Arias Montano: Institutional Repository of the University of Huelva

PHYSICAL REVIEW C 98, 034615 (2018)

Interaction of ⁸He with ²⁰⁸Pb at near-barrier energies: ⁴He and ⁶He production

G. Marquínez-Durán,¹ I. Martel,¹ A. M. Sánchez-Benítez,² L. Acosta,³ J. L. Aguado,¹ R. Berjillos,¹ A. R. Pinto,¹ T. García,¹ J. A. Dueñas,⁴ K. Rusek,⁵ N. Keeley,^{6,*} K. W. Kemper,^{7,5} M. A. G. Álvarez,⁸ M. J. G. Borge,⁹ A. Chbihi,¹⁰ C. Cruz,⁹ M. Cubero,^{11,12,9} J. P. Fernández-García,⁸ B. Fernández-Martínez,¹³ J. L. Flores,¹⁴ J. Gómez-Camacho,^{13,8} J. A. Labrador,¹³ F. M. Marqués,¹⁵ A. M. Moro,⁸ M. Mazzocco,¹⁶ A. Pakou,¹⁷ V. V. Parkar,^{1,†} N. Patronis,¹⁷ V. Pesudo,⁹ D. Pierroutsakou,¹⁸ R. Raabe,¹⁹ R. Silvestri,¹⁸ N. Soić,²⁰ Ł. Standyło,⁵ I. Strojek,⁶ O. Tengblad,⁹ R. Wolski,^{21,22} and Z. Abou-Haidar¹³ ¹Science and Technology Research Centre (STRC), University of Huelva, 21071 Huelva, Spain ²Departamento de Ciencias Integradas y Centro de Estudios Avanzados en Física, Matemáticas y Computación, Facultad de Ciencias Experimentales, Universidad de Huelva, 21071 Huelva, Spain ³Instituto de Física, Universidad Nacional Autónoma de México, A.P. 20-364, Distrito Federal 01000, Mexico ⁴Departamento Ingeniería Eléctrica y Centro de Estudios Avanzados en Física, Matemáticas y Computación, Universidad de Huelva, 21071 Huelva, Spain ⁵Heavy Ion Laboratory, University of Warsaw, ul. Pasteura 5a, 02-093 Warsaw, Poland ⁶National Centre for Nuclear Research, ul. Andrzeja Soltana 7, 05-400 Otwock, Poland ⁷Department of Physics, Florida State University, Tallahassee, Florida 32306, USA ⁸Departamento de Física Atómica, Molecular y Nuclear, Universidad de Sevilla, 41080 Seville, Spain ⁹Instituto de Estructura de la Materia, CSIC, 28006 Madrid, Spain ¹⁰GANIL, CEA and IN2P3-CNRS, B.P. 5027, 14076 Caen Cedex, France ¹¹Escuela de Física, Universidad de Costa Rica, 11501 apdo. 2060 San José, Costa Rica ¹²CICANUM, Universidad de Costa Rica, 11502 apdo. 2060 San José, Costa Rica ¹³Centro Nacional de Aceleradores (Universidad de Sevilla, Junta de Andalucía, CSIC), 41092 Seville, Spain ¹⁴Departamento de Ingeniería Eléctrica, Universidad de Huelva, 21071 Huelva, Spain ¹⁵Laboratoire de Physique Corpusculaire, 14050 Caen Cedex, France ¹⁶Dipartimento di Fisica and INFN, Università di Padova, 35131 Padova, Italy ¹⁷Department of Physics and HINP, University of Ioannina, 45110 Ioannina, Greece ¹⁸INFN - Sezione di Napoli, Via Cintia, 80126 Napoli, Italy ¹⁹KU Leuven, Intituut voor Kern-en Stralingsfysica, Celestijnenlaan 200D, 3001 Leuven, Belgium ²⁰Rudjer Bošković Institute, Bijenicka 54, 10000 Zagreb, Croatia ²¹Institute of Nuclear Physics PAN, Kraków, Poland ²²Flerov Laboratory of Nuclear Reactions, JINR, Dubna 141980, Russia

(Received 7 June 2018; revised manuscript received 16 August 2018; published 28 September 2018)

Angular distributions for the inclusive ⁴He and ⁶He production cross sections in the ⁸He + ²⁰⁸Pb system at incident energies of 16 and 22 MeV measured at the SPIRAL facility of the GANIL laboratory are presented. Using a combination of kinematical arguments and distorted wave Born approximation (DWBA) calculations, neutron transfer reactions were inferred to be the dominant contributors to both inclusive cross sections. Model-dependent values for the ratios of two- to one-neutron stripping, σ_{2n}/σ_{1n} , were derived and compared with previous results for ⁸He and ⁶He projectiles incident on other heavy targets. Three- and four-neutron stripping were inferred to be the main processes leading to ⁴He production, although the exact mechanism remains to be elucidated.

DOI: 10.1103/PhysRevC.98.034615

I. INTRODUCTION

Recently, precise data for the elastic scattering of ⁸He from a ²⁰⁸Pb target at an incident energy of 22 MeV, slightly above the Coulomb barrier, were presented and compared with existing data for ⁶He + ²⁰⁸Pb at the same incident energy

[1]. A larger total reaction cross section was obtained for ⁸He than for ⁶He, suggesting an increased neutron stripping cross section for ⁸He that more than compensates for an expected lower breakup cross section than ⁶He, due to its higher breakup threshold and probable weaker dipole coupling to the continuum.

