Towards Low-Complexity Wireless Technology Classification Across Multiple Environments

Jaron Fontaine¹, Erika Fonseca², Adnan Shahid¹, Maicon Kist², Luiz A. DaSilva², Ingrid Moerman¹, Eli De Poorter¹

Abstract

To cope with the increasing number of co-existing wireless standards, complex machine learning techniques have been proposed for wireless technology classification. However, machine learning techniques in the scientific literature suffer from some shortcomings, namely: (i) they are often trained using data from only a single measurement location, and as such the results do not necessarily generalise and (ii) they typically do not evaluate complexity/accuracy trade-offs of the proposed solutions.

To remedy these shortcomings, this paper investigates which resourcefriendly approaches are suitable across multiple heterogeneous environments. To this end, the paper designs and evaluates classifiers for LTE, Wi-Fi and DVB-T technologies using multiple datasets to investigate the complexity/accuracy trade-offs between manual feature extraction and automatic feature learning techniques.

Our wireless technology classification reaches an accuracy up to 99%.

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¹J. Fontaine (corresponding author, SB PhD fellow at FWO), A. Shahid, E. De Poorter and I. Moerman with the IDLab, Department of Information Technology, Ghent University - imec, iGent Tower, Technologiepark-Zwijnaarde 15, B-9052 Ghent, Belgium. (email: Jaron.Fontaine@Ugent.be)

²E. Fonseca, M. Kist and L. A. DaSilva are with the CONNECT Research Centre for Future Networks and Communications, Trinity College Dublin, 2 Dublin, Ireland.

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Moreover, we propose the use of data augmentation techniques to extend these results to unseen environments at the cost of only 2% reduction in accuracy. When concerning generalisation capabilities, complex automatic learning techniques surpass simple manual feature extraction approaches. Finally, the complexity of these automatic learning techniques can be significantly reduced by using computationally less intensive received signal strength indicator data while reaching acceptable accuracies in unseen environments (92% vs 97%).

Keywords: manual feature extraction, automatic feature learning, wireless technology classification, machine learning, CNN

1 1. Introduction

With the advent of multimedia-enriched mobile phone applications, traffic demand from wireless users is increasing substantially. Furthermore, the number of wireless Internet of Things (IoT) devices is growing at an unprecedented rate: it is predicted that by 2020 there will be around 20 billion wireless devices around the globe [1].

In this context, machine learning, which offers the ability to learn without
being explicitly programmed, shows enormous potential to better manage
the limited resources of a wireless network and enable the delivery of a new
generation of services.

Due to limited licensed bands and the growing traffic demands, the mo-11 bile communication industry is striving for offloading traffic from licensed to 12 unlicensed bands. In Releases 13 and 14 of Long Term Evolution (LTE), the 13 3rd Generation Partnership Project (3GPP) has proposed Licensed-Assisted 14 Access (LAA), in which LTE can operate on both licensed and unlicensed 15 bands via carrier aggregation [2]. This approach, however, raises questions 16 on its effect on the performance of legacy IEEE 802.11 (Wi-Fi) [3]. In such 17 a co-existence environment, it is necessary to make intelligent decisions for 18 maintaining the Quality of Service (QoS) requirements of both technologies. 19 On the other hand, it is predicted that the 5th generation (5G) network 20 will provide 1000 times the capacity as compared to the current system [4]. 21 Offloading licensed traffic to unlicensed bands is beneficial, nevertheless it 22 cannot solely fulfill the extensive capacity requirement. In this regard, an ef-23 ficient sharing of licensed bands is a promising solution [5]. Various standard-24 ization bodies, European Telecommunications Standards Institute (ETSI) 25

and the 3GPP are currently focusing on various licensed spectrum sharing
models such as to apply cognitive radio techniques by radio environment
maps (REM)s [6] and radio access network (RAN) sharing [7], respectively.

A first step towards achieving this objective is for wireless systems to be 29 able to identify what other wireless technologies are present in the same band 30 and what their characteristics of operation are. In this paper, we design and 31 analyse machine learning techniques for technology classification in shared 32 spectrum. In our evaluation of those techniques, we consider three tech-33 nologies: Wi-Fi, LTE and Digital Video Broadcasting Terrestrial (DVB-T). 34 These technologies are likely to operate in shared spectrum in the near fu-35 ture. Due to the 3GPP LAA proposals, LTE and Wi-Fi will operate and 36 compete with each other in unlicensed bands [2]. Moreover, the reuse factor 37 used in licensed DVB-T systems leads to significant amounts of unused spec-38 trum at a given location [8, 9, 10]. In order to efficiently utilise the licensed 30 spectrum, secondary users can use it without creating any harmful impact on 40 the primary network. This spectrum sharing model was used by the Federal 41 Communications Commission (FCC) for television bands and is termed as 42 white space reuse [10]. 43

To operate in shared spectrum, it is crucial that a wireless system is able to identify other technologies present in its vicinity, for interference avoidance and management, as well as for the detection of systems that may be operating in violation of the spectrum regime agreed upon for the band. The use of machine learning for wireless technology classification allows unprecedented technology classification accuracy using a wide range of signal features. However, a number of research issues still remain open:

 Extensibility of results to different environments. In theory, machine learning allows scalability by building a generalised model using a broad set of signals, collected in multiple environments. However, when using small datasets, as if often the case in scientific research, this generalisation remains a challenging problem [11].

Selection of the input features. It is currently still an open re-56 search question on how to best engineer input features to enable effi-57 cient machine learning [12]. Manual feature selection limits the number 58 of required input features to only the ones deemed most effective, but 59 it requires extensive domain expert knowledge and can limit the perfor-60 mance due to the inability to extract hidden or underlying features. On 61 the other hand, automatic feature learning enables faster development 62 of models and applications while also trying to improve the representa-63

tion of data by discovering previously unknown features, at the risk of
making the models more complex. To the best of our knowledge, the
efficiency gains of both approaches for wireless technology classification
have not yet been quantified and compared.

