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Search for ultrarelativistic magnetic monopoles with the Pierre Auger Observatory

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We present a search for ultrarelativistic magnetic monopoles with the Pierre Auger Observatory. Such particles, possibly a relic of phase transitions in the early universe, would deposit a large amount of energy along their path through the atmosphere, comparable to that of ultrahigh-energy cosmic rays (UHECRs). The air shower profile of a magnetic monopole can be effectively distinguished by the fluorescence detector from that of standard UHECRs. No candidate was found in the data collected between 2004 and 2012, with an expected background of less than 0.1 event from UHECRs. The corresponding 90% confidence level (C.L.) upper limits on the flux of ultrarelativistic magnetic monopoles range from 10^{-19} (cm² sr s)⁻¹ for a Lorentz factor $\gamma = 10^9$ to 2.5×10^{-21} (cm² sr s)⁻¹ for $\gamma = 10^{12}$. These results - the first obtained with a UHECR detector - improve previously published limits by up to an order of magnitude.

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I. INTRODUCTION

Maxwell's unified description of electric and magnetic phenomena is one of the greatest achievements of $19^{\rm th}$ century physics. Free magnetic charges and currents are not allowed in Maxwell's equations, a consequence of their apparent absence in Nature. On the other hand, there are essential theoretical motivations for magnetic monopoles. Their existence would naturally explain the quantization of electric charge, as first noted by Dirac [1] in 1931. Also, magnetic monopoles are required in Grand Unified Theories (GUTs), where they appear as intrinsically stable topological defects when a symmetry breaking results in a U(1) subgroup [2–4]. In typical GUT models, supermassive magnetic monopoles $(M \approx 10^{26} \text{ eV/c}^2)$ are produced in the early Universe at the phase transition corresponding to the spontaneous symmetry breaking of the unified fundamental interactions. When the original unified group undergoes secondary symmetry breaking at lower energy scales, socalled intermediate-mass monopoles (IMMs, $M \sim 10^{11} 10^{20} \text{ eV/c}^2$) may be generated. These particles, too massive to be produced at accelerators, may be present today as a cosmic-radiation relic of such early Universe transitions.

Supermassive magnetic monopoles should be gravitationally bound to the Galaxy (or to the Sun or Earth) with non-relativistic virial velocities [2–4]. Lighter magnetic monopoles can reach relativistic velocities through acceleration in coherent domains of the Galactic and intergalactic magnetic fields, as well as in astrophysical objects (e.g., neutron stars) [5, 6]. Kinetic energies of the order of 10^{25} eV have been predicted [7], which result in ultrarelativistic velocities for IMMs. Large-exposure experimental searches for magnetic monopoles are based on their velocity-dependent interactions with matter, with a wide range of velocities allowed for GUT monopoles.

There is a long history of experimental searches for magnetic monopoles with a variety of experiments such as MACRO [8], AMANDA [9], Baikal [10], SLIM [11], RICE [12], ANITA [13] and IceCube [14]. The strongest upper limit on the flux of non-relativistic magnetic monopoles $(4 \times 10^{-5} < \beta = v/c < 0.5)$ comes from the MACRO experiment at $\approx 1.5 \times 10^{-16}$ (cm² sr s)⁻¹ (90% C.L.) [8]. At relativistic velocities ($\beta \approx 0.9$), the IceCube Observatory has placed the best limit at $\approx 4 \times 10^{-18}$ (cm² sr s)⁻¹ [14]. The best limit on the flux of ultrarelativistic IMMs (Lorentz factor $\gamma \approx 10^{11}$) is reported by the ANITA-II experiment at $\approx 10^{-19}$ (cm² sr s)⁻¹ [13].

These upper limits are below the Parker bound [15] of $\sim 10^{-15} \ (\text{cm}^2 \text{ sr s})^{-1}$, which represents the largest possible magnetic-monopole flux consistent with survival of the Galactic magnetic field. However, the original Parker bound does not take into account the current knowledge of the Galactic magnetic field and its almost chaotic nature, with domain lengths in the range 1 - 10 kpc. The so-called "extended Parker bound" [16] becomes mass-dependent with $\Phi \sim 10^{-16} M/(10^{26} \text{ eV}) \ (\text{cm}^2 \text{ sr s})^{-1}$ with M the monopole mass, and is well below current experimental sensitivities (for relativistic and ultrarelativistic monopoles).

