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A rough set-based association rule approach implemented on exploring beverages product spectrum

Shu-Hsien Liao

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Abstract When items are classified according to whether they have more or less of a characteristic, the scale used is referred to as an ordinal scale. The main characteristic of the ordinal scale is that the categories have a logical or ordered relationship to each other. Thus, the ordinal scale data processing is very common in marketing, satisfaction and attitudinal research. This study proposes a new data mining method, using a rough set-based association rule, to analyze ordinal scale data, which has the ability to handle uncertainty in the data classification/sorting process. The induction of rough-set rules is presented as method of dealing with data uncertainty, while creating predictive if-then rules that generalize data values, for the beverage market in Taiwan. Empirical evaluation reveals that the proposed Rough Set Associational Rule (RSAR), combined with rough set theory, is superior to existing methods of data classification and can more effectively address the problems associated with ordinal scale data, for exploration of a beverage product spectrum.

Keywords Data mining · Rough set · Association rule ·
 Rough set association rule · Ordinal scale data processing ·
 Product spectrum

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44 1 Introduction

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When items are classified according to whether they have more or less of a characteristic, the scale used is referred to as an ordinal scale. The main characteristic of the ordinal scale is that the categories have a logical or ordered to

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relationship to each other. These types of scale permit the measurement of degrees of difference, but not the specific amount of difference, such as market segmentation. Thus the ordinal scale data processing is very common in marketing, satisfaction and attitudinal research. Any questions that ask the respondent to rate something are using ordinal scales. Likert scales are commonly used in attitudinal measurements. This type of scale uses a five-point scale ranging from strongly agree, agree, neither agree nor disagree, disagree, strongly disagree to rate people's attitudes. Although some researchers treat them as an *interval scale*, however we do not really know that the distances between answer alternatives are equal. Hence only the mode and median can be calculated, but not the mean. The range and percentile ranking can also be calculated. Ordinal measurements describe order, but not relative size or degree of difference between the items measured. In this scale type, the numbers assigned to objects or events represent the rank order (1st, 2nd, 3rd, etc.) of the entities assessed. In mathematical order theory, an ordinal scale defines a total preorder of objects (in essence, a way of sorting all the objects, in which some may be tied). The scale values themselves (such as labels like "great", "good", and "bad"; 1st, 2nd, and 3rd) have a total order, where they may be sorted into a single line with no ambiguities. If numbers are used to define the scale, they remain correct even if they are transformed by any monotonically increasing function. This property is known as the order isomorphism [10].

In decision making, many classical representations of preferences are cardinal (typically expected utility, or more elaborated models as Choquet expected utility based on monotone measures). They deal with utility functions which are real-valued, and use standard operations of arithmetic such as addition and multiplication [57]. However, it is nei-

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ther always easy nor desirable to deal with cardinal util-109 110 ity functions. A first noticing is that ordinal information is easier to get than cardinal one, and moreover, there are 111 112 many situations where only order is relevant, cardinals being merely used by tradition and convenience. More fun-113 damentally, the dominant viewpoint in economics, intro-114 115 duced by Hicks and Allen [27], is that utility is related to observable choices (revealed preferences), and any in-116 trospective judgments on intensity of preference should 117 be discarded since meaningless. As a consequence, if the 118 only purpose of utility is to explain choices, then util-119 ity is ordinal in nature [1]. In artificial intelligence, ordinal scale data processing on ranking, preference, ordinal measurement, classification, and categorization are imple-122 123 mented on different problem domains, such as: decision model [4, 7, 20, 30, 55], finite ordinals category on chronol-124 125 126 127 128 129 130 131 ogy [50], multi-criteria development [23, 47], measurement scale development [12, 54], medical study [9] and evaluation [37].

On the other hand, in physics, a spectrum is a series of colored bands of light, diffracted and arranged in the order of their respective wave lengths, produced by the passage of white light through a prism, or other diffracting medium. A spectrum may include many smaller spectrums; for example, the electromagnetic radiation spectrum includes the light spectrum, radio spectrum, infrared spectrum, etc. Beyond physics, a spectrum is a condition that is not limited to a specific set of scales or values, but can vary infinitely, within a continuum or sequence. Since the word saw its first scientific use within the field of optics, to describe the rainbow of the colors of visible light, when separated by a prism, it has been applied in many other fields. Thus, one might talk about a spectrum of political opinion, or the spectrum of activity of a drug, autism spectrum, or specific market segmentation. In these cases, values within the spectrum are not necessarily discrete numbers, as in optics: exact values within this type of spectrum are not precisely quantifiable. Such use implies a broad range of conditions, or behaviors, grouped together and studied under a single title, for ease of discussion. In most modern usages of the word, "spectrum", there is a unifying theme, between extremes at either end, the ordinal events set out below. Accordingly, to obtain a spectrum, the measured function must be transformed into independent scales/variables, with frequencies and the dependent variable must be reduced to the regions, over which the independent variable extends [39].

¹⁵⁵ Consumers prefer certain products, so there is an as-¹⁵⁶ sociated decision-making spectrum. An effective visualiza-¹⁵⁷ tion tool, especially for stakeholders, or managers, is a ¹⁵⁸ brand/product spectrum diagram, which highlights where ¹⁵⁹ the company's brands and products are situated, compared ¹⁶⁰ to other competitors. Some businesses have difficulty in un-¹⁶¹ derstanding their brand attributes and how their products

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fit into the retail landscape. Often, when questioned, com-163 164 panies espouse a wish to fulfill all promises to all people. However, this approach is often limiting, as a strat-165 egy, as it is lacking in targeted vision and segmentation. 166 Therefore, it must be asked whether a business can better 167 understand its consumers, by realizing its own position in 168 the industry, with respect to its specific product segmen-169 tation. However, this is easier said than done, since cus-170 171 tomers' opinions are known only to customers. The information is available, but difficult to access, and without an 172 effective method there is little hope of exploring the full 173 174 volume of data that might be collected. Thus, the effec-175 tive processing and use of this data is increasingly important [51, 56]. 176

