is faster and has achieved optimal prediction outcomes for lesion classification. 58 These kernels are making SVM a powerful tool that can perform both linear and non-linear classification by mapping the inputs 59 to a high dimensional feature space and separates the categories by a gap that is as wide as possible. The ML outcomes are 60 evaluated through the results obtained from the radiologist's report of the Perugia Hospital. These ML outcomes also have 61

been validated through established statistical measures. Preliminary results show the proposed method produces minimal 62 false-positives and false-negatives compared to other state-of-art methods and develop a viable anonymize method for mass 63

screening breast lesion detection in future. 64

Proposed Methodology 65

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A "pipeline" schematic of the proposed work has been shown in Figure 1. At first a subject undergoing conventional screening 66 is asked to also undertake a parallel UWB imaging examination. In this case the conventional methods offered were echography, 67 mammography, magnetic resonance imaging. The radiologist in charge reviewed the conventional imaging data as usual to 68 make a decision regarding the screening outcome. The radiologist decisions have been considered as a gold standard identity 69 of each breast type investigated. Then, these gold standard labels of the breasts have been employed to train the supervised 70 machine learning algorithms to identify breast lesions automatically via the UWB imaging system. The outcomes of breast 71 lesion detection from radiologists and ML have been compared to ensure system performance. The details of intermediate 72 stages have been described in the following sections. 73

Apparatus description and set-up 74

All of the UWB imaging data used in this paper were collected on subjects using the microwave prototype (MammoWave, UBT 75

Srl, Italy) located at the Department of Diagnostic Imaging, Perugia Hospital, Perugia, Italy. All of the data was anonymized. 76

The functioning principle of the MammoWave system is based on the dielectric property difference between normal tissue and 77

tissue with lesions at microwave frequencies, i.e. the different behaviors that tissues display when irradiated by microwave 78 signals. 79

The hardware of the microwave prototype is composed of an aluminum cylindrical hub and shown in Figure 2. The 80 cylindrical hub represents a shield from external interferences and as a bearing structure for the entire device. On top of 81

the cylindrical hub lies the examination bed. The bed incorporates a plexiglass cup aimed at containing the breast of the 82

patient (facing down), with no pressure added to the breast tissue. Several sizes of this cup are available to accommodate the 83 examination of different breast sizes. 84

The transmit and receive (T_X and R_X respectively) antennas are positioned inside the hub and external to the cup, as shown 85 in Figure 3. They can rotate around the azimuth, to irradiate the breast (through T_X) and receive signals scattered by the breast 86



Figure 1. Flow diagram of the proposed work.

itself (through R_X). T_X and R_X have a distance from the center $a_1=20$ cm and $a_0=7$ cm, respectively. Both T_X and R_X are

linearly polarized, operate in the 1-9 GHz frequency band and are connected to a vector network analyzer - VNA (Copper

⁸⁹ Mountain, Indianapolis, IN). Specifically, the received signals are the complex S21 data from the VNA. In particular, R_X can be

⁹⁰ rotated to measure the received signal at the points $rx_{np} \equiv (a_0, \phi_{np})$, displaced along a circular surface having radius a_0 , as

⁹¹ shown in Figure 3.

$$E_{np,tx_m}(a_0,\phi_{np};tx_m;f) = S21_{np,tx_m}(a_0,\phi_{np};tx_m;f)$$
(1)

with $np = 1, ..., N_{PT}$. The device uses M positions of the transmitting antennas, i.e. T_X can be rotated to transmit the signal 92 from the points $tx_m \equiv (a_1, \phi_m)$, with $m = 1, 2, \dots, M$. Also, the device uses number of frequency (NF) samples in the band 93 $B = [f_{min} \div f_{max}]$. The received signals are then processed through HP to calculate the field inside the cylinder; this field is then 94 used to generate an image, which is a homogeneity map of dielectric properties¹⁹. Here, instead of using the received signals to 95 generate images through the HP based algorithm, we employ ML methods on the raw signals to analyze and understand the 96 difference between signals scattered from normal breast and breast with lesion to make decision about breast condition. The 97 experiment was performed using Matlab R2017a tool in an Intel^R CoreTM i7 processor@ 3.60GHz based Windows 7 Enterprise 98 64-bit operating system and it has 7856 MB NVIDIA Graphics Processing Unit (GPU). 99

100 In-vivo acquisition

¹⁰¹ Continuous clinical recruitment of volunteers is underway at Perugia Hospital, Italy. The clinical validation for the first forty-five

volunteers has been approved by the Ethical Committee of Regione Umbria, Italy, (N. 6845/15/AV/DM of 14/10/2015). More
 recently, another partner hospital, Foligno Hospital, also in Italy, has been approved by the Ethical Committee of Regione

