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Spatial extent of the excited exciton states in WS₂ monolayers from diamagnetic shifts

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We experimentally study the radii of excitons in hBN-encapsulated WS₂ monolayers by means of magnetooptical reflectance spectroscopy at cryogenic temperatures in magnetic fields up to 29 T. We observe field-induced energy shifts of the exciton ground and excited states due to valley Zeeman and diamagnetic effects. We find the *g* factor of the first excited state of -4.2 ± 0.1 to be essentially equal to that of the ground state of -4.35 ± 0.1 . From diamagnetic shifts, we determine the root mean square radii of the excitons. The radius of the first excited state is found to be 5–8 nm and that of the ground state around 2 nm. Our results further confirm the Wannier-Mott nature of the exciton quasiparticles in monolayer semiconductors and the assignment of the optical resonances in absorption-type measurements. They also provide additional support for the applicability of the effective mass hydrogenlike models in these systems.

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I. INTRODUCTION

Transition metal dichalcogenide (TMDC) monolayers have been in the focus of solid-state physics research for several years due to their direct gap nature [1,2], efficient light-matter interaction [3,4], and intriguing spin-valley physics [5]. These phenomena are accompanied by a remarkably strong Coulomb interaction resulting from the two-dimensional (2D) quantum confinement [6,7] and weak dielectric screening in the monolayer surroundings [8–12]. One of the main consequences is the formation of highly robust, bound electron-hole pair states, or excitons, in 2D TMDCs with binding energies on the order of 0.5 eV [13,14]. The excitons were shown to dominate the optical properties of TMDCs, and it naturally motivated the question of their appropriate description.

Large binding energies in this range are commonly associated with tightly bound Frenkel-type excitons localized within a unit cell, as it is often the case in molecular crystals [15–17]. However, experimental and theoretical evidence so far points towards the applicability of a Wannier-Mott picture instead [14,18]. The latter is traditionally applied to describe spatially extended electron-hole pairs in inorganic semiconductors such as GaAs or Cu_2O [6,7,19]. One of the main findings supporting this interpretation in TMDC monolayers is the initial observation of a Rydberg-like series of resonances above the exciton ground state in the optical response. These features were attributed to higher excited states of the exciton in close analogy to the properties of inorganic bulk and quantum well systems, conceptually equivalent to a hydrogenlike model of Wannier excitons [6,7,19]. As a consequence, it became desirable to directly illustrate the spatial extent of both exciton ground and excited states in experiment and quantitatively compare the results with Wannier-based models.

An established method to directly measure the radius of an exciton is provided by studying its diamagnetic shift through magnetospectroscopy [20–22], as it has also been shown for bulk TMDCs both in the early and more recent studies [23–25]. The effect can be intuitively understood in the classical picture of a charge moving in circular motion, such as an electron around a hole, inside an external magnetic field inducing an antiparallel magnetic moment with respect to that field. In the weak-field limit, when magneto-induced effects are significantly smaller than the exciton binding energy, this leads to an energy shift of the exciton state that is quadratic in the magnetic field strength. Moreover, this change directly depends on the radius of the circular motion, i.e., on the average exciton size.

A quantum mechanical treatment of the diamagnetic shift ΔE^{dia} in 2D systems results in the following dependence on the applied out-of-plane magnetic field *B* [26–28]:

$$\Delta E_n^{\text{dia}} = \frac{e^2 \langle r_n^2 \rangle}{8\mu_{\text{eff}}} B^2 = \sigma_n B^2.$$
(1)

