A Low-Power Quadrature Digital Modulator

in 0.18 μm CMOS

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by

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ABSTRACT

Quadrature digital modulation techniques are widely used in modern communication systems because of their high performance and flexibility. However, these advantages come at the cost of high power consumption. As a result, power consumption has to be taken into account as a main design factor of the modulator.

In this thesis, a low-power quadrature digital modulator in $0.18\mu m$ CMOS is presented with the target system clock speed of 150 MHz. The quadrature digital modulator consists of several key blocks: quadrature direct digital synthesizer (QDDS), pulse shaping filter, interpolation filter and inverse sinc filter. The design strategy is to investigate different implementations for each block and compare the power consumption of these implementations. Based on the comparison results, the implementation that consumes the lowest power will be chosen for each block. First of all, a novel low-power QDDS is proposed in the thesis. Power consumption estimation shows that it can save up to 60% of the power consumption at 150 MHz system clock frequency compared with one conventional design. Power consumption estimation results also show that using two pulse shaping blocks to process I/Q data, cascaded integrator comb (CIC) interpolation structure, and inverse sinc filter with modified canonic signed digit (MCSD) multiplication consume less power than alternative design choices. These low-power blocks are integrated together to achieve a low-power modulator. The power consumption estimation after layout shows that it only consumes about 95 mW at 150 MHz system clock rate, which is much lower than similar commercial products.

The designed modulator can provide a low-power solution for various quadrature modulators. It also has an output bandwidth from 0 to 75 MHz, configurable pulse shaping filters and interpolation filters, and an internal $\sin(x)/x$ correction filter.

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DEDICATION

This thesis is dedicated to my wife and my parents.

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ABBREVIATIONS

ASIC	Application Specific Integrated Circuit
ATE	Automatic Test Equipment
ATPG	Automatic Test Pattern Generation
BPF	Band-Pass Filter
CIC	Cascaded Integrator Comb
CMOS	Complementary Metal Oxide Silicon
CSD	Canonic Signed Digit
DAC	Digital to Analog Converter
DDS	Direct Digital Synthesizer
DRC	Design Rule Check
DSP	Digital Signal Processor
FFT	Fast Fourier Transform
FIR	Finite Impulse Response
FPGA	Field Programmable Gate Array
FS	Full Scale
GUI	Graphical User Interface
HBF	Half-Band Filter
HDL	Hardware Descriptive Language
IC	Integrated Circuit
IF	Intermediate Frequency
IP	Intellectual Property
ISF	Inverse Sinc Filter
ISI	Intersymbol Interference
ITRS	International Technology Roadmap for Semiconductors
LO	Local Oscillator
LPF	Low-Pass Filter
LSB	Least Significant Bit

LVS	Layout Versus Schematic
MCSD	Modified Canonic Signed Digit
MSB	Most Significant Bit
PKS	Physically Knowledgable Synthesis
QAM	Quadrature Amplitude Modulation
QDDS	Quadrature Direct Digital Synthesizer
QLA	Quad Line Approximation
QPSK	Quadrature Phase Shift Keying
RF	Radio Frequency
RTL	Register Transfer Level
SNR	Signal to Noise Ratio
SOC	System on Chip
SQRC	Squared Root Raised Cosine
VGA	Variable Gain Amplifier
VLSI	Very Large Scale Integration

Chapter 1

Introduction

Transmitter and receiver are two major components for all the communication systems. The basic function of the transmitter is to take the information bearing signal produced by the source of information and modify it into a form suitable for transmission over a channel. The receiver operates on the received signal to produce an estimate of the original information bearing signal.

Traditional designs of analog transmitter employ the use of the phase locked loop, mixers, analog filters and amplifiers. Figure 1.1 shows an example of traditional analog transmitter. Digital baseband in-phase (I) and quadrature (Q) signals are converted to analog signals by digital to analog converters (DAC) and then fed into low-pass filters (LPF). Analog I/Q signals are upconverted to an intermediate frequency (IF) by mixing with the first local oscillator which goes through a phase splitter to provide in-phase and quadrature local oscillation (LO) signals. The outputs of the mixers are then summed. This IF signal is amplified, filtered and then mixed to the radio frequency (RF) by the IF variable gain amplifier (VGA), IF band-pass filter (BPF) and second local oscillator, respectively. The RF signal that has been processed by RF amplifier and RF band-pass filter is then ready to be fed to an antenna. As one can see from this figure, all the components are analog circuits. There are several disadvantages for this analog architecture. First, analog electronic circuits consume more space and power. Second, they are more subject to performance variations as a result of environmental factors such as temperature changes. Third, it is difficult to integrate these functions into one chip according to the current technology [1].



Figure 1.1 Analog transmitter.

In recent years, there is an increasing trend to replace most of these analog circuits with digital circuits and integrate them into one chip [1]. The advantage of this approach is that full digital control of the function is maintained as far as possible, and the limitations of analog design are minimized. Another trend in transceiver design is trying to reduce the cost and power consumption. It is becoming more and more important because it makes them feasible to be embedded into more types of electronic devices.

1.1 Research motivation

The ideal radio architecture brings the digital signal processing techniques as close as possible to the antenna. In this ideal architecture, the analog circuits are restricted to those which can not be performed digitally, i.e., antenna, RF filter and power amplifier. According to the newest technology, the closest towards this ideal architecture is the hybrid implementation, as shown in Figure 1.2, which consists of a digital subsystem and a analog subsystem. Compared with analog transceiver,



Figure 1.2 Hybrid implementation.

this architecture offers more flexibility, longer product life and lower cost; it is also more suitable for mass production. Devices such as digital signal processors (DSPs), field programmable gate arrays (FPGAs) and application specific integrated circuits (ASICs) can be used to realize the required digital functionality.

Although there are many advantages to using digital modulator in communication systems, power consumption is still a problem for high-performance quadrature digital modulator. For example, one commercially used quadrature digital modulator, AD9856 [2], consumes about 1100 mW at 150 MHz. The power consumption is unacceptable for most of the portable applications due to the limited battery capacity. Also, according to international technology roadmap for semiconductors (ITRS) 2005 report, "Power consumption is an urgent, short-term challenge. How to quickly shift from a performance-driven design procedure to a performance and power driven design procedure has to be solved. Design issues include high level power estimation, dynamic and leakage power reduction at different design stages and power optimization, etc [3]." As a result, power consumption has to be taken into account as a main design factor. Generally speaking, to achieve a low-power integrated circuit, many low-power design techniques can be used. These techniques can be applied at system level, algorithm level, circuit level and transistor level.

In this thesis, a fully digital modulator with low-power consumption is implemented, which is intended to function as a quadrature modulator and can be used in various portable devices where power and performance are critical. The designed modulator consists of pulse shaping filters, interpolation filters, a quadrature direct digital frequency synthesizer (QDDS) and an inverse sinc filter. Several low-power techniques are used to reduce the power consumption while maintaining high performance.

1.2 Research objectives

The objectives of the research work in this thesis are:

- To develop a quadrature digital modulator with less power dissipation
- To develop a novel low-power consumption QDDS that can be used in various

quadrature modulators and demodulators

• To investigate low-power design techniques and their application to quadrature digital modulator

• To develop a configurable digital quadrature digital modulator with high performance

1.3 Thesis outline

Chapter 2 reviews the principles of the digital modulator, including the principles of QDDS, pulse shaping filter, interpolation filter, digital modulation, DAC and inverse sinc filter.

Chapter 3 discusses integrated circuit (IC) design challenges and digital IC design flow that is used in this thesis. The main design flow described in this chapter follows CMC Microsystems' design flow. However, some changes have been made to make the whole design process more flexible and efficient.

Chapter 4 covers the circuit implementation details of the modulator. For the QDDS circuit, a novel architecture with low-power consumption is proposed. For the other blocks, several hardware efficient design approaches are considered as the possible choices.

Chapter 5 introduces high-level power estimation techniques and also presents the performance comparisons for each key block with different design options. The proposed QDDS is compared with conventional QDDS circuits. Pulse shaping filter, interpolation filter, inverse sinc filter are also compared with different design choices.

Chapter 6 concentrates on the functional verification of the final modulator which is implemented with the proposed QDDS and the other relatively low-power blocks. It also covers the power consumption estimation of the whole modulator.

Chapter 7 gives conclusions and several suggestions for future work.

Chapter 2

Background

As shown in Figure 2.1, a quadrature digital modulator consists of several key blocks: QDDS, pulse shaping filters, interpolation filters and inverse sinc filter. QDDS is used to generate sine/cosine reference carrier signals. Pulse shaping filters are used to limit the transmitting bandwidth and reduce intersymbol interference (ISI). Interpolation filters are used to increase sampling rate and inverse sinc filter is used to precompensate sinc distortion coming from the following DAC. This chapter provides the background related to these key blocks.



Figure 2.1 Digital quadrature modulator.

2.1 Quadrature direct digital synthesizer

Direct digital synthesizer (DDS) is a circuit which uses digital signal processing technique to generate a frequency-tunable output signal referred to a fixed frequency and high precision clock source [4]. As shown in Figure 2.2, a basic form DDS is composed of a precise reference clock, a phase accumulator, a sine look-up table and a DAC.

The phase accumulator can be an N bit counter that increments the stored



Figure 2.2 Block diagram of a basic DDS.



Figure 2.3 Digital phase wheel. As the vector rotates around the wheel, a corresponding sine wave is being generated.

number each time it receives a clock pulse. Figure 2.3 shows the diagram of digital phase wheel. The magnitude of the increment is determined by a digital word M, which sets how many points to skip around the phase wheel. The larger the M, the faster the phase accumulator overflows and completes the equivalence of a sine wave cycle.

The output from the phase accumulator addresses a sine look-up table which stores sine samples to generate a digital sine wave. The following DAC generates an analog sine wave in response to the digital input words from the sine look-up table. Low-pass filter is used to further smooth the sine wave output from the DAC so that a higher purity spectrum can be obtained. For any tuning word M, the output frequency of the DDS is

$$f_{out} = M \cdot \frac{f_{refclk}}{2^N},\tag{2.1}$$

where f_{out} is the output frequency of DDS, M is the binary tuning word, f_{refclk} is the reference clock frequency and N is the length in bits of the phase accumulator. It is clear that the frequency resolution is $f_{res} = \frac{f_{refclk}}{2^N}$.

Phase truncation is an important aspect of DDS. For example, to directly convert 32 bits of phase to corresponding 8 bit amplitude would require a 4 gigabytes ROM. It is impractical to implement such a huge ROM in a design. In real design, the solution is to use a fraction of the most significant bits of the phase accumulator output to provide phase information. This means that the N bits output from the phase accumulator is usually truncated to N_a bits. This truncation results in errors in the output signal. The worse case signal to noise ratio (SNR) for the basic DDS structure can be expressed by following equation [5]:

SNR (dB) =
$$10 \cdot \log_{10}(\frac{1}{\frac{\pi^2}{3}2^{-2N_a} + \frac{2}{3}2^{-2N_d}}),$$
 (2.2)

where N_a is the phase length after truncation and N_d is the amplitude word length stored in ROM.

Assume the maximum reference clock is 150 MHz and the phase accumulator is 32 bits. If the phase after truncation is 12 bits and the sine amplitude is stored with 12 bit accuracy, the frequency resolution, f_{res} , is $\frac{150 \times 10^6}{2^{32}} = 0.034$ Hz. If there is no compression applied to the sine ROM, the worse case SNR of the design is approximately $10 \cdot \log_{10}(\frac{1}{\frac{\pi^2}{3} \cdot 2^{-2N_a} + \frac{2}{3} \cdot 2^{-2N_d}}) = 66.3$ dB.

The DDS structure shown in Figure 2.2 can only generate one sine signal. Since the targeted application in this thesis is a quadrature digital modulator, quadrature digital reference carrier signals are desired. In other words, another ROM which stores cosine values has to be added to the basic DDS architecture to form a QDDS circuit.

2.2 Pulse shaping filter

As one can see from the system block diagram shown in Figure 2.1, I and Q data are processed by two kinds of digital filters. One is pulse shaping filter and the other is interpolation filter.

Rectangular pulses lead to a relatively large transmitting bandwidth because the frequency contents of a rectangular pulse have a $\sin(x)/x$ shape and the tails of the this sinc function decay slowly. This large signal bandwidth is not desirable for most of the bandwidth constrained communication systems. In order to reduce the bandwidth and mitigate ISI with adjacent pulses, these rectangular pulses must be filtered properly. Raised cosine filter is one of the pulse shaping filters that can limit the transmitting bandwidth of signals and avoiding ISI.

