PALAEO 🚟 3

Palaeogeography, Palaeoclimatology, Palaeoecology 451 (2016) 73-83





Palaeogeography, Palaeoclimatology, Palaeoecology

journal homepage: www.elsevier.com/locate/palaeo



Late Cenozoic sea level and the rise of modern rimmed atolls

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ARTICLE INFO

Article history: Received 9 October 2015 Received in revised form 3 March 2016 Accepted 18 March 2016 Available online 23 March 2016

Keywords: Reef Coral Dissolution Late Miocene Oxygen isotope stack

ABSTRACT

Sea-level records from atolls, potentially spanning the Cenozoic, have been largely overlooked, in part because the processes that control atoll form (reef accretion, carbonate dissolution, sediment transport, vertical motion) are complex and, for many islands, unconstrained on million-year timescales. Here we combine existing observations of atoll morphology and corelog stratigraphy from Enewetak Atoll with a numerical model to (1) constrain the relative rates of subsidence, dissolution and sedimentation that have shaped modern Pacific atolls and (2) construct a record of sea level over the past 8.5 million years. Both the stratigraphy from Enewetak Atoll (constrained by a subsidence rate of ~20 m/Myr) and our numerical modeling results suggest that low sea levels (50–125 m below present), and presumably bi-polar glaciations, occurred throughout much of the late Miocene, preceding the warmer climate of the Pliocene, when sea level was higher than present. Carbonate dissolution through the subsequent sea-level fall that accompanied the onset of large glacial cycles in the late Pliocene, along with rapid highstand constructional reef growth, likely drove development of the rimmed atoll morphology we see today.

Published by Elsevier B.V.

1. Introduction

The shapes of many modern atolls have been compared to a bucket of water, with a narrow coral rim at sea level encircling a deeper central lagoon (Ladd and Tracey, 1949; Purdy and Gischler, 2005). However, much controversy surrounds which geologic process (subsidence, Darwin, 1842; dissolution, MacNeil, 1954; or sea-level variability, Daly, 1910) led to the formation of these deep lagoons, or 'emptybuckets.' Following the drilling and recovery of basalt ~1267 m below the rim of Enewetak Atoll (a.k.a, Eniwetok, Eniewetok), Marshall Islands in 1952 A.D. (Ladd and Schlanger, 1960), Darwin's theory of subsidence control, which proposes an evolution from fringing reef (Fig. 1a) to barrier reef (Fig. 1b) to empty-bucket atoll (Fig. 1c) as an ocean island ages and subsides, became widely accepted.

Although these and other drilling efforts (Buigues, 1985; Ladd et al., 1970) provide compelling evidence that atolls are built on ocean island foundations, drill-core logs and morphologic observations expose several problems with subsidence as the driver of "empty-bucket" atoll formation. For instance, lagoon sedimentation rates (typically >1 mm/yr during the Holocene \approx 1000 m/Myr; Montaggioni, 2005)

far outpace atoll subsidence rates (~15-30 m/Myr; Section 3.1) and thus lagoons would rapidly be filled in the absence of depositional hiatuses due to subaerial exposure during sea-level lowstands (Purdy and Gischler, 2005) or sediment 'leaks' due to strong currents and incomplete closure of the rim (e.g., Betzler et al., 2015; Purdy and Gischler, 2005). Rapid infilling should produce 'full-bucket' atolls typified by shallow, sediment-filled lagoons (Fig. 1d, e) that are quite common throughout the equatorial Pacific. Further, initiation of modern atoll rims in the Marshall Islands (Lincoln and Schlanger, 1991). Maldives (Schlager and Purkis, 2013 and refs. therein) and French Polynesia (Buigues, 1985) during the late Miocene suggests that other environmental forcings, not local subsidence, drive changes in atoll morphology. Widespread evidence of surface dissolution of carbonate by rainwater (e.g., subaerial erosion) on uplifted atolls led MacNeil (1954) to suggest, alternatively, that deep atoll lagoons (Fig. 1c) formed through a combination of constructional reef growth along atoll rims during interglacial sea-level highstands coupled with enhanced dissolution of lagoonal sediments during glacial lowstands.

Perhaps the most striking evidence that carbonate dissolution (or lack thereof) has driven differential changes in atoll morphology is the geographic distribution of full-buckets, empty-buckets and submerged atolls/banks (rim still catching up to sea level) in the modern Pacific (Fig. 1e). Two submerged atoll/bank provinces are located within regions of high precipitation during the last glacial maximum (Western-Pacific Warm Pool and the South Pacific Convergence Zone; ≥ 10 mm/day;

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Fig. 1. Reef types and atoll provinces of the Central Pacific. (a) Tahiti is a young ocean island in the Society Islands with immature barriers and fringing reefs. (b) Maupiti, Society Islands, has a mature barrier reef. (c) Enewetak, Marshall Islands, is an example of 'empty-bucket' atoll morphology with a deep (max \approx 62 m; Purdy and Winterer, 2001) unfilled lagoon. Cross and circle show locations of cores KAR-1 and XEN-3, respectively. (d) Kiritimati, Line Islands, is an example of 'filled-bucket' geometry with a shallow lagoon (max depth \approx 4 m) (e) Map of modeled mean annual rainfall during the last glacial maximum (LGM) based on the HadCM3M2 model (Braconnot et al., 2007), highlighting atoll provinces and islands discussed in the text. The size of each orange triangle marking a full-bucket atoll is proportional to the atoll's area to perimeter ratio (Table 1). Blue crosses show empty-bucket atolls in the central Pacific. Green circles show the position of submerged atolls as mapped by the Millennium Coral Reef Mapping Project (Andréfouët et al., 2006). (f) Schematic cross section showing main atoll morphologic, stratigraphic and process zones similar to observation of Mururoa Atoll, French Polynesia (Buigues, 1985; Camoin et al., 2001). Images in (a–d) acquired from NASA (LANDSAT-7, EO-1, MODIS and ISS, respectively).