Here, μ_{eff} is the effective reduced mass and $\langle r_n^2 \rangle$ the mean square radius of the exciton state with the principal quantum number *n*; the elemental unit of charge is denoted by *e*. The combined parameters are commonly represented by the diamagnetic coefficient σ_n , measured in experiment. The mean square radius is defined by the radial exciton wave function $\psi_n(r)$ with the electron-hole separation *r* in 2D according to $\langle r_n^2 \rangle = \langle \psi_n | r^2 | \psi_n \rangle = 2\pi \int_0^\infty r^2 | \psi_n(r) |^2 r dr$. The root mean square (rms) radius, $\sqrt{\langle r_n^2 \rangle}$, therefore characterizes the spatial extent of the exciton. We note that an rms radius is not equivalent to the often-used concept of an exciton's Bohr radius a_B . The latter is traditionally defined for purely hydrogenic

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wave functions and corresponds to the peak in the radial probability density, that is $2\pi r |\psi_n(r)|^2$ in 2D. Moreover, for a 2D hydrogenic 1/r potential, this peak of the radial probability appears at $a_B = 1/2 \ a_{0,2D}$, where $a_{0,2D}$ is the exponential parameter in the wave function of the ground state, and the rms radius equals $\sqrt{6} \ a_B$.

For monolayer TMDCs, the diamagnetic shifts have been initially reported for the exciton ground states in WS₂ and WSe₂ systems [29–31], requiring magnetic fields of many tens of tesla due to relatively small radii in the range of 1-2 nm. The *excited* states, however, proved to be much more challenging to address due to their relatively low oscillator strengths and large broadening, the latter most probably related to spatial inhomogeneities. With respect to that, the use of encapsulation techniques with hexagonal boron nitride (hBN) resulted in significantly sharper linewidths of the excited states [32,33] and provided a more convenient spectroscopic access to their properties. However, it also stimulated alternative interpretations of the optical transitions above the energy of the ground state [34] involving coupling of excitons to the hBN phonons [34,35]. Still, only recently the observation of diamagnetic shifts of excited states was reported for the first time for WSe₂ monolayers [36].

Consequently, the main goal of the present work is to show that these physics are not limited to a single material system and can be clearly observed in a different TMDC semiconductor, both in hBN-encapsulated and in as-exfoliated samples, further supporting their general origin. In this study, we thus focus on WS₂ monolayers, which were heavily investigated in the context of exciton physics in 2D TMDCs and allowed for a clean observation of higher excited states unobstructed by the spin-split B excitons in contrast to Mo-based materials.

Using magnetoreflectance spectroscopy at liquid-helium temperature and applying large out-of-plane magnetic fields up to 29 T, we have monitored magnetoinduced energy shifts of both ground and excited state excitons in WS₂ samples. From circular-polarization-resolved data, we have independently obtained both valley Zeeman and diamagnetic effect contributions. From the analysis of the former, we found essentially equivalent g factors for the exciton ground and excited states. The latter allowed us to extract the radii of the exciton states within a realistic range of theoretically predicted effective masses according to Eq. (1). As a result, we find strong support for the applicability of the Wannier-Mott description for the excitons in TMDC monolayers and confirm the interpretation of the optical features. The comparison of our observations with the predictions of a basic effective mass theory further emphasizes the feasibility of approximate hydrogenlike models with a modified Coulomb potential to account for the main properties of the excitons in these systems.

II. EXPERIMENT

The samples under investigation were obtained from bulk crystals using mechanical exfoliation and a viscoelastic stamping technique [37] yielding monolayers of WS₂ and thin layers of hBN. The individual layers were stacked on top of each other with the WS₂ being sandwiched between two hBN sheets, as schematically shown in Fig. 1(a). A SiO₂/Si wafer was used as a substrate and also functioned as a reference for the reflectance



FIG. 1. (a) Schematic illustration of the experiment. Spectrally broadband light with right- and left-circular polarization, labeled as σ_+ and σ_- , couples to the excitons at K⁺ and K⁻ valleys, respectively. (b) (Top) Reflectance contrast of the hBN-encapsulated monolayer WS₂ measured with the SiO₂/Si substrate as a reference, including the simulated spectrum. Exciton ground and the first excited states are indicated by 1*s* and 2*s*, respectively. A closeup of the 2*s* feature is also shown in the inset. (Bottom) Corresponding first derivatives of the smoothed measured and simulated reflectance spectra.

contrast measurements. An additional nonencapsulated WS_2 monolayer, transferred directly to SiO_2/Si , was studied for comparison. The magneto-optical measurements were carried out in a resistive continuous-field magnet with fields up to 29 T. The samples were placed under He atmosphere and cooled to liquid-helium temperature. The plane of the monolayer was oriented perpendicularly to the direction of the magnetic field, corresponding to the Faraday geometry.

