## Sistema de Predicción

 Epileptogenica en Lazo Cerrado Basado en Matrices Sub-Durales
## James Brian Romaine

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Director, Tutor: Manuel Delgado Restituto<br>Director: Ángel Rodríguez Vázquez

Departamento de Electrónicaly
Electromagnetismo
Universidad de Sevilla
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I would like to dedicate this thesis to my family, friends and co-workers ...

## Declaration

I hereby declare that except where specific reference is made to the work of others, the contents of this dissertation are original and have not been submitted in whole or in part for consideration for any other degree or qualification in this, or any other university. This dissertation is my own work and contains nothing which is the outcome of work done in collaboration with others, except as specified in the text and Acknowledgements.

James Brian Romaine

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#### Abstract

The human brain is the most complex organ in the human body, which consists of approximately 100 billion neurons. These cells effortlessly communicate over multiple hemispheres to deliver our everyday sensorimotor and cognitive abilities.

Although the underlying principles of neuronal communication are not well understood, there is evidence to suggest precise synchronisation and/or de-synchronisation of neuronal clusters could play an important role. Furthermore, new evidence suggests that these patterns of synchronisation could be used as an identifier for the detection of a variety of neurological disorders including, Alzheimers (AD), Schizophrenia (SZ) and Epilepsy (EP), where neural degradation or hyper synchronous networks have been detected.

Over the years many different techniques have been proposed for the detection of synchronisation patterns, in the form of spectral analysis, transform approaches and statistical based studies. Nonetheless, most are confined to software based implementations as opposed to hardware realisations due to their complexity. Furthermore, the few hardware implementations which do exist, suffer from a lack of scalability, in terms of brain area coverage, throughput and power consumption.

Here we introduce the design and implementation of a hardware efficient algorithm, named Delay Difference Analysis (DDA), for the identification of patient specific synchronisation patterns. The design is remarkably hardware friendly when compared with other algorithms. In fact, we can reduce hardware requirements by as much as $80 \%$ and power consumption as much as $90 \%$, when compared with the most common techniques. In terms of absolute sensitivity the DDA produces an average sensitivity of more than $80 \%$ for a false positive rate of $0.75 \mathrm{FP} / \mathrm{h}$ and indeed up to a maximum of $90 \%$ for confidence levels of $95 \%$.


This thesis presents two integer-based digital processors for the calculation of phase synchronisation between neural signals. It is based on the measurement of time periods between two consecutive minima. The simplicity of the approach allows for the use of elementary digital blocks, such as registers, counters or adders. In fact, the first introduced processor was fabricated in a $0.18 \mu \mathrm{~m}$ CMOS process and only occupies $0.05 \mathrm{~mm}^{2}$ and consumes 15 nW from a 0.5 V supply voltage at a signal input rate of $1024 \mathrm{~S} / \mathrm{s}$. These low-area and low-power features make the proposed circuit a valuable computing element in closed-loop neural prosthesis for the treatment of neural disorders, such as epilepsy, or for measuring functional connectivity maps between different recording sites in the brain.

A second VLSI implementation was designed and integrated as a mass integrated 16 -channel design. Incorporated into the design were 16 individual synchronisation processors ( 15 on-line processors and 1 test processor) each with a dedicated training and calculation module, used to build a specialised epileptic detection system based on patient specific synchrony thresholds. Each of the main processors are capable of calculating the phase synchrony between 9 independent electroencephalography (EEG) signals over 8 epochs of time totalling 120 EEG combinations. Remarkably, the entire circuit occupies a total area of only $3.64 \mathrm{~mm}^{2}$.

This design was implemented with a multi-purpose focus in mind. Firstly, as a clinical aid to help physicians detect pathological brain states, where the small area would allow the patient to wear the device for home trials. Moreover, the small power consumption would allow to run from standard batteries for long periods. The trials could produce important patient specific information which could be processed using mathematical tools such as graph theory. Secondly, the design was focused towards the use as an in-vivo device to detect phase synchrony in real time for patients who suffer with such neurological disorders as EP, which need constant monitoring and feedback. In future developments this synchronisation device would make an good contribution to a full system on chip device for detection and stimulation.

El cerebro humano es el órgano más complejo del cuerpo humano, que consta de aproximadamente 100 mil millones de neuronas. Estas células se comunican sin esfuerzo a través de ambos hemisferios para favorecer nuestras habilidades sensoriales y cognitivas diarias.

Si bien los principios subyacentes de la comunicación neuronal no se comprenden bien, existen pruebas que sugieren que la sincronización precisa y/o la desincronización de los grupos neuronales podrían desempeñar un papel importante. Además, nuevas evidencias sugieren que estos patrones de sincronización podrían usarse como un identificador para la detección de una gran variedad de trastornos neurológicos incluyendo la enfermedad de Alzheimer(AD), la esquizofrenia(SZ) y la epilepsia(EP), donde se ha detectado la degradación neural o las redes hiper sincrónicas.

A lo largo de los años, se han propuesto muchas técnicas diferentes para la detección de patrones de sincronización en forma de análisis espectral, enfoques de transformación y análisis estadísticos. No obstante, la mayoría se limita a implementaciones basadas en software en lugar de realizaciones de hardware debido a su complejidad. Además, las pocas implementaciones de hardware que existen, sufren una falta de escalabilidad, en términos de cobertura del área del cerebro, rendimiento y consumo de energía.

Aquí presentamos el diseño y la implementación de un algoritmo eficiente de hardware llamado "Delay Difference Aproximation" (DDA) para la identificación de patrones de sincronización específicos del paciente. El diseño es notablemente compatible con el hardware en comparación con otros algoritmos. De hecho, podemos reducir los requisitos de hardware hasta en un $80 \%$ y el consumo de energía hasta en un $90 \%$, en comparación con las técnicas más comunes. En términos de sensibilidad absoluta, la DDA produce una sensibilidad promedio de más del $80 \%$ para una tasa de falsos positivos de $0,75 \mathrm{PF} / \mathrm{hr}$ y hasta un máximo del $90 \%$ para niveles de confianza del $95 \%$.

Esta tesis presenta dos procesadores digitales para el cálculo de la sincronización de fase entre señales neuronales. Se basa en la medición de los períodos de tiempo entre dos mínimos consecutivos. La simplicidad del enfoque permite el uso de bloques digitales elementales, como registros, contadores o sumadores. De hecho, el primer procesador introducido se fabricó en un proceso CMOS de $0.18 \mu \mathrm{~m}$ y solo ocupa $0.05 \mathrm{~mm}^{2}$ y consume 15 nW de un voltaje de suministro de 0.5 V a una tasa de entrada de señal de $1024 \mathrm{~S} / \mathrm{s}$.

Estas características de baja área y baja potencia hacen que el procesador propuesto sea un valioso elemento informático en prótesis neurales de circuito cerrado para el tratamiento de trastornos neuronales, como la epilepsia, o para medir mapas de conectividad funcional entre diferentes sitios de registro en el cerebro.

Además, se diseñó una segunda implementación VLSI que se integró como un diseño de 16 canales integrado en masa. Se incorporaron al diseño 16 procesadores de sincronización individuales ( 15 procesadores en línea y 1 procesador de prueba), cada uno con un módulo de entrenamiento y cálculo dedicado, utilizado para construir un sistema de detección epiléptico especializado basado en umbrales de sincronía específicos del paciente. Cada uno de los procesadores principales es capaz de calcular la sincronización de fase entre 9 señales de electroencefalografía (EEG) independientes en 8 épocas de tiempo que totalizan 120 combinaciones de EEG. Cabe destacar que todo el circuito ocupa un área total de solo $3.64 \mathrm{~mm}^{2}$.

Este diseño fue implementado teniendo en mente varios propósitos. En primer lugar, como ayuda clínica para ayudar a los médicos a detectar estados cerebrales patológicos, donde el área pequeña permitiría al paciente usar el dispositivo para las pruebas caseras. Además, el pequeño consumo de energía permitiría una carga cero del dispositivo, lo que le permitiría funcionar con baterías estándar durante largos períodos. Los ensayos podrían producir información importante específica para el paciente que podría procesarse utilizando herramientas matemáticas como la teoría de grafos. En segundo lugar, el diseño se centró en el uso como un dispositivo in-vivo para detectar la sincronización de fase en tiempo real para pacientes que sufren trastornos neurológicos como el EP, que necesitan supervisión y retroalimentación constantes. En desarrollos futuros, este dispositivo de sincronización sería una buena base para desarrollar un sistema completo de un dispositivo chip para detección de trastornos neurológicos.

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## Preface

This thesis was written to give a broad overview of the work conducted during the doctoral scholarship over a period of approximately 5 years. The main goal during the life of the project was the design and implementation of low powered and lower resource consuming VLSI hardware, for the efficient and reliable detection of synchronisation between neural assemblies.

The work was conducted in several key stages:
Firstly, through the research of state of the art in the field of neurological disorders and synchronisation, we gathered a thorough understanding of the current limitations and design challenges faced in this field of study. Using this information, we then targeted the design of a new mathematical algorithm, which focused on solving the most commonly faced problems. Furthermore, to test the algorithmic design a MATLAB implementation was introduced which was compared against the state of the art in terms of comparable features and accuracy. At this point, important aspects are tested such as the signal-to-noise ratio, algorithmic sensitivity, sliding window size and sampling rate distribution to name a few.

To follow, the algorithm was implemented into a field programmable gate array (FPGA) using a hardware description language (VHDL), which allowed us to verify the algorithm running at the logic gate level. This also provided us with prototype metrics which could then be used to validate the scalability of the device compared to the state of the art.

The FPGA implementation of the design was later mapped into CADENCE as a register technology level (RTL) circuit. This design, operating at 1.2 V , gave us a good estimation as to the real life functionality of the circuit and algorithmic design. Once the 1.2 V design was verified at the RTL level in CADENCE, a 0.5 V sub-threshold biased design was implemented using custom layout techniques. Afterwards, the ASIC design was tested in the laboratory using a mixture of test apparatus such as a logic analyser for basic variable verification and micro-controllers for longer in-depth neural signal simulations.

Later, a 16-channel mass VLSI implementation was integrated. This design incorporated 15 main synchronisation processors based on the previously integrated 2-channel processor. In order to integrate this design a similar method to that of the previous design was adopted. This included the FPGA implementation and verification before a CADENCE based custom layout and verification.

NOTE: Due to a change in the MPW policy of the selected foundry, $A M S A G$, regarding its $0.18 \mu \mathrm{~m}$ CMOS process (MPWs were finally cancelled in 2018), the 16channel VLSI DDA processor was received 13 months after the tape-out. The limited time that was available for the completion of the thesis meant that this design could not be tested in the laboratory. Nevertheless, FPGA simulations have been incorporated into the thesis as a verification of functionality.

## Organisation

This thesis has been separated into five chapters.
Chapter 1 describes the most relevant principles needed for the rest of the Thesis. Starting with a brief overview of the anatomy of the brain at the system level ("the larger brain"), including its distinct regions and basic functions, we later go on to describe the anatomy of the brain at the cell level ("the smaller brain") and the electrical signals, such as action potentials (APs) and local field potentials (LFPs), which are involved.

Moving forward, we introduce the concept of phase and synchronisation in both stationary signals and neural signals. This includes the introduction of the most common methods of detection and how synchronisation is being treated as one of the most fundamental underlying principles for the encoding and transfer of information between neuronal clusters.

Afterwards, we give a small overview of some of the most common neurological disorders which suggests that synchronisation could be used as a tool for the detection of pathological states.

Finally, we introduce the most recent advances in hardware implementations for synchronisation detection algorithms.

Chapter 2 presents the proposed Delay Difference Analysis (DDA) algorithm for phase synchronisation computation. The chapter discusses the mathematical premises behind the algorithm and illustrates its functionality in real world scenarios. It also shows how parameters such as quantisation, sample distribution or window evaluation length, affect synchrony estimations.

Next the algorithm is verified in the Matlab environment using neural recordings from 10 epilepsy patients. These recordings sum in total over 1800 hours of neural data
and contain over 60 annotated seizures. The noise tolerance and sensitivity performance of the DDA algorithm is evaluated and compared against more conventional techniques to give a true impression of the algorithms capabilities.

Chapter 3 introduce the design of a VLSI phase synchronisation processor based on the algorithm described in chapter 2 . The chapter firstly gives a broad overview of the design including its strengths and weaknesses. Next, the steps followed towards the implementation of the VLSI design are presented. They included the design in an FPGA, followed by the synthesis with an RTL compiler and finally the custom layout in the CADENCE environment.

Then, the experimental results from the prototype are introduced. After describing the laboratory test setup, a breakdown of the design's power consumption is presented. Then, several measurements using neural recording data from the mentioned epilepsy dataset are presented. They include functional connectivity and graph theoretical results.

Chapter 4 includes the design and implementation of a multi-channel phase synchronisation processor based on the initial design in chapter 3. This section is laid out similar to the previous section in that firstly, all of the individual digital blocks and digital flow functionality is introduced. This is accompanied by many illustrations of the digital blocks as well an illustration of the overall flow and the implemented ASIC micro-photograph.

Next, a FPGA implementation of the VLSI circuit is introduced and system simulations are presented.

Finally, Chapter 5 provides some final concluding comments and draw possible future work which will be conducted using the designed algorithm and VLSI implementations.

## Chapter 1

## Introduction

### 1.1 The larger brain

The human brain weighs approximately 1.5 kg and accounts for only $2 \%$ the total weight of the average human. Nevertheless, it is the most diverse and complex organism known in the universe today. The brain is responsible for everything that we do in our everyday lives from basic motor functions such as, walking, eating or talking to sensory functions such as seeing, listening and touch. It is also responsible for our underlying cognitive abilities in the form of thinking, memories, attention, logical processing and reasoning. It also gives rise to consciousness, which is the state of being aware of one's surroundings and the ability to comprehend them. The brain also has some impressive attributes. It has been theorised that the brain has a storage capacity of upwards of a quadrillion bytes and can perform upwards of 10 quadrillion calculations per second. This complex organ has been extensively studied over the past centuries with new knowledge and understanding being discovered every day.

The larger brain is made up of the cerebrum, cerebellum and brain stem. The cerebrum itself is made up of two hemispheres, the left and right which make up the cerebral cortex. Although it is the largest and most distinguishable part of the brain it only consists of 16 billion of the estimated 100 billion total neurons.

The cerebral cortex can be further broken down into four main lobes, namely, the frontal, parietal, temporal and occipital lobes.

The frontal lobe is the largest of the four main lobes and maintains connections to almost all other parts of the brain. Its main responsibilities include personality and decision making, as well as motor control. This lobe makes sense of the environment around us as well as making sense of memories and emotions. It also provides us with working memory which allows us to hold relative information for short periods in order to drive the attention span.

The parietal lobe interprets our sense of touch (somatosensation) and monitors the position of the body as well as the relative position of the limbs. It integrates information from senses in order to focus our attention on important tasks. It also receives information from the occipital lobe in terms of location, size and speed of objects and incorporates them into the sense of touch in order to interoperate our surroundings.

The temporal lobe is where memories, emotions and language comprehension are stored. It is also key to the recognition of objects, places and people.

| Frontal | Parietal | Temporal |
| :--- | :--- | :--- |
| Regulation of personality | Interoperates language and words | Understanding of Language |
| Behaviour and emotions | Touch and pain | Long term Memory |
| Judgement | vision | Hearing |
| Planning and problem solving | Hearing | Sequence and organisation |
| Speech | motor | Facial recognition |
| Writing | sensory | Emotions |
| Smell | memory | Emotions |
| Intelligence |  |  |
| Concentration |  |  |
| Self awareness |  |  |
| Emotional reactions |  |  |

Table 1.1 Table showing the basic control functions of the frontal, parietal and temporal lobes [1]

The occipital lobe is located at the far back of the cerebral cortex. It decodes information arriving from the retina. It mainly informs us of where, how and what we are seeing, via the detection of high contrast edges and their orientation and motion. This information is then passed to the parietal lobe for response mechanisms or to the temporal lobe to see if we recognise the object.

Fig.1.1 shows the relative positions and surface coverage of the four main lobes.[1], and Table 1.1 summarizes some of the basic functions for the frontal, parietal and temporal lobes.

The cerebellum is tucked underneath the occipital lobe and is actually small compared to the four main lobes. Nevertheless, the cerebellum contains approximately 70 billion neurons. This part of the brain is responsible for our talents from playing musical instruments to athletic agility. It does this by controlling complex movements, it detects errors and creates adjustments to compensate, which in turn strengthens neural circuits throughout the brain.


Fig. 1.1 Overview of the human brain including its four major regions of the cerebrum [1]

### 1.2 Connectivity and the smaller brain

### 1.2.1 Neurons

Neurons are the individual cells which make up the central nervous system. There exist many different types of neurons all of which are packed into small networks of upwards of 10000 neurons per network and are interconnected by kilometres of wiring per cubic millimetre. These are called individual neural circuits. Their main purpose is the transfer of information, which allows for the specific and complex movements, associated with human motor skills as well as allowing for cognitive perception and memory [2].

The basic neuron structure can be seen in Fig. 1.2. Consisting of three main parts. Firstly, the dendrites, which are the main collectors of information (they are analogous, to that of an input to a system).

The soma is the neuronal structure which is responsible for the central processing of the incoming information (similar to that of a systems function $f(x)$ ). The soma performs a non-linear threshold based comparison of the incoming information from the dendrites.

The axon, which is the final main component of the neuronal structure, is considered the main delivery system of information. This sends the soma generated information to other neurons within the network. At the end of each axon, there are axon terminals which connect to dendrites via synapses. In addition, there is a layer of fat which surrounds the axon known as the myelin sheath, which is an electrically insulating layer. The sheath regulates the proper transmission of electrical signals, helping speed up electrical transmission down the axon.

The transmitted information is referred to as an action potential (AP). The AP is a product of concentration gradients, which refers to the difference in ion concentrations inside and outside of the neuronal cell.

In general an AP is generated as follows. Firstly, neuronal cells are surrounded by an extracellular fluid (EF) which is full of positively charged sodium and potassium ions. While the inside of the neuronal cell there are also positively charged sodium and potassium ions. Nevertheless, the EF has many more positively charged ions than the inside of the neuronal cell. This leads to a high concentration gradient which causes a negative potential inside of the cell, known as a resting membrane potential (RMP).

The RMP is the state in which neurons spend most of their time, it is a negative concentration gradient of approximately -70 millivolts.

The membrane of the neuronal cell is very permeable to potassium ions, meaning that they leak out of the cell towards the EF via leakage channels. The membrane of the neuronal cell is also partially permeable to sodium ions which also flow out of the cell via sodium leakage channels. This creates instability within the cell. Nevertheless, a cell is constantly trying to to maintain its resting potential so it has tiny ion pumps which pump potassium back into the cell and sodium out.

In addition to the ion leakage channels and pumps, the neuronal cell also has two voltage controlled ion gates, one for sodium and the other for potassium. during RMP, these gates are always closed. When an event occurs at the dendrites of the cell, such as an AP sent from another neuron or a nerve input it causes the voltage-gated sodium channels to open, allowing sodium ions to flow into the cell which in turn causes a depolarisation in the current which tries to push the resting membrane potential towards 0 millivolts. If the membrane potential reaches a critical threshold, roughly speaking the threshold of approximately -55 millivolts an AP is formed. The AP itself is a positive electrical impulse which can push the membrane potential to +30 mV . Potassium channels then open and the sodium channels close in order to repolarise the cell. The basic overview of the AP can be seen in Fig. 1.2, which marks the opening and closing times of each voltage controlled gate. The potassium gate, however, stays open slightly too long creating a hyperpolarisation after the AP which then slowly moves back towards the resting potential $[3,4]$.

The interconnection between two neurons occurs at the synapse, which is an electro or chemical junction. The human brain contains anywhere between 100 and 500 trillion synapses of different varieties. Synapses are located at the dendrites (input terminals) and the axon terminals (output terminals).

In a chemical synapse, once the pre-synaptic (output terminal) AP or nerve impulse reaches the junction, a neurotransmitter chemical molecule is transmitted and diffused across a small space known as the synaptic cleft. These molecules then bind with neurotransmitter receptors on the postsynaptic (input terminal) neuron which opens or closes ion channels in the receiving neuron. This leads to a change in the membrane potential of the receiving neuron which can either lead to an AP or not. If the cell does fire it is what is known as an excitatory synapse, otherwise it is an inhibitory synapse. Since a neuronal cell has multiple synapse connections the firing of an AP is actually the combination or summation of all of the excitatory and inhibitory activity
at the input of the cell. If there are more excitatory signals, the membrane potential increase towards the AP threshold. For the signal to end, the synaptic cleft must then be cleaned of neurotransmitter.

Electrical synapse have a direct connection in the form of a gap junction, which allows current to flow extremely fast from one neuron to the next. This has the advantage of allowing neural circuits to synchronise rapidly. One of the benefits of an electrical synapse is the ability to allow current flow in both directions, meaning a bi-directional flow of information. It is believed that these types of synapses are used in fast response actions such as the 'fight or flight mode' in humans [5].


Fig. 1.2 Overview of neural connectivity, left, shows an example of an AP including approximate channel opening and closing times, right, shows the basic structure of a single neuron

### 1.2.2 Neural oscillations

The term neuronal oscillation refers to periodic variations in neural activity. These variations can be measured at different scales such as the microscopic scale, which could consist of the measuring of direct synaptic currents which produce spike trains of AP's, the mesoscopic scale, which consists of the summation of many synaptic currents from a Local network, named a local field potential (LFP), or the macroscopic scale, in the form of electroencephalography (EEG) data, which is the measure of multiple local networks [6].

The history of neural oscillations started with the first ever recordings of individual microscopic recordings. First recorded by Richard Caton in 1875, a physician from

Liverpool, England, who used electrodes to probe the exposed surface of the brain in animals. Using a reflecting galvanometer, he was successful in monitoring signals in the microamperes range [7].

Nevertheless, it was the work of Berger in 1929, who first reported that he had identified oscillations of approximately $8-12 \mathrm{~Hz}$ coming from the brain. Berger named this the alpha band since it was the first oscillation detected from such a source. This was early on in his pioneering work on the study of EEG. During one of his experiments Berger noticed that while the patients eyes were closed the prominent oscillations of the alpha band were visible. In the power spectrum the alpha waves produced a lone prominent peak of at approximately 12 Hz . However, when the patient opened their eyes the oscillations seemed to diminish in amplitude and become faster and more erratic, in a way the signals seemed to desynchronise and the prominent peak disappeared. This is known as the 'Berger effect'. Noting this, it was apparent that the alpha oscillations were attenuated by other more complex frequencies due to the visual stimuli originating from the occipital lobe.

Further observations of Hans Bergers works were carried out by W. Grey Walter in 1934, who devised an experiment entitled 'Thought and Brain: A Cambridge experiment', in Which one set of results was quoted as:
'When the eyes of a subject were open the lines were irregular, but when the subject's eyes were closed they showed as regular sinusoidal type signals occurring approximately every 10 seconds. Interestingly, When the subject closed their eyes and was asked to perform a simple arithmetic problem, the regular patterns disappeared, similar to that of when the patient's eyes were open. The lines continued to appear irregular until the simple problem was solved at which time the regular patterns reappeared'.

The fundamental observation by these pioneers revealed that the electrical fields recorded, must have been the combination of thousands of neurons firing in synchrony as stated by [8].

Since then, further advances in technology have led to the identification of multiple active frequency bands in which oscillations tend to occur. Namely,

- Infraslow $(<0.2 \mathrm{~Hz})$ and $\delta=0.2-3.5 \mathrm{~Hz}$. These wave patterns are usually seen during sleep of newborn infants or adults with serious brain diseases.
- $\theta=4-7.5 \mathrm{~Hz}$. These waves have been identified to mainly oscillate in the parietal and temporal regions of children's brains, and in healthy adults. Nonetheless, these slow varying oscillations are absent or indistinguishable under normal
conditions. Nevertheless, these oscillations do appear in healthy adults who show signs of emotional stress or frustration.
- $\alpha, \mu=8-13 \mathrm{~Hz}$. These oscillations tend to occur during the period when a person is awake but in a very relaxed state, mainly with the eyes closed. The introduction of complex thought was proven to also diminish alpha waves causing alpha blocking due to complex thought.
- $\beta=14-30 \mathrm{~Hz}$. The lower spectrum of the beta band usually falls into the same category as the alpha band, in that it can be disturbed by small amounts of complex activity or tension. The upper spectrum of the beta band is only affected by extreme thought processes, such as complex arithmetic. The beta band is usually considered as the awake and alert band, as we constantly process visual and auditory senses, as well as perform cognitive tasks throughout the day.

Other oscillatory bands include, $\gamma=30-90 \mathrm{~Hz}$ and the upper limit of High Frequency Oscillations $\mathrm{HFO}>90 \mathrm{~Hz}$. Recent research is, now starting to identify the gamma band as a communication layer between individual neural circuits [9]. Fig. 1.3, shows the decomposition of an original neural signal measured using EEG, into some common respective oscillatory bands.


Fig. 1.3 Example of the most common neuronal oscillatory bands

The interconnection of neurons forms several states of connectivity, three main types are as follows [10]:

1. structural connectivity, which refers to the anatomical connectivity via the structure of major tracts (i.e, white matter) connecting local and remote cortical regions of the brain.
2. functional connectivity, which is a statistical measure of the amount of connectivity in one region vs another and their dependence upon each other.
3. effective connectivity, the amount of connectivity in one cortical region which directly affects another cortical region by either activation or depression

### 1.3 Phase and Synchronisation

### 1.3.1 Basic concept

Phase is defined as the angular change in a signal over time. This can be represented as the anticlockwise rotation around the unit circle. Each adjustment is measured in terms of degrees, ranging from $0^{\circ}$ to $360^{\circ}$, which indicates a full rotation around the unit circle. The rotation can also be measured in the SI unit radians, where $360^{\circ}=2 \pi$, radians.

A sinusoidal wave can be expressed as:

$$
\begin{equation*}
x(t)=A \cdot \sin (\omega t+\theta) \tag{1.1}
\end{equation*}
$$

where, A is the amplitude, $\theta$ (this has no relation to the theta oscillatory band described above) is the initial phase of the signal and $\omega=2 \pi f$ denotes the rate of change of the vector rotation around the unit circle. The rate of change of phase increases or decrease as the frequency of the signal. If the frequency remains constant, the rate of change in phase will also remain constant. These types of signals are known as stationary signals.

Non-stationary signals, however, refers to a signal in which frequency changes over time, such as a synthetic sinusoidal chirp in which the rate of change in phase is constantly increasing. Another non-stationary source is that of EEG signals as LFP's tend to incorporate a wide range of frequencies.

Fig. 1.4, shows an example of the change in phase angle from a typical sinusoidal waveform and a cosine waveform. In this case, the first peak in the sine wave represents 0 radians and the first minimum in the cosine wave represents, $\pi$ radians. As the two signals evolve, by the time the first minimum has appeared in the sine wave the phase angle has increased to $\pi$ radians and the cosine has evolved to $2 \pi$ radians.

Since the sine wave and cosine wave are both stationary at 10 Hz , the phase of both signals increases at a fixed rate. In comparative situations, it is desirable to take the phase difference between the two waveforms. This can give rise to information on their frequency offsets with respect to one another and can be calculated as:

$$
\begin{equation*}
\theta=\phi_{\text {signal1 }}-\phi_{\text {signal2 }} \tag{1.2}
\end{equation*}
$$

Using specific markers in each signal such as minima or maxima, if the first derivative $\frac{d\left(\phi_{\text {signal1 }}-\phi_{\text {signal } 2}\right)}{d t}$, is constant it can be said that the signals have a constant phase difference. Since the two signals in Fig. 1.4 are of a constant 10 Hz , the phase difference between the two is constant. In this case, the constant phase change is $\pi$ radians [11].