⁶⁸ The main contributions of our work are the following:

• Quantitative comparison of the efficiency of machine learning 69 techniques using manual feature extraction versus automatic 70 feature learning for wireless technology classification. Specif-71 ically, we compare these two approaches by using multiple machine 72 learning techniques, including decision trees, neural networks, convolu-73 tional neural networks (CNN) and image classification techniques. In 74 addition, we evaluate the impact of different input features, including 75 Received Signal Strength Indicator (RSSI) data (suitable, for example, 76 to embedded devices) as well as more complex input features such as In-77 phase and quadrature (IQ) samples and Fast Fourier Transform (FFT) 78 of the IQ samples that generates spectrogram images, to explore how 79 well automatic deep learning can exploit features in more complex data. 80

Analysis of the generalisability and robustness to noise of
 wireless technology classification using machine learning. More
 specifically, we test generalisability using data collected in different un seen environments, to exploit the model's flexibility. Furthermore, the
 robustness of the models is explored by inducing noise into the datasets.
 This allows the assessment of the classification accuracy for multiple
 Signal to Noise (SNR) levels.

• Trade-off and complexity analysis of machine learning techniques. We compare the previously mentioned techniques by analysing their complexity in terms of trainable parameters, memory footprint and training time. We also discuss the trade-offs concerning the complexity of the proposed techniques.

The remainder of the paper is organised as follows. Section 2 discusses related work. Next, various feature learning techniques are presented, together with a dataset description, in section 3. In section 4, manual feature extraction techniques based on RSSI distributions are introduced, together with a detailed description of the decision trees and a fully connected neural network (FNN) that we used. Next, automatic feature learning techniques based on IQ samples and RSSI values, along with the CNN designs adopted, are introduced in section 5. In section 6, results of the aforementioned ap proaches are presented and compared in terms of accuracy, generalisation,
 robustness and complexity. The paper ends with conclusions in section 7.

¹⁰³ 2. Related work

Machine learning techniques are increasingly popular and widely adopted at different layers of the network protocol stack. Table 1 lists recent papers in the domain of wireless technology classification with their classification goals, input data, machine learning approaches and compares their contributions in terms of generalisation to multiple (unseen) locations, robustness to SNR and complexity trade-offs.

- The authors in [13] used CNNs for classifying 802.11 b/g, 802.15.4 and 802.15.1, all of which operate in unlicensed bands. Their accuracy exceeds 95% with a signal-to-noise ratio greater than -5dB.
- The authors of [14] classify the presence of radar signals, even with simultaneous transmissions of LTE and Wi-Fi systems.
- The authors of [15] target the same technologies as our paper. However, instead of machine learning, [15] uses fixed algorithms (heuristics) in an attempt to classify Wi-Fi, LTE and DVB-T, and the paper does not validate the results using different datasets.
- Besides technology classification, it is also possible to classify modulation techniques, for example using k-nearest neighbors (k-NN), Support
 Vector Machines (SVM) and Naive Bayes algorithms [16] or CNN based machine learning [17].
- Paper [18] identified eight kinds of signals: binary phase shift keying
 (Barker codes modulation), linear frequency modulation, Costas codes,
 Frank code and polytime codes (T1, T2, T3 and T4). This paper used
 image-based CNNs, which train on spectrogram images instead of RSSI
 or IQ data.
- In [19], the authors propose an end-to-end learning technique using 128 spectrum data. Their goal is to identify modulation techniques and 129 detect wireless interference with automatic feature learning. Three 130 CNNs are trained with different kinds of data: IQ samples, ampli-131 tude/phase data and frequency domain data. Their experiments show 132 that amplitude/phase data can outperform IQ and frequency domain 133 data in modulation classification, while the frequency domain achieves 134 the highest accuracy for interference detection. 135

-	F	F 1	F	F	r	F 1	F 1	
Paper	[13]	[14]	[15]	[16]	[17]	[18]	[19]	This
Classification	802.11,	Radar	802.11,	Modu-	Modu-	Modu-	Modu-	802.11,
goal	802.15.4,		DVB-T,	lation	lation	lation	lation,	DVB-T,
	802.15.1		LTE				interfer-	LTE
							ence	
Input Data	IQ	Spec-	RSSI	IQ	\mathbf{FFT}	Spec-	IQ	RSSI,
		trogram				trogram		IQ, FFT,
						-		spectrogram
Approach	CNN	CNN	Fixed	k-NN,	LSTM,	CNN	CNN	Rforest de-
			algor-	SVM,	DNN			cision trees,
			$_{\mathrm{tihm}}$	Naive				FNN, CNN
				Bayes				
Generalisation	ı		+-					\checkmark
locations								
Robustness	\checkmark	\checkmark		\checkmark	\checkmark	\checkmark	\checkmark	\checkmark
to SNR	-							
Complexity			+-	\checkmark	\checkmark			\checkmark
trade-offs			1 -	v	v			v

Table 1: Overview of related work in the field of wireless technology classification

Most of the above mentioned papers used IQ samples in the frequency-136 domain as training input, with some using additional data such as phase, am-137 plitude and average magnitude FFT. These samples are used as an input for 138 the machine learning techniques. However, IQ samples require complex sens-139 ing methods and such capability is not available on most resource-constrained 140 wireless devices. Only [17] and [15] (although [15] does not discuss complex-141 ity trade-offs) adopt a more resource-friendly solution using, respectively, 142 average magnitude FFT data or RSSI data that contains less information 143 compared to IQ samples but is easier to collect, while [16] discusses complex-144 ity trade-offs off multiple classifiers, with complex IQ data. Most papers do 145 validate robustness to noise with multiple SNR levels, an important metric 146 to validate classification performance. Unfortunately, only [15] uses train-147 ing data from multiple locations, but none of the above papers evaluate the 148 performance of its proposed machine learning techniques using multiple in-149 dependent and unseen datasets from different locations. Thus, in this paper 150 we propose and discuss which models are best suited to increase accuracy, 151 robustness and generalisability while trying to minimise complexity. To this 152 end, we (i) evaluate more types of input data than prior work (manual fea-153 tures from RSSI, RSSI, raw IQ, FFT IQ image-based), (ii) evaluate more 154 machine learning techniques than prior work (Decision Tree, FNN and CNN) 155 and *(iii)* analyse the impact of using two separate datasets from different lo-156

157 cations.