Fig. 1e), and, therefore would be expected to experience greater potential dissolution during lowstands. In contrast, the largest full-bucket atolls often occur within the equatorial dry belt (i.e. Kiritimati and Starbuck Atolls), where rainfall and rates of dissolution are likely considerably lower (Fig. 1e). In contrast, differential thermal subsidence due to hot spot/crustal age does not offer a feasible alternative mechanism for driving development of full or empty-bucket atolls. For instance, the Marshall Islands (Eocene) and southern Tuamotus (Miocene) are morphologically similar (Fig. 1e) despite differing substantially in age, and therefore expected thermal subsidence rate (Detrick and Crough, 1978; Stein and Stein, 1992).

Preservation of marine isotope stage (MIS) 5e highstand deposits 1–2 meters above sea level (masl) on the rim of Kiritimati Atoll (Line Islands; Fig. 1d; Woodroffe and McLean, 1998) can likely also be attributed to dry conditions (Table 1). Although emergent rims in the Line Islands could result from slow atoll subsidence or uplift, a gradient in maximum rim elevation (Malden, 15 masl; Jarvis, 7 masl; Christmas, 13 masl; Fanning, 4 masl; Washington, 5 masl; Palmyra, 2 masl; Kingman Reef, 1 masl) and rainfall (Table 1) moving from atolls near the equator towards the Inter-tropical Convergence Zone (ITCZ) (Keating, 1992) northward strongly suggests that these features are dissolution, not vertical motion, derived. Atoll rims well above modern sea level are also observed on many of the Phoenix Islands (Davis, 1928; 1700 km west of the Line Islands), which straddle the equator and typically receive ~1 mm/day or less of rainfall (Table 1). Drilling efforts on modern full-bucket atolls that receive more moderate rainfall have recovered MIS 5e deposits well below the modern rim (Enewetak, 8–14 m; Tarawa, 8–14 m; Mururoa, 9–24 m; Northern Cook Islands, 18–28 m; Dickinson, 2004, and refs. therein), likely indicating substantial dissolution through those deposits. Located far from active tectonic

Table 1

Locations and characteristics of islands classified as "full-buckets" on the basis of satellite imagery.

Chain	Island	Туре	LON (dd)	LAT (dd)	Area (km ²)	Perimeter (km)	A/P (km)	Mean rainfall (mm/day)
Tuvalu	Nanumanga	Brackish	176.321	-6.287	5.9	13.0	0.5	5.1
Tuvalu	Niutao	Filled	177.343	-6.108	4.6	10.4	0.4	4.6
Tuamotu	Puka Puka	Shallow	-138.817	-14.820	21.7	24.8	0.9	3.0
Tuamotu	Tekokota	Shallow	-142.570	-17.310	10.1	15.5	0.7	5.1
Tuamotu	Tehuata	Shallow	-141.921	-16.836	6.9	13.1	0.5	4.7
Tuamotu	Nukutavake	Filled	-138.787	-19.281	8.7	17.5	0.5	4.5
Tuamotu	Pinaki	Shallow	-138.675	-19.394	4.9	10.0	0.5	4.5
Tuamotu	Akiaki	Filled	-139.213	-18.559	2.8	8.2	0.3	4.4
Tuamotu	Tepoto North	Filled	-141.430	-14.430	3.2	9.9	0.3	3.9
Phoenix	Sydney	Shallow	-171.244	-4.455	12.5	18.9	0.7	1.1
Phoenix	Enderbury	Brackish	-171.085	-3.126	9.7	17.7	0.5	0.5
Phoenix	Baker	Filled	-176.479	0.194	5.7	11.7	0.5	0.2
Phoenix	Howland	Filled	-176.618	0.808	4.5	12.0	0.4	0.6
Phoenix	Rawaki	Brackish	-170.715	-3.724	2.3	8.1	0.3	0.8
Phoenix	McKean	Brackish	-174.122	-3.596	1.7	6.3	0.3	0.8
Phoenix	Birnie	Filled	-171.516	-3.587	2.3	9.0	0.3	0.7
Marshalls	Mejit	Filled	170.870	10.287	9.6	16.5	0.6	3.6
Marshalls	Lib	Shallow/Brackish	167.380	8.314	2.4	8.1	0.3	8.8
Marshalls	Jemo	Filled	169.546	10.093	6.0	21.8	0.3	3.9
Marshalls	Kili	Filled	169.120	5.643	3.0	11.0	0.3	11.6
Marshalls	Jabat	Filled	168.977	7.754	2.5	9.4	0.3	10.2
Line	Christmas	Brackish/Shallow	- 157.381	1.871	695.8	192.0	3.6	0.6
Line	Malden	Shallow	-154.928	-4.017	43.6	40.7	1.1	0.7
Line	Starbuck	Filled/Brackish	-155.880	-5.639	35.1	36.1	1.0	2.1
Line	Washington	Brackish	-160.394	4.689	29.7	34.3	0.9	6.8
Line	Jarvis	Filled	-159.996	-0.373	6.6	12.2	0.5	0.1
Line	Flint	Filled	-151.820	-11.430	4.5	16.1	0.3	7.2
Line	Vostok	Filled	-152.310	-10.066	1.0	5.4	0.2	6.7
Gilberts	Beru	Shallow	175.983	-1.324	60.9	52.2	1.2	0.2
Gilberts	Kuria	Filled	173.396	0.251	67.7	61.4	1.1	0.4
Gilberts	Nikunau	Filled	176.452	-1.351	36.4	53.9	0.7	0.2
Gilberts	Tamana	Filled	175.984	-2.499	8.4	17.9	0.5	0.2
Gilberts	Arorae	Filled	176.820	-2.637	15.8	34.4	0.5	0.3
Cook	Nassau	Filled	-165.415	-11.561	2.6	8.3	0.3	10.9
Carolines	Fais	Filled	140.520	9.763	5.9	11.7	0.5	8.5
Carolines	Fayu	Filled	151.340	8.549	4.6	10.2	0.4	9.4
Carolines	Losiep	Filled/Shallow	139.833	9.923	8.0	18.3	0.4	8.4
Carolines	Satawal	Filled	147.034	7.382	3.7	11.2	0.3	11.7
Carolines	Gaferut	Filled/Shallow	145.384	9.229	2.0	7.2	0.3	8.8
Carolines	Nama	Filled	152.577	6.993	3.1	11.6	0.3	11.7

boundaries, only a fraction of the offset between the modern position of last inter-glacial reef deposits on these islands and maximum MIS 5e sea level (>4 masl, Kopp et al., 2013) can be attributed to thermal subsidence (Stein and Stein, 1992), suggesting relatively rapid rates of dissolution over the past ~125 kyrs.