¹⁰³ recently, another partner hospital, Foligno Hospital, also in Italy, has been approved by the Ethical Committee of Regione ¹⁰⁴ Umbria, Italy, to join the clinical validation trials. This will extend the number of subjects to one hundred and fifty (N

Umbria, Italy, to join the clinical validation trials. This will extend the number of subjects to one hundred and fifty (N 10352/17/NCAV of 16/03/2017). This trial is a feasibility study of the method shown in Figures 2 and 3 employing microwave

imaging to detect breast lesions, with the intention of gauging the potential of the proposed system for medical screening and

¹⁰⁷ localization of breast lesions. The list of a first pilot set of 18 subjects, who have been recruited under the aforementioned

protocol and used for this study, is presented in Table 1. A previous table with 16 subjects was presented in 28 .



Figure 2. The UBT Microwave 'MammoWave' apparatus.



Figure 3. (a) Pictorial view of the system, where the transmit (T_X) and receive (R_X) antennas are placed inside the hub but external to the cup. (b) T_X (black dot) and R_X (red dot) can be moved around the azimuth, i.e. horizontal plane, on two circumferences having radius a_1 and a_0 , respectively²⁹.

All volunteers provided informed consent with five subjects undergoing the proposed microwave imaging for both breasts. Thirteen subjects underwent the prototype imaging as shown in Figure 3 for a single breast. This research was conducted adhering to the ethical standards of the institutional and/or national research committee incorporating the 1964 Helsinki declaration and its later amendments or analogous ethical standards. The study was performed in harmony with the Code of Ethics of the World Medical Association for experiments involving humans.

A conventional exam and full radiologist study was performed for each subject; echography and/or mammography or 114 (limited to one case) magnetic resonance imaging were the conventional exams performed in these cases. The MyLab 70 xvg 115 Ultrasound Scanner (Esaote, Italy) was the echographic method used; A Selenia LORAD Mammography System (Hologic, 116 Marlborough, USA) was employed for mammography examinations; and a 3T scanner (Siemens Healthcare, Germany) was 117 used for magnetic resonance imaging. The radiologists diagnosis is listed in Table 1 which presents the outcomes from the 118 radiologists report along with the subject's breast condition details. Where available, the breast type has been classified 119 according to density, as defined by the American College of Radiology (ACR) scale ranging from ACR1 (extremely fatty breast) 120 to ACR4 (extremely heterogeneous fibroglandular breast)³⁰. If present, the inclusion type was classified according to defined 121 standards^{31–33}. 122

Following a volunteer's agreement to participate, the clinical study coordinator supports each volunteer to place their breast 123 correctly into the system cup. This cup is integrated into the prototype bed for improved comfort and patient stability. Exam 124 data is processed via a computer interface and is observed by a system operator located in the room. Overall, the exam and data 125 collection phase require approximately five minutes per breast. The transmit and receive antennas (T_X and R_X are positioned 126 on the azimuth plane at the same height which crosses the center of the breast of the subject being examined (after ensuring 127 that the antennas half power beam angle include the breast). M=15 transmitting positions are employed, divided in 5 groups 128 centered at 0° , 72° , 144° , 216° , and 288° on the azimuth plane; each group has 3 transmitting positions displaced from each 129 other by 4.5° . For each transmitting position, four receiving positions, at 90° from each other are employed. The S21 was 130 acquired at NF=1601 frequencies from 1 to 9 GHz in Δf = 5 MHz increments for each T_x and R_x position. The received 131 signals are processed as follows: 132

Subject index and breast (left/ right)	Year of birth	Breast type	Diagnostic test	Output of the radiologist study
01R	1983	ACR4	ecography	Healty
01L	1983	ACR4	ecography	Healty
02R	1936	ACR2	mammography	carcinoma papillary
03R	1960	N/A	magnetic resonance	carcinoma infiltrating grade 2
04R	1987	ACR4	ecography	Healty
04L	1987	ACR4	ecography	Healty
05L	1987	N/A	ecography	benign fibroadenoma
06L	1975	ACR2	ecography + mammography	benign fibroadenoma
07R	1980	ACR3	ecography + mammography	benign microcalcifications
08R	1929	ACR4	ecography + mammography	carcinoma
09R	1963	ACR3	mammography	Healthy
09L	1963	ACR3	mammography	benign fibroadenoma
10L	1964	ACR4	mammography	Healthy
10R	1964	ACR4	mammography	Healthy
11R	1946	ACR2	mammography	Healthy
12R	1966	ACR3	mammography	carcinoma (4 cm), b5
13L	1971	ACR3	mammography	carcinoma
14L	1996	N/A	ecography	benign fibroadenoma
15R	1969	ACR4	mammography	microcalcifications
16R	1948	ACR2	mammography	Healthy
17R	1971	ACR4	mammography	Healthy
17L	1971	ACR4	mammography	Healthy
18R	1983	ACR3	mammography	Healthy

Table 1. Subject lists; details and related radiologist review. Overall shows 12 healthy and 11 non-healthy tissues. Included in the non-healthy is one post-surgical breast with seroma.