### 1.3.2 Synchronisation and phase locking

In general terms, synchronisation is defined as any two-coupled (phase locked) oscillating systems, which have a relationship in both phase and frequency, but at the same time are independent of amplitudes. In non-disturbed and noise free systems synchronisation is usually described as the phase locking between instantaneous phase angles such that $n \cdot \phi_{s 1}-m \cdot \phi_{s 2}=$ const, where $\phi_{s 1}$ and $\phi_{s 2}$ are the instantaneous phase angles of signal 1 and signal 2 , respectively. $m$ and $n$, are integer based weights which need adjusting based on the source of the oscillating system.

In the example in Fig. 1.4, although the two signals are in anti-phase there does exist a relationship between the two, in terms of phase locking.

In the case of non stationary signals, the phase locking condition should be considered as: $\left|n \cdot \phi_{s 1}-m \cdot \phi_{s 2}-\delta\right|<$ const. Where $\delta$, is some average phase shift. This condition indicates that although the rate of change is not completely constant, it should reside (fluctuate) around a common constant [12].


Fig. 1.4 Phase: example of how phase rotates anti-clockwise around the unit circle in a stationary sine wave

In many cases of phase locking, the values $m$ and $n$ are usually set to a fixed $1: 1$ ratio. This is especially true if the signals originate from the same source such as the brain. Nevertheless, this phase locking attribute also holds true for signals of different frequencies, such as a stationary sine wave of 10 Hz and a stationary sine wave of 20 Hz . Although the frequencies are not the same there does exist a relationship in phase known as cross-frequency phase locking [13, 14].

### 1.3.3 Synchronisation in the brain

The human brain seems to effortlessly communicate large quantities of information over multiple regions of the brain. However, one of the questions still unanswered is how neural communication between assembles throughout the larger brain actually works. That's to say, what decides what information is accepted or declined at the input of neural assemblies.

For many years it was assumed that general information processing was carried out by changes in firing patterns of so-called 'smart neurons'. which were dedicated to certain tasks and functions. Nevertheless, the work derived from Hans Berger and others has led to the question as to whether synchronisation of neural assemblies is the key to information processing and learning. The fact that neural oscillatory patterns exist, indicates that to some degree, neural synchrony at the given frequency must be intrinsic of some type of neural assembly collaboration.

Over recent years, new evidence is emerging that precise synchronisation and desynchronisation of neural assemblies may, in fact, be the key to the encoding of information transfer within the brain. This can be seen in various reviews and experimental results from [15-17]

Two main hypotheses have been suggested for the efficient transfer of information between neural circuits and brain regions. Namely, coherence, in the form of phase synchronisation and gating by inhibition.

Phase synchronisation could be used as an identifier between neural assemblies, similar to that of two radios set to the same frequency channel. If the presynaptic response from one neural circuit is oscillating at the correct excitability rate of the postsynaptic neurons, then the information is accepted. However, if the presynaptic response is oscillating at a different rate (different frequency), then the postsynaptic inputs of the second neural circuit then the information is blocked or diminished, as with a radios set at different frequencies.

In general terms, it is the phase of an oscillatory neuron population which determines their excitability, hence their spike timings. It is, therefore, the phase relationship between neuron populations which determines routing. This has been proposed to occur in the gamma band [18].

The flow of information is controlled by an increase of alpha oscillations which inhibit the neural population which is not firing in synchrony [19].

### 1.4 Synchronisation in pathological brain states

The topic of the synchrony between neural circuits for proper functional neuronal communication is a trending topic in neuroscience today.

When comparing brain states we like to consider the differences between normal and pathological brains, in order to identify the connectivity differences which may exist between them. Therefore, the data of pathological brain state patients is usually compared with that of a control subject (a patient with no medical history of neurological disorders). Nevertheless, in the case of neurological disorders such as epilepsy, the patients inter-ictal epileptic period can be associated with a non-pathological brain state, hence used in further analysis.

In order to distinguish between these two brain states, we use a common mathematical tool known as graph theory. This allows us to gather insight into the structural, functional and effective connectivity of the brain. It allows us to visualise the overall connectivity as a function of time.

For an in-depth look into the most common mathematical calculations and an overview of the steps required to calculate complex graph networks. Please see appendix A.

It is widely accepted that the brains neural communication is characteristic of a small world network where neural clusters are well connected and transfer information over small distances. Therefore comparing the small-worldness of a non-pathological brain state with that of pathological states can identify the changes which occur in terms of overall functional connectivity

Fig. 1.5, shows an overview of the steps required for identifying small-worldness in epilepsy when taken from EEG sources.


Fig. 1.5 Example of how graph theory methods can be applied to real data. In this case, we compare an epileptic patients ictal period to that of their non ictal period. We then calculate M and A using an binary/undirected graph and calculate metrics as per needed

1. Firstly, all synchronisation values for every possible combination of electrode positions are computed, creating a $O=N X M$ matrix. Where N corresponds to the electrode combination and M corresponds to each synchronisation value for the given electrodes over time.
2. Next, two matrices $G 1=N X N$ For the non ictal period and $G 2=N X N$ for the ictal period are constructed. This is done by creating a single mean representative value for each electrode combination from $O$ such that:

$$
\begin{equation*}
G_{x(i, j)}=\frac{1}{M} \sum_{z=0}^{M} O_{i, j} \tag{1.3}
\end{equation*}
$$

3. The next step is to apply thresholds to each matrix $G$, for the purpose of creating two binary based adjacent matrices $A_{x}$. The threshold which is applied is subject to the experimental data and the related subject at hand. In many cases, various thresholds are tested. This allows for the identification of the strongest connections and builds 3d topologies which give rise to information on $C, L, k$.

$$
\left[\begin{array}{ccccc}
\phi_{11} & \phi_{12} & \phi_{13} & \ldots & \phi_{1 n} \\
\phi_{21} & \phi_{22} & \phi_{23} & \ldots & \phi_{2 n} \\
\vdots & \vdots & \vdots & \ddots & \vdots \\
\phi_{d 1} & \phi_{d 2} & \phi_{d 3} & \ldots & \phi_{d n}
\end{array}\right]=\left[\begin{array}{ccccc}
0 & 0 & 1 & \ldots & 0 \\
1 & 0 & 1 & \ldots & 1 \\
\vdots & \vdots & \vdots & \ddots & \vdots \\
0 & 0 & 1 & \ldots & 1
\end{array}\right]
$$

4. Finally, we can calculate $\lambda, \gamma$ and $\eta$, by calculating the mean clustering coefficients and the mean shortest path lengths.to distinguish the small-world characteristics and small-worldness.

### 1.4.1 Synchrony in neurological disorders

Although each neurological disorder has distinct causes and effects, synchrony has been found to manifest itself as an identifier, to distinguish between the normal and neurologically damaged brain. Table 1.2 [20], shows an overview of the most common neurological disorders as described above and how long and short-range communication is affected by increases or decreases in synchronisation. Other numerical methods such as graph theoretical analysis (please see appendix A) have also been shown to be a useful tool in the identification of both functional and structural connectivity.

In Alzheimer Disease (AD) synchronisation has been observed to increase in the $\theta$ and $\delta$ bands whilst, conversely, reducing in both the $\alpha$ and $\beta$ bands at resting state. Using a synchronisation likelihood (SL) measure, it was determined that these bands decreased in synchronisation over both long and short range recording sites [21-23]. Whilst global efficiency measures are higher in AD patients compared to the normal brain, the brain's ability to synchronise decreased significantly over multiple EEG bands in AD patients when their eyes were closed according to [24]. Synchronisation in AD patients has also been analysed in patients during memory working tasks. These include EEG and functional Magnetic Resonance imaging (fMRI) analysis of functional connectivity. Once again it was shown that a decrease in synchronisation was present when compared to control patients specifically in the $\alpha$ and $\beta$ bands [25].

The way our brain synchronises does not just affect cognitive functions. In fact, there is evidence which suggests that synchronisation in the $\beta$ band is related to pre-motor movements (i.e preparation for movement). Nevertheless, once the actual movement takes place the $\beta$ activity is replaced by $\gamma$ activity [26, 27]. Moreover, there is evidence to suggest that an increase in $\beta$ activity could be responsible for tremors in Parkinson Disease (PD) [28]. Where in patients who do not suffer from PD a short

| Disorder | Neural synchrony |
| :--- | :--- |
| Epilepsy | Increase in local synchrony and evidence for long range reduction |
| Schizophrenia | Reduction in local and long range synchrony |
| Alzheimer | Reduced synchrony, evidence for reduced functional connectivity |
| Parkinson | Increase in synchrony |

Table 1.2 Synchrony in different neurological disorders.
period of $\beta$ synchrony prior to a motor movement is replaced by fast $\gamma$ bursts during the movement (where the $\beta$ oscillations are dulled by inhibition), in patients with PD, however, the hypersynchronous $\beta$ activity cannot be dulled and hence the $\gamma$ oscillations responsible for the movement cannot take place [29].

It has been proposed that memory, attention and perceptual organisation are associated with synchronisation in the $\beta$ and $\gamma$ bands [30]. Various studies of Schizophrenia (SZ) show that a deficit in perceptual organisation is a common symptom and could be related to a reduction in synchrony in the $\beta$ and $\gamma$ bands [20].

Epilepsy (EP), on the other hand, is a well studied neurological disorder with overwhelming evidence suggesting that seizures occur due to hyper-synchronous networks. High-frequency oscillations in the $\gamma$ band have especially been observed in EEG both during the ictal and pre-ictal periods [31]. It has also been observed that neurons synchronise with high precision in the $\beta$ band pre seizures, however, synchronous activity is reduced during the ictal event [32]. Conversely, a decrease in synchronisation was proposed by Le Van Quyen et al. who examined the synchronous activity of eight patients finding a pre-ictal reduction in the $\beta$ band in $77 \%$ of seizures [33].

### 1.5 Phase synchronisation methods

### 1.5.1 Analytical measures

Two main closed-form analytical approaches have been proposed for the estimation of phase angles. One is based on the Hilbert Transform and the other on the Wavelet Transform.

The Hilbert transform (HT) creates a projection of the original signal on to the imaginary plane in such a way that positive frequencies are phase shifted by $-\pi / 2$ and negative frequencies by $+\pi / 2$, while keeping the amplitude unaffected. Analytically, the

Hilbert transform $\tilde{s}(t)$ can be interpreted as the convolution of $s(t)$ with the function $h(t)=1 /(\pi t)$ and is given by [34]:

$$
\begin{equation*}
\tilde{s}(t)=\frac{1}{\pi} \cdot p \cdot v \int_{-\infty}^{+\infty} \frac{s(\tau)}{t-\tau} \cdot d \tau \tag{1.4}
\end{equation*}
$$

Where the integral is defined in terms of the Cauchy principal value $p . v$ and $\tilde{s}(t)$ is a $\left(90^{\circ}\right)$ phase shifted version of the original signal, $s(t)$.

In continuous time signals the HT can be represented as the convolution of a real signal $s(t)$ and a function $h(t)=\frac{1}{\pi t}$, such that $\tilde{s}(t)=s(t) * \frac{1}{\pi t}[35]$.

In the frequency domain the HT can be written as:

$$
\begin{equation*}
\tilde{s}(f)=X(f) \times(-j \operatorname{sgn}(f)) \tag{1.5}
\end{equation*}
$$

Where $(-j \operatorname{sgn}(f))$, is the HT of $X(f)$ [35].
An analytical construct introduced by Gabor in 1946 utilises the HT, to create an analytical signal, given by:

$$
\begin{equation*}
s_{a}(t)=s(t)+j \tilde{s}(t)=A(t) e^{j \phi(t)} \tag{1.6}
\end{equation*}
$$

The resulting complex signal $s_{a}(t)$, has the property that there exist no spectral components for negative frequencies, that's to say the Discrete Time Fourier transform of $s_{a}(t)$, is $S_{a}\left(e^{j \omega}\right)=0,-\pi<\omega<0$.

The instantaneous phase of the analytical signal $s_{a}(t)$ can be calculated as:

$$
\begin{equation*}
\phi(t)=\tan ^{-1}\left[\frac{\tilde{s}(t)}{s(t)}\right] \tag{1.7}
\end{equation*}
$$

Two other important metrics can be extracted from the HT. Firstly, the instantaneous amplitude of the signal, which can be extracted as [36]:

$$
\begin{equation*}
A(t)=\left(s(t)^{2}+\tilde{s}(t)^{2}\right)^{\frac{1}{2}} \tag{1.8}
\end{equation*}
$$

Secondly, the instantaneous frequency, which is given as the first derivative of the phase,

$$
\begin{equation*}
\omega(t)=\frac{d \phi}{d t} \tag{1.9}
\end{equation*}
$$

The HT, however, is a linear function which in retrospect only works on stationary signals. Nevertheless, an adaptation of the HT can be used known as the Hilbert-Huang Transform (HHT).

The HHT incorporates an empirical mode decomposition (EMD) to the signals before taking the HT. The EMD consists of breaking down the signal into a finite number of components which are called Intrinsic Mode Functions (IMFs). These are extracted from an arbitrary time series $x(t)$, by means of sifting. In order to sift all extrema, both maximum and minimum. The first IMF can be extracted as [37]:

$$
\begin{equation*}
h_{1}(t)=x(t)-m_{1}(t) . \tag{1.10}
\end{equation*}
$$

Where, $x(t)$ is the time series in question and $m_{1}(t)$, is the mean of the upper and lower envelope derived from the extrema.

However, $h_{1}(t)$, is usually not sufficient to satisfy the constraints of an IMF and hence the process is repeated such that:

$$
\begin{equation*}
h_{11}(t)=h_{1}(t)-m_{11}(t) . \tag{1.11}
\end{equation*}
$$

Where $m_{11}(t)$, is the mean of the upper and lower envelopes of $h_{1}(t)$.
In general, the process is as follows:

$$
\begin{equation*}
h_{1 k}(t)=h_{1(k-1)}(t)-m_{1 k}(t) \tag{1.12}
\end{equation*}
$$

where k is the number of iterations to find the first IMF $C_{1}(t)=h_{1 k}(t)$.
Furthermore, the residual part the signal should be obtained from such that:

$$
\begin{equation*}
h_{1}(t)=x(t)-c_{1}(t) \tag{1.13}
\end{equation*}
$$

at the end of the process the original signal can be represented as:

$$
\begin{equation*}
x(t)=\sum_{i=1}^{n} c_{i}(t)+r_{n}(t) \tag{1.14}
\end{equation*}
$$

The HT is then performed on each IMF [38]:

$$
\begin{equation*}
c_{a i}(t)=c_{i}(t)+j \tilde{c}_{i}(t) \tag{1.15}
\end{equation*}
$$

The instantaneous phase of the signal can be extracted as:

$$
\begin{equation*}
\phi_{i}(t)=\tan ^{-1}\left[\frac{\tilde{c}_{i}^{2}(t)}{c_{i}^{2}(t)}\right] \tag{1.16}
\end{equation*}
$$

A similar approach for estimating phase angles [39] uses a definition based on the Wavelet Transform (WT). Here, the phase variable is defined as,

$$
\begin{equation*}
\varphi_{s}(t)=\arctan \frac{\operatorname{Im}(W(t))}{\operatorname{Re}(W(t))} \tag{1.17}
\end{equation*}
$$

where $\operatorname{Im}(\cdot)$ and $\operatorname{Re}(\cdot)$ denote imaginary and real part, respectively, and $W(t)$ is the convolution of the band-limited signal $s(t)$ with a Morlet wavelet $\psi(t)$,

$$
\begin{align*}
W(t) & =\int_{-\infty}^{+\infty} \psi(t-\tau) s(\tau) \cdot d \tau  \tag{1.18}\\
\psi(t) & =\exp \left(\frac{-t^{2}}{2 \sigma^{2}}\right) \cdot \exp \left(j \omega_{0} t\right)
\end{align*}
$$

where $\sigma$ is the decay rate of the wavelet and $\omega_{0}$ is the centre frequency of the signal band. Both analytical methods give similar results when applied to neurophysiological data [40].

The Phase Locking Value (PLV) or mean phase coherence usually accompanies the $H T$ or $W T$ methods as an index for quantifying the amount of synchronisation between two signals.

$$
\begin{equation*}
P L V=\left|\frac{1}{N} \sum_{K=0}^{N-1} e^{j \phi(t)}\right|=\frac{1}{N} \cdot \sqrt{\left.\left[\sum_{K=0}^{N-1} \cos \left(\Delta \phi_{k}\right)\right]^{2}+\sum_{K=0}^{N-1} \sin \left(\Delta \phi_{k}\right)\right]^{2}} \tag{1.19}
\end{equation*}
$$

The $P L V$ converts instances of the relative phase $\triangle \varphi$ into unit vectors on the complex plane. If $N$ of said vectors all have the same instantaneous phase (i.e the same vector direction) then the $P L V$ will average out to 1 which equates to fully coupled oscillations for that period. However, in the case that the relative phase angles are very different the $P L V$ will result in a value close to 0 .

In some cases, a normalised PLV is more desirable than raw values as it gives a better approximation of the difference between normal state PLV and large changes, due to stimulus. The normalised values can be extracted as,

$$
\begin{equation*}
P L V_{\text {norm }}=\frac{P L V-\operatorname{mean}\left(P L V_{t s}\right)}{\sigma\left(P L V_{t s}\right)} \tag{1.20}
\end{equation*}
$$

Where $t s$, is a small baseline selection of samples taken before the episode. In this case, $\sigma$, represents the standard deviation of the baseline.

This metric is actually based on the Z-score and provides a zero mean offset.

### 1.5.2 Numerical measures

Phase synchronisation measures can be alternatively derived from the phase space trajectories of the signals. Using time-delay embedding procedures [41], the phase space trajectory of a time series $\{s(k)\}$ is obtained by constructing the vectors,

$$
\begin{equation*}
\vec{S}_{i}=\{s(j), s(j+d), \ldots, s(j+(m-1) d)\} \tag{1.21}
\end{equation*}
$$

where $i=1 \ldots N, j=i+\bmod [N-(m-1) d], m \geq 1$ is the embedding dimension and $d \geq 1$ is an arbitrary but fixed time increment.

Based on this topological representation, the phase synchronisation between two signals can be estimated by computing the cross-correlation between the probabilities of recurrence in their respective phase spaces [42]. This approach has been used recently for quantifying functional connectivity in EEG recordings [43]. The probability of recurrence of a signal measures the likelihood that each phase space vector returns to its neighbourhood after a time delay $\tau$. It is calculated as:

$$
\begin{equation*}
p_{r}(\tau)=\frac{1}{N-\tau} \sum_{i=1}^{N-\tau} \Theta\left(\epsilon-\left\|\vec{S}_{i}-\vec{S}_{i+\tau}\right\|\right) \tag{1.22}
\end{equation*}
$$

where $\epsilon$ is a pre-defined distance threshold, $\|\cdot\|$ is a norm to calculate the distance between vectors and $\Theta$ is the Heaviside function. The cross-correlation $C P R$ of two trajectories is calculated as:

$$
\begin{equation*}
C P R=\frac{\left\langle\left(p_{r, 1}(\tau)-m_{1}\right) \cdot\left(p_{r, 2}(\tau)-m_{2}\right)\right\rangle}{\sigma_{1} \cdot \sigma_{2}} \tag{1.23}
\end{equation*}
$$

where $m_{1}$ and $m_{2}$ are the mean, and $\sigma_{1}$ and $\sigma_{2}$ are the standard deviations of $p_{r, 1}(\tau)$ and $p_{r, 2}(\tau)$, respectively. If both signals are in synchrony, their probabilities of recurrence will peak at the same time and $C P R \sim 1$. Contrarily, if the signals are not synchronised, low values of $C P R$ can be expected.

Numerical techniques have been also proposed for the quantification of synchrony, as an alternative to the $P L V$ index in 1.19 [44]. Assuming that the phase angles of both signals have been previously estimated, a synchronisation index can be calculated based on the Shannon entropy of the phase difference distribution. Having an estimate $P_{s e}(l)$, $l=1, \ldots, L$ of the relative frequency of finding a phase difference $\Delta \varphi=\varphi_{s 1}-\varphi_{s 2}$ in a
certain bin $l$, the index is given by,

$$
\begin{equation*}
S_{s e}=1+\frac{1}{\ln (L)} \sum_{l=1}^{L} P_{s e}(l) \cdot \ln \left[P_{s e}(l)\right] \tag{1.24}
\end{equation*}
$$

where $L$ is the number of bins. Note that $S_{s e}$ is comprised in the interval $[0,1]$, where $S_{s e}=0$ corresponds to a uniform distribution (no synchronisation) and $S_{s e}=1$ corresponds to a distribution localised in one point. The estimate of this index heavily depends on $L$ [44].

Another synchronisation index is based on the conditional probability $P_{c p}(k, l)$ to find the phase of a first signal in a bin $k$ when the phase of the second signal falls in the $l$-th bin, $l=1, \ldots, L$. Denoting as $M_{l}$ the number of hits of the second signal in the $l$ bin, a synchronisation index can be defined as,

$$
\begin{equation*}
S_{c p}=\frac{1}{L} \sum_{l=1}^{L}\left|\frac{1}{M_{l}} \sum_{k=1}^{M_{l}} \exp \left[j P_{c p}(k, l)\right]\right| \tag{1.25}
\end{equation*}
$$

It has been found that this index is particularly suitable for revealing weak interactions between signals [44-47].

### 1.6 VLSI implementations of PS estimators

As mentioned in Sec.1.5.1, one popular approach for the calculation of the instantaneous phase of a signal relies on the construction of the analytic representation $s_{a}(t)=$ $s(t)+j \tilde{s}(t)$, where $\tilde{s}(t)$ is the Hilbert Transform of $s(t)$ [see 1.4]. Using time-frequency domain techniques, the Hilbert Transform can be derived by [48] (i) obtaining the Fourier transform of $s(t)$, (ii) nulling the negative frequency components, (iii) calculating the inverse Fourier transform and (iv) taking the imaginary part of the result. Given the non-stationary nature of neural signals, the Fourier transform should be applied over short intervals. This suggests the use of the Short Time Fourier Transform (STFT) algorithm instead of the classical Fast Fourier Transform (FFT) [36]. 1.4 and 1.19

A simpler method for the generation of the analytic signal representation $s_{a}(t)$ uses Hilbert Transformers based on digital filtering. These transformers can be implemented in complex domain or formed by the combination of two sub-components; a Hilbert filter with ideal transfer function $-j \operatorname{sgn}(f)$ for the generation of the imaginary part of $s_{a}(t)$, and a delay equal to that of the Hilbert filter for the real part. In both cases,
the total group delay of the signal components should be kept constant to not cause phase errors. The vector analyzer presented in [49] follows the second implementation approach and employs 16 -tap Hilbert finite impulse response (FIR) filters for obtaining $\tilde{s}(t)$, and 16-tap All-Pass FIR filters for implementing the delay. In a more recent implementation [50], the in-phase and quadrature components are directly provided by the mixed-signal acquisition front-end, and four 64-tap FIR filters are used for band selection.

Another transform-based approach for deriving the instantaneous phase of a signal uses Wavelets (see 1.18). In this case, the on-chip implementation of the method requires Multiply-and-ACcumulate (MAC) processors to correlate the input time series with the wavelet templates. As an example, [51] proposes a charge-recycling mixedsignal MAC processor for epilepsy detection in which time series of 1024 samples are serially loaded and correlated in parallel with all the Morlet wavelet templates (coded in 32 frequency bins with 4-bit coefficient resolution) stored in the on-chip memory.

The trigonometric functions involved in 1.7 and 1.17 as well as the computation of the phase locking value in 1.19 can be readily implemented by CORDIC (COordinate Rotation DIgital Computer) units. This is actually done in [52] where a digital signal processing (DSP) block formed by three 16-bit CORDIC cores and two 32 -tap moving average FIR filters is used for computing the phase locking value ( $P L V$ ) from the analytical signal $s_{a}(t)$.

Numerical methods for computing PS, such as the one based on probabilities of recurrence, $p_{r}(\tau)$, described in Sec. 1.5.2, typically use simpler logic than transformbased techniques at the price of increased latency and more memory resources. Thus, for instance, the evaluation of $p_{r}(\tau)$ in 1.22 requires the collection and combination of phase space trajectories, demanding for a large memory allocation. Nevertheless, it is worth observing that, depending on $\tau$, there are coincident terms in the sum 1.22. This opens doors for reducing the computational complexity of the algorithm by avoiding recalculations. This is actually the approach followed in [53], where a differential scheduling for the computation of the correlation integral of a signal (similar to the calculation of recurrences) allows for a substantial reduction in complexity. Following the calculation of $p_{r}(\tau)$, a MAC unit should be used for the calculation of the cross-correlation in 1.23 to serve as a synchronization index.

As shown in 1.24 and 1.25 , numerical methods can also be used for the computation of synchronization indexes. Although the computational complexity is relaxed as compared to $P L V$ (in particular for the index based on Shannon entropy), long sliding

Table 1.3 Performance summary of proposals related to on-chip PS calculation

|  | Process | Supply | Core Area | Input rate | Clk Freq. | Power cons. | Computation capability |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :--- |
| $[49]$ | $0.13 \mu \mathrm{~m}$ | 1.2 V | $1.86 \mathrm{~mm}^{2}$ | $7.2 \mathrm{kHz}(8$-bit) | 10 MHz | $400 \mu \mathrm{~W}$ | 32 input-pairs multiplexed phase synchronization processor |
| $[50]$ | $0.13 \mu \mathrm{~m}$ | 1.2 V | $1.27 \mathrm{~mm}^{2}$ | NA | NA | $260 \mu \mathrm{~W}$ | 32 input-pairs multiplexed phase synchronization processor |
| $[51]$ | $0.35 \mu \mathrm{~m}$ | 1.65 V | $16 \mathrm{~mm}^{2}$ | NA | 50 Hz | NA $^{a}$ | $128 \times 1024$ binary MAC operator |
| $[48]$ | $0.13 \mu \mathrm{~m}$ | 1.2 V | $1.18 \mathrm{~mm}^{2}$ | $40 \mathrm{kHz}(16$-bit) | 10.24 MHz | $3.64 .4 \mu \mathrm{~W}$ | 16 -channel multiplexed 16-bit Hilbert Transform block |
| $[52]$ | $0.13 \mu \mathrm{~m}$ | 0.85 V | $0.178 \mathrm{~mm}^{2}$ | $1.7 \mathrm{kHz}(8$-bit) | 2.5 MHz | $102 \mu \mathrm{~W}$ | 10-bit PLV Processor |
| $[53]$ | 90 nm | 1.0 V | $0.143 \mathrm{~mm}^{2}$ | $256 \mathrm{~Hz}(9$-bit) | 4096 Hz | $2.34 \mu \mathrm{~W}$ | 16-channel Correlation Integral Processor |
| $[55]$ | 90 nm | 1.0 V | $1.02 \mathrm{~mm}^{2}$ | $256 \mathrm{~Hz}(16$-bit) | 522.24 kHz | $57.3 \mu \mathrm{~W}$ | 1-channel EMD processor extracting 5 IMFs and residue |

[^0]windows are needed to populate the histograms and obtain meaningful distribution of probabilities. Hence, circuit simplicity is counterbalanced with an increase in latency and memory depth.