In this paper, we report a search for ultrarelativistic IMMs with data collected with the Pierre Auger Observatory between 1 December 2004 and 31 December 2012. Details of the Observatory are given in Section II. The search is motivated by the large energy deposited by ultrarelativistic IMMs along their path in the atmosphere, comparable to that of UHECRs, with a distinctive longitudinal development well-suited for detection by the fluorescence detector. The characteristics of air showers induced by IMMs are described in Section III. Simulations and event reconstruction procedures are presented in Section IV. The event selection criteria are described in Section V. The exposure, i.e., the time-integrated aperture, for the IMM search is evaluated in Section VI. Details of the data analysis and results are presented in Section VII. Conclusions are drawn in Section VIII.

II. PIERRE AUGER OBSERVATORY

The Pierre Auger Observatory [17] is the largest UHECR detector currently in operation. Located in the southern hemisphere in western Argentina, just northeast of the town of Malargüe (69°W, 35°S, 1400 m a.s.l.), it covers an area of 3000 km² with a surface-detector array (SD) [18] overlooked by a fluorescence detector (FD) [19].

The SD consists of 1660 water-Cherenkov detectors arranged in a triangular grid of 1500 m spacing, operating with a duty cycle of nearly 100%. The SD stations detect at ground level the secondary particles of the extensive air shower (EAS) produced by the UHECR primary interaction in the atmosphere. The FD detects the UV fluorescence light from nitrogen molecules excited by the EAS particles along their path in the atmosphere. Its operation is limited to clear moonless nights, resulting in a duty cycle of ~ 15% [17]. The FD consists of 24 telescopes, arranged in groups of six at four sites overlooking the SD. Each telescope has a field of view of $30^{\circ} \times 30^{\circ}$ in

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azimuth and elevation, with a 13 m^2 spherical segmented mirror collecting fluorescence light onto a 440 photomultiplier (PMT) camera. The telescope's 3.8 m^2 aperture optics are of the Schmidt design and are equipped with an annular corrector lens to minimize spherical aberration. The FD measures the longitudinal development of the UHECR shower in the atmosphere, since the fluorescence light is proportional to the energy deposited by the EAS particles [20–22]. The depth corresponding to the maximum energy deposit, X_{max} , and a calorimetric estimate of the shower energy are obtained from a fit of the shower profile. For the present analysis, we will use "hybrid" events - showers simultaneously detected by the FD and SD - which are reconstructed with superior resolution: $\sim 0.6^{\circ}$ in arrival direction, $\sim 6\%$ in energy and $\leq 20 \text{ g/cm}^2$ in X_{max} , respectively [23]. Systematic uncertainties on the energy and X_{max} are 14% [17, 24] and $\leq 10 \text{ g/cm}^2$ [23], respectively.

III. ULTRARELATIVISTIC MONOPOLE-INDUCED AIR SHOWERS

Electromagnetic interactions of magnetic monopoles have been extensively investigated [7, 25]. The electromagnetic energy loss of a magnetic monopole in air is shown in Figure 1 as a function of its Lorentz factor $\gamma = E_{\rm mon}/M$. Collisional energy loss is the dominant contribution for $\gamma \leq 10^4$. At higher Lorentz factors, pair production and photo-nuclear interactions become the main cause of energy loss. Bremsstrahlung is highly suppressed by the large monopole mass. An ultrarelativistic IMM would deposit a large amount of energy in its passage through the Earth's atmosphere, comparable to that of a UHECR. For example, a singly-charged IMM with $\gamma = 10^{11}$ loses $\approx 700 \text{ PeV}/(\text{g/cm}^2)$ (cf. Figure 1), which sums up to $\approx 10^{20.8}$ eV when integrated over an atmospheric depth of $\approx 1000 \text{ g/cm}^2$. This energy will be dissipated by the IMM through production of secondary showers initiated by photo-nuclear effects and pair productions along its path.