On another layer of the network stack, above signal and technology 158 recognition, sits traffic recognition. Likewise, traffic recognition is an ac-159 tive research topic in many performance optimisation and monitoring areas. 160 These include mobile, anonymity and encrypted traffic classification that en-161 able profiling and allow management tools to enhance network performance 162 [20, 21, 22]. However, the main difference is that our work focuses on robust-163 ness and generalisation towards multiple environments that can have various 164 channel conditions. Moreover, these works targeting traffic recognition tar-165 get manual and statistical feature extraction, while the models presented in 166 this paper favor raw signals to automatically extract features using CNNs. 167 However, when considering manual feature extraction, C4.5 decision trees 168 and random forests, the proposed models achieved good results comparable 169 to the traffic recognition papers. 170

¹⁷¹ 3. System description

In this section, we propose a spectrum manager framework which makes 172 use of the models in this paper and assists operators for fine tuning their 173 spectrum decisions. As mentioned above, one of our goals is to assess the 174 generalisability of the proposed machine learning techniques for technology 175 classification to systems deployed in different locations and under different 176 conditions. Hence, we describe the datasets we collected and used in our 177 study. These datasets are restricted to perform single-label classification. 178 Hence, no overlapping signals were allowed. Finally, an overview of the eval-179 uated technology classification approaches gives an overview of the models. 180 181

182 3.1. Spectrum manager framework

The proposed spectrum manager is shown in Figure 1 and performs the 183 following three tasks (i) fetch IQ samples, (ii) results from the trained mod-184 els, and (iii) spectrum decisions. The heart of the spectrum manager is a 185 classification module, which we design by using machine learning approaches 186 that do not require domain expertise. In the first task, IQ samples/RSSI 187 values are fetched from Universal Software Defined Radio (USRP) which is 188 part of the spectrum manager and is in a close proximity of the operators. 189 In the second task, the trained models are used for getting identification of 190 the technologies from the IQ samples fetched in the first task. Finally, the 191

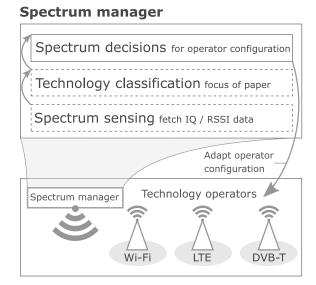


Figure 1: A spectrum manager can make decision based on technology classification models proposed in this paper to optimise usage of the wireless spectrum by different operators.

third task, makes spectrum policies and builds interference maps. This information can be conveyed by the spectrum manager to the operators for fine tuning their spectrum decisions so that they can fairly coexist with each other.

196 3.2. Data acquisition

To train technology classification models, we have utilised seven datasets: 197 the 6 datasets were captured at multiple locations in Ghent, Belgium and the 198 second one in Dublin, Ireland. We have made all datasets publicly available 199 for future research comparisons.⁴ ⁵ The objective of utilising datasets 200 captured at multiple and different locations is to investigate how well the 201 model can generalise for unseen environments. More precisely, the results 202 in this paper evaluate the performance of our models, trained on Ghent's 203 dataset and validated on Dublin's dataset. For the remainder of the paper, 204 we refer to training dataset as a *seen* dataset and the validation dataset as 205

⁴The dataset captured in Ghent is available at https://github.com/ewine-project/Technology-classification-dataset

⁵The dataset captured in Dublin is available at https://github.com/ewine-project/lte-wifi-iq-samples

206 an *unseen* one.

- The seen dataset consists of IQ samples of LTE, Wi-Fi and DVB-T captured in 6 various locations in Ghent ⁶.
- The unseen dataset consists of IQ samples for LTE and Wi-Fi. These samples were collected⁷ in the CONNECT building in Dublin city centre [23].

In both locations, IQ samples where captured, from which the RSSI was calculated⁸ using (1) for N = 16.

$$RSSI = 10 * log_{10}(\frac{1}{N}\sum_{k=1}^{N}(I_k^2 + Q_k^2))$$
(1)

where N and k correspond to the number of IQ samples per RSSI and the index of IQ samples, respectively.

Figures 2 and 3 show the time domain and spectrogram representation of the IQ samples of the seen (two locations in Ghent are shown) and unseen dataset, respectively. The figures show clear similarities but also have differences in terms of background noise, sending intervals and signal strength. These environmental and antenna-related differences are needed to enable and verify generalisation capabilities of the trained models in section 6.

222 3.3. Evaluated technology classification approaches

Table 2 provides an overview of the proposed approaches for wireless technology classification and the machine learning techniques adopted, together

⁶An Anritsu MS 2690A spectrum analyser was used to capture samples of each of the aforementioned signal types [15]. The Wi-Fi signal, captured in various office locations in Ghent, and contains traces at 5540 MHz and at 2412 MHz. The LTE signal was obtained from a base station nearby, operating at 806 MHz. Lastly, DVB-T signals were captured from a local TV broadcasting station that operates at 482 MHz. The IQ samples were collected at the rate of 10 MHz for a duration of 1.1 seconds.

⁷As a capture device, we used a B210 USRP software defined radio. From the dataset, we used 14 measurements, each of 2 sec, which consist of 125,000 RSSI or 2 million IQ samples, which translate to a total number of 1.75 million RSSI values or 28 million IQ samples.

 $^{^{8}}$ In total 68,750 RSSI values or 1.1 million I/Q samples were computed for each measurement of 1.1 seconds. We down sampled the measurements to a rate of 1 MHz to reduce the dataset footprint. 163 measurements were performed, which translate to 11,206,250 RSSI values or 179,300,000 IQ samples in total.

