Alignment of RNA Base Pairing Probability Matrices

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ABSTRACT

Motivation: Many classes of functional RNA molecules are characterized by highly conserved secondary structures but little detectable sequence similarity. Reliable multiple alignments can therefore be constructed only when the shared structural features are taken into account. Since multiple alignments are used as input for many subsequent methods of data analysis, structure based alignments are an indispensable necessity in RNA bioinformatics.

Results: We present here a method to compute pairwise and progressive multiple alignments from the direct comparison of basepairing probability matrices. Instead of attempting to solve the folding and the alignment problem simultaneously as in the classical Sankoff algorithm we use McCaskill's approach to compute base pairing probability matrices which effectively incorporate the information on the energetics of each sequences. A novel, simplified variant of Sankoff's algorithms can then be employed to extract the maximum weight common secondary structure and an associated alignment.

Availability: The programs pmcomp and pmmulti described in this contribution are implemented in Perl, and are available on request from the authors. A web server is available at http://rna.tbi.univie.ac.at/cgi-bin/pmcgi.pl

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INTRODUCTION

Many functional classes of RNA molecules, including tRNA, rRNA, RNAse P RNA, SRP RNA, exhibit a highly conserved secondary structure but little sequence homology. Reliable alignments thus have to take structural information into account.

Sankoff's algorithm (Sankoff, 1985) that simultaneously allows the solution of the structure prediction and alignment problem is computationally very expensive, $\mathcal{O}(n^6)$ in CPU time and $\mathcal{O}(n^4)$ in memory for a pair of sequences of length n. A further complication is that it requires the implementation of the full loop-based RNA energy model

(Mathews *et al.*, 1999). Currently available software packages such as foldalign (Gorodkin *et al.*, 1997) and dynalign (Mathews & Turner, 2002) therefore implement only restricted versions.

In this contribution we describe a different approach. Instead of attempting to solve the alignment and the structure prediction problem simultaneously we start from base pairing probability matrices predicted by means of McCaskill's algorithm (McCaskill, 1990) (implemented in the RNAfold program of Vienna RNA Package (Hofacker *et al.*, 1994; Hofacker, 2003). The problem then becomes the alignment of the base pairing probability matrices. This appears to be an even harder threading problem, which is known to be NP-complete in the general case (Lathrop, 1994). For RNA structure alignments, however, we shall see the threading problem remains tractable as long as we score the alignment based on the notion of a common secondary structure.

A VARIANT OF SANKOFF'S ALGORITHM

Suppose we are given two sequences A and B with their pair probability matrices P^A and P^B , resp. A natural way of determining the similarities of P^A and P^B is to search for the secondary structure of maximal "weight" that P^A and P^B have in common. In other words, we have to find a list of matches between pairs (i,j) from A and (k,l) from B that form a secondary structure and satisfy

$$\sum_{\text{matches }(ij;kl)} \left(\Psi^{A}_{ij} + \Psi^{B}_{kl} \right) \to \max, \tag{1}$$

where Ψ^A_{ij} is the weight of pair (i,j) from sequence A. Here, we use $\Psi_{ij} = \log(P_{ij}/p_{\min})$ with p_{\min} the miniumum pair probability that is deemed significant. More generally, we look for an alignment of the sequences A and B with N_{gap} insertions or deletions together with a consensus secondary structure $\mathcal S$ such that

$$\sum_{(ij;kl)\in\mathcal{S}} \left(\Psi_{ij}^A + \Psi_{kl}^B + \tau(A_i, A_j; B_k, B_l) \right) + \gamma N_{\text{gap}} + \sum_{i\in A, k\in B} \sigma(A_i, B_k) \to \max$$
(2)

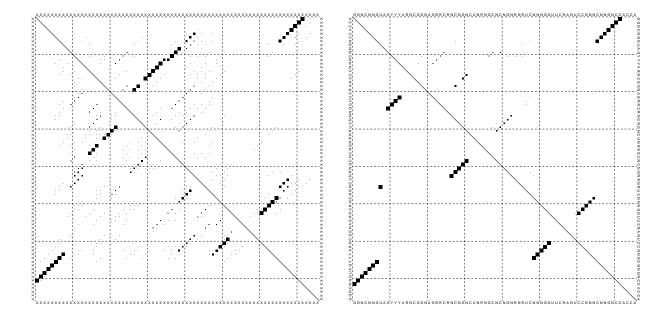


Fig. 1. Left: Two base pairing probability matrices of tRNAs DF1140 (GAA from *Mycoplasma capric.*, upper right) and DA0980 (TGC from *Thermoprot. tenax*, lower left) taken from M. Sprinzl's tRNA database (Sprinzl *et al.*, 1998). Right: pairwise alignment obtained based solely on the structural information using pmcomp with $\gamma = -5$. Note that the tRNA cloverleaf is not obvious from both individual structure predictions, while it is easily identified in the average of the aligned dot plots (upper right). The lower left triangle shows the base pairs of the consensus tree which, with the exception of the spurious isolated pair is identical to the consensus structure given in the database.