In order to study the characteristics of IMM-induced showers, we implemented magnetic-monopole interactions in the CORSIKA air-shower simulation software [26]. Specifically, existing subroutines for muonic collisional loss, e^+e^- -pair production and photo-nuclear interaction were appropriately modified in CONEX [27], which can be used within CORSIKA to perform a combination of stochastic particle production and numeric integration of particle cascades. We used [28, 29] to parameterize the differential cross section for e^+e^- -pair production and the Bezrukov-Bugaev parameterization [30, 31] for the photo-nuclear interaction model. To describe magnetic monopole interactions, the cross sections were scaled up by a factor z_M^2 [7, 25], where $z_M = 1/(2\alpha)$ is the singly-charged monopole charge and α is the finestructure constant. Pair production and photo-nuclear interactions were treated explicitly as stochastic pro-

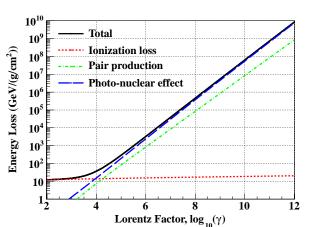


FIG. 1: Energy loss of a magnetic monopole in air as a function of its Lorentz factor γ .

cesses resulting in secondary particles produced along the monopole path in the atmosphere. Standard CONEX routines were used to simulate showers originating from these secondary particles. Collisional losses were implemented as continuous energy losses.

The longitudinal profile of the energy deposited by an ultrarelativistic IMM of $E_{\rm mon} = 10^{25}$ eV, $\gamma = 10^{11}$ and zenith angle of 70° is shown in Figure 2. When compared with a standard UHECR proton shower of energy 10^{20} eV (black solid line in Figure 2), the IMM shower presents a much larger energy deposit and deeper development, due to the superposition of many showers uniformly produced by the IMM along its path in the atmosphere. This distinctive feature will be used in our analysis, which is based on the shower development measured in the hybrid events. Also, we have confirmed this feature in case if we use other parameterizations (e.g., ALLM [32]), meaning the difference between cross sections is a second order effect for the shower profile of IMM. Depending on their energy, ultrarelativistic IMMs may traverse the Earth [13, 14] and emerge from the ground producing upwardgoing showers. We have not searched for this kind of candidate, which would not guarantee a high-quality reconstruction of the shower development.

IV. MONTE CARLO SIMULATIONS AND EVENT RECONSTRUCTION

Monte Carlo samples of ultrarelativistic IMMs were simulated for Lorentz factors in the range $\gamma = 10^8 - 10^{12}$ at a fixed monopole energy of $E_{\rm mon} = 10^{25}$ eV, because the monopole energy loss does not depend on $E_{\rm mon}$ but rather on γ in the ultrarelativistic regime of this search. While we used a fixed $E_{\rm mon}$ in the simulations, the results can be readily applied to a much larger range of monopole energies.

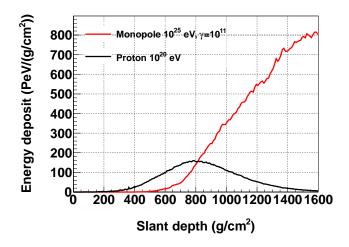


FIG. 2: Longitudinal profile of the energy deposited by an ultrarelativistic IMM of $E_{\rm mon} = 10^{25}$ eV, $\gamma = 10^{11}$ and zenith angle of 70° (red solid line). The profile of a UHECR proton shower of energy 10^{20} eV is shown as a black solid line.

To estimate the background from UHECRs, we simulated proton showers with energy $E_{\rm p}$ between 10^{18} eV and 10^{21} eV. Proton primaries are chosen to obtain a conservative estimate of the cosmic-ray background (cf. Sec. VII). We used three different models - QGSJetII-04, Sibyll 2.1 and EPOS-LHC - to account for uncertainties in the hadronic interactions. Events were simulated according to an $E_{\rm p}^{-1}$ energy spectrum, to ensure sufficient Monte Carlo statistics at the highest energy, and then appropriately weighted to reproduce the energy spectrum measured by the Pierre Auger Observatory [33].