The frequency characteristic of the raised cosine filter can be described as [6]:

$$H_{rc}(f) = \begin{cases} T & \text{if } 0 \le |f| < \frac{1-\beta}{2T}, \\ \frac{T}{2} \{ 1 + \cos[\frac{\pi T}{\beta}(|f| - \frac{1-\beta}{2T})] \} & \text{if } \frac{1-\beta}{2T} \le |f| < \frac{1+\beta}{2T}, \\ 0 & \text{if } |f| \ge \frac{1+\beta}{2T}. \end{cases}$$
(2.3)

where T is the symbol duration, and β is a roll-off factor which takes a value between 0 to 1. The corresponding impulse response of a raised cosine filter has the form [6]:

$$h_{rc}(t) = \frac{\sin(\pi t/T)}{\pi t/T} \cdot \frac{\cos(\pi \beta t/T)}{1 - 4\beta^2 t^2/T^2}.$$
 (2.4)

The raised cosine impulse response and spectral characteristics for $\beta = 0, 0.5$ and 1 are illustrated in Figure 2.4. As one can see from this figure, larger β leads to smaller pulse tails and larger bandwidth.

In practical communication systems, the raised cosine filter is split evenly between transmitter and receiver, with each implementing a squared root raised cosine (SQRC) filter. The cascaded response of these two filters is equivalent to the response of the raised cosine filter. The frequency response of the square root raised



Figure 2.4 Raised cosine pulse and spectrum.

cosine filter is given as [7]:

$$H_{sqrc}(f) = \begin{cases} \sqrt{T} & \text{if } 0 \le |f| < \frac{1-\beta}{2T}, \\ \sqrt{\frac{T}{2}} \{1 + \cos[\frac{\pi T}{\beta}(|f| - \frac{1-\beta}{2T})]\} & \text{if } \frac{1-\beta}{2T} \le |f| < \frac{1+\beta}{2T}, \\ 0 & \text{if } |f| \ge \frac{1+\beta}{2T}. \end{cases}$$
(2.5)

The impulse response of the square root raised cosine filter is [7]:

$$h_{sqrc}(t) = 4\beta \cdot \frac{\cos((1+\beta)\pi t/T) + \frac{\sin((1-\beta)\pi t/T)}{4\beta t/T}}{\pi\sqrt{T}(1-(4Rt/T)^2)}.$$
 (2.6)

Equation (2.6) represents a noncausal pulse. To implement this SQRC filter in a communication system, the pulse is first delayed by an integer number of symbol periods, say mT, and truncated 2mT. The value of m is a tradeoff between simplicity and accuracy. The pulse is then sampled by taking k samples per symbol so that $T = kT_s$, where T_s is the sampling period. It is common to operate the filter at 4 or 8 samples per symbol. Replacing t by t - mT, letting $t = nT_s$ and $T = kT_s$ yields:

$$\frac{t}{T} \to \frac{nT_s - mkT_s}{kT_s} = \frac{n}{k} - m. \tag{2.7}$$

Substituting Equation (2.7) into Equation (2.6), the sampled version of SQRC filter can be expressed as:

$$h_{sqrc}(n) = 4\beta \frac{\cos[(1+\beta)\pi(\frac{n}{k}-m)] + \frac{\sin[(1-\beta)\pi(\frac{n}{k}-m)]}{4\beta(\frac{n}{k}-m)}}{\pi\sqrt{T}\{1-[4\beta(\frac{n}{k}-m)]^2\}}.$$
 (2.8)

It should be noted that impulse response truncation introduces a rectangular window. Filters using a rectangular window usually result in poor stopband response and passband ripples due to time discontinuity introduced by the rectangle window. These disadvantages can be alleviated by choosing a window function which does not have abrupt discontinuities in its time domain characteristics. Kaiser window is one of the window functions that can be used [8]. Applying Kaiser window leads to increased ISI level at the receiver end. The tradeoff between acceptable ISI and required spectral performance must be considered when choosing a window function.

Another problem is the implementation of the finite impulse response (FIR) filter with impulse response shown in Equation (2.8). Figure 2.5 illustrates the signal-flow of a direct form structure FIR filter. The FIR filter computes the current output sample as a weighted sum of the current input sample and N-1 past samples.

$$y(n) = \sum_{i=0}^{N-1} h(i)x(n-i), \qquad (2.9)$$

where y(n) is the output sequence, x(n) is the input sequence, and h(n) is the corresponding impulse response. In many applications the FIR filter is designed to have linear phase [6]. Consequently, the impulse response is symmetric and satisfies the relation

$$h(i) = h(N - 1 - i)$$
 where $0 \le i \le N - 1$. (2.10)

By using this symmetric characteristic, one can simplify the signal flow shown in



Figure 2.5 Signal flow graph of the direct form structure FIR filter.

Figure 2.5.

The pulse shaping filter in a quadrature digital modulator can also be an FIR filter with symmetric impulse response. From the theoretical point of view, the input data sequences are upsampled by k before being processed by the pulse shaping filters. The upsampled time series contains samples of the original inputs separated by k - 1 zero valued samples. Figure 2.6 shows an example that the input data sequence is upsampled by 4. This zero packed data sequence is then processed by the SQRC filter. The SQRC filter actually limits the bandwidth to the band of interest and computes output samples at an increased rate (k-to-1) relative to input rate, replacing the zero packed values with the interpolated values. Figure 2.7 shows the output sequence when the upsampled data sequence shown in Figure 2.6 has been processed by a SQRC filter, where the filter length is 8 symbols (4 samples per symbol) and the roll-off factor is 0.22.

2.3 Interpolation filter

Interpolation filters in a modulator are used to raise the sampling rate to allow the translation of the input signal spectrum to an intermediate frequency in the digital domain. Two interpolation filter structures are considered here, cascaded integrator comb (CIC) filter and half-band FIR filter. Both of these two structures are hardware-efficient.

• Cascaded integrator comb (CIC) filter

A CIC filter consists of an integrator section operating at the high sampling rate and a comb section operating at the low sampling rate [9]. From the theoretical



Figure 2.6 An example of 1-to-4 upsampling. "x" shows the input binary data and "o" shows the output after 1-to-4 upsampling.



Figure 2.7 Output sequence of a SQRC filter. "x" shows the input binary data and "o" shows the output sequence.

point of view, the CIC filter can either increase or decrease the sampling rate at the output relative to the input, depending on the filter architecture.

Figure 2.8 shows the basic structure of the CIC interpolation filter. The comb section operates at a low sampling rate, f_s/R , where R is the integer rate change factor. This section consists of N comb stages with a differential delay of M samples per stage. The differential delay factor, which is usually 1 or 2 in a practical system, is a filter design parameter used to control the filter's frequency response. The integrator section of the CIC filters consists of N ideal integrator stages operating at the high sampling rate, f_s . A rate change switch between two sections can cause a rate increase by a factor of R by inserting R - 1 zero valued samples between consecutive samples of the comb section output.

The system function for the composite CIC filter referenced to the high sampling rate, f_s , is

$$H_{CIC}(z) = \frac{(1 - z^{-RM})^N}{(1 - z^{-1})^N} = \left(\sum_{k=0}^{RM-1} z^{-k}\right)^N.$$
 (2.11)

The frequency response of CIC filter evaluated at $z = e^{(2\pi f/R)}$ is:

$$H_{CIC}(f) = \left[\frac{\sin(\pi M f)}{\sin(\pi f/R)}\right]^N,$$
(2.12)

where f is the frequency relative to the low sampling rate f_s/R .

CIC filter is chosen as one of the possible interpolation structures because it is



Figure 2.8 Block diagram of the CIC interpolation filter.

very hardware efficient. The advantages of CIC filter are: (1) no multipliers are required; (2) no storage is required for filter coefficients; (3) intermediate storage is reduced compared to the equivalent implementation using cascaded uniform FIR filters; and (4) the same filter design can be easily extended to a wide range of rate change factors.

For the CIC interpolation filter design, the minimum register width must be determined. Rounding can not be used because the small error in the integrator stages can cause the variance of the error to grow without bound and result in an unstable filter [9].

The minimum register width for *j*th filter stage, W_j , is determined by [9].

$$W_j = [B_{in} + \log_2 G_j]$$
 for $j = 1, 2, ..., 2N$, (2.13)

where B_{in} is the input register width, G_j is the maximum register growth up to jth stage, and [] represents for ceiling function. G_j can be calculated according to Equation (2.14).

$$G_{j} = \begin{cases} 2^{j} & \text{if } j = 1, 2, ..., N, \\ \frac{2^{2N-j}(RM)^{j-N}}{R} & \text{if } j = N+1, ..., 2N. \end{cases}$$
(2.14)

There is a special case for Equation (2.13). When M = 1, the equation used to calculate the minimum register width for Nth stage is expressed as:

$$W_N = B_{in} + N - 1$$
 if $M = 1$. (2.15)

• Half-band filter

Half-band filters are widely used in multirate signal processing applications when interpolating/decimating by a factor of two. A half-band low pass filter has a pass band bandwidth between $\pm \frac{1}{4}$ sampling rate for a two-sided bandwidth equal to half the sampling rate [10]. The impulse response of an ideal noncasual discrete filter



Figure 2.9 Impulse response and frequency response of a half band FIR filter with the length of 21.

can be shown as:

$$h_{hb}(n) = \frac{1}{2} \cdot \frac{\sin(n\pi/2)}{n\pi/2}.$$
 (2.16)

The impulse response and the corresponding frequency response of a casual halfband filter with the length of 21 are shown in Figure 2.9.

The impulse response of the half-band filter are all zero at the even index offsets from the center point of the filter. The coefficients with odd index offsets are symmetric about the filter center point. These two properties permit a half-band filter with the length of 2N + 1 to be implemented with only $\frac{N}{2}$ multiplications per output sample. This structure is very efficient for upsampling applications. The limitation for this filter is that the interpolation ratio can only be two. If several half-band filters are connected serially, the interpolation ratio can be expanded to the power of two.



Figure 2.10 I - Q format.

2.4 Modulation

To transmit a signal over the air, a carrier is modulated with the information to be transmitted. This process usually involves modulating the amplitude, frequency and/or phase of the carrier. A simple way to view the amplitude and phase is with polar diagram. The carrier becomes a frequency and phase reference and the signal is interpreted relative to the carrier. The signal can be expressed in polar form as a magnitude and a phase.

In digital communication, modulation is often expressed in terms of I and Q[11]. As shown in Figure 2.10, the I axis lies on the zero degree phase reference and the Q axis is rotated by 90 degrees. The signal vector's projection to the I axis is the I component and projection to the Q axis is the Q component. I/Q diagrams are particularly useful because they can mirror the way most digital communication signals are created using an I/Q modulator.

At the transmitter side, I and Q signals are mixed with LO. A 90 degree phase shifter is placed in one of the LO paths. Signals that are separated by 90 degrees are also known as being orthogonal to each other or in quadrature. A composite output signal is generated by combining these two signals. The main advantage of I/Q modulation is the convenience of combining independent signal components into a composite signal and later splitting the signal into its independent component parts.

At the receiver side, the composite signal with magnitude and phase information is mixed with the LO signal at the carrier frequency in two forms. One is at an arbitrary zero phase and another one has a 90 degree phase shift. The composite input signal is thus broken into an in-phase component, I, and a quadrature component Q. These two components are independent and orthogonal.

Quadrature modulation can be accomplished with quadrature modulators. Most quadrature modulators map the data to a number of discrete points on the I/Qplane. These are known as constellation points. As the signal moves from one points to another, simultaneous amplitude and phase modulation results.

• QPSK modulation

Quadrature Phase Shift Keying (QPSK) is a common type of phase modulation, which is widely used in applications including CDMA cellular systems, wireless local loop and DVB-S (Digital Video Broadcasting - Satellite). Quadrature means that the signal shifts between phase states which are separated by 90 degrees. The equation describing QPSK is:

$$s(t) = u(t)\cos(\omega_c t + \theta_m), \qquad (2.17)$$

where $\theta_m \in \{\frac{\pi}{4}, -\frac{\pi}{4}, \frac{3\pi}{4}, -\frac{3\pi}{4}\}$ and u(t) is a real value pulse. The constellation diagram for QPSK is shown in Figure 2.11. The signal shifts in increments of 90 degrees from 45 to 135, -45 or -135 degrees. These points are chosen as they can be easily implemented using I/Q modulator. The symbol rate is half of the bit rate.

• QAM modulation

Another member of quadrature digital modulation family is Quadrature Amplitude Modulation (QAM). QAM is used in applications including microwave digital radio, DVB-C (Digital Video Broadcasting - Cable) and modems. The equation describing QAM is:

$$s(t) = V_m u(t) \cos(\omega t + \theta_m), \qquad (2.18)$$



Figure 2.11 QPSK constellation.

where θ_m represents possible phase values, V_m represents possible amplitude values and u(t) is a real value pulse.

Here, 16-QAM is used as an example. The constellation diagram for 16-QAM is shown in Figure 2.12. There are four I values and four Q values resulting in a total of 16 possible states for the signal. Transit from any state to another state is allowed at every symbol time. In each symbol period, 4 bits, i.e., two bits I and two bits Q, can be sent.

For these quadrature modulations described above, I and Q data are mixed



Figure 2.12 16-QAM square constellation.

together in a modulator after the pulse shaping and interpolation stages. The whole modulation process can be described as:

$$y(t) = I(t)\cos(\omega_c t) - Q(t)\sin(\omega_c t).$$
(2.19)

The carrier frequency is decided by programming the QDDS circuit with an appropriate tuning word. The digital sine and cosine data is multiplied by the Q and I data respectively to create the quadrature components of the original data upconverted to the carrier frequency. The quadrature components are then digitally summed and passed on to the following stages. The key point is that the modulation is done totally digital, which eliminates the phase and gain imbalance and crosstalk issues typically associated with analog modulators [2].

