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First-Principles Method of Propagation of Tightly Bound Excitons: Verifying the Exciton Band Structure of LiF with Inelastic x-Ray Scattering

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We propose a simple first-principles method to describe the propagation of tightly bound excitons. By viewing the exciton as a composite object (an effective Frenkel exciton in Wannier orbitals), we define an exciton kinetic kernel to encapsulate the exciton propagation and decay for all binding energies. Applied to prototypical LiF, our approach produces three exciton bands, which we verified quantitatively via inelastic x-ray scattering. The proposed real-space picture is computationally inexpensive and thus enables study of the *full* exciton dynamics, even in the presence of surfaces and impurity scattering. It also provides an intuitive understanding to facilitate practical exciton engineering in semiconductors, strongly correlated oxides, and their nanostructures.

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Excitons, which are elementary excitations comprising a bound electron-hole pair, are crucial in optoelectronic materials applications, such as photovoltaics, solid-state lasers, light-emitting diodes, etc. [1-7]. One of the key issues in such applications is understanding the efficiency with which excitons propagate, as well as their associated decay and recombination, in the diverse contexts in which they arise, including not only bulk semiconductors but also polymers, thin films, quantum dots, and various other nanostructured materials [1–7]. Recent advances in inelastic x-ray scattering have provided, for the first time, an experimental means to map out the momentum-energy dispersion, and to some extent the internal structure, of excitons [8]. However, this method, like any experiment, yields incomplete information, the cross section being limited by the matrix element of photon-electron coupling. Understanding the full details of exciton propagation therefore remains a crucial yet challenging task.

Current state-of-the-art theoretical studies of excitons are based either on perturbation theory, via solution to the Bethe-Salpeter equation (BSE) [9-13], or on specially tuned approximations within the time-dependent density functional theory [13-16]. While providing great accuracy in some cases, the BSE method requires evaluation of fourpoint functions with both space and time indices, and are thus too computationally expensive to describe the full exciton kinetics or to address practical applications. Application of such methods have therefore been restricted to zero-momentum excitons only, and have not yet broached the issue of exciton propagation.

Furthermore, an increasing number of functional materials now make use of the strongly correlated nature of the electrons, which requires treatment of the many-body problem beyond the framework of perturbation theory. There is therefore a great need for new, first-principles approaches capable of treating both the propagation and the decay of excitons that can facilitate interpretation of experiments and provide an intuitive, physical picture that deepens our understanding of strongly correlated systems. Progress in this area would greatly facilitate efforts to tailor exciton properties in functional materials and devices.

In this Letter, we propose a general approach that focuses on the essence of the kinetics of exciton while allowing various treatments of many-body interactions. By integrating out the higher-energy virtual pair-breaking processes, the exciton can be treated as a single composite object, instead of a pair of a particle and a hole. Its kinetics can then be formulated in real space via an exciton kinetic kernel (exciton hopping integral). This kinetic kernel encapsulates the exciton decay process and the necessary energy dependence to react to all binding energies. For systems where the excitonic effect is large, this real-space description, together with the reduction of the two-body problem to one body, is significantly more efficient in computation, easily by several orders of magnitude. This approach can thus account for the *full* exciton kinetics with ease for practical applications. In addition, the separation of the nonlocal kinetic from the local interacting problem allows an accurate treatment of the local many-body problem beyond perturbation. Taking the prototypical LiF as a case study, our results give three branches of excitons, which we verified experimentally via inelastic x-ray scattering. The proposed approach offers a simple and intuitive physical picture easily applicable to systems with surfaces (or other boundary conditions), impurity scattering, or strong many-body interactions. Therefore, it should facilitate greatly the understanding of exciton propagation in all semiconductors, their nanostructures, and numerous strongly correlated functional materials.