For both the IMM and UHECR simulations, we used the CORSIKA package [26] to generate an isotropic distribution of showers above the horizon, and the Auger $\overline{\text{Offline}}$ software [34] to produce the corresponding FD and SD events. We found that the standard event reconstruction, which is optimized for UHECRs, provides equally accurate direction and longitudinal profile for ultrarelativistic IMM showers. An example of reconstructed longitudinal profile for a simulated magnetic monopole of energy 10^{25} eV and $\gamma = 10^{11}$ is shown in Figure 3 indicating the profile of the generated COR-SIKA shower (blue line) and the result of a fit of the reconstructed profile with a Gaisser-Hillas function [35] (red line). For standard UHECRs, the energy, $E_{\rm sh}$, and the depth of maximum development, X_{max} , of the shower are estimated by the integral of the fitted profile and by the position of its maximum, respectively. When applied to an ultrarelativistic IMM shower profile, the Gaisser-Hillas parameterization provides a very good fit of the portion of the profile detected in the FD field of view (cf. red and blue lines in Figure 3 in the relevant range). Also, due to the steep rising of the ultrarelativistic IMM profile, the fit systematically converges to a value of X_{max} beyond the lower edge of the FD field of view, correspond-

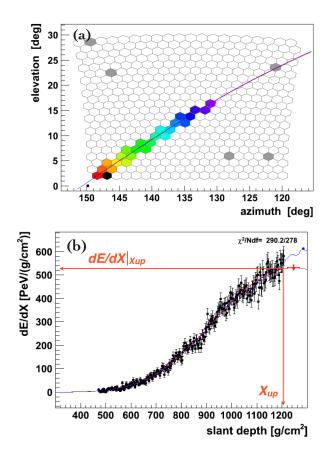


FIG. 3: Reconstructed signals for a simulated magnetic monopole of energy 10^{25} eV and $\gamma = 10^{11}$. In (a), the FD camera view is shown with color-coded timing of triggered pixels (time increases from blue to red). The red (blue) line indicates the reconstructed (simulated) shower direction projected on the camera view. In (b), the reconstructed longitudinal profile of the shower is shown. The red line is the result of a Gaisser-Hillas fit of the profile, with the red cross indicating the position of X_{max} . The blue line represents the simulated profile of the monopole shower. The selection variables X_{up} , the largest visible slant depth, and $dE/dX|_{X\text{up}}$, energy deposited at X_{up} , are also indicated.

ing to the largest visible slant depth, $X_{\rm up}$. We will use this characteristic to reject most of the standard UHECR showers, which constitute the background for this search. Since $X_{\rm max}$ of standard UHECR showers are located in FD field of view, a specific selection is required to search for the IMM profile.

V. EVENT SELECTION

We restricted our event selection to time periods with good operating conditions of the FD telescopes and welldefined calibration constants. Additional requirements were imposed on the quality of the atmosphere (aerosols and cloud coverage). Details on these data-quality criteria can be found in [23]. A total of 376,084 hybrid shower candidates were selected.

A further set of selection criteria was applied to ensure good-quality showers. We required the zenith angle of the shower to be $< 60^{\circ}$, and the distance of the shower core to the SD station with the highest signal to be less than 1500 m. The shower must be seen by at least five FD pixels over a slant depth interval of at least 200 g/cm^2 . We rejected events with gaps in their profile of more than 20% of the profile length, which could be due to telescope-border effects. The Gaisser-Hillas fit of the shower profile was required to have a $\chi^2/\text{ndf} < 2.5$, where ndf is the number of degrees of freedom. To guarantee full SD-trigger efficiency, the shower must have a minimum energy. Rather than using $E_{\rm sh}$, which is illdefined for an ultrarelativistic IMM shower, we employed the energy deposited at the largest visible slant depth $X_{\rm up}, dE/dX|_{X\rm up}$, as a discriminating variable related to the shower energy (Figure 3). The $dE/dX|_{Xup}$ is calculated by the result of the Gaisser-Hillas fit. The requirement $dE/dX|_{Xup} > 3.0 \text{ PeV}/(\text{g/cm}^2)$ is equivalent to an energy threshold of $\approx 10^{18.5} \text{ eV}$, where the SD is fully efficient. These shower-quality criteria selected a sample of well-reconstructed events, and are efficient for UHECRs as well as ultrarelativistic IMM showers.

