## Anisotropic magnetic phase diagram of the Kondo-lattice compound Ce<sub>3</sub>Pd<sub>20</sub>Ge<sub>6</sub>: Observation of antiferromagnetic and quadrupolar ordering

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From the measurement of the specific heat of single crystalline samples of  $Ce_3Pd_{20}Ge_6$ , we have constructed magnetic phase diagrams for a magnetic field up to 4 T, which disclose a pronounced anisotropy along the three principal directions of [100], [110], and [111]. We have found that both the quadrupolar and antiferromagnetic ordering temperatures exhibit distinct directional dependences on the external magnetic field and that new phase transitions evolve in the antiferromagnetic phase as well as in the ordered quadrupolar phase. These facts strongly suggest the existence of a complicated form of anisotropic interaction between the electric quadrupolar moment and the magnetic dipolar moment. The present result is briefly discussed in comparison with the reported one for  $CeB_6$ . [S0163-1829(98)04913-3]

Quadrupolar ordering has been observed in several Ce-, Pr-, Tm-, and U-based compounds.<sup>1</sup> For Ce-based compounds, quadrupolar ordering has been so far observed only in compounds with a  $\Gamma_8$  quartet ground state which results from the splitting of J = 5/2 multiplet of the Ce<sup>3+</sup> ion under a cubic crystalline electric field. CeAg and CeB<sub>6</sub> are wellknown compounds with the  $\Gamma_8$  ground state: CeAg shows a ferroquadrupolar (FQ) ordering accompanied by a structural transition and a ferromagnetic ordering at 15.85 and 5.2 K, respectively,<sup>2</sup> and  $CeB_6$  is believed to exhibit an antiferroquadrupolar (AFQ) ordering at 3.3 K and an antiferromagnetic (AFM) ordering at 2.3 K under the influence of the Kondo effect.<sup>3,4</sup> The latter compound has been extensively investigated in the last decade, but still remains controversial on several points, for example, concerning the type of order parameter realized in the AFQ phase, the origin of the strong magnetic field dependence of the AFQ ordering temperature  $T_{O}$ , and the detailed interplay of the Kondo effect and quadrupolar effect. Several theories based on different models have been put forward to attempt to clarify these important questions about CeB<sub>6</sub>.<sup>5-9</sup>

Similar AFQ and AFM orderings as in CeB<sub>6</sub> have been recently proposed for another Kondo-lattice compound Ce<sub>3</sub>Pd<sub>20</sub>Ge<sub>6</sub>.<sup>10</sup> This compound crystallizes into a cubic structure of C<sub>6</sub>Cr<sub>23</sub> type with two inequivalent crystallographic sites for Ce atoms, both having a cubic symmetry  $(O_h$  and  $(T_d)$ ,<sup>11</sup> and it is an AFM Kondo-lattice compound  $(T_N)$ =0.75 K) with the  $\Gamma_8$  ground state. In addition this compound shows a phase transition around 1.2 K detected by the specific-heat measurement, whereas the magnetic susceptibility does not exhibit any anomaly there. By slightly adjusting the composition we found that this anomaly in the specific heat is strongly correlated with the one at  $T_N$ . Furthermore, the temperature dependence of the specific heat resembles very much that of CeB<sub>6</sub>. From these facts was it suggested that a quadrupolar ordering takes place around 1.2 K, as in  $CeB_6$ .<sup>10</sup>  $Ce_3Pd_{20}Ge_6$  would then provide us with a good opportunity for further investigating the interplay between the AFQ ordering and the Kondo effect, and unresolved problems concerning CeB<sub>6</sub>. We have already reported some preliminary experimental results,<sup>12</sup> but herein present more detailed experimental results exhibiting some evidence for a direct interaction between the magnetic dipolar and electric quadrupolar moments, obtained by a specific-heat measurement carried out on single-crystalline samples in external magnetic fields up to 4 T along the three principal directions of [100], [110], and [111]. We also give a brief discussion by comparing the present magnetic phase diagram with that of CeB<sub>6</sub>.