1. Let us consider the first transmitting antennas group and the antennas in the group are numbered as tx_1, tx_2, tx_3 ; the first 133 transmitting group is assumed to be centered at $\phi = 0^{\circ}$. For each transmitting antenna of the group, we consider the 134 signals received at $N_{PT} = 4$ points displaced at $\phi = 45^{\circ}, 135^{\circ}, 225^{\circ}, 315^{\circ}$ with respect to the corresponding transmitting 135 antenna. 136

2. To remove skin artefacts, we generate the following signals: 137

$$E_{1-2}(a_0, \phi_{np}; tx_{1-2}; f) = E_{np,tx_m}(a_0, \phi_{np}; tx_1; f) - E_{np,tx_m}(a_0, \phi_{np}; tx_2; f)$$
(2)

$$E_{2-3}(a_0, \phi_{np}; tx_{2-3}; f) = E_{np,tx_m}(a_0, \phi_{np}; tx_2; f) - E_{np,tx_m}(a_0, \phi_{np}; tx_3; f)$$
(3)

where, $\phi_{np} = 45^{\circ}$, 135° , 225° , 315° 138

3. The procedure is repeated for the other four transmitting groups. It follows that, for each microwave exam, we have 40 139 signals in the frequency domain. 140

Supervised Machine Learning 141

The data gathered from the microwave examination are considered for classification purpose and/or to predict future lesion 142 detection instances. This is the first investigation to use microwave clinical data from this apparatus undergoing machine 143 learning classification. Labeled information about the healthy and non-healthy breast pattern have been gathered from the output 144 of the radiologist study. Specifically, a healthy breast is a breast with no lesion, while a non-healthy breast is a breast containing 145 a lesion which may be benign or malignant. The accumulated clinical data have high variance in Euclidean space, so both 146 linear and non-linear classifiers are employed to optimised performance for identifying healthy and non-healthy subjects. There 147 are several ML algorithms present for classification tasks in the literature, some of them being very problem specific while 148 others aim to be more general requiring an investigation approach to be fitted to available data. The selection of appropriate ML 149 methods is quite intuitive and the data distribution in the plane needs to be initially observed. It has been found that the gathered 150

microwave data are non-linearly distributed in the plane. Thus, the leading supervised and non-linear classifiers, KNNs, MLPs, 151 SVMs have been examined, where cross validation techniques, augmented by random sub-sampling methods are employed to 152 asses the performance, through statistical metrics, and discover the most appropriate classification model. Initial results from 153 non-linear classifiers such as, KNNs and MLPs were unsatisfactory. The radial basis function (RBF) could be an option, but it 154 performs well where the data are in loop or spherical shape and circular decision boundary can differentiate the groups. Though, 155 the data are non-linear they are not spherically distributed, hence the SVM has been implemented with a linear kernel function 156 because, although the data distribution appears non-linearly separable in the 2D plane, there is still a possibility to classify 157 most lesion instances accurately by linear decision boundary while the data are being projected into hyperplane i.e., impossible 158 to visualise. The linear kernel of SVM also failed to achieve satisfied performance, and SVM has been experimented with 159 quadratic kernel function which outperformed other classification techniques. 160

161 Cross validation and performance evaluation

A cross validation technique has been used to assess, enhance predictive outcomes, and select models for developed ML 162 prototypes. This has been done by repeated random sub-sampling of the data, which is also known as Monte Carlo cross-163 validation³⁴. The dataset has been randomly partitioned to select the training and validation dataset, where training and 164 validation sets have been used to train and evaluate performance of a selected ML model. The ratio of training and testing data 165 has been specified during each round e.g., training has been started with 10% randomly selected data when rest of the 90% 166 data have been considered as validation/testing data. The amount of training data has been increased by 10% while amount of 167 validation dataset decreased by 10% in each round and this process has been repeated till the model has not overfitted. Each 168 model has been run 25 rounds to select the appropriate ratio of training and testing and found 40% of training and 60% of 169 testing data is necessary to prevent the ML algorithms from overfitting. The results (statistical metrics) have been aggregated 170 and averaged over all the rounds. A number of statistical metrics³⁵, accuracy, true positive rate (TPR) or sensitivity, true 171 negative rate (TNR) or specificity, positive predictive value (PPV), and negative predictive value (NPV) have been used to 172 investigate the classification performance of the classifiers. A receiver operating characteristic (ROC) curve has been generated 173 for each ML model with the validation dataset to illustrate the diagnostic ability and stability of the classification system with 174 different discrimination threshold. Subsequently, Matthews Correlation Coefficient (MCC)³⁶ and Youden's index³⁷ have been 175 implemented to investigate the classification outcomes, where, MCC and Youden's index estimate quality of classification and 176 probability of the informed decision respectively. The outcomes and it's analysis have been described in next section. 177