Although simple numerical reef models (e.g., Bosence and Waltham, 1990; Chappell, 1980; Koelling et al., 2009; Paulay and McEdward, 1990) have been widely used to explore the dominant controls on the morphology of reef-bound volcanic islands during the late Pleistocene, a lack of late Miocene (and earlier) sea-level records has limited similar application to atolls. Here we use a simple numerical model to explore the most likely sea-level histories since the late Miocene (<8.5 Ma) that are consistent with observed core stratigraphy from Enewetak Atoll. We then examine the controls on modern atoll morphology (subsidence, dissolution or sea-level variability) and identify the relative process rates that have led to the formation of "empty-bucket" versus "full-bucket" atolls today and in the geologic past.

2. Materials and methods

2.1. Overview

We use a numerical box model consisting of two reservoirs, representing rim and lagoon elevations, to test the relative contributions of subsidence, dissolution and sea-level variability in determining reef form. This model is similar to, but simpler than, previous models used to study the evolution of island atoll systems (e.g., Montaggioni et al., 2015; Quinn, 1991a; Toomey et al., 2013; Warrlich et al., 2002). An overview is given here, with a more detailed description provided below (Sections 2.2–2.5).

Both elevation nodes, the rim and lagoon, experience subsidence and, additionally, erosional surface lowering from dissolution when they are subaerially exposed (defined by a typical proportion of dissolution relative to local rainfall). The carbonate accretion rate on the atoll rim decreases as water depth increases due to light attenuation (~15-30 meters below sea level-mbsl) in the water column (Bosscher and Schlager, 1992). Sediment deposited in the lagoon derives from in situ carbonate production as well as from the transport of reef material from the rim by waves. Lagoonal sedimentation only occurs when the rim is below a minimum depth allowing for free exchange of water and nutrients between the lagoon and the open ocean. In the model, in situ production occurs across the lagoon, accumulating within the lagoon box at a fixed rate independent of lagoon area; however, the flux of rim-derived, wave-transported sediment is controlled by the atoll's geometry, and vertical accumulation in the lagoon therefore depends on the ratio of lagoon area to the area of carbonate production along the atoll rim (e.g., Purdy and Winterer, 2001, and refs. therein). We assume that the footprint of each atoll remains fixed over the duration of the model run.

The model was calibrated and tested in three main steps using corelogs and bathymetry from multiple data sources: (1) rates of dissolution of the atoll rim and subsidence within the model were calibrated over the mid-late Pleistocene (<2 Ma; Fig. 2) using stratigraphy from Enewetak Atoll. (2) Markov Chain Monte Carlo methods were used to iteratively solve for the sea-level history since 8.5 Ma as well as the lagoon dissolution rate that best fit corelog stratigraphy from Enewetak



Fig. 2. Model calibration. (a) Oxygen isotope stack (Lisiecki and Raymo, 2005). δ^{18} O converted to sea level assuming typical late Pleistocene values for the ice-volume to temperature ratio (2:1) and ice-volume calibration parameters (0.10%/10 m). Red bars represent Pleistocene ice-rafted debris δ^{18} O thresholds from Bailey (2010). '100k' and '40k' world designates the change in glacial–interglacial frequency from the mid-late Pleistocene. (b) Model v. real world stratigraphy error for Enewetak's rim. The dissolution factor (F_d) represents the amount of carbonate dissolution for each mm/day of local rainfall. F_d can also be expressed as a dimensionless multiplier on the rainfall accumulated over the interval 'dt.' (c) Evaluation of subsidence and dissolution rates found along gray line in panel B required to produce submerged atolls at rainfall rates around 11.5 mm/yr. Contours represent modeled final rim elevation in meters.

Atoll (Wardlaw and Quinn, 1991) (Fig. 3). (3) Lagoon depths produced by the model for different atoll sizes and dissolution rates were compared to a dataset of real-world observations from the Gilbert, Caroline and Marshall Island chains (Fig. 4). This multi-step approach greatly increased numerical efficiency by allowing for targeted calibration of model components using specific real-world datasets described in further detail below.

2.2. Model formulation

Fig. 1f illustrates the model domain and the processes (e.g., reef accretion, subsidence, dissolution, sedimentation) that shape the elevation of the atoll lagoon and rim. Assuming the lagoon and rim maintain fixed horizontal areas (a_l and a_r respectively), the model simulates the time evolution of their surface heights z(t) from a fixed compensation depth as:

$$\frac{dz_l}{dt} = C_l(t) - E_l(t) - S \tag{1}$$

$$\frac{dz_r}{dt} = C_r(t) - E_r(t) - S \tag{2}$$

where *C* is the accumulation rate of carbonate sediment (lagoon) or reef framework (rim), *E* is the rate of vertical dissolution (subaerial

erosion) at time 't', *S* is the subsidence rate, and subscripts *r* and *l* refer to the rim and lagoon, respectively. A constant rate of subsidence, approximating long-term lithospheric cooling (Detrick and Crough, 1978; Parsons and Sclater, 1977; Stein and Stein, 1992), is applied throughout each model run (parameters used are summarized in Table 4). We relate dissolution to local rainfall using a conversion factor F_d . Rainfall for each site was linearly scaled between the Last Glacial Maximum (LGM) and Pre-Industrial rates (HadCM3M2, Braconnot et al., 2007; Gordon et al., 2000) in proportion to ice volume at time 't'. Comparison of available proxy and general circulation model data suggest HadCM3 output closely matches the pattern of rainfall change between the LGM and Pre-Industrial in the Western Tropical Pacific (DiNezio and Tierney, 2013).