The general idea of our approach is to map the generic exciton problem to an "effective" Frenkel exciton description, and encapsulate their propagation into an exciton kinetic kernel, like the hopping integral. This real-space approach makes sense because binding of particles and holes is only significant in the short range, and thus the size of the exciton with practically relevant binding should be reasonably small. To this end, one needs to (1) define a "local" region, in which the local excitons would be treated accurately enough (beyond perturbation if necessary), and (2) construct the kinetic kernel of the local excitons that describes their propagation and decay in the system. The first step is strongly case dependent, in both the physical size of the local region and the required treatment of local interaction. The case study of LiF below gives a detailed example of this step. The second step, on the other hand, is quite generic and will be the focus of this study.

Let us define the exciton kinetic kernel T through the one-body equation of motion of the exciton propagator D (in matrix notation),

$$D[H] = D[H_L] + D[H_L]TD[H], \qquad (1)$$

that allows the local exciton (described by $D[H_L]$) to propagate in D[H]. Here, H_L refers to the local Hamiltonian and H the full Hamiltonian containing additional coupling beyond the local region. Note that the excitonic degree of freedom $b_{\mathbf{R}N}^{\dagger}$, as a basis for $D_{\mathbf{R}N,\mathbf{R}'N'}$ and $T_{\mathbf{R}N,\mathbf{R}'N'}$, is defined in the direct product space of the particle p and hole h orbitals at the *same* local region indexed by \mathbf{R} : $b_{\mathbf{R}N}^{\dagger} = c_{\mathbf{R}p}^{\dagger}c_{\mathbf{R}h}$, since only strongly bound excitons smaller than the local region are of interest.

This rigorous definition becomes practically useful with the simplification

$$T \equiv D^{-1}[H_L] - D^{-1}[H]$$

= $(D_0^{-1}[G[H_L]] - I[H_L]) - (D_0^{-1}[G[H]] - I[H])$
 $\cong D_0^{-1}[G[H_L]] - D_0^{-1}[G[H]].$ (2)

Here, $D_0(\mathbf{R}N, \mathbf{R}'N'; t, t') = G(\mathbf{R}p, \mathbf{R}'p'; t, t') * G(\mathbf{R}'h', \mathbf{R}h; t', t)$ is the bare polarization bubble describing unbound pairs of fully dressed particles and holes (described by *G*.) This simplification of the exciton selfenergy *I*[*H*] by its local counterpart *I*[*H*_L] is similar to that previously employed with the dynamical mean field approximation [17]. It is physically reasonable because of the general short-range nature of the self-energy. Particularly, at the lowest order approximation of *I*, employed in practically all first-principles implementations of the BSE, *I*[*H*] = *I*[*H*_L], and this simplification is exact. Once *T* is obtained from Eq. (2), the full spectrum of D[H] can be obtained effortlessly from Eq. (1).

We now use the prototypical LiF to demonstrate the simple method and the deep insights it can offer. Crystal LiF has a simple NaCl structure with a 14.2 eV band gap [18] defined by three occupied F-2p bands and an unoccupied Li-2s band. The strong ionicity of the system implies a dominating short-range attraction between a hole in the F-2p orbitals and a particle in the nearest neighboring Li-2s orbital. We will therefore define a local region containing only one F for simplicity. The straightforward choice is to include one or six (in 3D) neighboring Li atoms as in Figs. 1(a) and 1(b), commonly used in cluster models [19]. These two choices, however, do not respect the rotational and translational symmetry simultaneously without being overcomplete. Figure 1(c) gives a better choice of the local region, containing one F and effectively one Li from combining all its neighboring sites. It respects both the translational and rotational symmetries, and thus forms a good basis for the entire lattice.