177 Data mining is the process of discovering significant 178 knowledge, such as patterns, associations, changes, anoma-179 lies and significant structures, from the large amounts of data 180 stored in databases, data warehouses, or other information 181 repositories [39]. Therefore, knowledge of customers, ex-182 tracted through data mining, can be combined with customer 183 profiles, purchased preferences, records of purchased prod-184 ucts and marketing knowledge, from research. This knowl-185 edge then provides an understanding of consumers, as well 186 as the product spectrum in a market. Association rules are 187 a data mining method. Previous studies in mining associa-188 tion rules have had two deficiencies. Firstly, the discovery 189 of rules from ordinal data has been ignored. Secondly, the 190 discovery of rules from imprecise data has also been ig-191 nored [14]. Corporations, ranging from Coca-Cola, Nestle 192 and McDonald's to Disney and Sony, have invested millions 193 of dollars in developing their corporate image. However, the 194 biggest threats to brand equity are not likely to be trade-195 mark or patent infringements, but rather the firm's own ac-196 tions, or those of its myriad of agents, joint venture/alliance 197 partners, suppliers and subsidiaries [21]. In commerce, busi-198 nesses use branding to differentiate their products and ser-199 vices, or offerings from those of their competitors [6, 34]. 200 The brand incorporates a set of product or service features 201 that are associated with that particular brand name and at-202 tribute [11]. Data classification is used to reduce the large 203 number of conditional attributes, based on the value of the 204 decisional attribute, as well as to extract the key charac-205 teristics of certain groups from a wide spectrum of cus-206 tomer attributes [17]. An effective visualization tool, espe-207 cially for stakeholders or managers, is a brand spectrum di-208 agram, which highlights where the company's brands and 209 products are situated, compared to other competitors. Some 210 businesses have difficulty in understanding their brand at-211 tributes and how their products fit into the retail landscape. 212 Often, when questioned, companies espouse a wish to fulfill 213 all promises to all people. However, this approach is often 214 limiting, as a strategy, lacking in targeted vision and seg-215 mentation [39]. 216

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A rough set-based association rule approach implemented on exploring beverages product spectrum

217 Accordingly, this study investigates the concept of the 218 product spectrum, by the analysis of algorithms, to sort 219 consumer product preferences and then provide the appro-220 priate decisions. The empirical evaluation reveals that the proposed Rough Set Associational Rule (RSAR), combined with the rough set theory, is superior to existing methods, for ordinal scale data classification, and can more effectively address the marketing issue associated with the investigation of product spectrum on the beverage market in Taiwan. The rest of this paper is organized as follows. Section 2 reviews literature relevant to this research. Section 3 considers the ordinal scale data. Section 4 uses a rough set method to generate associational rules. Computational experiments and conclusion are presented in Sects. 5 and 6.

2 Research background

2.1 Literature review of the development of RST

Rough set theory (RST) was originally proposed by Pawlak, in the 1980's, as a mathematical approach to aid decision making in the presence of uncertainty. It can be used not only as the basis of formal reasoning, with uncertain information, machine learning, knowledge extraction and demand forecasting [31, 44, 65], but also as for a tool for data analysis and autonomous decision-making, and has been used to extract knowledge from datasets [16, 44]. It classifies imprecise, uncertain, or incomplete information, expressed in terms of data acquired from experience [5, 29, 33]. The Pawlak rough set model provides a mathematical tool for the determination of data dependencies and the reduction of the number of features contained in a dataset, using purely structural methods. RST is a theory for the study of intelligent systems, which are characterized by inexact, uncertain, or vague information. In less than two decades, rough sets theory has rapidly established itself in many real-life applications [31]. Presently, rough set theory is used in many fields, such as learning, intelligent systems, inductive reasoning, pattern recognition, image processing, signal analysis, knowledge discovery, decision analysis and environment quality [24, 42, 44, 52, 53, 59]. It has become a key topic in the research area of information science [31, 62]. An information system is a quadruple $S = \{U, A, V, f\}$, where U is a finite set of objects, called the universe, A is a finite set of attributes, V is a domain of attribute a and $f: U \times A \rightarrow V$ is called an information function, such that f(x, a) [40]. Any union 266 of elementary sets is called a crisp set and other sets are 267 referred to as rough sets. Ziarko [64] describes the tech-268 nique as non-statistical and notes that it has been devel-269 oped with full mathematical rigor, within the realm of logic 270

and set theory. In one sense, this is strength, given that 271 272 there are no explicit distributional assumptions and no re-273 quirements for selection of functional forms. Rough set 274 theory allows easy acquisition knowledge from data, even 275 when the operator has limited prior knowledge. Addition-276 ally, the model has the ability to reduce superfluous vari-277 ables, is easily commanded with 'IF THEN' statements 278 and can be easily modified [38]. Therefore, rough sets 279 can be considered as uncertain or imprecise as the follow-280 ing [15, 25].

281 An attribute a is a mapping $a: U \to Va$ where U is 282 a non-empty finite set of objects (called the universe) and 283 Va is the value set of a. An information system is a pair 284 T = (U, A) of the universe U and a non-empty finite set A 285 of attributes. Let B be a subset of A. The B-indiscernibility 286 relation is defined by an equivalence relation I_B on U such 287 that $I_B = \{(x, y) \in U_2 \mid \forall a \in B \cdot a(x) = a(y)\}$. The equiv-288 alence class of I_B for each object $x \in U$ is denoted by 289 [x]B. Let X be a subset of U. We define the lower and 290 upper approximations of X by $B(X) = \{x \in U | [x] | B \subseteq X\}$ 291 and $B(X) = \{x \in U \mid [x]B \cap X \neq \emptyset\}$. A subset B of A 292 is a reduct of T if $I_B = I_A$ and there is no subset B of 293 B with $I_B = I_A$ (i.e., B is a minimal subset of the con-294 dition attributes without losing discernibility). A decision 295 table is an information system $T = (U, A \cup \{d\})$ such that 296 each $a \in A$ is a condition attribute and $d \notin A$ is a decision 297 attribute. Let V_d be the value set $\{d_1, \ldots, d_u\}$ of the deci-298 sion attribute d. For each value $d_i \in V_d$, we obtain a decision 299 class $U_i = \{x \in U \mid d(x) = d_i\}$ where $U = U_1 \cup \cdots \cup U \mid V_d$ 300 and for every $x, y \in U_i, d(x) = d(y)$. The *B*-positive region 301 of d is defined by $P_B(d) = B(U_1) \cup \cdots \cup B(U \mid V_d \mid)$. A sub-302 set B of A is a relative reduct of T if $P_B(d) = P_A(d)$ and 303 there is no subset B of B with $P_B(d) = P_A(d)$. We define a 304 formula $(a_1 = v_1) \land \cdots \land (a_n = v_n)$ in *T* (denoting the con-305 dition of a rule) where $a_i \in A$ and $v_i \in Va_i$ $(1 \le j \le n)$. 306 The semantics of the formula in T is defined by $[(a_1 = v_1) \land$ 307 $\cdots \wedge (a_n = v_n)$]] $T = \{x \in U | a_1(x) = v_1, \dots, a_n(x) = v_n\}.$ 308 Let ϕ be a formula $(a_1 = v_1) \land \cdots \land (a_n = v_n)$ in T. A deci-309 sion rule for T is of the form $\phi \rightarrow (d = d_i)$, and it is true if 310 $\llbracket \phi \rrbracket T \subseteq \llbracket (d = d_i) \rrbracket T (= U_i)$. The accuracy and coverage of 311 a decision rule r of the form $\phi \rightarrow (d = d_i)$ are respectively 312 defined as follows: 313

$$accuracy(T', r, U_i) = \frac{|U_i \cap \llbracket \phi \rrbracket_{T'}|}{|\llbracket \phi \rrbracket_{T'}|}$$
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$$accuracy(T', r, U_i) = \frac{|U_i \cap \llbracket \phi \rrbracket_{T'}|}{|U_i|}$$
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In the evaluations, $|U_i|$ is the number of objects in a decision class U_i and $[[\phi]]_{T'}|$ is the number of objects in the universe $U = U_1 \cup \cdots \cup U |V_d|$ that satisfy condition ϕ of rule r. Therefore, $|U_i \cap [[\phi]]_{T'}|$ is the number of objects satisfying the condition ϕ restricted to a decision class U_i . 320 321 322 323 324

