

**Charge transport in underdoped bilayer cuprates**

Feng Yuan

*Department of Physics, Beijing Normal University, Beijing 100875, China  
and The Abdus Salam International Centre for Theoretical Physics, 34014 Trieste, Italy*

Jihong Qin and Shiping Feng

*Department of Physics and Key Laboratory of Beam Technology and Material Modification, Beijing Normal University,  
Beijing 100875, China;**Interdisciplinary Center of Theoretical Studies, Chinese Academy of Sciences, Beijing 100080, China;  
and National Laboratory of Superconductivity, Chinese Academy of Sciences, Beijing 100080, China*

Wei Yeu Chen

*Department of Physics, Tamkang University, Tamsui 25137, Taiwan*

(Received 13 November 2002; published 2 April 2003)

Within the  $t$ - $J$  model, we study the charge transport in underdoped bilayer cuprates by considering the bilayer interaction. Although the bilayer interaction leads to the band splitting in the electronic structure, the qualitative behavior of the charge transport is the same as in the case of single-layer cuprates. The conductivity spectrum shows a low-energy peak and the unusual midinfrared band. This midinfrared band is suppressed severely with increasing temperatures, while the resistivity in the heavily underdoped regime is characterized by a crossover from the high-temperature metalliclike to the low-temperature insulatinglike behaviors, which are consistent with the experiments.

DOI: 10.1103/PhysRevB.67.134504

PACS number(s): 74.72.-h, 74.20.Mn, 74.25.Fy

It has become clear in the past ten years that cuprate superconductors are among the most complex systems studied in condensed matter physics.<sup>1,2</sup> The complications arise mainly from (1) strong anisotropy in the properties parallel and perpendicular to the  $\text{CuO}_2$  planes which are the key structural element in the whole cuprate superconductors, and (2) extreme sensitivity of the properties to the compositions (stoichiometry) which control the carrier density in the  $\text{CuO}_2$  plane, and, therefore, the regimes have been classified into the underdoped, optimally doped, and overdoped, respectively.<sup>1,2</sup> In the underdoped and optimally doped regimes, the experimental results<sup>3</sup> show that the ratio of the  $c$  axis and in-plane resistivities  $R = \rho_c(T)/\rho_{ab}(T)$  ranges from  $R \sim 100$  to  $R > 10^5$ , which reflects that the charged carriers are tightly confined to the  $\text{CuO}_2$  planes. This large magnitude of the resistivity anisotropy also leads to the general notion that the physics of doped cuprates is almost entirely two dimensional, and can be well described by a single  $\text{CuO}_2$  plane.<sup>4</sup> However, this picture seems to be incompatible with the fact that the superconducting transition temperature  $T_c$  is closely related to the number of  $\text{CuO}_2$  planes per unit cell, with single-layer compounds of a family generically having lower  $T_c$  than bilayer or trilayer compounds.<sup>2</sup> Additionally, there are some subtle differences of the magnetic behaviors between doped single-layer and bilayer cuprates. By virtue of systematic studies using NMR and the muon spin rotation ( $\mu\text{SR}$ ) techniques, particularly, the inelastic neutron scattering, only incommensurate neutron-scattering peaks for the single-layer lanthanum cuprate are observed in the underdoped regime,<sup>5</sup> however, both low-energy incommensurate neutron-scattering peaks and high-energy commensurate  $[\pi, \pi]$  resonance for the bilayer yttrium cuprate in the normal state are detected.<sup>6</sup> These experimental results highlight

the importance of some sort of coupling between the  $\text{CuO}_2$  planes within a unit cell. It is believed that all these experiments produce interesting data that introduce the important constraints on the microscopic models and theories.

The charge transport of doped single-layer cuprates has been addressed from several theoretical viewpoints.<sup>7,8</sup> Based on the charge-spin separation, an attractive proposal is spinons and holons as basic low-energy excitations, serving as the starting point for the gauge-theory approach.<sup>7</sup> It has been shown<sup>7</sup> within the  $t$ - $J$  model that above the Bose-Einstein temperature, the boson inverse lifetime due to scattering by the gauge field is of order  $T$ , which suppresses the condensation temperature and leads to a linear  $T$  resistivity. On the other hand, the spin-fermion model near the antiferromagnetic instability has been developed to study the normal-state properties of doped cuprates.<sup>8</sup> This spin-fermion model describes low-energy fermions interacting with their own collective spin fluctuations. Within this approach,<sup>8</sup> the anomalous transport of doped single-layer cuprates has been studied extensively,<sup>8</sup> and the results are consistent with the experiments.