2.5 Digital to analog converter (DAC)

At the end of digital modulator, a DAC is needed to convert digital signals into analog signals. There are several advantages with a DAC circuit on-chip. One advantage is that the power consumption can be reduced compared with the design which needs to drive an off-chip DAC. Another advantage is that it can avoid delays and line loading caused by interchip connections.

Figure 2.13 shows the conceptual block diagram of the DAC. The inputs of the DAC consists of a digital word of N bits and a reference voltage, V_{ref} . The voltage output, V_{out} , can be expressed as:

$$V_{out} = K V_{ref} D, \tag{2.20}$$

where K is a scaling factor and the digital word D is given as:

$$D = b_1 2^{-1} + b_2 2^{-2} + b_3 2^{-3} + b_N 2^{-N}, (2.21)$$

where b_i is the *i*th bit coefficient. It is preferred that the digital word is synchronously clocked. In this case, latches can be used to hold the word for conversion



Figure 2.13 Conceptual block diagram of a DAC.



Figure 2.14 Ideal input output characteristics for a 2 bit DAC.

and a sample and hold circuit is provided at the output [12].

Figure 2.14 shows the transfer characteristic of an ideal 2-bit DAC, where analog outputs occur at odd multiples of $\frac{1}{8}$ of the the full scale (FS) signal.

2.6 Inverse sinc filter

In a digital modulator, input data propagate through the device as digital stream. At the end of this processing, this digital stream must be converted into analog signals. The output signal of DAC that shows staircase pattern in Figure 2.14, is known as the zero-order hold function; i.e., the DAC holds its output con-
stant for the entire sampling period. The spectrum of zero-order hold function is a sinc envelope. The frequency response of the zero-order hold of the DAC is shown in Equation (2.22) [13].

$$H_{zo}(f) = \frac{\sin(\pi f/f_s)}{\pi f} e^{-j\pi f/f_s},$$
(2.22)

where f_s is sampling frequency.

The series of digital words presented at the input of the DAC represent the desired transmitting signal. Due to the zero-order hold effect of the DAC, the output spectrum of the output signal is the product of the sinc envelope and Fourier transform of the desired output signal. Thus, there is an intrinsic sinc distortion in the output spectrum.

If the desired output signal spectrum has the flat top amplitude, the output spectrum from a real world DAC is illustrated in Figure 2.15. The amplitude of the output signal and its images follows a sinc response. The amplitude roll off due to this envelop in a system is 3.92 dB in the first Nyquist zone. Since the sinc response is deterministic and predictable, it is possible to predistort the input data stream in a manner that compensates for the sinc envelop distortion. An inverse sinc filter (ISF) can be used in front of DAC which will pre-compensate for the roll off and maintain flat output amplitude over the bandwidth of the first Nyquist zone. The amplitude response of an ideal inverse sinc filter and its impact on the whole system is shown in Figure 2.16. The frequency response of this FIR filter is the inverse sinc function. Thus, the data sent through this filter is altered to correct for the sinc envelop distortion. This inverse sinc filter can also be bypassed depending upon applications.

The desired amplitude response of the inverse sinc filter can be described as:

$$H_d(f) = \frac{\pi f/f_s}{\sin(\pi f/f_s)}$$
 where $0 \le f \le f_s/2.$ (2.23)

With this desired response, a digital filter can be designed using the minimum mean



Figure 2.15 Output spectrum of a real world DAC.



Figure 2.16 Amplitude response of the ideal inverse sinc filter.

square error method. Given the desired frequency response, the impulse response of the designed filter is symmetrical and the filter length is odd. The equation used to get $h(0), h(1), ..., h(\frac{N-1}{2})$ is shown in Equation (2.24).

$$h(\frac{N-1}{2}-k) = \frac{2}{f_s} \int_0^{\frac{f_s}{2}} H_d(f) \cos(\frac{2\pi kf}{f_s}) df \qquad \text{for } k = 0, 1, \dots, \frac{N-1}{2}, \quad (2.24)$$

where N is the filter length. $h(\frac{N+1}{2})$, $h(\frac{N+3}{2})$,...,h(N-1) are symmetrical about the midpoint, i.e., $h(\frac{N-1}{2})$. The designed filter coefficients can be windowed to reduce ripples. Normally, the designed filter can compensate for the roll off and maintain flat output amplitude over the bandwidth of DC to 80% of the first Nyquist zone.

2.7 Summary

QDDS, pulse shaping filter, interpolation filter and inverse sinc filter are key blocks in a quadrature digital modulator. The background information related to these blocks are introduced in this chapter, including the basic form of DDS structure and its performance, principles and implementation of square root raised cosine filter, CIC filter and half-band filter. Quadrature digital modulation techniques, including QPSK and QAM, are also introduced. Since a DAC circuit is necessary at the end of a digital modulator, DAC and its zero-order hold characteristic are discussed. In order to precompensate the sinc distortion introduced by DAC, an inverse sinc filter has to be included. The design technique for this inverse sinc filter is also covered. These background information are the basis of the circuit implementation.

Chapter 3

Integrated Circuit Design Flow

The semiconductor industry has evolved from the first integrated circuit of early 1960s and matured rapidly since then. Early small-scale integrated circuits contained only a few logic gates. It is well known as Moore's law that the number of transistors on an integrated circuit for minimum component cost doubles every 18 months [14]. Current very large scale integration (VLSI) ICs can combine millions of gates on a single device.

Accompanied with the fast advancement of IC fabrication processing technology, IC designers face many design challenges. ITRS 2005 report listed a number of the challenges [3] in which two are related to design technology.

1. Design productivity, which is closely linked to system and design process complexity, and of course affecting design cost, is the most massive and critical challenge. Issues related to it include high level of abstraction, system integration and analog circuit synthesis, etc.

2. Manufacturability, that is, the ability to produce a chip in large quantities at acceptable cost and according to an economically feasible schedule, has been affecting the industry primarily due to lithography hardware limitations but will become a major crisis in the long term as variability in its multiple forms invades all aspects of a design. Design issues include device parameter variability, mixed-signal test and quality models, etc.

A good design flow can increase both design productivity and manufacturability. Since the IC design in this thesis is totally digital, the digital IC design flow chosen is described as follows.

3.1 Digital IC design flow

The design flow for creating VLSI digital circuits consists of a sequence of steps. Each step in the design flow either creates a database supporting the design flow, or verifies that the design meets specific requirements. Generally speaking, these steps can be separated into front-end design flow and back-end design flow. The front-end design flow focuses on the steps of preparing a gate-level netlist to be used in physical design of the chip. The back-end design flow focuses on steps of the physical design and ends up with a mask layout for fabrication. The main design flow described in this chapter is similar to the design flow provided by CMC microsystems [15]. Some modifications are made to make the whole design flow more flexible and more suitable for large designs.

3.1.1 Front-end design flow

Figure 3.1 shows the front-end design flow which includes the design steps before the physical layout of an IC design. The first step is register transfer level (RTL) coding which describes the functionality of a design. The RTL coding can be written in Verilog or VHDL. Verilog is chosen as the RTL coding language in this thesis.

The second step is to verify the functionality of the RTL code using an hardware descriptive language (HDL) simulator. A corresponding testbench must be provided for verification. The simulator used in this step is NC-Sim. The design and the testbench files, both in Verilog, must be compiled first. The command used to compile Verilog files is nevlog. It performs syntactic and semantic checking on the Verilog design units. If no errors are found, compilation produces an internal representation for each HDL design unit in the source files. Before one can run simulation, the design must be 'elaborated' to construct a design hierarchy based on the instantiation and configuration information in the design, to establish signal connectivity, and to compute initial values for all objects in the design. The command used for elaborating the design is called ncelab. The elaborated design hierarchy is stored as a simulation 'snapshot', which is the representation of the design that the simulator uses to run simulations. The snapshot is stored in a library



Figure 3.1 Block diagram of the front-end design flow.

database file along with the other intermediate objects generated by the compiler and elaborator. After compilation and elaboration, one can invoke the simulator, NC-Sim, to verify Verilog design.

The design flow provided by CMC microsystems suggests that users use NC-Sim in graphical user interface (GUI) mode. However, it is more convenient to verify the functionality in batch mode for large designs so that designers can observe inputs, outputs and internal nodes over a long period of time. Appendix A.1 shows one script example for invoking the simulator in batch mode.

After functional verification, the design is ready for synthesis. The logic synthesizer used is Synopsys Design Compiler. In order to synthesize the design, the same RTL code has to be analyzed and elaborated again. Similar with NC-Sim, the analysis step checks the syntax and semantics of Verilog files. The elaborate command replaces Verilog operators with equivalent combinational logic and determines correct bus sizes.

The next step is to set constraints for the design. The constraints here refer to defining the clock, specifying I/O cells, defining output load, etc. With these pre-set constraints, the design compiler can automatically create a gate-level netlist for a targeted processing technology. Synopsys Design Compiler can also report the timing, area and power consumption of the design.

The logic synthesis procedure described in the CMC microsystems' design flow are performed in GUI mode. Due to the fact that a design will be synthesized for several times with different constraints, an efficient way to use the logic synthesizer is to perform the synthesis in batch mode instead of GUI mode. Appendix A.2 shows one example script for using the logic synthesizer in batch mode. It should be noted that this example script contains basic synthesis steps only. One needs to modify it to meet different synthesis requirements.

To ensure the resulted gate-level netlist is correct, one needs to verify the functionality of the gate-level netlist following the same procedure as RTL code verification. With the verified gate-level netlist, one can insert the scan chain using Mentor Graphics DFTAdvisor. The purpose of inserting scan chain is to improve the testability of the fabricated chip for physical defects. This step involves replacing sequential elements with scannable sequential elements and then stitching the scan cells together into scan registers, or scan chains. Figure 3.2 shows one example before and after scan chain insertion [16]. Testing engineers can then use these serially-connected scan cells to shift data in and out when the design is in scan mode.

The next step after scan chain insertion is automatic test pattern generation (ATPG). Test patterns generated in this step are sets of 1s and 0s placed on primary input pins during manufacturing test process to determine if the chip is functioning properly. When the test pattern is applied, the automatic test equipment (ATE) determines if the circuit is free from manufacturing defects by comparing the fault-free output which is also contained in the test pattern with the actual output measured by the ATE. The tool used in this step is Mentor Graphics Fastscan. Both the DFTAdvisor and Fastscan are used under batch mode. The generated test patterns can be verified in NC-Sim.

After scan chain insertion, the gate-level netlist with scan chain is read back to Synopsys Design Compiler to finalize the design by adding I/O cells and output corresponding constraint files.

3.1.2 Back-end design

The back-end design flow, which consists of the design steps of physical layout, is shown in Figure 3.3. The flow begins with virtual design procedure, which involves I/O cells placement, power planning and trial placement and routing. During the trial placement and routing of the virtual design procedure, cells are placed and routed without consideration for timing. The next step is to use Cadence Physically Knowledgeable Synthesis (PKS) to optimize the design with the consideration of timing constraints and parasitic values. The design is optimized for three separate times to account for parasitics that are obtained during place and route to attain a high performance. It should be noted that all the optimizations in this step are based on an 'ideal' clock.





sin

sen

sin sen

sin

sen

clk

- (b) After scan chain insertion
- **Figure 3.2** One example to compare the circuit before and after scan chain insertion. After adding scan circuitry, the design has two additional inputs, sc_in and sc_en, and one additional output, sc_out. These extra ports will be used when the design is in scan mode.



Figure 3.3 Block diagram of the back-end design flow.

After the placement and optimization, clock tree synthesis can be performed. Cadence PKS treats clock tree as an entire sub-circuit and adds buffers into the tree during the clock tree synthesis process. With the physically inserted clock tree, optimizations based on the real propagated clock can be performed.

The design is ready for the final route and optimization after the clock tree insertion. With this step done, one needs to perform static timing analysis to make sure the routed design meets the timing goal.

The final steps before tape out are mainly to verify the physical layout of the design. These steps include layout versus schematic (LVS) verification and design rule check (DRC). LVS is to verify that the physical layout contains the same instances, nets and connectivity as the verified design netlist and DRC is to verify that the physical layout meets the foundrys design rule.

It is a good practice to carry out all the steps involved in back-end design in batch mode in stead of GUI mode. Appendix A.3 shows one script example for timing optimization after clock tree insertion using Cadence PKS.

It should be noted that the design flows of front-end design and back-end design shown in Figure 3.1 and Figure 3.3 assume that the design requirements can be met at every stage. In practical design, there will be several changes in iterations of the design or constraints at various design points until the design requirements are met.

3.2 Summary

To tackle the challenges of integrated circuit design productivity and manufacturability, it is very important to choose the right design flow. The whole integrated circuit design flow are generally split into front-end design flow and back-end design flow. Both of them are discussed step by step in this chapter. Compared with CMC microsystems' design flow, the design flow introduced here is more efficient and flexible as a result of extensive use of scripts for batch mode processing. Some simple scripts are also provided as examples.