The low-energy Hilbert space of such a local region can be constructed by making use of the gauge freedom of the Wannier function [20,21]. Figure 1(d) shows the resulting Wannier orbital centered at the F site, as a symmetric superposition of atomic Li-2s orbitals. Recall a similar construction [22] in the well-known Zhang-Rice singlet in the cuprate. Effectively, the local region is just a "super F atom" containing three p orbital [Fig. 1(e)] and one s'orbital [Fig. 1(d)] [8] in a simple fcc lattice, and the tightly bound excitons can now be viewed effectively as "intraatomic" Frenkel excitons. The excitonic Hilbert space N is



FIG. 1 (color online). Three ways to define local regions via unit cells respecting (a) translational symmetry, (b) rotational symmetry, and (c) both. In case (c), an effective F-s' Wannier orbital (d) composed of symmetric superposition of Li-2s orbitals is compared to a F-2p Wannier orbital (e). (f) Shape of the exciton from product of F-s' and F-2p gives the x-ray matrix element $M_N(\mathbf{q})$ (g) in momentum space. Boxes in (d)–(f) denote the conventional unit cell.

then simply spanned by three local excitons made of a particle in the p = s' orbital and a hole in the $h = p_x$, p_y , or p_z orbital. Obviously, similar construction applies to all charge transfer insulators [23]. Figure 1(f) also demonstrates the probability amplitude of the exciton in real space, obtained from the product of the particle and hole orbitals [24].

Now the exciton kinetic kernel can be easily computed via Eq. (2). For a simple illustration, the fully dressed Green function is obtained approximately from selfconsistent Kohn-Sham Hamiltonian with a +5 eV shift in the on-site energy of s' orbital to counter the selfinteraction error. The corresponding band structure contains a 14.2 eV band gap, consistent with the GW calculation [18,25], where G denotes the Green function and W denotes the screened Coulomb interaction. We then compute the corresponding $D_0[H_L]$ and $D_0[H]$ from the standard convolution (see the Supplemental Material [26]) in the Wannier function basis. The resulting $D_0[H_L]$ contains trivially a pole at $\omega_0 = \epsilon_p - \epsilon_h = 21.9$ eV, corresponding to the energy difference between the particle ϵ_n and the hole ϵ_h . Turning on the local binding interaction $U_B \sim \int dx dx' n_s(x) n_p(x') / |x - x'| \sim 7 \text{ eV}$ simply lowers the pole to $\omega_{\text{exciton}} = \omega_0 - U_B = 14.9 \text{ eV}$ in $D[H_L]$ (ignoring the fine multiplet splitting) [27].

As shown in Fig. 2, the resulting exciton kinetic kernel obtained from Eq. (2) contains several interesting characteristic features. First, the kinetic kernel is strongly energy dependent. This is physically necessary because T needs to generate the correct U_B -dependent kinetics of excitons without the prior knowledge of U_B [to be introduced in $D[H_L]$ through Eq. (1)]. Particularly, T hosts a $1/(\omega - \omega_0) \propto 1/U_B$ decay in all its components. Since T is like the



FIG. 2 (color online). The real (solid lines) and imaginary (dashed lines) parts of exciton kinetic kernel $T(\mathbf{R}N, \mathbf{R}'N)$ for (a) $\mathbf{R}' - \mathbf{R} = (0, 0.5, 0.5)$, (b) $\mathbf{R}' - \mathbf{R} = (0, 0, 1)$, and (c) $\mathbf{R}' - \mathbf{R} = (0, 0, 0)$ for $N = P_x$, P_y , and P_z . The P_x , P_y , and P_z characters are color-coded in black, red (gray), and green (light gray), respectively. Virtual processes of dressed hopping in strong binding limit (d), unbound particle (solid circles with red arrows) and hole (open circles with blue arrows) motion absorbed in off-site (e) and on-site (f) components of T.

hopping integral, this indicates a heavier mass for excitons with stronger binding. This is the exact behavior in the strong coupling limit, in which the exciton can only propagate by virtually moving the particle first (with energy U_B in the intermediate state) followed by the hole to reform the pair, a second order process [Fig. 2(d)] giving $T \sim 2t_p t_h/U_B \propto 1/U_B$ [t_p (t_h) refers to the hopping of the particle (hole)].