For the optical measurements, we used a spectrally broad incandescent white light source focused on an area of several micrometers. The reflectance spectra were taken in 1 T intervals for both right- and left-circular polarization of the reflected light during the upward field sweep (0 \rightarrow 29 T). For the detection of spectrally dispersed signals, we used a spectrometer equipped with a liquid nitrogen cooled charge-coupled-device camera. The nominal spectral resolution of the setup is 0.2 nm, corresponding to about 0.7 meV in the spectral range of the exciton resonances in WS₂. The reference measurements on the substrate were taken during the downward sweep (29 \rightarrow 0 T) to reduce the repositioning of the sample to a minimum. In the encapsulated sample, the measurements were repeated on two different positions and subsequently reproduced on one of them. Reflectance contrast R_C was then obtained from the difference of the sample reflectance R_s relative to the reference R_r according to $R_C = (R_s - R_r)/R_r$.

A typical reflectance contrast spectrum of the studied hBNencapsulated WS₂ monolayer sample in a similar experimental configuration without the magnet (i.e., at B = 0 T) is presented in the upper panel of Fig. 1(b), with the smoothed derivative shown in the lower panel. Further included are simulated spectra, obtained using a multi-Lorentzian parametrization of the exciton resonances in the dielectric function and the transfer matrix approach, assuming normal incidence conditions and equally thick top and bottom hBN layers of 10 nm height (the simulated response is found to be almost insensitive to the relative heights in this thickness range).

The ground-state and the first-excited-state resonances of the exciton at the fundamental band gap of 1L WS₂ (located at the K⁺ and K⁻ points of the hexagonal Brillouin zone and labeled as A exciton in the literature [38,39]) are centered at 2.067 and 2.208 eV, respectively. According to the hydrogenlike notation, these transitions are commonly identified as 1s and 2s states. The corresponding energy separation of about 140 meV is largely consistent with the encapsulation in the surrounding dielectric [36,40]. As further highlighted in the insets of Fig. 1(b), the 2s resonance is rather pronounced due to the linewidth being as narrow as 15 meV in contrast to typical values in as-exfoliated samples on the order of 60-90 meV. We note that higher excited states with $n \ge 3$ are not clearly observed, potentially merging into each other due to their low binding energies and overlapping with the onset of the band gap in the encapsulated samples.

III. RESULTS

The influence of the magnetic field on the peak energies of the 1s and 2s exciton resonances in the hBN-encapsulated WS_2 sample is presented in Fig. 2. First derivatives of the circularly polarized reflectance contrast are shown in a 2D intensity plot in Fig. 2(a) for magnetic fields between 0 and 29 T. In monolayer TMDCs, the right- and left-circular polarization components (σ_+) and (σ_-) of the reflected light couple to exciton resonances at the K⁺ and K⁻ valleys, respectively [5,41–44]. Corresponding spectra at selected magnetic fields are presented in Fig. 2(b). The extracted energy shifts $\Delta E_{\sigma\pm}$ relative to the respective energies E_0 at zero field are plotted in Fig. 2(c) for the 2s (top) and 1s (bottom) transitions as function of the magnetic field. Also included in Fig. 2(c) are the results from the second measurement on a different sample position with nearly equivalent overall optical response and peak energies of the 1s and 2s states. A second measurement repeated on the first position (not shown here) yielded essentially the same results.