Chapter 4

Circuit Design and Low Power Considerations

Low-power circuits can be achieved at different levels. At system level, dynamic power management can be used to dynamically reconfiguring systems to provide the requested services and performances with a minimum number of active components or a minimum load on such components. At algorithm level, different algorithms can be compared for their power consumptions to identify one with the lowest power consumption. At circuit level, parallelization implementation, multiple supply voltages, dynamic supply voltage scaling, retiming, etc., can be used to reduce power consumption. At transistor level, variable threshold transistors, dynamic threshold voltage scaling, input vector control, etc., can be used to reduce leakage power which has become more and more important in nanometric technologies. Most of the low-power techniques used in this thesis are at algorithm level. Some low-power techniques at system level and circuit level are also used.

4.1 Quadrature digital modulator

The detailed block diagram of the designed modulator is shown in Figure 4.1. Most of the interfaces in this modulator are chosen to be 12 bits. This interface width is chosen to be the same as [2]. The width of the interface between symbol generator block and pulse shaping block is decided by the modulation technique used. All the blocks in this modulator which are not working at system clock rate, i.e., pulse shaping filter and interpolation filter blocks, use clock split from system clock. This clock splitting technique causes clock skew, but as will be described in Chapter 5, total power consumption is less than the scheme where the circuits



Figure 4.1 The detailed block diagram of the designed quadrature digital modulator.



Figure 4.2 ROM design using quarter-wave symmetry.

operate at the same high clock speed. The maximum system clock rate is targeted at 150 MHz in this design, i.e., output bandwidth is from 0 to 75 MHz. This clock speed is enough for most of the real applications because the highest intermediate frequency is usually 70 MHz.

4.2 QDDS

4.2.1 ROM compression

In the conventional DDS design [17], a commonly used technique to design the phase-to-amplitude converting ROM is illustrated in Figure 4.2. The ROM stores only 0 to $\frac{\pi}{2}$ of sine wave instead of 0 to 2π , i.e., it uses quarter-wave symmetry to generate a full range sine wave. The most significant bit (MSB) determines the sign of the output and second MSB determines whether the phase between 0 to $\frac{\pi}{2}$ should be increasing or decreasing. The rest $N_a - 2$ bits are used to address a sine ROM.

In this design, a $\frac{1}{2}$ least significant bit (LSB) offset must be introduced in all phase addresses. If the phase address, N_a , is assumed to be 3 bits, Figure 4.3 shows the phase wheel comparison between no phase offset and $\frac{1}{2}$ -LSB phase offset. Figure 4.4 shows error comparison between them. As one can see from Figure 4.4, if quarter-wave ROM stores $\sin(0)$ and $\sin(\frac{\pi}{4})$, i.e., without phase offset, there are some errors introduced because one's complementor can't map the phase values without errors. If quarter-wave ROM stores $\sin(\frac{\pi}{8})$ and $\sin(\frac{3\pi}{8})$, i.e., with $\frac{1}{2}$ -LSB phase offset, one's complementor can map the phase values to the first quadrant without error. This $\frac{1}{2}$ -LSB offset is also necessary for all the ROM compression methods introduced later.



Figure 4.3 Phase wheel comparison between no phase offset and $\frac{1}{2}$ -LSB phase offset.



Figure 4.4 Error comparison between no phase offset and $\frac{1}{2}$ -LSB phase offset.

The conventional design only needs to store a quarter of the sine wave values without introducing any errors. However, the ROM size is still too big considering ROM is the most power hungry part in a DDS circuit [17]. One way to reduce the ROM size is Suntherland algorithm [18]. In this algorithm, the phase address of the quarter-wave, θ , is decomposed to three components; i.e., $\theta = \alpha + \beta + \gamma$.

$$\sin(\alpha + \beta + \gamma) = \sin(\alpha + \beta)\cos(\gamma) + \cos(\alpha + \beta)\sin(\gamma)$$
$$\approx \sin(\alpha + \beta) + \cos(\alpha)\sin(\gamma), \tag{4.1}$$

where α , β and γ are the MSBs, the middle bits, and the LSBs of the phase address, respectively. The variables α and β form a 'coarse' ROM address and the variables α and γ form a 'fine' ROM address. If the word lengths of α , β and γ are assumed to be A, B and C, computer simulations are usually used to determine the optimum partitioning of the ROM address. Assume the word length of the input phase address is 12 bits and output sine samples are also 12 bits, i.e., the phase address of the quarter-wave sine ROM is 10 bits and the output of quarter-wave sine ROM is 11 bits, Table 4.1 shows partition simulation results. Given the tradeoff between mean square error and ROM size, A = 4, B = 3 and C = 3 are optimum choices for this scenario, where the output of the coarse ROM is 11 bits and the output of the fine ROM is 5 bits. As one can see from this example, this method can compress the ROM size. The compression ratio achieved here is $\frac{2^{10} \times 11}{2^7 \times 11 + 2^7 \times 5} = 5.5$.

Based on the Suntherland algorithm, the sine phase difference method was introduced in [19] to reduce the size of coarse ROM. With the sine phase difference method, the coarse ROM stores the sine phase difference instead of the real sine values. The equation used to describe sine phase difference method is:

$$y(\theta) = \sin(\theta) - \frac{2\theta}{\pi}.$$
(4.2)

Since the maximum value of sine phase difference, $y(\theta)$, is less than $\frac{1}{4}$, this method can save 2 bits of word length of the data in the coarse ROM.

	$\overline{\mathrm{error}^2}$	ROM size (bits)
A = 6, B = 3, C = 1	2.7675×10^{-10}	$2^9 \times 11 + 2^7 \times 3 = 6016$
A = 4, B = 3, C = 3	7.4979×10^{-8}	$2^7 \times 11 + 2^7 \times 5 = 2048$
A = 3, B = 5, C = 2	7.5748×10^{-8}	$2^8 \times 11 + 2^5 \times 4 = 2944$
A = 3, B = 4, C = 3	3.0273×10^{-7}	$2^7 \times 11 + 2^6 \times 5 = 1728$
A = 3, B = 3, C = 4	1.1813×10^{-6}	$2^6 \times 11 + 2^7 \times 6 = 1472$
A = 3, B = 2, C = 5	4.4364×10^{-6}	$2^5 \times 11 + 2^8 \times 7 = 2144$
A = 2, B = 5, C = 3	1.1784×10^{-6}	$2^7 \times 11 + 2^5 \times 5 = 1568$
A = 2, B = 4, C = 4	4.6640×10^{-6}	$2^6 \times 11 + 2^6 \times 6 = 1088$
A = 2, B = 3, C = 5	1.8129×10^{-5}	$2^5 \times 11 + 2^7 \times 7 = 1248$
A = 1, B = 5, C = 4	1.7011×10^{-5}	$2^6 \times 11 + 2^5 \times 6 = 896$
A = 1, B = 3, C = 6	2.5962×10^{-4}	$2^4 \times 11 + 2^7 \times 8 = 1200$

Table 4.1 Comparison between different A, B, C partitions.

Double trigonometric approximation method is revised to reduce the coarse ROM size. The coarse ROM stores the errors between the sine phase difference and a triangle waveform. The double trigonometric line, $d(\theta)$, can be expressed as:

$$d(\theta) = \begin{cases} \frac{\theta}{2\pi} & \text{if } 0 \le \theta < \frac{\pi}{4}, \\ \frac{1}{4} - \frac{\theta}{2\pi} & \text{if } \frac{\pi}{4} \le \theta \le \frac{\pi}{2}. \end{cases}$$
(4.3)

Because the maximum error of the double trigonometric approximation is less than $\frac{1}{8}$, this method can save 3 bits of word length of the data in the coarse ROM. The data for $0 \le \theta < \frac{\pi}{4}$ are generated by shifting right the phase, $\frac{2\theta}{\pi}$, by 2 bits. The data for $\frac{\pi}{4} \le \theta \le \frac{\pi}{2}$ are symmetric and can be accomplished by a complementor.

Quad line approximation (QLA) method [17] can further compress coarse ROM size. Similar to the double trigonometric approximation, the coarse ROM only stores the errors between the sine phase difference and the quad line waveform.

The quad line waveform, $q(\theta)$, is expressed as follows:

$$q(\theta) = \begin{cases} \frac{\theta}{\pi} & \text{if } 0 \le \theta < \frac{\pi}{8}, \\ \frac{1}{16} + \frac{\theta}{2\pi} & \text{if } \frac{\pi}{8} \le \theta < \frac{\pi}{4}, \\ \frac{1}{16} - \frac{\theta}{2\pi} + \frac{1}{4} & \text{if } \frac{\pi}{4} \le \theta < \frac{3\pi}{8}, \\ \frac{1}{2} - \frac{\theta}{\pi} & \text{if } \frac{3\pi}{8} \le \theta \le \frac{\pi}{2}. \end{cases}$$
(4.4)

The data for $0 \le \theta < \frac{\pi}{8}$ are generated by shifting right the phase, $\frac{2\theta}{\pi}$, by 1 bits. The data for $\frac{\pi}{8} \le \theta < \frac{\pi}{4}$ are generated by shifting right the phase by 2 bits and by changing the first and second MSBs of the phase to "10". These data are implemented with a MUX. The data for $\frac{\pi}{4} \le \theta \le \frac{\pi}{2}$ are symmetric and can be accomplished by a complementor.

Since the maximum value of QLA errors is less than $\frac{1}{16}$, the QLA method can save 4 bits of word length of the data in the coarse ROM. The waveforms of sinephase difference, double trigonometric approximation, QLA are shown in Figure 4.5. The errors of double trigonometric approximation and QLA methods are also shown in the same figure.

Table 4.2 compares different implementation choices for the coarse ROM. As the QLA method can save 4 bits of the word length for the coarse ROM with simple additional circuits, this method is chosen as the DDS implementation structure in the modulator. For a DDS ROM with 12 bits phase address and 12 bits output sine samples, the conventional design needs a $2^{10} \times 11$ bits ROM. Based on the Suntherland algorithm and the simulation results shown in Table 4.1, the input phase address can first be decomposed to α , β and γ with lengths of 4, 3 and 3 respectively. Together with the QLA method, the ROM can be implemented with a $2^7 \times 7$ bits coarse ROM and a $2^7 \times 5$ bits fine ROM. The total compression ratio achieved is $\frac{2^{10} \times 11}{2^7 \times 7 + 2^7 \times 5} = 7.33$. The implementation block diagram of such a sine-to-amplitude converting ROM using QLA method is shown in Figure 4.6. Similar to the conventional design shown in Figure 4.2, the second MSB determines whether the amplitude is increasing or decreasing. { α, β } is used to address the coarse sine



Figure 4.5 Curves of sine-phase difference, double trigonometric approximation and QLA and the error curves of double trigonometric approximation and QLA.

ROM and recover the compression from the sine phase difference method and QLA method. $\{\alpha, \gamma\}$ is used to address the fine sine ROM. These four outputs are added together to create a half sine wave. MSB is then used to determine the sign of the output and create a full sine wave.

Approximation method	Approximation function	Saved bits	Additional circuits
Without approximation	$\sin(heta)$	-	-
Sine phase approximation	$\frac{2\theta}{\pi}$	2 bits	1 adder
Double Trigonometric	d(heta)	3 bits	2 adders 1 complementor
QLA	q(heta)	4 bits	2 adders 1 complementor 1 MUX

Table 4.2Comparison between various sine approximation
methods to reduce the coarse ROM output bits.



Figure 4.6 Sine phase to amplitude converter using QLA method.

An example is used here to demonstrate how the sine-to-amplitude converting ROM shown in Figure 4.6 works. If the 12-bit input is assumed to be 0B000110001101, the corresponding phase is $\frac{2\pi \times 397}{2^{12}} + \frac{1}{2} \times \frac{2\pi}{2^{12}}$ and the ideal output is 0.572669. Since the second MSB is zero, $\{\alpha, \beta, \gamma\}$ is the least significant 10 bits of the input and α , β , γ are 0B0110, 0B001, 0B101, respectively. Binary word $\{\alpha, \beta\}$ is used to address the coarse sine ROM and the output is 0B0110010. Binary word



Figure 4.7 Errors for QLA sine phase to amplitude converter.

 $\{\alpha, \gamma\}$ is used to address the fine sine ROM and the output is 0B01110. Because $\alpha(3)$ is 0 and $\alpha(2)$ is 1, output of mux is 0B1010001. Thus, output from addition is $\{00, 1010001, 00\} + \{0110001, 0000\} + \{0000, 0110010\} + \{000000, 01110\} = 0B10010010100$. Since the MSB of the input is 0, the final output remains 0B10010010100, which represents for $\frac{1172}{2^{11}} = 0.572266$. The output error for the input is approximately 0.572669-0.572266=0.000403. Errors for the full sine wave is shown in Figure 4.7. As one can see from this figure, the maximum error is less than 1.6×10^{-3} . The mean square error for the full sine wave is 3.169×10^{-7} .