Additional criteria for IMM selection were established from Monte Carlo simulations described in Section IV. We required X_{max} to be larger than X_{up} , which is almost always fulfilled by ultrarelativistic IMM showers. Only 6% of the UHECR proton showers of $10^{18.5}$ eV survived this cut, the fraction increasing to 32% for $10^{20.5}$ eV showers. A further reduction was obtained by appropriate constraints on the penetration of the shower and its energy deposit. To illustrate this second requirement, we show in Figure 4(a) the correlation of $dE/dX|_{Xup}$ with $X_{\rm up}$ for UHECR background events passing the showerquality criteria. When $X_{\text{max}} > X_{\text{up}}$ is required, the number of events is drastically reduced and the population becomes constrained in a much smaller region, as shown in Figure 4(b). The maximum value of X_{max} found in the UHECR proton simulated events is $\approx 1100 \text{ g/cm}^2$, which results in the X_{up} upper boundary of Figure 4(b): X_{max} is always in the FD field of view when $X_{\rm up} \gtrsim 1100 \text{ g/cm}^2$. On the other hand, the reconstructed X_{max} will always be outside the FD field of view for ultrarelativistic IMM showers, independently of the shower's $X_{\mu\nu}$. This is apparent in Figure 5, where the correlation of $dE/dX|_{Xup}$ with X_{up} is shown for ultrarelativistic IMM simulated events. The background from UHECRs is almost eliminated by excluding an appropriate region of the $(X_{up}, dE/dX|_{Xup})$ plane. We optimized the selection to achieve less than 0.1 background event expected in the data set of this search. The final requirement, $X_{\rm up} > 1080 \text{ g/cm}^2 \text{ or } dE/dX|_{X \rm up} > 150 \text{ PeV/(g/cm}^2),$ is shown in Figure 4(b) and Figure 5 as dashed boxes, and results in an expected background of 0.07 event in the search-period data set.

The selection criteria used for this search are summarized in Table I. The corresponding selection efficiency

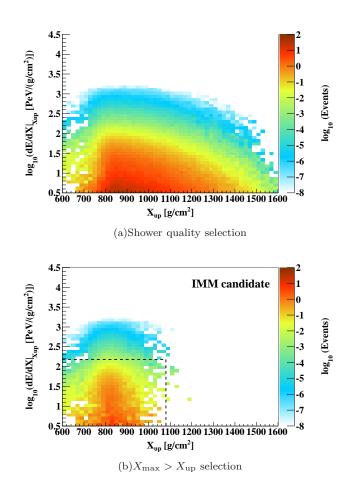


FIG. 4: Correlation of $dE/dX|_{Xup}$ with X_{up} for simulated UHECR proton showers passing the quality-selection criteria (a) and the additional requirement $X_{max} > X_{up}$ (b). The color-coded scale indicates the number of events expected in the search-period data set based on the energy spectrum measured with Auger [33]. Only events outside the dashed box in (b) are kept in the final selection for ultrarelativistic IMMs.

for ultrarelativistic IMMs ranges from 3% for $\gamma = 10^9$ to 91% for $\gamma = 10^{12}$ (see Table II).

VI. EXPOSURE

The flux Φ of ultrarelativistic IMMs of Lorentz factor γ is given by

$$\Phi(\gamma) = \frac{k}{\mathcal{E}(\gamma)},\tag{1}$$

where k is the number of events surviving the selection criteria of Table I (or an appropriate upper limit if no candidate is found), and $\mathcal{E}(\gamma)$ is the exposure, i.e., the time-integrated aperture for the hybrid detection of ul-

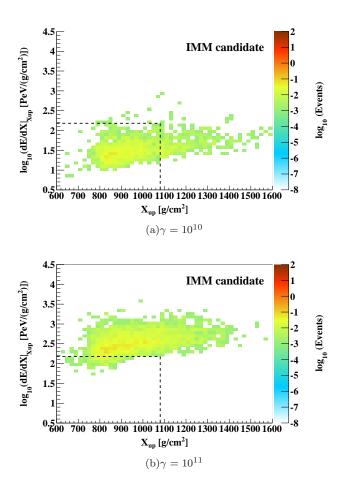


FIG. 5: Correlation of $dE/dX|_{Xup}$ with X_{up} for simulated ultrarelativistic IMM of energy 10^{25} eV and Lorentz factors $\gamma = 10^{10}$ (a) and 10^{11} (b). The color-coded scale indicates the number of events expected in the search-period data set assuming a flux of 10^{-20} (cm² sr s)⁻¹. Only events outside the dashed boxes are kept in the final selection for ultrarelativistic IMMs.