Single crystals were grown by a Czochralski pulling method either in a tetra-arc furnace for sample No. 1 or in an induction furnace for sample No. 2. The specific heat was measured by a semiadiabatic heat-pulse method in a dilution refrigerator in the temperature range between 0.1 and 6 K. Most of the measurements were carried out with sample No. 2 except for the high-field data ( $\geq 1$  T) of the [100] direction. Other characterizations about sample Nos. 1 and 2 are given in our previous report.<sup>12</sup>

Figure 1 exposes the temperature dependence of the specific heat, C(T), for several magnetic fields applied along the [100] direction. The AFM ordering temperature  $T_N$  shifts to lower temperatures with increasing magnetic field as expected for ordinary antiferromagnets, but a small peak (denoted as  $T_3$ ) sprouts below  $T_N$  around 0.5 T and outgrows the Néel peak above 0.9 T, fading out around 2 T (see the inset for B = 0.8, 0.85, and 0.9 T). It should be noted here that the nature of the transition appears to change from the mean-field type at  $T_N$  to the  $\lambda$ -type at  $T_3$ . On the other hand, the conjectured quadrupolar ordering temperature  $T_1$  slowly shifts to higher temperatures with a considerable breadth in magnetic fields. This broadening of the anomaly of C(T)contrasts with the peculiar enhancement by the magnetic field observed for CeB<sub>6</sub>.<sup>13</sup> Although several explanations have been proposed for the enhanced anomaly of C(T) for  $CeB_6$ <sup>7</sup>, it is not well understood yet. At present, we do not know the reason for the contrasted behavior of these com-

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FIG. 1. Temperature dependence of the specific heat of  $Ce_3Pd_{20}Ge_6$  in several external magnetic fields applied along the [100] direction. The origin for the ordinate is shifted by every 15 J/mol K for clarity. The inset shows the temperature dependence of the specific heat at 0.8, 0.85, and 0.9 T.

pounds, but it may be attributed to the difference in the quality of the single crystals. Other possible causes will be discussed in the following.

Similar plots of C(T) are shown in Figs. 2 and 3 for the [110] and [111] directions, respectively.  $T_N$  in both directions is gradually depressed by the magnetic field and lowered below 0.2 K above about 1.8 T. Below  $T_N$  a weaker anomaly is clearly recognized at  $T_3$  also for these directions. It should be noticed further that another phase transition denoted by  $T_2$  in the figures evolves above about 1.2 T. The anomaly at  $T_1$  broadens considerably above 1 T for both directions as for [100], and in particular the assignment of  $T_1$ along [111] becomes ambiguous around 3 T probably by the closeness to  $T_2$ . The anomaly at  $T_2$  for both directions becomes distinct above around 1.5 T and has a slight tendency to shift to higher temperatures with the magnetic field, as can be seen in Figs. 2 and 3. We finally notice that there exists a faint inflection just below  $T_2$  on the C(T) curves around 4 T, which may not, however, be considered as a distinct phase transition. At present, we do not know what all these anomalies are, although  $T_3$  has also been observed in magnetization experiments.<sup>14</sup> Neutron diffraction experiments in magnetic fields are awaited for a definitive clarification.

From the experimental results described above, the magnetic phase diagram for the three directions can be constructed as shown in Fig. 4, where we call the paramagnetic phase above  $T_1$  as phase I, the quadrupolar phases between  $T_1$  and  $T_N$  as phases II and II', and the AFM one above and below  $T_3$  as phases III and III', respectively, after the mag-

FIG. 2. Temperature dependence of the specific heat of  $Ce_3Pd_{20}Ge_6$  in several external magnetic fields applied along the [110] direction. The origin for the ordinate is shifted by every 15 J/mol K for clarity.