The field-induced changes of the 1s state are predominantly the energy shifts of the σ_+ and σ_- transitions in the opposite directions, linear in magnetic field. In contrast to that, we observe a pronounced nonlinear shift to higher energies of the 2s resonance for both polarizations in addition to a linearly increasing peak separation similar to the 1s behavior. The linear component is the well-studied valley Zeeman effect in TMDC monolayers that shifts the conduction and valence bands proportionally to the magnetic field, with opposite sign for the K^+ and K^- valleys [14,45–48]. The nonlinear symmetric shift to higher energies of both polarization-resolved resonances, however, stems from the diamagnetic effect. It is very small for the ground state but is rather pronounced for the excited state due to the much larger exciton radius, as discussed further below. Similar to the observations in WSe₂ [36], it further confirms the initial assignment of the 2s resonance in the optical response to an excited excitonic state. In particular, we can exclude the proposed interpretation of this feature as a phonon-assisted transition related to the ground-state exciton [34], which should otherwise closely follow the shift of the 1s transition with magnetic field.



FIG. 2. (a) First derivatives of the reflectance contrast in the range of 1s and 2s resonances combined in a two-dimensional false color plot. The top and bottom panels show σ_{-} and σ_{+} polarization-resolved data, respectively. Dotted lines are guides to the eye for the peak energy shifts. (b) Selected reflectance contrast derivative spectra, vertically offset for clarity. Dotted lines indicate the respective resonance energies at zero field. (c) Extracted relative energy shifts of the exciton 2s (top) and 1s (bottom) resonances as function of the magnetic field. The data are shown for two different positions on the encapsulated sample. The dashed lines indicate the average shift from combined valley Zeeman and diamagnetic effects (see Fig. 3 for details).

We analyze the data quantitatively according to the model $E_{\sigma\pm}(B) = E_0 + \Delta E_{\sigma\pm} = E_0 \pm \Delta E^Z/2 + \Delta E^{\text{dia}}$ and extract the individual contributions from the valley Zeeman (ΔE^Z) and diamagnetic (ΔE^{dia}) effects by either subtracting or averaging the polarization-resolved peak energies E_{σ_+} and E_{σ_-} :

$$\Delta E^Z = E_{\sigma_+} - E_{\sigma_-},\tag{2}$$

$$\Delta E^{\text{dia}} = \frac{1}{2} (E_{\sigma_+} + E_{\sigma_-}) - E_0. \tag{3}$$

The results are presented in Figs. 3(a) and 3(b) for the Zeeman and diamagnetic components, respectively. The valley Zeeman shifts are strictly linear in magnetic field, and their magnitude is the same for both 2s and 1s states within the experimental uncertainty. They essentially follow the change of the respective quasiparticle transitions, i.e., the electronic band gap, at the K⁺ and K⁻ valleys and seem to be largely



FIG. 3. (a) Zeeman shifts for the 1s and 2s exciton states measured on two sample positions and extracted according to Eq. (2). The black line represents a g factor of -4.2. (b) Diamagnetic shifts obtained by using Eq. (3) including purely quadratic fits to the experimental results indicated by solid lines. The data from a bare, not encapsulated WS₂ sample on SiO₂/Si is shown by open circles for comparison.

independent from the different spread of the 1s and 2s exciton wave functions in reciprocal space. The corresponding g factors of $g_{1s} = -4.35 \pm 0.1$ and $g_{2s} = -4.2 \pm 0.1$ obtained from the linear fitting according to $\Delta E^Z = g\mu_B B$ (with the Bohr magneton $\mu_B = 57.9 \ \mu \text{eV T}^{-1}$) are consistent with previous measurements on WS₂ monolayers for the 1s exciton [29,30,49].