| Shower-quality selection criteria | #events | f(%) | |
|---|-------------|------|--|
| Reconstructed events | 376,084 | | |
| Zenith angle $< 60^{\circ}$ | 360,159 | 95.8 | |
| Distance from nearest SD < 1500 m | 359,467 | 99.8 | |
| Number of FD pixels > 5 | 321,293 | 89.4 | |
| Slant-depth interval $> 200 \text{ g/cm}^2$ | 205,165 | 63.9 | |
| Gaps in profile $< 20\%$ | $199,\!625$ | 97.3 | |
| profile fit $\chi^2/\text{ndf} < 2.5$ | 197,293 | 98.8 | |
| $dE/dX _{Xup} > 3.0 \text{ PeV/(g/cm}^2)$ | 6812 | 3.5 | |
| Magnetic-monopole selection criteria | | | |
| $X_{\max} > X_{up}$ | 352 | 5.2 | |
| $X_{\rm up} > 1080 \ {\rm g/cm^2} \ {\rm or}$ | | | |
| $dE/dX _{Xup} > 150 \text{ PeV/(g/cm^2)}$ | 0 | 0.0 | |

TABLE I: Event-selection criteria and data-selection results. The number of events passing each selection criterion is reported, together with the corresponding fraction of events remaining, f.

trarelativistic IMMs. The exposure is defined as [36]:

$$\mathcal{E}(\gamma) = \int_{S_{\text{gen}}} \int_{\Omega} \int_{T} \epsilon(\gamma, t, \theta, \phi, x, y) \cos \theta dS d\Omega dt, \quad (2)$$

where ϵ is the detection efficiency for an ultrarelativistic IMM of zenith angle θ and azimuth angle ϕ intersecting the ground at a position (x, y), Ω is the solid angle, S_{gen} is the area over which events are detectable, and T is the time period of the search data set.

In general, the detection efficiency ϵ changes over time, which must be taken into account in the calculation of the exposure. In fact, the effective area of the SD array and the number of operating FD telescopes grew during the Observatory installation from 2004 to 2008, and then varied due to occasional failures of the SD stations or FD telescopes. Sometimes weather conditions (e.g., wind, rain) introduced down-time in the operation of the FD. Also, the night-sky background and atmospheric conditions, such as aerosol concentration and cloud coverage, changed during data taking, which affected the sensitivity of the FD telescopes.

These effects were properly taken into account with a time-dependent detector simulation [36], which makes use of slow-control information and atmospheric measurements recorded during data taking. The detector configuration and atmospheric characteristics were changed in the simulation according to the time period T. For each Lorentz factor γ , we generated a number $N(\gamma, \cos \theta)$ of ultrarelativistic IMM showers over an area S_{gen} , with $n(\gamma, \cos \theta)$ of them fulfilling the event-selection criteria of Table I. Then the exposure given by Equation 2 was numerically evaluated:

$$\mathcal{E}(\gamma) = 2\pi \ S_{\text{gen}} \ T \ \sum_{i} \frac{n(\gamma, \cos\theta_i)}{N(\gamma, \cos\theta_i)} \ \cos\theta_i \ \Delta\cos\theta_i.$$
(3)