Carbonate dissolution occurs when the rim, or the rim and lagoon, are exposed above sea level. Although channeling of rainwater likely leads to spatially heterogeneous dissolution across real-world rims and lagoons over any given glacial lowstand, this is likely balanced by focusing of sediment into topographic lows during subsequent interglacial flooding. Local water depth above or below the rim (d_r) is defined as.

$$d_r = SL(t) - z_r(t)$$



Fig. 3. Enewetak Atoll stratigraphy and relative sea-level history. (a) Model fit to Enewetak corelogs. Thick solid black and gray lines represent the preserved model lagoon and rim stratigraphy, respectively, run with the corrected sea-level curve shown in panel 'b'. Dashed black and gray lines show the subsidence corrected accretion and dissolution history. Thin solid black and gray lines show modeled stratigraphy generated using sea-level curve (panel c) based on δ^{18} O corrected using late Pleistocene calibration parameters only but the same subsidence and dissolution parameters as above. Black dots indicate bio-stratigraphic tie points for the KAR-1 core (bottom of lagoon) and combined XEN-3 and F-1 cores (top of rim). Unconformities in KAR-1 (lagoon) are taken from Wardlaw and Quinn (1991). (b) Best-fit model relative sea-level curve (medium gray). (c) Light gray line shows the δ^{18} O stack and its equivalent sea level using late Pleistocene calibration parameters. (d) Deep-ocean Mg/Ca temperature reconstructions from the Pacific (thin line, light gray circles) and Atlantic (thick line, dark gray circles) (LaRiviere et al., 2012; Lear et al., 2003). Dark solid lines in panels b–d show LOWESS filter (Cleveland, 1979) of the underlying data.

We compute sea level (*SL*) over millennial timescales by applying long-term deep ocean temperature (*T*) and ice volume/temperature corrections (I_c) to the $\Delta \delta^{18}$ O stack:

$$SL(t) = I_c(t) \left[\Delta \delta^{18} O(t) + T(t) \right]$$
(4)



Fig. 4. Influence of atoll size and rainfall on lagoon depth. (a) Comparison of observed spatial mean modern lagoon depth and modeled lagoon depth as a function of atoll lagoon–rim area ratio for the study atolls indicated in Table 2. (b) Plot of modeled modern lagoon depth versus mean rainfall rate and rim sediment input (for which atoll size is a proxy). Subsidence was 20 m/Myr for these model runs. For panel b rainfall was held constant.

where $\Delta \delta^{18}$ O is the difference between modern benthic δ^{18} O and the value at time *t*. *I_c* accounts for the proportion of $\Delta \delta^{18}$ O due to ice volume changes (not temperature) and a scaling factor (typically 10 m/0.1 ‰ $\Delta \delta^{18}$ O; Miller et al., 2012). Each equation is solved forward in time using an explicit finite difference approximation with a time step of 100 yr.

When the rim is submerged below sea level ($d_r < SL$), the rate of carbonate accumulation on the atoll rim (C_r) is calculated using an equation similar to Bosscher and Schlager's (1992) formulation for coral growth as a function of water depth:

$$C_r = A_{\max} \tanh\left[\frac{I_0}{I_k} \left(1 - \frac{Dm}{d}\right)e^{-kd}\right] dr \ge Dm$$

$$C_r = 0 \qquad d_r < Dm$$
(5)

where A_{max} is the maximum reef accretion rate (m/yr), I_0 is the surface light intensity (μ Em⁻² s⁻¹), k is the light extinction coefficient (m⁻¹), I_k is the saturating light intensity (μ Em⁻² s⁻¹) and D_m is the minimum depth needed for free water exchange over the rim. We use an accretion rate (A_{max}), the vertical build-up of reef framework as well as rubble/ sediment, of 5 mm/yr, in line with observations at Enewetak (Szabo et al., 1985) and throughout the Pacific (Montaggioni, 2005). While faster Holocene rates (\geq 10 mm/yr) of accretion are observed in individual drill cores at Enewetak and elsewhere (Montaggioni, 2005), such fast accretion rates would likely over-estimate the instantaneous accretion rate of the entire atoll rim. Other parameters are similar to those originally proposed by Bosscher and Meester (1992). Altogether, this equation yields high accretion rates for water depths less than 10 to 15 m, with accretion rate rapidly decreasing at greater depths.

In the model, lagoon sediment derives from in situ, primary production (*P*) and rim-transported material. A scaling factor is applied to the rim-derived sediment based on the area ratio of lagoon (a_l) to rim (a_r) (e.g., Daly, 1910; Purdy and Winterer, 2001):

$$C_l = P + R_s \frac{a_l}{a_r} d_r > D_m$$

$$C_l = 0 \quad d_r \le D_m$$
(6)

where C_i is the total lagoon sedimentation rate and R_c represents the unscaled rim-derived sediment infill rate, which we determine empirically (Section 2.5). Sedimentation does not occur when the rim exceeds a minimum depth (D_m) needed for water exchange with the lagoon, consistent with stratigraphic and field observation (Tables 3, 4). For example, none of the sedimentary sequences recovered from Enewetak's lagoon (Henry and Wardlaw, 1987; Henry et al., 1986) show evidence of deposition between MIS 5e and the Holocene, indicating that either sedimentation is minimal when the rim is exposed and the flow of ocean water into the lagoon is restricted, or lowstand lagoon sediments may be organic-rich gyttja (observed in meromictic atoll lakes today, e.g., Sachs et al., 2009) that is rapidly oxidized once exposed. By analogy, widespread hard bottom at Lake Tengano, Rennell Island (Christiansen, 1964), an uplifted, completely enclosed (rim ~100 masl) atoll in the Solomon Islands, indicates that minimal deposition occurs if the lagoon is restricted. Additionally, in the model, sediment deposition does not occur if the lagoon elevation would then exceed that of the rim. This assumes that, without the sheltering of the rim, wave stirring and associated currents across the lagoon would prevent deposition of relatively fine-grained lagoon sediment.

2.3. Atoll morphology

A dataset of morphologic characteristics was compiled for 28 atolls in the Marshall, Gilbert and Caroline chains (Table 2) from published charts as well as morphologic surveys completed as part of the Millennium Coral Reef Mapping Project (Andréfouët et al., 2006). At present, atoll lagoons across much of the Pacific remain relatively poorly mapped, so we chose to focus on these three atoll chains owing to the extensive mapping efforts archived by the UK Hydrographic Office and the National Geospatial-Intelligence Agency (US). Submerged atolls identified in Fig. 1e were drawn from the Millennium Coral Reef Mapping Project, whereas filled atolls, not including makatea islands, were identified based on subjective visual criteria using Google Earth[™] and satellite bathymetry (Robinson et al., 2000).