Some experimental studies of the reactions of ⁸He incident on heavy targets at near-barrier energies have already been performed. Direct and fusion-evaporation reactions for the ⁸He + ²⁰⁸Pb system were studied at 26 MeV via γ spectroscopy [2]. Although the statistics were low, the

^{*}Corresponding author: nicholas.keeley@ncbj.gov.pl

[†]Present address: Nuclear Physics Division, Bhabha Atomic Research Centre, Mumbai 400085, India.

observed population of low-spin states in ²⁰⁹Pb suggests a strong 1n stripping process, with a cross section comparable to that for the most probable fusion-evaporation channel, 208 Pb(8 He, 4n) 212 Po, to within a factor of about 2 in favor of fusion evaporation. In Refs. [3,4], measurements of heavy residue production in the ${}^{8}\text{He} + {}^{197}\text{Au}$ system at several near-barrier energies are presented. Excitation functions are reported which show that neutron stripping dominates over fusion for energies up to about 10 MeV above the barrier. Coupled reaction channels (CRC) calculations that describe the total neutron transfer strength provide a good simultaneous description of the fusion excitation function, suggesting that breakup is not as important for ⁸He as for ⁶He. A comparison between the fusion cross sections (σ_{Fus}) for the 4,6,8 He + 197 Au systems showed that σ_{Fus} for 6 He and 8 He are similar at energies below the barrier and larger than for ⁴He.

In this work, we present inclusive ⁴He and ⁶He production angular distributions for the ⁸He + ²⁰⁸Pb system at incident energies of 16 and 22 MeV. A combination of kinematics and calculations enables a number of conclusions to be drawn concerning the relative importance of neutron stripping reactions, as well as an upper limit on the fusion cross section at 22 MeV.

II. EXPERIMENT AND DATA ANALYSIS

The experiment was carried out at the SPIRAL facility of the GANIL laboratory in Caen, France, and a detailed description of the experimental setup was given in Refs. [1,5]. As shown in these works, the double-sided silicon strip detector ΔE -E telescopes of the GLORIA array [5] provided clear separation between the He isotopes produced in the interaction between the beam and target so that the ⁸He, ⁶He, and ⁴He yields were unambiguously extracted. The strip detectors are subdivided into pixels, defined as the intersection of a p strip (vertical) and an n strip (horizontal), see Ref. [5], with each pixel covering $3-4^{\circ}$ in the laboratory frame at the target. The ΔE and E stages of the telescopes were 40 μ m and 1 mm thick, respectively. The rapid variation of the elastic scattering as a function of scattering angle required great care in determining the angle of each pixel since, as usual with radioactive beams, the beam spot on target was large, \sim 3.5 mm in diameter. The procedure for establishing the detection angle of a given strip is given in Ref. [1] and relied on comparing a detailed simulation of the detection system with the elastic scattering in the region where it is dominated by Coulomb scattering.

In addition to the previously reported elastic scattering data at a ⁸He incident energy of 22 MeV [1], elastic scattering data were also obtained at 16 MeV and ⁶He and ⁴He yields at both energies. Figure 1(a) shows the events from all the strip detectors gated on ⁴He at 22 MeV. The vertical axis is the total energy deposited in a given telescope as a function of the scattering angle. The intense horizontal line at the bottom of the figure corresponds to α particles arising from fusion-evaporation events, matching very well the α -decay energies of ²¹²Po. There are two other main groups, the first at scattering angles between 60 and 160° from neutron transfer reactions and a second, weaker group at forward angles, between 20 and 40°, from ⁸He \rightarrow ⁴He + 4*n* breakup.

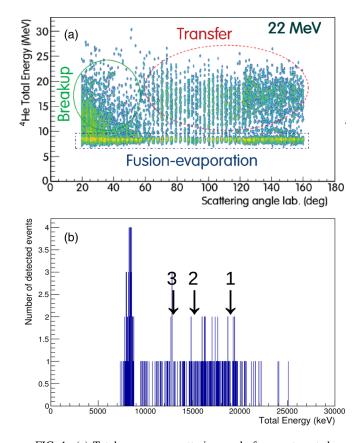


FIG. 1. (a) Total energy vs scattering angle for events gated on ⁴He produced in the ⁸He + ²⁰⁸Pb interaction at an incident energy of 22 MeV. Regions corresponding to the different production mechanisms are labeled. (b) Number of counts vs energy for events gated on ⁴He summed over pixels at a scattering angle of $\theta_{lab} = 94.5^{\circ}$. The numbered arrows denote the energy of ⁴He ejectiles corresponding to the optimum *Q* values of Table II for the following reactions: (1) ²⁰⁸Pb(⁸He, ⁴He)²¹²Pb, (2) ²⁰⁸Pb(⁸He, ⁵He \rightarrow ⁴He + *n*)²¹¹Pb, and (3) ²⁰⁸Pb(⁸He, ⁶He^{*}_{1.8} \rightarrow ⁴He + 2*n*)²¹⁰Pb. For reactions 2 and 3, the arrows mark the centers of the energy distributions of ⁴He arising from the decay of the ⁵He 3/2⁻ ground-state resonance and the ⁶He 1.8-MeV 2⁺ resonance, respectively; see text for further details. The narrow peak at approximately 8.8 MeV corresponds to α particles from the decay of the ground state of ²¹²Po produced by fusion evaporation.