Results Analysis

According to the radiologist's review, 12 healthy breasts and 11 non-healthy breasts, i.e. breasts with lesions, underwent the

microwave exam of the 18 subjects. As described in the previous section, each microwave exam leads to 40 different patterns in

the frequency domain. As an example, Figure 4 below shows $E_{1-2}(a_0, \phi_{np}; tx_{1-2}; f)$ for $\phi_{np} = 45^o$ for one healthy and one

¹⁸² non-healthy breast.



Figure 4. Example signals of healthy and non-healthy patterns in 45°.

k-nearest neighbor classifier 183

Initially, the investigation began by employing the k-NN classifier³⁸. The classifier is particularly simple, measuring the 184 proximity of features in the hyperspace without any assumption of the underlying data distribution to predict a category, making 185 it flexible for decision making. Two effective distance metrics, Euclidean and Mahalanobis perform well with k-NN, but 186 Mahalanobis distance requires the inversion of covariance matrix which could increase the computational overhead. Therefore, 187 the Euclidean distance is considered here to measure the distance of a feature vector from its nearest neighbor. The k is chosen 188 as odd for this two-class problem that one pattern could not predict under the same class label by the classifier. Table 2 displays 189 the classification outcomes, where k is varied from 1 to 5 and 10%, 20%, 30%, and 40% data are randomly selected for 190 the training phase. The results show that the algorithm exhibited good performance with increasing training data volume as 191 expected. Here, k = 1, produces the optimal result among other NNs with 40% of training data volume. It attained the testing 192 accuracy 0.608 ($\equiv 60.8\%$). TPR or sensitivity measures the ability of the algorithm to identify the non-healthy subjects, which 193 is $0.541 (\equiv 54.1\%)$ in the case of k = 1. It could correctly identify the subjects with lesions with a rate of 0.667 ($\equiv 66.7\%$). 194 PPV and NPV are influenced by the prevalence of having a lesion in the breast that is being tested. In case of k = 1, PPV 195 and NPV the probability that the subjects with positive lesion identification truly have the lesion and negative identification 196 of lesions truly do not have the lesion. The 1NN produces fewer false predictions close to the decision boundary bringing 197 improved accuracy over 3NN and 5NN; also, truly positive prediction for having lesion and vice versa. Additionally, the MCC 198 measurements over prediction results are also not cogent for 1NN, 3NN, and 5NN. The average MCC is approximately 0.206 199 in case of 1NN and decreases towards 0 with the increment of k. This trend states that the addition of random predictions with 200 greater number of NN. The average proportions obtained from Youden's index are also very low, 0.206, 0.130, and 0.086 for 201 1NN, 3NN, and 5NN respectively further indicating the probability to predict those lesions is random and unreliable. This 202 index works along with the ROC curve, the outcomes have been correlated at the discussion of ROC analysis. Therefore, the 203 overall performance of 1NN is better than the other NNs because of data compactness, where one nearest neighbor results in a 204 good prediction if a greater number of neighbors have been chosen, the misclassification increases. 205

NNs	% of Training Data	Accuracy	Sensitivity	Specificity	PPV	NPV	MCC	Youden's Index
1NN -	10	0.555	0.567	0.545	0.521	0.590	0.203	0.202
	20	0.551	0.441	0.650	0.532	0.563	0.225	0.225
	30	0.586	0.580	0.592	0.551	0.620	0.186	0.186
	40	0.608	0.541	0.667	0.587	0.624	0.210	0.209
3NN	10	0.519	0.648	0.405	0.488	0.569	0.143	0.142
	20	0.528	0.448	0.600	0.505	0.544	0.125	0.124
	30	0.559	0.460	0.652	0.553	0.562	0.123	0.122
	40	0.568	0.520	0.609	0.531	0.598	0.134	0.132
5NN -	10	0.532	0.434	0.619	0.499	0.555	0.084	0.082
	20	0.541	0.412	0.656	0.517	0.555	0.088	0.087
	30	0.549	0.577	0.524	0.513	0.588	0.092	0.089
	40	0.550	0.419	0.665	0.522	0.567	0.082	0.081

Table 2. Results obtained from nearest neighbor algorithm.