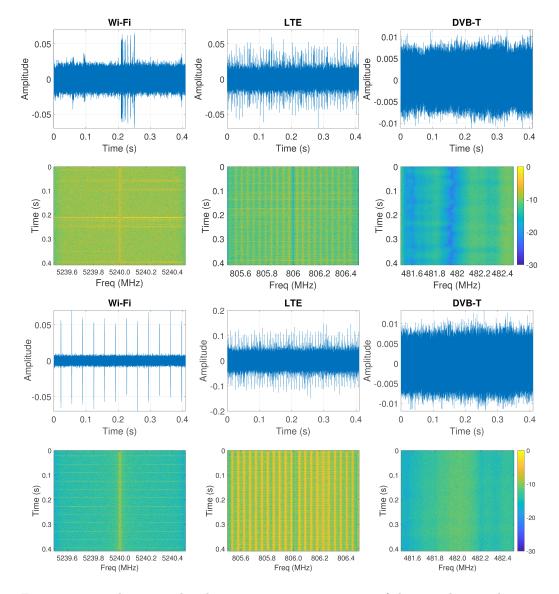


Figure 2: Time domain and and spectrogram representation of the seen dataset showing different characteristics for each technology. Two locations in Ghent with different environmental characteristics are shown, which can boost generalisation to multiple locations.

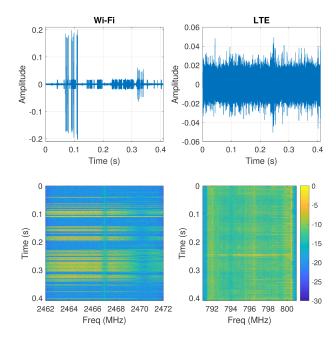


Figure 3: Time domain and and spectrogram representation of the unseen dataset captured at Dublin showing different characteristics compared to the seen dataset.

with their training data format. In the final column, we refer to the section where we discuss each approach in detail.

Table 2: Machine learning techniques and feature extraction approaches for technology classification proposed in this paper

Approach	ML technique	Data	Section
Man. feat.	Fully connected neural networks	RSSI	4.3
Man. feat.	Decision trees and random forests	RSSI	4.4
Auto. feat.	Conv. neural networks	RSSI	5.2
Auto. feat.	Conv. neural networks	IQ	5.2
Auto. feat.	Conv. neural networks	Spectrogram	5.2

Figure 4 draws an overview of the steps taken to achieve manual and autonomous feature extraction. Every training process starts with RAW IQ sample datasets collected at our various locations. Depending on the approach, samples will need to be recomputed to other formats. RSSI values, computed as discussed in 3.2, are used to manually extract features. In this scenario, discussed in 4.2, the model receives only the optimal selected subset
of features. IQ samples can be processed with FFT and visualised with a
spectrogram or directly used as raw input to the model. Once the data is
processed, the corresponding model is trained.

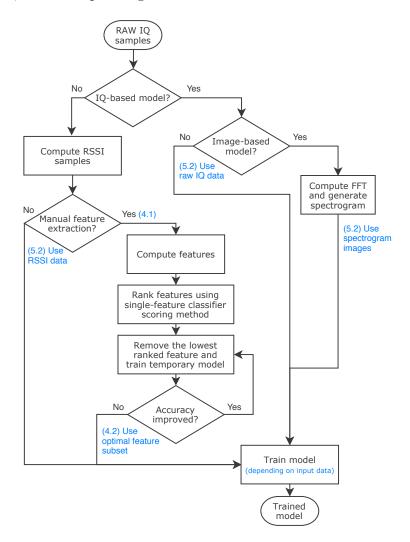


Figure 4: Overview of the steps taken to achieve manual and autonomous feature extraction, including their sections.

²³⁶ 4. Manual feature extraction based on RSSI distributions

This section discusses the manual feature extraction and selection processes and describes briefly the machine learning techniques which were used to train classifiers and generate results.

240 4.1. Manual feature extraction

Before extracting features, we preprocessed and converted RSSI data into 241 histograms that estimate the probability distributions of RSSI values. As 242 a use-case, these histograms are calculated using 256 RSSI samples which 243 corresponds to a sample duration of 4.096 ms. This method is based on 244 [15], which shows that these distributions offer valuable features. However, 245 here we extract and evaluate more and different features that are simple 246 to calculate. The histograms are used as input for the feature extraction 247 module. The output of this module is a feature vector X_i such that, 248

$$X_i = [r_0, r_1, ..., r_{19}, R_{min}, R_{max}, P_n, P_w, H_{std}, D_{mean}, D_{median}]$$
(2)

where:

250

• $\{r_0, r_1, ..., r_{19}\}$ is a set of 20 intervals selected from the input histogram. r_0 corresponds to the leftmost part of the histogram, while r_{19} represents the rightmost part. Each interval thus contains 5% of the histogram and its value indicates the frequency of RSSI values within the corresponding interval.

- R_{min} is the minimum RSSI value and thus the left boundary of the histogram.
- R_{max} is the maximum RSSI value and thus the right boundary of the histogram.
 - P_n is the measured number of peaks in the histogram.
- P_w is the width of the highest peak.
- H_{std} is the standard deviation of the histogram values.
- D_{std} is the standard deviation of the RSSI values upon which the histogram is calculated.
- D_{mean} is the mean of the RSSI values upon which the histogram is calculated.
- D_{median} is the median of the RSSI values upon which the histogram is calculated.