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5 2.2 Previous research of RST functionalities

Kryszkiewicz [35, 36] assigned a null value, to replace all the incomplete attribute values. The null value represents all of the possible values attainable by the attribute with an incomplete value. Felix et al. [18, 19] solved the incomplete information problem by introducing rough discernibility relations, i.e. surely discernible and possibly indiscernible. These relations were used for the derivation of rules, to replace the original indiscernibility relation, in an incomplete information system. Some studies [13, 26, 31–33, 43, 49, 60, 61] used a hybrid approach to deal with incomplete data.

Walczak and Massart [58] mentioned that the "application of RST to qualitative attributes is straightforward. For nominal attributes, RST offers evident advantages when compared with other classifiers". Previous studies of the application of rough sets in intelligent systems, focused on classification accuracy and on preserving the information, or the order generated by the ordinal decision classes. Huang et al. [28] used a RST approach for intelligent systems and their results showed that their method could reduce the number of conditional attributes used in motherboard EMI fault diagnosis and maintain acceptable classification accuracy. The theory has a strong mathematical foundation and is well suited to deal effectively with various decision problems. It can be employed to extract concepts, or decision rules, from a given set of data, and has been used successfully in many application domains [19, 22]. In another article, John W.T. Lee et al. [29] mentioned that, in the article "rough set theory has been successfully applied in selecting attributes to improve the effectiveness in deriving decision trees/rules for decisions and classification problems. When decisions involve ordinal classes, the rough set reduction process should try to preserve the order relation generated by the decision classes". They proposed a new way of evaluating and determining reducts, involving ordinal decision classes, which focused on the order generated by the ordinal decision classes. Zhao et al. [63] present a hormone based nearest neighbor classification algorithm for data stream classification, in which the classifier is updated every time a new record arrives. The records could be seen as locations in the feature space, and each location can accommodate only one endocrine cell.

³⁷¹ 2.3 Association rules

Associations in complex data objects, such as data items, occur when one set of attributes is likely to co-occur with another set. The prototypical application is the analysis of supermarket transactions where associations like '68 % of all customers who buy fish also buy white wine' may be

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found in a transaction database. For knowledge discoverydata mining-in databases, an association is a rule to be mined from databases which infers an attribute set from another. As stated by Agrawal et al. discovering association rules is an important data mining problem, and there has been considerable research in using association rules in the field of data mining problems [2]. The association rules algorithm is used mainly to determine the relationships between items or features that occur synchronously in databases. For instance, during a trip to the shopping center, if the people who buy item X also buy item Y as well, there exists a relationship between item X and item Y. Such information is useful for decision makers. Therefore, the main purpose of implementing the association rules algorithm is to find synchronous relationships by analyzing random data and to use these relationships as a reference for decision-making. The association rules are defined as follows [46].

Make $I = \{i_1, i_2, \dots, i_m\}$ the item set, in which each item 398 represents a specific literal. D stands for a set of transac-399 tions in a database in which each transaction T represents 400 an item set such that $T \subseteq I$. That is, each item set T is 401 a non-empty sub-item set of I. The association rules are 402 403 an implication of the form $X \to Y$, where $X \subset I, Y \subset I$ and $X \cap Y = \Phi$. The rule $X \to Y$ holds in the trans-404 405 action set D according to two measurement standards-406 support and confidence. Support (denoted as Sup(X, D)) 407 represents the rate of transactions in D containing the item 408 set X. Support is used to evaluate the statistical impor-409 tance of D, and the higher its value, the more important 410 the transaction set D is. Therefore, the rule $X \to Y$ which 411 has support Sup($X \cup Y, D$) represents the rate of trans-412 actions in D containing $X \cup Y$. Each rule $X \to Y$ also 413 has another measuring standard called confidence (denoted 414 as $Conf(X \to Y)$), representing the rate of transactions in 415 D that contain X and also Y. That is, $Conf(X \to Y) =$ 416 $Sup(X \cap Y)/Sup(X, D).$ 417

In this case, $Conf(X \rightarrow Y)$ denotes that if the transac-418 tion includes X, the chance that transaction also contains Y419 is relatively high. The measure of confidence is then used 420 to evaluate the level of confidence about the association 421 rules $X \to Y$. Given a set of transactions D, the problem 422 of mining association rules is used to generate all transac-423 tion rules that have certain user-specified minimum support 424 (called Min sup) and confidence (called Min conf). Accord-425 ing to Agrawal et al. the problem of mining association rules 426 427 can be broken down into two steps. The first step is to de-428 tect a large item set whose support is greater than Min sup 429 and the second step is to generate association rules, using 430 the large item set. Such rules must satisfy the following two 431 conditions [3]:) 432

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A rough set-based association rule approach implemented on exploring beverages product spectrum

1. $Sup(X \cup Y, D) \ge Min sup$

2. $Conf(X \rightarrow Y) > Minconf$

To illustrate the concepts, we use a small example from the supermarket domain. The set of items is I =*{milk, bread, butter, beer}* and a small database containing the items (1 codes presence and 0 absence of an item in a transaction) is shown in the table to the right. An example rule for the supermarket could be {butter, bread} \rightarrow {milk} meaning that if butter and bread are bought, customers also buy milk.

In addition, to explore association rules, many researchers use the Apriori algorithm [2]. In order to reduce the possible biases incurred when using these measurement standards, the simplest way to judge the standard is to use the *lift* judgment. Lift is defined as: Lift = Confidence $(X \rightarrow Y)/Sup(Y)$.

2.4 Rough set association rules

The primary difficulty associated with the maximal association approach is that the generation of frequent maximal set is based on an underlying assumption-a taxonomy existing for the document collections. However, this assumption may be only feasible for collections of labeled documents with keywords which are mainly for training text classifiers and very expensive to construct, therefore limiting the general applicability of this approach. In addition, Bi et al. investigate the applicability of Rough Set theory to detecting maximal associations [8]. The work reported on some other papers shows that by using Rough Set, rules discovered are similar to maximal association rules, and the rough set approach is much simpler than the maximal association method in discovering association rules for knowledge discovery and reasoning on different data format/scale problem [45, 55].

