Flow separation effects on shoreline sediment transport

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Abstract

Field-tested numerical model simulations are used to estimate the effects of an inlet, ebb shoal, wave height, wave direction, and shoreline geometry on the variability of bathymetric change on a curved coast with a migrating inlet and strong nearshore currents. The model uses bathymetry measured along the southern shoreline of Martha's Vineyard, MA, and was validated with waves and currents observed from the shoreline to ~10-m water depth. Between 2007 and 2014, the inlet was open and the shoreline along the southeast corner of the island eroded ~200 m and became sharper. Between 2014 and 2015, the corner accreted and became smoother as the inlet closed. Numerical simulations indicate that variability of sediment transport near the corner shoreline depends more strongly on its radius of curvature (a proxy for the separation of tidal flows from the coast) than on the presence of the inlet, the ebb shoal, or wave height and direction. As the radius of curvature decreases (as the corner sharpens), tidal asymmetry of nearshore currents is enhanced, leading to more sediment transport near the shoreline over several tidal cycles. The results suggest that feedbacks between shoreline geometry and inner-shelf flows can be important to coastal erosion and accretion in the vicinity of an inlet.

1 1. Introduction

Sediment transport on shorelines is affected by wave-orbital velocities, breaking-wave-driven 2 currents, tidal currents, and inlet flows. In particular, inlet flows can interrupt alongshore 3 4 sediment transport, resulting in sediment deposition inside the bay (flood tide delta), in the ocean near the inlet mouth (ebb-tide delta or shoal) or farther offshore [1-4, references therein and 5 6 many others]. Erosion downstream of the inlet is possible owing to inlet-induced reduction in alongshore sediment supply. The inlet influence can extend for more than 10 km along the coast 7 [5], although it often extends less than 4 km [4–7]. The inlet region of influence depends on 8 9 many factors, including the geometry of the ebb shoal and main inlet channel [8], the offshore bathymetry [9,10], wave climate [11,12], tidal prism [4,13], and the presence of headlands 10 [14,15]. 11

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Traditional knowledge associates increased sediment transport around the shoreline at Wasque 13 Point on the southeast corner of Martha's Vineyard, MA, USA (Figure 1) with the opening of the 14 nearby Katama Inlet [16]. Katama Inlet breached in 2007 near the middle of Norton Point 15 (Figure 1c) and migrated east until it closed in 2015 (Figure 1d). While the inlet was open, the 16 17 shoreline near the corner of Wasque Point eroded ~200 m [Figure 1d, compare the purple curve (2014) with the blue curve (2008, similar to 2007)]. Once Norton Point extended eastward and 18 wrapped around Wasque Point, closing the inlet, the corner reverted toward its 2007 position 19 20 [Figure 1d, compare the yellow curve (2015) with the blue curve (2008)]. Here it is shown that although the erosion and subsequent accretion of the southeast corner of Martha's Vineyard is 21 consistent with a potential reduction (increase) in alongshore transport when the inlet is open 22 23 (closed), the variability of transport (magnitude of erosion plus magnitude of deposition)

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- 24 depends strongly on the radius of curvature of the corner, a proxy for flow separation, which also
- 25 may impact the shoreline evolution.



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Figure 1: (a) Location of Martha's Vineyard, MA, (b) photograph of Chappaquiddick Island, Katama Bay and Inlet, and Wasque Point in 2014 [within the yellow box in (a)], (c) Google Earth image of the Katama area 2 months after Norton Point was breached in Apr 2007, and (d) close up image of Wasque Point in 2015, with shorelines from 2008 (blue curve, similar to 2007), 2011 (green), 2014 (purple), and 2015 (yellow). Photograph in (b) by Bill Brine.

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- 33 Similar to the Martha's Vineyard coastline, many shorelines with inlets also have complex
- 34 larger-scale bathymetry and strong inner-shelf currents, including inlets throughout New
- England [17], along the U.S. Atlantic Coast [18], and on sandy coasts around the world [12,19].