These regions are drawn following many published heavyion reaction data, where it is always found that for energies below the Coulomb barrier the transfer cross section peaks at 180° and falls off more or less rapidly as the scattering angle decreases until it becomes negligible at forward angles. For incident energies just above the Coulomb barrier, the transfer angular distributions exhibit the classical bell-shaped peak structure, with the peak angle gradually moving to more forward angles as the incident energy increases. Both incident energies studied in this experiment were sufficiently low that there was a clear kinematic separation between transfer and breakup and any ⁴He and ⁶He events at forward angles necessarily arise from breakup processes since the transfer cross sections will be negligible in this region. There may be some slight overlap of breakup and transfer contributions

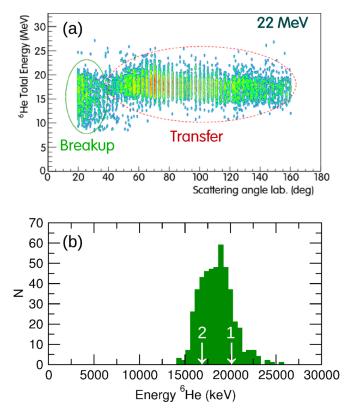


FIG. 2. (a) Total energy vs scattering angle for events gated on ⁶He produced in the ⁸He + ²⁰⁸Pb interaction at an incident energy of 22 MeV. Regions corresponding to the different production mechanisms are labeled. (b) Number of counts vs energy for events gated on ⁶He summed over pixels at a scattering angle of $\theta_{lab} = 70^{\circ}$. The numbered arrows denote the energy of ⁶He ejectiles corresponding to the optimum Q values of Table II for the following reactions: (1) ²⁰⁸Pb(⁸He, ⁶He)²¹⁰Pb and (2) ²⁰⁸Pb(⁸He, ⁷He \rightarrow ⁶He + n)²⁰⁹Pb. For reaction 2, the arrow marks the center of the energy distribution of ⁶He arising from the decay of the ⁷He 3/2⁻ ground-state resonance; see text for further details.

but this is not expected to be significant. The shapes of the extracted inclusive angular distributions and distorted wave Born approximation (DWBA) calculations provide *a posteriori* justification for these conclusions. The energy spectrum of events gated on ⁴He from several pixels around $\theta_{lab} = 94.5^{\circ}$ added together is given in Fig. 1(b). In Fig. 2, we show similar plots for events gated on ⁶He.

In Fig. 3, we present the elastic scattering data for an incident ⁸He energy of 16 MeV, together with the previously published data at 22 MeV [1]. The solid curves represent optical model fits to the data. The 22-MeV curve employs the potential parameters from Table I of Ref. [6]. These also give a reasonable description of the data at 16 MeV but the best fit, displayed on Fig. 3 as the solid red curve, was obtained by increasing the imaginary well depth W to 50.0 MeV. The dashed red curve denotes the 16-MeV elastic scattering angular distribution calculated using the same optical potential parameters as at 22 MeV. There is a small but noticeable difference in the angular distribution calculated with these parameters compared to the best fit,

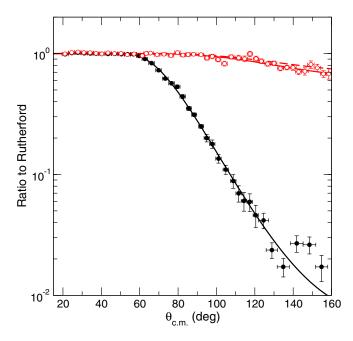


FIG. 3. Angular distributions for the 8 He + 208 Pb elastic scattering at 16 MeV (open circles) and 22 MeV [1] (filled circles). The solid curves denote optical model fits to the data; see text for details. The dashed curve denotes the 16-MeV elastic scattering angular distribution calculated using the same optical potential parameters as at 22 MeV.

leading to an ~8% increase in χ^2 and a ~24% decrease in total reaction cross section (σ_R) compared to the best-fit values. The σ_R extracted from the optical model fits are given in Table I. The uncertainties represent the effect of varying W such that χ^2 increased by 10% compared to the minimum values.

Ratios of the number of ⁶He to ⁸He and ⁴He to ⁸He detected, the latter excluding the ⁴He at low energies arising from fusion evaporation, were formed for each pixel and the results converted into laboratory frame absolute cross sections by multiplying by the appropriate elastic scattering cross-section angular distributions obtained from the optical model fits to the elastic scattering data, suitably transformed to the laboratory frame. The resulting angular distributions are plotted in Fig. 4. Errors are purely statistical. It is apparent that

TABLE I. Integrated cross sections for ⁶He ($\sigma_{^{6}\text{He}}$) and ⁴He ($\sigma_{^{4}\text{He}}$) production obtained from fits to the experimental angular distributions shown in Fig. 4. Also given are the total reaction cross sections from the optical model fits to the elastic scattering data plotted on Fig. 3 (σ_{R}) and total 1*n*-stripping cross sections (σ_{1n}) from the DWBA calculations described in Sec. III, while $\sigma_{\text{Fus}} = \sigma_{\text{R}} - (\sigma_{^{6}\text{He}} + \sigma_{^{4}\text{He}})$ represents an upper limit on the fusion cross section.