The diamagnetic shift, however, is almost an order of magnitude larger for the 2s state in comparison to the 1s transition in the studied magnetic field range. The solid lines in Fig. 3(b) correspond to purely quadratic fit curves according to Eq. (1), i.e., $\Delta E_n^{dia} = \sigma_n B^2$. The use of the weak-field model is well justified, since both the diamagnetic effect and the estimated Landau level separation for free charge carriers [20,21,36] are on the order of 10 meV at 29 T and thus far below the binding energies of the 1s and 2s excitons [14]. For the data taken at two sample positions, the fits yield the diamagnetic shift parameters of $\sigma_{1s}^{\text{pos1}} = 0.58 \pm 0.03 \,\mu\text{eV}\,\text{T}^{-2}$ and $\sigma_{1s}^{\text{pos2}} = 1.2 \pm 0.08 \,\mu\text{eV}\,\text{T}^{-2}$ for the exciton ground state. For the first excited state, we obtain $\sigma_{2s}^{\text{pos1}} = 4.9 \pm 0.14 \,\mu\text{eV}\,\text{T}^{-2}$ and $\sigma_{2s}^{\text{pos2}} = 7.9 \pm 0.22 \,\mu\text{eV}\,\text{T}^{-2}$. The combined relative shifts $\Delta E_{\sigma\pm}$ of the 1s and 2s resonances for the averaged measured values of the Zeeman and diamagnetic contributions are presented in Fig. 2(c).

We note that while the statistical errors from fitting are negligible, the deviations in the obtained values for the diamagnetic shifts are very likely to be related to systematic uncertainties in the experiment. For the 1s data, in particular, the analysis of the diamagnetic effect in the range of 0.5-1meV is rather nontrivial for the studied fields up to 29 T and is potentially the reason for the measured values being above the ones previously reported for 65 T experiments [29]. In addition to that, it is on the order of the spectral resolution of the setup, even if the detection of relative shifts is usually more sensitive than the absolute resolution. Thus, aside from the observation of the 1s shifts being very small compared to the diamagnetic shift of the 2s state, it seems reasonable to refer to studies performed in much higher magnetic fields for more accurate absolute values. In addition, considering the similarities of the optical response at the two sample positions, the two sets of data should be regarded as equivalent for the excited 2s state. The relative deviation between the two measurements is about 40% in the diamagnetic coefficient and thus roughly 20% in the estimated exciton radii discussed below due to the square root dependence of the latter.

The data for the 2*s* state obtained from the nonencapsulated WS₂ sample on SiO₂/Si substrate is presented in Fig. 3 for direct comparison. While being more noisy due to the weaker signals from larger peak broadening, it roughly follows the results for the hBN-encapsulated monolayer with respect to both valley Zeeman and diamagnetic components. It is further reasonable that the extracted diamagnetic coefficient of $3.5 \pm 0.55 \ \mu eV T^{-2}$ is found to be slightly lower than the ones for the encapsulated sample due to weaker dielectric screening and thus smaller exciton radii [31].

IV. DISCUSSION

According to Eq. (1), the diamagnetic shift is a measure for the ratio of the mean squared radius $\langle r^2 \rangle$ and the reduced effective mass μ_{eff} . As a consequence, the relation for the rms radius of the *n*th exciton state with the diamagnetic coefficient σ_n reads $r_n = \sqrt{8\mu_{\text{eff}}\sigma_n}/e$. This dependence is illustrated in Fig. 4(a) by plotting the estimated exciton radii $\sqrt{\langle r^2 \rangle}$ for the 1s and 2s states as function of the effective mass for the experimentally measured values of σ_n for the two sample positions. The corresponding colored lines thus represent the contours of constant diamagnetic shifts. For a relatively broad range of the mass parameter, the rms radii of the 1s state are on the order of 2 nm and those of the 2s exciton are found to be between 5 and 8 nm.