netic phase diagram of CeB<sub>6</sub>.<sup>3</sup> The very large anisotropic variation of  $T_N$ ,  $T_1$ ,  $T_2$ , and  $T_3$  along the three principal directions is evident, rendering the phase diagram more complex than that of  $CeB_6$ . It is pointed out here that the variation of  $T_1$  especially along [100] is not so linear as for CeB<sub>6</sub> up to 4 T and the anisotropic difference in  $T_1$  attains about 0.8 K at 4 T, which is much bigger than that for  $CeB_{6}$ .<sup>4</sup> Although the phase diagrams along [110] and [111] are qualitatively identical, the different variation of  $T_N$  with the magnetic field and the absence of  $T_2$  along [100] are particularly noteworthy, suggesting that there exists a very anisotropic interaction between the ordered magnetic dipolar moment and the electric quadrupolar moment. It is also pointed out that the appearance of the new phases II' and III' may be direct evidence for the interaction of the magnetic dipolar moment with the quadrupolar moment and it makes a sharp contrast with the phase diagram of CeB<sub>6</sub>. The AFM phase of  $CeB_6$  looks simpler than the present case.<sup>15</sup>

NMR and neutron diffraction experiments have confirmed that magnetic dipolar moments are induced in the phase II of CeB<sub>6</sub> by external magnetic fields,<sup>16,17</sup> although both results are contradictory on details. According to theories,<sup>5,8</sup> the existence of these induced magnetic dipolar moments is essential to account for some peculiar features of the magnetic phase diagram of CeB<sub>6</sub>. It is therefore important to verify whether or not magnetic dipolar moments are also induced by the external magnetic field in the phase II and/or II' of Ce<sub>3</sub>Pd<sub>20</sub>Ge<sub>6</sub>. Furthermore, we notice therein that  $T_{N[100]}$  $< T_{N[110]} \leq T_{N[111]}$  and  $T_{1[111]} \leq T_{1[100]} < T_{1[100]}$  generally



FIG. 3. Temperature dependence of the specific heat of  $Ce_3Pd_{20}Ge_6$  in several external magnetic fields applied along the [111] direction. The origin for the ordinate is shifted by every 15 J/mol K for clarity.



FIG. 4. Magnetic phase diagrams along the three principal directions of Ce<sub>3</sub>Pd<sub>20</sub>Ge<sub>6</sub>.  $T_N$ ,  $T_1$ ,  $T_2$ , and  $T_3$  are denoted by  $\bigcirc$ ,  $\spadesuit$ ,  $\times$ , and  $\triangle$ , respectively.



FIG. 5. Temperature dependence of  $S_{mag}$  per Ce ion of Ce<sub>3</sub>Pd<sub>20</sub>Ge<sub>6</sub> at 2 and 4 T applied along three principal directions.  $S_{mag}$  at 0 T is also shown for sample No. 2.

hold, i.e., "an anticorrelation" between  $T_N$  and  $T_1$  at least in low magnetic fields (<1.5 T). This fact may indicate that the exchange interaction between magnetic dipolar moments and that between electric quadrupolar moments also compete with each other in the present compound, as pointed out for CeB<sub>6</sub>.<sup>4</sup> It is interesting to note further that  $T_1$  shifts to either lower or higher temperatures below about 2 T depending on the field direction, whereas it tends to increase above 2 T where AFM ordering is suppressed in all three directions. It may be considered to be consistent with the anticorrelation between  $T_N$  and  $T_1$  just remarked above for low magnetic fields.