4.2.2 Quadrature outputs

Since the application is a quadrature modulator, quadrature outputs from DDS are required to provide sine/cosine carrier references for the modulator. In the QDDS circuit presented in this thesis, the word lengths of the phase accumulator and the truncated phase address, N and N_a , are 32 bits and 12 bits, respectively. The output word length, N_d , is 12 bits. For this application, one sine phase-toamplitude converting ROM and one cosine phase-to-amplitude converting ROM are required. If both sine and cosine samples from 0 to $\frac{\pi}{2}$ are stored, the size of the ROM will be doubled. Since sine samples from 0 to $\frac{\pi}{4}$ are the same as cosine samples from $\frac{\pi}{2}$ to $\frac{\pi}{4}$ and sine samples from $\frac{\pi}{4}$ to $\frac{\pi}{2}$ are the same as cosine samples from $\frac{\pi}{4}$ to 0, only the sine and cosine samples from 0 to $\frac{\pi}{4}$ need to be stored. The third MSB and the second MSB are XORed to select the data between 0 to $\frac{\pi}{4}$ sine samples and 0 to $\frac{\pi}{4}$ cosine samples. Because only 0 to $\frac{\pi}{4}$ sine and cosine samples are stored, the lowest 9 bits of the 12 bits phase address are actually needed for the sine and cosine look up tables. This 9-bit phase is decomposed to $\alpha+\beta+\gamma$ according to the Suntherland algorithm. Since the data stored in 0 to $\frac{\pi}{4}$ sine ROM and 0 to $\frac{\pi}{4}$ cosine ROM are the same as a 0 to $\frac{\pi}{2}$ sine ROM, the simulation data shown in Table 4.1 is still applicable for determining the wordlength of α , β and γ . The only difference is that the actual word length of α is A-1 now. Given the relationship between mean square error and ROM size, the word lengths of α , β and γ are chosen to be 3, 3 and 3, respectively. The coarse sine ROM and coarse cosine ROM are then further compressed by the sine phase difference method and QLA method. Since the phase of stored samples are from 0 to $\frac{\pi}{4}$, only the two expressions between 0 to $\frac{\pi}{4}$ shown in Equation (4.4) are used. The data for the phase between 0 to $\frac{\pi}{8}$ are generated by shifting right the phase by 1 bit and the data for the phase between $\frac{\pi}{8}$ to $\frac{\pi}{4}$ are generated by shifting right the phase by 2 bits and changing the highest two bits to "10".

The block diagram of the proposed QDDS is shown in Figure 4.8. The sizes for coarse sine ROM, fine sine ROM, coarse cosine ROM and fine cosine ROM are $2^6 \times 6$, $2^6 \times 5$, $2^6 \times 7$ and $2^6 \times 4$ bits, respectively. Instead of designing four ROMs with different sizes, the word lengths of the coarse sine ROM and fine cosine ROM are increased by 1 bit. As a result, the two coarse ROMs are $2^6 \times 7$ bits and the two fine ROMs are $2^6 \times 5$ bits. Compared with the conventional design which needs two $2^{10} \times 11$ bits ROM, the total ROM compression ratio achieved is $\frac{2 \times 2^{10} \times 11}{2 \times 2^6 \times 7 + 2 \times 2^6 \times 5} = 14.7.$

As one can see in Figure 4.8, additional adders and muxes are needed to reconstruct the output sine and cosine waves. These extra hardware are worthwhile considering the savings from the area and power. It should be noted that these



Figure 4.8 Proposed QDDS architecture.

ROM compression methods used introduce extra compression noises.

4.3 Pulse shaping filter

4.3.1 Polyphase structure

As described in Section 2.2, input data sequences are upsampled by k before being processed by the pulse shaping filter. That is, the original data are separated by k - 1 zero valued samples. The zero packing process shown in Figure 2.6 helps visualize the process, not to offer implementation instructions. Equation (2.9) indicates that only the non zero samples of the input data contribute to the output samples. Since these zero packed samples do not contribute to the filter output, they are usually not inserted in the input data sequences. Tracking the position of these non zero samples to determine which coefficients interact with the input data samples is equivalent to the polyphase partition of the filter. The strategy of polyphase partition is shown in the following equations.

$$H(z) = \sum_{n=0}^{N-1} h(n) z^{-n}.$$
(4.5)

$$H(z) = \sum_{r=0}^{k-1} z^{-r} \sum_{n=0}^{N/k-1} h(r+nk) z^{-nk}.$$
(4.6)

$$H(z) = \sum_{r=0}^{k-1} z^{-r} H_r(z^k).$$
(4.7)

Equation (4.5) is the Z-transform of the standard FIR structure corresponding to Equation (2.9). Equation (4.6) is the polyphase partition of the same filter representing the filter as a sum of successively delayed subfilters with coefficients separated by stride of k samples. Finally, Equation (4.7) is a compact representation of Equation (4.6) where the rth stage $H_r(z^k)$ of the polyphase filter is formed by the coefficient set that starts at index r and increments in steps of length k.

Figure 4.9 shows the block diagram of a 1-to-k upsampling pulse shaping filter using polyphase structure based on Equation (4.6), Equation (4.7) and the noble identity of a upsampler , which indicates that the resampler can be slid through the



Figure 4.9 An efficient implementation of 1-to-k upsampling polyphase filter.

filter and replace the k units of delay at the output clock rate with one unit delay at the input clock rate [10]. An 1-to-k upsampling pulse shaping filter is implemented by moving to different coefficient sets at each time.

The block diagram shown in Figure 4.9 can be further simplified by utilizing the symmetric characteristic of the pulse shaping filter's impulse response; thus, only half of the coefficients needs to be stored in memory, such as register files. The user configured coefficients are loaded into these register files during the initialization phase.

4.3.2 Design considerations of the pulse shaping filter

The pulse shaping filters apply pulse shaping to the incoming digital signals. An ideal SQRC shaping pulse is given in Section 2.2. Two parameters must be considered to implement this filter in a digital system. One parameter is the filter length after the impulse response has been delayed and truncated, and the other is the length of the digital word to represent a coefficient. The length of the SQRC filter determines the frequency response of the SQRC filter. If the truncated impulse response is too short, then the resulting filter either can not have enough stopband rejection, or has big ripples in the passband. Since the stopband rejection and passband ripple are very important for most of the communication systems, the truncated impulse response must be long enough to meet the system specification. The truncated impulse response can also be windowed to further reduce the passband ripple and stopband rejection. However, applying another window increases ISI. For a real design, the trade-off between the desired frequency response, acceptable ISI and the reasonable hardware costs should be considered.

In this design, the length of the SQRC filter is chosen to be 32 symbols and 4 samples per symbol. Each coefficient is quantized with 14 bits. It should be noted the SQRC filter designed in Matlab has an odd number of coefficients. It is not easy to implement an odd number of coefficients in hardware. To simplify the hardware design, an even number of coefficients is preferred. An even number of coefficients can be accomplished by doubling the desired sample rate, and then down sampling the impulse response by a factor of 2 [20]. According to the design of this thesis, there are $32 \times 4 = 128$ coefficients. Users can configure these coefficients according to their own applications.

Figure 4.10 is the impulse response of a SQRC filter example and Figure 4.11 is the corresponding frequency response. The roll-off factor used in Figure 4.10 and Figure 4.11 is 0.22 and the impulse response is windowed by Kaiser window, where β for Kaiser window is 2.2.

The detailed implementation block diagram of SQRC filter is shown in Figure 4.12, which utilizes the polyphase structure and the symmetric characteristic of the impulse response. Because this filter has a built-in four times upsampling function, all the circuits except the input data registers run at 4×symbol rate.

4.3.3 Quadrature processing

It is clear that the pulse shaping filter in a quadrature modulator must process I and Q data. There are two general approaches to this filter design for a quadrature modulator. The first approach uses two pulse shaping blocks to process I and Q data separately. The second approach uses only one pulse shaping block to process I and Q data by interleaving them in time. The processing speed of the second approach must be twice faster than the first one. The power consumptions of these two implementations will be discussed in the next chapter.



Figure 4.10 An example of the SQRC impulse response.



Figure 4.11 The frequency response of the SQRC filter whose impulse response is shown in Figure 4.10.



Figure 4.12 Block diagram of the SQRC filter.

4.4 Interpolation filter

The interpolation filters following the pulse shaping filter are used to increase the sampling rate. Two hardware efficient interpolation filter structures are considered here. One is CIC filter and the other is half-band FIR filter.

4.4.1 Design of CIC filter

As described earlier, the targeted system clock frequency is 150 MHz. The CIC filter block diagram shown in Figure 2.8 can not meet this timing requirement. A pipelined CIC structure is used in the system. Figure 4.13 is the block diagram of implemented CIC filter. As shown in Equation (2.12), the frequency response of the CIC filter depends on three factors: the rate change factor R, the order of the filter N and the differential delay M. In the design of this thesis, M and N are fixed at 1 and 4. The rate change factor, R, is the only variable parameter. The available choices for R are 4, 8, 16 and 32. According to those design parameters, Equation (2.12) which describes the CIC frequency response can be re-written as:

$$H(f) = \left[\frac{\sin(\pi f)}{\sin(\pi f/R)}\right]^4 \quad \text{where } R \in \{4, 8, 16, 32\}.$$
(4.8)

Figure 4.14 shows the periodic spectrum of the zero packed time series after the processing of the pulse shaping filter and the frequency response of the 1-to-4 CIC filter and Figure 4.15 shows the periodic spectrum of the zero packed time series after the processing of the pulse shaping filter and the frequency response of the 1-to-8 CIC filter. One can clearly see the effect of the CIC spectral zeros on the up-sampled input time series from the figures. It is also clear that there is frequency range of the data to be transmitted. The degree of the impact of the attenuation introduced by CIC filter is application specific. It is shown in the result of [9] that if less attenuation is desired, the higher rate change factor should be used. Alternatively, data can be precompensated through a filter which has the inverse CIC frequency response. Because the coefficients of the shaping filter are configurable, users can combine the pulse shaping filter and the inverse CIC filter. Then the resulting



Figure 4.13 Pipelined CIC interpolation filter.



Figure 4.14 Spectral response of 1-to-4 CIC interpolator. Solid line shows the periodic spectrum of the zero packed time series and dashed line shows the frequency response of the CIC filter with rate change factor of 4.



Figure 4.15 Spectral response of 1-to-8 CIC interpolator. Solid line shows the periodic spectrum of the zero packed time series and dashed line shows the frequency response of the CIC filter with rate change factor of 8.

impulse response of the shaping filter should be the convolution of the two impulse responses, the impulse response of the pulse shaping filter and the impulse response of the inverse CIC filter.

As mentioned earlier, the CIC filter is designed to handle rate change factors of R = 4, 8, 16 and 32. The input and output register widths are all 12 bits. Since the same filter will be used over a range of rate change factors, maximum register widths must be chosen over all the rate change factors. These maximum widths occur at the maximum rate change factor, i.e., R = 32. The register widths are calculated according to Equation (2.13) and Equation (2.15). The register widths for each stage are 13, 14, 15, 15, 15, 19, 23 and 27 respectively. The number of LSB's discarded going into the output register is 6, 9, 12 and 15 for the rate change factor of 4, 8, 16 and 32, respectively.

4.4.2 Design of half-band filter

To reach the similar image rejection ratio of the designed 4th order CIC filter, the length of the half-band FIR filter is at least 13. Since the interpolation ratio of the designed CIC filter is limited to 4, 8, 16 and 32, two-, three-, four- and fivehalf-band FIR filters can be cascaded to achieve the same interpolation ratio as the CIC filter.

Figure 4.16 shows the periodic spectrum of the zero packed time series after the processing of the pulse shaping filter and the frequency response of two cascaded half-band FIR filters. Figure 4.17 shows the periodic spectrum of the zero packed time series after the processing of the pulse shaping filter and the frequency response of three cascaded half-band FIR filters.

The half-band FIR filter of the length of 13 is implemented according to the polyphase half-band FIR filter shown in [10]. The input data sequence is theoretically upsampled by 2 before being processed by a half-band filter, i.e., one zero valued sample is inserted between two input samples. This is very similar to the situation described in Section 4.3.1; thus, the half-band filter can also be partitioned into a pair of polyphase filters instead of inserting zero valued samples. The



Figure 4.16 Spectral response of two cascaded half-band FIR filters. Solid line shows the periodic spectrum of the zero packed time series and dashed line shows the frequency response of the two cascaded half-band FIR filters.



Figure 4.17 Spectral response of three cascaded half-band FIR filters. Solid line shows the periodic spectrum of the zero packed time series and dashed line shows the frequency response of the three cascaded half-band FIR filters.



Figure 4.18 Polyphase half-band filter.

strategy of partitioning a polyphase half-band filter with length of 2N + 1 is shown in the following equation.

$$H(z) = \sum_{n=0}^{2N} h(n) z^{-n}$$

=
$$\sum_{n=0}^{N} h(2n) z^{-2n} + z^{-1} \sum_{n=0}^{N-1} h(2n+1) z^{-2n}$$

=
$$H_0(z^2) + z^{-1} H_1(z^2).$$
 (4.9)

Based on the Equation (4.9) and the noble identity of a upsampler [10], half-band FIR filter can be implemented with polyphase architecture. Figure 4.18 shows the block diagram of the polyphase half-band filter for even N in Equation (4.9).