| $\overline{E_{\text{lab}}}$ (MeV) | σ_{1n} (mb) | $\sigma_{^{6}\mathrm{He}} (\mathrm{mb})$ | $\sigma_{^{4}\mathrm{He}} (\mathrm{mb})$ | $\sigma_{\rm R}~({\rm mb})$ | $\sigma_{\rm Fus}~({\rm mb})$ |
|-----------------------------------|--------------------|--|--|-----------------------------|-------------------------------|
| 16 | 90 ± 3 | 203^{+10}_{-28} | 26 ± 5 | 254 ± 60 | 25^{+61}_{-66} |
| 22 | 292 ± 61 | 871 ± 31 | 393^{+10}_{-33} | 1529 ± 40 | 265^{+52}_{-60} |

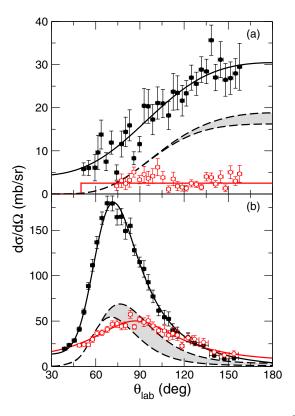


FIG. 4. Laboratory frame angular distributions of total ⁶He (filled circles) and ⁴He (open circles) yields at 16 (a) and 22 MeV (b). The solid curves represent fits to the data while the dashed curves and gray shaded areas denote the results of ²⁰⁸Pb(⁸He, ⁷He)²⁰⁹Pb single-neutron stripping DWBA calculations including the uncertainties due to the use of different distorting potentials in the exit channels (see text for details).

the shapes of the angular distributions (with the exception of the ⁴He yield at 16 MeV where the statistics are too low to determine accurately the shape) are characteristic of transfer reactions. However, it will be noted that the angular distributions displayed in Fig. 4 are confined to angles $\theta_{lab} > \sim 40^{\circ}$ whereas the measurements extend down to $\theta_{lab} = 20^\circ$, as seen in Figs. 1 and 2. This cutoff was imposed by the angular resolution of the pixels of the GLORIA array. At forward angles (in this case, for angles $\theta_{lab} \lesssim 40^{\circ}$) the elastic scattering cross section varies too rapidly as a function of angle over the range subtended by a pixel for a reliable absolute cross section to be extracted from the ⁶He to ⁸He and ⁴He to ⁸He ratios (the ratios themselves are, of course, unaffected by this problem). At larger angles, the variation of the elastic scattering cross section as a function of angle is slow enough not to cause a problem. This does mean that we are, unfortunately, unable to make any quantitative deductions concerning the contribution of breakup to the ⁶He and ⁴He yields.

The solid curves on Fig. 4 represent fits to the experimental angular distributions. At 16 MeV, the ⁶He yield was fitted with a third-order Legendre polynomial which reproduces the shape very well. The ⁴He yield was simply fitted by two straight line segments, 0 mb/sr for angles $0^{\circ} < \theta_{lab} < 50^{\circ}$ and 2.5 mb/sr for $50^{\circ} < \theta_{lab} < 180^{\circ}$. At 22 MeV, the ⁶He yield

was well reproduced by the sum of two Lorentzian peaks while the ⁴He yield was well described by a single Lorentzian. The integrated cross sections obtained from these fits are given in Table I. The uncertainties were estimated by scaling the fits to give χ^2 values 20% greater than the minimum values. The asymmetric errors on some values reflect the scatter in the points, emphasized somewhat by this procedure.

III. DISCUSSION

In Tables II and III, we give the Q values for the various direct reaction processes that can yield ⁴He and ⁶He nuclei in the exit channel, respectively, together with the optimum Q values for the A(a, b)B transfer processes calculated according to the Brink matching rules [7,8]:

$$Q_{\text{opt}} = (Z_b Z_B - Z_a Z_A) e^2 / R - \frac{1}{2} m v^2,$$
 (1)

where the charge on nucleus *i* is denoted by $Z_i e$, the relative velocity of the two nuclei in the region of interaction (separated by distance *R*) by *v*, and the mass of the transferred particle by *m*. For transfers of neutron(s), the first term is zero so Q_{opt} will always be negative in these cases. The relative velocity *v* may be calculated as [9]

$$v = [2(E_{\rm c.m.} - E_{\rm B})/\mu]^{1/2},$$
 (2)

where $E_{\rm B}$ and μ are the Coulomb barrier and reduced mass of the projectile-target system, respectively. We took a Coulomb barrier of 18 MeV, similar to the empirical result of Ref. [10] for the ⁶He + ²⁰⁸Pb system, when calculating the relative velocity of the ⁸He + ²⁰⁸Pb nuclei. The $Q_{\rm opt}$ values given are for an incident ⁸He energy of 22 MeV.

Tables II and III indicate that the ⁴He production is the most complicated of the two, since more processes may, in principle, contribute. However, Fig. 1(a) suggests that the ⁴He arising from breakup are well separated from those produced by transfer events. Three-body kinematics calculations with the code PAKINE3 [11] support this suggestion, indicating that at the angles where we have extracted the angular distributions the contribution to the ⁴He yield from breakup should be negligible. The three numbered arrows on Fig. 1(b) mark the energies of ⁴He ejectiles corresponding to Q_{opt} for the following reactions: (1) ²⁰⁸Pb(⁸He, ⁴He)²¹²Pb, (2) ²⁰⁸Pb(⁸He, ⁵He \rightarrow ⁴He + n)²¹¹Pb, and (3) ²⁰⁸Pb(⁸He, ⁶He^{*}_{1.8} \rightarrow ⁴He + 2n)²¹⁰Pb. For reactions 2 and 3, the markers are positioned at the centers of the range of allowed ⁴He energies from the decay of the $3/2^{-}$ ground-state resonance of ⁵He and the 1.8-MeV 2^+ resonance of ⁶He, respectively, calculated with PAKINE3. These distributions are approximately ± 3.0 and ± 3.7 MeV wide, respectively. The possibility of Coulomb postacceleration was neglected. These kinematic considerations are consistent with the shape of the angular distribution in Fig. 4, indicating a dominant contribution from transfer reactions to the ⁴He production mechanism.