Table II shows the estimated hybrid exposure as a function of the IMM Lorentz factor. The exposure corresponding to the search period ranges from $\approx 100 \text{ km}^2 \text{ sr}$ yr for $\gamma = 10^9$ to ≈ 3000 km² sr yr for $\gamma \ge 10^{11}$. Several sources of systematic uncertainties were considered. The uncertainty of the on-time calculation resulted in an uncertainty of 4% on the exposure. The detection efficiency estimated through the time-dependent detector simulation depends on the fluorescence yield assumed in the simulation, on the FD shower-reconstruction methods and on the atmospheric parameters and FD calibration constants recorded during data taking. Following the procedures of [36], the corresponding uncertainty on the exposure was estimated to be 18%. To estimate the uncertainty associated with the event selection, we changed the size of the $(X_{up}, dE/dX|_{Xup})$ selection box according to the uncertainty on the two selection variables. X_{up} was changed by ± 10 g/cm², corresponding to the uncertainty on X_{max} [23], and $dE/dX|_{X_{\text{up}}}$ was changed by the uncertainty on the FD energy scale [33]. The number of selected IMM events changed by 9%, which was taken as an estimate of the uncertainty on the exposure. From the

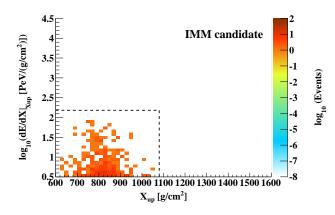


FIG. 6: Correlation of $dE/dX|_{Xup}$ with X_{up} for the data sample passing the shower-quality selection criteria and $X_{max} > X_{up}$. The color-coded scale indicates the number of events. No event is found outside the dashed box in the final selection for ultrarelativistic IMMs.

sum in quadrature of these uncertainties, a total systematic uncertainty of 21% was assigned to the exposure.

VII. DATA ANALYSIS AND RESULTS

The search for ultrarelativistic IMMs was performed following a blind procedure. The selection criteria described in Section V were optimized using Monte Carlo simulations and a small fraction (10%) of the data. This training data set was excluded from the final search period. Then the selection was applied to the full sample of data collected between 1 December 2004 and 31 December 2012. The number of events passing each of the selection criteria is reported in Table I. The correlation of $dE/dX|_{Xup}$ with X_{up} for events passing the showerquality criteria and $X_{\text{max}} > X_{\text{up}}$ is shown in Figure 6. The corresponding distributions of $dE/dX|_{Xup}$ and X_{up} are compared in Figure 7 with Monte Carlo expectations for a pure UHECR proton background, showing a reasonable agreement between data and simulations. The partial difference indicates there are heavier nuclei than protons as well. No event passed the final requirement in the $(X_{up}, dE/dX|_{Xup})$ plane, and the search ended with no candidate for ultrarelativistic IMMs.

Given the null result of the search, a 90% C.L. upper limit on the flux of ultrarelativistic IMMs, $\Phi_{90\% C.L.}$, was derived from Equation 1, with exposure $\mathcal{E}(\gamma)$ as in Table II and k = 2.44. This value of k corresponds to the Feldman-Cousins upper limit [37] for zero candidates and zero background events. We derived in Section V a background level of 0.07 event which is likely to be overestimated, since a pure proton composition was assumed while heavier nuclei appear to be a dominant component at the highest energies [23]. In fact, the fraction of deeply-penetrating showers produced by heavy nuclei is

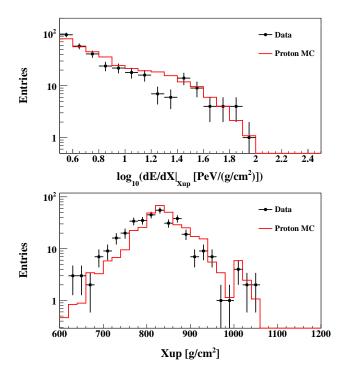


FIG. 7: Distribution of $dE/dX|_{Xup}$ (a) and X_{up} (b) for the data sample (black dots) passing the shower-quality selection criteria and $X_{max} > X_{up}$. The red solid line is the Monte Carlo prediction for a pure UHECR proton background, normalized to the number of selected events in the data.

significantly smaller resulting in fewer background events for the IMM search. Given the uncertainty in the background, we have taken a conservative approach and assumed zero background events, which provides a slightly worse limit.

In Section VI we estimated a 21% systematic uncertainty on the exposure which must be taken into account in the upper limit. Rather than following the propagation of statistical and systematic uncertainties outlined in [38], which would worsen the upper limit by a factor of 1.05, we adopted a more conservative approach and multiplied $\Phi_{90\% C.L.}$ by a factor of $f = 1 + n \times 0.21$, where n = 1.28 corresponds to the 90% C.L.