Table 1.3 illustrates the performance of the different integrated circuits presented in this section. The two first rows are for complete PS processors while the rest corresponds to building elements which can be eventually used depending on the particular PS implementation strategy. The table clearly shows that the algorithms used for PS calculation, although easily programmable in computers, tend to occupy large area and consume significant power when dealing with silicon integration. The problem is even more acute in the context of functional brain connectivity, where multiple phase synchronisation indexes from different sites are needed. For instance, if functional connectivity has to be measured between 16 recording sites, as it is typically done in a standard 10-20 EEG electrode system, 120 different combinations of neural signal pairs should be simultaneously addressed. This means application specific integrated circuits (ASIC's) for functional connectivity quickly become far to big and/or power hungry, even if sophisticated multi-thread sharing DSP techniques are employed.

### 1.7 Thesis Objectives

This thesis aims to address three major aspects:

- Development of an algorithm for the detection and quantification of phase synchronisation between pairs of neural signals which significantly alleviate the constraints of power consumption and area occupation as compared to state-of-art methods. The algorithm should exhibit little or no degradation
on performance metrics such as seizure detection sensitivity, noise tolerance or functional connectivity computation.
- Implementation of a low-power, low area silicon prototype of the proposed algorithm to confirm its suitability for VLSI, and performance validation with human recordings in a realistic application scenario, namely, the detection of seizures in patients with different epileptic pathologies.
- Demonstration of the scalability of design through the implementation of a multichannel processor for surface or intracranial EEG signals, and confirmation that the proposal represents a low-cost, low-complexity, programmable and portable solution for computing functional connectivity in wearable/implantable systems.


## Chapter 2

Delay Difference Analysis for Phase Synchronisation Computation

In this chapter, an algorithm for phase synchronisation computation, which aims to alleviate the area/power consumption burden of silicon integration of previous approaches such as in Sec.1.6 is proposed. The synchronisation algorithm, called Delay Difference Analysis (DDA), is based on the piece-wise linear approximation in [12], however, it has been modified by us to achieve a more hardware friendly implementation. Furthermore, a new synchronisation index is introduced which allows for a more reliable identification of synchronisation peaks. The two components of the algorithm, were then subjected to tests, including: simulation of nearly two thousand hours of real neural data, noise analysis and sensitivity analysis. Moreover, we include the effects of sampling rate, window length and sample distribution.

All of the following was carried out by the author of this thesis.

### 2.1 Proposed algorithm

Similar to the transform-based methods, this proposal is also based on the estimation of instantaneous phases in band-limited signals, however, instead of using complex filtering or wavelet convolutions, phases are extracted through the identification of distinct marker events in wave forms. Without loss of generality, in this work, it is assumed that such events correspond to the local minima of the signal at time instants $t_{n}$. The time interval between two consecutive minima correspond to one complete cycle and, therefore, the phase increment during this period is exactly $2 \pi$. Hence, the signal phase can be approximated for any arbitrary time instant $t_{n}<t<t_{n+1}$ as,

$$
\begin{equation*}
\varphi_{s}(t) \approx 2 \pi \frac{t-t_{n}}{t_{n+1}-t_{n}}+2 \pi n \tag{2.1}
\end{equation*}
$$

where the term $2 \pi n$ unwraps the phase angle and $T_{n}^{s}=t_{n+1}-t_{n}$ measures the duration of the transition period between the minima, as illustrated in Fig.2.1. Note that this approximation notably simplifies phase estimation as the problem basically reduces to a measure of time intervals. For this reason, the proposed algorithm is denoted as Delay Difference Analysis.

Based on the approximation in (2.1), an index for quantifying the synchronisation level between two signals has been proposed in [56]. It relies on creating histograms on how many times the events in one signal are preceded by events in the other. The approach has a low computational cost, however, similarly to the numerical techniques
described in Sec. 1.5.2, it requires long time series to build meaningful statistics and, in some sense, it wastes the time information between events.

The proposed approach for measuring synchronisation is similar to the PLV technique in (1.19) but avoids the use of trigonometric functions. DDA analyses the time difference between the transition periods of both signals, not their relative phase $\Delta \varphi$, and, remarkably, it operates on-the-fly with no need to store long signal sequences. The procedure simply consists in pairing transition periods from both signals as soon as they are detected. If a pair is formed between the $i$-th transition period of signal $s_{1}(t)$ and the $j$-th transition period of $s_{2}(t)$, the absolute difference $\triangle T_{n}=\left|T_{i}^{1}-T_{j}^{2}\right|$ is calculated, where $T_{i}^{1}$ and $T_{j}^{2}$ denote, respectively, the durations of said transition periods. If two or more transition periods in one signal are detected before a transition period is found in the other, only the last transition period of the former signal is accounted for in the computation of $\triangle T_{n}$. Fig. 2.1 shows an example of the procedure. This, in turn, increases the phase error distribution.

Let us denote by $K$ the number of absolute differences $\Delta T_{n}$ computed in the $k$-th sliding window of length $N$, and let us assume with no loss of generality that $N=2^{m}$. A synchronisation index between signals $s_{1}(t)$ and $s_{2}(t)$ can be defined as,

$$
\begin{equation*}
S_{d d a}^{(r)}(k)=1-\frac{2^{r}}{N} \min \left(\sum_{n=0}^{K-1}\left|\triangle T_{n}\right|-T_{o s}, \frac{N}{2^{r}}\right) \tag{2.2}
\end{equation*}
$$

where $r \in[0, m]$ is a user-defined selectivity control parameter and $T_{o s}$ is a positive integer offset for adjusting the synchronisation index range. Fig.2.2(a) plots $S_{d d a}^{(r)}$ for $T_{o s}=0$ and different selectivity configurations assuming that $s_{1}(t)$ is a sine wave at 20 Hz , and $s_{2}(t)$ is a chirp whose frequency linearly sweeps from 10 to 30 Hz . Both signals had a sampling rate of $1024 \mathrm{~S} / \mathrm{s}$ and were quantised at $10-\mathrm{b}$ of resolution. Every calculated index was obtained assuming a non-overlapping sliding window of length $N=1024$. Clearly, the higher the selectivity parameter, the narrower the band for which the synchronisation index obtains non-null values. No matter the $r$ parameter, the plots in Fig.2.2 are not symmetrical around the tone frequency of $s_{1}(t)$; they decay linearly for chirp frequencies below said tone but fall away more smoothly for higher frequencies. This is because the number of absolute differences $K$ is limited by the smaller frequency, $f_{\text {min }}$, of both signals as $K=N \cdot f_{\text {min }} / f_{s}$. In Fig.2.2(a), it is also observed that the peak value of the synchronisation index decreases with the selectivity parameter. This can be compensated, without drastically increasing the sampling frequency or the number of samples per observation window, by means of the offset


Fig. 2.1 Transition periods and approximated phases of two signals. Starting at point A, the DDA algorithm generates the following absolute differences between transition periods: $\left|T_{1}^{1}-T_{1}^{2}\right|,\left|T_{2}^{1}-T_{2}^{2}\right|,\left|T_{3}^{1}-T_{3}^{2}\right|$ and $\left|T_{5}^{1}-T_{4}^{2}\right|$.
parameter $T_{o s}$. This is illustrated in Fig.2.2(b) where $T_{o s}=6$ making the synchronised indexes for all selectivity parameters to mostly cover the range between 0 , indicating no coupling, and an approximate 1 for perfect coupling.

Note that too large of an offset may eventually make the synchronisation index larger than 1 , hence, a limiter, which can be easily implemented in hardware by an overflow detector, should be used together with (2.2).


Fig. 2.2 Synchronisation indexes obtained through the DDA algorithm for different selectivity parameters, using a sine wave and a swept-frequency cosine as input signals.
(a) $T_{o s}=0 ;$ (b) $T_{o s}=6$.

For comparison purposes, Fig. 2.3 shows the $P L V$ index (dashed line) for the same experiment as in Fig. 2.2 together with the index $S_{d d a}^{(4)}$ with no offset. Both approaches give comparable results, with the DDA producing a piecewise linear approximation of the main lobe of the $P L V$ index and eliminating the smaller side lobes. This is not surprising as the $P L V$ index can be approximated as $P L V \simeq 1+\alpha \sum_{k=0}^{N-1}\left|\triangle \varphi_{k}\right| / N$ for small $\Delta \varphi$ values, where $\alpha$ is a fitting parameter (see equation 1.19). Given the relationship between phases and time delays expressed in (2.1), a clear connection between the phase locking value and the Delay Difference Analysis can be established.

Appendix B.1, shows the MATLAB code used in the design and construction of the DDA algorithm.


Fig. 2.3 Results from DDA and Hilbert transform approaches for the same experiment in Fig. 2.2. The inset shows a zoom of the shaded area.

### 2.2 Parameters setting

### 2.2.1 Quantisation

In this section, we try to explain the effects of quantisation on the output of the algorithm. The test was the same as in Fig. 2.2(a) however, quantising the two input signals 1 and 2 , from 6 to 13 -b of resolution. The characteristics of the test can be seen below. From the results shown in Fig. 2.4, we can note that 6, 7 and 8-b of resolution cause a noisy output, significantly more for $r=0$ to $r=2$, whereas from 9-b onwards the output becomes recognisably consistent with Fig. 2.2(a). In this case, we can see that after 9-b of resolution at a fixed sampling frequency of $1024 \mathrm{~S} / \mathrm{s}$ the performance of the algorithm no longer increases. Nevertheless, to allow for multiple sampling frequencies a resolution of $10-\mathrm{b}$ is recommended. Mathematically speaking, the number of bits needed is relative to the sampling frequency and signal frequency such that $2^{n}>2 \cdot \frac{\text { samplingfrequency }}{\text { lowestsignalfrequency }}$.

### 2.2.2 Sample distribution

The sample distribution is another variable which should be analysed for this algorithm, as we consider the phase errors in terms of samples. Fig. 2.5, shows the sample distributions for 3 different sampling rates $1024 \mathrm{~S} / \mathrm{s}, 512 \mathrm{~S} / \mathrm{s}$ and $256 \mathrm{~S} / \mathrm{s}$ varied over a frequency range of 1 to 50 Hz .

Firstly, in Fig. 2.5, we can note that the general sample distribution at fixed sampling rates tend towards a non-linear exponential distribution at lower frequencies. This means that during lower frequencies the accumulated errors will present much higher values than that of the higher frequencies for a set window length. Nevertheless, if we consider relatively low sampling frequencies such as seen in Fig. 2.5. We can deduce that an approximate linear distribution can be extracted for frequencies ranging from 5 Hz upwards. Since the number of samples is defined as $\frac{f_{s}}{f}$ as $f$ increases the number of samples gets smaller.

It is, however, important to point out that samples at high values of $f$ will present themselves as the same value due to the rounding of samples in the distribution. As an example, at $1024 \mathrm{~S} / \mathrm{s}$ and 48 Hz the number of samples is $\frac{1024}{48}=21.3$ and at 49 Hz $\frac{1024}{49}=20.89$, therefore 48 Hz will obtain 21 samples after rounding and 49 Hz will also obtain 21 samples.


Fig. 2.4 Example of how quantisation of the input signals can effect the results obtained by the algorithm


Fig. 2.5 Example of the non-linearity of a sample distribution at different sampling frequencies

Therefore the most accurate results will occur using a 512 or 1024 bit sampling rate from 5 Hz upwards towards 30 Hz . That said the sampling frequency can always vary based on the specific frequency band of interest. As an example, if we would like to monitor signals in the 80 Hz range we could always increase the sampling frequency above 1024 as the distribution will be approximately linear at that frequency given the higher sampling rate. If we want to monitor the 10 Hz to 20 Hz range it makes more sense to use a lower sampling frequency of $256 \mathrm{~S} / \mathrm{s}$, where the linearity is highest and the effects of quantisation are not prominent.

### 2.2.3 Window length

The window length is a common factor which can greatly vary the outcome of the results as well as the detection of specific biomarkers. In Fig. 2.6, the effect of various window
lengths on the DDA algorithm can be seen, once again using the same experiment as in Fig. 2.2(a). The variables for the test can be seen below.

1. sampling frequency fixed 1024
2. window size variable $32 \cdot 2^{i}$, where i is varied from 1 to 10
3. Signal 1: sine frequency fixed 20 Hz
4. Signal 2: chirp frequency $10 \mathrm{~Hz}-30 \mathrm{~Hz}$

The results show that for very small time windows, the output of the DDA suffers. This occurs since at the lowest frequency of 10 Hz and the fixed sampling rate of 1024 , a single period of the waveform is composed of approximately 124 samples. However, the window length is only 64 samples, this indicates that DDA is unable to collect a sufficient amount of data for accurate results, instead, creating noise perturbations. At the other extreme, when the window length is very long such as 32 seconds, the DDA over collects samples meaning the central 20 Hz of the fixed sine wave never coincides solely with the 20 Hz of the chirp signal. Instead, the error accumulations from the chirp consist of more widespread frequencies. Therefore, the DDA never reaches one and has broader angles. In the case of the medium length windows of approximately 0.5 to 1 second, we see an optimal performance. As the window is sufficiently short, that the two tone frequencies can exist solely together within 1 window and is long enough to collect a reliable amount of errors.

It is important to point out that the signals captured during EEG, posses what is known as the 3 N's, non-stationary, non-linear and noisy. This can make identification of specific markers difficult using linear time-based approaches. Nevertheless, it has been observed that well filtered EEG signals posses quasi-stationary attributes for periods lasting up to 1 second.

Therefore, with these two factors in mind, it remains clear that the optimal window length should be the same as or similar to that of the sampling frequency of the device. Once again it is still possible to vary the sampling frequency as long as the window length adjusts accordingly.

### 2.3 Verification

The algorithm has been verified and validated using neural recording data available in the European Epilepsy database (http://epilepsy-database.eu/) [57]. This database


Fig. 2.6 Example of the effects of different window sizes on the algorithm

Table 2.1 Records used in the verification of the phase synchronisation processor

| Id | Patient | Dominant pattern | Electrodes ${ }^{a}$ | Sync. Pairs | Sample Rate | Seizures | Hours |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| \#1 | male 22y | rhythmic sharp waves | 1/114/0/0 | SCL7 - \{SCL8, SCR9, TPL1\} | 1024 Hz | 26 | 113.20 |
| \#2 | female 29y | rhythmic beta waves | 0/121/0/0 | HAR1 - \{HPR12, HPR1, HPR2\} | 1024 Hz | 9 | 183.10 |
| \#3 | female 16y | low amplitude fast activity | 21/0/12/48 | IHB2 - \{IHA1, IHA2, GB6 $\}$ | 256 Hz | 9 | 229.30 |
| \#4 | male 18y | repetitive spiking | 21/20/46/32 | BLB1- \{BLB3, TRB1, FP1 | 1024 Hz | 13 | 245.20 |
| \#5 | male 35y | rhythmic beta waves | 21/10/46/0 | TBLB1 - \{TBLB3, TBRB1, FP1 | 256 Hz | 26 | 180.00 |
| \#6 | female 53y | rhythmic beta waves | 19/25/16/0 | HL2 - \{HL1, HL4, TBB1\} | $256-512 \mathrm{~Hz}$ | 6 | 164.40 |
| \#7 | male 5y | low amplitude fast activity | 21/20/50/0 | TBA1 - \{TBA2, HRA4, HRA5\} | 1024 Hz | 22 | 170.60 |
| \#8 | male 15y | rhythmic beta waves | 51/72/52/58 | GG3 - \{TL2, GG4, GH2 \} | 256 Hz | 19 | 199.8 |
| \#9 | female 32y | rhythmic beta waves | 36/34/35/37 | HL4 - \{HL2, HL3, HL5\} | 1024 Hz | 9 | 162.6 |
| \#10 | female 11y | rhythmic alpha waves | 60/57/59/4 | HR12 - \{HR9, HR11, TBA4\} | 1024 Hz | 14 | 155.0 |

${ }^{a}$ (S/D/M/G) for surface, depth, strip and grid electrodes.
contains recordings of multiple patients including 225 scalp recordings, 50 intracranial recordings and over 100 annotated sets using both intracranial and surface electrodes which were organised into a standard 10-20 format.

In this work, simulation experiments including the $D D A$ and the $P L V$ with 10 recording sets included in the European Epilepsy database have been conducted. In total, 1803.2 hours of recordings and 61 annotated seizures have been analysed. Simulations were carried out in Matlab using mathematical models of the $D D A$ and the $P L V$ processors. In the $D D A$ case, the model closely follows the block diagram of Fig. 3.1 for $N=1024, r=1, M=10$ and $Q=2$ (see chapter 3, subsection 3.2.1 for definition of $M$ and $Q$ ) and the Matlab code can be seen in Appendix B. 1 while, in the PLV case, the model uses the architecture presented in [50]. In both cases, an input signal resolution of 10 -b has been assumed.

Table 2.1 shows the records used for the verification of the proposed phase synchronisation calculation approach. For each patient the table shows the electrode configuration (both EEG and invasive), sampling rate, number of seizures, recording duration and dominant seizure pattern. The EEG data were acquired using a Neurofile NT digital video EEG system, while the invasive measurements were obtained with depth, strip or grid electrodes from Ad-Tech. For each patient, three different phase synchronisation indexes, involving four intracranial electrodes, were calculated. In all cases, the three contact pairs have one electrode in common, located in the proximity of the epileptic focus, while the other three electrodes, not necessarily from the same array, were used as reference. These electrodes are identified in Table 2.1 as \#F-\{\#R1, $\# R 2$, \#R3\}, where $\# F$ denotes the electrode at the seizure focus and $\# R x$ denote the references. Prior to the calculation of the synchronisation indexes, records were


Fig. 2.7 (a) Simulated DDA algorithm index and simulated PLV value from recordings at positions M5 and M8 of a $1 \times 8$ EcoG strip implanted in patient FR_1084. Signals were pre-filtered in the $\beta$-band. The input rate of the chip was adjusted to the sample rate of the recordings, i.e., 1024S/s. (b) Correlation between both plots.
band-pass filtered in the frequency bands where higher activities were observed. This gave the selection of $\beta$-band for all patients but patient $\# 4$, for which the $\alpha$-band was most insightful. In the case of patient $\# 10$, the $\beta$ - and $\theta$ bands offered similar results.

### 2.3.1 DDA-PLV correlation

For illustration purposes, 2 examples of the correlation results between the DDA SI index and the PLV can be seen in Figs. 2.7 and 2.8, respectively, the synchronisation results obtained from two recording blocks measured in patient FR_1084 (48 year old female). In both blocks (6h long) three low amplitude fast activity (lafa) seizures were annotated (red dotted lines). For each figure, the plots on the left show the simulated synchronisation index (labeled as "SI") and the calculated PLV value (labeled as "SIM PLV"), while the plots on the right represent the correlation between both measures calculated at the time instants in which the experimental synchronisation indexes were recorded. The $D D A$ algorithm detects all major changes in synchrony and indeed follows a similar trend as the PLV algorithm. This is verified by the high correlation results of approximately $90 \%$ on average.

Figs. 2.7 and 2.8 also show that seizures manifest with a remarkable increase in the synchronisation measures. This feature is in fact on the basis of the detection


Fig. 2.8 (a) Similar as for Fig. 2.7 using the electrodes GA2 and GA5 of a $8 \times 8$ subdural grid implanted in patient FR_1084. (b) Correlation between both plots.
mechanism presented in [52] and [50] in which seizures are detected by applying thresholds on the $P L V$ indicators calculated between pairs of channels.

### 2.3.2 SNR

The simplicity of the $D D A$ circuit comes at the expense of higher susceptibility to noise on the recorded signals as compared to the $P L V$ approach. This is illustrated in Fig. 2.9 which shows the correlation between the ideal $P L V$ values obtained with two noise-free 60 minutes long neural signals, and the synchronisation indexes, derived from the $D D A$ approach, when the same signals are contaminated with white Gaussian noise. The correlation is plotted against the spot Signal-to-Noise Ratio ( $S N R$ ), assuming 1 Hz bandwidth, at the maximum frequency of the $\beta$ band, i.e. 30 Hz . PS estimations are derived on that frequency band as well. Spot $S N R s$ in the range between 10 dB and 70 dB at 5 dB steps have been considered and, for each $S N R$, a Montecarlo analysis (100 instances) has been carried out. The error bars show both the mean value and the $\pm 3 \sigma$ of the synchronisation indexes. It is worth observing that for spot $S N R s$ above 30 dB the average correlation between the $D D A$ approach and the noise-free $P L V$ technique is larger than $90 \%$. Also note that for large $S N R s$, i.e. when the noise contamination is negligible, the correlation is in the order of $95 \%$. This "intrinsic" deviation can be attributed to the structural differences between the $D D A$ and the $P L V$ algorithms. Fig. 2.9 also shows the correlation between the noise-free $P L V$ values and those obtained with a 16-tap Hilbert transformer with passband ripple of


Fig. 2.9 Correlation of the $D D A$ synchronisation index and the $P L V$ processor in [52] with an ideal noise-free $P L V$ calculation when the input signals are contaminated by Gaussian noise.
0.01 dB when input signals are corrupted by noise, following the implementation in [52]. Similar as for the $D D A$ case, performance worsens for $S N R s$ below 20dB.

To assess the impact of the noise behaviour shown in Fig. 2.9, it must be emphasised that surface and intracranial EEG signals exhibit $1 / f^{x}$-like power spectra at low frequencies [58,59]. This makes low frequency bands more tolerant to the aggregated noise contributed by biological tissue, electrodes and recording front-ends [60, 61]. Indeed, it has been shown that even with modest amplifier noise specifications, without suppressing flicker contributions, SNRs larger than 30 dB can be obtained at low frequencies [62]. This suggests that PS calculations can be relevant as a neurological biomarker in the $\beta$ and lower frequency bands although the reliability decreases for the high- $\gamma$ band and higher frequencies. This observation is indeed confirmed in Section 2.3.1, where it is also demonstrated that $D D A$ deviations compared to $P L V$ can be tolerated without sensibly degrading the quality of the results while the $D D A$ approach
offers light and modular hardware implementations, easily scalable to large neural recording arrays.

### 2.3.3 Sensitivity

In order to estimate the sensitivity (number of seizures which are correctly detected divided by the total number of real positive cases) of the $D D A$ and the $P L V$ approaches in terms of the False Positive Rate, $F P R$ (number of wrong positive detections divided by the total number of actual negative events), different thresholds per contact pair and patient have been applied over the corresponding synchronisation indexes. Thresholds for the $D D A$ and the $P L V$ algorithms do not necessarily coincide even if applied on the same electrode pair. Thresholds are obtained by scanning the synchronisation results and identifying the index value leading to a specific $F P R$ performance. To identify each of the 5 thresholds for each individual contact pair and patient the following procedure is enforced. Firstly, by identifying the total length of the resulting $S I$ and $P L V$ values (the length is in hours and does not include the pre, post and ictal periods). Secondly, by multiplying the total hours by the desired $F P R$ we can extract the exact amount of false positives allowed during the resulting $S I$ and $P L V$ values. Since we are looking for peaks (false positives), we then search the $S I$ and $P L V$ values for the top $x$ peaks in descending order. From there, using the last peak from the $x$ peaks selected we set a threshold. The Matlab code for the thresholding can be seen in Appendix B.2.

In our experiment, a detection is produced whenever one out of three synchronisation indexes (or $P L V$ values) rises above their corresponding thresholds. Hence, decisions are taken based on the outcomes from three contact pairs, not just one. Additionally, the following considerations have been adopted [63]. An observation window of 15 min before the annotated seizure has been defined for the detection of true positives. Hence, if a crossing is detected any time within this window, which can be associated to a preictal state, a true seizure detection is accounted for. Further, in order to exclude effects from postictal states, recording periods within 30 min after the onset of a seizure were discarded for threshold calculations. If two successive seizures are separated by less than 45 min , the preictal window before the onset of the following seizure is preserved in the analysis. Fig. 2.11 illustrates a true positive detection identified in patient $\# 7$. In this case, the synchronisation indexes calculated with $D D A$ from the three contact pairs pass their respective thresholds during the preictal period.

Fig. 2.10, shows an example of the full $S I$ index results obtained from patient $\# 7$. The 5 horizontal red lines indicate the different thresholds for each $F P R$ and the vertical red boxes indicate the pre/post and ictal periods. All though the results can be somewhat noisy, it is apparent that there do exist very Strong prominent peaks in synchronisation.

Fig. 2.12 shows the sensitivity variation with respect to $F P R$, averaged over all the 10 patients in Table 2.1, according to the one out of three detection rule described before. Five different $F P R$ values, in units of number of events per hour, have been considered. Both $D D A$ and $P L V$ detectors were analysed. Error bars indicate the $95 \%$ confidence interval limits per method and $F P R$ value. The average detection threshold variation along the $F P R$ range (from 0.15 to $0.75 \mathrm{FP} / \mathrm{hr}$ ) was $8.8 \%$ for $D D A$ and $14.5 \%$ for $P L V$. Table 2.2, shows all of the true positives, false negatives and sensitivity results which where used for the sensitivity analysis.

As can be seen in Fig. 2.12, there are little differences between the two approaches (only $4.6 \%$ sensitivity variation averaged over all $F P R$ ), with $D D A$ slightly outperforming $P L V$ detection, excepting at $0.45 \mathrm{FP} / \mathrm{hr}$ for which both methods obtain similar results. As the constraint is relaxed in terms of $F P R$, it is observed that the sensitivity rises and the confidence levels get tighter. In fact, at $0.75 \mathrm{FP} / \mathrm{hr}, D D A$ achieves an $84 \%$ sensitivity whilst its upper confidence level reaches as much as $92 \%$. These results are comparable to those in [50].

Although results can be hardly generalised, it was observed in the analysis that certain seizure patterns tend to offer better sensitivities than others. In particular, those patients showing low-amplitude, fast activity or rhythmic $\beta$ waves, obtained some $5 \%$ better sensitivity in $\beta$ band. This was observed both for $D D A$ and $P L V$ PS detection.