In view of the prior research, this research does not discuss the rules of order, but rather focuses on decision-makers for consumer product preferences. Thus, this study proposes a new data mining approach, which analyzes ordinal scale data and has the ability to handle uncertainty in the data classification/sorting process. In the domain of knowledge extraction, rough set theory offers the benefits of efficiency, understandability and results that can be interpreted directly. This paper proposes the induction of rough-set rules, to deal with data uncertainty, while creating predictive if-then rules that generalize data values for the beverage industry.

3 Ordinal scale data processing

Traditional association rules ignore the discovery of rules from ordinal data. This study combines association rules with Rough sets, to create an application for ordinal scale 486

Table 1 Example database with 4 items and 5 transactions of association rules

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lion rules					488
Transaction ID	Milk	Bread	Butter	Beer	489
1	1	1	0	0	490 491
2	0	0	1	0	492
3	0	0	0	1	493
4	1	1	1	0	494
5	0	1	0	0	495

Table 2 Information system: ordinal scale data sets

U	A							
	a_1	a_2	<i>a</i> ₃	<i>a</i> ₄	<i>a</i> 5	a_6	a_7	<i>a</i> ₈
1	1	5	7	4	3	2	8	6
2	1	6	8	2	4	5	3	7
3	1	7	2	4	6	5	3	8
4	1	2	3	5	7	6	4	8
5	1	3	6	2	4	5	8	7

data. The processing of ordinal scale data is described in Table 1.

Definition 1 Transform the questionnaire answers into information system IS = (U, A), where $U = \{x_1, x_2, \dots, x_i\}$ is a finite set of objects and $i = 1, \dots, n, A = \{a_1, a_2, \dots, a_i\}$ is a finite set of general attributes/criteria and $j = 1, \ldots, m$. $f_a = U \times A \rightarrow V_a$ called the information function, V_a is the domain of the attribute/criterion a, and f_a is a ordinal function set such that $f(x, a) \in V_a$ for each $x_i \in U$.

Example Table 2 shows the ranking of non-alcoholic beverages, from the first to eighth, by x_1 , named Tea, Packagedwaters, Sports, Juice, Soda, Others, Coffee and Energy.

Then:

$f = \{1\}$ $f = \{2, 3, 5, 6, 7\}$	525
$Ja_1 = \{1\}, \qquad Ja_2 = \{2, 3, 5, 6, 7\},$	526
$f_{a_3} = \{2, 3, 6, 7, 8\}, \qquad f_{a_4} = \{2, 4, 5\}$	527
$f_{a_5} = \{3, 4, 6, 7\}, \qquad f_{a_6} = \{2, 5, 6\},$	528
$f_{a_{1}} = \{3, 4, 8\}, \qquad f_{a_{2}} = \{6, 7, 8\}$	529
Ju_1 (c, ., c), Ju_8 (c, ., c)	530
$V_{a_1}^{x_1} = 1, \qquad V_{a_2}^{x_1} = 5, \qquad V_{a_3}^{x_1} = 7, \qquad V_{a_4}^{x_1} = 4$	531
$V_{a_5}^{x_1} = 3, \qquad V_{a_6}^{x_1} = 2, \qquad V_{a_7}^{x_1} = 8, \qquad V_{a_8}^{x_1} = 6$	532
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Definition 2 According to specific universe of discourse	534

Definition 2 According to specific universe of discourse classification, a similarity relation of the general attributes $a \in A$, denoted by $\frac{U}{A}$. All of the similarity relation, denoted by $R(a_i)$.

$$\frac{U}{A} = \left\{ [x_i]_A | x_i \in U \right\}$$
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$$[X_i]_A[X_i] \subset O$$
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 Table 3
 The core attribute values of the ordinal scale data for nonalcoholic beverages

 Table 4 Decision-making table showing drinking habits for "nonalcoholic beverages"

$R(a_j)$	f_{a_5}	f_{a_6}	D_{c}
${x_1}$	3	2	D
$\{x_2, x_5\}$	4	5	D_{i}
${x_3}$	6	5	D_{i}
${x_4}$	7	6	D_{i}
$R(a_i)$	f_{a_5}	f_{a_6}	D_{i}

Example

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 $R(a_3) = \{\{x_1\}, \{x_2\}, \{x_3\}, \{x_4\}, \{x_5\}\},\$ $R(a_5) = \{\{x_1\}, \{x_2, x_5\}, \{x_3\}, \{x_4\}\},\$ $R(a_6) = \{\{x_1\}, \{x_2, x_3, x_5\}, \{x_4\}\},\$ $R(a_7) = \{\{x_1, x_5\}, \{x_2, x_3\}, \{x_4\}\},\$

Definition 3 The Information system is an ordinal scale data, therefore between the two attributes will have the ordinal response, where D_a is the pair wise comparison results of ordinal scale data, which are defined as follows,

$$D_a^+ = \left\{ x_i \left| \frac{U}{a}, V_{a_1} > V_{a_j} \right\}, \qquad D_a^- = \left\{ x_i \left| \frac{U}{a}, V_{a_i} < V_{a_j} \right. \right\}$$

Then, using the concept of similarity relation in rough set theory foundation, and finding the value of ordinal scale data between a_i and a_j , where ind(B) is the core attribute value of ordinal scale data in the first step, and B is the subset of A.

$$ind(B) = [f_a]_{B \subseteq A} = \bigcap_{B \subseteq A} \left[\frac{U}{a}\right]$$

Example According to the similarity relation and the fact that $R(a_5) = \{\{x_1\}, \{x_2, x_5\}, \{x_3\}, \{x_4\}\}$ and $R(a_6) = \{\{x_1\}, \{x_2, x_3, x_5\}, \{x_4\}\}$ both belong to the same fundamental set, the ordinal function set is $f_{a_5} = \{3, 4, 6, 7\}$ and $f_{a_6} = \{2, 5, 6\}$. Therefore, a_5 and a_6 are both core attribute values of the ordinal scale data for non-alcoholic beverages and for customer x_1 , x_3 and x_4 , a_5 always places after a_6 , denoted by D_a^+ . The pair wise comparison of a_5 and a_6 , as shown in Table 3.

 $ind(B) = [a_5, a_6]$

4 Rough set method for the generation of associational rules

Definition 4 As a first step, this study identifies the core at tribute values of ordinal scale data. In this step, the object
 tribute values of ordinal scale data.