As regards an intracell hopping, the band splitting in doped bilayer cuprates was shown by the band calculation,<sup>9</sup> and clearly observed<sup>10,11</sup> recently by the angle-resolved photoemission spectroscopy in the doped bilayer cuprate  $\text{Bi}_2\text{Sr}_2\text{CaCu}_2\text{O}_{8+\delta}$  above  $T_c$ . This bilayer band splitting is due to a nonvanishing intracell coupling. Moreover, the magnitude of the bilayer splitting is constant over a large range of dopings.<sup>11</sup> Considering these highly unusual normal-state properties in the underdoped regime,<sup>1,2,5,6</sup> a natural question is what is the effect of the intracell coupling on the normal-state properties of doped bilayer cuprates. This is a challenge issue since the mechanism for the superconductivity in

doped cuprates has been widely recognized to be closely related with the anisotropic normal-state properties.<sup>12</sup> Based on the  $t$ - $J$  model, the charge transport and spin response of doped single-layer cuprates in the underdoped regime have been discussed<sup>13-15</sup> within the fermion-spin theory,<sup>16</sup> and the obtained results are consistent with experiments.<sup>17</sup> In this paper, we apply this successful approach to study the charge transport of the underdoped bilayer cuprates. Our results show that although the bilayer interaction leads to the band splitting in the electronic structure, the qualitative behavior of the conductivity and resistivity is the same as in the single-layer case. The conductivity shows the non-Drude behavior at low energies and anomalous midinfrared band separated by the charge-transfer gap, while the temperature-dependent resistivity in the heavily underdoped regime is characterized by a crossover from the high-temperature metalliclike to the low-temperature insulatinglike behaviors.

We start from the bilayer  $t$ - $J$  model, which can be written as

$$H = -t \sum_{ai\hat{\eta}\sigma} C_{ai\sigma}^\dagger C_{ai+\hat{\eta}\sigma} - t_\perp \sum_{i\sigma} (C_{1i\sigma}^\dagger C_{2i\sigma} + \text{H.c.}) - \mu \sum_{ai\sigma} C_{ai\sigma}^\dagger C_{ai\sigma} + J \sum_{ai\hat{\eta}} \mathbf{S}_{ai} \cdot \mathbf{S}_{ai+\hat{\eta}} + J_\perp \sum_i \mathbf{S}_{1i} \cdot \mathbf{S}_{2i}, \quad (1)$$

where  $\hat{\eta} = \pm \hat{x}, \pm \hat{y}$  within the plane,  $a=1$  and  $2$  is plane indices,  $C_{ai\sigma}^\dagger$  ( $C_{ai\sigma}$ ) is the electron creation (annihilation) operator,  $\mathbf{S}_{ai} = C_{ai\sigma}^\dagger \boldsymbol{\sigma} C_{ai\sigma} / 2$  are spin operators with  $\boldsymbol{\sigma} = (\sigma_x, \sigma_y, \sigma_z)$  as Pauli matrices, and  $\mu$  is the chemical potential. The bilayer  $t$ - $J$  model (1) is defined in the subspace with no doubly occupied sites, i.e.,  $\sum_\sigma C_{ai\sigma}^\dagger C_{ai\sigma} \leq 1$ . The strong electron correlation in the  $t$ - $J$  model manifests itself by this single occupancy on-site local constraint.<sup>4</sup> To deal with the local constraint in analytical calculations, the fermion-spin theory,<sup>16</sup>  $C_{ai\uparrow} = h_{ai}^\dagger S_{ai}^-$  and  $C_{ai\downarrow} = h_{ai}^\dagger S_{ai}^+$ , has been proposed, where the spinless fermion operator  $h_{ai}$  keeps track of the charge (holon), while the pseudospin operator  $S_{ai}$  keeps track of the spin (spinon), then it naturally incorporates the physics of the charge-spin separation. In this case, the low-energy behavior of the bilayer  $t$ - $J$  model (1) in the fermion-spin representation can be rewritten as

$$H = t \sum_{ai\hat{\eta}} h_{ai+\hat{\eta}}^\dagger h_{ai} (S_{ai}^+ S_{ai+\hat{\eta}}^- + S_{ai}^- S_{ai+\hat{\eta}}^+) + t_\perp \sum_i (h_{1i}^\dagger h_{2i} + h_{2i}^\dagger h_{1i}) (S_{1i}^+ S_{2i}^- + S_{1i}^- S_{2i}^+) + \mu \sum_{ai} h_{ai}^\dagger h_{ai} + J_{\text{eff}} \sum_{ai\hat{\eta}} \mathbf{S}_{ai} \cdot \mathbf{S}_{ai+\hat{\eta}} + J_{\perp\text{eff}} \sum_i \mathbf{S}_{1i} \cdot \mathbf{S}_{2i}, \quad (2)$$

with  $J_{\text{eff}} = J[(1-\delta)^2 - \phi^2]$ ,  $J_{\perp\text{eff}} = J_\perp[(1-\delta)^2 - \phi_\perp^2]$ , the holon particle-hole order parameters  $\phi = \langle h_{ai}^\dagger h_{ai+\hat{\eta}} \rangle$  and  $\phi_\perp = \langle h_{1i}^\dagger h_{2i} \rangle$ ,  $\delta$  is the hole doping concentration, and  $S_{ai}^\pm$  ( $S_{ai}^\mp$ ) is the pseudospin raising (lowering) operator. Since the