We may make one further deduction concerning the ⁴He production. Despite being the best matched of the three transfer processes that yield ⁴He in the exit channel, the ²⁰⁸Pb(⁸He, ⁶He^{*}_{1.8} \rightarrow ⁴He + 2n)²¹⁰Pb reaction is unlikely to

TABLE II. Q values for the various processes that can lead to the production of ⁴He nuclei in the interaction of a ⁸He beam with a ²⁰⁸Pb target. Optimum Q values, Q_{opt} , calculated according to the Brink [7,8] matching rules are also given for the transfer reactions.

| Reaction | Q (MeV) | $Q_{\rm opt}$ (MeV) |
|--|---------|---------------------|
| ²⁰⁸ Pb(⁸ He, ⁴ He) ²¹² Pb | +14.99 | -1.7 |
| 208 Pb(8 He, 5 He $\rightarrow {}^{4}$ He + n) 211 Pb | +9.12 | -1.2 |
| 208 Pb(8 He, 6 He $^{*}_{1.8} \rightarrow {}^{4}$ He + 2n) 210 Pb | +5.20 | -0.8 |
| 208 Pb(8 He, 8 He $^{*} \rightarrow {}^{4}$ He + 4n) 208 Pb | -3.11 | |
| ²⁰⁸ Pb(⁸ He, ⁸ He [*] \rightarrow (⁶ He [*] _{1.8} \rightarrow ⁴ He + 2n) + 2n) ²⁰⁸ Pb | -3.94 | |

contribute significantly due to the small spectroscopic factor for the $\langle {}^{8}\text{He} | {}^{6}\text{He}_{18}^{*} + 2n \rangle$ overlap [13]. Coupled channel Born approximation (CCBA) calculations including direct transfer to both the 0^+ ground state and 1.8-MeV 2^+ excited state of ⁶He and the inelastic coupling between them bears this out, predicting negligible cross sections for hypothetical states in ²¹⁰Pb at excitation energies such that the reaction Q value is close to Q_{opt} . We may thus infer that the main production mechanisms for ⁴He are the 4n and 3n stripping reactions, preferentially populating states in the residual ²¹²Pb and ²¹¹Pb nuclei at excitation energies centered at about 17 and 10 MeV, respectively. However, it is not possible to infer anything about the details of the mechanism, i.e., whether the reactions proceed as direct, one-step transfers or sequential transfer of, e.g., two dineutron-like clusters in the case of the 4n stripping.

For the ⁶He production, Fig. 2(a) suggests that ⁶He arising from breakup are also well separated from those produced by transfers, and three-body kinematics calculations again support this, indicating that any breakup contribution to the extracted ⁶He angular distributions should be negligible, breakup being essentially confined to forward angles. The numbered arrows on Fig. 2(b) mark the energies of ⁶He ejectiles corresponding to Q_{opt} for the following reactions: (1) ²⁰⁸Pb(⁸He, ⁶He)²¹⁰Pb and (2) ²⁰⁸Pb(⁸He, ⁷He \rightarrow ⁶He + $n)^{209}$ Pb. For reaction 2, the marker is positioned at the center of the range of allowed ⁶He energies from the decay of the ⁷He $3/2^-$ ground-state resonance, again calculated with PAKINE3. The distribution is approximately ±2.0 MeV wide.

We can make some further deductions concerning the ⁶He production, although these will necessarily be more or less model dependent. The 1n stripping can be calculated rather accurately using the DWBA since the necessary spectroscopic factors are known and the reaction is well Q matched and thus most likely to be a one-step transfer process. Such

TABLE III. Q values for the various processes that can lead to the production of ⁶He nuclei in the interaction of a ⁸He beam with a ²⁰⁸Pb target. Optimum Q values, Q_{opt} , calculated according to the Brink [7,8] matching rules are also given for the transfer reactions.

| Reaction | Q (MeV) | Q _{opt} (MeV) |
|---|---------|------------------------|
| ²⁰⁸ Pb(⁸ He, ⁶ He) ²¹⁰ Pb | +7.00 | -0.8 |
| 208 Pb(8 He, 7 He $\rightarrow {}^{6}$ He + n) 209 Pb | +1.40 | -0.4 |
| ${}^{208}\text{Pb}({}^{8}\text{He}, {}^{8}\text{He}^{*} \rightarrow {}^{6}\text{He} + 2n)^{208}\text{Pb}$ | -2.14 | |

calculations were therefore performed using the code FRESCO [12], with $\langle {}^{8}\text{He} | {}^{7}\text{He} + n \rangle$ and $\langle {}^{209}\text{Pb} | {}^{208}\text{Pb} + n \rangle$ overlaps taken from Refs. [13] and [14], respectively. The following states in ²⁰⁹Pb were included: 0.0 MeV 9/2⁺, 0.78 MeV 11/2⁺, 1.42 MeV 15/2⁻, 1.57 MeV 5/2⁺, 2.03 MeV 1/2⁺, 2.49 MeV 7/2+, and 2.54 MeV 3/2+. The entrance channel optical potentials were taken from Table I of Ref. [6], with the imaginary well depth at 16 MeV increased to 50 MeV, as described in Sec. II. Since the exit channel potential is unknown, involving as it does the unbound ⁷He nucleus, the effect of employing several different choices was investigated: (1) the same parameters as in the entrance channel, (2) the global ⁶Li parameters of Cook [15], (3) the global ⁷Li parameters of Cook [15], and (4) the 16 and 22 MeV 6 He + 208 Pb parameters of Ref. [16] for the calculations at incident ⁸He energies of 16 and 22 MeV, respectively.