4.5 Inverse sinc filter

An FIR filter with inverse sinc response can be designed using Equation (2.24). The filter length is chosen to be 9 and the synthesized impulse response is windowed with the Kaiser window, where the parameter β is chosen to be 2.8. The main purpose of applying this window is to reduce ripples of the combined system frequency response when this inverse sinc filter is being used. The impulse response after applying the Kaiser window is shown in Figure 4.19.

The frequency responses of the sinc distortion, the designed inverse sinc filter and the combined system are shown in Figure 4.20. As shown in this figure, the



Figure 4.19 Impulse response of the designed inverse sinc filter.



Figure 4.20 Frequency responses of the sinc distortion, ISF and the combined system.

designed inverse sinc filter can compensate for the sinc distortion and maintain the flat output amplitude (less than 0.1 dB) over the bandwidth of 0 to 80% of the first Nyquist zone. Using longer filter to implement this inverse sinc filter can lead to less ripple and wider working bandwidth. For example, if the filter is implemented with the length of 19, the ripple is less than 0.04 dB over the bandwidth of 0 to 90% of the first Nyquist zone. However, for high clock speed, longer length will increase the complexity of the filter and consume more power.

It should also be noted that the inverse sinc filter exhibits an insertion loss of about 3 dB. Thus, signal levels at the output port with this filter bypassed are 3 dB higher than with this filter engaged. For relatively wide bandwidth application, the benefits of the inverse sinc compensation usually outweighs the 3 dB loss in the output level. The decision of using this filter or not is related to the specific application.

In order to implement this filter, the coefficients have to be quantized first. The coefficients that are scaled to represent integers are listed in Table 4.3. Since the impulse response of this filter is symmetrical about the center, the signal flow for FIR filter shown in Figure 2.5 can be simplified. As shown in Figure 4.21, in order to reduce the number of multipliers, the symmetrical taps outputs are added together before they are multiplied by the coefficients.

h(n)	Coefficients	Scaled coefficients (12-bit quantization)
h(0) = h(8)	0.0016	3
h(1) = h(7)	-0.0057	-12
h(2) = h(6)	0.0179	37
h(3) = h(5)	-0.0693	-142
h(4)	0.8109	1660

Table 4.3Coefficients for the designed inverse sinc filter.


Figure 4.21 Signal flow graph of symmetrical FIR filter.

4.5.1 Multiplication for inverse sinc filter

Because all the multiplications in this filter deal with constant integer, they can be implemented using a network of binary shifts, adders and substractors instead of using real multipliers. In an integrated circuit implementation, binary shifts (scaling by a power of 2) can be replaced by hardwiring without using logic gates. Logic gates are only required to implement adders and substractors. The hardware cost of multiplier is thus approximately proportional to the number of adders and substractors.

In a binary multiplier, a constant C is represented as:

$$C = \sum_{i=0}^{n} c_i 2^i, \tag{4.10}$$

where the digits c_i are taken from the set $\{0, 1\}$. If P of the digits c_i are nonzero, to form the product, P shifted values of the multiplicand must be added, requiring P-1 additions.

In signed digit notation, c_i shown in Equation (4.10) are taken from the set $\{-1, -1, -1\}$

h(n)	Scaled coefficients	Binary	CSD	MCSD
h(0) = h(8)	3	11	10-1	11
h(1) = h(7)	12	1100	10-100	1100
h(2) = h(6)	37	100101	100101	100101
h(3) = h(5)	142	10001110	100100-10	100100-10
h(4)	1660	11001111100	10-1010000-100	11010000-100

Table 4.4Comparison of binary, CSD and MCSD representa-
tions for the coefficients of the inverse sinc filter.

0, 1} instead of just {0, 1}. Assume hardware cost of implementing the adders and subtractors are the same and both are referred to as adders. The signed digit representation which requires the fewest adders is known as canonic signed digit (CSD) representation [21]. In fact, the addition and subtraction can not be considered as the same cost of operations. An improved algorithm, modified canonic signed digit (MCSD) algorithm, uses -1 only when the total number of operations can be reduced [22].

Here, the inverse sinc filter coefficients are used as an example to compare different representations. As shown in Table 4.4, the absolute value of scaled h(4), i.e., 1660, is represented as {11001111100} by binary representation, {10-1010000-100} by CSD representation, {11010000-100} by MCSD representation. To implement $x \times h(4)$, binary representation requires 6 adders, CSD representation requires 1 adder and 2 substractors, and MCSD representation requires 2 adders and 1 substractors. These three implementation methods for $x \times h(4)$ are shown in Figure 4.22, where "<<" denotes left-shift. It is clear that CDS and MCSD representations lead to much less hardware than binary representation. Therefore, the inverse sinc filter is implemented with CSD and MCSD multiplication methods. The power consumptions of these methods will be compared in following chapter.

4.5.2 Clock gating

Clock gating, which is one of the most well-known low-power techniques, is an effective way to reduce the power consumption in digital circuits. This technique is



Figure 4.22 Comparison of the three different ways to implement $x \times h(4)$.

also implemented in Synopsys Power Compiler [23]. The goal of this technique is to disable or suppress transitions from propagating to parts of a clock path under a certain condition. The dynamic power of a digital Complementary Metal Oxide Silicon (CMOS) circuit is proportional to clock frequency and the square of the supply voltage [24]. Power can be saved by reducing the clock frequency (in the limit by stopping), or by reducing the supply voltage (in the limit by powering off the components). Note that the two limiting cases, clocking freezing and powering off, are applicable to idle components [25]. When there are idle digital components, clock gating is a commonly used technique for saving power. Clock gating technique

Without clock gating	Clock gating
always @ (posedge clk) if (enable) q <= d;	always @ (enable or clk) if (!clk) latch_output=enable; assign gated_clk = latch_output&clk always @ (posedge gated_clk) q <= d;

Table 4.5Verilog codes of a flip-flop without clock gating and
one with clock gating.



(a) Without using clock gating

(b) Using clock gating

Figure 4.23 Implementation comparison between a flip-flop without clock gating and with clock gating.

can be used at module level or register level in a system. Module level clock gating involves shutting off an entire block or module in a design if the block or module is used only for a specific mode. At the register level clock gating, the clock to a single register or a set of registers is gated. The registers in this application do not receive the clock signal when no new data are loaded. By using this technique, the clock of the idle components will be stopped during idle period. Power savings can be achieved by stopping the clock of registers and propagating signals from combinational logic circuits due to the freezing of data in registers.

A flip-flop without clock gating and with clock gating are compared here. Ta-



Figure 4.24 The mechanism of using latch to prevent the glitch on the gated clock net.

ble 4.5 shows Verilog code comparison and Figure 4.23 shows the corresponding implementations.

As shown in Figure 4.23, a latch and an AND gate are used in the clock gating implementation. The main reason for using a latch is to prevent the glitches on the gated clock since its changes happen during the low phase of the clock. This mechanism is shown in Figure 4.24. When the clock is low, the latch is enabled. The enable input is propagated to the latch output. In the mean time, when the clock arrives, it gets propagated to the gated clock net, without any glitches because the latch output is stable for sufficient time to meet the flip-flop's setup requirements. When the enable input goes low, output from the AND gate and is also low preventing the clock from being propagated to the gated clock net. This makes the gated clock net to be low without any switching activity.

Since whether to use the inverse sinc filter block is application dependant, module level clock gating technique is used to shut off the clock signal for this block when users choose not to use it. The block diagram is similar to the one shown in Figure 4.23(b) except that the register is replaced with the inverse sinc filter block.

4.6 Multipliers

Since the frequency of the output IF signal is tunable, real digital multipliers are required to multiply the outputs of the QDDS and the outputs of the interpolation filters. There are 6 different digital multipliers available in the Synopsys Design-Ware library, which is a broad portfolio of synthesizable implementation intellectual properties (IPs) for ASIC, system on chip (SOC) and FPGA design [26], including DW02_mult, DW02_mult_2_stage, DW02_mult_3_stage, DW02_mult_4_stage, DW02 _mult_5_stage and DW02_mult_6_stage. Synopsys Design Compiler maps "*" in HDL code to DW02_mult by default. DW02_mult is a totally combinational circuit, which has the parameterized word length and unsigned or signed (two'scomplement) data operation selection. During the logic synthesis process, Design Compiler selects the appropriate combinational circuit architecture according to the constraints set by users. Other multipliers available in the DesignWare library are all pipelined multipliers. For example, DW02_mult_3_stage is a three stage pipelined multiplier, which produces a product with a latency of two clock cycles. These pipelined multipliers also have the parameterized word length and unsigned or signed (two's-complement) data operation selection. It should be noted that for automatic pipeline retiming the combinational circuits in these pipelined multipliers are different from the one in DW02_mult.

It is found that the resulting circuit using DW02_mult does not meet the timing requirements for the design of this thesis. As a result, a pipelined multiplier is necessary for the design. Also, the automatic pipeline retiming technique has to be used to optimize the timing. This automatic pipeline retiming can be achieved by using the special register retiming command in Design Compiler.

The *compile* command in Design Compiler optimizes combinational logic by performing Boolean optimization and mapping the design to the target technology library. The optimization leaves unchanged the location and number of any registers present in the design. To further improve the circuit timing, register retiming technique can be used. Register retiming is a sequential optimization technique that moves registers through the combinational logic gates of a design to optimize timing and area. Designers can determine the optimal register locations and code them into the HDL description. However, it is difficult to find the optimal register locations inside a multiplier in the DesignWare library without total understanding



(b) After register retiming

Figure 4.25 Block diagram of DW02_mult_2_stage before register retiming and after register retiming.

of the implementation methods of the multiplier. In this case, the special register retiming command, *optimize_registers -period* 0, provided by Design Compiler can be used to automatically find the optimal locations of the registers in the design. This register retiming is performed after a design is compiled. Figure 4.25 shows the block diagram of DW02_mult_2_stage before register retiming and after register retiming. As one can see from the sub-figure (a), registers are placed at output before register retiming. After register retiming, shown in sub-figure (b), registers are moved inside the combinational logic gates to optimize timing and area. The multipliers in this design are implemented with DW02_mult_2_stage and DW02_mult_3_stage. Although the results show that both implementations can meet the timing requirements after register retiming, the implementation using DW02_mult_3_stage consuming more power and area. As the result, DW02_mult_2_stage with register timing is chosen as the multiplier in this modulator.

4.7 Summary

The implementation of all the key blocks in the modulator are elaborated. A novel QDDS architecture is proposed, which combines Suntherland algorithm, sine phase difference method and QLA method to compress ROM size. For the implementation of pulse shaping filter, two general design approaches are introduced. One approach uses two pulse shaping blocks to process I/Q data and the other uses one pulse shaping block by interleaving I/Q data. The implementation of pipelined CIC filter and polyphase half-band filter are covered. For the implementation of the inverse sinc filter, CSD multiplication and MCSD multiplication are used to implement the multipliers inside. Clock gating technique is also used to save power when the inverse sinc filter is not being used. The implementation of digital multipliers in the modulator is also discussed in this chapter.

Chapter 5

Performance Evaluation

As described in Chapter 4, there are different design options for each block. The performance of these design choices will be compared in this chapter with an emphasis on power consumption. To this end, a high-level power estimation technique is described. The technique can be used as a fast power consumption comparison for different design choices. The design choice which leads to less power consumption will be integrated together to achieve a low-power modulator.

5.1 High-level power estimation

5.1.1 Sources of power consumption

Power consumption in an integrated circuit has two components, dynamic power consumption and static power consumption. Dynamic power is dissipated when a device is switching. Switched capacitance power comes from charging and discharging capacitive loads. The calculation of the switched capacitance power is shown in Equation (5.1), where C_{load} is the capacitive load, α models the switching probability during a cycle of the clock toggling at frequency f and V_{dd} is the supply voltage. Short-circuit power is the second part of the dynamic power consumption. It is dissipated due to the current that conducts when both pull-up and pull-down networks are momentarily conducting at the same time. Equation (5.2) gives a simple model of the short circuit power, where β models the transistors' conductivity per voltage factoring the linear region, T is the inputs' rise/fall time, and τ is the gate delay [24]. Leakage power, which is the major source of static power consumption, is mostly due to leakage currents flowing through the channel even when the gate-source voltage is below threshold voltage.

$$P = \frac{1}{2} \cdot C_{load} \cdot \alpha \cdot V_{dd}^2 \cdot f \tag{5.1}$$

$$P_{sc} = \frac{\beta}{12} (V_{dd} - 2V_{th})^3 \frac{\tau}{T}$$
(5.2)

According to the data shown in [24], the power consumption for integrated circuits at 0.18μ m and larger technology is still dominated by the dynamic power consumption. However, the leakage power has to be considered for a design using 0.13μ m or more advanced technology [27]. For the design presented in this thesis, the modulator is implemented with 0.18μ m technology. All the low-power methods used are trying to save the dynamic power because dynamic power consumption dominates in this technology. Note that some dynamic power efficient implementations actually lead to increasing leakage power consumption.