single occupancy local constraint has been treated properly within the fermion-spin theory, this leads to disappearing of the extra gauge degree of freedom related with this local constraint under the charge-spin separation.<sup>16</sup> In this case, the charge fluctuation couples only to holons.<sup>13,14</sup> However, the strong correlation between holons and spinons is still included self-consistently through the spinon's order parameters entering the holon's propagator, therefore, both holons and spinons are responsible for the charge transport. In this case, the conductivity can be expressed as  $\sigma(\omega) = -\text{Im} \Pi^{(h)}(\omega)/\omega$ , with  $\Pi^{(h)}(\omega)$  is the holon current-current correlation function, and is defined as  $\Pi^{(h)}(\tau - \tau') = -\langle T_\tau j^{(h)}(\tau) j^{(h)}(\tau') \rangle$ , where  $\tau$  and  $\tau'$  are the imaginary times, and  $T_\tau$  is the  $\tau$  order operator. Within the Hamiltonian (2), the current density of holons is obtained by the time derivation of the polarization operator using Heisenberg's equation of motion as

$$j^{(h)} = 2\chi e t \sum_{ai\hat{\eta}} \hat{\eta} h_{ai+\hat{\eta}}^\dagger h_{ai} + 2\chi_\perp e t_\perp \sum_i (R_{2i} - R_{1i}) \times (h_{2i}^\dagger h_{1i} - h_{1i}^\dagger h_{2i}), \quad (3)$$

where  $R_{1i}$  ( $R_{2i}$ ) is lattice site of the  $\text{CuO}_2$  plane 1 (plane 2),  $\chi = \langle S_{ai}^+ S_{ai+\hat{\eta}}^- \rangle$  and  $\chi_\perp = \langle S_{1i}^+ S_{2i}^- \rangle$  are the spinon correlation functions, and  $e$  is the electronic charge, which is set as the unit hereafter. The holon current-current correlation function can be calculated in terms of the holon Green's function  $g(k, \omega)$  as in the single-layer case.<sup>13,14</sup> However, in the bilayer system, because there are two coupled  $\text{CuO}_2$  planes, then the energy spectrum has two branches. In this case, the one-particle holon Green's function can be expressed as a matrix  $g(i-j, \tau - \tau') = g_L(i-j, \tau - \tau') + \sigma_x g_T(i-j, \tau - \tau')$  with the longitudinal and transverse parts are defined as  $g_L(i-j, \tau - \tau') = -\langle T_\tau h_{ai}(\tau) h_{aj}^\dagger(\tau') \rangle$  and  $g_T(i-j, \tau - \tau') = -\langle T_\tau h_{ai}(\tau) h_{a'j}^\dagger(\tau') \rangle$  ( $a \neq a'$ ), respectively. Following discussions of the single-layer case,<sup>13,14</sup> we obtain the conductivity of doped bilayer cuprates as  $\sigma(\omega) = \sigma^{(L)}(\omega) + \sigma^{(T)}(\omega)$  with the longitudinal and transverse parts are given by

$$\sigma^{(L)}(\omega) = \frac{1}{N} \sum_k [(2Z\chi t \gamma_{sk})^2 + (2\chi_\perp t_\perp)^2] \times \int_{-\infty}^{\infty} \frac{d\omega'}{2\pi} A_L^{(h)}(k, \omega' + \omega) A_L^{(h)}(k, \omega') \times \frac{n_F(\omega' + \omega) - n_F(\omega')}{\omega}, \quad (4a)$$

$$\sigma^{(T)}(\omega) = \frac{1}{N} \sum_k [(2Z\chi t \gamma_{sk})^2 - (2\chi_\perp t_\perp)^2] \times \int_{-\infty}^{\infty} \frac{d\omega'}{2\pi} A_T^{(h)}(k, \omega' + \omega) A_T^{(h)}(k, \omega') \times \frac{n_F(\omega' + \omega) - n_F(\omega')}{\omega}, \quad (4b)$$

respectively, where  $Z$  is the coordination number within the plane,  $\gamma_{sk} = (\sin k_x + \sin k_y)/2$ , and  $n_F(\omega)$  is the fermion distribution function. The longitudinal and transverse holon spectral functions are obtained as  $A_L^{(h)}(k, \omega) = -2 \text{Im} g_L(k, \omega)$  and  $A_T^{(h)}(k, \omega) = -2 \text{Im} g_T(k, \omega)$ , respectively. The full holon Green's function  $g^{-1}(k, \omega) = g^{(0)-1}(k, \omega) - \Sigma^{(h)}(k, \omega)$  with the longitudinal and transverse mean-field (MF) holon Green's functions  $g_L^{(0)}(k, \omega) = 1/2 \sum_{\nu} 1/(\omega - \xi_k^{(\nu)})$  and  $g_T^{(0)}(k, \omega) = 1/2 \sum_{\nu} (-1)^{\nu+1}/(\omega - \xi_k^{(\nu)})$ , where  $\nu = 1, 2$ , and the longitudinal and transverse second-order holon self-energy from the spinon pair bubble are obtained by the loop expansion to the second-order as