The reduced mass can also be estimated from the individual conduction and valence band masses m_c and m_v calculated in the single-particle picture according to $\mu_{\text{eff}} = 1/(m_c^{-1} + m_v^{-1}) = 0.15 m_0$ for WS₂ [50], with m_0 being the free electron mass. This yields rms radii of 2.0–2.9 nm for the exciton ground state and 5.8–7.4 nm for the first excited state. For comparison, the 1s radii in the nonencapsulated WS₂ monolayers on SiO₂/Si were reported to be on the order of 1.5 nm [29] and for the recent measurements of the 2s state in encapsulated WSe₂ of about 6.6 nm [36], in reasonable agreement with our findings. Here, we note that the effective masses obtained from the single-particle picture can be, in principle, further renormalized due to the interactions with photons or phonons.

Theoretically, the exciton radii in TMDCs can be calculated using effective-mass models [11,51], commonly applied to describe Wannier-Mott excitons [7]. To solve the corresponding Schroedinger equation and appropriately address the influence of the nonuniform dielectric environment on the interaction between charges, we use an approximate form for the radial



FIG. 4. (a) Estimated root mean square radii $\sqrt{\langle r_n^2 \rangle}$ from the measured values of the diamagnetic shifts of the exciton ground (1s)and first excited (2s) states as function of the reduced effective exciton mass μ_{eff} . The colored lines denote contours of constant diamagnetic shift coefficient $\sigma_n \sim \langle r_n^2 \rangle / \mu_{\text{eff}}$, according to Eq. (1), that correspond to the experimental measurements. Reasonable correspondence is obtained near the theoretically predicted effective mass of 0.15 for WS_2 , indicated by vertical line [50]. The gray lines show the rms radius of the 1s and 2s excitons in WS₂ as a function of reduced mass, calculated by solving Schroedinger's equation using the potential shown in Eq. (4). These calculations use $\epsilon_s = 4.5$ and results are shown for three different screening lengths $r_0 = 3$, 4, and 5 nm. (b) Exciton envelope wave functions of the 1s and 2s states, presented as radial probability densities $2\pi r |\psi_n(r)|^2$ depending on the electronhole separation r. (Top) Numerical solutions of the exciton problem using the thin-film Coulomb potential from Eq. (4) with $\mu_{eff} = 0.15$ $m_0, r_0 = 4$ nm, and $\epsilon_s = 4.5$. (Bottom) Illustration of the experimental results using pure 2D hydrogen wave functions [54] [Eqs. (5) and (6)] with the rms radii for 1s and 2s fixed to the average of the values from the measurements of 2.45 and 6.6 nm, respectively, for $\mu_{\rm eff} = 0.15$ m_0 . Bohr radius of the 1s state $a_{B,1s}$ (according to the definition as maximum of the radial probability) and the corresponding a_1 constant from Eq. (5) are indicated for comparison.

dependence of the thin-film Coulomb potential V(r) in the ultrathin limit [8–11,52]:

$$V(r) = -\frac{e^2}{8\epsilon_0 r_0} \left[H_0\left(\frac{\epsilon_s r}{r_0}\right) - Y_0\left(\frac{\epsilon_s r}{r_0}\right) \right]. \tag{4}$$

Here, H_0 and Y_0 are the Struve and Neumann functions. The parameter r_0 represents a characteristic length scale where the logarithmic form of the potential at short-range smoothly transforms to the more common reciprocal radial dependence at longer distances. The dielectric constant of the monolayer surroundings is denoted by ϵ_s . For the hBN-encapsulated sample, it is fixed to the value of 4.5 at optical frequencies [53], while the material constant r_0 is varied in the typical range for TMDC monolayers between 3 and 5 nm [11,52]. The results of the calculations are presented in Fig. 4(a) alongside experimental estimations for the exciton radii and predict similar spatial extent of the envelope wave functions for both ground and first excited states.