Table 2.2 DDA and PLV results showing the number of true positives (TP), false negatives (FN) and sensitivity for each of the 10 patients shown above. The $F P R$ rate ranges from 0.15 through to 0.75

| Patient | Metric | DDA |  |  |  |  | PLV |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | FPR | 0.15 | 0.3 | 0.45 | 0.6 | 0.75 | 0.15 | 0.3 | 0.45 | 0.6 | 0.75 |
| \#1 | TP | 4 | 5 | 5 | 6 | 6 | 4 | 4 | 5 | 5 | 5 |
|  | FN | 3 | 2 | 2 | 1 | 1 | 3 | 3 | 2 | 2 | 2 |
|  | Sensitivity | 0.57 | 0.71 | 0.71 | 0.86 | 0.86 | 0.57 | 0.57 | 0.71 | 0.71 | 0.71 |
| \#2 | TP | 7 | 8 | 9 | 9 | 10 | 9 | 10 | 10 | 10 | 10 |
|  | FN | 3 | 2 | 1 | 1 | 0 | 1 | 0 | 0 | 0 | 0 |
|  | Sensitivity | 0.70 | 0.80 | 0.90 | 0.90 | 1.00 | 0.90 | 1.00 | 1.00 | 1.00 | 1.00 |
| \#3 | TP | 2 | 3 | 3 | 3 | 3 | 3 | 3 | 3 | 3 | 3 |
|  | FN | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
|  | Sensitivity | 0.67 | 1.00 | 1.00 | 1.00 | 1.00 | 1.00 | 1.00 | 1.00 | 1.00 | 1.00 |
| \#4 | TP | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 |
|  | FN | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 |
|  | Sensitivity | 0.67 | 0.67 | 0.67 | 0.67 | 0.67 | 0.67 | 0.67 | 0.67 | 0.67 | 0.67 |
| \#5 | TP | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 |
|  | FN | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
|  | Sensitivity | 1.00 | 1.00 | 1.00 | 1.00 | 1.00 | 1.00 | 1.00 | 1.00 | 1.00 | 1.00 |
| \#6 | TP | 4 | 4 | 4 | 4 | 4 | 3 | 3 | 3 | 3 | 3 |
|  | FN | 0 | 0 | 0 | 0 | 0 | 1 | 1 | 1 | 1 | 1 |
|  | Sensitivity | 1.00 | 1.00 | 1.00 | 1.00 | 1.00 | 0.75 | 0.75 | 0.75 | 0.75 | 0.75 |
| \# 7 | TP | 1 | 6 | 6 | 7 | 10 | 0 | 3 | 7 | 8 | 10 |
|  | FN | 11 | 6 | 6 | 5 | 2 | 12 | 9 | 5 | 4 | 2 |
|  | Sensitivity | 0.08 | 0.50 | 0.50 | 0.58 | 0.83 | 0.00 | 0.25 | 0.58 | 0.67 | 0.83 |
| \#8 | TP | 3 | 3 | 3 | 3 | 3 | 2 | 3 | 3 | 3 | 3 |
|  | FN | 4 | 4 | 4 | 4 | 4 | 5 | 4 | 4 | 4 | 4 |
|  | Sensitivity | 0.43 | 0.43 | 0.43 | 0.43 | 0.43 | 0.29 | 0.43 | 0.43 | 0.43 | 0.43 |
| \#9 | TP | 3 | 3 | 3 | 3 | 4 | 1 | 3 | 3 | 3 | 4 |
|  | FN | 1 | 1 | 1 | 1 | 0 | 3 | 1 | 1 | 1 | 0 |
|  | Sensitivity | 0.75 | 0.75 | 0.75 | 0.75 | 1.00 | 0.25 | 0.75 | 0.75 | 0.75 | 1.00 |
| \#10 | TP | 5 | 5 | 6 | 7 | 7 | 1 | 6 | 7 | 7 | 7 |
|  | FN | 5 | 5 | 4 | 3 | 3 | 9 | 4 | 3 | 3 | 3 |
|  | Sensitivity | 0.50 | 0.50 | 0.60 | 0.70 | 0.70 | 0.10 | 0.60 | 0.70 | 0.70 | 0.70 |



Fig. 2.11 Zoom synchronisation indexes for patient \#7 during a clinically annotated seizure and pre/post ictal padding at a false positive rate of 0.15 per hour. (a) Pair TBA1-HRA4, (b) pair TBA1-HRA5, (c) pair TBA1-TBA2.


Fig. 2.12 Average Sensitivity against $F P R$ for DDA +SI and PLV + HT including $95 \%$ confidence analysis obtained via 1803.2 hours of recordings and 61 annotated seizures.

### 2.4 Conclusions

In this chapter, a hardware friendly algorithm for the detection of phase synchronisation has been introduced. The algorithm achieves a very high absolute sensitivity of approximately $80 \%$ for an FPR of $0.75 \mathrm{FP} / \mathrm{h}$. Indeed, it produces an absolute sensitivity of close to $90 \%$ at $0.75 \mathrm{FP} / \mathrm{h}$ at the upper bound of the $95 \%$ confidence levels. The effect of noise has also been assesed which shows for SNR values greater than 30dB the algorithm performs almost perfectly with over $90 \%$ correlation to an ideal PLV. The correlation between other proven methods of phase detection has been assessed giving on average a $90 \%$ correlation to the PLV.

## Chapter 3

## Synchronisation Processor

The contributions in this chapter includes the design, implementation and verification of a sub-threshold phase synchronisation processor capable of calculating 'phase synchronisation between two neural signals. The processors design and verification process was firstly implemented in an FPGA environment and RTL compiler, later the design was implemented manually in the CADENCE layout environment.

All of the design and verification processes were carried out by the author of this thesis.

### 3.1 Overview

The synchronisation processor is based on the measurement of time periods between two consecutive minima as described in section 2 . The simplicity of the approach allows for the use of elementary digital blocks, such as registers, counters or adders. In fact, the processor, fabricated in a $0.18 \mu \mathrm{~m}$ CMOS process, only occupies $0.05 \mathrm{~mm}^{2}$ and consumes 15 nW from a 0.5 V supply voltage at a signal input rate of $1024 \mathrm{~S} / \mathrm{s}$. These low-area and low-power features make the proposed processor a valuable computing element in closed-loop neural prosthesis for the treatment of neural disorders, such as epilepsy, or for measuring functional connectivity maps between different recording sites in the brain.

The ASIC uses circuit elements from a full-custom digital library for 0.5 V power supply operation, based on low-leakage transistors in weak inversion. The library blocks were generally designed using conventional CMOS logic, with device dimensions close to minimum size, as they were found to offer an acceptable trade-off between power dissipation and operating frequency [64]. Indeed, the library was exhaustively verified and characterised under PVT deviations assuming a maximum clock frequency of 25 kHz , i.e., about twice the operation frequency needed by the I/O ports of the ASIC. In spite of the reduced noise margin and the slow switching transitions, postlayout simulations of the chip showed complete functionality with no data loss for 0.5 V operation.

The implemented ASIC is competitive when compared to currently available FDA approved devices and other state-of-the-art devices such as described in chapter 1.6. The small size and power consumption allows for increased scalability, allowing for more EEG data streams to be incorporated, leading to an increase in sensitivity
when compared to more complex algorithmic structures such as the HT and PLV combination.

Based on the algorithmic design from chapter 2, An overview of the system can be seen in Fig. 3.1. The design consists of 5 main layers. Firstly the minimum detection layer, which is used for the identification of the quasi-periodic local minima as denoted by $t_{n}$ from equation 2.1, in each given neural signal denoted s1 and s2 for neural signal 1 and neural signal 2, respectively. The Timestamp layer is the practical identification of the phase/frequency increase between two consecutive local minima within a given signal i.e $T_{n}^{s}$ from equation 2.1. The third and most complex layer is the calculation layer, which is responsible for calculating the difference in samples between consecutive minima in the two signals, such that we get the relative error $\triangle T_{n}=\left|T_{i}^{1}-T_{j}^{2}\right|$. The calculation block is also responsible for the accumulation of these errors such that $S d d a(k)=\sum_{n=0}^{K-1} \triangle T_{n}$. The filtering layer is used for the smoothing of $S d d a(k)$, leading to more interoperable data and easier to set thresholds at the output of the device. The final, detect layer, is a test platform for setting epileptic alarm thresholds.

### 3.2 Design

The following section describes each of the 5 layers in-depth including examples. Appendix C.1, provides a pseudo code of the hardware flow for the design.

### 3.2.1 Minimum detection

From Fig. 3.1, The minimum detection architecture consists of two identical subsystems, one for neural data stream $S 1$ and the second for neural data stream $S 2$.

In order to reduce hardware utilisation and minimise power consumption, the minimum detection scheme introduces a simple yet robust toggling architecture.

To begin, each subsystem is comprised of a 10-b most significant bit comparator which, compares two samples, $S(i)$ and $S(i-1)$, corresponding to the signals current sample and previous sample respectively. Where $S(i-1)$ is delayed 1 clock cycle via a 10-b register. If $S(i)$ is smaller than $S(i-1)$, then, a logic 0 is produced such that the result from the comparison is, $C=0$. Contrarily, if the opposite is true then a logic 1 is produced such that $C=1$. In the final case that $S(i)=S(i-1)$, then $C=C$, i.e there is no change in the output. Nevertheless, the final scenario is unlikely to occur


Fig. 3.1 Synchronisation processor: Block diagram of the main blocks used for the design of the synchronisation processor. This design consists of 5 main layers and incorporates a non complex architecture structure
if the sampling rate of the system is sparse enough. To reduce hardware utilisation and power consumption, the MSB comparator first compares the 5 most significant bits of $S(i)$ and $S(i-1)$. If a solution is found then the result $C$ is produced else the comparator moves on to the lower 5 bits for comparison. In general $C$ is given as:

$$
C=\left\{\begin{array}{rrr}
0 & \text { for } & S(i)<S(i-1) \\
1 & \text { for } & S(i)>S(i-1) \\
C & \text { for } & S(i)=S(i-1)
\end{array}\right.
$$

The value of $C$ gives an indication as to whether, at the current sample in time, the signal is traversing in a downwards fashion or in an upwards fashion. Additionally, to achieve a more robust system, a 10-b $M$ shift left register was implemented which records the signals history over the past 10 values of $C$. The result from this register $O$, is outputted every clock cycle with the newly updated word.

In the case that the shift left registers output is $O=0000011111$, it becomes evident that at some point during the signals history, it moved in a downward trend followed by an upward trend. This indicates that at points $O(6)=0$ and $O(5)=1$, there was a local minimum $t_{n}$. Fig. 3.2, shows this concept.

This simple architecture is hardware friendly, nevertheless, as described in section 2 subsection 2.3.2 the noisy nature of neural data and the possibility of random fluctuations can produce false positives in detection out the output.

Therefore, to increase robustness of the minimum detection system, bubble detection logic, as seen in Fig 3.2, is used. This small piece of logic relaxes the strict rule of $O$, by allowing for one outlier $(Q)$ either side of the values $O(6)=0$ and $O(5)=1$, such that a detection $M 1=1$, of a local minimum is confirmed if any single value in $O(9: 6)=1$ or any single value in $O(4: 0)=0$. However, the values $O(6)=0$ and $O(5)=1$ must be true in any of the cases.

### 3.2.2 Time stamp

The time stamp layer relies heavily on a single 10-b up counter. Whose, main purpose is to count upwards with time between two consecutive minima within a signal, hence discovering $T_{n}^{s}$. This gives a good understanding of the instantaneous frequency of the signal at that given point in time.


Fig. 3.2 Minima detection logic (left) and example of bubble detector(right). The example shows an example of a real EEG data stream pre filtered into the beta band. Here we can note that the first minimum in the signal is detected as $O=0000011111$. As for the second minimum it is also detected due to the relaxed outlier condition such that $O=0100011111$

In the case that a minimum is detected, M1 activates a 10-b array of reading logic gates which are implemented as standard 2 input AND gates and the current value in the up counter $C o(9: 0)$ is passed into a $10-\mathrm{b}$ latch and stored. simultaneously, since a new minimum has been detected the counter is reset and it once again begins its count towards the next minimum in the signal.

### 3.2.3 Calculation

The architecture of the calculation layer starts with a signed 10-b subtracter with one-bit overflow. This is used to calculate the difference $\triangle T_{n}=\left|T_{i}^{1}-T_{j}^{2}\right|$, between the two signals detected minima. The subtracter runs continuously subtracting values every cycle. However, since the algorithm simplifies the calculations to a minima detection basis only, rather than a sample by sample basis, a small piece of extra logic is needed.

This logic comes in the form of two 1 bit latches and a logic AND gate. Once $T_{n}^{1}$ has been detected in $S 1$ the logic value of $M 1$ gets latched. This indicates that $S 1$, is ready for the calculation stage, Similarly, $M 2$, is latched if $T_{n}^{2}$ is detected in $S 2$.

If $M 1=M 2=1$, then a signal is sent to read logic block situated at the output of the previous latching stage. This allows the values from both of the counter modules to be subtracted. Simultaneously the small piece of logic resets the latches holding M1 and $M 2$ such that the output is now of logic state 0 . In terms of the read logic if they are inactive then the output of the read logic is a constant logic 0 , for all $10-\mathrm{b}$.

Therefore, although the subtracter is in continuous operation, when no relevant data is ready for calculation it will simply subtract $0-0$. Since non-switching is necessary for this specific case, the dynamic power consumption of the subtracter during non-crucial data is almost null and only consumes static power.

The initial subtraction can create two different outputs at $S u b(9: 0)$, firstly, if $L 1(9: 0)>L 2(9: 0)$, then the result will be a positive unsigned 10-b result. However, in the reverse case that $L(9: 0)<L 2(9: 0)$, a 2 's complement negative result is produced. In this case, the MSB (the eleventh bit of the subtracter(S)), is set to 1 indicating the result is negative. Since the algorithm desires $\left|\triangle T_{n}\right|$, the 2's complement result needs converting back to standard unsigned notation. To achieve this the design incorporates an array of 10 bit XOR gates which perform the logic conversion to 1's complement and a full adder adds 1 to $\operatorname{Sub}(9: 0)$ producing $\operatorname{Abs}(9: 0)$.

The next stage requires the accumulation of errors for the value of $S d d a(k)$, This is achieved using a 10-b add and accumulate block, where the window size $K$, consists of a variable up counter with a maximum size of 2048 samples. When the window counter is less than its maximum value. $\operatorname{Adderout}(9: 0)$, consistently calculates $\operatorname{Abs}(9: 0)+\operatorname{feed}(9: 0)$, However, once again, since $\operatorname{Abs}(9: 0)$, is only non zero when relevant data is available the resulting sum is $0+f e e d(9: 0)$, which requires no switching.

Once the counter reaches its maximum value. A pulse is generated which resets the feedback register in the accumulator creating a zero-sum, at which point read logic at the output of the accumulator captures $S d d a(k)=\phi(i)$ and is passed to the post-processing stage for smoothing. This happens every $K$ samples and avoids irrelevant data being passed into the next stage.

### 3.2.4 Filter

Due to fast fluctuations of $\phi(i)$ at the processors output, the detection of high and low values of $\phi(i)$, becomes troublesome. To counteract this problem an unconventional exponential filter was adopted, which is based on an autoregressive IIR filter. Mainly used for time series, the filter acts as a low pass filter and provides a substantial amount smoothing with very little cost in terms of hardware. the basic equation for the exponential filter is given by:

$$
\begin{equation*}
y(i)=\alpha \cdot \phi(i)+(1-\alpha) \cdot y(i-1) \tag{3.1}
\end{equation*}
$$

Where, $y(i)$, is the new filtered value, $\phi(i)$, is the new incoming value (in this case new synchronisation value $S d d a(k)), y(i-1)$, is the previously filtered value, and $\alpha$, is a weighting for the function, also known as a smoothing factor.

At this point, it is clear to see that this function produces an approximation of what the next value in the sequence should be, based solely on the current synchronisation value and the previously filtered value. This is why only currently relevant data can be passed into the filter, otherwise, its predictions will be erratic.

The smoothing factor, can be set such that $0 \leq \alpha \leq 1$, where a $\alpha=1$ provides no smoothing, hence $y(i)=\phi(i)$, and $\alpha=0$, provides maximum smoothing.

At first glance, the terms $\alpha \cdot \phi(i)$ and $(1-\alpha) \cdot y(i-1)$, may seem complicated leading to floating point multiplication. However, re-writing the formula we get the equation:

$$
\begin{equation*}
y(i)=y(i-1)-y(i-1) \cdot \alpha+\phi(i) \cdot \alpha \tag{3.2}
\end{equation*}
$$

By choosing, $\alpha$, such that it is always a power of 2 , we can replace $\alpha$, with $2^{\text {pos }}$ such that:

$$
\begin{equation*}
y(i)=y(i-1)-y(i-1) \cdot 2^{\text {pos }}+\phi(i) \cdot 2^{\text {pos }} \tag{3.3}
\end{equation*}
$$

Where pos, is an integer value. Since a bit shift right, results in a division, a drastic hardware reduction can be made. This approach limits our range of smoothing, nevertheless, for the generalised purpose of smoothing $\phi(i)$, it is sufficient. As an example, if pos is set to 1 , then that would correspond to:

$$
\begin{equation*}
y(i)=y(i-1)-\frac{y(i-1)}{2}+\frac{\phi(i)}{2} \tag{3.4}
\end{equation*}
$$

It is also important to note that since the filter relies heavily on its previous value, if $y(i)$, is initially set to one, a certain time frame must pass before stabilisation.

Fig.3.3, shows the basic architecture of this block. Firstly, a 10-b shift right register, which is externally adjustable to provide the smoothing factor and a 10-b full subtracter are used to calculate $y(i-1)-y(i-1) \cdot 2^{\text {pos }}$. Secondly, a 10-b shift right register is used to calculate $\phi(i) . \alpha$, which is added to $y(i-1)-y(i-1) \cdot \alpha$, via a full adder to produce the final value of $y(i)$.



Fig. 3.3 Block diagram of the implemented exponential filter with variable smoothing capabilities (left). Filters magnitude response (right)

### 3.2.5 Detect

The detection block was designed for the detection of large changes in synchronisation. Namely, this would prove useful for such neurological disorders as epilepsy. In which large changes in synchronisation occur during different periods before, during and after the event. it is important, to stress the fact that since $S d d a(k)$, is now effectively equal to $\sum_{n=0}^{K-1} \triangle T_{n}$, then a large drop in synchronisation is equivalent to better synchrony, whilst the opposite is true increases in $S d d a(k)$. Therefore if $\phi(i)<T h h$, then an alarm is triggered indicating there has been a significant increase in synchrony, contrarily if $\phi(i)$ $>T h l$, an active high alarm is triggered indicating a significant reduction in synchrony. This is performed by 210 bit comparators. Nonetheless, due to the inherent noisy output, 2 small counters of 4 bits are also placed in the detect block. These counters place the constraint that Thl and Thh, must be active for a set number of consecutive outputs. This diminishes the possibility of false positive detections. This block relies heavily on the previous filtering stage such that insufficient smoothing can increase the number of false detections. Thl, Thh and the set number of consecutive outputs are all injected into the device from an outside source and are not set dynamically within. This gives more control for testing.

### 3.3 Methods

The hardware implementation of the test was built and verified at several keys stages via various platforms.

### 3.3.1 Design flow

## FPGA implementation and verification

The digital design was firstly realised in the VIVADO design environment using a VHDL. After successful simulation of the design within the environment, it was later synthesised and downloaded onto a XILINX ARTIX 7 AC701xc7a200tfbg676-2 evaluation board. For ease of testing, a hardware Co-Simulation of the DDA algorithm was ran through the MATLAB DSP SIMULINK environment along with a MATLAB based calculation of the HT and PLV index.

Fig.3.7, shows an overview of the top-level RTL compiled schematic from the VHDL code. This consists of 4 main blocks. Firstly, the synchronisation processor as described above (a view of the synchronisation processor blocks can be seen in Fig. 3.8).

Secondly, the SPI interface, which used to convert serial input streams to parallel data for the processor. The SPI has 3 main inputs 'datain1', 'datain2' and 'loadparameters'. The first two inputs convert neural signals 1 and 2, from a 1-b binary serial stream into a 10-b parallel unsigned binary sample. Since the processor requires $2 \times 10-\mathrm{b}$ unsigned parallel data at the input (1x10-b for each signal), the conversion of 'datain1' and 'datain2' are made via a $2 \times 10$ shift registers which operates 10 times faster than the core clock. Due to the 10 times increase in speed for the datain SPI interface the 'datain1' and 'datain2' samples from the SPI are latched at the output until 1 clock cycle of the main processor is complete. The final input 'loadparameters', allows for all of the static variables of 'K', 'Thh', 'Thl', '2 $2^{\text {pos }}$ ' and others, to be uploaded via a single binary stream. This allows us to reduce the total number of PADS used in the ASIC implementation, hence, reducing overall area consumption of the final design.

The third block, 'Check parameters', was used as a test strategy in order to verify that all of the uploaded variables were correct. This, block simply re-downloads the data sent onto the chip for verification.

Lastly, the PSI interface is the download link for the data generated by the synchronisation processor. Similar to the SPI interface this block is used to reduce area consumption of the device. Nevertheless, this block works in the opposite fashion converting parallel data streams into a single serial data stream. Assuming a clock frequency of approximatley 1024 Hz operating frequency for the main processor this output PSI can run at the standard processor frequency.

Fig. 3.4, shows an example of how 'loadparameters' and the data stream 'datain1' are uploaded in a serial fashion and ultimately re-downloaded and checked via 'Parameter check' and 'checkdatal'.

Fig. 3.5, shows the minima detected by the system for signals S1 and S2. Here we can see that there exists a delay between the actual minimum and the detection pulse (the delay is indicated by the blue box). This delay exists because we need to gather 10 samples of history before an accurate decision can be made. Nevertheless, this delay in no way disturbs the systems ability to calculate phase as the exact same delay is present in both signals. Furthermore, we can see that no minima were detected during the section of signal encompassed in the red boxes. This is due to the outlier logic described previously which correctly dismisses these very small dips for minima.

Fig. 3.6, shows an example of the output $\phi(i)$ using a filtering of $\alpha=1$ and two detection thresholds $T h h=170$ and $T h l=590$. During the simulation 1 drop in synchrony was detected (i.e when $\phi(i)>T h l$ 'dropdetected' $=1$ ) and one increase in synchrony (i.e when $\phi(i)<T h h$ 'risedetected' $=1$ ) (both of which are highlighted by blue boxes). There do exist false positive at the beginning of the output due to the time needed for the filter to build reliable data.

## RTL compiler verification

In the second phase of the design, the VHDL code was implemented using the RTL compiler from CADENCE (An example of the RTL compiler script used to build the RTL schematic can be seen in Appendix B.4. This compiler maps all of the logic gates from the synthesised FPGA design to a specific technology in this case $0.18 \mu \mathrm{~m}$. The RTL compiler delivers a complete schematic of the design at the register level. Once obtained the schematic is then uploaded to the CADENCE environment and simulated for error detection. If the design produces errors, certain attributes and optimisations can be enforced in the RTL compiler and re-simulated as per needed.

1
Fig. 3.4 VHDL simulation showing the uploading of parameters and data stream S1 along with the download verification 'Parameters check'

Fig. 3.5 VHDL simulation showing the minima detection of a small section of EEG recording for S1 and S2

Fig. 3.6 VHDL simulation showing the results for phi for real EEG data and the detection




Fig. 3.9 Layout view of the 2-channel 0.5 V synchronisation processor from CADENCE

## CADENCE layout

Fig 3.9, shows the circuit layout from the CADENCE design environment. Due to a sub-threshold operating voltage the design was implemented via a manual layout approach. The design was fully tested using extracted layouts including parasitic components.

### 3.4 Discussion

### 3.4.1 Indexing

The synchronisation index from equation 2.2 described in section 2, is a construct related to the comparative studies of the algorithm and is not actually needed to produce results of synchrony for a patient. In the previous sections the index was used mainly to emphasise the fact that the results obtained follow a similar pattern to that of more complex algorithms. Actually, the SI index is a form of scaling and does not change the results at the output. By omitting this from the hardware implementation. A drastic reduction in hardware can be achieved.

### 3.4.2 Minimum detection scheme

This overall detection scheme was chosen for several specific reasons, Firstly, due to the quasi-periodic nature and variations in the neural data, it is not guaranteed that a local minimum will have specific identifiers such as a zero crossing point. This means that it is imperative to follow the history of the signal as it moves forward in time.

Secondly, the toggling system was chosen to reduce hardware utilisation. In many systems which do not use a zero crossing identifier. There is a need to record the previous x samples and x future samples of the signal. This can lead to large memory allocations. The use of the outlier logic omits these memories.

The outlier logic in this design was set to a static 1 each side of the switching point. This was set to 1 as observations of many band limited signals there exist only small perturbations.

### 3.4.3 Filtering

Standard low pass filtering and smoothing such as the moving average filter use the averaging of multiple points in a signal to derive a single output. Defined as:

$$
y(i)=\frac{1}{M} \sum_{j=0}^{M-1} \phi[i+j]
$$

Where M, represents the total number of points to average, i.e, the window size for the filter. In single-sided averaging, when $j=0$, the moving average filter sufferers from lag as a new result is only produced every M samples. In hardware, this would be implemented with an accumulator for the addition of samples and a shift right register if $M$ is set to a power of 2 . Nevertheless, for sensitive systems such as the detection of epilepsy, new and reliable data is needed fast to increase the reliability of detection.

Another alternative is that of the two sided moving average window, set such that $j=\frac{-(M-1)}{2}$ to $j=\frac{(M-1)}{2}$. This method reduces latencies, however increases hardware resources due to temporary storage of $j=\frac{-(M-1)}{2}$.

The exponential filter avoids the problems of lag and storage, by utilising only the current and previous sample, where more importance is placed on the new value.

We should also point out that although the filter is of an exponential origin, the 10 -bit resolution is sufficient as the filter can never overflow, instead, it can only produce a maximum value of 1024 . Such that: $y(i)=1024-\frac{1024}{x}+\frac{1024}{x}=1024$

### 3.4.4 Power/Accuracy trade-off

The power consumption of the chip and its performance largely depends on the sampling frequency of the input signals. The slower the sampling rate, the lower the number of operations per second carried out by the chip and, hence, the lower the power consumption. However, the accuracy achievable on the calculation of transition periods decreases and the overall performance of the DDA algorithm degrades. On the other hand, for high sampling rates, the performance improves at the cost of higher power dissipation. This is illustrated in Fig. 3.10, which shows the power consumption of the chip in terms of the sampling frequency, assuming that both input signals are band-limited in the $\beta$ band. In the same plot, the correlation between the measured synchronisation index and the PLV value (calculated off-chip with the same input signals) is represented as a measure of the DDA approach accuracy. It is worth noting that beyond a given sampling rate of about $2-3 \mathrm{kS} / \mathrm{s}$, no further improvement can be observed in the chip performance as the correlation states around $85 \%$. Hence, a sampling rate of $2 \mathrm{kS} / \mathrm{s}$ is chosen for which the power consumption of the chip core is 15 nW from a 0.5 V supply voltage. Similar trade-offs can be observed for other frequency bands.


Fig. 3.10 Power/sampling frequency trade off overview

### 3.4.5 Resource allocation

Fig. 3.11, gives an impression of the hardware reductions which can be obtained by the DDA algorithm. the DDA algorithm can be calculated using as little as 37 slices, 112 flip-flops and 60 LUT(Look-Up Tables), excluding SPI interface, PSI interface and CHECK PARAMETERS. Which is significantly less than other systems, HT1[65] and HT2[66], which both utilize a Hilbert transform based filter and CORDIC arctan phase extraction system. The mean number of resources needed to calculate the discrete distances (DDA approach) is 69.6, which is almost $95 \%$ less than system 1 (1348) and almost $96.8 \%$ less than system 2 (2149).

Resource allocation comparison


Fig. 3.11 Bar chart showing the FPGA resource allocation for the designed DDA algorithm and two other FPGA based implementations of the Hilbert transform and Cordic PLV values


Fig. 3.12 Circuit layout fabricated in a $0.18 \mu \mathrm{~m}$ CMOS process and occupies an active area of $0.05 \mathrm{~mm}^{2}$ (left) adn dedicated PCB testing platform (right)


Fig. 3.13 Laboratory functional test setup, showing the logic analyser, power supply and the laptop used to transfer data files.

### 3.5 Experimental results

Fig. 3.12 shows a microphotograph of the chip implementing the $D D A$ algorithm. The chip has been fabricated in a $0.18 \mu \mathrm{~m}$ CMOS process and occupies an active


Fig. 3.14 Illustration of the system response versus supply voltage for two input tones at 25 and 30 Hz .
area of $0.05 \mathrm{~mm}^{2}$ including the main processor core, two series-to-parallel input (SPI) ports, one parallel-to-series output (PSO) port and some additional buffers for testing intermediate nodes. The I/O ports work 10 times faster than the rest of the ASIC in agreement with the $10-\mathrm{b}$ resolution used for the input signal samples. The total number of integrated gates is 6053.