# features	Training accuracy	Validation accuracy
28 (all)	88.4%	74.0%
15	88.9%	77.0%
11	88.8%	76.1%

Table 3: Number of selected features with their accuracy on a (un)seen dataset

268 4.2. Feature selection

One advantage of using manual feature extraction methods is the con-269 trol over which features are used to train the model. [24] discusses feature 270 selection as a method to improve the accuracy of the model. To allow op-271 timal selection, each feature is ranked according to the score calculated by 272 a ranking method. Several such methods have been proposed by [24]. In 273 this work, we used the single-feature classifier method which gives the high-274 est prediction accuracy compared to other methods such as entropy-based, 275 correlation-based, etc. The single-feature classifier method takes each of the 276 features, one-by-one, and calculates the resulting accuracy as a ranking met-277 ric for the corresponding feature. 278

In order to determine how many features we select from the ranked list, we 279 start removing the lowest ranked feature and proceed up the list. Each time, 280 the classifier uses the remaining features to train. Finally, we know which 281 and how many are the most optimal features to select. The following fifteen 282 features were selected: $r_1, r_2, r_3, r_4, r_8, r_9, r_{10}, r_{11}, r_{12}, r_{19}, R_{min}, r_{max}, P_w, D_{std}$ 283 D_{mean} . Table 3 illustrates a higher accuracy when selecting a subset of fif-284 teen features compared to all 28 features, which confirms the findings of [24] 285 are also valid for wireless technologies, where using too many features can 286 complicate the model. In addition, the results show that removing too many 287 features results in a lower accuracy score. The model losing valuable infor-288 mation to learn classifying wireless technologies explains this behaviour. For 289 further results, the fifteen highest scoring features, according to the single-290 feature classifier ranking method, were used to compare the performance of 291 the classifier against competing approaches. 292

293 4.3. Fully connected neural network

Table 4 provides an overview of the employed artificial neural network (ANN) architecture. This ANN is also known as a FNN because of its multiple (two) hidden layers having connections to all nodes of the previous and following layers. The input layer with a size of 29 neurons, or 15 after feature selection, receives the manually extracted feature vectors, $v_n \in \mathbb{R}^{29}$, containing values as described in subsection 4.1. This layer is followed by two fully connected layers with 25 and 10 neurons respectively. Finally, an output layer classifies the wireless signal through three neurons for DVB-T, Wi-Fi and LTE. The first two layers use a radial basis activation function (3):

$$output = radbas(|| \boldsymbol{w} \cdot \boldsymbol{p} || b), \tag{3}$$

where \boldsymbol{w} and \boldsymbol{p} are weight and input vectors respectively, b is the bias and radbas(n) is

$$radbas(n) = e^{-n^2}.$$
(4)

The output of this activation function will be 1 when the difference between w and p is 0.

The last layer of the neural network uses a softmax activation function (5):

$$softmax(z)_i = \frac{e^{z_i}}{\sum_j e^{z_j}} \tag{5}$$

where j = 1, ..., # classes and z_i is

$$z_i = \sum_k p_k W_{ki} \tag{6}$$

where *i* is the considered output neuron, k = 1, ..., #neuronsPreviousLayer, 310 p_k is the output of the previous layer's neuron and W_{ki} is the weight applied 311 to p_k . In contrast to the models proposed in section 5, this neural network 312 is much smaller. There is no need for feature learning in raw data using 313 many deep and convolutional layers. Rather we designed a less complex 314 FNN that can perform better given already extracted features [25], hence 315 this design choice. The model learns by applying scaled conjugate gradient 316 back-propagation each time it is given training data. This gradient is used 317 to update the weights and bias values of the neural network. The training 318 of such a network requires the inputs, weights and activation functions all to 319 have derivative functions. 320

321 4.4. Decision tree and random forest

Compared to neural networks, decision trees offer insight into how classification is performed. Unlike neural networks, they are not considered blackboxes. Decision trees compare one of the features at each of their nodes. If

Table 4: FNN structure

Layer type	Layer size	Activation function
Input	15 neurons	radbas
Fully connected	25 neurons	radbas
Fully connected	10 neurons	radbas
Output	3 neurons	softmax

the value of the feature is smaller than the trained value, then the algorithm follows the left branch; if it is larger, then it follows the other direction. During the training phase of a decision tree, decisions are made upon which feature should be selected and what the value should be. This decision depends on the implementation, e.g., the C4.5 algorithm, which we used, splits the tree using normalised information gain, also called gain ratio (7) [26]:

$$Gainratio(Y, X) = \frac{H(Y) - H(Y|X)}{H(X)}$$
(7)

331 with

$$H(X) = -\sum_{i=1}^{n} P(x_i) \ln_2 P(x_i),$$
(8)

332 and

$$H(Y|X) = H(Y,X) - H(X),$$
 (9)

where $P(x_i)$ is the probability of feature X having a value x_i out of all possible values. H(X) thus represents uncertainty in X or the minimum bits needed to encode X [26]. H(Y,X) is the joint entropy and H(Y|X) is the conditional entropy between class Y and feature X.

337

The C4.5 algorithm for building decision trees is illustrated in Algorithm 338 1 [27]. In the algorithm, T represents the considered instances at each node. 339 The chosen label at a leaf is set when only one class is present in the instances 340 of a node or when there are no instances. In the last case, the chosen class 341 is the most frequent one in the instances at the parent node. Another case 342 is when only a few instances are present. Then, the class is set as the most 343 frequent one, present in these instances. Note that these early stopping 344 conditions try to prevent overfitting. Overfitting occurs when the model has 345 high accuracy on the training data, but low accuracy on the validation data. 346 Techniques such as pruning are further applied to prevent overfitting. Nodes 347

Algorithm 1: C4.5 Algorithm.

```
Input: Instances containing features X and classes Y.
Output: A classification decision tree.
ConstructTree(T):
if OneClass or FewCases then
    return leaf;
else
    create decision node N:
    for each attribute X do
     ComputeGainRatio(Y,X);
    end
    N.test = AttributeWithHighestGain;
    if N.test is continuous then
        find threshold;
     end
    foreach splitted T' in T do
         if T' is Empty then
             child of N is leaf;
         else
             child of N = ConstructTree(T');
         end
    end
    return N;
end
```

are replaced by one of their children nodes and the resulting accuracy with 348 validation data is captured. Finally, the algorithm chooses the node which 349 resulted in the most significant improvement on validation data. This method 350 is called sub-tree replacement and is executed as long as the accuracy on 351 validation data is increased [28]. As an alternative, C4.5 implementations do 352 sometimes only use the largest subtree to replace its parent. We implemented 353 pruning together with a maximum tree depth of 25 in order to maximise 354 generalisation while reducing the tree size and thus minimising complexity. 355

Finally, to further improve the accuracy of decision trees, we have explored and used ensemble learning techniques such as random forests for our results to compare state-of-the-art decision tree methodologies. Random forests further prevent overfitting by generating multiple C4.5-generated decision trees, each trained with a random subset of features at each node to reduce correlation between the trees. Each tree votes for the predicted class. Finally, the most voted for class Y is chosen given input X [29].