Multilayer perceptron classifier 206

Two different multilayer perceptron^{39,40} algorithms are studied where, each algorithm is created with one hidden layer and 207 the number of nodes in the hidden layer are decided using a 'rule of thumb' ($\sqrt{(number of inputs + number of outputs)}$ + 208 (a constant between 1 to 10 set by experimentally)). The optimal size of the hidden layer is decided typically between the 209 size of the input and output layers. The bias and weights are initialized randomly, the learning rate $\eta = 0.1$ is varied up to 0.99. 210 The output of the layers is determined by the hyperbolic tangent sigmoid transfer function. The Mean Square Error (MSE) 211

 $=\frac{1}{N}\sum_{i=1}^{N}(t_i-a_i)^2$ is calculated for each output to back-propagate and update the weights, where t and a signify the targets and 212 outputs, respectively. 213

First, the network is trained using the Levenberg-Marquardt (LM) algorithm which adaptively varies the parameter updates 214 and performs better (because of the weight updation using a damping coefficient) than the simple gradient decent method 215 that defines simple first order iterative optimization function and finds the local minimum, local maximum for parameter 216 updating. The training stops when the maximum number (=1000) of epochs is reached, where one set of weight updating using 217 backpropagation is considered as one epoch. Table 3 presents the results for both MLP using Levenberg-Marquardt MLP_{LM}^{41} 218 and Bayesian-Regularization (BR) backpropagation MLP_{BR}^{42} . In the case of MLP_{LM} , the testing accuracy increases for up 219 to 40% training data, but the increment rate is negligible, and reached 0.532 (\equiv 53.2%), but results 0.076 (\equiv 7.6%) sensitivity 220 or TPR indicates the network can only identify 7.6% subjects correctly. However, it shows good performance in recognizing 22

subjects without lesions (TNR=0.936). Also, the probability of the prediction for identification of subjects having or not having 222 lesions is slightly more than 50%. In the case of MLP_{BR} , the overall performance is similar to MLP_{LM} . The maximum testing 223 accuracy reached 0.538 (\equiv 53.8%) when 40% training data is used but results only 0.038 TPR demonstrates the inability to 224 make predictions about lesions whereas 0.951 specificity or TNR shows a strong performance in predicting the absence of a 225 lesion. Therefore, neither MLPs could predict the healthy breast pattern, but did make acceptable predictions for subjects with 226 lesions. The probability of the prediction for identification of subject with or without lesions is between 0.511 to 0.542 for both 227 MLP_{BR} and MLP_{LM}. Additionally, the estimation of MCC and Youden's statistic state insignificant power of MLPs to identify 228 breast lesions. MCC of MLP_{LM} and MLP_{BR} are 0.019 and 0.082 respectively, implies the performance of MLPs are no better 229 than random prediction with a large, unacceptable, misclassification rates. Subsequently, Youden's statistics of MLP_{LM} and 230 MLP_{BR} are 0.018 and 0.082 respectively. The zero tendency of the indices show the high proportion of false positives and false 231 negatives. Misidentifications have been found here because the error surfaces are very complex for both of these networks and 232 have stagnant into several local minima, producing unexpected outcomes for healthy and non-healthy patient identification. 233

MLPs	% of Training Data	Accuracy	Sensitivity	Specificity	PPV	NPV	MCC	Youden's Index
MLP _{LM}	10	0.498	0.111	0.847	0.394	0.514	0.020	0.019
	20	0.530	0.052	0.962	0.551	0.529	0.010	0.009
	30	0.531	0.190	0.825	0.482	0.542	0.016	0.015
	40	0.532	0.076	0.936	0.511	0.534	0.031	0.030
MLP _{BR}	10	0.532	0.035	0.953	0.428	0.532	0.081	0.081
	20	0.533	0.032	0.934	0.462	0.513	0.088	0.088
	30	0.538	0.037	0.957	0.414	0.527	0.082	0.082
	40	0.538	0.038	0.951	0.425	0.538	0.078	0.078

Table 3. Results obtained from multilayer perceptron algorithm.

234 Support vector machine classifier

Subsequently, the SVM is investigated with two different kernel functions to acquire the hyperplane that can separate healthy and non-healthy subjects. Table 4 shows the results for classification of the 2 subject types where, SVM_L and SVM_Q represents the SVMs using the linear and quadratic kernel functions^{43,44} for prediction. SVM_L uses the optimization method, $c = \sum w_i k(s_i, x) + b$ where, subject pattern vector x is targeted to classify, s_i is the support vector, w_i is weight, and b is the