$$\Sigma_L(k, \omega) = \frac{1}{N^2} \sum_{pq} \sum_{\nu\nu'} \Xi_{\nu\nu'}(k, p, q, \omega), \quad (5a)$$

$$\Sigma_T(k, \omega) = \frac{1}{N^2} \sum_{pq} \sum_{\nu\nu'} (-1)^{\nu+\nu'+\nu''+1} \Xi_{\nu\nu'}(k, p, q, \omega), \quad (5b)$$

respectively, with  $\Xi_{\nu\nu'}(k, p, q, \omega)$  is given by

$$\begin{aligned} \Xi_{\nu\nu'}(k, p, q, \omega) &= \frac{B_{q+p}^{(\nu')} B_q^{(\nu)}}{32 \omega_{q+p}^{(\nu')} \omega_q^{(\nu)}} \{ Z t [\gamma_{q+p+k} + \gamma_{q-k}] \\ &\quad + t_{\perp} [(-1)^{\nu+\nu''} + (-1)^{\nu'+\nu''}] \}^2 \\ &\quad \times \left( \frac{F_{\nu\nu'}^{(1)}(k, p, q)}{\omega + \omega_{q+p}^{(\nu')} - \omega_q^{(\nu)} - \xi_{p+k}^{(\nu')}} \right. \\ &\quad + \frac{F_{\nu\nu'}^{(2)}(k, p, q)}{\omega - \omega_{q+p}^{(\nu')} + \omega_q^{(\nu)} - \xi_{p+k}^{(\nu')}} \\ &\quad + \frac{F_{\nu\nu'}^{(3)}(k, p, q)}{\omega + \omega_{q+p}^{(\nu')} + \omega_q^{(\nu)} - \xi_{p+k}^{(\nu')}} \\ &\quad \left. + \frac{F_{\nu\nu'}^{(4)}(k, p, q)}{\omega - \omega_{q+p}^{(\nu')} - \omega_q^{(\nu)} - \xi_{p+k}^{(\nu')}} \right) \quad (6) \end{aligned}$$

with  $\gamma_k = (\cos k_x + \cos k_y)/2$ ,  $B_k^{(\nu)} = B_k - J_{\perp \text{eff}} [\chi_{\perp} + 2\chi_{\perp}^z (-1)^{\nu}] [\epsilon_{\perp} + (-1)^{\nu}]$ ,  $B_k = \lambda [(2\epsilon\chi^z + \chi)\gamma_k - (\epsilon\chi + 2\chi^z)]$ ,  $\lambda = 2ZJ_{\text{eff}}$ ,  $\epsilon = 1 + 2t\phi/J_{\text{eff}}$ ,  $\epsilon_{\perp} = 1 + 4t_{\perp}\phi_{\perp}/J_{\perp \text{eff}}$ , and

$$F_{\nu\nu'}^{(1)}(k, p, q) = n_F(\xi_{p+k}^{(\nu'')}) [n_B(\omega_q^{(\nu)}) - n_B(\omega_{q+p}^{(\nu')})] + n_B(\omega_{q+p}^{(\nu')}) [1 + n_B(\omega_q^{(\nu)})],$$

$$F_{\nu\nu'}^{(2)}(k, p, q) = n_F(\xi_{p+k}^{(\nu'')}) [n_B(\omega_{q+p}^{(\nu')}) - n_B(\omega_q^{(\nu)})] + n_B(\omega_q^{(\nu)}) [1 + n_B(\omega_{q+p}^{(\nu')})],$$

$$F_{\nu\nu'}^{(3)}(k, p, q) = n_F(\xi_{p+k}^{(\nu'')}) [1 + n_B(\omega_{q+p}^{(\nu')}) + n_B(\omega_q^{(\nu)})] + n_B(\omega_q^{(\nu)}) n_B(\omega_{q+p}^{(\nu')}),$$

$$F_{\nu\nu'}^{(4)}(k, p, q) = [1 + n_B(\omega_q^{(\nu)})] [1 + n_B(\omega_{q+p}^{(\nu')})] - n_F(\xi_{p+k}^{(\nu'')}) \times [1 + n_B(\omega_{q+p}^{(\nu')}) + n_B(\omega_q^{(\nu)})], \quad (7)$$