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U	General attributes, Q				Dee	cision attributes
	g_1	<i>g</i> ₂	<i>g</i> ₃	<i>8</i> 4	Pro	duct ranking
l	g_{1_1}	g_{2_1}	<i>g</i> ₃₁	g_{4_1}	3	<i>a</i> 5
	g_{1_1}	g_{2_2}	g_{3_1}	g_{4_2}	6	a_5
	g_{1_2}	g_{2_1}	<i>8</i> 3 ₂	g_{4_1}	6	<i>a</i> 5
	g_{1_2}	g_{2_1}	<i>8</i> 3 ₂	g_{4_1}	7	<i>a</i> ₅
5	g_{1_1}	g_{2_2}	g_{3_1}	<i>8</i> 4 ₂	5	a_5

generates the rough associational rule. The consideration of other attributes and the core attributes of ordinal scale data as the highest decision-making attributes is used to establish the decision table and to generate rules, as shown in Table 4.

DT = (U, Q), where $U = \{x_1, x_2, \dots, x_i\}$ is a finite set 614 of objects and i = 1, ..., n, Q is usually divided into two 615 parts. $G = \{g_1, g_2, \dots, g_i\}$ is a finite set of general at-616 617 tributes/criteria and $j = 1, ..., m, D = \{d_1, d_2, ..., d_l\}$ is a 618 set of decision attributes and k = 1, ..., p. $f_g = U \times G \rightarrow$ V_g is called the information function, V_g is the domain of 619 620 the attribute/criterion, g, and f_g is a total function, such that 621 $f(x, g) \in V_g$, for each $g \in Q$; $x \in U$. $f_d = U \times D \rightarrow V_d$ is 622 called the sorting decision-making information function, V_d 623 is the domain of the decision attributes/criterion, d, and f_d 624 is a total function, such that $f(x, d) \in V_d$, for each $d \in Q$; 625 $x \in U$.

Then:

Definition 5 According to the specific universe of discourse classification, a similarity relation for the general attributes is denoted by $\frac{U}{G}$. All of the similarity relations are denoted by $R(g_t)$ and t is the combination of all the general attributes.

$$R(g_t) = \frac{U}{G} = \left\{ [x_i]_G | x_i \in U \right\}$$

Example

$$R_1 = \frac{U}{g_1} = \left\{ \{x_1, x_2, x_5\}, \{x_3, x_4\} \right\}$$

$$R_2 = \frac{U}{g_2} = \{\{x_1, x_3, x_4\}, \{x_2, x_5\}\}$$
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ind(B)	R	Product features g_1	Product information source g_2	Consumer behavior g_3	Channels g ₄	Decision attributes D (sports)
$\frac{U}{g_1g_2g_3g_4}$	${x_1}$	Price	Seen on shelves	Purchased due to promotions	Convenience stores	Third $d_{a_5}^1 = 3$
	$\{x_2, x_5\}$	Price	Advertising	Purchased due to promotions	Hypermarkets	Sixth $d_{a_5}^2 = 6$ Fifth $d_{a_5}^5 = 5$
	$\{x_3, x_4\}$	Brand	Seen on shelves	Not purchased due to promotions	Convenience stores	Sixth $d_{a_5}^3 = 6$ Seventh $d_{a_5}^4 =$
$\frac{U}{g_2g_4}$	$\{x_2, x_5\}$	Price	Advertising	Purchased due to promotions	Hypermarkets	Fourth $d_{a_5}^2 = 4$ Fourth $d_{a_5}^2 = 4$
	$\{x_1, x_3, x_4\}$	Price	Seen on shelves	Purchased due to promotions		Third $d_{a_5}^1 = 3$
		Brand		Not purchased due to promotions	Convenience stores	Sixth $d_{a_5}^3 = 6$
		Brand		Not purchased due to promotions		Seventh $d_{a_5}^4 =$

$$R_5 = \frac{U}{g_2g_4} = \{\{x_1, x_3, x_4\}, \{x_2, x_5\}\}$$

$$R_t = \frac{U}{g_1 g_2 g_3 g_4} = \{\{x_1\}, \{x_2, x_5\}, \{x_3, x_4\}\}$$

Definition 6 By the similarity relation, and determination of the reduct and core, the attribute, g, of G and the set G, which was ignored, has no effect, so g is an unnecessary attribute and can be reducted. $R \subseteq G$ and $\forall_g \in R$. A similarity relation for the general attributes of the decision table is denoted by ind(G). If $ind(G) = ind(G - g_1)$, then g_1 is the reduct attribute and if $ind(G) \neq ind(G - g_1)$, then g_1 is the core attribute.

Example

$$\frac{U}{ind(G)} = \{\{x_1\}, \{x_2, x_5\}, \{x_3, x_4\}\}$$

$$\frac{U}{ind(G)} = \{\{x_1\}, \{x_2, x_5\}, \{x_3, x_4\}\}$$

$$\frac{U}{ind(G - g_1)} = \frac{U}{g_2g_3g_4} = \{\{x_1\}, \{x_2, x_5\}, \{x_3, x_4\}\}$$

$$= \frac{U}{ind(G)} = \frac{U}{g_1g_2g_3g_4}$$

$$\frac{U}{ind(G - g_1g_3)} = \frac{U}{g_2g_4} = \{\{x_1, x_3, x_4\}, \{x_2, x_5\}\}$$

$$\frac{U}{ind(G)} = \frac{U}{g_1g_2g_3g_4}$$

When considering g_1 , alone, g_1 is the reduct attribute, but when considering g_1 and g_3 , simultaneously, g_1 and g_3 are the core attributes. A similarity relation and the relational attribute value are shown in Table 5.

Definition 7 The lower approximation, denoted as G(X), is defined as the union of all of the elementary sets that are contained in $[x_i]_G$. More formally:

$$\underline{G}(X) = \bigcup \left\{ [x_i]_G \in \frac{U}{G} \middle| [x_i]_G \subseteq X \right\}$$

The upper approximation, denoted as $\overline{G}(X)$, is the union of those elementary sets that have a non-empty intersection with $[x_i]_G$. More formally:

$$\overline{G}(X) = \bigcup \left\{ [x_i]_G \subseteq \frac{U}{G} \middle| [x_i]_G \cap X \neq \phi \right\}$$

The difference: $Bn_G(X) = \overline{G}(X) - G(X)$ is called a boundary of $[x_i]_G$.