5.1.2 Power estimation and analysis flow

Generally speaking, all the tools for switched capacitance power consumption estimation need to evaluate Equation (5.1). This can be done at different levels of abstraction, such as algorithm level, RTL level, gate level or circuit level. Power calculator collects the parameters of Equation (5.1) at the respective level of abstraction. Floorplan and the architecture determine the physical and structural architecture and represent the capacitance C_{load} in Equation (5.1). Activity calculator produces an activation profile for each of the components modeling the switching probability, α in Equation (5.1). Finally, the supply voltage V_{dd} and the clock frequency f are provided by the designer. For accurate short circuit power and leakage power estimation, transistor level models are necessary.

For the power consumption estimation in this thesis, a fast comparison of different design options is desired. The primary goal of this thesis is to know which design option should be chosen to follow. Thus, relative power consumption figures for each of the design options are needed. Although the predicted power figure of the different options may differ to some extent from the final power figure after implementation, it is important that the estimated most power efficient option really leads to the least power consumption. Based on this consideration, the gate level power estimation is chosen.

5.1.3 Power estimation in logic synthesizer

The power estimation flow of Synopsys Design Compiler is shown in Figure 5.1. After performing synthesis, Synopsys Design Compiler uses the synthesized gate level netlist to estimate the power consumption. The dynamic power considered by Synopsys Design Compiler includes net switching power and cell internal power. Net switching power is computed according to Equation (5.1). Capacitance is computed based on the capacitance specified in library cells and wire-load model. The cell internal power includes the power consumed due to switching activities on internal nodes of cells and the short circuit power consumed by the cells. The leakage power is estimated according to the leakage power annotation for each cell in the library. The leakage power annotations may vary with different input states of one cell because leakage model can be state dependant [24, 27].

The two most significant sources of inaccuracy at the gate level power estimation are the switching activities and the prelayout wire-load values [28]. There are two ways to estimate the switching activities, vector analysis and vectorless analysis. For the vector analysis, the switching activities can be estimated from simulation data. For the vectorless analysis, power estimator annotates the switching activity for the ports and propagates this value through the design based on statistical calculations.

The vector analysis has several limitations. First, for large design, circuit simulation is very time consuming. Second, it is difficult to determine if the test cases causing the highest power consumption are covered by simulation data. Since the goal is to compute the relative power consumption figures for each design option, the vectorless power analysis is chosen. The Synopsys Design Compiler uses the default switching activity (0.25 toggle per positive edge) for the ports and the wire-load



Figure 5.1 Power estimation in logic synthesizer.

values are chosen to be worst case wire-load estimates.

Although the vectorless power consumption estimations in Synopsys Design Compiler are just rough estimates, these estimations are good indicators of power consumption trends at the design stage to determine which design option leads to less power consumption, i.e., such data are more useful in comparing the power implications of various design strategies than in predicting a chip's actual power consumption [28]. The relative low-power design options indicated by Synopsys Design Compiler are chosen to build final modulator.

5.2 Performance of QDDS

In order to evaluate the performance of the proposed QDDS, the proposed QDDS is compared with two other QDDS implementation methods. The block diagrams of these two other implementations are shown in Figure 5.2. The first QDDS implementation method does not use any phase-to-amplitude ROM compression method, while the second implementation compress the phase-to-amplitude ROM using the quarter-wave symmetry method.



Figure 5.2 Two conventional QDDS implementations.

5.2.1 Output spectrum

In order to compare the output spectrum of three QDDS architectures, it is important to identify the sources of noise in QDDS circuit. The first source of noise is truncation noise due to phase truncation at the input of the phase-to-amplitude converting ROM. The second is ROM compression noise which is a nonlinear distortion that usually exists when phase-to-amplitude converting ROM compressing methods are employed. The third is the quantization noise which is introduced by the finite precision of the samples stored in the phase-to-amplitude converting ROM.

As discussed in Section 4.2.1, phase-to-amplitude converting ROM using quarterwave symmetry doesn't introduce any compression noises if a $\frac{1}{2}$ -LSB phase offset is introduced. Therefore, the output spectrum purity of the two conventional structures are the same.

The spectrum of two frequencies for the conventional QDDS architectures and the proposed QDDS architecture are shown in Figure 5.3 and Figure 5.4 respectively. Figure 5.3 is the spectrum of the outputs when the 32-bit tuning word is 0X1999999A. With this tuning word, the output frequency is $f_{out} = \frac{M}{2^{32}} \times f_{refclk} \approx$ $0.1 \times f_{refclk}$. Both spectrum shows big spurs in this figure as a result of phase truncation. As one can see in this figure, the biggest spur of the proposed QDDS is about 2 dB larger than the conventional architecture's biggest spur. This is because that the phase-to-amplitude compression method used in the proposed architecture introduces compression noises. Figure 5.4 is the spectrum of the outputs when the 32-bit tuning word is 0X1AA00000. With this tuning word, the output frequency is $f_{out} = \frac{M}{2^{32}} \times f_{refclk} \approx 0.104 \times f_{refclk}$. Since all non-zero bits of the tuning word are located in the highest 12 bits, there is no phase truncation for this tuning word. The main noise source for the conventional QDDS are the quantization noise. For the proposed QDDS architecture, the phase-to-amplitude compression method still introduces extra compression noises and lowers down the SNR.







Figure 5.4 Spectrum of the QDDS output $(f_{out} \approx 0.104 \times f_{refclk})$.

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Figure 5.5 Power consumption comparison for 3 different QDDS architectures.

5.2.2 Power consumption

Figure 5.5 shows the power consumption of three different QDDS architectures. As one can see from this figure, the proposed QDDS can save up to 90% power consumption at 150 MHz compared with the QDDS which uses full size ROM, and can save up to 60% power consumption at 150 MHz compared with the QDDS which uses quarter-wave symmetry. Reports from logic synthesizer also show that the proposed QDDS can save area compared with the conventional ones. The proposed QDDS can save up to 98% area compared with the design which uses full size ROM, and can save up to 91% area compared with the design which uses quarter-wave symmetry.

5.3 Performance of pulse shaping filter

As described in Section 4.3.3, there are two general approaches to design the pulse shaping filter for a quadrature modulator. One approach requires two pulse shaping filter blocks to process the I/Q data separately, while the other approach requires only one pulse shaping filter block by interleaving the data in time. When



Figure 5.6 Power consumption comparison for 2 different pulse shaping filter implementations (interpolation ratio of interpolation filter=4).

multiple paths use the same filter coefficients to process different data, the second interleaving technique is more area efficient. Figure 5.6 shows the power consumption comparison of these two methods. The figure shows the interleaving I/Q data method consumes more power although it is more hardware efficient. Since the design focus is on low power, two pulse shaping filter blocks is chosen for be the implementation method of the modulator.

5.4 Performance of interpolation filter

As described in Section 4.4, two interpolation filter structures are considered in the modulator. One is CIC filter and the other is half-band filter. For the design of this thesis, the interpolation ratios available are 4, 8, 16 and 32. CIC filter can support these interpolation ratios with the same structure. In order to compare frequency response and power consumption, two, three, four and five half-band filters are cascaded respectively.



Figure 5.7 Comparison of HBF and CIC frequency response.

5.4.1 Frequency response

Figure 5.7 shows the frequency responses of the CIC filter with the interpolation ratio of 4 and two cascaded half-band filters with the filter length of 13. Both of them can suppress extra spectra copies with more than 60 dB image rejection ratio. The difference is that the CIC filter has an obvious passband attenuation, while the half-band filter only has a small passband ripple which is less than 0.05 dB.

5.4.2 Power consumption

Figure 5.8 to Figure 5.11 show the power consumption comparison between the CIC filter and the half-band filter when the interpolation ratio is 4, 8, 16 and 32, respectively. The CIC filter can save more than 70% of power compared with the half-band FIR filter for all the possible configurations. A penalty comes from the frequency dependent attenuation that the CIC filter introduces over the frequency range of the data to be transmitted. As described in Section 4.4.1, two methods can be used to alleviate this frequency dependent attenuation, i.e., using higher



Figure 5.8 Power consumption comparison for two interpolation filters with the interpolation ratio of 4.



Figure 5.9 Power consumption comparison for two interpolation filters with the interpolation ratio of 8.



Figure 5.10 Power consumption comparison for two interpolation filters with the interpolation ratio of 16.



Figure 5.11 Power consumption comparison for two interpolation filters with the interpolation ratio of 32.

System	Power consumption	Power consumption
clock	of ISF using CSD	of ISF using MCSD
frequency	multiplications	multiplications
(MHz)	(mW)	(mW)
50	2.795	2.785
60	3.353	3.335
70	3.916	3.894
80	4.479	4.454
90	5.044	5.016
100	5.598	5.567
110	6.103	6.072
120	6.691	6.657
130	7.224	7.188
140	7.867	7.828
150	8.385	8.342

Table 5.1Power consumption comparison of ISF using CSD
multiplication and MCSD multiplication.

rate change factor or precompensating it by configuring SQRC coefficient memory. Disadvantage of the precompensating method is that it will affect the frequency response of the SQRC filter.

5.5 Performance of inverse sinc filter

As described in Section 4.5.1, the inverse sinc filter can be implemented with two multiplication methods, CSD multiplication and MCSD multiplication. The power consumption of these two implementations are compared in Table 5.1. The results show that less power consumption can be achieved when the MCSD multiplication method is used in the filter. Synthesis results also show that this filter implemented with the MCSD multiplication results in smaller area compared with the implementation with CSD multiplication.

5.6 Summary

High level power estimation technique for IC design is introduced in this chapter. Using the high level power estimation technique, different design choices are compared for power consumption. The performance comparison shows that the proposed QDDS architecture can save up to 60% of power consumption at 150 MHz compared with one conventional design which just uses quarter-wave symmetry characteristic. The power consumption comparisons for other key blocks show that using two pulse shaping filters for I/Q processing, CIC interpolation structure and inverse sinc filter with MCSD multiplication consume less power than alternative design choices. These blocks with less power consumption will be integrated to achieve a low-power modulator.

Chapter 6

System Integration

The performance evaluation results show that the proposed QDDS, the two pulse shaping filters for I/Q processing, the CIC interpolation structure, and the inverse sinc filter with MCSD multiplication consume less power than alternative design choices. A low-power consumption modulator is implemented with these low-power consumption blocks. This chapter describes functional verification and power estimation of the designed modulator.

6.1 Functional verification

6.1.1 Testing model

In order to perform functional verification for the designed modulator, a testing model is developed. Referring to Figure 6.1, random binary data are generated in Matlab and saved in a testing data file. These data are used as the input for the designed modulator. Final output data of the modulator as well as the intermediate output data from each block are dumped into individual data files. Matlab is then used to analyze these data files with fast fourier transform (FFT) to verify the functionality. The coefficients of the SQRC filter, the interpolation ratio of the CIC filter and the digital tuning word of the QDDS must be configured before testing.

For testing purpose, the coefficient data for the SQRC filter is configured with the impulse response shown in Figure 4.10, i.e., the roll-off factor is 0.22. All the spectrums shown in this chapter are based on this same roll-off factor for SQRC filter. Since the configuration of the roll-off factor only controls the transmitting signal's bandwidth, the output spectrum purity won't be affected by this configu-



Figure 6.1 Testing model.

ration.

6.1.2 QDDS

The outputs of the QDDS are the first intermediate results to be verified. As described in Equation (2.1), the QDDS output frequency is controlled by the digital tuning word. Four tuning words are used to test the QDDS. These tuning words are 0X1999999A, 0X1AA00000, 0X266666666 and 0X66666666666. The corresponding output frequencies for the tuning words are about $0.1 \times f_{refclk}$, $0.104 \times f_{refclk}$, $0.15 \times f_{refclk}$ and $0.45 \times f_{refclk}$, respectively. The spectrums for four tuning words are shown in Figure 6.2.

As one can see from the output spectrum, the largest spur for sub-figure $f_{out} \approx 0.1 \times f_{refclk}$ is about 62 dB lower than the expected output signal, the largest spur for sub-figure $f_{out} \approx 0.104 \times f_{refclk}$ is about 70 dB lower than the expected output signal, the largest spur for sub-figure $f_{out} \approx 0.15 \times f_{refclk}$ is about 64 dB lower than

the expected output signal and the largest spur for sub-figure $f_{out} \approx 0.45 \times f_{refclk}$ is about 65 dB lower than the expected output signal. It should be noted that there is no phase truncation for sub-figure $f_{out} \approx 0.104 \times f_{refclk}$, because only the highest 12 bits of the tuning word are not zeros. The main noise sources in this case are ROM compression and quantization. For other three tuning words, the main noise sources are ROM compression, quantization and phase truncation.



Figure 6.2 Spectrum of QDDS outputs.



Figure 6.3 Signal spectrum after pulse shaping filter.

6.1.3 Pulse shaping filter

The output of the pulse shaping filter is the second intermediate results to be verified. Referring to the output signal spectrum in Figure 6.3, the minimum outof-band rejection ratio is about 55 dB. The spectrum shown in this figure is similar with the frequency response shown in Figure 4.11, which means that the designed SQRC filter functions properly.