The resulting general picture of the spatial extent of the excitons in WS₂ monolayers is presented in Fig. 4(b). Here, we plot the exciton envelope wave functions of the 1s and 2s states, shown as 2D radial probability densities $2\pi r |\psi_n(r)|^2$ as a function of the electron-hole separation r. The crystal lattice of WS₂ with a lattice constant of 0.315 nm is schematically shown for comparison, matching the scaling of the x axis. In the top panel, we demonstrate the numerical solutions of the exciton problem using the thin-film Coulomb potential from Eq. (4) with $\mu_{\text{eff}} = 0.15 m_0$, $r_0 = 4$ nm, and $\epsilon_s = 4.5$. Corresponding binding energies of the 1s and 2s states are 147 and 31 meV, respectively. In the lower panel, the experimental results are illustrated using radial 2D hydrogen wave functions $\psi_n(r)$ [54] for the same effective mass of 0.15 m₀:

$$\psi_{1s}(r) \propto \exp\left(-\frac{r}{a_1}\right),$$
(5)

$$\psi_{2s}(r) \propto \left(2 - \frac{4r}{3a_2}\right) \exp\left(-\frac{r}{3a_2}\right).$$
 (6)

The parameters a_1 and a_2 in the exponential functions are deliberately chosen to obtain the root mean square radii corresponding to the average values obtained in the experiment of 2.45 and 6.6 nm for the 1s and 2s states, respectively. We note that in the 2D hydrogen model, these two parameters are equal and correspond to the 2D Bohr radius value times factor of 2, i.e., $a_1 = a_2 = 2 a_B$. In the present case, however, their values deviate from each other, highlighting the quantitative discrepancy between the *hydrogenlike* exciton physics in the studied monolayers and the *ideal* 2D hydrogen model. We note that the issue of the wave function orthogonality (for $a_1 \neq a_2$) is neglected for this illustration.

It is interesting to consider that the overall shape of the wave functions obtained from the numerical solution of the potential Eq. (4) roughly resembles the ideal 2D hydrogen model aside from rescaling and more subtle details. In addition, quantitative differences in the rms radii are further attributed to potential deviations of the calculated effective masses used for the estimations, the approximate form of the Coulomb potential, and experimental uncertainties. Similar arguments apply for the binding energies and the 1s - 2s separation, found to be slightly higher in the experiment (\approx 140 meV) in comparison to the calculated value of 116 meV for the chosen set of parameters.

Overall, our results further support the applicability of the Wannier-Mott model to describe exciton states in WS_2 monolayers. The exciton wave functions of both ground

and excited states are shown to extend over multiple lattice constants. The 2s state in particular spreads across many hundreds of individual lattice sites, when the two-dimensional representation is considered. Moreover, as highlighted by the comparison between experimental values and the results from an effective mass model, a hydrogenlike description of the exciton states modified by the thin-film Coulomb potential provides a reasonably adequate description. It captures not only the binding energies of the exciton states to a large degree as previously shown [14,52] but also their spatial extent, as we demonstrate in this work. In this respect, we emphasize that while high-level ab initio calculations remain extremely useful for an accurate microscopic description of these states with high numerical precision [12,55,56], the approximate hydrogenlike Wannier-Mott approach seems to provide an intuitive and sufficiently adequate description of the underlying physics.

V. CONCLUSIONS

In summary, we have experimentally studied the spatial extent of the exciton ground and the first excited states in WS_2 monolayers using magnetoreflectance spectroscopy and monitoring the diamagnetic shifts of the exciton resonances. The size of the exciton states was found to spread over a large number of lattice sites, i.e., several hundreds for the first excited state, in particular. We have further experimentally confirmed the applicability of the Wannier-Mott model for

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excitons in WS₂ monolayers and the assignment of the excited state resonance in hBN-encapsulated samples. Our results provide additional support for the approximate effective mass description of the exciton quasiparticles, with the main exciton parameters such as the size largely reproduced by hydrogenlike approaches. Furthermore, essentially equivalent g factors for the 1s and 2s excitons extracted from the valley Zeeman shifts indicate negligible influence of the different spread of the two states in reciprocal space on the Zeeman effect. The findings have implications with respect to the current picture of the fundamental physics of the excitons in monolayer TMDCs. They should further motivate and support future experimental and theoretical work relying on the accurate description of bound electron-hole complexes in 2D semiconductors.

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