bias. Here, the linear kernel function is k. The vector x is considered a member of the lesion free group when, $c \ge 0$ or lesion 239 group otherwise. This creates a hyperplane that achieved better accuracy than the other classifiers used above. SVM_L is trained 240 using 10% to 40% data and associated testing results are shown in the table. It produces the highest testing accuracy with 40% 241 training data which is 0.620 (=62.0%). It achieved TNR of 0.998 (=99.8%) in that case, which indicates a good performance 242 to identify the subjects with no lesions, but TPR (maximum $0.193 \equiv 19.3\%$ among all cases of SVM_L) shows a very weak 243 performance in identifying subjects with lesions. Though the probability in identifying subjects who truly have lesions is better 244 than the subjects who truly do not have lesions. The number of false negatives are continuously high, but false positives are low, 245 which resulting an average MCC 0.319 for SVM_L . Though, MCC is better than the other algorithms, it is still not powerful 246 enough to reduces false negatives. The average Youden's index is 0.180 which is close to the Youden's index obtained from 247

²⁴⁸ 1NN beacuse, SVM_L produced more false negatives and fewer false positives, whereas 1NN resulted in fewer false negatives and more false positives, thus the total number false predictions are high in both the cases.

 Table 4. Results obtained from SVM using different kernel.

SVMs	% of Training Data	Accuracy	Sensitivity	Specificity	PPV	NPV	MCC	Youden's Index
SVM _L	10	0.620	0.191	0.997	0.981	0.584	0.319	0.182
	20	0.619	0.184	0.998	0.985	0.584	0.318	0.178
	30	0.616	0.194	0.996	0.977	0.579	.324	0.180
	40	0.620	0.171	0.998	0.989	0.589	0.318	0.181
SVMQ	10	0.985	0.969	0.996	0.985	0.973	0.959	0.956
	20	0.984	0.967	0.997	0.983	0.972	0.963	0.960
	30	0.984	0.965	0.996	0.985	0.970	0.963	0.959
	40	0.989	0.977	0.997	0.985	0.981	0.955	0.951

Subsequently, SVM_Q have been employed to obtain an improved testing accuracy to differentiate subjects by minimising the gap between the two groups. The considered quadratic function is $\min_x \frac{1}{2}x^T Hx + c^T x$, where $Ax \le b$, c is a real valued vector, H is real symmetric matrix, A is real matrix, b is a real vector, and the notation $Ax \le b$ means that every entry of the vector A_x is less than or equal to the corresponding entry of the vector b. The quadratic programming aims to find the vector x which could minimize that function. This function creates the best hyperplane to classify the subjects here. SVM_Q achieved 0.989 (\equiv 98.9%)

testing accuracy to identify the lesion affected and unaffected subjects. Correspondingly, TPR (is $0.9770 \equiv 97.70\%$) and TNR

(is $0.997 \equiv 99.7\%$) both are high in this case, which indicates a good implementation of the hyperplane for separation which

²⁵⁷ could correctly identify those subjects with and without lesions. Also, the high probabilities (PPV and NPV) support the results.

²⁵⁸ In addition, MCC and Youden's index both are high (i.e., 0.960 and 0.956 respectively) in this case. Figure 5 illustrates the ²⁵⁹ outcomes more clearly, where no false positives, and few false negatives have been found in each run. This greatly influences

outcomes more clearly, where no false positives, and few false negatives have been found in each run. This greatly the score of MCC and Youden's index and proves the strong ability of the SVM_Q model to identify breast lesions.



Figure 5. Confusion Matrices of SVM_Q : (a) 10% training data, (b) 20% training data, (c) 30% training data, and (d) 40% training data are used.

Figure 5 shows the outcomes of SVM_O more closely from the confusion matrices. The numeric values listed in the confusion 261 matrix with a blue background demonstrates the correct classification of lesion affected and unaffected patterns. Very few 262 misclassification occurred here (between 1.1% to 1.5%). Without lesion and with lesions are denoted by class-1 and class-2, 263 respectively. It is shown that all the normal tissue subjects are classified correctly, few misclassifications are found with the 264 training data variation (10% to 40%) in each case of SVM_Q . The most important part of this lesion classification is to reduce 265 the negative predictions (including false positive and false negative). It is found from the confusion matrices that the false 266 prediction rate of lesion detection is zero in each case (all the patterns of class-2 are being predicted as class-2). False positive 267 rate (FPR) is zero (from Figure 5a to 5d) for all the cases of SVM_{Q} , which implies all the non-lesion breast patterns are correctly 268 classified but, few false negative rates (FNR) occurred, 0.027 (2.7% for 10% training data), 0.028 (2.8% for 20% training data), 269 0.029 (2.9% for 30% training data), and 0.019 (1.9% for 40% training data). Results here are far exceed other state-of-art 270 methods reported to miss 15% of lesions. The effect of this classification and misclassification has been discussed earlier. 271



Figure 6. (a) Actual data distribution in two-dimensional plane, (b) decision boundary produced by 1NN classifier, (c) decision boundary produced by SVM with quadratic kernel.