Fig. 3.13 shows the test setup used for functional verification. The chip was mounted on a dedicated PCB together with a set of adjustable level shifters and regulators for scaling the logic levels and supply voltage of the ASIC. Firstly, Low voltage operation was experimentally verified by driving the chip with different tones in the $\beta$ band and comparing the generated synchronisation index stream with electrical and behavioural simulations. A logic analyser (Agilent 16823A) was used for synthesising the tones, sampled at $1024 \mathrm{~S} / \mathrm{s}$, and for serially retrieving binary information from the output and
other test points of the ASIC through a pod connector. For two tones at 25 and 30 Hz (100k samples each), deviations from the ideal synchronisation index were noticeable for supply voltages below 0.35 V . At this point, the index starts to drop and, for 0.2 V supply, the system breaks down completely with no observed activity. The reset signal generated in the ASIC after and-ing the latched outputs of the two minima logic blocks (see Fig. 3.1) was also monitored along this transition. This signal goes high every time a transition period is computed. For supply voltages above 0.35 V , the train generated by the ASIC is quite regular (only minor variations due to the quantisation of the inputs) in good agreement with the expected response, however, pulses are eventually missed below 0.35 V and, at 0.2 V supply, they are no longer observable.

Electrical simulations show that this behaviour is compatible with data transfer failures from the SPI input ports of the ASIC. This is illustrated in Fig. 3.14 which plots: (i) the experimentally observed degradation of the synchronisation index as the supply voltage decreases according to $S_{\text {meas }} / S_{i d}$, where $S_{\text {meas }}$ and $S_{i d}$ denote, respectively, the measured and ideal values of the index and, (ii) the simulated SPI register position, normalised to the vector resolution, at which input data fails to be shifted. In both cases, 1 indicates no error while 0 means complete breakdown. It is worth observing the good agreement between both curves. Similar behaviour was obtained for other tones in the $\beta$ band.

At a signal input rate of $1024 \mathrm{~S} / \mathrm{s}$ and 0.5 V supply voltage, the power consumption of the chip core is 15 nW . Table 3.1 shows the power budget of the chip. Event detection and time stamp calculations by the finite state machine are the two most power demanding tasks of the processor due to the higher switching activity. Table 3.2 shows the normalised performance of the ASIC compared to other designs in Table 1.3. Variables have been normalised to a single channel and, in the case of core area occupation, an additional normalisation has been applied by arbitrarily assuming all chips are fabricated in CMOS 65nm. Accordingly, the original area per channel has been scaled by $\left(65 \mathrm{~nm} / W_{\text {min }}\right)^{2}$, where $W_{\text {min }}$ is the feature size of the fabrication technology. Note that the proposed implementation exhibits the smallest normalised area and it is among the designs with lower energy consumption.

### 3.5.1 Experimental Setup with Neural Recordings

The processor has been also verified and validated using neural recording data available in the European Epilepsy database [57]. This database contains recordings of over

Table 3.1 Power breakdown of the synchronisation processor based on the blocks in Fig.3.1

| Block | Average Power (nW) |
| :---: | :---: |
| Event detection | 4.01 |
| Finite state machine | 4.52 |
| Counter | 1.46 |
| Indexing | 2.64 |
| Filtering | 2.86 |

Table 3.2 Normalised performance summary

|  | Norm. area <br> $\left(\mathrm{mm}^{2} / \mathrm{ch}\right)$ | Power <br> $(\mu \mathrm{W} / \mathrm{ch})$ | Energy <br> $(\mathrm{pJ} / \mathrm{ch} / \mathrm{bit})$ |
| :---: | :---: | :---: | :---: |
| $[49]$ | 0.0073 | 6.25 | 108 |
| $[50]$ | 0.0050 | 4.06 | NA |
| $[51]$ | 0.0043 | 49.22 | NA |
| $[48]$ | 0.0184 | 0.23 | 0.36 |
| $[52]$ | 0.0223 | 51 | 3.75 k |
| $[53]$ | 0.0047 | 0.15 | 63.5 |
| $[55]$ | 0.5320 | 57.3 | 14 k |
| This work | 0.0033 | 0.0075 | 0.73 |

275 patients including 225 scalp recordings and 50 intracranial recordings. As very long recording sessions, often lasting for more than 6 h , are included in the database, a specific experimental set-up has been devised. As shown in Fig. 3.15, it uses an mbed LPC1768 MCU based on a 32-bit ARM ${ }^{\circledR}$ Cortex $^{\mathrm{TM}}$-M3 core from NXP Semiconductors. The test platform has been expanded with an application board which includes an RJ45 Ethernet connector and a USB-A Host/Device port (in addition to the built-in USB drag'n'drop FLASH programmer). The MCU defines settings and transmits driving stimuli to the $D D A$ chip through the available GPIO ports and other I/O interfaces. Neural input signals are stored as CSV files in a 32 GB Fat-32 formatted stick memory plugged into the USB-A port of the test platform. These files are sequentially read by the MCU and serially transmitted to the SPI ports of the ASIC. Long testing sessions have been run uninterruptedly using this setup with no need to split the database recordings into smaller blocks (this would clear the internal states of the


Fig. 3.15 Test setup showing the ASIC mounted on a dedicated PCB, mbed LPC1768 micro controller and dedicated level shifters.

ASIC). The synchronisation index generated by the chip is transferred back to the MCU and steered through the USB port to a host computer where data are further analysed with MATLAB ${ }^{\circledR}$.

The C++ code to send data from the MBED device to the ASIC and retrieve data from the ASIC can be seen in appendix B.5.

Neural recording signals from the database have to be pre-processed prior to being used as stimuli in the described platform. This involves the following steps: (i) bandpassfiltering for selecting the frequency band of interest (fourth-order Butterworth filters have been used), (ii) resampling for matching the frequency rates of the recordings and the ASIC (only if needed), (iii) adding noise for a given input-referred SNR value, (iv) digitising the samples to the resolution of the ASIC (10-b), and (v) casting data in CSV format files for storing in the stick memory. As mentioned, files as large as 10GB have been handled without any observed problem.


Fig. 3.16 Experimental synchronisation index and simulated PLV value from recordings at positions M5 and M8 of a $1 \times 8$ EcoG strip implanted in patient 1 . Signals were pre-filtered in the $\beta$-band. The input rate of the chip was adjusted to the sample rate of the recordings, i.e., $1024 \mathrm{~S} / \mathrm{s}$. The $S_{d d a}$ curve (labeled "ASIC SI") was obtained at a sample rate of $1 \mathrm{~S} / \mathrm{s}$.

### 3.5.2 Epilepsy Detection Results

Different blocks of intracranial data from the referred database were used for assessing the epilepsy detection capabilities of the $D D A$ chip. These blocks were selected for their high confirmed seizure rate. No other consideration was taken into account. For each block, signals were first pre-filtered in MATLAB ${ }^{\circledR}$ into conventional neuro-physiological bands. After a preliminary computer analysis of the records, the frequency band with the largest synchronisation index activity was finally selected. For each experiment, the set of valid values were plotted alongside with the theoretical $P L V$ value obtained through the Hilbert Transform method.

For illustration purposes, Fig. 3.16 shows the synchronisation results obtained from two channels of a recording block measured in a 48 years old, female patient. In this block, one low amplitude fast activity (lafa) seizure was annotated (dotted line). Before driving the ASIC, Gaussian noise were added to the signals for a spot SNR of 30 dB at 30 Hz . The plot shows the experimental synchronisation index (labeled as "ASIC SI") and the calculated $P L V$ value (labeled as "SIM PLV"). The $D D A$ algorithm detects all major changes in synchrony and, indeed, follows a similar trend as the $P L V$ algorithm.

This is verified by the high correlation measure of approximately $91 \%$ (in line with Fig. 2.9) .

Fig. 3.16 also shows that the seizure manifests with a remarkable increase in the synchronisation measures. This feature is in fact on the basis of the detection mechanism presented in [52] and [50] in which seizures are detected by applying thresholds on the PLV indicators calculated between pairs of channels. In some cases, as in Fig. 3.16, seizures are preceded by a sudden drop in synchronisation [67], however, we have not verified this feature in all the analysed blocks.

### 3.5.3 Functional Connectivity Results

The proposed $D D A$ prototype has been also used for estimating functional brain connectivity. As in the previous section, chip results were later compared with computer simulations of the Hilbert Transform approach with PLV indexing. Recordings from patient \#7 have been considered. This patient suffers from simple and complex partial seizures originated from temporal lobe. Among the recordings, a block including one rhythmic $\beta$ wave episode has been analyzed. This has been the only aspect taken into account for the selection.

To assess the functional connectivity strength between neural assemblies, a mapping approach has been followed in which synchronisation indexes for every possible electrode combination at a given observation window were arranged into a symmetric matrix. A 1h long recording block including inter-ictal, pre-ictal, ictal and post-ictal periods was examined. Signals were band-pass filtered in the $\beta$ band.

Both EEG and ECoG recordings are available from patient \#7, however, only the results from EEG analysis are herein presented. The EEG recordings consisted of 16 EEG captures selected from a standard 10:20 system. The resulting 120 pairwise combinations were arranged in a $16 \times 16$ matrix. For easy visualisation, index values were colour-coded between yellow (index close to 1 ) and dark blue (no coupling).

Figure 3.17 shows the connectivity maps obtained through the Hilbert Transform (first column) and the $D D A$ chip (second column) for observation windows in the four mentioned time segments. Both sets are clearly correlated as verified by the absolute differences between the two methods (third column). This is particularly noticeable during the ictal stage (first row), where the difference across all neural combinations is almost null. This shows that for high values of synchronisation, $D D A$ retains the detectability of high synchronisation changes when compared to other more
complex algorithms. For smaller synchrony levels, as occurs in the pre-ictal, post-ictal and inter-ictal periods, the variations between both methods become a little more pronounced. That said, the biggest difference can be seen in the post-ictal period (third row) between electrodes T3-F8 at approximately $10 \%$.

Similar conclusions were drawn from the analysis of ECoG maps on the same recording block (not shown). Good correlation between both approaches was also observed. Nevertheless, it was noticed an overall increase in synchrony for all the observation windows. This is consistent with the closer proximity of ECoG electrodes compared to surface electrodes. In any case, the ictal-period was still clearly identifiable.

Next, we analysed the graph theoretical metrics as described in Appendix A. Using non-directional, un-weighted binary matrices were the thresholds were set for each individual partition. To maintain consistency each threshold was set as $25 \%$ less than the maximum swing between the maximum and minimum respective values, such that: Threshold $_{\text {partition }}=\max -\frac{\text { max-min }}{4}$.

In order to calculate the small world metric we introduce a comparison between the inter-ictal and ictal periods. Notably, we use the graph metrics from the inter-ictal period as a random reconnection of the ictal period such that $\lambda=\frac{C_{\text {ictal }}}{C_{\text {inter-ictal }}}$ and $\gamma=\frac{L_{i c t a l}}{L_{\text {inter-ictal }}}$. Conversely, for the inter-ictal period $\lambda=\frac{C_{\text {inter-ictal }}}{C_{\text {ictal }}}$ and $\gamma=\frac{L_{\text {inter-ictal }}}{L_{\text {ictal }}}$.

Fig.3.18, shows the various average graph theoretical metrics over the ictal and inter-ictal partitions. As expected the average nodal degree and clustering increases substantially during the ictal period. Conversely, the average path length drops over the ictal period. This indicates an overall more heavily synchronised and connected network, as can be seen in the ictal connectivity graph. Fig. 3.18, also shows that the ictal partition tends towards a higher small world connectivity than the inter-ictal period. Nevertheless, this highly connected ictal period as compared to the inter-ictal period indicates a mass synchrony between multiple nodes. In a normal brain network, however, these characteristics can be considered undesirable as neural clusters should operate with a certain degree of independence and not oscillate at the same frequencies.

Further analysis, was made for patient \#7 in terms of the variance in nodal degrees and clustering coefficients. Using, 'topoplots' in the form of colour graded contour plots projected onto a 2D representation of the brain.

Fig. 3.19, show the variance of these metrics for patient \#7. Over the ictal period, there exists a high nodal degree towards the right temporal lobe which would indicate higher connectivity from other nodes to this area. This is indeed consistent with the
clinical prognosis for this patients type of epilepsy. Nevertheless, The clustering during the ictal period tends to shift to the left hemisphere, indicating that although the right temporal lobe is heavily connected during this period the connections tend to be longer range and less clustered than the left hemisphere, Nevertheless they remain high at approximately 0.6 . Over the next three periods, noticeable reductions in nodal degree in the right temporal lobe can be seen, indicating that this area actually has a lower connectivity than other regions. In fact, a reduction in both the inter-ictal and pre-ictal periods accounts for an approximate $23 \%$ reduction from in the epileptic event time. Interestingly, the highest connectivity during the non-ictal period shifts towards the P4 parietal electrode which is consistent with the correlation colour maps seen in Fig. 3.17.

Another interesting, characteristic for this patient is the reduction in clustering during the pre-ictal period, indicating a sudden drop in clustering around the epileptic centre before the ictal event is triggered.

Once again the gathered DDA data shown in the plots was compared with that of the PLV and HT method for a comparative visual aid. In all cases, the two algorithms show a strong correlation with all shifts in clustering and nodal degrees trending towards the same pattern.

In conclusion, the ictal period proves itself to evolve from a non-hyper synchronous network to a hypersynchronous network. Where the epileptic event originates from one point of origin and incorporates new clusters into the firing process. This is indicated by the short path lengths, meaning that long-range synchrony does not necessarily take place, instead, the synchrony evolves from one cluster to another. On the contrary, during the inter-ictal period, long rage synchrony is more apparent and the average nodal degree is low.


Fig. 3.17 EEG connectivity maps for patient \#7. Columns 1 through 2 are colour maps representing the mean values for both the $P L V$ and $D D A$ for all possible combinations of EEG signals. Column 3, shows the absolute difference between columns 1 and 2. EEG data were organised into a standard 10-20 format.


Fig. 3.18 Graph theoretical results for patient\#7. Row 1, shows the average metrics for both the PLV and DDA approach over both the ictal and inter-ictal periods. Row 2 , shows the functional connectivity representation of the brain using a standard 10-20 EEG electrode set-up for both the ictal and inter-ictal partitions. The blue solid line represents the connectivity of the PLV value and the dashed red line represents the connectivity of the DDA approach

Fig. 3.19 Graph theoretical coloured contour maps for patient 442012 during each partition period ictal,inter-ictal,pre-ictal and post-ictal. Where each row shows both the variance of nodal degree and clustering for both the PLV and DDA approaches.

### 3.6 Conclusion

A dedicated processor, fabricated in a $0.18 \mu \mathrm{~m}$ CMOS process, has been proposed for the estimation of phase synchronisation between neural signals. It obtains similar results as those achievable with more computationally demanding algorithms, but it consumes much less power and it is highly scalable. This makes the proposal suitable for parallel multi-channel phase synchronisation calculations on-chip.

In some sense, the proposed algorithm can be regarded as an inexact computing paradigm [68] in which a small amount of errors can be tolerated, without sensibly degrading the quality of results, but attaining considerable efficiency gains.

Although the processor performance has been demonstrated for surface and intracranial EEG signals, its usage can be extended to other scenarios where a low-cost, low-complexity, programmable and portable solution for computing functional connectivity is needed as, for instance, in functional magnetic resonance imaging (fMRI) or positron emission tomography (PET).

## Chapter 4

## Multi-channel synchronisation processor

The contributions in this section include the design, implementation and verification of a sub-threshold phase mass integrated phase 16 -channel VLSI synchronisation processor capable of calculating 'phase synchronisation between 9 independent neural signals and 120 neural combinations. The processors design and verification process was firstly implemented in an FPGA environment for architecture verification, later the design was implemented manually in the CADENCE layout environment and verified through simulation.

All of the design and verification processes were carried out by the author of this thesis.

### 4.1 Overview

This design was implemented with a multi-functional purpose in mind, firstly, as a clinical aid for the identification of pathological brain states, by monitoring and mapping synchronisation features of patients using graph theory. Secondly, as a dedicated epileptic seizure diagnosis tool.

The ASIC was designed in an AMS $0.18 \mu m$ high voltage, low leakage technology using a fully custom 0.5 v threshold digital logic library to reduce total power consumption and operates from a main clock frequency of 2 KHz .

Incorporated into the design are 16, individual synchronisation processors (15 on-line processors and 1 test processor) each with a dedicated training and calculation module, used to build a specialised epileptic detection system based on patient-specific synchrony thresholds. Each of the 15 main synchronisation processor are based on the previously verified synchronisation processor in section 3 and are capable of calculating the phase synchrony between 9 independent EEG signals over 8 epochs of time totalling 120 EEG combinations. Furthermore, two SPI interfaces are incorporated for ease of communication to $3^{\text {rd }}$ party devices.

To optimise area, the processors were organised into an array of 4X4 of processors $(\mathrm{P})$ and training and calculation modules ( T ), this is illustrated in Fig. 4.1. In addition, an independent control logic unit was implemented for each row of the array.

The last processor in the array was used as a test processor which was implemented completely independently from the other array.

The final VLSI implmented design can be seen in Fig 4.2. The core area of the design occupies only $3.64 \mathrm{~mm}^{2}$, whilst the SPI input interface occupies $0.091 \mathrm{~mm}^{2}$ and the output interface occupies $0.063 \mathrm{~mm}^{2}$. Each synchronisation processor occupies $0.04 \mathrm{~mm}^{2}$ (This is less than the original processor described in section 3, due to a reduction in control logic) and consumed on average 12-15nW (Simulated power estimation), whilst, each training and calculation module occupies $0.066 \mathrm{~mm}^{2}$.


Fig. 4.1 Top level matrix layout for the 16 synchronisation processors and associated training and calculation modules


Fig. 4.2 Microscopic view of 16-Channel ASIC

### 4.2 Design

### 4.2.1 Input conversion SPI

A single 1 to 160 -b serial to parallel converter is used at the input of the ASIC to convert a single 1 bit EEG data stream into a $16 \times 10$ bit array of neural data. Where each 10-b of data represents a single sample from every 16 channels of data. Fig. 4.3 shows a block diagram of the converter which is made up of three distinct layers. Firstly, a concatenated serial array of D-type flip-flops are interconnected via their inputs and outputs, where the input of the $n^{\text {th }}$ flip-flop is connected to the output of the $(n-1)^{\text {th }}$ flip-flop for a total of 160 flip-flops. Since each neural data stream sample consists of 10 unsigned bits, the converter can translate 1 sample for each neural data stream over a total of 160 clock cycles. The serial data stream is feed into the input of the converter as the least significant bit first. Once 160 cycles are complete, the data is shifted out of the registers in parallel, which then gets stored into an individual latch for each bit of data (i.e there are 160 1-b latches). This latching is necessary as the clock of the input converter (Clk2) is running 160 times faster than the main clock of the circuit (Clk), the latching system is therefore used to hold the data in place for 1
complete cycle of the main Clk. This way, the initial registers can continue loading the next samples, while the previous sample is held stable.

Finally, the latched data is pushed into an individual buffer for each data bit, in order to drive the logic 1 values high and pull the logic 0 values low. This is a crucial part of the system as the long conversion dissipates power every cycle, leading to a diminished voltage. The new data samples are then pushed onto a 160 -b bus which interconnects all of the processors.

The serial interface is beneficial for interfacing the ASIC with $3^{r d}$ party hardware platforms such as FPGAs and reduces overall area consumption from 160 individual inputs.

### 4.2.2 Output conversion PSI

The output converter is a 160 to 1 bit parallel to serial converter and is used at the output to capture synchronisation values from the 15 main processors. Fig. 4.4 shows a block diagram of the converter. The architecture consists solely of a concatenated array of D-type flip-flops and a single buffer at the output. An enable line is activated every time new synchronisation values are ready, which tells the converter to accept the data at its input. If no new values are available the converter blocks new inputs and starts shifting the values out of the registers. The long period between updated synchronisation values means that this converter can run using the master clock of the circuit.



### 4.2.3 Epoch selection

Using 16 main electrodes, a combinational total of 120 neural combinations need to be assessed. Normally, this would lead to a large array of 120 synchronisation processors, where each processor is capable of handling two data streams. To combat this, we use a custom epoch based multiplexing of neural data to reduce the array of processors from 120 down to just 15.

The 'epoch', on which the method is based, can be considered as a small time segment window, where 1 epoch lasts for a total window size of x samples. The actual time of the window is dependent on the sampling frequency of the master clock, however, for argument's sake, let's assume for now that it is set to a standard sampling rate of 1024 S .

During an epoch, each processor will receive 1024 samples from any two given neural data streams. Therefore, during 1 epoch the 15 processors can calculate the correlation between 15 neural data combinations. In order to reach the total of 120 combinations, 8 epochs are required.

The epoch system, therefore, reduces the number of processors from 120 to 15, at the cost of losing small amounts of data between epoch cycles. In terms of samples, this means that each neural data combination will get updated every 8192 samples or in terms of time every 8 seconds.

The tradeoff between data loss and realistic implantation schemes is questionable. Nevertheless, it is clear that as a diagnostic tool for pathological brain states such as Alzheimers, Parkinsons or schizophrenia, the need for constant data monitoring is unnecessary. Mainly due to the constant and stable change or deterioration in the neural network. That's to say, the instability in the neural network does not change rapidly or fluctuate from a better to a worse state or visa versa. In epilepsy, however, abrupt rapid changes in the neural network are the most common attribute. A paper by et. al Sigmund Jenssen [69], reports that on average a Tonic seizures last for a median time of 18.5 seconds, simple partial seizures last for 28 seconds, primary generalised tonic-clonic seizures lasted approximately 66 seconds and complex partial seizures lasted for as long as 78 seconds. From these results, it is clear that an 8 -second refresh rate for neural synchronisation values is sufficient. In the fastest seizures of 18.5 seconds there would be a minimum of two attempts at detection of the epileptic event and in the slowest seizures, there would be almost 10 attempts at identification.

| Processor | Epoch 1 | Epoch 2 | Epoch 3 | Epoch 4 | Epoch 5 | Epoch 6 | Epoch 7 | Epoch 8 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 1 | 1,2 | 1,3 | 1,4 | 1,5 | 1,6 | 1,7 | 1,8 | 1,9 |
| 2 | 2,3 | 2,4 | 2,5 | 2,6 | 2,7 | 2,8 | 2,9 | 2,10 |
| 3 | 3,4 | 3,5 | 3,6 | 3,7 | 3,8 | 3,9 | 3,10 | 3,11 |
| 4 | 4,5 | 4,6 | 4,7 | 4,8 | 4,9 | 4,10 | 4,11 | 4,12 |
| 5 | 5,6 | 5,7 | 5,8 | 5,9 | 5,10 | 5,11 | 5,12 | 5,13 |
| 6 | 6,7 | 6,8 | 6,9 | 6,10 | 6,11 | 6,12 | 6,13 | 6,14 |
| 7 | 7,8 | 7,9 | 7,10 | 7,11 | 7,12 | 7,13 | 7,14 | 7,15 |
| 8 | 8,9 | 8,10 | 8,11 | 8,12 | 8,13 | 8,14 | 8,15 | 8,16 |
| 9 | 9,10 | 9,11 | 9,12 | 9,13 | 9,14 | 9,15 | 9,16 | 10,1 |
| 10 | 10,11 | 10,12 | 10,13 | 10,14 | 10,15 | 10,16 | 11,1 | 11,2 |
| 11 | 11,12 | 11,13 | 11,14 | 11,15 | 11,16 | 12,1 | 12,2 | 12,3 |
| 12 | 12,13 | 12,14 | 12,15 | 12,16 | 13,1 | 13,2 | 13,3 | 13,4 |
| 13 | 13,14 | 13,15 | 13,16 | 14,1 | 14,2 | 14,3 | 14,4 | 14,5 |
| 14 | 14,15 | 14,16 | 15,1 | 15,2 | 15,3 | 15,4 | 15,5 | 15,6 |
| 15 | 15,16 | 16,1 | 16,2 | 16,3 | 16,4 | 16,5 | 16,6 | 16,7 |

Table 4.1 Table showing which neural data streams are connected to specific processor during each of the 8 epochs of time

Table 4.1, shows a grid of the neural signals being computed for each processor during any given epoch. As an example processor 1 (P1), calculates the synchrony between neural data channels, [1-2,1-3,1-4,1-5,1-6,1-7,1-8,1-9] at epochs 1 through 8 respectively. Whilst processor 15 (P15), calculates the synchrony between [15-16,16-1,16-2,16-3,16-4,16-5,16-6,16-7].

### 4.2.4 Window, epoch and memory addressing logic

Structurally speaking, the control logic for the entire system is simple and consists of basic logic gates and counters. Firstly, as can be seen in Fig. 4.5 (Window counter), the window logic consists of a simple 10-b up counter with self-reset. This counts from 0 to 1024, when the maximum of 1024 is reached a single clock cycle positive pulse ' K ' is created. From observations in the previous design discussed in chapter 3, a fixed window of 1024 was chosen. This allows for a reduction in hardware and power consumption by omitting the variable shifting aspect.

The epoch selection of the neural signal inputs and addressing of memory elements is driven by a 3 bit up counter, built from D-type flip-flops as seen in Fig. 4.5 (Epoch selection and memory addressing logic). Where the output of each flip-flop is hard-wired to 8 distinct 3 input AND gates in combinations which create an up sequence ranging from 1 through 8 (a1 through a8). The counter has an enable line connected to ' K ',
hence the counter only counts up once ' $K$ ' is introduced. Contrarily, when ' $K$ ' is low, the counter is paused in its current state meaning that the count is kept constant until the next ' K '. This combination allows us to produce logic high signals of exactly 1024 samples long. Using the hard-wired AND gates at the output has the advantage of hardware reduction over ring counters as a reduction of five D-type flip-flops can be introduced. The long pulses of a1 through a8 are used as a reference for the current epoch as well as address memory locations, which will be described later. Fig. 4.5 shows a basic timing diagram, where the 1024 sample pulses of a1 through a8 rotate continuously. In the zoomed view of a1, we can see how a single cycled pulse of 'K' activates the epoch a1.


Fig. 4.5 Dedicated control logic for the window length, epoch selection and memory addressing.

### 4.2.5 Flow

From Fig. 4.6, we can see an overview of the hardware implemented for processor 1 (P1) (all 15 processors are identical). Firstly, during any given epoch, 2 of the 9 possible channels of parallel neural data are multiplexed into the synchronisation processor as per, table 4.1. During epoch 1 signals S1 and S2 are evaluated, the phase error between these two signals is then continuously monitored and updated until the window has finished $(\mathrm{K}=1)$ producing a phase value $\phi_{\text {epoch } 1}$. Simultaneously, the Epoch has increased to 2, hence new data streams S1 and S3 are feed into the
synchronisation processor for assessment. Working as a pipelined system $\phi_{\text {epoch } 2}$, is now being processed whilst $\phi_{\text {epoch } 1}$ continues to be post-processed. In general $\phi_{\text {epoch(n) }}$, is always being processed whilst $\phi_{\text {epoch }(n-1)}$, is always being post-processed.
$\phi_{\text {epoch } 1}$, is then passed into a dedicated custom low pass filter and stored in a custom dedicated memory for future retrieval. After filtering, $\phi_{\text {epoch } 1}$, is then passed to a dedicated training and calculation module which uses the values of synchrony to produce patient-specific epileptic detection and graph theoretical thresholds for online epileptic detection and offline graph analysis respectively.

The dedicated thresholds are then used as a comparison in a detection block which compares new synchrony values to determine whether a rise or fall in a patient's specific synchrony values has occurred.


Fig. 4.6 Overview of the 16 -channel processors control and flow

### 4.2.6 Neural multiplexing

To accommodate all 120 neural data combinations over 8 epochs of time, each processor must manage the phase calculations of 9 independent neural combinations. In order to minimise the large area occupation enforced by standard multiplexing schemes, our design incorporates a non-conventional hard-wiring via tristate buffers.