The temperature dependence of the magnetic entropy,  $S_{mag}(T)$ , at 0, 2, and 4 T up to 6 K is compared for the three directions in Fig. 5. Here  $S_{mag}(T)$  is deduced by subtracting C(T) of La<sub>3</sub>Pd<sub>20</sub>Ge<sub>6</sub> as the nonmagnetic part and by assuming it independent of the magnetic field.  $S_{mag}(T)$  below about 0.1 K is neglected in the calculation because of its probable irrelevance to the discussion of the ground state. All curves tend to smoothly approach toward  $R \ln 4$  up to 6 K, and so one can conclude that C(T) in a magnetic field up to 4 T shown in Figs. 1–3 really originates from the  $\Gamma_8$  quartet ground state, as concluded earlier from the zero-field data.<sup>10</sup>

Although we have just seen above that Ce<sub>3</sub>Pd<sub>20</sub>Ge<sub>6</sub> and CeB<sub>6</sub> reveal a somewhat different magnetic phase diagram, it is interesting to note that they are akin to Kondo-lattice compounds with a close Kondo temperature ( $\approx$  a few degrees kelvin) (Refs. 3, 4, and 10) and  $T_Q$  (or  $T_1$ )  $/T_N \sim 1.5$ . The fact may signify that their low-temperature properties represented by the magnetic phase diagrams are governed by

some similar mechanism. The induced magnetic dipolar moment which is observed for CeB<sub>6</sub> by neutron diffraction and NMR (Refs. 16 and 17) is the most characteristic and important fact of the AFQ phase under a magnetic field. So it is very important to verify whether such dipolar moments are also induced in Ce<sub>3</sub>Pd<sub>20</sub>Ge<sub>6</sub> and this may in turn provide useful information about the broadened anomaly at  $T_1$  in a magnetic field. In this regard, one could not neglect possible contributions from the Zeeman splitting of the  $\Gamma_8$  ground state or the Kondo effect. The measurement of C(T) or other physical properties in a magnetic field higher than 4 T will be helpful to clarify the nature of this transition.

It is recently reported that CeB<sub>6</sub> also has an anisotropic magnetic-field dependence of  $T_Q$ ,<sup>4</sup> although it is much smaller than that of  $T_1$  in Ce<sub>3</sub>Pd<sub>20</sub>Ge<sub>6</sub>. Moreover, the anisotropy seems to be reversed, i.e.,  $T_{Q[100]} < T_{Q[111]} < T_{Q[110]}$  and  $T_{N[110]} < T_{N[111]} < T_{N[100]}$  for CeB<sub>6</sub>,<sup>4</sup> while  $T_{1[111]} < T_{1[110]} < T_{1[110]} < T_{1[100]} < T_{N[110]} < T_{N[110]} < T_{N[111]}$  for Ce<sub>3</sub>Pd<sub>20</sub>Ge<sub>6</sub>, as described above. The anisotropy in both compounds seems, however, to be consistent with a picture of the competing AFM exchange interaction with the quadrupolar interaction. The difference of the anisotropy in these compounds may merely come from the difference in the crystal structure

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and/or the magnetic structure. It should be recalled that  $Ce_3Pd_{20}Ge_6$  possesses a face-centered-cubic Ce sublattice in addition to the simple cubic one in  $CeB_6$ . The magnetic structure of  $Ce_3Pd_{20}Ge_6$  should be resolved in any case for further discussions.

In summary, we have measured the C(T) of Ce<sub>3</sub>Pd<sub>20</sub>Ge<sub>6</sub>, which is a Kondo-lattice compound with AFM and quadrupolar ordering, in a magnetic field applied along [100], [110], and [111], and constructed a magnetic phase diagram which is much more complex than that of  $CeB_6$ . We found a large anisotropic magnetic-field dependence of  $T_N$  and  $T_1$ , and a new phase at lower temperatures in the AFM phase III for the three directions. For the [110] and [111] directions, we confirmed an extra new phase transition to evolve in the low-temperature region of the quadrupolar phase II. These results may be interpreted as a consequence of an interaction between the magnetic dipolar moments and the electric quadrupolar moments. It certainly needs more experiments to clarify the nature of these new phase transitions as well as the quadrupolar ordering and their relevance to the Kondo effect. A more complete version of the present work including results of magnetoresistance is planned to be published soon.

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