It was found that the cross sections calculated using these exit channel potentials all lie between two extreme values at both energies, those calculated with the entrance channel parameters (the smallest) and those calculated with the global ⁶Li parameters of Ref. [15] (the largest). The summed angular distributions for the calculations using these parameters, transformed into the laboratory reference frame, are plotted on Fig. 4 as the dashed lines with the gray areas denoting the degree of uncertainty. Note that the angular distributions are for the ⁷He particle, although given the large difference in mass between the ⁶He and neutron fragments produced by its decay the ⁶He distribution should not differ significantly. Monte Carlo calculations of the ⁶He angular distribution, similar to those performed in Ref. [17] for the single-neutron stripping and pickup reactions in the $^{7}\text{Be} + ^{58}\text{Ni}$ system, using the calculated ⁷He angular distributions as input confirm this. The mean values of the summed integrated cross sections are given in Table I with uncertainties indicating the range covered by the use of the different exit channel potentials. We thus see that 44^{+3}_{-6} % and 33 ± 7 % of the total ⁶He production cross section may be attributed to 1n stripping at ⁸He incident energies of 16 and 22 MeV, respectively, the proportion diminishing slightly (within the uncertainty) as the beam energy is increased above the Coulomb barrier. The remaining cross section must come almost exclusively from 2n stripping since, as Fig. 2(b) shows, breakup may be ruled out as a significant contributor on purely kinematic grounds.

It is also possible to estimate an upper limit for the total fusion cross section by subtracting the integrated ⁶He and ⁴He cross sections from the total reaction cross section extracted from the optical model fits to the elastic scattering angular

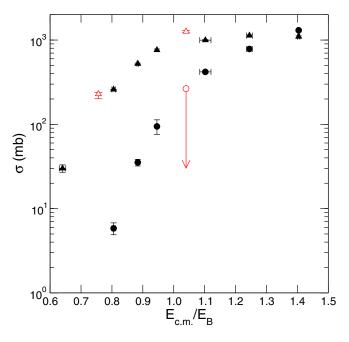


FIG. 5. Excitation functions of the fusion (filled circles) and neutron transfer (filled triangles) cross sections for the ${}^{8}\text{He} + {}^{197}\text{Au}$ system [4] compared with the present results for the upper limit on fusion (open circle) and combined ${}^{4}\text{He}$ and ${}^{6}\text{He}$ cross sections (open triangles) for the ${}^{8}\text{He} + {}^{208}\text{Pb}$ system.

distributions. Other contributions to the total reaction cross section should be small, DWBA estimates of the cross sections for inelastic scattering to the 2.60-MeV 3^- , 3.09-MeV 5^- , and 4.18-MeV 2^+ states of ²⁰⁸Pb being negligible, for example. The resulting values are given in Table I. However, the uncertainty in the value at 16 MeV is such that we cannot make any meaningful deduction concerning the fusion cross section at this energy.

We may compare our results for the ${}^{8}\text{He} + {}^{208}\text{Pb}$ system with those obtained by Lemasson *et al.* [3,4] for ${}^{8}\text{He} + {}^{197}\text{Au}$. The measured fusion and transfer excitation functions of Ref. [4] are plotted in Fig. 5, together with the upper limits on fusion and the sum of the ⁴He and ⁶He yields from this work as a function of $E_{\text{c.m.}}/E_{\text{B}}$, where E_{B} is the nominal Coulomb barrier ($E_{\text{B}} = 19.84$ MeV for ⁸He + ¹⁹⁷Au and $E_{\text{B}} =$ 20.37 MeV for ${}^{8}\text{He} + {}^{208}\text{Pb}$). In this comparison, we have used the nominal barriers since only their difference (due to the different targets) is important here. The upper limit on the fusion cross section at 22 MeV is in good agreement with the data of Lemasson et al. [4]. The sum of the ⁴He and ⁶He production cross sections agrees reasonably well with the trend of the transfer cross-section data of Ref. [4], being approximately 25% larger at both 16 and 22 MeV. This could reflect a larger 1*n*-stripping cross section for the ²⁰⁸Pb target due to the fragmentation of the single-neutron levels in ¹⁹⁸Au.

Lemasson *et al.* [3] also give model-independent lower limits on the ratio of 2n to 1n transfer cross sections, their only assumption being that any contributions to the observed ¹⁹⁸Au, ¹⁹⁹Au, and ^{198m}Au residue cross sections from 3n and 4n transfers could be neglected. We may carry out a similar exercise, although the result is necessarily model dependent

since it relies on the DWBA calculations for the 1n stripping cross sections. We further make the assumption, based on our inferences concerning the ⁴He production, that 2n stripping only contributes significantly to the ⁶He cross section so that $\sigma_{2n} = \sigma_{^{6}\text{He}} - \sigma_{1n}$. We obtain values of $\sigma_{2n}/\sigma_{1n} = 1.26^{+0.12}_{-0.31}$ and 1.98 ± 0.48 at ⁸He incident energies of 16 and 22 MeV, respectively, considerably larger than the results of Ref. [3] which range from about 0.1 to 0.3 but nevertheless compatible with them since they are *lower* limits. However, the rather large difference between our values and those of Lemasson et al. could indicate that either their assumption that contributions from 3n and 4n transfers could be neglected or our assumptions regarding 2n transfer require revision. Only full coincidence measurements, unfortunately not possible with currently available ⁸He beam intensities, will be able to provide a definitive answer.