36 Strong currents near headlands or sharp shoreline transitions such as Wasque Point (Figure 1) can impact sediment transport significantly. In particular, the separation of currents flowing 37 around headlands or sharp corners can generate eddies that suspend, transport, and deposit 38 39 sediment [18,20–23 and many others]. Flow separation and the generation of eddies depend on the radius of curvature of the corner (or aspect ratio of a headland) [24], the balance of bottom 40 friction and current strength, and the ratio of flow strength to local acceleration [21]. Near 41 Wasque Point, the strong ebb jet through Muskeget Channel separates from the shoreline, 42 resulting in a quiescent zone at the southeastern corner of Chappaquiddick Island (Figure 1a,b). 43 44 The evolution of the radius of curvature of Wasque Point, a primary control of flow separation, over the lifetime of Katama Inlet (Figure 1d) suggests that flow separation, in addition to the 45 inlet, could impact sediment transport at nearby shorelines. Here, field-tested numerical model 46 47 simulations are used to estimate the effects of an inlet, the ebb shoal, wave height, wave direction, and shoreline geometry on erosion and deposition along a curved coast with a 48 migrating inlet. 49

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51 **2. Numerical simulations**

Waves and currents were simulated with the numerical models SWAN (waves [25]) and Delft3D-FLOW (currents [26]). The wave model solves the spectral action balance and includes the effects of shoaling, refraction, and wave-current interaction. Similar to previous studies at this location [27], for the no-wind cases and relatively short evolution distances here, wind and nonlinear interactions were not included. The circulation model includes the effects of waves on currents through wave radiation-stress gradients, combined wave and current bed shear stress, and Stokes drift. The wave and flow models were coupled such that FLOW passes water levels
and Eulerian depth-averaged velocities to SWAN and SWAN passes wave parameters to FLOW.

SWAN was run with 36 10°-wide directional bins and 37 frequency bands logarithmically spaced between 0.03 and 1.00 Hz. The model also used a depth-limited wave breaking formulation without rollers [28], with the default value $\gamma = H_{sig}/h = 0.73$ (where the significant wave height H_{sig} is 4 times the standard deviation of sea-surface elevation fluctuations, and *h* is the water depth), and a JONSWAP bottom friction coefficient associated with wave-orbital motions set to 0.10 m²/s³ [27].

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The circulation model was run using the 13 most energetic satellite-generated tidal constituents [29] along open boundaries, which were dominated by the M2 (~80% of the variance, with small variation along the boundary) and N2 (~10% of the variance) constituents. In addition, the model used a free slip condition at closed (land) side boundaries, a spatially uniform Chezy roughness of 65 m^{0.5}/s (roughly equivalent to a drag coefficient of $C_d = 0.0023$) at bottom boundaries, and default Delft3D parameters for coupling the FLOW and WAVE models [30]. Second-order differences were used with a time step of 0.15 s for numerical stability.

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Sediment transport [31] was simulated using the modeled waves and currents. Model parameters were set to default values with a grain size of 300 μ m, except for the reference height (0.5 m), the current-related reference concentration factor (0.25), and the wave-related suspended and bed-load transport factors (0.1), which were reduced from the default values (1) that smoothed all bedforms and produced unrealistic transport around the island. Transport was averaged over several tidal cycles to remove variability within ebb or flood flows. The divergence

82 (convergence) of the transport vectors was used as a proxy for erosion (deposition), and the

83 morphology was not updated during the model run. These proxies primarily are a function of the

simulated hydrodynamics, which have been verified with field observations at this [27] and other

85 [10,32–35] shallow-water locations.

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SWAN and Delft3D-FLOW (in depth-averaged mode) were run over 4 nested grids with both 87 two-way (FLOW) and one-way nesting (SWAN). The outermost grid, with 1 km resolution, 88 89 spans about 150 km along the north and south boundaries and 100 km along the east and west boundaries. Nested in this coarse grid are finer grids of 200, 40, and 13 m resolution [27]. Using 90 higher resolution does not change simulation results significantly. Large-scale bathymetry within 91 92 the model domain was obtained during 1998 and 2008 USGS surveys (Northeast Atlantic 3 arc 93 second map [36] and Nantucket 1/3 arc second map [37]), and has horizontal resolution of 10 to 94 90 m. The bathymetry near the shoreline, inlet channel, bay, and ebb shoal near Katama Inlet was obtained each summer between 2011 and 2015 with a GPS and an acoustic altimeter 95 mounted on a jetski. The horizontal resolution of the jetski surveys is on the order of 10 m, with 96 97 finer resolution near steep features. For 2008 (similar to 2007 immediately after the inlet was breached), the location of the inlet and the geometry of the southeastern corner of 98 Chappaquiddick Island (Figure 1) were estimated from satellite images. 99 100 When initialized with frequency-directional spectra from WaveWatch III [38] along the offshore 101

boundary of the model domain, and run over the bathymetry observed in 2015, the model

simulates the currents observed near the southeastern shoreline of Chappaquiddick Island,

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including the sharp gradient from the strong ebb flows in Muskeget Channel (red in Figure 2) to
the quiescent zone of weak flows near the shoreline (blue in Figure 2). The observed currents
were estimated with an acoustic Doppler current profiler (ADCP) mounted on a small boat. Each
suite of six transects (Figure 2a and 2b) took about 2 h, during which time the tidal flows
changed (increasing ebb currents flowing from Vineyard Sound to the Atlantic), explaining some
of the discrepancies with the 1-h flow simulations.