Here $\gamma < 0$ is a gap penalty. The scores $\sigma(A_i, B_k)$ and $\tau(A_i, A_j; B_k, B_l)$ describe the substitution of unpaired bases and base pairs, respectively. In the simplest case we disregard sequence-specific components, setting $\sigma = \tau = 0$.

Let $S_{i,j;k,l}$ be the score of the best matching of the subsequences A[i..j] and B[k..l]. Furthermore, let $S_{i,j;k,l}^M$ be the best match subject to the constraint that (i,j) and (k,l) are matched base pairs. With this definition one easily obtains dynamic programming recursions

$$S_{i,j;k,l} = \max \begin{cases} S_{i+1,j;k,l} + \gamma, \\ S_{i,j;k+1,l} + \gamma, \\ S_{i+1,j,k+1,l} + \sigma(A_i, B_k), \\ \max_{h \le j, q \le l} \left(S_{i,h;k,q}^M + S_{h+1,j;q+1,l} \right) \end{cases}$$

$$S_{i,j;k,l}^M = S_{i+1,j+1,k+1,l+1} + \Psi_{ij}^A + \Psi_{kl}^B + \tau(A_i, A_j; B_k, B_l)$$
(3)

with the initialization $S_{i,j;k,l} = |(j-i)-(l-k)|\gamma$ for $j-i \leq M+1$ or $l-k \leq M+1$. Here M is the minimum size of a hairpin loop, usually M=3. The first two terms in the upper line of equ.(3) account for gaps in one of the two sequences. The third term describes the extension of both sub-sequences with an unpaired position. The max-

term, finally, describes a match of the pairs (i,h) in A with (k,q) in B. The expression for the score restricted to a match of (i,j) with (k,l) is straightforward. Recursion (3) requires $\mathcal{O}(n^4)$ memory to store the scores $S_{i,j;k,l}$ and requires $\mathcal{O}(n^6)$ operations.

This is the same as the (maximum circular matching version of the) Sankoff algorithm (Sankoff, 1985) when we set $P_{ij}^A=1$ if A_i and A_j can form a base pair and $P_{ij}^A=0$ otherwise. The algorithm shown here is not restricted to canonical alignments, in which adjacent insertions and deletions occur only in one of the two possibles orders (Waterman, 2003). This restriction is important if suboptimal alignments are computed, an appropriate modification of the algorithm is straightforward.

Restricting the difference $\Delta = |(j-i)-(l-k)|$ in the "span" of matching base pairs $(i,j) \in A$ and $(k,l) \in B$ reduces the complexity to $\mathcal{O}(n^5)$ CPU usage; restricting this difference for all partial alignments reduces the computational effort to $\mathcal{O}(n^3)$ memory and $\mathcal{O}(n^4)$ CPU usage. Note that in the latter case Δ must be larger than the difference in sequence length.

Standard backtracking can be used to retrieve the matched sequence positions. Here we have two kinds: matches of a base pair $(i,j) \in A$ with $(k,l) \in B$ and matches of unpaired bases corresponding to the third term

in the first line of equ.(3). Note that matches of unpaired bases do not contribute to the score in the simple scoring scheme with $\sigma = \tau = 0$. Thus the exact positions of gaps within a stretch of unpaired bases is arbitrary in this case.

MULTIPLE ALIGNMENTS

Given the alignment we can define a "consensus" or "average" base pair probability matrix as

$$P_{p,q}^{AB} = \begin{cases} \sqrt{P_{i_p,j_q}^A P_{k_p,l_q}^B} & \text{for matches} \\ 0 & \text{for gaps} \end{cases}$$
 (4)

where i_p is the positions in sequence A corresponding to the position p of the alignment. As a consequence we can easily extend the method to progressive alignments of more than two sequences.

In the current implementation a script pmmulti first calls pmcomp to compute all pairwise alignments, then takes the similarity scores to produce a guide tree using the weighted pairgroup clustering methods and assembles the multiple alignment. For the construction of multiple alignments it is not necessarily desirable to use canonical alignments since the correct order of insertions/deletions in a pairwise alignment is in general determined by the other sequences in the multiple alignment.