As reported, SVM_Q has achieved the best performance among the classifiers investigated here in terms of accuracy, sensitivity, and specificity. It's important here to visualize the data with corresponding hyperplanes formed by the ML algorithms. Figure 6 presents the data distribution along with the two optimal decision boundaries produced by 1NN and SVM_Q . Figure 6a represents the breast with lesion and healthy breast data distribution in a two-dimensional feature space for visualization of the studied data pattern for the classification purpose. All the healthy breast patterns scatter the microwaves in a particular way whereas a breast lesion may occur in any position of the breast, which produces different scattering effect for the breasts with lesion. Hence, it has been found healthy data formed the cluster in the center and lesion data scattered around that group. Thus, these two groups of data could only be handled by the parabolic or quadratic curve, which has been made by SVM_Q here (decision boundary of Figure 6c). In addition, Figure 6b shows the decision boundary to correlate the misidentifications obtained by 1NN algorithm, which also have been illustrated in Table 4.

Finally, the obtained classification results are compared to conclude the investigation. Figure 7 shows the visual comparison of average classification accuracy, sensitivity, specificity, MCC, and Youden's index to make the contrast over performance, where *x* and *y*-axis represent different classifiers and accuracy, sensitivity, specificity, MCC, and Youden's index respectively. It can be seen, the performance of SVM_Q is better than other classifiers attempted here in terms of average accuracy (98.55%), sensitivity (96.95%), specificity (99.65%), MCC (96%), and Youden's statistic (95.6%) which illustrates robust ability to detect breast lesions from new microwave data.



Figure 7. Comparison of performance metrics for all classifiers, (a) average accuracy, (b) average sensitivity, (c) average specificity, (d) average MCC, (e) Youden's index.

The ROC curve has also been plotted and shown in Figure 8 to compare and analyse the diagnostic ability of all three 288 classifiers, where the number of nearest neighbour, learning rate, and threshold for detection have been varied for NNs, MLPs, 289 and SVMs respectively. The area under curve (AUC) has also been determined for each classifier. The x and y-axes of 290 Figures 8a, 8b, 8c represent false positive rate (FPR) or (1-specificity) and true positive rate (TPR) or sensitivity respectively. 291 Though, the accuracy of 1NN is better than other classifiers, except SVM_L and SVM_O , the AUC of overall KNN (Figure 8a) is 292 only 0.599 indicating the large presence of false predictions. In the case of MLP_{BR} and MLP_{LM}, AUCs are only 0.389 and 0.446 293 respectively. Both the MLPs produce vast amount of false predictions, as discussed earlier, and generate low AUC, and the 294 tendency of performance is highly random in terms of all performance metrics. Though, the accuracy of SVM_L is approximately 295 0.619, it made a large number of false predictions and produced an AUC of 0.228 when the threshold had been varied. The 296 highest AUC ($\equiv 0.937$) is created by SVM_O as this delivers the lowest number of false predictions among all tested and scored 297 the highest performance metric for all the cases. 298

The parametric (i.e., MLP, and SVM) and non-parametric (i.e., KNN) both types of learning techniques have been used here to obtain optimal performance on the currently available dataset. The work has two main limitations, high dimensional feature space and availability of data (i.e., still ongoing). The dimension of the feature space has not been reduced in this study and considered as future scope. The KNN and SVM make the decision based on the similarity measure, whereas MLP depends upon features. The non-parametric KNN does not require any assumption of feature distribution to check similarity, but it requires a large amount of uncorrelated and independent training data in order to make good predictions, whereas the data used in this



Figure 8. ROC curve analysis of the classifiers, (a) KNN, (b) MLP using Levenberg-Marquardt and Bayesian-Regularization backpropagation functions, (c) SVM using linear and quadratic kernels.