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Figure 2. Observed (colored symbols within black outlines of the boat transects) and simulated (color contours, scale above) currents near Wasque Point during approximately (a) mid- and (b) maximum-ebb tide. If model and data agree, the colors along the transect lines match the colors of the surrounding simulation contours. The observations (13 Jul 2015) from the ADCP transects are averaged over depth and over ~10 m along the track (boat speed ~1 m/s). The simulated currents are from 1-h model runs initialized with wave and tidal conditions corresponding approximately to those observed during the middle of each ~2-h long suite of transects.

119 **3. Results and Discussion**

120 Model simulations were used to investigate the effects of the inlet, the ebb shoal, incident wave

- 121 height, incident wave direction, and the shape of the southeast corner of Chappaquiddick Island
- 122 (a proxy for flow separation) on erosion and deposition of sediment near Wasque Point. Along
- 123 the offshore boundaries the model wave field had a JONSWAP spectral shape with $H_{sig} = 1$
- 124 (representative of typical conditions in this area occurring ~70% of the time in the last decade) or

125 3 m (representative of storm events that occur ~5% of the time) and 8 s waves with a cos²⁰ 126 directional distribution centered either on shore-normal or 30° west of normal. Tides on the 127 boundaries were set to values between spring and neap. Model simulations were averaged over 128 three tidal cycles for each year with observed nearshore bathymetry (2008, 2011-2015).

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The radius of curvature of the southeast corner of Chappaquiddick Island is used as a proxy for 130 flow separation [24]. The center of the curve is at a point closest to where ebb flows begin to 131 separate from the shoreline, estimated as the location with the largest simulated cross-shore 132 velocity gradient near the corner (green circle in Figure 3a). The angles of tangents to the 133 shoreline (relative to the tangent at the center point) are calculated every 13 m on either side of 134 the center, and the slope of a least squares fit of distance as a function of angle is used as the 135 136 estimate of the radius of curvature (Figure 3b). The sum of the absolute values of total erosion and total deposition within an area +/- 400 m from the center point extending from the shoreline 137 to 2-m water depth (Figure 3c) is used as a proxy for sediment transport. The results are not 138 139 significantly different for areas that extend between +/- 200 to +/- 500 m tangential to the center and to 4-m water depth. 140

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Figure 3: (a) Color contours of elevation (relative to mean sea level, scale on right) on the southeast corner of Chappaquiddick Island near Wasque Point in 2011. The black dots are the shoreline, and the green circle is the center of the radius of curvature. (b) Distance from the center point *versus* angle of tangents to the shoreline (relative to a tangent at the center). The slope of the least squares fit (dashed line) is the radius of curvature. (c) Color contours of erosion (blue) and deposition (red) (scale on right, arbitrary units) within a region between the shoreline (black dotted curve) and 2 m depth (black dashed curve).

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151 Five scenarios were simulated for each of the 6 years with measured bathymetry. Erosion and

deposition were estimated for 1-m high normally incident waves using i) the measured

bathymetry (dark open circles in Figure 4), *ii*) the same bathymetry with the inlet artificially

154 closed (dark closed circles on Figure 4), and *iii*) with the inlet open, but the ebb-tidal delta (ebb

shoal) replaced with alongshore uniform bathymetry similar to that on either side of the shoal

156 (open squares in Figure 4). In addition, erosion and deposition were simulated for 3-m high

incident waves for each year using iv) the measured bathymetry with normally incident waves

(light open circles in Figure 4), v) the measured bathymetry with normally incident waves and

the inlet artificially closed (light closed circles, Figure 4), *vi*) the measured bathymetry with

160 waves from 30° west of normal incidence (light open diamonds in Figure 4), and *vii*) the same

bathymetry with the inlet artificially closed with waves from 30° west of normal incidence (light

162 closed diamonds in Figure 4).