Our final 90% C.L. upper limits on the flux of ultrarelativistic IMMs are reported in Table II and shown in Figure 8, together with results from previous experiments. Following the treatment of [13], the MACRO and SLIM limits extrapolated to $\gamma \geq 10^9$ were weakened by a factor of two to account for the IMM attenuation when passing through the Earth.

Several checks of the analysis were performed. Variation of the selection criteria within reasonable ranges still resulted in no candidate. The UHECR energy spectrum was varied within its uncertainties [33], with negligible effect on the background estimation. The background for the IMM search is dominated by deeply-penetrating UHECR showers, which are found in the tail of the $X_{\rm max}$

| $\log_{10}(\gamma)$ | $\mathcal{E}(\gamma) \; (\mathrm{km}^2 \; \mathrm{sr} \; \mathrm{yr})$ | $\Phi_{90\%C.L.} (cm^2 \text{ sr s})^{-1}$ |
|---------------------|--|--|
| 8 | 1.16 | 8.43×10^{-18} |
| 9 | 9.52×10^{1} | 1.03×10^{-19} |
| 10 | 4.50×10^{2} | 2.18×10^{-20} |
| 11 | 3.15×10^{3} | 3.12×10^{-21} |
| ≥ 12 | 3.91×10^{3} | 2.51×10^{-21} |

TABLE II: Exposure and 90% C.L. upper limits on the flux of ultrarelativistic IMMs ($E_{\rm mon} = 10^{25}$ eV) for different Lorentz factors γ . A 21% Systematic uncertainty on the exposure was taken into account in the upper limits.

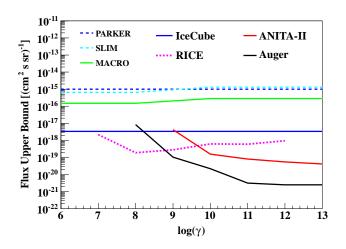


FIG. 8: 90% C.L. upper limits on the flux of ultrarelativistic IMMs: this work (black solid line); Parker bound (blue dashed line) [15]; SLIM (sky-blue dashed line) [11], MACRO (green solid line) [8], IceCube (blue solid line) [14], RICE (pink dotted line) [12] and ANITA-II (red line) [13]. The MACRO and SLIM limits above $\gamma = 10^9$ were weakened by a factor of two to account for the IMM attenuation through the Earth.

distribution and depend on the characteristics of the hadronic interactions. We used three different hadronicinteraction models (Section V) to simulate UHECR protons for background estimation. Ultrahigh-energy photons are also expected to produce deeply-penetrating showers, which may mimic an IMM event. The photon hypothesis should be carefully evaluated in case a candidate IMM is found. Since this search ended with a null result, the zero background assumption produces the most conservative limit also including the possibility of ultrahigh-energy photons. Lastly, we compared the CORSIKA energy-loss model with analytical approximations and other Monte Carlo codes [39], and found good agreement.

VIII. CONCLUSIONS

We presented the first search for magnetic monopoles ever performed with a UHECR detector, using the Pierre Auger Observatory. The particle showers produced by electromagnetic interactions of an ultrarelativistic monopole along its path through the atmosphere result in an energy deposit comparable to that of a UHECR, but with a very distinct profile which can be distinguished by the fluorescence detector. We have looked for such showers in the sample of hybrid events collected with Auger between 2004 and 2012, and no candidate was found. A 90% C.L. upper limit on the flux of magnetic monopoles was placed, which is compared with results from previous experiments in Figure 8. Ours is the best limit for $\gamma \ge 10^9$, with a factor of ten improvement for $\gamma \ge 10^{9.5}$. This result is valid for a broad class of intermediatemass ultrarelativistic monopoles ($E_{\rm mon} \approx 10^{25}$ eV and $M \sim 10^{11} - 10^{16} \text{ eV/c}^2$ which may be present today as a relic of phase transitions in the early universe. Since the background - less than 0.1 event in the current data set - is not a limiting factor in the search, the upper bound will improve with the steadily increasing exposure of the Pierre Auger Observatory.

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