Our results for the σ_{2n}/σ_{1n} ratio may also be compared with similar values obtained with ⁶He beams incident on heavy targets at energies close to the Coulomb barrier. A series of α neutron coincidence measurements carried out at the TwinSol facility of the University of Notre Dame for the ⁶He + ²⁰⁹Bi system [18–20] gave a value of $\sigma_{2n}/\sigma_{1n} = 2.58 \pm 0.77$ for a beam energy of 22 MeV. Standyło *et al.* [21] obtained a value of about 1.4 for the same ratio in the ⁶He + ²⁰⁶Pb system at an incident ⁶He energy of 18 MeV, although like the present result for ⁸He + ²⁰⁸Pb this is also model dependent. Both ⁶He values are fully compatible with our ⁸He results.

IV. CONCLUSIONS

The inclusive ⁴He and ⁶He yields were measured for the ${}^{8}\text{He} + {}^{208}\text{Pb}$ system at ${}^{8}\text{He}$ incident energies of 16 and 22 MeV. Employing a combination of kinematics and model calculations it was possible to draw some model-dependent but nevertheless reasonably robust conclusions as to the production mechanisms. It is clear from the discussion in the previous section that breakup can only make a small contribution to the inclusive ⁴He and ⁶He cross sections in this system at near-barrier energies. First, any breakup events seem to be kinematically rather well separated from those due to transfer processes. Second, the shapes of the angular distributions (and their evolution with increasing beam energy) are consistent with those of transfer reactions. Finally, the upper limit on the fusion cross section at 22 MeV obtained by subtracting the integrated ⁴He and ⁶He cross sections from the total reaction cross section extracted from an optical model fit to the elastic scattering data leaves little or no room for a significant breakup cross section when compared to the measured fusion cross sections for the ${}^{8}\text{He} + {}^{197}\text{Au}$ system [4].

The σ_{2n}/σ_{1n} ratios obtained from our analysis, while model dependent since they rely on calculated values for σ_{1n} , are compatible with the model-independent lower limits obtained by Lemasson *et al.* [3] for the ⁸He + ¹⁹⁷Au system. They are also compatible with the results for the ⁶He + ²⁰⁹Bi [18–20] and ⁶He + ²⁰⁶Pb [21] systems. This is consistent with the intriguing possibility that the structure of ⁸He may be represented as a ⁴He core plus two dineutron-like clusters arranged on opposite sides of the core, somewhat similar to the model proposed by Nesterov *et al.* [22]. Given that the matching

conditions for 1n and 2n stripping are similar for ⁶He and ⁸He (they are somewhat better matched for ⁸He) the cross sections should roughly scale according to the spectroscopic factors. In this simple picture, the spectroscopic factors for 1nand 2n stripping for ⁸He would both be twice those for ⁶He, since the probability of stripping either a single neutron or a dineutron-like cluster is twice as large for ⁸He as it is for ⁶He. The σ_{2n}/σ_{1n} ratio would then be the same for both projectiles, as is apparently the case. However, the reality is presumably more complicated since while the empirical spectroscopic factors for the $\langle {}^{8}\text{He} | {}^{7}\text{He} + n \rangle$ and $\langle {}^{6}\text{He} | {}^{5}\text{He} + n \rangle$ overlaps do differ by approximately a factor of 2 [23], those for the $\langle {}^{8}\text{He} | {}^{6}\text{He} + 2n \rangle$ and $\langle {}^{6}\text{He} | {}^{4}\text{He} + 2n \rangle$ are about the same [23]. The apparent similarity of the σ_{2n}/σ_{1n} ratios for the two isotopes could possibly be explained by an increased importance of two-step neutron stripping for ⁸He, but this remains to be confirmed. Also, the uncertainties in the transfer cross sections are at present still too large to draw firm conclusions. Nevertheless, it is clear that for ⁸He incident on a ²⁰⁸Pb target the breakup cross section must be considerably smaller than the values obtained for the ${}^{6}\text{He} + {}^{206}\text{Pb}$ (151) mb at 18 MeV, calculated [21]) or ${}^{6}\text{He} + {}^{209}\text{Bi} (205 \pm 65 \text{ mb})$