We followed a similar approach to Purdy and Winterer (2001)) in compiling our dataset of lagoon depths, but we only included islands with complete spatial coverage and more than 100 bathymetric soundings across the lagoon. We also excluded islands in areas of apparent past or ongoing active tectonics. Charted depths were digitized in ArcGIS (Esri, Redlands, California) in order to calculate a spatial mean depth for each atoll's lagoon. Similar to previous efforts (Purdy and Winterer, 2001), Nukuoro was excluded because its lagoon depth represents a major outlier, particularly in comparison with nearby islands (e.g., Satawan, Luknor) that have likely experienced similar environmental conditions.

2.4. Enewetak stratigraphy

A composite stratigraphy for Enewetak was compiled using existing U-series (Szabo et al., 1985), biostratigraphic (Bybell and Poore, 1991) and strontium isotope (Ludwig et al., 1988; Quinn et al., 1991) information available in the literature. In general, we followed the approach of Wardlaw and Quinn (1991) but updated the timing of identified large nanofossil datums using recent chronology (Raffi et al., 2006). Rim stratigraphy was based on three datasets: (1) core XEN-3, taken on Enjebi island as part of the EXPOE program (Couch et al., 1975), was used to constrain chronology in the upper part (0–83.8 m) of the rim while

Table 2

Compilation of empty-bucket atolls from the Marshall, Caroline and Gilbert island chains. Rainfall for each island is the average from HadCM3M2 GCM simulations for the Pre-industrial and Last Glacial Maxim (Braconnot et al., 2007). Rainfall data is available online from: https://pmip2.lsce.ipsl.fr/.

Name	Island	LON (dd)	LAT (dd)	Atoll area (km ²)	Lagoon area (km²)	Mean depth (m)	Mean rainfall (mm/day)
Marshall	Enewetak	162.227	11.501	1074.0	908.6	33.1	3.4
Marshall	Ujelang	160.894	9.824	108.5	68.2	27.1	5.4
Marshall	Bikini	165.386	11.598	749.1	633.1	38.1	2.9
Marshall	Ailuk	169.936	10.325	254.6	187.2	38.5	3.6
Marshall	Arno	171.680	7.083	461.9	342.2	36.2	10.9
Marshall	Aur	171.097	8.254	284.7	231.1	45.1	8.7
Marshall	Maleolap	171.047	8.728	1043.0	932.7	46.0	7.4
Marshall	Bikar	170.107	12.245	65.9	38.6	9.9	1.8
Marshall	Likiep	169.138	9.909	504.6	405.2	34.1	4.2
Marshall	Majuro	171.190	7.125	374.1	291.1	37.1	11.0
Marshall	Taka	169.622	11.153	147.5	96.4	33.8	2.9
Marshall	Utirik	169.791	11.259	110.4	66.6	25.8	2.8
Marshall	Taongi	168.964	14.655	122.0	74.8	5.4	1.9
Marshall	Wotje	170.021	9.450	809.5	706.5	45.2	5.5
Carolines	Ant	157.961	6.780	101.8	71.1	27.7	11.7
Carolines	Kapingmarangi	154.766	1.069	78.1	54.1	40.1	3.0
Carolines	Lamotrek	146.323	7.489	51.6	31.2	32.7	11.6
Carolines	Losap	152.701	6.878	51.3	29.6	34.9	11.8
Carolines	Lukunor	153.760	5.522	75.2	52.5	31.9	12.6
Carolines	Satawan	153.596	5.402	428.4	366.0	42.8	12.7
Carolines	Murilo	152.214	8.680	413.9	355.5	36.4	9.1
Carolines	Namonuito	150.080	8.708	2145.2	1956.6	48.8	9.3
Carolines	Nomwin	151.779	8.534	345.6	290.1	37.9	9.4
Carolines	Oroluk	155.295	7.519	476.1	415.4	47.6	11.3
Carolines	Woleai	143.867	7.353	55.3	26.1	29.7	11.6
Gilbert	Abemama	173.862	0.400	287.5	150.2	11.1	0.5
Gilbert	Butaritari	172.820	3.167	442.5	278.7	13.7	4.9
Gilbert	Tarawa	172.991	1.450	553.2	319.4	4.2	1.5

(2) cores F-1, E-1 and K-1B from the original coring of Enewetak Atoll (Ladd et al., 1953; Lincoln and Schlanger, 1987) and seismic stratigraphy from KOA crater (Folger, 1986) were used for lower sections. Lagoon stratigraphy was based on detailed ⁸⁷Sr/⁸⁶Sr measurements (Ludwig et al., 1988; Quinn et al., 1991) and biostratigraphy in core KAR-1 (Bybell and Poore, 1991) taken as part of the PEACE program (Henry and Wardlaw, 1990). Correlation between the chronometers in various boreholes is possible using local biostratigraphic indicators (Cronin et al., 1986) and unconformities (Henry et al., 1986). A summary of chronometers used in this study can be found in Table 3.

2.5. Model calibration

As a first step, we drove the model with a Pleistocene (0–2 Ma) sealevel record using a wide range of potential subsidence and rim dissolution rates, and identified the combination of these rates that produced the closest match to Enewetak Atoll rim stratigraphy over the same time interval (Table 3). We chose the 0 to 2 Ma time interval because it offers the best age control within Enewetak's stratigraphic record and because a reasonable estimate of eustatic sea level can likely be made by converting the δ^{18} O stack using late Pleistocene ice volume and temperature values (2:1 ice volume to temperature ratio and 10 m/ 0.1 ‰ $\Delta \delta^{18}$ O).