Figure 4. The sum of the absolute values of simulated erosion and deposition along 400 m of 164 the shoreline between 0- and 2-m water depths (Figure 3c) versus the radius of curvature of the 165 southeastern corner of Chappaquiddick Island in each of 6 years (colors, legend in upper right). 166 Simulations used the bathymetry observed each year with the inlet open (open symbols), with the 167 inlet artificially closed (closed symbols), with normally (circles) and obliquely (30° west of 168 normal, diamonds) incident offshore wave directions, and with the ebb shoal removed artificially 169 (open squares) for incident significant wave heights of 1 (dark colors) and 3 m (light colors). 170 Inlet-open cases are not shown for 2015 because the inlet was closed. 171

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173 Although momentum from the inlet flows during ebb tide tends to enlarge the separation region a

174 few tens of meters (not shown), the simulated total erosion and deposition is not strongly

affected by closing the inlet [compare open with closed circles for each year (colors) in Figure

4]. Similarly, removing the ebb shoal (Figure 4, open squares) does not have a significant effect

- 177 on erosion and deposition, except in 2014 (Figure 4, purple symbols) when the inlet mouth and
- ebb shoal were < 0.5 km from Wasque Point (Figure 1b). Although as expected, there is more
- sediment motion with 3 m waves than with 1 m waves with the inlet open or closed (Figure 4,

compare light with dark circles), and more transport with obliquely incident waves that drive more alongshore flow (Figure 4, compare light diamonds with light circles), the differences in erosion and deposition at the corner are relatively small. In contrast, the simulated erosion and deposition depends more on changes in the radius of curvature than on the different scenarios in any year (Figure 4), suggesting that sediment transport near the shoreline is influenced more by separation from the coast of the strong Muskeget Channel ebb-tidal flows than on the presence or absence of the inlet or the ebb shoal or on the details of the incident wave field.

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The simulations further suggest that the geometry of the separation region and the intensity of 188 189 the separated jet combine to influence sediment transport at the southeast corner, and that the 190 vorticity generated at the boundary of the quiescent zone does not correlate to radii of curvature 191 or to erosion and deposition (not shown). Instead, tidally asymmetric transport is enhanced at the shoreline when the corner is sharper (smaller radius) and the ebb-tide quiescent zone is larger, 192 because sediment is mobilized during the stronger flood flows and deposited during ebb when 193 194 currents decrease. The strength of the ebb jet outside of the quiescent zone also increases when 195 the corner is sharper, allowing for more sediment motion. In 2008, 1 year after Katama Inlet formed, the radius of curvature was small and the simulations have relatively high erosion and 196 197 deposition near the shoreline (dark blue symbols in Figure 4). As the shoreline eroded between 198 2011 and 2013, the radius of curvature increased, and although the shoreline continued to erode, 199 satellite images suggest the rate slowed (not shown), consistent with the reduction in simulated 200 erosion and deposition (2011 through 2013 in Figure 4). In 2014 the inlet mouth was south 201 (rather than west) of Chappaquiddick Island (compare Figure 1b with 1c), and Norton Point had 202 extended eastward to within the separation region (Figure 1b), resulting in a greatly sharpened 203 corner (Figure 1b, purple symbols in Figure 4), and increased erosion and deposition. Between

summer 2014 (Figure 1b) and summer 2015 (Figure 1d) Norton Point extended rapidly (several
m/day from satellite and visual observations) until the inlet closed. When the Norton Point sand
spit reached the shoreline near Wasque Point in 2015, the corner was smooth (largest radius of
curvature), and erosion and deposition was smallest (yellow symbols in Figure 4), consistent
with visual observations that suggest the shoreline did not evolve significantly between 2015 and
2016.

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Although the simulations suggest erosion and deposition near the shoreline do not depend 211 212 strongly on the presence or absence of the inlet, nor on wave-driven alongshore transport, there is increased erosion downstream after the inlet opens, in contrast with a relatively stable 213 shoreline with the inlet closed (not shown). Disruption of alongshore transport or changes in 214 215 circulation when the inlet opens (e.g., the simulated tidally averaged momentum of the currents near the southeast corner of Chappaquiddick Island decreases up to 10% when the inlet is open) 216 may enhance corner erosion and impact the strength of flow separation around the corner. Field-217 218 verified simulations with evolving morphology might help determine why the shoreline starts to 219 erode when the inlet opens, and why the shoreline is stable when the inlet is closed. The 220 simulations here do not include morphological evolution. However, they suggest that erosion and deposition decrease as the curvature of the southeast corner of Chappaquiddick Island increases 221 222 and separation from the coast of the strong Muskeget Channel ebb flows decreases.

Acknowledgements and data

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