5. Automatic feature learning based on raw IQ samples and image based spectrograms

This section describes the automatic feature learning approaches that we have explored. Additionally, a description of CNNs, along with corresponding configuration details, is provided.

368 5.1. Feature learning

The approaches described in this chapter are based on supervised feature learning techniques which are heavily exploited in the computer vision domain. In this field, the manual feature extraction followed by dimensionality reduction (as in Section 4.1) is replaced by applying deep learning techniques directly on raw pixel intensities (e.g., the method proposed by the authors of [30]). Similarly, in our research, we apply FNN and CNNs on raw IQ values, their derived, simpler, RSSI samples and image-based spectrograms.

376 5.2. Convolutional neural networks

Table 5 provides an overview of the CNN architecture we adopted for the classification of wireless technologies. We started the design of our CNN architecture based on our previous work [31]. Next, we further improved generalisation to multiple locations and improved robustness to noise by experimentally fine tuning parameters as discussed further in this section. We implemented three types of CNNs based on their used data-type:

- 383
- 1. **RSSI-based CNN**: for training this CNN, we used RSSI samples, which are less complex than IQ samples. This CNN uses 256 RSSI samples as an input, which corresponds to 4.096 ms, similar to the sample length described in section 4.1.
- IQ-based CNN: In this CNN, 4,096 raw IQ samples are used, which
 corresponds also corresponds to 4.096 ms. In Table 5 an input size of
 8,192 is used because each IQ sample has two components.
- 391 3. Image-based CNN: The data used in this CNN are FFT IQ samples.
 392 Spectrograms are generated and saved as an image with dimensions 64
 393 x 64 pixels. Again, this corresponds to 4.096 ms per input.

Compared to the FNN, described in section 4.3, the CNN includes many layers without typical neurons. These layers include functions to process

RSSI-Ba	RSSI-Based CNN	IQ-Base	IQ-Based CNN	Image-Ba	Image-Based CNN
Layer	Output dimensions	Layer	Output dimensions	Layer	Output dimensions
Input	$1 \ge 256$	Input	$2 \ge 4096$	Input	64 x 64
Conv (64, 1x3), Relu	$1 \ge 254 \ge 64$	Conv (64, 1x2), Relu	$2 \ge 4095 \ge 64$	Conv (64, 2x2), Relu	63 x 63 x 64
Dropout	$1 \ge 254 \ge 64$	Dropout	$2 \ge 4095 \ge 64$	Max pooling (2,2)	$31 \times 31 \times 64$
Conv (16, 1x3), Relu	$1 \ge 252 \ge 16$	Conv (32, 1x3), Relu	$2 \ge 4093 \ge 32$	Batch normalization	$31 \ge 31 \ge 64$
Max pooling $(1,2)$	$1 \ge 126 \ge 16$	Max pooling $(1,2)$	$2 \ge 2046 \ge 32$	Zero padding	$35 \ge 35 \ge 64$
Dropout	$1 \ge 126 \ge 16$	Dropout	$2 \ge 2046 \ge 32$	Conv (32, 1x3), Relu	$35 \ge 33 \ge 32$
Flatten	2016	Conv (16, 2x2), Relu	$1 \ge 2045 \ge 16$	Max pooling $(2,2)$	$17 \times 16 \times 32$
Dense (20), Relu	20	Max pooling $(1,4)$	$1 \ge 511 \ge 16$	Batch normalization	$17 \times 16 \times 32$
Dropout	20	Flatten	8176	Zero padding	$21 \times 20 \times 32$
Softmax	33	Dense(25), Relu	25	Conv (16, 1x3), Relu	$21 \times 18 \times 16$
		Dense(3)	ĉ	Conv (4, 3x1), Relu	$19 \ge 18 \ge 4$
		Softmax	ĉ	Conv (2, 2x2), Relu	$18 \times 17 \times 2$
				Flatten	612
				Dense (75)	75
				Dropout	75
				Dense (10), Relu	10
				Dropout	10
				Softmay	5

Table 5: CNN architectures with their corresponding data-type

the output from previous layers. The first kind of processing layer is a con-396 volutional layer. Such layers contain multiple learnable feature maps and 397 calculate their values from various, but not all (such as in fully connected 398 layers), previous neurons. They intend to have small receptive fields and 399 decrease parameters by sharing filter weights [32]. The size of these feature 400 maps varies in the convolutional layers, e.g., the first convolutional layer 401 from the image-based CNN contains 64 feature maps with a size of 2 x 2, 402 connected to neurons of the input layer. We experimented with increased 403 stride sizes, which control the number of values the filter has to move. This 404 is by default 1 by 1 so that each convolution connects all neighbours values 405 within the convolutional filter size. However, increased stride sizes decreased 406 the performance of the model. We believe this is due to features being more 407 present locally and chronologically in our data. Increasing the stride size will 408 decrease the number of local receptive fields, which results in lower perfor-400 mance. 410

⁴¹¹ Dropout is the next type of layer we used in our CNN. This layer produces
⁴¹² more generalised models by preventing overfitting of training data, which we
⁴¹³ experimentally validated.

Pooling is another type of layer with the intent of reducing the total number of parameters to train on. This dimensionality reduction dramatically enhances training time and reduces the model's required memory footprint. In our case, we found optimal results with a max-pool size of 1X2 and 2X2. This pool will take 2 and 4 values, respectively, from the previous layer and output the maximum. Using max-pooling in the RSSI CNN, the number of trainable parameters decreased from 87,494 to 43,747.