6.1.4 CIC filter

The output of the CIC filter is the third intermediate results to be verified. The four possible configurations for the interpolation ratio are 4, 8, 16 and 32. The results for the interpolation ratio of 4 and 8 are shown here. Figure 6.4 shows the signal spectrum when the interpolation ratio is 4 and Figure 6.4 shows the signal spectrum when the interpolation ratio is 8.

It can be seen that these plots are the normalized amplitudes as a function of symbol rate. Note that the maximum value for each x-axis is actually the half system clock frequency. For the CIC filter with the interpolation rates 4 and 8, the



Figure 6.4 Signal spectrum after CIC filter (R = 4).



Figure 6.5 Signal spectrum after CIC filter (R=8).

maximum value is $8 \times \text{symbol}$ rate and $16 \times \text{symbol}$ rate respectively. The frequency is normalized to the symbol rate instead of the system clock frequency for better demonstration of the position of the residual spectrum. For example, when the CIC filter is configured with the interpolation ratio of 4, there are 3 unwanted images located at $4 \times \text{symbol}$ rate, $8 \times \text{symbol}$ rate and $12 \times \text{symbol}$ rate. One can clearly see the residual spectrum at $4 \times \text{symbol}$ rate and a small residual spectrum at $8 \times \text{symbol}$ rate in Figure 6.4. The other residual spectrum at $12 \times \text{symbol}$ rate is symmetrical with the residual spectrum at $4 \times \text{symbol}$ rate about half system clock frequency.

One can also compare Figure 6.4 with Figure 4.14, and compare Figure 6.5 with Figure 4.15. The spectrum shown in Figure 6.4 and Figure 6.5 are almost identical to the periodic spectrum times the corresponding frequency response of the CIC filter. This means that the designed CIC filter is working properly.

6.1.5 Modulator

Since both the interpolation ratio of the CIC filter and the output frequency of the QDDS are configurable, there are a number of possible configurations. Only a selected testing results are shown here. Note that all the results are obtained with the inverse sinc filter turned on.

Figure 6.6 shows the results with tuning word of 0X1999999A and four possible interpolation ratios. The corresponding output center frequency is about $0.1 \times f_{refclk}$. There are two images at about $0.3 \times f_{refclk}$ and $0.5 \times f_{refclk}$ in Figure 6.6. By comparing this figure with the spectrum plot for $f_{out} \approx 0.1 \times f_{refclk}$ in Figure 6.2, one can understand that the images at about $0.3 \times f_{refclk}$ and $0.5 \times f_{refclk}$ are resulted from the multiplication of the baseband signal with the spurs of the QDDS.

Figure 6.7 shows the results with tuning word of 0X1AA00000 and four possible interpolation ratios. The corresponding output center frequency is about $0.104 \times f_{refclk}$. There are also two small images at about $0.314 \times f_{refclk}$ and $0.48 \times f_{refclk}$ shown in Figure 6.7. For the same reason that the baseband signal is multiplied with the big spurs of the QDDS in Figure 6.2.



Figure 6.6 Output signal spectrum of the designed modulator with $f_{out} \approx 0.1 \times f_{refclk}$.



Figure 6.7 Output signal spectrum of the designed modulator with $f_{out} \approx 0.104 \times f_{refclk}$.



Figure 6.8 Power consumption estimation of the designed modulator after logic synthesis.

6.2 Power consumption estimation

6.2.1 Power consumption estimation after logic synthesis

The power consumption of the designed modulator is estimated in logic synthesizer first. The power consumption estimated at this stage is the core power of a chip [28]. It is estimated under the following conditions: interpolation ratio of the CIC filter is 4; the inverse sinc filter is turned on; the switching activity for the input port is set at 0.25; and the wire-load values are chosen to be worst case wire-load values. As shown in Figure 6.8, the core of the designed modulator consumes about 25 mW at 150 MHz system clock frequency.

6.2.2 Power consumption estimation after layout

Layout of the designed modulator is done in Cadence Encounter and the result is shown in Figure 6.9. There are a total of 66 input/ouput pads, 5 pairs of core power pads and 11 pairs of ring power pads. The core area is about 4.3 mm² and the chip area is about 7.06 mm². With the same configuration, i.e., the interpolation ratio of the CIC filter is 4 and the inverse sinc filter is turned on, the power consumption



Figure 6.9 Layout of the designed modulator.

of the designed modulator is also estimated. The power consumption at this stage is called overall power estimation [28]. The power consumption estimation method is still the same as the estimation method described in Section 5.1.2. However, power consumption estimation at this stage is more accurate because the wire-load values are close to real values now and power consumption estimation at this stage also considers the power consumption from pads. As shown in Figure 6.10, the overall power consumption of the designed modulator consumes about 95 mW at 150 MHz system clock frequency. The designed modulator is compared with other designs and the results are shown in Table 6.1. As one can see from this table, only the design shown in [29] consumes similar power as the design presented in this thesis. However, the design shown in [29] doesn't have pulse shaping filters and interpolation filters. One still has to implement these functions off-chip in a real application. Therefore, the modulator presented in this thesis has superior performance in power consumption.



Figure 6.10 Power consumption estimation of the designed modulator after layout.

Table 6.1	Comparison	of different	modulator	ICs
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Chip	Process	Power (mW/MHz)	Max. clock (MHz)	On-chip DAC
AD9856 [2]	-	7.3@3V	200	12-bit
Vankka [30]	$0.35 \mu m CMOS$	2.04@2.8V	500	12-bit
Lindeberg [31]	$0.13 \mu m CMOS$	0.69@1.5V	200	1-bit
Wu [29]	$0.25 \mu m CMOS$	0.6@2.5V	800	-
This Work	$0.18 \mu m CMOS$	0.63@1.6V	150	-

6.3 Summary

The low-power blocks described in Chapter 5 are integrated together to achieve a low-power quadrature modulator. Functional verification is performed to verify the design. Both the intermediate outputs and final output are analyzed in frequency domain. The results show that the designed modulator functions properly. Power consumption estimation of the modulator is also shown in this chapter. The core power consumption estimation shows that the core of the modulator consumes about 25 mW at 150 MHz system clock frequency and the overall power consumption estimation shows that the modulator consumes about 95 mW at 150 MHz system clock frequency. The designed modulator is also compared with other designs and the results show that it has superior performance in power consumption.

Chapter 7

Conclusions

Quadrature digital modulation techniques are widely used in modern wireless communication systems because of their high performance and flexibility. However, these advantages come at the cost of high power consumption. For example, one commercially used modulator [2] consumes about 1100 mW at 150 MHz. This thesis focuses on the integrated circuit implementation of a low-power quadrature digital modulator in 0.18μ m CMOS technology which is intended to be used in a variety of portable applications such as cell phones and personal digital assistants.

The designed quadrature digital modulator consists of several key blocks: a QDDS, pulse shaping filters, interpolation filters and an inverse sinc filter. The QDDS generates sine/cosine carrier reference signals for the modulator. The pulse shaping filters are used to limit transmitting bandwidth and reduce intersymbol interference. The interpolation filters are used to increase sampling rate and enable the translation from baseband to intermediate frequency within digital domain. The inverse sinc filter is used to precompensate the sinc distortion coming from the following DAC.

The design strategy used in this modulator is trying to find low-power implementation for each block inside and then integrate them together to achieve a low-power quadrature digital modulator. In order to find low-power consumption implementation for the key blocks, each block is implemented with multiple design choices and high-level power estimation is used for fast comparison between these multiple design choices. Lower power consumption blocks are integrated to achieve a low-power modulator and performance of the designed modulator is evaluated.

7.1 Conclusions

Several ROM compression methods are used to reduce the ROM size for the implementation of the QDDS. By combining Suntherland algorithm, sine-phase difference method and quad line approximation method, the final ROM compression ratio achieved is 14.7 compared with one conventional design which simply uses quarter-wave symmetry characteristic of sine and cosine waves. The power consumption comparison shows that the proposed QDDS circuit can save up to 60% of the power consumption at 150 MHz system clock frequency compared with the same conventional design. Extra noises are introduced because of these compression methods used.

The pulse shaping filter is implemented according to the polyphase structure and the filter length is 128 with a built-in four times upsampling function. There are two general approaches to design this filter for a quadrature modulator. The first approach uses two pulse shaping blocks to process I and Q data separately. The second approach just uses one pulse shaping block by interleaving I and Qstreams in time. The power consumption comparison shows that the second approach consumes more power although it is more hardware efficient. So the one using two pulse shaping blocks is chosen as the implementation method in this design.

Interpolation ratio of the interpolation filters in the modulator is limited to 4, 8, 16 and 32. Two hardware efficient interpolation architectures are considered in the modulator. One is CIC filter and the other is half-band FIR filter. The power consumption comparison shows CIC filter consumes less power than its counterpart. So CIC interpolation structure is chosen as the interpolation structure in this modulator. The penalty is the frequency dependant distortion coming from CIC filter. However, one can alleviate this distortion by using higher interpolation ratio or by configuring the coefficient RAM of pulse shaping filter with the convolution of two impulse responses - one is the impulse response of the pulse shaping filter and the other is the impulse response of an inverse CIC filter.
The inverse sinc filter is implemented with the length of 9. Since all the multiplications in this filter are constant multiplications, conventional design usually uses CSD multiplication method to implement all the multipliers. However, the MCSD multiplication method is more suitable for ASIC design. The power consumption estimation shows the filter using MCSD multiplication method does lead to less power consumption and is more hardware efficient compared with the design using CSD multiplication method.

The final quadrature digital modulator is implemented with the proposed lowpower QDDS architecture and other low-power consumption blocks which are found by comparing power consumption of different design approaches for each block. The results show that the modulator designed with this strategy leads to less power consumption and provides a universal low-power solution for quadrature digital modulator design. The power consumption estimation shows that the designed modulator consumes about 95 mW at 150 MHz system clock frequency which is much lower than the similar product that consumes about 1100 mW at 150 MHz system clock frequency.

The novel 32-bit low-power QDDS in the modulator can be used in various quadrature digital modulators and demodulators which have low-power consumption requirement. The designed modulator also has a number of other features:

- \bullet 0 to 75 MHz output bandwidth
- Configurable pulse shaping filters and interpolation filters
- Internal $\sin(x)/x$ correction filter

7.2 Future work

There are still a number of interesting areas that can be investigated further in the future.

• Circuit level low-power techniques

Most of the low-power consumption techniques used in this thesis are at system level and algorithm level. Other low-power techniques at circuit level, such as multiple supple voltages and dynamic supply voltage scaling can also be applied to study how much power can further be saved.

• On-chip digital to analog converter

There will be several advantages if a low-power on-chip DAC can be included. One advantage is that it can avoid delays and line loading caused by interchip connection to an off-chip DAC. Another advantage is that it can save both power and area.

• Multilevel QAM

The modulator structure described in this thesis can be used for many quadrature digital modulation. It is interesting to apply this structure to a quadrature modulator with low-power consumption that can support multilevel QAM.

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Appendix A

Scripts for Digital IC Design

A.1 A script for invoking NCsim in batch mode

#!/bin/csh -f
ncvlog ./test.v
ncvlog ./testbench.v
ncelab -access +r worklib.testbench:module
ncsim -tcl worklib.testbench:module <<!
run 10000 us
quit
!</pre>

A.2 A script for invoking Synopsys Design Compiler in batch mode

#!/bin/csh -f
dc_shell <<!
analyze -format verilog -lib DEFAULT { "./test.v" }
elaborate test -arch "verilog" -lib DEFAULT -update
current_design = "./test.db:test"
check_design
set_load 10 find(port, "output")
create_clock -name "clk" -period 5 -waveform { "0" "2.5" } { "clk" }
set_clock_skew -plus_uncertainty 0.5 "clk"</pre>

```
set_clock_skew -minus_uncertainty 0.5 "clk"
set_dont_touch_network find( clock, "clk")
set_fix_multiple_port_nets -all
compile -ungroup_all
compile -map_effort high -incremental_map
report_area > ./test.rpt
report_power >> ./test.rpt
report_timing -path full -delay max -max_paths 1 -nworst 1 >> ./test.rpt
write -format verilog -hierarchy -output "./test_gate.v" {"./test.db:test"}
quit
!
```

A.3 A script for invoking Cadence PKS in batch mode for timing optimization

#!/bin/csh -f
pks_shell <<!
read_alf /CMC/kits/artisan18/FE/aci/sc/alf/fast.alf
read_tlf -force /CMC/kits/artisan18/FE/.../tpz973gbc.tlf
read_lef /CMC/kits/artisan18/FE/aci/sc/lef/tsmc18_6lm.lef
read_lef_update /CMC/kits/artisan18/FE/.../tpz973g_6lm.lef
check_library checklib.rpt
read_verilog test_ctgo.v
do_build_generic
read_def test_ctgo.def
set_clock clk -period 5
set_clock_insertion_delay 0.1 clk
set_clock_propagation propagated
set_clock_root -clock</pre>

do_route -timing_driven

do_fix_hold -buffer -critical_ratio 0.0

do_place -eco

do_route -timing_driven

 $report_timing > pks_postholdfix.rpt$

write_verilog -hier test_postholdfix.v

write_def -hier_delimiter "/" modulator_postholdfix.def

exit

!