Fig. 4.7 shows the basic hard-wiring technique. Where select processor input channels are connected via a multi-dimensional $8 \times 10$ array of tristate buffers. Each of the 8 rows of 10 tristate buffers connects to an individual neural data stream of $10-\mathrm{b}$, which all have a dedicated enable line connected to a specific epoch. This allows us to connect 8, 10-b neural data streams to a single bus.

When a current epoch is active (a1 through a8, see section 4.2.4), the output of that given tristate array is set to low impedance, Hence, the data can pass onto the main line and feed into the synchronisation processor unimpeded. Contrarily, when an epoch is not active the output is set to a state of high impedance $(Z)$, meaning that the neural data is blocked from passing onto the main line.

From Table. 4.1, for synchronisation processors 1 through 8, the first channel is always hard connected to neural data streams 1 through 8 , respectively. Whilst channel 2, is connected to each processor's dedicated tristate array. As an example in Fig. 4.7, channel 1 (Ch1) of processor 1, is hard-wired to the neural data stream 1 (D1), whilst channel 2 (Ch2), is connected to the tristate array, the first row in the array is connected to neural data stream 2 (D2), the second row to neural data stream 3 (D3) and so on until the $8^{t h}$ row, which is connected to neural data stream 9 (D9).

Synchronisation processors 9 through 15 incorporate an extra 2-row tristate array at channel 1 . As per table 4.5 , eventually the input at channel 1 will have to change, however, this is not a uniform process so a small piece of distinct logic is added to control the switching of these tristate rows. As an example during epoch 8 of processor 9, the Ch1 input will need to switch from D9 to D10. To achieve this a simple inverter is added to the enable line of the first row, such that if epoch 8 is not active then neural data D9 can flow into Ch1, else D10 is allowed to pass unimpeded. The additional logic for each of the processors 10 through 15 can be seen in Fig.4.7.

The timing diagram shows the currently active rows for processors 1 and 9 during epochs 1 (highlighted in green) and 8 (highlighted in blue).


Fig. 4.7 Example of the neural input multiplexing scheme and dedicated control logic. The top figures show how tristate buffer arrays are used to control 8 separate neural streams to one processor. The bottom figures shows the extra control logic needed in order to control the first input channel

### 4.2.7 Post processing

The epoch based method chosen means that temporary variables and data need to be stored for future access. The exponential filtering is an example of this, where the original low pass filtered $\phi(i)$, from Fig. 3.3 of section 3.2.4 in chapter 3:

Now needs to store the previous value of $y(i)$ for each epoch, until a full rotation of the signals has been complete. The equation can then be expressed as:

$$
y(i)^{(P)}=y(i-1)_{\text {epochx }}^{(P)}-y(i-1)_{\text {epochx }}^{(P)} \cdot 2^{\text {pos }}+\phi(i)_{\text {epochx }}^{(P)} \cdot 2^{\text {pos }}
$$

Were $y(i-1)_{\text {epochx }}$, represents the previously stored filtered value for that current epoch and P , represents the processor.

From herein, we will omit the term epochx and $(P)$ for clarity of reading, hence we assume that all further references are indicative of all 15 processors and epochs

Since each processor manages multiple neural data streams, a dedicated $8 \times 10$ memory, which is illustrated in Fig. 4.8 (a), is used to store the previous values of $y(i-1)$, until the epoch selection module makes a full round and returns back to the chosen epoch. The memory itself consists of a 10x8 array of D-type latches all interconnected at the output via tristate buffers (T1 through T8) onto a single 10-b bus. This allows for both the read and write operations to be carried out simultaneously. The latching of the data to the correct address requires a single cycle positive pulse in this case 'a1Lf' through 'a8Lf'. Which are activated by 'anding' the current epoch with the single cycled window pulse of ' $K$ ' as illustrated in Fig. 4.8 (b). Once the new data is latched to the correct address, the output of the memory is read constantly throughout the life of each individual epoch via epoch selection signals a1 through a8.

Fig. 4.8 (c), shows an overview of the hardware requirements for such a filter. Which is similar to the hardware described in from Fig. 3.3 of section 3.2.4 in chapter 3. Nevertheless, by assuming a constant value of pos, in this case, pos $=2$ a reduction of two 10-b shift registers can be omitted by hard wiring the shift into the dedicated hardware. Firstly, a 10-b subtracter calculates $y(i-1)-y(i-1) \cdot 2^{\text {pos }}$ (collected from memory), where, $y(i-1) \cdot 2^{p o s}$ is hard-wired to the subtracter by taking the most significant bits from 10 down to 2 and grounding out the first 2 most significant bits and concatenating bits 10 to 2 in position 8 down to 1

The result from the subtracter, is then added to $\phi(i) \cdot 2^{p o s}$ (once again hard-wired), using a 10-b adder to create the final result $y(i)$, which is simultaneously passed on to the next stage and stored into memory as $y(i-1)$.


Fig. 4.8 Adapted exponential filter from processor 1, using a hard-wired smoothing factor and memory array

### 4.2.8 Training and Thresholds overview

It is well known that there are a wide variety of different forms of epilepsy which can produce different varying quantities of synchrony between different regions. Additionally, each and every patient will produce varying amounts of synchrony due to the uniqueness of every brain. These variations make it difficult to set reliable static thresholds for epileptic detection as seen in Fig. 3.6 of section 3.2.5 in chapter 3, where the thresholds were set based on pre simulation. Therefore, in this design, a patient-specific epileptic threshold calculator was implemented.

To begin, an initial training phase is set, such that 2 separate arrays are built, 1 containing the maximum filtered synchronisation values and the other the minimum values, from each processor at each epoch (i.e the maximum and minimum filtered values for each neural data combination).

In an ideal situation, the training period would be performed during a patient's epileptic episodes by clinical specialists. The arrays, give an accurate starting point for
the patient's pathological synchronisation state. Once training is complete, the data accumulated is then used to set a patient specific low and high threshold voltage such that:

$$
\begin{gather*}
T h h=\max (y(i))-\Delta  \tag{4.1}\\
T h l=\min (y(i))+\Delta \tag{4.2}
\end{gather*}
$$

Where, $p$, is the processor in question and $\Delta$ is a margin calculated as the voltage swing between the maximum and minimum values stored in the array divided by a constant such that::

$$
\begin{equation*}
\Delta=[\max (y(i))-\min (y(i))] \cdot \frac{1}{2^{n}} \tag{4.3}
\end{equation*}
$$

A threshold low (Thl) is set to produce alerts when the patient synchrony levels are increasing towards the maximum recorded value in the array, warning the patient to a possible upcoming episode. The threshold high (Thh) is set as a diagnostic tool to track a possible upcoming epileptic seizure.

The time for an accurate array to be built depends greatly on the patient and the amount of successfully induced episodes recorded. Take for example a patient who, did not reach a positive seizure state during the training period, this patients Thh and Thl thresholds will not give an accurate gauge of his/her hypersensitive network detection.

This dynamic approach to thresholds gives rise to several advantages over fixed threshold based architectures. Firstly, since the thresholds are based from a patient's specific source, the thresholds are dynamically adjusted to account for a synchronisation offset which may occur from patient to patient. Secondly, In the fixed threshold hold based algorithmic designs a normalization between 0 and 1 is usually applied. This makes setting the thresholds easier, however, the thresholds are still susceptible to large error margins due to offsets of patient-specific synchrony.

The dynamic thresholds also provide an all-important feature towards the graph theoretical analysis. The complexity of threshold setting for the binary adjacent matrices (see appendix A for definition of graph theory), usually leads researches to handle multiple data sets at varying thresholds.

It is pertinent to point out that, these dynamic thresholds can be recalibrated at any moment in time. This may be desirable to change when different frequency bands are being evaluated, due to synchrony baseline offsets.

The architecture can be seen in Fig. 4.9. In order to minimise hardware utilisation, a combination of multi-purpose/reusable, $8 x 10$ D-type latch memories are used for the 2 arrays, in combination with a 10-bit subtracter, several hard-wired tristate arrays, twin MSB comparators and control logic.

## Training

1. During the initial set up of the device, a small initialisation period is set (Inital $=1$ ). This allows for the low memory $M e m L$, which will ultimately store the low thresholds Thl to be loaded with a logic level 1 and the high memory MemH which will ultimately store the high thresholds $T h h$, to be preloaded with a logic level 0 . The initial period lasts for a total round of epochs from 1 to 8 , hence lasts approximately $8 \cdot 1024$ samples in order to fully initialise the memories.
2. Once complete, the training period is set (Train $=1$ ). In this case, the twin comparators are activated, one of which, compares the newly filtered synchronisation value $y(i)$, with the currently stored value in the memory MemL. If $y(i)$ is less than that in the memory it overwrites the current value in memory location MemL by activating the tristate array T6, if false tristate array T7 is activated which rewires the output of the memory back to the input. Conversely, the second comparator checks to see whether $y(i)$ is greater than the current value in the memory MemH , if true tristate array T3 is activated, allowing for the new data to overwrite the data in location MemH , otherwise, tristate array T 1 is activated re-storing the current value of MemH .

Over a designated period of time, the memory arrays will slowly build the lowest and highest recorded values. We should note, that we initially pre-set the memories to 0 and 1, for memories high and low respectively, hence the probability that all values in the memories will initially be overwritten is high.

When a suitable amount of data has successfully been gathered for the patient in question the true thresholds $T h l$ and $T h h$, can be calculated.

| Stage | MemL | MemH |
| :---: | :---: | :---: |
| Inital | $\operatorname{Min}(y(i))$ | $\operatorname{Max}(y(i))$ |
| Stage1 | $\Delta$ | MemH |
| Stage2 | $\Delta$ | Thh |
| Stage3 | Thh $-2 \Delta$ | Thh |

Table 4.2 Table showing the memory allocation during calculation phase of the patient specific thresholds

## Calculation

In order to reduce area occupation, we re-utilise the high and low memories and pipeline information. The calculations of the thresholds occur over three master clock cycles per epoch, these stages are named S1, S2 and S3. The information during each stage can be seen in table 4.2.

The stages are controlled via a simple 4 stage ring counter as seen in Fig. 4.10, where the fourth stage is a delay element needed for synchronising internal signals of the device. The memories in the training module are latched via a1L through a8L, the logic for latching can be seen in Fig. 4.10 and depends on the multiple stages being accessed.

1. Firstly, during S1, the value of $\Delta$, is calculated, by activating T8 and subtracting the maximum and minimum values from training, hence making the calculation MemH - MemL. T4 is then activated which is a hard-wired tristate buffer array which mimics a shift left of $2^{2}$, to create a final division by 4 , to create $\Delta$ which is then stored in MemL. T1 is activated for MemH keeping it constant.
2. During stage $\mathrm{S} 2, \mathrm{Th}$, is calculated and stored in MemH , by calculating $\mathrm{MemH}-$ $(\Delta)$. In this case T2 and T8 is activate for memory MemH and T 7 is activated for memory $M e m L$, in order to preserve $\Delta$.
3. Finally, during stage S 3 , $T h l$ is calculated. In order to minimise hardware, we forgo the use of an additional adder which would normally be required to calculate equation 4.2 and re-utilise the subtracter such that $T h l=T h h-2 \cdot \Delta$. Where, tristate T5 are activated to push the subtraction to memory MemL and T9 is activated to perform a hard-wired shift right of $2^{1}$, i.e, a multiplication of 2 . The high memory maintains its value of Thh, once again by activating T1.

The processes of calculation run through all 8 epochs, hence lasting approximately $3 \cdot 1024$, samples. Once, the calculation mode has finished, a stable mode of synchronisation values can begin. At this point, the write enable to MemL and MemH , are disabled in favour of read-only mode via the epoch selection signals a1 through a8.



Fig. 4.10 Dedicated control logic overview for memory latching

## Detection

The thresholds $T h l$ and $T h h$ held in the two memories are then feed into the first terminal of two 10 bit comparators $C_{l}$ and $C_{h}$ at each given epoch respectively. At the same time, the most current synchronisation value $\phi(i)$ is feed into the two comparators.

Comparator $C_{l}$ checks if $\phi(i)<T h l$ and $C_{h}$ checks if $\phi(i)>$ Thl.

### 4.3 FPGA Implementation

In order to design the circuit in a VLSI environment, the design was first implemented and verified in the VIVADO design suit and eventually passed on to the ARTIC 7 FPGA used in section 3.3.1. An elaborated schematic view of the design can be seen in Fig. 4.11, which shows block diagrams of the tristate multiplexing arrays as well as the 15 synchronisation processors. To be architectural correct, the inputs and outputs
of the design incorporated an SPI and PSI, respectively. Whilst, Fig. 4.12 shows a schematic of the inner blocks which make up a single synchronisation processor, which are largely the same as in Fig. 3.8 in chapter 3, with the addition of the 3 memories and a training and calculation module.

Fig. 4.13, shows a VHDL simulation of the basic control unit signals a1 through a8, as well as the preloading of the high and low memory modules for training and calculation.

Fig. 4.14, Shows a VHDL simulation example of the threshold calculations. In this case the highlighted circles in red represent the calculation of $\operatorname{Thh}(1)$ and $\operatorname{Thl}(1)$. Firstly, when the training is turned of and the calculation signal goes high. $\max (y(i))=292$ and $\min (y(i))=18$. In this case n , from equation 4.3 is set to 2 , hence we get:

$$
\Delta=[292-18] \cdot \frac{1}{4}=68
$$

which represents a quarter of the maximum voltage swing. Calculating Thh and $T h l$ from here is easy.

$$
\begin{gathered}
\text { Thh }=292-68=224 \\
\text { Thl }=224-2 \cdot 68=88
\end{gathered}
$$

Fig. 4.15 shows an example of how the resulting outputs of the design change over various epochs for all of the 15 main processors. In this case, each vertical line represents the accumulated results gathered by the synchronisation processor during 1 epoch, where each consecutive line, represents epoch +1 . To test the full range of possible combinations for the synchronisation processors, 16 synthetic signals were created. Each signal had a fixed sampling frequency of $1024 \mathrm{~S} / \mathrm{s}$, all odd numbered signals were assigned an increasing frequency chirp starting from the range 26 to 51 Hz , and increasing by 1 every following signal. All of the even channels, however, were assigned a fixed sine wave of 37 Hz .

As an example the signals introduced into processor P1 can be seen in table 4.3. Referring to table 4.1, we know that processor 1 receives signal combinations [1-2,1-3,1-4,1-5,1-6,1-7,1-8,1-9], over epochs 1 through 8 respectively.

Therefore, we can see a distinct triangular shaped output (identified by the red line) as the chirps of the odd signals converge towards the tone frequency $(37 \mathrm{~Hz})$ of the stationary even signals. This effect can be seen in all processors, however, the tone


Fig. 4.11 Array of 15 synchronisation processors synthesised using VHDL code



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Fig. 4.13 Simulation of the basic control logic and threshold memory storage




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Fig. 4.14 Simulation of the basic calculation stage

| Signal (P1) | Static or chirp | frequency range |
| :---: | :---: | :---: |
| 1 | chirp | $26-51 \mathrm{~Hz}$ |
| 2 | static | 37 Hz |
| 3 | chirp | $27-52 \mathrm{~Hz}$ |
| 4 | static | 37 Hz |
| 5 | chirp | $28-53 \mathrm{~Hz}$ |
| 6 | static | 37 Hz |
| 7 | chirp | $29-54 \mathrm{~Hz}$ |
| 8 | static | 37 Hz |
| 9 | chirp | $30-55 \mathrm{~Hz}$ |

Table 4.3 Table showing the signals for processor 1 during VHDL simulation of 16channel design

| Resource | Utilisation |
| :--- | :---: |
| LUT's as logic | $4035(3 \%)$ |
| Register as Flip Flop | $4418(2 \%)$ |
| Input/output | $25(9 \%)$ |
| Clocking | $2(6 \%)$ |

Table 4.4 Table showing all design resource allocation for the DDA hardware implementation.
frequencies converge at an earlier stage as the processors get higher due to the odd chirp signals increasing in frequency the higher the signal number.

As another example the first result for epoch 1 is 292 which corresponds to the synchronisation results for $\mathrm{S} 1(26 \mathrm{~Hz})$ and $\mathrm{S} 2(37 \mathrm{~Hz})$, since their frequencies are distant from one another we get a large value at the output. However, during epoch 2 signals $1(26 \mathrm{~Hz})$ and $3(27 \mathrm{~Hz})$ are compared hence producing a small value of 43 .

Table 4.4, shows the resources used in the FPGA implementation of the 16 -channel synchronisation processor.

Fig. 4.15 Output results from VHDL simulation of 16-channel processor

### 4.4 Conclusions

In this chapter a 16 -channel VLSI phase synchronisation processor was implemented The design only occupies $3.64 \mathrm{~mm}^{2}$. Due to a change in the MPW policy of the selected foundry, AMS AG, regarding its $0.18 \mu \mathrm{~m}$ CMOS process, the processor was received 13 months after the tape-out and finally it was not tested. Nevertheless, the design has been fully verified in an FPGA environment.

## Chapter 5

## Conclusions

### 5.1 Conclusions

In this thesis a new algorithm and synchronisation index for the detection of phase synchronisation between neural signals has been introduced. The algorithm shows a high correlation of approximately $90 \%$ when compared to more complex transformbased methods with only a slight decrease on noise performance. In addition, an exhaustive sensitivity analysis with human neural recordings shows that the algorithm produces average values of over $80 \%$ for FPR values of 0.6 and 0.75 .

Two VLSI phase synchronisation processors have been introduced.
The first circuit, implemented with a custom 0.5 V subthreshold digital library in a $0.18 \mu \mathrm{~m}$ standard CMOS process, allows for the detection of phase synchronisation between two independent neural signals. The circuit occupies just $0.05 \mathrm{~mm}^{2}$, including SPI AND PSO interfaces. The design consumes on average 15 nW of power at 2 KHz operating frequency which has been proven to be much lower than current state-of-the-art. In fact, when normalised to a 65 nW technology, the design consumes just $0.0075 \mu \mathrm{~W}$ per channel. That is a remarkable 20 times less power.

The functionality of the prototype has been extensively tested with neural recordings from an epilepsy database and its correct operation demonstrated both in seizure detection tasks and functional connectivity computation.

The second multi-channel processor, using the same library and technology node as above, is capable of calculating phase synchrony between 16 independent neural signals. The circuit occupies $3.64 \mathrm{~mm}^{2}$ in total and incorporates novel patient-specific training and on-the-fly seizure detection mechanisms. The design has been implemented in FPGA and shows very small resource allocations of just above 4000 LUTs and 4400 registers.

En esta tesis se ha introducido un nuevo algoritmo e índice de sincronización para la detección de la sincronización de fase entre señales neuronales.

Los resultados del algoritmo propuesto mostraron una alta correlación de aproximadamente el $90 \%$ en comparación con el método PLV basado en la transformación más complejo.

También se demostró que cuando se realizó un análisis de SNR de ruido puntual en el algoritmo, se produjeron valores de correlación con una señal ideal libre de ruido superior a $90 \%$ para valores de SNR de 25 a 70 dB . Esto es solo un poco más bajo que el del método más complejo de HT + PLV.

Además, un fuerte análisis de sensibilidad absoluta mostró que el algoritmo produjo valores promedio de más del $80 \%$ para valores de FPR de 0,6 y 0,75 . Increíblemente, se demostró que el algoritmo DDA superó el método más complejo de HT + PLV en todos los valores de FPR.

Además, se han introducido dos procesadores de sincronización de fase implementados por VLSI. El primero de ellos permitió detectar la sincronización de fase entre 2 señales neuronales independientes y tenía una frecuencia de operación principal de 2 KHz. El VLSI se implementó utilizando una biblioteca digital por debajo del umbral de 0.5 V y una tecnología estándar de $0.18 \mu \mathrm{~m}$.

La implementación de FPGA del diseño mostró que el diseño usaba hasta un $90 \%$ menos de recursos de FPGA en comparación con otras 2 implementaciones avanzadas.

El VLSI ocupaba solo $0.05 \mathrm{~mm}^{2}$ que incluía interfaces SPI Y PSO. Además, cuando se normalizó en torno a una tecnología de 65 nm , el diseño ocupó solo $0,0033 \mathrm{~mm}^{2}$ por canal, que es 1,5 veces más pequeño que el diseño más pequeño del estado de la técnica.

El diseño consumió un promedio de 15 nW de potencia a 2 KHz de frecuencia de funcionamiento, que se ha demostrado que es mucho más bajo que el estado actual de la técnica; de hecho, cuando se normaliza a una tecnología de 65 nW , el diseño consume solo $0,0075 \mu \mathrm{~W}$ por canal. Eso es un notable 20 veces menos poder. Además, a través de una prueba de laboratorio, se demostró que el diseño puede operar tan solo a 0.3 voltios antes de que la corrupción de datos comience a infringir el circuito.

Los resultados tomados de la implementación VLSI a través de la configuración de prueba de laboratorio mostraron que el ASIC estaba funcionando correctamente, lo que se indica por un aumento repentino en la sincronización justo después del inicio de la crisis. Esto fue respaldado por la simulación del método HT + PLV que muestra un patrón muy similar.

Además, el análisis estadístico mostró altos aumentos en la sincronía alrededor del evento epiléptico en términos de conectividad funcional y análisis teórico de gráficos.

El segundo procesador multicanal fue capaz de calcular la sincronía de fase entre 16 señales neuronales independientes. Una vez más, se implementó utilizando una biblioteca digital por debajo del umbral de 0.5 V y una tecnología estándar de $0.18 \mu \mathrm{~m}$.

El VLSI ocupó $3,64 \mathrm{~mm}^{2}$ en total e incorpora el entrenamiento específico del paciente y el umbral de cálculo, así como la detección de la mosca.

Los umbrales específicos del paciente son de última generación y no se han integrado hasta este punto.

El diseño se implementó en FPGA y mostró asignaciones de recursos muy pequeñas de poco más de 4000 LUT y 4400 registros.

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## Chapter A

## Graph Theory concepts

Graph theory is common mathematical approach which provides interesting metrics for the determination of networks. The applications for graph theory have a strong hold in many disciplines including computer science, biology and sociology to name a few. A historical mathematical problem named Seven bridges of Konigsberg written by Leonhard Euler in 1736, is considered to be the first introduction to graphs and topologies, where Euler proved using graphs that it was impossible to traverse the city of Königsberg exactly once and return to the starting point using seven different interconnected bridges [70].

In neuroscience graph theory is used as a tool to further identify underlying characteristics of the brains structural, functional and effective connectivity.

Figure A.1, shows an overview of some of the underlying concepts behind graph theory. Firstly, every object in the network is assigned as a node (identified as a grey dot). Where each node in the network are connected via edges, which are the abstract connections between the nodes. As an example, in a typical EEG/MEG scalp recording set-up the electrodes would be considered the nodes and all the interconnections between the electrodes would be considered the edges of the network. In the 10-20 system this would typically consist of 16 nodes and 120 edges (excluding isolated nodes).

In general, graph networks are complex networks which should follow the following logical steps[71, 72]:

1. Define all nodes in the network: As stated above, the definition of the nodes could be in the form of EEG/MEG electrodes or as anatomically defined regions via the interpretation of MRI or DTI data.
2. The second step, is to identify a continuous measure of association between nodes. This is usually done between all combinations of nodes. This continuous measure could be time based correlation, spectral analysis or DTI analysis.
3. The next step is to derive an 'association matrix', $M$, which consists of a square $N x N$, map of all the continuous measures from the previous step.
4. The next step is to derive an 'adjacency matrix', $A$, from the association matrix. These can be constructed in several ways depending on the application intended. Nevertheless, the most common $A$, is a binary matrix, in which a static or dynamically varying threshold is applied the $M$. In this case anything above the threshold is set to 1 , conversley, anything below is set to 0 , this produces a symmetrical $A$ matrix filled with zeros and ones.
5. The final step in the process is to conduct analysis on $A$, using graph theoretical based metrics to build information maps on the network.

Other types of networks do exist beyond the non-weighted non-directional network, such as weighted/directed graphs, binary/directed graphs, however functional connectivity is usually set as binary/undirected graphs.

In general there are three main desirable metrics which can prove useful to the identification of structural and functional connectivity in brain networks[73]:

## 1. Degree

The degree $k$, is a metric which identifies the number of edges connected to a given node such that:

$$
\begin{equation*}
k_{i}=\sum_{i}^{N} A_{i, j} \tag{A.1}
\end{equation*}
$$

Where $A$, is the adjacency matrix and $i$ and $j$ are the row and coulomb in the matrix respectively. In the case of binary threshold matrices, this gives a clear indication of how heavily each node in the network is connected with other nodes. More often than not the averaging of the edges per node is calculated such that:

$$
\begin{equation*}
\langle k\rangle=\frac{1}{N} \sum_{i}^{N} k_{i} \tag{A.2}
\end{equation*}
$$

This gives an overall value for the brains connectivity patterns (i,e) the total number of nodes which passed the threshold. This metric is especially useful for time varying analysis and dynamic thresholds as time lapse maps can be built.

## 2. Path length

The average path length $L$, indicates the minimum number of edges between any two nodes within a network, using global efficiency $E$ to account for isolated nodes. The path length indicates how well information or other entities in the network can be transferred from one region to another. Given as:

$$
\begin{gather*}
E=\frac{1}{N(N-1)} \sum_{i, j, i \neq j}^{N} \frac{1}{d_{i, j}}  \tag{A.3}\\
L=\frac{1}{E} \tag{A.4}
\end{gather*}
$$

Where, $d$, is the distance between two nodes.

## 3. Clustering coefficient

The clustering coefficient $C$, measures the occurrence of clusters in a given network by showing the probability that a nodes neighbours are also connected. This measure is an index of local structure and is used as a resilience factor, i.e if a node is lost (doesn't pass threshold), what's the probability that its nearest neighbours are still connected.

$$
\begin{equation*}
C=\frac{1}{N} \sum_{i}^{N} \frac{2 n_{i}}{k_{i}\left(k_{i}-1\right)} \tag{A.5}
\end{equation*}
$$

Where $n_{i}$, represents the number of edges between the neighbours of node i.

## 4. Edge density

The edge density $m$, identifies the fraction of existing edges in a network out of the total number of edges in the network:

$$
\begin{equation*}
m=\frac{1}{N(N-1)} \sum_{i, j}^{N} A_{i, j} \tag{A.6}
\end{equation*}
$$

figure A.1, shows an example of how graph theory can be applied to a network. In this case the network (shown in the upper left hand corner), comprises of 5 nodes, A,B,C,D and E.

To calculate the average nodal degree of the network the mean of the total number of edges per node is taken. In this case, $A=3$, as it is connected to 3 other nodes via edges, $B=4$, etc... To grade the overall network the average is taken such that: $\operatorname{avg}\left(k_{i}\right)=\frac{1}{5} \cdot(3+4+2+2+1)$, giving a mean total of 2.4.

The average minimum distance between any two nodes is such that: $E=\frac{1}{5 \cdot 4} \cdot(3.5+$ $4+3+3+2.5$ ), giving a mean total of 0.8 , this is known as the global efficiency. The Path length is calculated as $L=\frac{1}{0.8}=1.25$.

As an example in the case of the distance between nodes A and E , there exists a shortest route of 2 edges, therefore, $\frac{1}{d_{i, j}}=\frac{1}{2}=0.5$.

For the clustering coefficient node $A=\frac{2 \cdot 2}{3 \cdot(3-1)}=\frac{1}{3}$, the denominator signifies the amount of edges connected to the node A, whereas the numerator signifies the number of connections made between other nodes connected to these edges. In A the numerator $n_{i}=2$, since C is connected to B and D is also connected to B .