The above mentioned layers are followed by a fully-connected dense layer.
Each neuron of this layer is connected to all of the previous layer's neurons.
This way, learned local features from previous convolutional layers get connected and are used to perform the final steps of classification.

The final layer contains three neurons, one for each class, and is activated with a softmax layer, as described in 4.3. In contrast to the FNN discussed in 4.3, each convolutional and dense layer is succeeded by a ReLU activation function. Here, this activation function performs slightly better than the radial basis activation function. The ReLU function, first proposed in [33], is defined in (10):

$$f(x) = max(0, x) \tag{10}$$

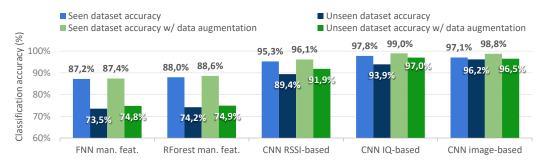


Figure 5: Results of manual and automatic feature learning approaches.

Finally, the models are trained for maximum 100 epochs using early stopping criteria (no loss improvement for 10 epochs) and a batch size of 256 samples.

434 6. Results and comparison

This section first presents results regarding accuracy in seen environments and afterwards generalisation towards unseen environments. Next, robustness towards additional noise levels is analysed, followed by a complexity analysis of the proposed approaches. All results are validated using 10-fold cross-validation to ensure there is no bias towards portions of the dataset and minimise variation of the results [34].

441 6.1. Accuracy

Results of the proposed approaches are presented in Figure 5. In this 442 scenario, automatic feature learning with the CNN using raw IQ samples 443 achieves the highest accuracy (97.8%), followed closely by the image-based 444 CNN (97.1%) and the RSSI-based CNN (95.3%). Manual feature extraction 445 methods achieve a slightly lower accuracy for both the FNN (87.2%) and 446 the Random Forest (RForest) decision trees (88.0%). Figures 6a - 6e show 447 the above results in more detail using confusion matrices. More specifically, 448 accuracies for each correct classification and classification errors of Wi-Fi, 449 LTE and DVB-T are shown. We observe classification errors to be the highest 450 for Wi-Fi for manual RSSI based methods. Around 40% of Wi-Fi is identified 451 as DVB-T. This leads to the conclusion that better features are needed to 452 differentiate the two technologies. Despite these results, LTE classification 453 seems to perform well across all models, even for less-complex manual feature 454 extraction-based and raw RSSI-based methods. The IQ and image-based 455

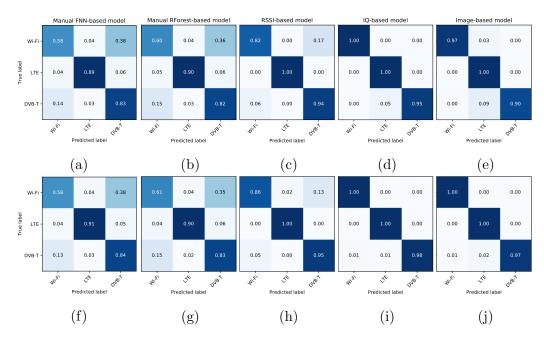


Figure 6: Above confusion matrices of all five approaches (a) Manual FFN model, (b) Manual RForest model, (c) RSSI CNN model (d) IQ CNN model (e) Image CNN model. Below confusion matrices with approaches using data augmentation including different SNR levels (f) Manual FFN model, (g) Manual RForest model, (h) RSSI CNN model (i) IQ CNN model (j) Image CNN model.

⁴⁵⁶ models clearly have superior performance as a result of the more complex⁴⁵⁷ models and feature-rich data.

458 6.2. Generalisability

The above results are only viable for environments that closely resemble 459 those where the training data was collected. Therefore, we assess the gen-460 eralisation of the models and validate the classification performance with a 461 dataset from an unseen and different environment. Figure 5 shows for each 462 approach lower accuracy on unseen datasets. This result is expected because 463 the environment has other properties and captured signals are influenced in 464 different ways. However, IQ- and image-based approaches still manage to 465 achieve an accuracy above 93%, while the RSSI-based CNN achieves 89.4%. 466 Manual feature extraction techniques struggle to generalise, exhibiting an ac-467 curacy just under 75%. This behaviour occurs because valuable information 468 is lost through conversion of IQ samples to RSSI and further through manual 469 extracted features. 470

To remedy this, we combined the techniques to improve generalisation 471 and avoid overfitting discussed in 5.2, with additional data augmentation 472 techniques. These techniques transform each sample of the dataset in various 473 ways and add them to the original dataset. Specifically, we post-processed the 474 seen dataset and included noise of different SNR levels, which is considered 475 as a way of applying data augmentation techniques to IQ samples and RSSI 476 values. Each sample is extended with noise, with SNR levels ranging from 477 -15dB to +30dB with a step of 5dB. As a result, the original dataset size is 478 increased by a factor of 10. 470

The results presented in Figure 5 illustrate accuracy improvements in all 480 approaches through data augmentation, especially on the unseen dataset with 481 the CNN using raw RSSI and IQ data (achieving and additional 2.5% - 3.1%482 generalisation increase). This leads to a very competitive scenario were RSSI, 483 IQ and image-based CNN can be considered feasible for wireless technology 484 classification. While manual feature extraction techniques show performance 485 just under 90% in scenarios similar to those of the trained datasets, unseen 486 scenarios keep struggling, with accuracies around 75%. These data augmen-487 tation techniques also show 1-7% improvement for single class classification 488 accuracy on the seen dataset as shown in figures 6f - 6j. 489