A coarse, but *much* faster, method to compare pair probabilities was already introduced in Bonhoeffer *et al.* (1993). From the pairing probabilities of base i we construct a vector containing the probabilities of being paired upstream $p^{<}(i) = \sum_{j>i} P_{ij}$, downstream $p^{>}(i) = \sum_{j<i} P_{ji}$, or unpaired $p^{\circ}(i) = 1 - p^{<}(i) - p^{>}(i)$. The resulting profiles can be aligned by means of a standard string/profile alignment algorithm in $\mathcal{O}(n^2)$ time using

$$\rho = \sqrt{p_A^> p_B^>} + \sqrt{p_A^< p_B^<} + \sqrt{p_A^\circ p_B^\circ}$$
 (5)

as the match score. While this fast method, to which we will refer as the "string-like alignment", often produces misaligned pairs, we have found the quality to be sufficient for the pairwise alignments used to construct the guide tree. Thus for a multiple alignment of N RNAs, we can use a fast approximate algorithm to compute the N(N-1)/2 pairwise alignments and restrict the expensive Sankoff algorithm to the N-1 progressive alignments along the guide trees.

As an example for the quality of pmmulti alignments we compare the predicted structure conserved structure of the IRES Ib element of Aphtovirus and Cardiovirus, two genera of the family picornaviridae in Fig. 3. The two approximate methods for structure-enhanced alignments, MARNA (Siebert & Backofen, 2003) and an alignment computed by pmmulti in the "string-like" alignment

mode (labeled PMstring in the Figure) produce acceptable results. In contrast, ClustalW (Thompson *et al.*, 1994) yields a low quality alignment in structural terms, showing many inconsistent mutations. The Sankoff algorithm (pmmulti), finally, slightly improves the manual alignment, finding one additional compensatory mutation.

DISCUSSION

The dynamic programming algorithm (3) is a variant of Sankoff's algorithm (Sankoff, 1985) for simultaneously aligning and folding two RNA sequences. The main difference is that the simultaneous folding and alignment problem requires the usage of the sophisticated loop-based thermodynamic energy model for RNA folding (Mathews et al., 1999), while for our purposes the much simpler analogue of Nussinov's weighted circular matching problem (Nussinov et al., 1978) is sufficient. In our approach the thermodynamic information about the RNA molecules is included in the base pair probability matrices P^A and P^B that are used as input. Another advantage over combined alignment-and-folding programs such as dynalign (Mathews & Turner, 2002) and FoldAlign (Gorodkin et al., 1997) is the fact that the input pairing matrices can be computed independently. For example, one might want to use the results of kinetic folding simulations (Flamm et al., 2000) that can differ significantly from the equilibrium thermodynamics results for some molecules.

Multiple structural alignments can be analyzed further by familiar techniques. For example, a parsimony program can be used to extract the phylogenetic relationships from structural information. Since the alignment is constructed such that only base pairs (i.e., matching pairs of parentheses) and unpaired positions are aligned with each other, the original version of the Fitch algorithm can be used to obtain meaningful parsimony scores directly from the aligned dot-parenthesis strings. This effectively weights base pairs with double weight compared to unpaired positions. For the example in Fig. 2 the unique most parsimonious tree is ((T1)(T2)((T3)((T4)(T5)))) with a score of 13, compared to the guide tree shown in the figure, ((T1)((T2)(T3))((T4)(T5))), with a score of 14. More elaborate scoring schemes and even associated maximum likelihood techniques acting directly on RNA secondary structures are algorithmically unproblematic but will require detailed knowledge of the dynamics RNA of structure evolution, while at present even RNA sequence evolution in the presence of (partially) conserved structures is understood only partially, see e.g. (Knudsen & Hein, 1999; Savill et al., 2001; Otsuka & Sugaya, 2003).