In the case that isolated nodes are located such as node E , the clustering coefficient is set to 0 , because the denominator $k_{i}\left(k_{i}-1\right)$, is set to 0 , and is hence undefined.

From the metrics above it is possible to construct special networks topologies which derive an association to brain connectivity and can be seen in figure A.1. These are,ordered, small-world and random networks. The ordered network is a such that each node is connected to its K nearest neighbours. In general the ordered network has a high C and high L (neighbouring nodes are well connected and the path length is long).

The random network is such that all edges are randomly connected to nodes, in this case C tends to be very small L very small (neighbouring nodes are not well connected and the path length is short).

The final network, small world, is a form of the ordered network, where some nodes are disconnected and reconnected based on probability, Small world tends to have a high C but a very low L.

The brains connectivity tends to show characteristics similar to that of a small world network, where neuronal clusters are well connected via short connections [74].

The small-worldness of a given network H , which comprises of N nodes can be obtained by normalising its C and L with that of a random network such that: $\lambda=\frac{C_{H}}{C_{\text {random }}}$ and $\gamma=\frac{L_{H}}{L_{\text {random }}}$. If $\lambda>1$ and $\gamma \approx 1$, the network is said to be characteristic of a small world network. $\eta=\frac{\lambda}{\gamma}$, defines the small worldness but must strictly be greater than 1 [73].

It is however important to stress that the probability factor allows for many networks between $p=0$ and $p=1$, By increasing the rewiring probability.


Fig. A. 1 Graph theory: Overview of some of the basic concepts in graph theoretical analysis. A node is represented as a grey dot and an edge is represented as the connection between two nodes. The degree defines the number of connections connected to a node, in this case the number of connections connected to the blue dot. The path length, is the shortest distance between two nodes and clustering refers to the probability that neighbouring nodes are connected to each other. In the top example, which consists of nodes A through E, the degree of node A is 3, the minimum path length between nodes A and E is 2. The clustering coefficient of A is $\frac{2}{3}$. The three network topologies show an ordered network, which has a high C and long L, the random network has a small C and a short L, the small world network has a high C and shot L, which are properties similar to that of the human brain. In the ordered case the number of nodes are $8 \mathrm{~N}=8$ and $\mathrm{k}=4$

## Chapter B

## Code listings

## B. 1 Matlab Code DDA

```
clc;
clear all;
%Inital setup of signals
samples = 1024;
bins = 2048;
t = 0:1:samples*bins;
fs = 2048;
fc = 20;
%Signal 1
S1 = 10*sin(2*pi*fc/fs*t);
f1 = 10;
f2 = 30;
%Signal 2
S2 = 10*chirp(t,f1/fs,t(end),f2/fs);
r = 4;
% Initiate variables
j = 0; p = 0; l = 0; n = 0; k = 0; storageal = 0; storageb1 = 0;
count1 = 0; count2 = 0; v = 1; Deltas(1) = 0; Deltas(2) = 0;
wincount = 0; RS = 0; window = samples;
for i = 2:length(s1)
    windowcount = windowcount + 1;
    %Signal 1 event detection based on variable M and Q
```

```
26 %Toggeling comparator
if sl(i) < sl(i-1)
    M(end) = 0;
elseif sl(i) > sl(i-1)
    M(end) = 1;
end
%Shift register minima
M = circshift(M,[0 1]);
%Logic outlier decision
if sum(M(1:(length(M)/2))) == length(M)/2 && ...
    sum(M((length(M)/2)+1:end)) == 0;
    j = j + 1;
elseif nnz(\negM(1:length(M)/2)) < Q && ...
    nnz(M((length(M)/2)+1:end)) < Q
    j = j + 1;
end
%Same set-up for signal 2
if s2(i) < s2(i-1)
    M2 (end) = 0;
elseif s2(i) > s2(i-1)
    M2 (end) = 1;
end
M2 = circshift(M2,[0 1]);
if sum(M2(1:(length(M2)/2))) == length(M2)/2 && ...
    sum(M2 ((length(M2)/2) +1:end)) == 0;
    p = p + 1;
elseif nnz(\negM2(1:length(M2)/2)) < Q && ...
    nnz(M2 ((length(M2)/2) +1:end)) < Q
    p = p + 1;
    end
    % signal1 minimum found start count
    if j == 1
        count1 = count1 + 1;
        % signall second minimum found store count and reset
elseif j == 2
    count1 = count1 + 1;
    storagea1 = count1;
```

```
    count1 = 0;
    j = 1;
    n = 2;
    end
    % signal2 minimum found start count
    if p == 1
        count2 = count2 + 1;
        % signal2 second minimum found store count and reset
    elseif p == 2
        count2 = count2 + 1;
        storageb1 = count2;
        count2 = 0;
        p = 1;
        l = 2;
    end
    % Minimum trasition period found in both signals abs(diff)
    if n == 2 && l == 2
        Deltas(i-3) = abs(((storageal) - (storagebl)));
        storageal = 0;
        storageb1 = 0;
        n = 1;
        l = 1;
        V = v + 1;
    else
        Deltas(i-3) = 0;
    end
    % accumulate error for N samples (window)
    if wincount < window
        RS = Deltas(i-3) + RS;
    else
        %If window reached store phi(i)
        k = k + 1;
        RSfinal(k,:) = [k*window RS];
        wincount = 0;
        RS = 0;
    end
    end
    %Synchronisation index
    SI = RSfinal(2,:);
```

```
110 SIH2 = 1-min(SI (:,2),samples/2^r)/(samples/2^r);
111 SIH2 = smooth(SIH2,15);
```


## B. 2 Matlab Code Threshold

```
%%%%%%%%%%%%%%%%%%%%Signal }1\mathrm{ dda }%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
%This is how many false positives are allowed over the length of ...
    the signal
%Find total length of SI values minus the pre, post and ictal periods
%Multiply by the desired FPR rate in order to find the total ...
    number of
%false positives
totalpeaks015 = (length(Mineoverall1(SI))/60/60)*0.15;
%Find all of the highest peaks within this period
peaks = findpeaks(Mineoverall1(SI));
%Organise the peaks from highest to lowest
[val ind] = sort(peaks,'descend');
%Take the x highest peaks
Threshold015 = val(round(totalpeaks015));
%FPR @ 0.3
totalpeaks03 = (length(Mineoverall1(SI))/60/60)*0.3;
peaks = findpeaks(Mineoverall1(SI));
[val ind] = sort(peaks,'descend');
Threshold03 = val(round(totalpeaks03));
%FPR @ 0.45
totalpeaks045=(length(Mineoverall1(SI))/60/60)*0.45;
peaks = findpeaks(Mineoverall1(SI));
[val ind] = sort(peaks,'descend');
Threshold045 = val(round(totalpeaks045));
%FPR @ 0.6
totalpeaks06=(length(Mineoverall1(SI))/60/60)*0.6;
peaks = findpeaks(Mineoverall1(SI));
[val ind] = sort(peaks,'descend');
Threshold06= val(round(totalpeaks06));
%FPR @ 0.75
totalpeaks075 = (length(Mineoverall1(SI))/60/60)*0.75;
```

```
peaks = findpeaks(Mineoverall1(SI));
[val ind] = sort(peaks,'descend');
Threshold075 = val(round(totalpeaks075));
threshold(1,:)= zeros(1,length(Mineoverall1)) + Threshold015;
threshold(2,:)= zeros(1,length(Mineoverall1)) + Threshold03;
threshold(3,:)= zeros(1,length(Mineoverall1)) + Threshold045;
threshold(4,:)= zeros(1,length(Mineoverall1)) + Threshold06;
threshold(5,:)= zeros(1,length(Mineoverall1)) + Threshold075;
```


## B. 3 VHDL Code DDA

```
.
    SIGNALS
    entity adder is
    port(adder_in_s1: in std_logic_vector(9 downto 0);
        clr,clk: IN std_logic;
        alpha2: in std_logic_vector(3 downto 0);
        adder_out: out std_logic_vector(9 downto 0)
        );
    end adder;
architecture Behavioral of adder is
signal tmp2: std_logic_vector(9 downto 0):= (others => '0');
attribute dont_touch : string;
attribute dont_touch of tmp2 : signal is "true";
begin
process(clk,tmp2)
begin
if clk'event and clk = '1' then
if clr = '1' then
tmp2 \leq (others => '0');
adder_out \leq (others => '0');
else
--this is the calculation to create the exponential filter using ...
    shift left registers and bitvectors
tmp2 \leq ((tmp2 - to_stdlogicvector((to_bitvector(tmp2) srl ...
        to_integer(unsigned(alpha2))))) + ...
```

```
    to_stdlogicvector((to__bitvector(adder_in_sl) srl ...
    to_integer(unsigned(alpha2)))) );
end if;
end if;
adder_out \leq tmp2;
end process;
end Behavioral;
    MINIMA DETECTION
    COMPARATOR VALLEY DETECTION
entity Comparator is
port(compare_in_sample: in std_logic_vector(9 downto 0);
    compare_in_ref: in std_logic_vector(9 downto 0);
    clk,rst: in std_logic;
    compare_out: out std_logic);
end Comparator;
architecture Behavioral of Comparator is
signal tempcomp: std_logic := '0';
begin
process(clk,tempcomp)
begin
if clk'event and clk = '1' then
if rst = '1' then
tempcomp \leq '0';
compare_out \leq '0';
else
-- Compare the previous value and new value coming value and ...
    assign 1,0 or equal to accordingly
if (compare_in_sample > compare_in_ref) then
tempcomp \leq '0';
elsif(compare_in_sample < compare_in_ref) then
tempcomp s '1';
else
tempcomp \leq tempcomp;
end if;
end if;
end if;
compare_out \leq tempcomp;
end process;
end Behavioral;
_—_SHIFT REGISTER OUTLIER LOGIC
```

```
entity Shifter is
port(reg2_in: in std_logic;
    reg2_out: out std_logic_vector(9 downto 0);
    rst: in std_logic;
    clk: in std_logic
        );
end Shifter;
architecture Behavioral of Shifter is
signal sig2: std_logic_vector(9 downto 0):= (others => '0');
begin
process(clk,sig2)
begin
if (clk'event and clk = '1') then
if rst = '1' then
reg2_out \leq (others => '0');
sig2 \leq (others => '0');
-- Shift left and store the values out from COM1 these are telling ...
    us about the signal if we are
--going down the signal or up the signal for the outlier event
else
    sig2(0) \leq reg2_in;
    sig2(1) \leq sig2(0);
    sig2(2) \leq sig2(1);
    sig2(3) \leq sig2(2);
    sig2(4) \leq sig2(3);
    sig2(5) \leq sig2(4);
    sig2(6) \leq sig2(5);
    sig2(7) \leq sig2(6);
    sig2(8) \leq sig2(7);
    sig2(9) \leq sig2(8);
end if;
end if;
reg2_out \leq sig2;
end process;
end Behavioral;
_-_MINIMA . . .
```



```
signal temp20: std_logic_vector(9 downto 0);
signal temp31: std_logic ;
signal ones: std_logic:='0';
```

```
107 signal valleyfoundtemp: std_logic:='0';
signal zeros: std_logic:='0';
signal change: std_logic:='0';
begin
    ADD : adder PORT MAP (adder_in_s1 => data_in,adder_out => ...
        temp1,clr => clr,clk =>clk,alpha2=>alpha2);
    COM1: Comparator PORT MAP (compare_in_sample => ...
        temp11, compare_in_ref \(=>\) temp12, compare_out \(=>\) temp31,clk ...
        =>clk,rst=>clr);
    SHFT: Shifter PORT MAP (rst => clr, reg2_in => temp31,clk => ...
        clk,reg2_out => temp20);
    SHFT2: shft22 PORT MAP (rst = \({ }^{2}\) clr,shft_in => temp1, clk => clk, ...
        shft_out (21 downto 11) => templ1, shft_out (10 downto 0) => ...
        temp12);
115
    -- Calculations to find the valleys in the signal using data from ...
        shifter
    --ones, if we detect 4 ones in a row outut 1
    ones \(\leq((\) temp20 (3) AND temp20 (2) AND temp20 (1)AND temp20 (0)) ) OR
        (NOT (temp20(3)) AND temp20 (2) AND temp20 (1) AND temp20(0)) OR
        (temp20 (3) AND NOT (temp20 (2) ) AND temp20 (1) AND temp20 (0) ) OR
        (temp20 (3) AND temp20 (2) AND NOT (temp20 (1)) AND temp20 (0)) OR
        (temp20 (3) AND temp20 (2) AND NOT (temp20 (1)) AND NOT (temp20 (0)) );
    --zeros, if we detect 4 zeroes in a row output 1
    zeros \(\leq((N O T(t e m p 20(9))\) AND NOT (temp20(8)) AND NOT (temp20(7)) AND ...
        NOT (temp20 (6)) )) OR
            ((temp20 (9)) AND NOT (temp20 (8)) AND NOT (temp20 (7) ) AND ...
                NOT (temp20(6))) OR
            (NOT (temp20 (9)) AND (temp20 (8)) AND NOT (temp20 (7)) AND ...
                NOT (temp20(6))) OR
            (NOT (temp20(9)) AND NOT (temp20(8)) AND (temp20(7)) AND ...
                NOT (temp20(6))) OR
            (NOT (temp20(9)) AND NOT (temp20(8)) AND NOT (temp20(7)) AND ...
                    (temp20 (6)) );
    - if the middle two bits are 0 and 1 output is one this ...
    indicates a change in direction
    change \(\leq(\) NOT (temp20(5)) AND temp20(4));
    -- If all are true possible valley detected output a 1
    valley_found \(\leq\) (ones AND zeros AND change);
    end Behavioral;
```

```
    __TIME STAMP TRANSITION ... 
        port(startstop,rst,clk: in std_logic;
        countout: out std_logic_vector(9 downto 0)
        );
        end CountMod;
    -- This is a start, stop and reset counter, when a valley is ...
        detected from the valdet block
    -- the counter starts if another is detected we reset the count, ...
        and start counting again.
        architecture Behavioral of CountMod is
        signal count: std_logic_vector(9 downto 0) := (others => '0');
        signal startcount: std_logic := '0';
        begin
        process(clk,count)
        begin
        if clk'event and clk = '1' then
        if rst = '1' then
        count \leq (others => '0');
        countout \leq (others => '0');
        startcount \leq '0';
        else
        _-if a valley is detected
        if startstop = '1' then
        --send a flag to start the transitional up counter
        startcount \leq '1';
        end if;
        --if the counter is currently counting a transition and a ...
        second transition has yet to be found
    --then start counting. The variable startstop is sent in from ...
        a control block which indicates
        -- a reset
        if startcount = '1' and startstop = '0' then
        count \leq count + 1;
        else
        count \leq (others => '0');
        end if;
        end if;
```

```
    end if;
    countout \leq count;
    end process;
    end Behavioral;
    ——CONTROL BLOCK FLAGS FOR CALCULATION ...
        BLOCK
entity Calculations is
PORT(ready1, ready2,clk,rst: in std_logic;
    flag1,flag3,flag5: out std_logic);
end Calculations;
architecture Behavioral of Calculations is
signal countv1: std_logic:='0';
signal countv2: std_logic:='0';
type states is (sr,calcl);
signal current_s,next_s: states;
begin
process (clk)
begin
    if clk'event and clk = '1' then
    if rst='1' then
    current_s \leq sr;
else
    current_s \leq next_s;
    end if;
    end if;
    end process;
    process(current_s,countv1, countv2,rst)
    begin
    case current_s is
    when sr => if rst = '1' then
        next_s \leq sr;
            else
            __countv1 is 1 if a minima was detected in signal 1 and ...
                countv2 is 1 if --
            __a minima was detected in signal 2, else ...
                if countv1 = '1' and countv2 = '1' then
```

```
            next_s \leq calc1;
            else
            next_s \leq sr;
            end if;
            end if;
    when others => next_s \leq sr;
    end case;
    end process;
process(clk)
    begin
    if clk'event and clk = '1' then
    if next_s = calcl then
    -_2 minima detected reset-_
    countv1 s '0';
    countv2 \leq '0';
    else
    ___-this is the block which sets the minima detected ...
        signals_
    ___readyl cis a flag which comes from the minima detection ...
        logic block-
    if ready1 = '1' then
    countv1 \leq '1';
    else
    countv1 \leq countv1;
    end if;
    if ready2 = '1' then
    countv2 \leq '1';
        else
    countv2 \leq countv2;
    end if;
end if;
end if;
    end process;
process (current_s,ready1,ready2)
begin
            if current_s = sr then
            flag5 \leq '0';
            if readyl = '1' then
```

```
260 flag1 \leq '1';
    else
    flag1 \leq '0';
end if;
    if ready2 = '1' then
    flag3 \leq '1';
    else
    flag3 \leq '0';
    end if;
else
flag5 \leq '1';
    if ready1 = '1' then
flag1 \leq '1';
else
flag1 \leq '0';
end if;
if ready2= '1' then
flag3\leq '1';
else
flag3 \leq '0';
end if;
end if;
end process;
end Behavioral;
                    CALCULATION BLOCK ABSOLUTE VALUE OF TRANSITIONS ...
            FROM TIMESTAMP BLOCK
    entity Calcflags is
PORT(clk: in std_logic;
        flag1,flag3,flag5,rstorage: in std_logic;
        offset: in std_logic_vector(2 downto 0);
        flagout: out std_logic;
        countsubed: out std_logic_vector(9 downto 0);
        raw: out signed(9 downto 0);
        countin1, countin2: in std_logic_vector(9 downto 0)
    );
    end Calcflags;
    architecture Behavioral of Calcflags is
signal storagea1 : std_logic_vector(9 downto 0) := (others => '0');
```

```
signal storageb1 : std_logic_vector(9 downto 0) := (others => '0');
signal calcul : signed(9 downto 0) := (others => '0');
begin
process(clk,calcu1)
begin
if clk'event and clk = '1' then
if rstorage = '1' then
storagea1 \leq (others => '0');
storageb1 \leq (others => '0');
calcul \leq (others => '0');
countsubed \leq (others => '0');
flagout \leq '0';
else
if flag1 = '1' then
--if a transition period was found then store the value of count-
--to the storage registers
storageal \leq countin1;
else
storageal \leq storageal ;
end if;
if flag3 = '1' then
storageb1 \leq countin2-offset;
else
storageb1 \leq storageb1;
end if;
if flag5 = '1' then
--If a transition period in both signals has been detected then ...
    calculate the error
calcul \leq (signed(storagea1) - signed(storageb1));
flagout \leq '1';
else
calcul \leq (others => '0');
flagout \leq '0';
end if;
end if;
end if;
raw \leq calcu1;
--Calculate the absolute value of the error
countsubed \leq std_logic_vector(abs(calcul));
end process;
```

```
~
end Behavioral;
INDEXING AND ACCUMULATION ...
    BLOCK
entity Indexing is port
(clk,rst: in std_logic;
    flag: out std_logic;
    flagin: in std_logic;
        N: in std_logic_vector(9 downto 0);
                cal: in std_logic_vector(9 downto 0);
                sum: out std_logic_vector(9 downto 0)
);
end Indexing;
architecture Behavioral of Indexing is
signal accumvalue: std_logic_vector(9 downto 0) := (others => '0');
signal numberofsamples:std_logic_vector(9 downto 0) := (others => ...
        '0');
attribute dont_touch : string;
attribute dont_touch of sum,accumvalue : signal is "true";
begin
process(clk)
begin
if clk'event and clk = '1' then
if rst = '1' then
sum \leq (others => '0');
accumvalues (others => '0');
numberofsamples \leq (others => '0');
else
if numberofsamples < N then
if flagin = '1' then
--while the the number of accumulations are less than N accumlate...
    errors
accumvalue \leq accumvalue + cal;
flag \leq '0';
numberofsamples \leq numberofsamples + 1;
sum \leq (others => '0');
else
accumvalue \leq accumvalue;
flag \leq '0';
numberofsamples \leq numberofsamples;
sum \leq (others => '0');
end if;
```

```
else
flag < '1';
sum \leq accumvalue;
numberofsamples \leq (others => '0');
accumvalue\leq (others => '0');
end if;
end if;
end if;
end process;
end Behavioral;
__OUTPUT EXPONENTIAL ...
    FILTER
library IEEE;
use IEEE.STD_LOGIC_1164.ALL;
USE IEEE.STD_LOGIC_UNSIGNED.ALL;
use IEEE.NUMERIC_STD.ALL;
entity SmoothDetect is port
(sumin: in std_logic_vector(9 downto 0);
    flag,rst: in std_logic;
    sumout: out std_logic_vector(9 downto 0);
    alpha: in std_logic_vector(3 downto 0);
    clk: in std_logic);
end SmoothDetect;
architecture Behavioral of SmoothDetect is
signal y_minus_1: std_logic_vector(9 downto 0):= (others => '0');
attribute dont_touch : string;
attribute dont_touch of y_minus_1 : signal is "true";
attribute dont_touch of sumout : signal is "true";
begin
process(clk,y_minus_1)
begin
if clk'event and clk = '1' then
if rst = '1' then
y_minus_1 \leq (others => '0');
sumout \leq (others => '0');
else
if flag = '1' then
```

```
430 --This is the main calculation for the output exponential filter
4 3 1 ~ y \_ m i n u s \_ 1 ~ \leq ~ ( y \_ m i n u s \_ 1 ~ - ~ . . . ~
    to_stdlogicvector((to_bitvector(y_minus_1) srl ...
    to_integer(unsigned(alpha))))) + ...
    to_stdlogicvector(to_bitvector(sumin) srl ...
    to_integer(unsigned(alpha)));
    else
    y_minus_1 \leq Y_minus_1;
    end if;
    end if;
    end if;
    sumout \leq Y_minus_1;
end process;
end Behavioral;
    UPLOAD LINK BLOCK UPLOADS ALL OF THE PARAMETERES FOR THE ...
    ASIC-_
    NOTE THAT THIS USES A 48 BIT SIPO REGISTER-
entity UploadLink is
port(clk2,rst,datain1,datain2,loadparameters:in std_logic;
    clkout,paramcomplete,rst2:out std_logic;
    dataout1,dataout2: out std_logic_vector(9 downto 0);
        N: out std_logic_vector(9 downto 0);
        alpha: out std_logic_vector(3 downto 0);
        alpha2: out std_logic_vector(3 downto 0);
        offset: out std_logic_vector(2 downto 0);
        Ndetected: out std_logic_vector(5 downto 0);
        Tdropout: out std_logic_vector(9 downto 0);
        Triseout: out std_logic_vector(9 downto 0)
);
end UploadLink;
architecture Behavioral of UploadLink is
signal shiftdatal: std_logic_vector(9 downto 0):= (others => '0');
signal shiftdata2: std_logic_vector(9 downto 0):= (others => '0');
signal dummy1: std_logic_vector(9 downto 0):= (others => '0');
signal dummy2: std_logic_vector(9 downto 0):= (others => '0');
signal parameterreg: std_logic_vector(47 downto 0):= (others => '0');
signal counterdld2: std_logic_vector(3 downto 0):= (others => '0');
signal countertlt2: std_logic_vector(5 downto 0):= (others => '0');
signal slavecounter: std_logic_vector(3 downto 0);
signal paramcomplete2: std_logic := '0';
signal clktemp,test: std_logic;
```

```
attribute dont_touch : string;
attribute dont_touch of dummy1,dummy2: signal is "true";
begin
process(clk2,dummy1,dummy2,paramcomplete2)
begin
if clk2'event and clk2 = '1' then
                                    clockslave-
if rst = '1' then
shiftdatal \leq (others => '0');
shiftdata2 \leq (others => '0');
paramcomplete2 \leq '0';
parameterreg \leq (others => '0');
counterd1d2 \leq (others => '0');
countert1t2 \leq (others => '0');
dataout1 \leq (others => '0');
dataout2 \leq (others => '0');
Tdropout \leq (others => '0');
Triseout \leq (others => '0');
N \leq (others => '0');
alpha \leq (others => '0');
alpha2 \leq (others => '0');
offset \leq (others => '0');
Ndetected \leq (others => '0');
slavecounter \leq (others => '0');
dummy1 \leq (others => '0');
dummy2 \leq (others => '0');
clktemp \leq '0';
rst2 \leq '1';
else
if slavecounter \leq "0101" then
slavecounter \leq slavecounter + 1;
clktemp \leq '1';
elsif slavecounter \geq "0110" and slavecounter < "1011" then
clktemp \leq '0';
slavecounter \leq slavecounter + 1;
else
rst2 \leq '0';
slavecounter \leq (others => '0');
end if;
if paramcomplete2 = '1' then
if counterd1d2 \leq "1001" then
```

```
513 shiftdatal(9 downto 1) \leq shiftdatal(8 downto 0);
shiftdatal(0) \leq datain1;
shiftdata2(9 downto 1) \leq shiftdata2(8 downto 0);
shiftdata2(0) \leq datain2;
counterd1d2 \leq counterd1d2 + 1;
elsif counterd1d2 = "1010" then
dummyl \leq shiftdatal;
dummy2 \leq shiftdata2;
counterd1d2 \leq counterdld2 + 1;
else
shiftdatal \leq (others => '0');
shiftdata2 \leq (others => '0');
counterd1d2 \leq (others => '0');
end if;
else
shiftdatal \leq (others => '0');
shiftdata2 \leq (others => '0');
counterd1d2 \leq (others => '0');
end if;
if countert1t2 < "110001" then
countert1t2 \leq countert1t2 + 1;
parameterreg(47 downto 1) \leq parameterreg(46 downto 0);
parameterreg(0) \leq loadparameters;
paramcomplete2 \leq '0';
else
--parametercheckreg \leq parameterreg;
Tdropout \leq parameterreg(47 downto 37);
Triseout \leq parameterreg(36 downto 27);
Ndetected \leq parameterreg(26 downto 21);
offset \leq parameterreg(20 downto 18);
alpha \leq parameterreg (17 downto 14);
alpha2 \leq parameterreg(13 downto 10);
N \leq parameterreg(9 downto 0);
paramcomplete2 \leq '1';
end if;
end if;
end if;
dataout1 s dummy1;
dataout2 \leq dummy2;
paramcomplete \leq paramcomplete2;
end process;
clkout s clktemp;
```

```
end Behavioral;
__DOWNLOAD LINK THIS IS THE PISO REGISTER__
                                    FOR THE SYNCHRONISATION VALUES-
                                    AND TEST PARAMETERS
entity DownloadLink is
port(clk,rst,load: in std_logic;
    sumin:in std_logic_vector(9 downto 0);
    nonsmoothed: in STD_LOGIC_VECTOR (9 downto 0);
    sumserialout,beforesmooth: out std_logic
);
end DownloadLink;
architecture Behavioral of DownloadLink is
signal holdsum: std_logic_vector(9 downto 0):= (others => '0');
signal nonsmoothedsum: std_logic_vector(9 downto 0):= (others => '0');
begin
process(clk,holdsum, nonsmoothedsum)
begin
if clk'event and clk = '1' then
if rst = '1' then
holdsum \leq (others => '0');
sumserialout \leq '0';
nonsmoothedsum \leq (others => '0');
beforesmooth \leq '0';
else
if load = '1' then
holdsum \leq sumin;
nonsmoothedsum \leq nonsmoothed;
else
holdsum(9 downto 1) \leq holdsum(8 downto 0);
holdsum(0) \leq '0';
nonsmoothedsum(9 downto 1) \leq nonsmoothedsum(8 downto 0);
nonsmoothedsum(0) \leq'0';
end if;
end if;
end if;
sumserialout \leq holdsum(9);
beforesmooth \leq nonsmoothedsum(9);
end process;
end Behavioral;
```