Example $\{x_1, x_2, x_4\}$ are the customers of interest, so $\underline{G}(X) = \{x_1\}, \ \overline{G}(X) = \{x_1, x_2, x_3, x_4, x_5\} \text{ and } Bn_G(X) =$ $\{x_2, x_3, x_4, x_5\}.$

Definition 8 Using the traditional association rule to calculate the value of Support and Confidence, the formula is shown as follows:

$$Sup(ind(B)) = \left| \left\{ ind(B) | \underline{G}(X) \subseteq \overline{G}(X) \right\} \right|$$
$$- \left| ind(B) | \underline{G}(X) \right|$$

$$\frac{nd(B)|\underline{G}(X)|}{\overline{G}(X)}$$
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$$Conf(ind(B) \to d_{g_m}) = \left| \left\{ ind(B) \cap d_{g_m} \left| Sup(ind(B)) \right\} \right|$$
$$= \left| \frac{Sup(ind(B) \cap d_{g_m})}{Sup(ind(B))} \right|$$

Definition 9 Rough set-based association rules.

$$\frac{\{x_1\}}{g_1g_3}: g_{1_1} \cap g_{3_1} \quad \Rightarrow \quad d^1_{d_1} = 4$$
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$$\frac{\{x_1\}}{g_1g_2g_3g_4} : g_{1_1} \cap g_{2_1} \cap g_{3_1} \cap g_{4_1} \quad \Rightarrow \quad d_{d_1}^1 = 4$$
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Algorithm-Step 1						
Input:						
Information System (IS);						
Oulpul:						
{Core Auribules};						
wiethou:						
1. Begin						
2. IS = (U, A);						
3. $x_i \in U; /*$ where x_1, x_2, \ldots, x_n are the of	bjects of set U */					
4. $a_1, a_2, \ldots, a_m \in A; /* \text{ where } a_1, a_2, \ldots,$	a_m are the elements of set $A * a_j \in A$; /* where					
a_1, a_2, \ldots, a_m are the elements of set A	*/					
5. For each a_m do;						
6. compute $R(a_j)$; /* where $R(a_j)$ are the s	similarity relation in IS as described in Definition 5 */					
7. generate D_a ; /* where D_a are the result	that compute the V_a as condition attributes in $R(a_j)$ as described in					
Definition 6 */						
8. Endfor;						
Output {Core Attributes};						
10. End;						
Algorithm-Step 2						
Input:						
Decision Table (DT);						
Output:						
{Classification Rules};						
Method:						
D = DT - (U, Q);						
DI = (U, Q),	biants of set II */					
$x_1 \in O, f \text{ where } x_1, x_2, \dots, x_n \text{ are the } O$						
$\mathcal{Q} = (0, \mathbf{D}),$	e the elements of set G^{*}					
$d_i \in D^{*} / * \text{ where } d_i = d_i = d_i = d_i$	the "core attributes" generated in Step 1 */					
7 For each $a_k \in D$, γ where a_1, a_2, \ldots, a_p are	the core autorices generated in step 1 7					
compute $R(q_t)$: /* where $R(q_t)$ are the s	similarity relation in DT as described in Definition $5 * /$					
9. compute $ind(G - g_i)$: /* compute the re	elative reduct of the elements for element <i>m</i> as described in					
Definition 6 */						
10. generate $ind(B)$: /* where $ind(B)$ are the	he indiscernibility relation of DT as described in Definition 6 */					
11. compute $G(X)$: /* where $G(X)$ are the	lower-approximation of DT as described in Definition 7 */					
12. compute $\overline{\overline{G}}(X)$; /* where $\overline{\overline{G}}(X)$ are the	upper-approximation of DT as described in Definition 7 */					
13. compute $Bn_G(X)$; /* where $Bn_G(X)$ are the bound of DT as described in Definition 7 */						
14. compute $Sup(ind(B))$; /* where $Sup(ind(B))$ are the core attribute support as described in Definition 8 */						
15. compute $Conf(ind(B) \rightarrow d_{g_i})$; /* wher	re $Conf(ind(B) \rightarrow d_{g_i})$ are the core confidence as described in					
Definition 8 */	• • • • • • • • • • • • • • • • • • •					
16. Endfor;						
17. Output {Classification Rules};						
18. End;						
Computational appariments	report groups of desigion makes Using traditional acception					
o Computational experiments	tiesent groups of decision-maker. Using traditional associa					
5.1 Ordinal scale data on consumer behavior	tion rules, it is only possible to see the relationship between					
	diapers and beer, but no deeper understanding of the infor					
rent a state of the	y motion is possible. Furthermore desision makers want to					

Intuitively, consumers who bought beer after buying dia-809 pers and those who bought diapers after buying beer, rep-810

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mation is possible. Furthermore, decision-makers want to 863 know the customer's product preferences, in order, for ex-864 « APIN 10489 layout: Large v.1.3.2 file: apin465.tex (Judita) class: spr-twocol-v1.4 v.2013/04/17 Prn:2013/07/19; 12:26 p. 9/15»
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A rough set-based association rule approach implemented on exploring beverages product spectrum

Attribute name	Attribute value	Attribute name set
Basic information		
Gender	Male; Female	{1,2}
Age	Below 18 years old; 18-25; 26-30; 31-35; 36-40; 41-45; above 51 years old	{1,2,3,4,5,6,7}
Income	Below NT\$5,000; BetweenNT\$5,001 and NT\$15,0000; Between NT\$15,001 and NT\$20,000; Between NT\$20,001 and NT\$25,000; Between NT\$25,001 and NT\$30,000; Between NT\$30,001 and NT\$35,000; Above NT\$35,001	{1,2,3,4,5,6,7}
Consumer behaviors		
Non-alcoholic beverages	Tea; Soda; Coffee; Juice; Sports; Packaged-waters; Energy; Others	{1,2,3,4,5,6,7,8}
Medium	Advertising; Seen on shelves; Internet; Magazine; Newspaper; Broadcasting; Billboard; Belongings	{1,2,3,4,5,6,7,8}
Channel	Hypermarkets; Supermarkets; Convenience Stores	{1,2,3}
Product Features	Price; Brand; Flavor; Quality	{1,2,3,4}
Consumer Behavior	Purchased due to promotions; Not purchased due to promotions	{1,2}

ample, the favorite brand, next favorite brands and overall brand ranking. It can be seen that the sequence of information for decision makers is very important. Therefore, the non-alcoholic beverages sold in the drink market are consolidated and then divided into eight items, which are listed in the questionnaire, for consumers to rank. The questionnaire is shown below:

(1) Tea (Oolong Tea, Red Tea, Green Tea, Fruit Tea...)

3 (2) Soda (Cola, soft drinks, ...)
4 (3) Cofee (Latte, Mocha, ...)

(4) Juice (Grape juice, Apple juice, ...)

(5) Sports (Shupao, Pocari, ...)

(6) Packaged-waters (Pure water, mineral water, Deep-sea water)

9 (7) Energy (Comebest, ...)

0 (8) Others (Milk, Rice Milk, Other vinegar, ...)