Here  $n_B(\omega_k^{(\nu)})$  is the boson distribution function, the MF holon excitation  $\xi_k^{(\nu)} = 2Z\chi t \gamma_k + \mu + 2\chi_{\perp} t_{\perp} (-1)^{\nu+1}$ , the MF spinon excitation  $(\omega_k^{(\nu)})^2 = \omega_k^2 + \Delta_k^2 (-1)^{\nu+1}$  with  $\omega_k^2 = A_1 \gamma_k^2 + A_2 \gamma_k + A_3$  and  $\Delta_k^2 = X_1 \gamma_k + X_2$  where

$$A_1 = \alpha \epsilon \lambda^2 (\chi/2 + \epsilon \chi^z),$$

$$A_2 = \epsilon \lambda^2 [(1-Z)\alpha(\epsilon\chi/2 + \chi^z)/Z - \alpha(C^z + C/2) - (1-\alpha)/(2Z)] - \alpha \lambda J_{\perp \text{eff}} [\epsilon(C_{\perp}^z + \chi_{\perp}^z) + \epsilon_{\perp}(C_{\perp} + \epsilon\chi_{\perp})/2],$$

$$A_3 = \lambda^2 [\alpha(C^z + \epsilon^2 C/2) + (1-\alpha)(1+\epsilon^2)/(4Z) - \alpha\epsilon(\chi/2 + \epsilon\chi^z)/Z] + \alpha \lambda J_{\perp \text{eff}} [\epsilon\epsilon_{\perp} C_{\perp} + 2C_{\perp}^z] + J_{\perp \text{eff}}^2 (\epsilon_{\perp}^2 + 1)/4,$$

$$X_1 = \alpha \lambda J_{\perp \text{eff}} [(\epsilon_{\perp} \chi + \epsilon\chi_{\perp})/2 + \epsilon\epsilon_{\perp} (\chi_{\perp}^z + \chi^z)],$$

$$X_2 = -\alpha \lambda J_{\perp \text{eff}} [\epsilon\epsilon_{\perp} \chi/2 + \epsilon_{\perp} (\chi^z + C_{\perp}^z) + \epsilon C_{\perp}/2] - \epsilon_{\perp} J_{\perp \text{eff}}^2/2, \quad (8)$$

where the spinon correlation functions  $\chi^z = \langle S_{ai}^z S_{ai+\hat{\eta}}^z \rangle$ ,  $\chi_{\perp}^z = \langle S_{1i}^z S_{2i}^z \rangle$ ,  $C = (1/Z^2) \sum_{\hat{\eta}\hat{\eta}'} \langle S_{ai+\hat{\eta}}^+ S_{ai+\hat{\eta}'}^- \rangle$ ,  $C^z = (1/Z^2) \sum_{\hat{\eta}\hat{\eta}'} \langle S_{ai+\hat{\eta}}^z S_{ai+\hat{\eta}'}^z \rangle$ ,  $C_{\perp} = (1/Z) \sum_{\hat{\eta}} \langle S_{2i}^+ S_{1i+\hat{\eta}}^- \rangle$ , and  $C_{\perp}^z = (1/Z) \sum_{\hat{\eta}} \langle S_{1i}^z S_{2i+\hat{\eta}}^z \rangle$ . In order to satisfy the sum rule for the correlation function  $\langle S_{ai}^+ S_{ai}^- \rangle = 1/2$  in the absence of the antiferromagnetic long-range order, a decoupling parameter  $\alpha$  has been introduced in the MF calculation, which can be regarded as the vertex correction.<sup>18</sup> All these order parameters, decoupling parameter  $\alpha$ , and the chemical potential  $\mu$  have been determined self-consistently, as done in the single-layer case.<sup>18</sup>

The frequency- and temperature-dependent conductivity is a powerful probe for systems of interacting electrons, and provides very detailed informations of the excitations, which interacts with carriers in the normal state and might play an important role in the superconductivity. In Fig. 1, we present the results of the conductivity  $\sigma(\omega)$  at doping  $\delta = 0.05$  (solid line),  $\delta = 0.06$  (dashed line), and  $\delta = 0.07$  (dotted line) for parameters  $t/J = 2.5$ ,  $t_{\perp}/t = 0.25$  and  $J_{\perp}/J = 0.25$  with temperature  $T = 0$  in comparison with the experimental data<sup>19</sup> taken on the underdoped  $\text{YBa}_2\text{Cu}_3\text{O}_{7-x}$  (YBCO) (inset). The conductivity of bilayer cuprates in the underdoped regime shows a sharp low-energy peak at  $\omega < 0.5t$  and the unusual midinfrared band appearing inside the charge-transfer gap of the undoped system. After an analysis, we found that this low-energy peak decays fastly as  $\sigma(\omega) \sim 1/\omega$  (non-Drude fall-off) with increasing energies. Moreover, the weight of the midinfrared peak is doping dependent, and the peak position is shifted to low energy with increasing dopings. For a