## B. 4 RTL-compiler

```
#set_attribute hdl_vhdl_environment common
set_attribute hdl_vhdl_read_version 1993
set_attribute hdl_vhdl_case original
# this tells the compiler where to look for the libraries
set_attribute lib_search_path ...
    /cad/KITS/CADENCE_13/ams_cdk_4.11_upd1/liberty/h18_1.2V
#this defies the libraries to use
set_attribute library {h18_CORELIB_HVT_TYP.lib}
#convert non conventional operands to library specified operands
set_attribute lp_insert_operand_isolation true /
#Clock gating on (reduces power consumption)
set_attribute lp_insert_clock_gating true /
#How much information to show user on design
set_attribute information_level 7
#Flag black box errors
set_attribute hdl_error_on__blackbox 1
#Flag latch errors
set_attribute hdl_error_on_latch 1
set_attribute interconnect_mode ple
#Load all VHDL files
read_hdl -vhdl ../rtl/adder.vhd
read_hdl -vhdl ../rtl/Calcflags.vhd
read_hdl -vhdl ../rtl/Comparator.vhd
read_hdl -vhdl ../rtl/CountMod.vhd
read_hdl -vhdl ../rtl/Detection.vhd
read_hdl -vhdl ../rtl/Indexing.vhd
read_hdl -vhdl ../rtl/Main.vhd
read_hdl -vhdl ../rtl/MainMain.vhd
read_hdl -vhdl ../rtl/shft22.vhd
read_hdl -vhdl ../rtl/Shifter.vhd
read_hdl -vhdl ../rtl/SmoothDetect.vhd
read_hdl -vhdl ../rtl/Valleydetect.vhd
read_hdl -vhdl ../rtl/Comlink.vhd
read_hdl -vhdl ../rtl/UploadLink.vhd
read_hdl -vhdl ../rtl/DownloadLink.vhd
read_hdl -vhdl ../rtl/Paramcheck.vhd
#Elaborate the design
elaborate Comlink
#Read constraints file
read_sdc ../constrains/CountMod.sdc
```

```
#setup clocks in this case max frequency 125Khz
define_clock -domain "system" -period 8000000 -fall 50 -rise 50 ...
    -name clkup [find / -port clkup]
#Define the amount of skew
set_attribute clock_setup_uncertainty {100 50} [find -clock clkup]
#Define the amount of slew {minrise,minfall,maxrise,maxfall}
set_attribute slew {1000 1000 1500 1500} [find -clock clkup]
#Define input delays #all inputs will change 10000 ps after rising ...
    edge
external_delay -input 100000 -clock [find -clock clkup] -edge_rise ...
    [find /des* -port ports_in/*]
#Define output delays #all output data will be ready 10000 ps ...
    before rising edge
external_delay -output 100000 -clock [find -clock clkup] ...
    -edge_rise [find /des* -port ports_out/checkdatal]
external_delay -output 100000 -clock [find -clock clkup] ...
    -edge_rise [find /des* -port ports_out/checkdata2]
#Synthesise the design
synthesize -to_generic -effort high
synthesize -to_mapped -effort high
#Write final verilog file to be used in encounter layout
write_hdl > ../Outputs/Phase_final_VERILOG_preserved.v
```


## B. 5 MBED-C++ test platform code

```
#include "mbed.h"//import mbed libraries
#include "MSCFileSystem.h"
#include "rtos.h"
#include "FastPWM.h"
//Setup all the GPIO pins and special pins
DigitalOut Clear(p14);
DigitalOut Msel1(p13);
DigitalOut Msel2(p15);
DigitalOut Enable(p10);
DigitalOut aaout(p29);
DigitalOut Sig1Out(p11);
DigitalOut Sig2Out(p16);
DigitalOut CLK(p12);
FastPWM CLK2(p23);
DigitalIn SIindex(p27);
```

```
//Use the MSCFilesystem to read from the Fat32 SUB stick
MSCFileSystem fs("usb");
Ticker ticker2;
Ticker ticker3;
InterruptIn CLKs(p18);
InterruptIn Mux(p28);
Thread thread;
//Open serial USB port
Serial pc(USBTX, USBRX);
//Intermidiate variables
bool rising = false;
bool rising2 = false;
bool rising3 = false;
char s1;
char s2;
bool slint = false;
bool s2int = false;
int loop = 1;
bool runit = true;
int temp = 0;
//This is a seperate thread which reads the output of the ASIC ...
    every clock cycle it is active only if the end
//of the binary neural data files are still not empty, if the ...
    variable K from the ASIC is active high and if the processors
//CLK is also high. It reads 10 samples.
void clockslow_thread()
{
    while(runit == true) {
        if(rising2 == true) {
            for(int nn = 0; nn < 11; nn++) {
                if(CLK == true) {
                    pc.printf("%d%d \r\n",SIindex.read(),rising2);
                }
                    }
            }
        }
//Seperate function which sets up the main synchronisation CLK for ...
    the processor 2KHz
//This gets called using a timer and is called periodically.
    void clocktick2() {
        CLK = !CLK;
    }
```

```
//This is a function which is activated by an external interrupt ...
    Mux.rise.
//How this is activated is explained later
        void interrupt_triggered2() {
            rising2 = true;
        }
//The next functions setup a matched register case PWM fast clock ...
    of 20KHz on a dedicated
//PWM pin on the MBED
    void PWMInit();
    void PWM1_IRQHandler () {
        if((LPC_PWM1->IR & 0x01) == 0x01) { // Check whether it is ...
            an interrupt from match 0
                //If the PWM is rising then set this variable to true, ...
                    this is an edge detector
            rising = true;
                LPC_PWM1->IR |= 1<<0; // Clear the interrupt flag
        }
        return;
    }
        void PWMInit() {
        LPC_SC->PCONP |= 1 << 6; // enable power for PWM1
        LPC_SC->PCLKSEL0 |= 1 << 12; // PCLK_PWM1 = CCLK
        LPC_PWM1->MR0 = 16000; // PWM freq = CCLK/16000
        LPC_PWM1->MCR |= 1 << 0; // interrupt on Match0
        LPC_PINCON-PPINSEL3 | = (2 << 14 ); // P2.4 works as PWM1 ...
            output
        LPC_PINCON->PINMODE3 |= 2 << 14; // enable neither pull up ...
            nor pull down
        LPC_PWM1->PCR |= 1 << 4; // Configure channel 4 as double ...
            edge controlled PWM
        LPC_PWM1->PCR |= 1 << 12; // Enable PWM channel 4 output
        LPC_PWM1->MR0 = 16000; // PWM freq = CCLK/16000
        LPC_PWM1->TCR = (1 << 0) | (1 << 3); // enable timer ...
            counter and PWM
```

```
    NVIC_SetVector(PWM1_IRQn, (uint32_t)&PWM1_IRQHandler);
    NVIC_EnableIRQ(PWM1_IRQn);
    return;
}
int main() { // start main function
    PWMInit();
//Set the serial communication bandwidth for the USB port
pc.baud(115200);
//These variables set an internal MUX inside the ASIC such ...
        that the ASIC sends out
//a pulse every 1024 samples. This tells us every time ...
    that an accumulation of errors
//has been colleted
Msel1=1;
Msel2 = 1;
//Enable sets an internal variable in the ASICs SPI ...
    interface which tells it to activate
Enable = 1;
//Open the two neural signal files which are stored on the ...
    Fat32 formatted memory stick
FILE *fp = fopen("/usb/Signal1.txt", "r");
FILE *fp2 = fopen("/usb/Signal2.txt", "r");
//Print an error message if there was a problem opening ...
    the files
    pc.printf("%s\n", (!fp ? "Fail :(" : "OK"));
if (!fp)
        error("error: %s (%d)\n", strerror(errno), -errno);
    wait(2);
    //Start runnning a seperate thread which calls the CLK ...
        funtion as described above
    //This calls the Clk function every 500 micro seconds ...
        which is equal to 2KHz main
    //processor operating frequency
    thread.start(&clockslow_thread);
    ticker2.attach_us(&clocktick2, 500);
    //This is an external interrupt which is connected to the ...
        value K from the ASIC.
```

```
//This is a single pulse every }1024\mathrm{ samples which sets the ...
        variable rising2 to true
Mux.rise(&interrupt_triggered2);
//This is the main file loop it continues until the end of ...
    the fneural signal file
while (!feof(fp)) {
    LPC_PWM1->MR3 = 6000;
    LPC_PWM1->MR4 = 15000;
    LPC_PWM1->LER |= (1<<3) | (1<<4) ;
    //If the variable rising is true it means that a ...
        rising edge on the 20KHz clock has been detected
    //If this is true then we want to read data from the ...
        Fat32 USB stick and send it to the ASIC
    if(rising == true) {
        rising = false;
        //Collect 1 bit of data from each of the two ...
                neural signal files
        s1 = fgetc(fp);
        s2 = fgetc(fp2);
        //Since the function fgetc is a character we have ...
                to do a test and assign an intermidate
        //variable with a boolean variable which is ...
                representative of the character.
        if(s1 == '1') {
                slint = true;
            } else if (sl == '0') {
                slint =false;
            }
            if(s2 == '1') {
                s2int = true;
            } else if (s2 == '0') {
                s2int = false;
            }
        //Send the data to the GPIO pins which are ...
                connected to the ASICS data intput pins
        SiglOut = slint;
        Sig2Out = s2int;
    }
}
fclose(fp);
fclose(fp2);
runit = false;
```


## Chapter C

## Pseudo codes

## C. 1 Pseudo code DDA hardware flow

The following is a pseudo code representation of the synchronisation algorithm hardware flow as seen in chapter 3.

```
procedure Minima detection \(\triangleright\) Example signal 1, same applies to signal 2
loop:
    if \(S 1(i)<S 1(i-1)\) then
                \(C 1 \leftarrow 0\).
        else if \(S 1(i)>S 1(i-1)\) then
            \(C 1 \leftarrow 1\).
        else
            \(C 1 \leftarrow C 1\).
            if \(O 1=0000011111\) then \(\quad \triangleright\) Possible to have one outlier each side
            \(M 1 \leftarrow 1\).
        else
            \(M 1 \leftarrow 0\).
    procedure Time stamp
        if \(M 1=1\) then
        \(C o \leftarrow\) Count .
        \(C o \leftarrow 0\).
        else
            \(C o \leftarrow C o+1\).
    procedure Calculation and Filter
```

```
20: \(\quad\) if \(K<\) Window then

21:
```

22:

```
```

```
22:
```

```
\[
L 1 \leftarrow C o
\]

\[
L 2 \leftarrow C o
\]

24:
\[
S u b \leftarrow L 1-L 2
\]

\[
\text { if } s=0 \text { then }
\]
\(26:\)
\[
A b s \leftarrow S u b
\]

27:
else

28:
\[
A b s \leftarrow|S u b| .
\]
\[
\text { Adderout } \leftarrow A b s+f e e d .
\]

29: \(\quad\) Adderout \(\leftarrow\) Abs + feed.
30:
\[
M 1 \leftarrow 0
\]

31 :
\[
M 2 \leftarrow 0
\]

32:
33 :
34 :
35 :
36:
37:
38: procedure Detect

40:
\[
\text { if } M 1=1 \wedge m 2=1 \text { then }
\]
else
null
else
\(\phi(i) \leftarrow\) phiraw.
Exp \(\leftarrow\) smoothed (Addreg).
\(y(i) \leftarrow y(i-1)-y(i-1) \alpha+\phi(i) \alpha\).

\section*{39: if \(y(i)<t h l\) then \\ Detect \(\leftarrow 1\).}
else if \(y(i)>t h h\) then
Detect \(\leftarrow 1\).
else
Detect \(\leftarrow 0\).

\section*{C. 2 Pseudo code for training and calculation hardware flow}
```

procedure Train and Calculate
if Inital $=1$ then
Mem $_{\text {epoch }, 1: 8} \leftarrow 1$.
Mem $_{\text {epoch }, 1: 8} \leftarrow 0$.
else if Train $=1$ then
if $y()_{\text {epoch }(x)}<\operatorname{Mem}_{\text {epoch }(x)}$ then
Mem $_{\text {epoch }(x)} \leftarrow y(i)_{\text {epoch }(x)}$.
$T 6 \leftarrow 1$.
else
$M e m L_{\text {epoch }(x)} \leftarrow M e m L_{\text {epoch }(x)}$.
$T 7 \leftarrow 1$.
if $y(i)_{\text {epoch }(x)}>\operatorname{MemH}_{\text {epoch }(x)}$ then
$M e m H_{\text {epoch }(x)} \leftarrow y(i)_{\text {epoch }(x)}$.
$T 2 \leftarrow 1$.
else
Mem $H_{\text {epoch }(x)} \leftarrow$ Mem $_{\text {epoch }(x)}$.
$T 1 \leftarrow 1$.
else
loop while epoch $<9$ :
if $S 1=1$ then
$M_{\text {em }} L_{\text {epoch }(x)} \leftarrow \Delta$.
Mem $_{\text {epoch }(x)} \leftarrow$ Mem $_{\text {epoch }(x)}$.
$T 4 \leftarrow 1$.
$T 1 \leftarrow 1$.
$T 8 \leftarrow 1$.
else if $S 2=2$ then
$M e m L_{\text {epoch }(x)} \leftarrow \Delta$.
$M e m H_{\text {epoch }(x)} \leftarrow M e m H_{\text {epoch }(x)}-\Delta$.
$T 7 \leftarrow 1$.
$T 8 \leftarrow 1$.
$T 2 \leftarrow 1$.
else if $S 3=3$ then
$M e m H_{\text {epoch }(x)} \leftarrow \operatorname{MemH}_{\text {epoch }(x)}$.
$M e m L_{\text {epoch }(x)} \leftarrow$ Mem $_{\text {epoch }(x)}-2 \Delta$.
$T 9 \leftarrow 1$.
$T 5 \leftarrow 1$.
$T 1 \leftarrow 1$.

```

\section*{Chapter D}

\section*{Control signals for future 16-channel testing platform}

The following appendix shows the main control signals for the 16 -channel ASIC implementation of the DDA algorithm. Where, the first column indicates if the signal is an input or an output. Next, the signal name is given as seen in the layout view of the device. The number column indicates the pin number as per the selected encapsulation package. The Voltage is the desired voltage for the pin. The pin type differentiates between pad ring power supply voltages, circuit supply voltages and general input output pins. The function column gives a brief description of the pin and the last column dictates whether the pin is active on a high or low signal.
E.
E.
E.














 CIRCUIT SUPPLY
CIRCUIT SUPPLY
PADRING SUPPLY










 0
0
0
0
0
0
0
0
0
0
0
0
0
0
4
0
0
0
0
0
0
0
0
0
0
0

CIRCUIT SUPPLY
PADRING SUPPLY PADRING SUPPLY

set bit for logic unit ring counter
Training finished calculate thresholds
CIRCUIT SUPPLY
CIRCUIT SUPPLY








\section*{Chapter E}

\section*{James Romaine, Publication list and curriculum}

Phase Synchronization Operator for on-chip Brain Functional Connectivity Computation Manuel Delgado-Restituto, James B. Romaine and Ángel Rodríguez-Vázquez Journal Paper-IEEE Transactions on Biomedical Circuits and Systems (TBioCAS) 2019

Highly scalable real time epilepsy diagnosis architecture via phase correlation and functional brain maps J.B. Romaine, M. Delgado-Restituto and A. Rodríguez-Vázquez Conference - IEEE Biomedical Circuits and Systems Conference BioCAS 2018

Highly Scalable Real Time Epilepsy Diagnosis Architecture Via Phase Correlation J.B. Romaine, M. Delgado-Restituto and A. Rodríguez-Vázquez Journal Paper - Procedia Technology, vol. 27, pp 55-56, 2017 ELSEVIER DOI: 10.1016/j.protcy.2017.04.026 ISSN: 2212-0173

Real-time phase correlation based integrated system for seizure detection J.B. Romaine, M. Delgado-Restituto, J.A. Leñero-Bardallo and A. Rodríguez-Vázquez Conference - Bio-MEMS and Medical Microdevices III Conference 2017

Integer-based digital processor for the estimation of phase synchronization between neural signals J.B. Romaine, M. Delgado-Restituto, J.A. Lenero-Bardallo and A. Rodriguez-Vazquez Conference - Conference on Ph.D Research in Microelectronics and

Electronics PRIME 2016

Highly scalable real time epilepsy diagnosis architecture via phase correlation and functional brain maps J.B. Romaine, L. Acasandrei, M. Delgado-Restituto, A. Rodríguez-Vázquez Conference - World Congress on Biosensors BIOSENSORS 2016

Hardware friendly algorithm for the calculation of phase synchronization between neural signals J.B. Romaine and M. Delgado-Restituto Conference - IEEE Biomedical Circuits and Systems Conference BioCAS 2014


\section*{Curriculum Vitae}

\section*{Personal information} First name(s) / Surname(s) Address
Telephone(s)
E-mail
Nationality
Date of birth
Gender
Work experience

\section*{Romaine, James}

Calle Camino de la valdovina,Castilleja de la cuesta 30,41950 , Sevilla
Mobile: +34 654567811
jamesbrianromaine@gmail.com
British
10.06.1985

Male

\section*{2014-2019}

PhD researcher (Microelectronics digital/analogue ASIC design and test engineer), Institute of microelectronics Sevilla (CSIC and University of Seville).
This position included the design, implementation and verification of low powered and low area consuming medical application specific integrated circuits, for the diagnosis and detection of pathological brain states. This position included a multi-disciplinary approach to work by incorporating, Mathematics and programming using Matlab, python and \(\mathrm{C}++\) for algorithmic designs and Electronics and physics for digital and analogue circuit layouts.

I have successfully integrated 3 separate integrated circuits. All of which started with the design of efficient algorithms in Matlab which were exhaustively simulated. Secondly, the algorithms were then coded into an FPGA environment using VHDL and Verilog. This stage provides hardware verification, the FPGA designs were then tested using a FPGA to Simulink co-simulation over JTAG connection. Finally, the circuit designs were implemented in CADENCE using RTL-COMPILER and Encounter layout managers.

Skills: Matlab, VHDL, Verilog, C++, CAD design, Analogue electronic design, Digital electronic design, FPGA, Mbed microcontrollers, Electronic circuit schematic designs, Electronic circuit physical layout, Mathematical modelling, Data analysis and Arduino.

Programmes: Simulink, CADENCE design suite, Encounter, Matlab, Vivado design suite, RTL compiler and Visual studio.

Other Skills: Presentations, Group work and publication writing.
Responsibilities: Time management for strict circuit integration deadlines, Circuit design, Circuit testing, publication of results and Organisation of workload for group projects.

Manuel Delgado Restituto and Ángel Rodríguez Vázquez, Instituto de microelectrónica de Sevilla (IMSE-CNM), Parque científico y tecnología cartuja, calle amercio Vespucio \(\mathrm{s} / \mathrm{n} 41902\) Sevilla

\section*{2017-2017}

\section*{Design engineer, University college London}

Working in the electronic engineering department at the University College London as part of a 3month exchange from the institute of microelectronics Seville. My main activities included:
- The manual layout design of an application specific integrated medical device for the treatment of epilepsy.
- Organisation of time.
- Presentations of previous work carried as well as the state of the art.
- Mathematical modelling and verification of microprocessors.

Skills: Matlab programming, CAD design, Analogue electronic design, Digital electronic design, Electronic circuit schematic designs, Electronic circuit physical layout, Mathematical modelling, Data analysis.

Programmes: CADENCE design suite, Matlab.
Other Skills: Presentations, Group work and publication writing.

Name and address of employer Prof Andreas Demosthenous, UCL department of electronic and electrical engineering. Department of Electronic \& Electrical Engineering - University College London - Torrington Place - London WC1E 7JE - +44 (0)20 31081123

Dates
2013
Main activities and responsibilities Project (Magnetic Liquids), University of York
This project involved the characterisation of several different magnetic liquids with the focus on Magneto rheological fluids. The goal of the project was to determine which fluid would produce the best results for a vehicle magneto rheological damping system. To achieve this goal a set of test apparatus was constructed which simulated a magneto rheological damping system. The test apparatus used a wide variety of skills.

Skills: C++ programming, Analogue electronic design, Mbed microcontrollers, Electronic circuit schematic designs, Mathematical modelling, Data analysis, Tunnelling electron microscopy, Scanning electron microscopy, VSM, PCB design, Characterisation and formulating, Magneto rheological fluids, Nano laboratory access and use of specialist Nano laboratory equipment.

Programmes: Proteus design suit, Visual studio, Complex Tunnelling/Scanning electron microscopy software.

Other Skills: Presentations, Group work and publication writing.
Prof. Yongbing Xu, University of York Heslington, York, YO10 5DD, United Kingdom
Dates
Occupation or position held Main activities and responsibilities

Name and address of employer
2004-2007
Satellite technician
Installation of satellite systems, Maintenance, Driving, customer advisor, schedule organizer, Sales and accounting.

Satellite systems, 7 Rio Vinalopo, La Colina, Javea, Spain.

\section*{Education and training}

Dates
Title of qualification awarded
Principal subjects/occupational skills
covered
Name and type of organisation providing education and training

2014-2019
PhD Physics
Analogue integrated circuits, Micro and nanometric technologies, Bio inspired algorithms and circuits Digital and analogue CAD design (cadence), Treatment of information, Electromagnetics, Advanced analogue design, Mathematical modelling and simulation using MATLAB (Including GUI interfaces).

Universidad de Sevilla, C/ S. Fernando, 4, C.P. 41004-Sevilla

Dates 2014-2015
Mark \(8.1(0-10)\)
Title of qualification awarded
Principal subjects/occupational skills

Name and type of organisation Page 2/4-Curriculum vitae of

Romaine, James
providing education and training

Title of qualification awarded Principal subjects/occupational skills covered

Name and type of organisation providing education and training

Dates
Title of qualification awarded
Principal subjects/occupational skills
covered
Name and type of organisation providing education and training

\section*{Personal skills and} competences Mother tongue(s)
Other language(s) Self-assessment European level ( \({ }^{*}\) )

Social skills and competences

Organisational skills and competences

Technical skills and competences

Universidad de Sevilla, C/ S. Fernando, 4, C.P. 41004-Sevilla
2009-2013
2:1
BEng Electronic engineering
Programming software/ Hardware (C, Java, Assembly, VHDL, M-code)
Math, Physics, Analogue/Nano electronics, Digital electronics
Control engineering, Communications, Project management, Electromagnetics

University of York, Heslington, York, YO10 5DD, United Kingdom

2008-2009
Access to Higher Education Diploma Computing, Lincoln College
Computer systems, Networks and communications, Web page design and production, Systems analysis and design, Presentation skills, Advanced database. Lincoln College,Monks Road, Lincoln, LN2 5HQ

\section*{English}

\section*{Spanish}
\begin{tabular}{|c|c|c|c|c|c|c|c|c|c|}
\hline & \multicolumn{3}{|l|}{Understanding} & \multicolumn{4}{|c|}{Speaking} & \multicolumn{2}{|r|}{\multirow[t]{2}{*}{Writing}} \\
\hline & Listening & & Reading & & Spoken interaction & & Spoken production & & \\
\hline C & Independent & C & Independent & C & Independent & C & Independent & C & Independent \\
\hline 1 & & 1 & & 1 & & 1 & & 1 & \\
\hline \multicolumn{10}{|l|}{(*) Common European Framework of Reference for Languages} \\
\hline
\end{tabular}
(*) Common European Framework of Reference for Languages

The ability to work and communicate well with others in order to achieve mutual goals, gained from my work experience. Solid presentation skills, gained from presenting my PhD work in various conferences such as BioCas. I am also a very social person who enjoys social events with work colleagues.
Organisation of large quantities of work with close deadlines along with self- dedication and discipline gained during university and through work experience. I also have to abide by very strict integration deadlines.
Analogue integrated circuits, Micro and nanometric technologies, Bio inspired algorithms and circuits, Digital and analogue CAD design (cadence), Treatment of information, Electromagnetics, Advanced analogue design, Mathematical modelling and simulation using MATLAB (Including GUI interfaces), Programming software/ Hardware (C, Java, Assembly, VHDL, M-code), Math, Physics, Analogue/Nano electronics, Digital electronics, Control engineering, Communications, Project management, Electromagnetics.

Computer skills and competences

Good control over all Microsoft office programs (Word, Excel, PowerPoint and Access).gained through a qualification from college and work experience.

Driving licence Full, category B
\begin{tabular}{lll} 
Referees & Current supervisor & Supervisor \\
& INSTITUTE OF MICROELECTRONICS & INSTITUTE OF MICROELECTRONICS \\
& Manuel Delgado Restituto & Ángel Rodríguez-Vázquez \\
& Department IMSE & Department IMSE \\
& mandel@imse-cnm.csic.es & angel@imse-cnm.csic.es \\
& +34954466666 &
\end{tabular}

\section*{Additional activities Teaching experience}
- 72 hours teaching circuits and systems at the University of Seville. Teaching gave me the opportunity to help others in the discipline of electronics. It also helped me perfect my communication skills and how to approach new learners to a subject. The practical laboratory sessions allowed me to show students how to build basic circuits and characterise them using theoretical and real values.

\section*{Courses}
- LabVIEW Core 1, National instruments
- Event-based auditory processing with spiking silicon cochleas and deep network
- Matlab beginner-Intermediate
- Matlab Advanced
- Arduino and robotics

\section*{Attended conferences}
- PRIME 2016, IEEE Circuits and systems society, 2016 12th Conference on Ph.D.Research in Microelectronics and Electronics (PRIME)
- BIOSENSORS 2016, Elsevier
- IEEE Biomedical Circuits and Systems Conference BioCAS 2014

This thesis introduces a state-of-the-art algorithm and indexing equation for the detection of phase synchronisation in pathological brains. When tested on Epileptic data the algorithm produced results similar to that of more complex methods, such as the Hilbert transform and phase locking value. The proposed algorithm produced an absolute sensitivity of over 80 \(\%\) for an FP/h of 0.75 and as much as \(90 \%\) at the upper limit of the \(95 \%\) confidence thresholds. Furthermore the algorithm allows for nearly a \(90 \%\) reduction in digital logic when compare to other methods with the total number of flip-llops, LUTs and slices of 112, 60 and 37 respectively.

In addition, a sub-threshold digital VLSI processor was designed. The main processor consits of 15 sub-processors" (including dedicated training and threshold calculation modules for patient specific epilepsy treatment and detection) and is capable of calculating the phase synchrony between 9 independent EEG signals over 8 epochs of time totalling 120 EEG combinations. The ASIC was designed in an AMS \(0.18 \mu \mathrm{~m}\) high voltage, low leakage technology using a fully custom 0.5 v threshold digital logic library to reduce total power consumption and operates from a main clock frequency of 2 KHz . Each sub processor consumes just 15 nW of power.

The core area of the design occupies only \(3.64 \mathrm{~mm}^{2}\), whilst the SPI input interface occupies \(0.091 \mathrm{~mm}^{2}\) and the output interface occupies \(0.063 \mathrm{~mm}^{2}\). Each synchronisation processor occupies \(0.04 \mathrm{~mm}^{2}\), whilst, each training and calculation module occupies \(0.066 \mathrm{~mm}^{2}\).
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[^0]:    ${ }^{a}$ Power consumption mainly due to the $4 \times 1288$-bit $\Sigma \Delta$ algorithmic ADCs. At 15 kHz parallel sample rate, the bank of ADCs dissipates 6.3 mW from a 3.3 V supply [54].