Both subsidence and dissolution can create accommodation space for reef growth. The best-fit model rim dissolution and island subsidence rates calibrated using stratigraphy from core XEN-3 (Henry and Wardlaw, 1987) therefore occur along a line (Fig. 2b) representing how lower (higher) subsidence rates are balanced in the model by higher (lower) dissolution rates to match the recorded stratigraphy. Final (t = 0) rim elevations (Fig. 2c) for combinations of possible subsidence rates and rim dissolution factors taken along this line (Fig. 2b) were then compared to observations of real world rim submergence which occur as rainfall rates approach 11.5 ± 0.9 mm/yr (Fig. 1e). After calibrating the subsidence and rim dissolution rates, a total lagoon sedimentation rate (in situ + rim derived) was estimated by running the model from deglacial flooding of the rim (~10 kyr BP) to present.

Next, we used a standard Metropolis Sampler (Chib and Greenberg, 1995; Metropolis et al., 1953) Markov Chain-Monte Carlo (MCMC) approach, to (1) determine if faster rates of lagoon sediment dissolution, relative to rim reef framework, may have contributed to the development of modern deep bucket atolls and (2) produce 1000 possible sea-level records for the past 8.5 Ma. The elevation of the lagoon, z₁

Table 3

Chronologic constraints on Enewetak stratigraphy. All tie points between cores are based on local biostratigraphic and ⁸⁷Sr/⁸⁶Sr data except for the rim KK/LL transition (275.6 mbsl), which is based on seismic reflector R90 and biostratigraphy from core KBZ-4. Stratigraphic horizons below 220 mbsl are not thought to have sustained significant deformation or subsidence during nuclear weapons testing (Folger, 1986). The 'Organic Interval,' which occurs at the JJ/KK transition in the PEACE cores was placed at the lower limit of transitional zone identified by Lincoln and Schlanger (1991), consistent with the IJ/KK transition in KBZ-4 and seismic observations (Folger, 1986).

Time (Ma)	Horizon	Biozone	Chronometers	Lagoon (mbsl)	Rim (mbsl)
0.00	Surface	AA	Surface	32.0	0.0
0.01	DIS 1	AA/BB	¹⁴ C	45.9	15.8
0.12	DIS 1	AA/BB	U-Series	45.9	15.8
0.28		BB/CC	NN21-NN20	53.5	23.3
0.45		MID. CC	U-Series, NN20-NN19	62.9	34.7
1.00		CC/DD	NN19-NN19a, ⁸⁷ Sr/ ⁸⁶ Sr	67.7	38.7
1.98	DIS 3	EE/FF	NN19a-NN18	97.8	65.5
2.51	DIS 3	EE/FF	NN17-NN16	97.8	65.5
3.81	DIS 4	FF/GG	NN16-NN14	105.4	76.2
4.13	DIS 5	GG/HH	NN14-NN13	117.1	83.8
5.09	DIS 6	HH/II	NN13-NN12	178.9	
5.56	PLIO/MIO	II/JJ	NN12-NN11	216.4	187.5
7.00	Organic Interval	JJ/KK	⁸⁷ Sr/ ⁸⁶ Sr	245.4	240.0
8.36		KK/LL	NN11-NN10	275.8	275.6

Table 4

Model parameters used in (and determined by) numerical experiments. Dissolution is calculated by multiplying amount of rainfall over time-step, ' Δ t' by the dissolution factor (*F*_d).

Parameter	Symbol	Value	Units
Timestep	dt	100	yr
Max accretion rate	G_m	0.005	m/yr
Surface light intensity	Io	2000	$\mu Em^{-2} s^{-1}$
Saturating light intensity	I_k	350	$\mu Em^{-2} s^{-1}$
Light extinction coef.	k	0.1	[]
Rim minimum depth	D_m	2	mbsl
Subsidence	S	20	m/Myr
Erosion factor (rim, lagoon)	F_d	7.5e ⁻⁵ , 10.4e ⁻⁵	[]
Primary production	Р	0.003	m/yr
Transported sediment	R _S	0.001	m/yr

(t) is not sufficiently constrained after 8.5 Ma, given Enewetak's transition to an empty-bucket atoll, to set an initial condition for the model due to the effects of post-depositional dissolution on the preserved lagoon stratigraphy, discussed further in Section 3.2. As our 'Prior,' *I*_c and *T*, the ice-volume and deep ocean temperature parameters used to convert $\Delta \delta^{18}$ O stack to sea level, were adjusted to bring Pleistocene and late Pliocene ice-rafted debris thresholds (Bailey et al., 2010; Flesche Kleiven et al., 2002) into alignment and account for a ~4-5 °C degree decrease in bottom water temperatures between the late Miocene and Pliocene (Lear et al., 2003) (linearly applied here). Lagoonal and rim dissolution factors were initially set equal. Throughout the MCMC experiment, ice volume and temperature corrections for 0 to 0.5 Ma were held at conventional late Pleistocene values (~2:1 ice volume to temperature; 10 m/0.1 $\& \Delta \delta^{18}$ O) and a maximum mid-Pliocene Warm Period highstand (2.9-3.2 Ma) between 12 and 32 masl (Miller et al., 2012) was enforced due to an unconformity in the Enewetak section over the late Pliocene (Fig. 3a).

An initial simulation (Run₀) was run using the above constraints for the lagoon dissolution rate (F_{dl}) , as well as assumed ice volume (I_c) and deep-ocean temperature (T) corrections (independently defined at 2 Myr intervals) for converting the benthic $\Delta\delta^{1\bar{8}}O$ stack (e.g., Lisiecki and Raymo, 2005; Zachos et al., 2001) to sea level (Eq. 3). A fit $(X_{Run_0}^2)$ between the resulting model stratigraphy and published core accumulation histories from Enewetak Atoll (Fig. 3a; Table 3) (Wardlaw and Quinn, 1991) was then evaluated using a cost function which takes a form similar to the chi-squared test statistic. Next, we proposed a new set of values for the parameters above (F_{dl}, I_c, T) randomly drawn from a fixed search distance from their current values and, again, ran the model (Run_1) to produce a new synthetic corelog stratigraphy. The newly proposed parameters (Run_1) were accepted for: (1) combinations that produced a better fit to corelog stratigraphy than the parameters from the last 'accepted' iteration or (2) the exponential change in the fit exceeded a random number drawn from a uniform distribution (0,1). Accepted parameters were saved and a new set proposed. Repeated many times (n runs), the model minimizes the cost and identifies a range of parameter combinations that produce stratigraphy closely matching Enewetak's.