Second, the kinetic kernel has an imaginary part spanning over a wide energy range, representing excitonic decaying channels. In fact, its energy span is exactly that of the Landau continuum from unbound excitations. This is not surprising because plugging $D[H_L]$ with unbound excitons $(U_B = 0 \text{ and } D[H_L] = D_0[H_L])$ into Eq. (1) must, by construction, recover exactly the Landau continuum in the resulting $D[H] = D_0[H]$, and the information of the continuum can only come from T. $(D_0[H_L])$ is entirely local.) Physically, this reflects the fact that the definition of $T_{\mathbf{R}N,\mathbf{R}'N'}$ via Eq. (1) integrates out all the virtual processes involving unbound particle and hole traveling independently from \mathbf{R}' to \mathbf{R} [cf. Fig. 2(e)]. Therefore, the resulting T describes the exciton kinetics exactly in the weak binding limit as well.

Third, the kinetic kernel has a significant negative diagonal elements [cf. Fig. 2(c)] that reduces the average exciton energy to $\tilde{\omega}_{\text{exciton}} \sim 13.4 \text{ eV}$ (estimated from $\omega - \omega_{\text{exciton}} - \text{Re}T_{0N,0N}(\omega) = 0$). This renormalization originates from virtual *kinetic* processes illustrated in Fig. 2(f), and is to be distinguished from the binding of local exciton.

Now, plugging $D[H_L]$ and T into Eq. (1), the complete description of exciton propagation and decay is given by the resulting D[H], illustrated by the red spectral intensity of ImD in Fig. 3(a). Notice a striking similarity of the dispersion of the exciton bands to that of the red F-p bands of LiF in Fig. 3(b). This is because the excitons here have the same symmetry properties as the F-2p orbitals [cf. Figs. 1(e) and 1(f)]. Consequently, $T \sim (2t_p/U_B)t_h$



FIG. 3 (color online). (a) Exciton spectrum (red contour) from $\text{Im}D(\mathbf{q}, \omega)$, compared with simple estimation from $\text{Re}T(\omega = 13.4 \text{ eV})$ (dotted curves). (b) LiF band structure containing Li-2s (black line) and F-2p (red lines) bands. (c) Brillouin zone boundaries and high-symmetry points used in (a) and (b), and selected k paths in the xy plane, denoted by ϕ , for Fig. 4.

resembles the hole hopping t_h with a $2t_p/U_B$ reduction that suppresses all longer-range hoppings. (The comparison appears upside down because $t_p < 0$). In essence, contrary to the standard effective mass description [28,29] of Wannier exciton, a strong exciton binding always enhances the tight-binding nature of the excitons, making them propagate more like Frenkel excitons.

The exciton band dispersion can in fact be estimate by simply diagonalizing $\omega_{\text{exciton}} + \text{Re}T(\tilde{\omega}_{\text{exciton}})$ (see the Supplemental Material [26]), since *T* is like the hopping integral for excitons. Indeed, the actual dispersion is resembled very closely by the resulting eigenvalue [dotted curves in Fig. 3(a)], except (1) a weaker dispersion near the bottom of the exciton bands, due to the above-mentioned decay of $T(\omega)$ at lower energy, and (2) broadened exciton peak near the top of the exciton bands, reflecting a shorter lifetime from decaying into the Landau continuum encapsulated in Im*T*.