490 6.3. Robustness

Next, we discuss the robustness of our proposed solutions against addi-491 tional noise levels. Again, the models are trained with data containing SNR 492 levels ranging from -15dB to +30dB. Validation results are collected for un-493 trained samples in each SNR level. Figure 7 illustrates classification accuracy 494 as a function of SNR. The image-based CNN achieves the highest accuracy 495 overall, even in the low SNR scenario of -15dB. This is due to the fact that 496 the image based CNN, which uses FFT of the IQ samples, is more immune 497 to noise. As such the authors of [35] prove that such FFT frequency-based 498 features surpass time-based features for wireless device identification in de-499 graded SNR scenarios. Unsurprisingly, in high SNR scenarios it is clear that 500 the automatic feature learning techniques outperform the manual feature ex-501 traction methods, which have limited features. Moreover, the similar and 502 limited performance of the RForest and the FNN also hint to inferior feature 503 extraction compared to their automatic extraction counterpart. Looking fur-504 ther at the results, the IQ-based CNN performs notably worse in low SNR 505 scenarios. High sensitivity to noise by IQ samples is one possible underlying 506 reason for this result. With these fluctuations in the dataset, the IQ-based 507

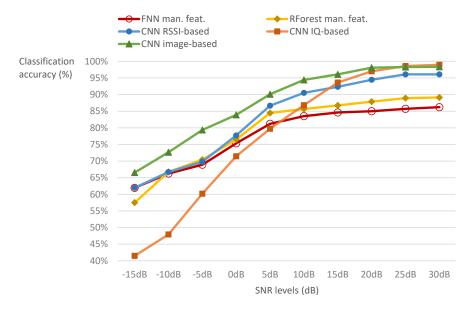


Figure 7: Classification accuracy as a function of SNR levels, for manual and automatic feature learning approaches.

CNN cannot learn to classify technologies in a reliable way. Results of the 508 RSSI-based CNN further support this explanation because multiple IQ sam-509 ples are averaged to become RSSI samples, as explained in equation 1 and are 510 thus less susceptible to fluctuations due to added noise. As such, the input 511 to the neural network has a much larger impact considering noise for IQ sam-512 ples compared to RSSI samples. The RSSI-based CNN model achieves good 513 performance, even in low SNR scenarios with an utmost difference of 10%514 compared to image-based CNN at -5dB, while performing only 3% less at 515 high SNR scenarios compared to other automatic feature learning methods. 516 These CNN-enabled methods prove to be robust from 10dB and upwards 517 with accuracies ranging between 86% and 98%. 518

519 6.4. Complexity

Table 6 illustrates the complexity of the proposed approaches. Results are collected on a Windows computer with an Intel® CoreTM CPU i9-9900K 0 3.60GHz, NVIDIA® TITAN RTXTM 24GB graphics card and 32GB of system memory. Manual feature extraction methods require less memory and are much faster in terms of training time. Moreover, the RSSI-based CNN achieves a much smaller memory footprint compared to the more complex

Model	Weights	Memory	Train time
RForest man. feat.	6393	0.08 GB	19s
FNN man. feat.	1018	0.12GB	51s
CNN RSSI-based	43747	0.81GB	100s
CNN IQ-based	212935	8.46GB	1500s
CNN Image-based	55430	2.61GB	950s

Table 6: Trainable weights, memory footprint and training time of the proposed approaches

IQ- and image-based methods. One of the reasons is the 16 times smaller 526 input size. The IQ- and image-based methods require high-end GPUs to 527 train on. Furthermore, because of their high number of weights, layers and 528 convolutions, they require more resource-heavy systems to deploy as wireless 529 technology classification systems. Although IQ-based models require most 530 resources, we want to highlight that these model require no pre-processing. 531 This makes the model very interesting compared to image-based models 532 which require computational-heavy FFT and image generation capabilities. 533 This pre-processing can limit the feasibility when the model is deployed for 534 wireless classification. 535

As a conclusion, manual feature extraction methods are very resourcefriendly, but only perform well in known environments. Automatic feature learning methods perform better, especially in terms of generalisation. On the one hand the RSSI-based CNNs show great efficiency potential with their relative small memory footprint and high accuracy. On the other hand, IQand image-based methods achieve the highest prediction accuracies no matter their resource requirements.

⁵⁴³ 7. Conclusions and future work

Machine learning techniques show enormous potential in many domains, 544 including wireless technology classification. In this domain, due to increasing 545 heterogeneity in wireless communications, often sharing the same spectrum 546 band, sensing the environment and making intelligent decisions is crucial. 547 Many of the previous works present deep learning approaches to successfully 548 identify wireless technologies on the fly. However, many of the proposed 549 methods target only resourceful devices and fail to address generalised and 550 robust models for different environments with changing noise levels. 551

In this paper, we have proposed and evaluated techniques to allow wire-552 less technology classification for resource-constrained devices, as well as for 553 more resourceful devices. Furthermore, we have shown that data augmen-554 tation techniques add an additional boost to generalisation, next to vari-555 ous model design choices, for unknown environments up to 3.1%. We have 556 demonstrated that applying FFT algorithms to IQ samples, to further create 557 image-based spectrograms, enables high accuracy, even in lower SNR scenar-558 ios. Raw IQ files achieve the highest generalisation capabilities by achieving 559 the highest accuracy in unseen environments. Finally, manual feature extrac-560 tion proved to be inferior compared to automatic feature learning in terms 561 of accuracy, but can still be useful in known environments, while requiring 562 very low complexity. Moreover, the less complex RSSI-based model offers a 563 good balance between complexity, accuracy, generalisation and robustness to 564 noise. These results demonstrate the positive effect of choosing the correct 565 machine learning technique and data format. As such, the outcome of this 566 paper enables wireless domain experts to incorporate intelligence into wireless 567 communications using machine learning techniques while targeting multiple 568 environments and recommends multiple approaches for wireless technology 569 classification. 570

571

We envision future research adding support for overlapping signals. This 572 will enrich the models support for irregular signal behaviour and prevent 573 misclassification for these kind of signals. Additionally, autoencoders can 574 be used for semi-supervised learning, minimising the required amount of 575 labelled data that is needed. This will further accelerate the adoption of new 576 supported technologies in many environments. Furthermore, future work 577 can make intelligent decisions for wireless technology operators based on the 578 detected present technologies. Finally, models with even lower complexity 579 should be developed with a small accuracy-complexity trade-off, reducing the 580 operational costs of future intelligent devices. 581

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