Next, we compared lagoon depths produced by the model for islands of different size to an observational dataset of atoll bathymetric surveys from the western Pacific Ocean (n = 28; Table 2). Study atolls span a range of sizes (26 to 1957 km²) and rainfall regimes (1.7 to 12.7 mm/day mean rainfall), are well mapped and located far from active tectonic boundaries. For each modeled island, we used the best-fit subsidence, dissolution (scaled for local rainfall) and sea-level parameters from the 1000 sets produced in the experiments described above. We split the observational dataset from the western Pacific Ocean into two groups, first, using the Caroline and Gilbert Islands (n = 13) to calculate the relative contribution of primary (P) v. rim-derived (R_s) contribution to the total sedimentation rate used for modeling Enewetak stratigraphy above. Observations from the Marshall Islands (n = 14, excluding Enewetak) were then compared to model-generated lagoon depths to provide an overall, independent test of the model formulation. Altogether, this process yields two key results: a relative sea-level (RSL) curve extending from the late Miocene to the present (Fig. 3b) and a simple, calibrated, atoll formation model.

3. Results and discussion

3.1. Subsidence and rim dissolution rates

Stratigraphic and morphologic constraints on the model, outlined above (Section 2.5), suggest an island subsidence rate around 20.0 m/ Myr for Enewetak Atoll, consistent with findings by previous authors. For example, basalt dated to 56.4 \pm 5 Ma (Kulp, 1963; Lincoln and Schlanger, 1991) recovered from 1267 m below Enewetak's rim (Ladd and Schlanger, 1960) suggests a long-term mean subsidence rate between ~20.6 and 24.6 m/Myr. Plate cooling models (Stein and Stein, 1992) predict a subsidence rate of 14–18 m/Myr over the past 8.5 Ma for Enewetak, assuming thermal reset of the crust during island formation (Detrick and Crough, 1978; Li et al., 2004). Likewise, a mean subsidence rate of 19.5 m/Myr since the late Cretaceous can be estimated from cores drilled on Wodejebato guyot (submerged 1485 mbsl), 250 km east of Enewetak (Larson et al., 1995). In general, long-term subsidence rates of western Pacific Ocean guyots (drowned atolls) drilled as part of ODP Leg 144 range from 15.8 to 29.0 m/Myr (Larson et al., 1995).

The best-fit modeled rim dissolution factor (F_{dr}) , a dimensionless multiplier on local rainfall used to calculate dissolution is 7.5×10^{-5} (or 27.5 m/Myr of vertical dissolution for each mm/day of rainfall). Fast rim dissolution (~93.5 m/Myr) relative to subsidence (20 m/Myr) at Enewetak (mean rainfall = 3.4 mm/day) is consistent with the scarcity of subaerial exposure horizons preserved in corelogs (KAR-1, 9 subaerial erosion horizons of Pleistocene age; Quinn, 1991b) relative to the much larger number depositional units that must have been produced (and presumably eroded through; Fig. 3a) over the course of the many (~50) Pleistocene glacial/interglacial sea-level cycles indicated by the benthic δ^{18} O stack (Lisiecki and Raymo, 2005, Fig. 2a). Subsequent dissolution through previously deposited interglacial units and variable highstand amplitude are recognized to cause 'missing beats' in shallow water carbonate successions (Eberli, 2013), behaviors captured by our model. Our modeled rim dissolution factor also falls between estimates for Majuro (9.3×10^{-5}) and Enewetak (3.9×10^{-5}) based on contemporary hydrologic observations in the Marshall Islands (Anthony et al., 1989). Sub-soil micro-erosion measurements on Grand Cayman Island (0.27–0.06 mm/yr) (Spencer, 1985), a potential modern analog to down-wearing during glacial-interglacial cycles, yield F_d values between 5.7×10^{-5} and 25.7×10^{-5} . On longer timescales, Purkis et al. (2010)) found similar dissolution rates ($F_d \sim 6.0 \times 10^{-5}$) were needed to form Pleistocene karst landforms observed along the Red Sea and Arabian Gulf coasts. The mean dissolution factor calculated using cosmogenic denudation rates of MIS 5e and older corals from Barbados (Lal et al., 2005), a raised, mostly carbonate island, is 5.7×10^{-5} assuming mean rainfall of 2.3 mm/day (HadCM3M2: LGM, Pre-Industrial; Braconnot et al., 2007).

3.2. Late Miocene to present sea-level variability

In general, the best-fit reconstructed relative sea-level curve derived from the model corrected δ^{18} O stack and published drill core stratigraphy for Enewetak Atoll (Section 2.3) shows consistently low sea level throughout the late Miocene, followed by a peak in sea level during the Pliocene and a subsequent fall moving into the Pleistocene (Fig. 3b).

Beyond the numerical modeling results, basic dimensional arguments demonstrate that sea levels derived from an unadjusted $\Delta \delta^{18}$ O (Fig. 3c) stack are incongruous with the stratigraphy preserved at Enewetak (Fig. 3a). Reef-derived deposits dating to ~5.6, 7.0 and

8.4 Ma, found at core depths between 200–300 m below Enewetak's rim today (Fig. 3a), constrain late Miocene sea level to have been between ~50-125 mbsl. Only ~100 m of the vertical offset between present sea level and these late Miocene carbonate deposits (200-300 mbsl) can likely be accounted for by subsidence (thermal, glacial isostatic adjustment, dynamic topography). For instance, if we were instead to accept the $\Delta \delta^{18}$ O stack as is and convert it to sea level using late Pleistocene ice volume/temperature calibration parameters, a subsidence rate of at least 36 m/Myr would be needed to reconcile model stratigraphy with that observed in drill cores from Enewetak. Such a rate would be nearly twice as fast as the predicted thermal subsidence rate and observations from drowned western Pacific Ocean guyots (see Section 3.1). Ultimately, we find little evidence to support such a high subsidence rate (~36 m/Myr), especially given the island's location far from any polar ice sheet (Mitrovica and Milne, 2002) and minimal changes in dynamic topography over the past 30 million years (Moucha et al., 2008).