Interestingly, our calculation indicates that all three branches of the excitons can be partially observed experimentally. Naively, given the *p* character of the probability amplitude $M_N(\mathbf{q}) = \int d\mathbf{x} \exp^{-i\mathbf{q}\cdot\mathbf{x}} \langle \mathbf{x} | \mathbf{0} p \rangle \langle \mathbf{0} h | \mathbf{x} \rangle$ [24] shown in Fig. 1(g), one expects that only the longitudinal mode can be observed. However, in reality the zone folding (umklapp coupling) always hybridizes the longitudinal and the transverse branches near the zone boundaries in most off-high-symmetry directions. This is clearly demonstrated in our resulting charge susceptibility $\chi(\mathbf{q}, \omega) =$ $\sum_{NN'} M_N(\mathbf{q}) D_{NN'}(\mathbf{q}) M_{N'}^*(\mathbf{q})$, shown in Fig. 4(a) [30]. Even with the strong spectral weight suppression in $q < 0.5, q \sim 1.5-2$, and $q > 5(2\pi/a)$ from $M_N(\mathbf{q})$, one still observes a clear switching from one exciton band to another at $q \sim 3.5$ for $\phi = 7.5^\circ$, at $q \sim 3.25$ for 30° , and at $q \sim 3.25$ and $q \sim 4$ for 37.5°.

We verify these results by performing inelastic x-ray scattering along different q directions between (100) and (110) (see the Supplemental Material [26]), and comparing to the theoretical response function. The agreement, illustrated in Fig. 4(b), is good in three different respects. First, there is close correspondence in the momentum dependence of the intensity. Second, the dispersion agrees well, with close correspondence between the overall bandwidth and locations of the extrema. Finally, clear indications of the predicted switching between exciton bands (most visible at $\phi = 37.5^{\circ}$) are observed, despite the resolution-related broadening in the experimental data. The dispersion and switching are even clearer when viewed on line plots (see the Supplemental Material [26]). This is, to our knowledge, the first experimental observation of multiexciton band dispersion in an insulator of any kind.

We stress that the "invisible" part of the exciton band structure also represents physical channels of exciton kinetics for propagation, scattering, and decay processes. It is merely invisible to this particular experimental probe. Therefore, it is essential to obtain the *full* exciton band



FIG. 4 (color online). (a) Imaginary part of dynamical linear response function χ in selected directions (cf. Fig. 3). The theoretical intensity for $q \leq 1.5$ is reduced by 2.6 to mimic screening by the plasmon pole. (b) Exciton dispersion measured by inelastic x-ray scattering in the same directions. The correspondence in the q dependence of the intensity is good. The dispersion and branching are also in good agreement (see the line plots provided in the Supplemental Material [26]). Vertical dashed lines indicate the Brillouin zone boundaries (cf. Fig. 3).

structure theoretically. However, to keep the entire exciton band structure using the standard two-body BSE formulation would be many orders of magnitudes more expensive, if even affordable, as it requires keeping the three momentum and four band indices. In contrast, our approach gives easy and intuitive access to the full exciton band structure, with superior efficiency necessary for practical applications.

Finally, several important aspects of our method are worth mentioning. First, our real-space formulation is particularly suitable for treating exciton scattering from surfaces, impurities, or other boundary conditions that disrespect translational symmetry. Second, the separation of the nonlocal kinetics from the local binding of the exciton in our framework allows a more accurate manybody treatment of the local excitation in $D[H_L]$ (say, via exact diagonalization) before applying Eq. (1). This is particularly important in strongly correlated systems, in which significant multiplet splitting [23] exists. Furthermore, such separation of the problem reduces significantly the computational expense of exciton dynamics: Evaluation of exciton kinetic kernel T involves no interaction, while the potentially expensive interacting problem is only local. On top of that, our use of the Wannier function as basis, and the implicit absorption of virtual pairbreaking processes, further reduces the computation greatly. For a simple illustration of the superior scaling of our method, the standard BSE requires $\sim 10^8$ elements of the particle-hole interaction [25], while our method needs only $\sim 10^4$ elements. Our real-space approach can straightforwardly incorporate scattering via impurities or boundary conditions, and thus will find broad applications in the studies and engineering of excitons in modern functional materials, including doped semiconductors and strongly correlated transition metal oxides, as well as their nanostructures, thin films, and heterogeneous interfaces.

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