- G. Marquínez-Durán, I. Martel, A. M. Sánchez-Benítez, L. Acosta, R. Berjillos, J. Dueñas, K. Rusek, N. Keeley, M. A. G. Alvarez, M. J. G. Borge *et al.*, Phys. Rev. C 94, 064618 (2016).
- [2] Z. Podolyák, P. M Walker, H. Mach, G. de France, G. Sletten, F. Azaiez, J. M. Casandjian, B. Cederwall, D. M. Cullen, Zs. Dombrádi *et al.*, Nucl. Instrum. Methods Phys. Res. A **511**, 354 (2003).
- [3] A. Lemasson, A. Navin, M. Rejmund, N. Keeley, V. Zelevinsky, S. Bhattacharyya, A. Shrivastava, D. Bazin, D. Beaumel, Y. Blumenfeld *et al.*, Phys. Lett. B **697**, 454 (2011).
- [4] A. Lemasson, A. Shrivastava, A. Navin, M. Rejmund, N. Keeley, V. Zelevinsky, S. Bhattacharyya, A. Chatterjee, G. de France, B. Jacquot *et al.*, Phys. Rev. Lett. **103**, 232701 (2009).
- [5] G. Marquínez-Durán, L. Acosta, R. Berjillos, J. A. Dueñas, J. A. Labrador, K. Rusek, A. M. Sánchez-Benítez, and I. Martel, Nucl. Instrum. Methods Phys. Res. A 755, 69 (2014).
- [6] G. Marquínez-Durán, N. Keeley, K. W. Kemper, R. S. Mackintosh, I. Martel, K. Rusek, and A. M. Sánchez-Benítez, Phys. Rev. C 95, 024602 (2017).
- [7] D. M. Brink, Phys. Lett. B 40, 37 (1972).
- [8] J. L. C. Ford, Jr., K. S. Toth, G. R. Satchler, D. C. Hensley, L. W. Owen, R. M. DeVries, R. M. Gaedke, P. J. Riley, and S. T. Thornton, Phys. Rev. C 10, 1429 (1974).
- [9] C. Olmer, M. Mermaz, M. Buenerd, C. K. Gelbke, D. L. Hendrie, J. Mahoney, D. K. Scott, M. H. Macfarlane, and S. C. Pieper, Phys. Rev. C 18, 205 (1978).
- [10] K. Rusek, N. Alamanos, N. Keeley, V. Lapoux, and A. Pakou, Phys. Rev. C 70, 014603 (2004).

at 22.5 MeV, measured [20]) systems. Definitive conclusions will have to await the availability of more intense ⁸He beams than those currently available to allow multiple α or ⁶He plus neutron coincidence measurements although, as this work has shown, much can be inferred from inclusive charged-particle measurements by making physically reasonable assumptions.

ACKNOWLEDGMENTS

The authors would like to thank the staff of the GANIL accelerator facility for providing the high-quality ⁸He beam. This work was supported in part by Grants No. FPA-2010-22131-CO2-01 (FINURA) and No. FPA2013-47327-C2-1-R from the Spanish Ministry of Economy and Competitiveness, UNAM-PAPIIT IA103218 (Mexico); Grant No. N202 033637 from the Ministry of Science and Higher Education of Poland; the National Science Centre of Poland under Contracts No. 2013/08/M/ST2/00257 (LEA-COPIGAL) and No. 2014/14/M/ST2/00738 (COPIN-INFN Collaboration); and Grant No. EUI2009-04163432 (EUROGENESIS) from the European Science Foundation.

- [11] P. A. Assimakopoulos, Comput. Phys. Commun. 10, 385 (1975).
- [12] I. J. Thompson, Comput. Phys. Rep. 7, 167 (1988).
- [13] N. Keeley, F. Skaza, V. Lapoux, N. Alamanos, F. Auger, D. Beaumel, E. Becheva, Y. Blumenfeld, F. Delaunay, A. Drouart *et al.*, Phys. Lett. B 646, 222 (2007).
- [14] D. G. Kovar, N. Stein, and C. K. Bockelman, Nucl. Phys. A 231, 266 (1974).
- [15] J. Cook, Nucl. Phys. A 388, 153 (1982).
- [16] A. M. Sánchez-Benítez, D. Escrig, M. A. G. Álvarez, M. V. Andrés, C. Angulo, M. J. G. Borge, J. Cabrera, S. Cherubini, P. Demaret, J. M. Espino *et al.*, Nucl. Phys. A **803**, 30 (2008).
- [17] M. Mazzocco, D. Torresi, D. Pierroutsakou, N. Keeley, L. Acosta, A. Boiano, C. Boiano, T. Glodariu, A. Guglielmetti, M. La Commara *et al.*, Phys. Rev. C **92**, 024615 (2015).
- [18] J. P. Bychowski, P. A. DeYoung, B. B. Hilldore, J. D. Hinnefeld, A. Vida, F. D. Becchetti, J. Lupton, T. W. O'Donnell, J. J. Kolata, G. Rogachev *et al.*, Phys. Lett. B **596**, 26 (2004).
- [19] P. A. DeYoung, P. J. Mears, J. J. Kolata, E. F. Aguilera, F. D. Becchetti, Y. Chen, M. Cloughesy, H. Griffin, C. Guess, J. D. Hinnefeld *et al.*, Phys. Rev. C 71, 051601(R) (2005).
- [20] J. J. Kolata, H. Amro, F. D. Becchetti, J. A. Brown, P. A. DeYoung, M. Hencheck, J. D. Hinnefeld, G. F. Peaslee, A. L. Fritsch, C. Hall *et al.*, Phys. Rev. C 75, 031302(R) (2007).
- [21] Ł. Standylo, L. Acosta, C. Angulo, R. Berjillos, J. A. Duenas, M. S. Golovkov, N. Keeley, T. Keutgen, I. Martel, M. Mazzocco *et al.*, Phys. Rev. C 87, 064603 (2013).
- [22] A. V. Nesterov, V. S. Vasilevsky, and O. F. Chernov, Phys. At. Nucl. 64, 1409 (2001).
- [23] N. Keeley, N. Alamanos, K. W. Kemper, and K. Rusek, Prog. Part. Nucl. Phys. 63, 396 (2009).