Alignments of base pairing probability matrices could also be employed as part of a structure search procedure. For example, the locally stable secondary structure motifs in a large RNA (as computed e.g. using the RNALfold

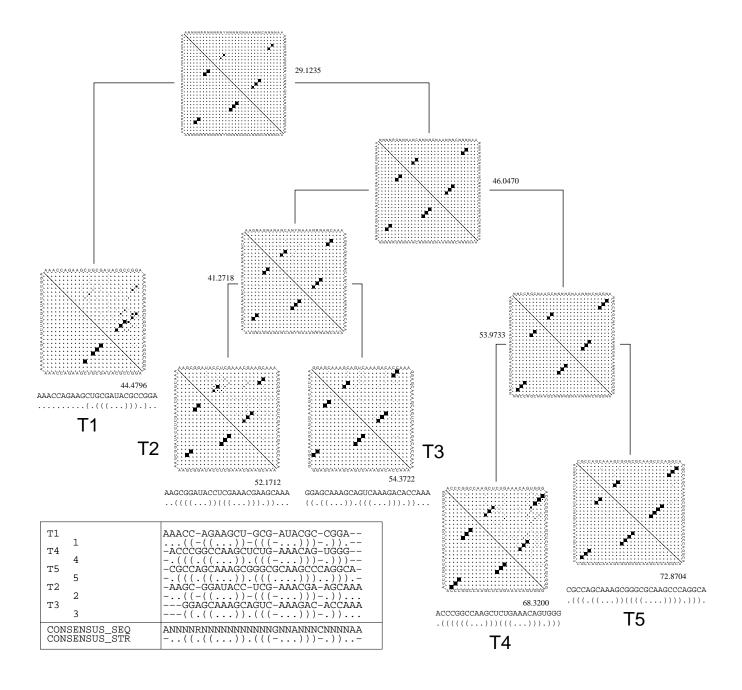


Fig. 2. A toy example for a multiple alignment of five RNA sequences aligned solely based on their base pairing probability matrices. For each sequence T1-T5 we give its minimum free energy structure and the self-similarity score of their base pairing probability matrices. The guide tree is constructed based on the scores of pairwise alignments using $\gamma = -3$. The inset contains the final multiple alignment.

algorithm (Hofacker *et al.*, 2003).) could be compared with a the base pairing probability matrices of one or a collection of query sequences. Due to high computational cost of the Sankoff algorithm it will probably by necessary to pre-select promising candidate sequences using a pattern search procedure. Tools such as HyPa (Gräf *et al.*, 2001), rnaforester (Höchsmann *et al.*, 2003), or the

Algebraic Dynamic Programming approach advocated in (Meyer & Giegerich, 2002) could be used to scan for candidate sequences, that are then folded by McCaskill's algorithm (e.g. using RNAfold -p) and compared to either each individual or the consensus structure of a multiple alignment of query structures.

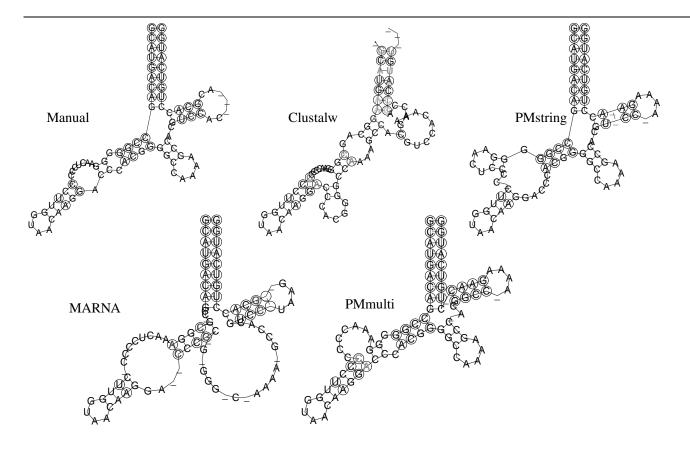


Fig. 3. Consensus structure of the IRES Ib region predicted from four Aphtovirus (FDI251473, FMDVALF, PIFMDV2, FAN133359) and three Cardiovirus sequences (MNGPOLY, EMCBCG, TMEPP). All structures were predicted by the RNAalifold program (Hofacker et al., 2002) from multiple alignments produced by different methods as input. Upper left: manual alignment taken from Witwer et al. (2001), upper center: ClustalW alignment, upper right: pmmulti in string-like alignment mode, lower left: MARNA (Siebert & Backofen, 2003) alignment, lower center: pmmulti. Circles indicate consistent and compensatory mutations while gray letters mark inconsistent mutations.

While the approximate methods MARNA and PMstring (pmmulti in string-like alignment mode) produce acceptable results, purely string-based approaches ClustalW yields a low quality alignment in structural terms, showing many inconsistent mutations. The two approximate methods for structure-enhanced alignments, MARNA and PMstring produce acceptable results but do not reach the number of compensatory mutations obtained in the manually edited alignment (upper left). The Sankoff algorithm (pmmulti), on the other hand, slightly improves the manual alignment, finding one additional compensatory mutation.

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