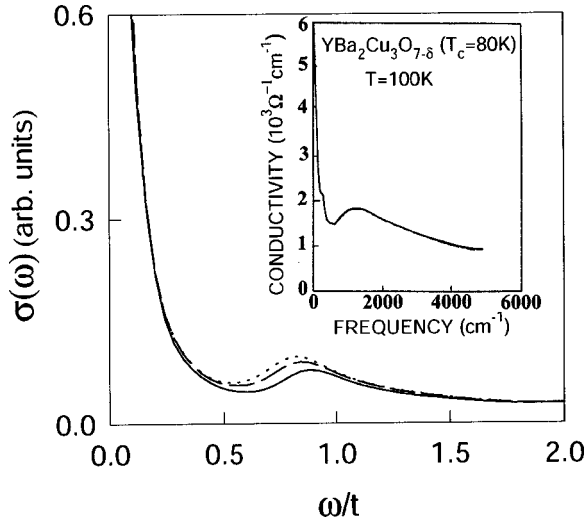


FIG. 1. The conductivity at  $\delta=0.05$  (solid line),  $\delta=0.06$  (dashed line), and  $\delta=0.07$  (dotted line) for  $t/J=2.5$ ,  $t_{\perp}/t=0.25$ , and  $J_{\perp}/J=0.25$  in the zero temperature. Inset: the experimental result on the underdoped  $\text{YBa}_2\text{Cu}_3\text{O}_{7-x}$  taken from Ref. 19.

better understanding of the optical properties of doped bilayer cuprates, we have studied conductivity at different temperatures, and the results at doping  $\delta=0.06$  for  $t/J=2.5$ ,  $t_{\perp}/t=0.25$ , and  $J_{\perp}/J=0.25$  in  $T=0$  (solid line),  $T=0.3J$  (dashed line), and  $T=0.5J$  (dotted line) are plotted in Fig. 2 in comparison with the experimental data<sup>19</sup> taken on the underdoped YBCO (inset). It is shown that  $\sigma(\omega)$  is temperature dependent, and the charge-transfer gap is severely suppressed with increasing temperatures, and vanishes at higher temperature ( $T>0.4J$ ). Our results are in qualitative agreement with the experiments.<sup>19</sup> In comparison with the results from Refs. 13,14, it is shown that the present conductivity also is qualitatively consistent with these in the single-layer case. In the above calculations, we also find that the conduc-

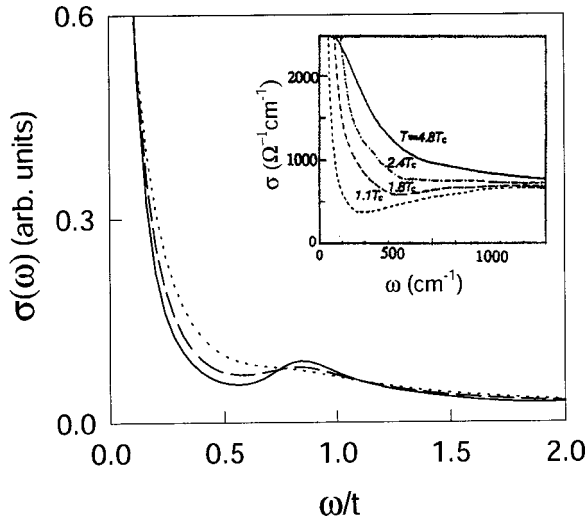


FIG. 2. The conductivity at  $\delta=0.06$  for  $t/J=2.5$ ,  $t_{\perp}/t=0.25$ , and  $J_{\perp}/J=0.25$  in  $T=0$  (solid line),  $T=0.3J$  (dashed line), and  $T=0.5J$  (dotted line). Inset: the experimental result on the underdoped  $\text{YBa}_2\text{Cu}_3\text{O}_{7-x}$  taken from Ref. 19.

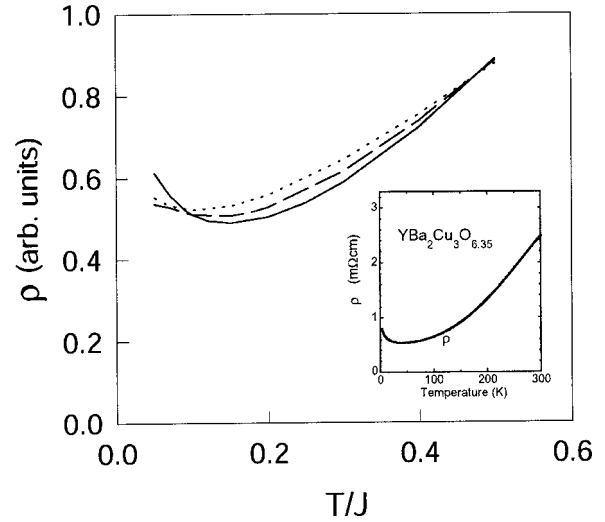


FIG. 3. The resistivity at  $\delta=0.05$  (solid line),  $\delta=0.06$  (dashed line), and  $\delta=0.07$  (dotted line) for  $t/J=2.5$ ,  $t_{\perp}/t=0.25$ , and  $J_{\perp}/J=0.25$ . Inset: the experimental result on the underdoped  $\text{YBa}_2\text{Cu}_3\text{O}_{7-x}$  taken from Ref. 20.