Please indicate your preferred product choices, in the following space:

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By means of this open-ended questionnaire, consumers rank each product category. In order to demonstrate the superiority of the proposed approach over traditional as-908 sociation rules, an empirical study was undertaken and 909 is described in this section. A questionnaire, with sin-910 gle and multiple-choice answers, was produced, to deter-911 mine customer behavior. The questionnaire comprised two 912 parts; the first to collect basic information and the second 913 to determine the consumer behaviors that are involved in 914 the decision process. The results provide the retailer with 915 useful information about the beverage product spectrum, 916 to allow the development of effective marketing strate-917 gies. 918

5.2 Construction of the information table for customer behavior in the retail market

The research sample comprised mainly members of the public who had purchased non-alcoholic beverage products in retail chain stores, within the last three months. One thousand questionnaires were distributed and 772 were returned, of which 172 were disqualified, as incomplete, or invalid. This left a total of 600 valid questionnaires, yielding a valid completion rate of 60 %. The domain values of the personal attributes for the primary survey are shown in Table 6. The profiles are shown in Table 7.

5.3 Results using reducts and core

According to Sai et al. [48], if an ordered information ta-954 ble has one or more reducts, then attributes that are not 955 part of any reduct are dispensable. These dispensable at-956 tributes can be removed from the data table, without af-957 fecting the ordering of the objects. Table 8 shows that 958 three non-alcoholic beverages are related (No 1). In other 959 words, when these three non-alcoholic beverage products 960 are combined, it is found that consumers prefer Tea, to 961 Juice, and like Juice more than others. The Strength is the 962 963 total number of consumers in the sample that make such 964 a choice. Using data processing algorithms, the eight non-965 alcoholic beverages can be classified according to the re-966 sults of Table 8. Marketing decision-makers can assign the 967 preferences of consumers to a promotion or the develop-968 ment of a new product. For example, the first class of 73 969 consumers ranked Tea as first, Juice as second and oth-970 ers as fourth. The second class of 65 consumers ranked 971 Tea as second, Juice as third and others as fifth. The first 972

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S.-H. Liao

74	Distribution	Distribution sample size	Frequency (%)
75	Gender		
76	Male	367	61.2
77	Female	233	38.8
8	Age		
9	Below 18 years old	21	3.5
0	18–25	237	39.5
1	26–30	174	29.0
2	31–35	78	13.0
3	36–40	29	4.8
4 -	41–45	43	7.2
5 6	Above 51 years old	18	3.0
7	Income		
8	Below NT\$5,000	127	21.2
9	Between NT\$5,001 and NT\$15,0000	90	15.0
0	Between NT\$15,001 and NT\$20,000	66	11.0
1	Between NT\$20,001 and NT\$25,000	61	10.2
2	Between NT\$25,001 and NT\$30,000	74	12.3
3	Between NT\$30,001 and NT\$35,000	81	13.5
4	Above NT\$35,001	101	16.8
5	Non-alcoholic beverages		
6	Теа	Ranking of non-alcoholic beverages	See the results
7	Soda		
8	Coffee		
9	Juice		
0	Sports	/	
1	Packaged-waters		
2	Energy		
3	Others		
4	Medium (multiple-choice answers)		
5	Advertising	489	81.5
6	Seen on shelves	105	17.5
/ 2	Internet; Magazine	47	7.8
8	Newspaper	30	5.0
9	Broadcasting	53	8.8
1	Billboard	122	20.3
י ס	Belongings	349	58.2
<u>د</u> ع	Channel (multiple choice anguare)		
4	Hypermarkets	202	33.7
,	Supermarkets	255	42.5
6	Convenience Stores	561	93 5
7	convenience stores	501	10.0
, 8	Product features (multiple-choice answer	3)	
9	Price	418	69.7
0	Brand	175	29.2
1	Flavor	367	61.2
2	Quality	183	30.5
- 3	Consumer behavior		
-	Purchased due to promotions	402	67.0
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A rough set-based association rule approach implemented on e	exploring	beverages	product spectrum
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Table 8 The significance of condition attributes/criteria	No.	ind(B)	fa	D_a	Strength (U/a)
	1	{Tea, Juice, Others}	$\{\{2,3,5\},\{1,2,4\},\{1,4,7\}\}$	D_a^+	{65,73,52}
	2	{Tea, Juice, Soda}	$\{\{1,2,3\},\{1,3,7\},\{2,3,6\}\}$	D_a^+	{73,64,52}
	3	{Tea, Juice, Others, Sports}	{{1,2,4,6},{2,3,5,7}}	D_a^+	{60,52}
	4	{Tea, Juice, Packaged, Energy}	$\{\{1,2,5,8\},\{2,3,4,8\},\{1,4,6,8\}\}$	D_a^+	{73,52,52}
	5	{Tea, Juice, Others, Energy}	$\{\{1,2,4,8\},\{2,3,5,8\},\{1,4,7,8\}\}$	D_a^+	{60,52,52}
	6	{Tea, Juice, Packaged, Sports}	{{1,2,5,6},{2,3,4,7}}	D_a^+	{60,52}
	÷	÷	:	÷	÷
			6		
Table 9 Possible rules for non-alcoholic beverages by rough set association rule	Condi	tion	Preference ranking Sup(ind() of non-alcoholic	3)) Co	$nf(ind(B) \to d_{g_j})$
	(Chan (Produ	nels = 3) & act Features = 1) & (Medium = 1)	${Tea = 1}$ 44.44 %	60.	.00 %

and second categories of consumers like the product category equally, but the preferences for non-alcoholic beverages are different, so marketing decision-makers can change the consumer behavior of the second class, so that the first and second categories of consumer behaviors are the same. This not only enhances the ordering of the product, but also increases the market share for Tea, juice and others.

In this case, the significance of the condition attributes/ criteria associated with dispensable attributes can be used to help retail decision-makers understand the spectrum of beverage products.

5.4 Rules using core criteria and personal attributes

A database always contains a lot of attributes that are redundant and not necessary for rule discovery. If these redundant attributes cannot be removed, the time complexity of the rule discovery process increases and the quality of the discovered rules may be much degraded. Decisions whether to delete attributes are very difficult for non-experts and even for experts. Clearly, it is necessary to develop methods for the selection of feature (attribute) subsets. An optimal feature subset should contain all of the indispensable features, because removing any of these features causes inconsistency, in a decision table. The discernibility matrix [5, 62, 64, 65] can be used for CORE searching. CORE searching searches such a subset of features, each of which uniquely discerns some instances. If CORE is not a reduct, some of the dispensable features must be selected and added to it, to make a reduct.

Using the reduced core criteria, shown in Table 8, a set
 of rule was established. These consider the personal profile
 attributes, including purchasing medium, channel, product
 features and consumer behavior.

The calculus of the research process generated by the rough set association rules, and the consumers ranked Tea as first as an example; the interesting target group is those customers who ranked Tea as first, and *B* is all ranked sets included tea. Thus, according to this calculation process produced 20 sets (all sets in the study are 45), therefore the rough associated support (Sup(ind(B))) is 44.44 %. Furthermore, the ranked sets included tea and ranked Tea as first are 12, therefore the rough associated confidence ($Conf(ind(B) \rightarrow d_{g_j})$) is 60 %. The rough set association rule for non-alcoholic beverages ranked Tea as first as an example is shown in Table 9.