study are highly correlated and high dimensional in nature. Thus, the KNN has overfitted with 40% of training data, the overall 305 performance is unsatisfactory and also deteriorated with the increment of k. Both the MLPs MLP_{BR} and MLP_{IM} are parametric 306 in nature and make assumptions of feature space to minimise cost function and get optimised weights. Though, the function 307 LM which directs *MLP_{LM}* is well known for optimising cost function but, choice of damping parameter played vital role for the 308 study and the model stuck in local minima within 50 epochs which prevents the model to optimise weights and create good 309 decision boundary. Thus, the damping parameter needs further tune to obtain good results. The Bayesian-Regularization (BR) 310 is a well known optimisation technique that works well with MLP even if the data are high dimensional. But, the possible 311 reason for incorrect predictions of MLP_{BR} is miss-specification of the model which indicates the function model does not suit 312 BR for this problem. The SVM has been used by two different kernel functions, linear (SVM_L) and quadratic (SVM_O) . The 313 methods rely on similarity, unlike the KNN model, SVMs is sensitive to the curse of dimensionality problem while the the 314 features are not engineered to uncorrelated values. SVM_L is well known for its ability to separate non-linear data linearly in the 315 higher feature space. Here, the dot product weight and features with the conventional bias have been employed to create a 316 linear hyperplane and maximise the gap between support vectors and samples. Also, the estimation of bias is trivial in this case, 317 thus, the maximisation of the linear kernel function created hard margins and increased errors as a result. On the other hand, 318 SVM_Q is an extended version (2nd order polynomial) of SVM_L which creates a soft margin in the feature space. The SVM_Q is 319 focused on the minimisation problem. The kernel has two other variables, c and x which denote penalty constraint and the slack 320 variable respectively. This is the advantage found using SVM_O , where x minimise error and c minimise the gap at the same time 321 so that the non-linear boundary has been formed for one group (healthy or non-healthy) and rest of the samples fall in the other 322 side of the boundary. 323

324 Discussion

The frequency domain scattering parameters of subject breasts are obtained using the UWB microwave mammogram apparatus 325 described above in an ongoing clinical trial. The same subject breasts included in this study have also undergone radiologist 326 scrutiny obtained using conventional imaging methods (echography and/or mammography or (limited to one case) magnetic 327 resonance imaging), which has been used as labeled information. The microwave mammogram apparatus clinical data are 328 pre-processed and transformed for machine learning approaches. Various algorithms are trained and tested to differentiate 329 lesion-containing and lesion-free breast tissues. Here, breasts with lesions may be benign or malignant. The experimental 330 results show that the quadratic kernel of SVM has successfully created the hyperplane and maximizes the margins between the 331 support vectors, resulting in a sensitivity for breast lesion classification equal to 97%. Such value outperforms the sensitivity 332 given in 16 and 17 , which are 74% and 90% respectively, where machine learning is not employed. The successful employment of 333 machine learning on clinical data obtained using a microwave mammogram could help the radiologist in the diagnosis process. 334 The integrated system with microwave non-ionizing imaging augmented by machine learning algorithms can be a step change 335 in mass breast screening deployment. The system could be deployed across all female age groups, and during pregnancies, in 336 more local settings, increasing the detection and hence survival rates of breast cancer sufferers. 337

This study aimed to differentiate between breast with or without lesions, but the type of lesion cannot yet be identified at this stage. The authors are currently gathering more clinical data to understand the category and property of lesions through the MammoWave device. Once more data have been gathered to make generalized decisions about lesions, this work will

be extended further to identify the type of lesions automatically using ML. Although, the SVM_O has worked very well in 341 terms of all statistical performance metrics, the study is limited by some factors and those are considered for future work. The 342 data used here have a high dimension and values are correlates, which placed the experimented ML methods in the curse 343 of dimensionality problem. Thus, suitable dimensionality reduction techniques will be investigated in the next stage. The 344 analysis of ROC curve shows that performance improvement for all experimented ML algorithms are possible. This study is 345 an empirical study on ML application of automatic lesion detection to investigate suitable classifiers to categorise the data in 346 hyperspace. The performance analysis directs focus on hyperplanes created by a quadratic function, thus the fine tuning of 347 the parameters such as, slack variable and penalty parameter would be observed subsequently. Also, the parameter bias of 348 other algorithms would be taken into account since the performance of current prototype may vary when the type of lesion will 349 be identified with new datasets. Expert clinical input will be ensured in further research to meet clinical expectations in the 350 assistance of breast lesion identification and classification. In addition, deep learning approaches will be investigated to provide 351 higher sensitivity and specificity towards automation. 352

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Author contributions statement

G.T., L.S., A.V., and G.R. have designed and manufactured the UWB microwave non-ionising apparatus with associated signal processing techniques comprising MammoWave. Subjects have been recruited and screened through MammoWave. M.D. has conducted the conventional radiological investigation on the same subjects and confirmed the outcomes of UWB MammoWave experiment. S.P.R. and M.D. have performed the machine learning algorithms and analysed the prediction outcomes for automatic breast lesion detection through clinical UWB MammoWave. S.D. and M.G. have supervised the work. S.D. managed the experiments performed along with co-authors at LSBU and instigated the collaborative work on this paper between teams at Perugia and LSBU. All authors reviewed the manuscript.

441 Additional information

Lorenzo Sani, Alessandro Vispa and Giovanni Raspa are employed by UBT Srl, Italy. Gianluigi Tiberi and Lorenzo Sani are shareholders of UBT Srl, Italy.