tivity  $\sigma(\omega)$  is essentially determined by its longitudinal part  $\sigma^{(L)}(\omega)$ , this is why in the present doped bilayer cuprates the conductivity spectrum appears to reflect the single-layer nature of the electronic state.<sup>1,2,13,14</sup> This is also why the in-plane charge dynamics is rather universal within whole doped cuprates.<sup>1,2</sup>

Now we turn to discuss the resistivity, which is closely related to the conductivity, and can be obtained as  $\rho(T) = 1/\lim_{\omega \rightarrow 0} \sigma(\omega)$ . This resistivity has been calculated, and the results at doping  $\delta=0.05$  (solid line),  $\delta=0.06$  (dashed line), and  $\delta=0.07$  (dotted line) for parameter  $t/J=2.5$ ,  $t_{\perp}/t=0.25$ , and  $J_{\perp}/J=0.25$  are plotted in Fig. 3 in comparison with the experimental results<sup>20</sup> taken on the underdoped YBCO (inset). These results show that in the heavily underdoped regime, although the temperature-dependent resistivity is characterized by a crossover from the high-temperature metalliclike to the low-temperature insulatinglike behaviors, the nearly temperature linear dependence in the resistivity dominates over a wide temperature range, in agreement with the experimental results.<sup>20</sup> In comparison with the results from Refs. 13,14, it is shown that the present resistivity also is qualitatively consistent with these in the single-layer case. We emphasize that since the order parameters, decoupling parameter  $\alpha$ , and the chemical potential  $\mu$  have been determined self-consistently, then these theoretical results were obtained without any adjustable parameters. Furthermore, it is found in the above discussions that the present results are insensitive to the reasonable values of  $t/J$ ,  $t_{\perp}/t$ , and  $J_{\perp}/J$  as in the single-layer case.<sup>13,14</sup>

An explanation for the metal-to-insulating crossover in the resistivity in the heavily underdoped regime can be found from the competition between the kinetic energy and magnetic energy in the system. Since cuprate superconducting materials are doped Mott insulators, obtained by chemically adding charge carriers to a strongly correlated antiferromagnetic insulating state, therefore, doped cuprates are charac-

terized by the competition between the kinetic energy  $t$  and magnetic energy  $J$ . The magnetic energy  $J$  favors the magnetic order for spins, while the kinetic energy  $t$  favors delocalization of holes and tends to destroy the magnetic order. In the present fermion-spin theory, although both holons and spinons contribute to the charge transport, the scattering of holons dominates the charge transport,<sup>13</sup> where the charged holon scattering rate is obtained from the full holon Green's function [then the holon self-energy, Eqs. 5(a) and 5(b), and holon spectral function] by considering the holon-spinon interaction, therefore, in the heavily underdoped regime, the observed crossover from the high-temperature metalliclike to the low-temperature insulatinglike behaviors in the resistivity is closely related with this competition. At lower temperatures, the holon kinetic energy is much smaller than the magnetic energy, in this case the magnetic fluctuation is strong enough to severely reduce the charged holon scattering and thus is responsible for the insulatinglike behavior in the resistivity. With increasing temperatures, the holon kinetic energy is increased, while the spinon magnetic energy is decreased. In the region, where the holon kinetic energy is much larger than the spinon magnetic energy at higher tem-

peratures, the charged holon scattering would give rise to the temperature linear resistivity.

In summary, we have studied the charge transport in the underdoped bilayer cuprates by considering the bilayer interaction. It is shown that although the bilayer interaction leads to the band splitting in the electronic structure, the qualitative behavior of the charge transport is the same as in the single-layer case. The conductivity spectrum shows a low-energy peak and the anomalous midinfrared band. This midinfrared band is suppressed severely with increasing temperatures, while the resistivity exhibits a crossover from the high-temperature metalliclike to the low-temperature insulatinglike behaviors. Our results also show that the mechanism that cause this unusual charge transport in the underdoped cuprates is closely related to the background antiferromagnetic correlations.

This work was supported by the National Natural Science Foundation of China under Grant Nos. 10074007, 10125415, and 90103024, the special funds from the Ministry of Science and Technology of China, and the National Science Council under Grant No. NSC 90-2816-M-032-0001-6.