In addition, calculated by use of the traditional association rules, thereby creating a rough association rules, under the conditions of the support is greater than 10 %, and confidence greater than 20 %, take the life is greater than 1, and the decision rules generated by the nonalcoholic beverage preferences are 201. A part of rules set of non-alcoholic beverage preferences, as shown in Table 10.

6 Conclusion

This study explores the association between sequences, for non-alcoholic beverages, according to the condition attributes set for non-alcoholic beverages, consumer products channel, advertising media sources, purchaser's consideration of product characteristics and consumer behavior, considered in conjunction with the purchase order. The core criteria of the non-alcoholic beverages product spectrum are shown in Fig. 1.

The study finds that most consumers buy non-alcoholic beverages because of the price and that advertising is the source of most product information. Before, or after the

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S.-H. Liao

1189 1190	Table 10Possible rules fornon-alcoholic beverages bytraditional association rule	No.	Condi	ion			Prefer of nor	ence ranking -alcoholic	Sup. (%)	Conf. (%)	Lift
1191 1192			(Chan	nels = Convenien	ce Stores)&	5	{Tea =	= 1}	23.00	52.17	1.06
193		1	(Produ	ct Features = Pri	ce)&		{Tea =	= 2}	23.00	31.16	1.10
194			(Medi	um = Broadcastir	g)		-				
195			(Chan	nels = Hypermark	æts)&		{Tea =	= 1 }	17.50	53.33	1.09
196		2	(Produ	ct Features = Pri	ce)&		-				
197			(Medi	um = Broadcastin	g)&						
198			(Const	umer Behavior =	Purchase by	y promotions	s)				
99			(Chan	nels = Hypermarl	tets)&	-	{Juice	= 2}	24.00	25.69	1.09
200		3	(Produ	ct Features = Pri	ce)&		{Juice	= 3	24.00	38.89	1.13
201			(Medi	um = Broadcastir	g)						
202			(Const	umer Behavior =	Purchase by	y promotions	s)& {Juice	= 3}	15.33	36.96	1.07
203		4	(Produ	ct Features = Co	venience S	stores)&					
204			(Produ	ct Features = Pri	ce)&		(
205			(Medi	um = Broadcastin	g)						
206			(Const	mer Behavior =	Purchase by	y promotions	s)& {Spor	ts = 6	40.17	31.95	1.14
207		5	(Produ	ct Features = Pri	ce)&		{Spor	ts = 7	40.17	26.14	1.05
208			(Medi	um = Broadcastin	g)						
209		6	(Produ	ct Features = Hy	permarkets	&	{Spor	ts = 6	24.00	31.94	1.14
210			(Produ	ct Features = Pri	ce)&		Y -				
211			(Medi	um = Broadcastin	g)						
212 013											
214	Fig. 1 The core criteria of the			Non-alcoholic be	verage produ	ict enectrum					
215	non-alcoholic beverages product	st	rong	Non-alcohone be	verage prout	iet speetrum		16 16		We	eak
216	spectrum	pro	oduct	Tea Juice	<u> </u>	Others		Sports		pro	duct
217		prefe	erences	Spectrum Spectrum	n	Spectrum		Spectrum		prefer	rences
218				1 2		4		6			
219		st	rong							we	eak
220		pro	oduct	Tea	Juice		Others	Sp	orts	pro	duct
21		prefe	erences		n Spectrum		Spectrum		trum	prefer	rences
222				2	3		5		7		
223		et									al
224		pro	oduct	Tea Juice			Packaged- waters	Sports	Ï	pro	duct
225		prefe	erences	Spectrum Spectrum	n		Spectrum	Spectrum		prefer	rences
226				1 2	-		5	6			
227		20.2									
		st	rong	Теа	Juice	Packaged-		l Sp	orts	We pro	eak duct
28		Pre	erences	L		Superiors 1	P <u></u> _	Sear		prefe	rences
228 229	1	prete		Canad				5000			
28 29 30	~	prete		Spectrur 2	a spectrum	4			7		
228 229 230 231		prete			3 3	4			7		
28 29 30 31 32		prete		Spectrur 2	3	4			7		
28 29 30 31 32 33	product ranking, consumers bu	y non	1-alcoł		in in in	4 order to av	 void both t	he retention	of only tr	rivial rules	that

product ranking, consumers buy non-alcoholic beverages in
 Hypermarkets and convenience stores, but those who buy
 non-alcoholic beverages in convenience stores are more sig nificantly affected by promotions. The integrated rules for
 the non-alcoholic beverages product spectrum are shown in
 Table 11.

Although rough set theory has found uses in a variety of
 areas, it is still not often applied in the study of customer
 behavior [41]. Traditional association rules should be fixed,

the discarding of interesting rules. In fact, the use of relative comparison, to express preferences, yields better results than absolute comparison. This paper presents a new method for the determination of association rules, which has the ability to handle uncertainty in the classification process and is suitable for ratio scale data. In contrast with other research this study's data processing included that of quantity attribute data and quality attribute data. In the second step, the gen-

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A rough set-based ass	sociation rule approac	h implemented	on exploring	beverages produ	ct spectrum
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for the non-alcoholic beverage	Product	Medium	Channel		Product features	Consumer behavior
products spectrum		Advertising	Hypermarkets	Convenience stores	Price	Purchased due to promotions
	Strong product sp	ectrum				
	Tea	V		V	V	
		V	V		V	V
	Juice	V	V		V	
		V		V	V	V
	Middle product sp	ectrum				
	Others	v		V	V	V
	Packaged waters	V	V		V	V
	-	V		V	v	V
	Weak product spec	ctrum				
	Sports	V			V	V
		V	V		V	
	:				:	
	•				•	

eration of rough association rules, the decision variable is generated from the core data of the first step, which provides a scientific method of addressing the problem. This study proposes a new data mining method, for ordinal scale data, which has the ability to handle uncertainty in the data classification/sorting process.

The products at the front end of the product spectrum were more popular with consumers; these products were favored by consumers, had large sales volumes and made good profits. The products at the back end of the product spectrum were less favored by consumers and had relatively lower sales volumes and profits. It is suggested that manufacturers could create marketing strategies that move their products toward the front end of the spectrum, in order to increase sales volumes and profits.

Finally, this study suggests that customer market segmentation allows a greater understanding of consumers' demands and preferences. In addition, the characteristics of the product spectrum can be used to determine whether brands are ideal, from the perspective of customers'. The product spectrum analysis diagram can be used to understand the product and to construct marketing strategies that allow greater penetration of the market.

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