- 
- <sup>1</sup>See, e.g., *Physical Properties of High Temperature Superconductors*, edited by D. M. Ginsberg (World Scientific, Singapore, 1994).
- <sup>2</sup>See, e.g., *Proceedings of Los Alamos Symposium*, edited by K. S. Bedell, D. Coffey, D. E. Meltzer, D. Pines, and J. R. Schrieffer (Addison-Wesley, California, 1990).
- <sup>3</sup>T. Ito, K. Takenaka, and S. Uchida, *Phys. Rev. Lett.* **70**, 3995 (1993); S. Uchida, *Physica C* **282-287**, 12 (1997).
- <sup>4</sup>P. W. Anderson, in *Frontiers and Borderlines in Many Particle Physics*, edited by R. A. Broglia and J. R. Schrieffer (North-Holland, Amsterdam, 1987), p. 1; P.W. Anderson, *Science* **235**, 1196 (1987).
- <sup>5</sup>K. Yamada, C.H. Lee, K. Kurahashi, J. Wada, S. Wakimoto, S. Ueki, H. Kimura, Y. Endoh, S. Hosoya, and G. Shirane, *Phys. Rev. B* **57**, 6165 (1998), and references therein.
- <sup>6</sup>P. Dai, H.A. Mook, R.D. Hunt, and F. Doğan, *Phys. Rev. B* **63**, 054525 (2001), and references therein.
- <sup>7</sup>N. Nagaosa and P.A. Lee, *Phys. Rev. Lett.* **64**, 2450 (1990); P.A. Lee and N. Nagaosa, *Phys. Rev. B* **46**, 5621 (1990).
- <sup>8</sup>A. Abanov, A.V. Chubukov, and J. Schmalian, cond-mat/0107421 (unpublished); A. Abanov and A.V. Chubukov, *Phys. Rev. Lett.* **88**, 217001 (2002); A. Abanov, A.V. Chubukov, and J. Schmalian, *Phys. Rev. B* **63**, 180510 (2001); R. Haslinger, A.V. Chubukov, and A. Abanov, *ibid.* **63**, 020503 (2001).
- <sup>9</sup>O.K. Anderson, A.I. Liechtenstein, O. Jepsen, and F. Paulsen, *J. Phys. Chem. Solids Suppl.* **56**, 1573 (1995); A.I. Liechtenstein, O. Gunnarsson, O.K. Anderson, and R.M. Martin, *Phys. Rev. B* **54**, 12 505 (1996).
- <sup>10</sup>D.L. Feng, N.P. Armitage, D.H. Lu, A. Damascelli, J.P. Hu, P. Bogdanov, A. Lanzara, F. Ronning, K.M. Shen, H. Eisaki, C. Kim, Z.X. Shen, J.-i. Shimoyama, and K. Kishio, *Phys. Rev. Lett.* **86**, 5550 (2001).
- <sup>11</sup>Y.-D. Chuang, A.D. Gromko, A.V. Fedorov, Y. Aiura, K. Oka, Yoichi Ando, and D. Dessau, cond-mat/0107002 (unpublished); Y.-D. Chuang, A.D. Gromko, A.V. Fedorov, Y. Aiura, K. Oka, Yoichi Ando, H. Eisaki, S.I. Uchida, and D. Dessau, *Phys. Rev. Lett.* **87**, 117002 (2001).
- <sup>12</sup>See, e.g., P. W. Anderson, *The Theory of Superconductivity in the High- $T_c$  Cuprates* (Princeton, New Jersey, 1997).
- <sup>13</sup>Shiping Feng and Zhongbing Huang, *Phys. Lett. A* **232**, 293 (1997).
- <sup>14</sup>Feng Yuan and Shiping Feng, *Phys. Lett. A* **297**, 235 (2002).
- <sup>15</sup>Feng Yuan, Shiping Feng, Zhao-Bin Su, and Lu Yu, *Phys. Rev. B* **64**, 224505 (2001); Shiping Feng and Zhongbing Huang, *ibid.* **57**, 10 328 (1998).
- <sup>16</sup>Shiping Feng, Z.B. Su, and L. Yu, *Phys. Rev. B* **49**, 2368 (1994); *Mod. Phys. Lett. B* **7**, 1013 (1993).
- <sup>17</sup>M.A. Kastner, R.J. Birgeneau, G. Shiran, and Y. Endoh, *Rev. Mod. Phys.* **70**, 897 (1998).
- <sup>18</sup>J. Kondo and K. Yamaji, *Prog. Theor. Phys.* **47**, 807 (1972); Shiping Feng and Yun Song, *Phys. Rev. B* **55**, 642 (1997).
- <sup>19</sup>J. Orenstein, G.A. Thomas, A.J. Millis, S.L. Cooper, D.H. Rapkine, T. Timusk, L.F. Schneemeger, and J.V. Waszczak, *Phys. Rev. B* **42**, 6342 (1990).
- <sup>20</sup>Y. Ando, K. Segawa, S. Komiya, and A.N. Lavrov, *Phys. Rev. Lett.* **88**, 137005 (2002).