Low sea-level indicators across the Miocene/Pliocene transition, distributed globally, provide further confidence that glacial conditions inferred at Enewetak Atoll during the late Miocene mainly reflects increased ice volume, not uncertainty in our estimated subsidence rate, possibly caused by regional dynamic topography or glacial-isostatic adjustment. Additional evidence of low sea level during the late Miocene is found in drill cores from Midway Atoll, 2800 km NE of Enewetak (Lincoln and Schlanger, 1987). There, the Miocene/Plio-Pleistocene boundary is found ~146 m below the rim, which, corrected for subsidence, indicates sea levels at least ~75 m below present (Ladd et al., 1970; Lincoln and Schlanger, 1987). Low late Miocene sea levels are also consistent with carbonate depositional sequences from Makatea, French Polynesia (Montaggioni and Camoin, 1997), as well as the nearly ubiquitous Miocene/early Pliocene discontinuity observed in shallow water carbonate sections worldwide (Adams et al., 1977). If the late Miocene lowstands implied by Enewetak's stratigraphy reflect eustatic sea level (ice volume) changes, a lack of corresponding heavy isotope excursions in the δ^{18} O stack calls into question its utility in reconstructing sea level deep in time without substantial correction.

Much of the late Miocene δ^{18} O signal appears dominated by changes in bottom water temperature (Fig. 3c, d). Our results suggest changes in deep ocean temperature (T) would be needed to explain $\sim 1\%$ of the variation in the benthic δ^{18} O stack during the late Miocene, consistent with independent estimates of a ~4-5 °C change in deep ocean temperature (Lear et al., 2003) and the ~0.55% change in δ^{18} O caused by a ~2 °C warming during the last deglaciation (Fairbanks, 1989). The model also suggests the amplitude of sea-level variability was considerably lower during the late Miocene (~50 m) than over the last few glacial cycles (~120 m) though still much greater (~2 \times) than would be expected just using late Pleistocene ice volume calibration parameters. This echoes conclusions from a paired Mg/Ca and benthic δ^{18} O analysis by Billups and Schrag (2002), which suggests deep ocean temperature variability during the mid-late Miocene may have masked ice volume changes during large regressive events. Other proposed mechanisms for changing the relationship between $\Delta \delta^{18}$ O and sea level include: (1) the extent of Arctic (e.g., Broecker, 1975; Jakobsson et al., 2010) or Antarctic ice shelves which would effect $\Delta \delta^{18}$ O but not sea level, (2) a change in the δ^{18} O of glacial ice (Pekar and DeConto, 2006; Winnick and Caves, 2015), (3) salinity (Rohling and Bigg, 1998) and/or (4) ocean circulation.

Global climate and ice-sheet models (DeConto et al., 2008) suggest that climatic conditions during much of the Miocene may have been conducive to bipolar glaciation, which would be required if the low sea levels inferred here were the result of enhanced global ice volume. While seismic imaging and drilling confirm that Antarctic ice sheets were established by the late Miocene (Anderson and Shipp, 2001) and ice volume estimates suggest the East Antarctic Ice Sheet periodically grew larger (25%) than present (Pekar and DeConto, 2006) during the mid Miocene, it is hard to envision how an additional 50 m (sea level equivalent vertical meters) or more of ice could be added on top of the present-day volume of ice on Antarctica. Evidence of late Miocene glaciation of the Northern Hemisphere is sparser, possibly owing to poor preservation. However, ice-rafted debris deposits in marine sediment cores of Miocene age are recognized in the Arctic (<16 Ma), Fram Strait (<18 Ma), Greenland (<7 Ma), Norwegian Sea (<11 Ma), Iceland Sea (<7.5 Ma), Baffin Bay (<9 Ma) and North Pacific (<6.6 Ma) (De Schepper et al., 2014) indicating the presence of Northern Hemisphere ice by the late Miocene. Likewise, synthesis of late Miocene δ^{18} O data from planktonic foraminifera by Williams et al. (2005) suggest significantly cooler than modern sea surface temperatures may have occurred at this time. Colder temperatures would also be consistent with the occurrence of bi-polar glaciations; however, uncertainties in ice-sheet thickness preclude a straightforward estimation of the Northern v. Southern Hemispheric contribution to the late Miocene sea-level lowstands we infer at Enewetak.

Moving into the Pliocene, our best-fit relative sea-level reconstruction (Fig. 3b), suggests that sea level, and consequently Enewetak's reefs, rose rapidly between 4–5 Ma with maximum highstand sea level exceeding modern during most of the Pliocene. Rapid reef accretion (>50 m) around 5 Ma is also observed in well-dated stratigraphic sections from uplifted atolls in the Pacific (e.g., Kita-Diato-Jima–Ohde and Elderfield, 1992; Niue–Aharon et al., 1993), providing further evidence that a period of sustained low sea level during the late Miocene may have produced the accommodation depth necessary for the



Fig. 6. Sensitivity of lagoon and rim final elevations to variable vertical motion rates. Rim and lagoon elevations are given by gray and black lines, respectively. Rainfall was held constant for these model runs.

observed reef growth during the ensuing early Pliocene transgression. Perhaps release of CO₂ during this rapid buildup of coral reefs $(Ca^{2+}+2HCO_3^- \rightarrow CaCO_3 + CO_2 + H_2O)$ may have contributed to observed shoaling of the carbonate compensation depth during the late Miocene and early Pliocene (Pälike et al., 2012).

Moving into the mid-late Pliocene, the model suggests an escalation of glacial-interglacial sea-level variability. Modeled lowstands around



Fig. 5. Conceptual models of modern empty-bucket atoll formation. (top) Darwin's theory of subsidence control suggests volcanic islands progress along a path from fringing reef to barrier reef to atoll as an island ages, subsides and erodes. (bottom) In contrast, paleo-environmental data (Cronin et al., 1991) and our model indicate that the deep lagoon (empty-bucket) of Enewetak Atoll developed since the late Pliocene due to high magnitude glacial-interglacial cycles. Seismic and drilling evidence from the Maldives (Schlager and Purkis, 2013 and refs. therein) also suggests that atolls have oscillated regularly between rimmed and un-rimmed morphologies during the geologic past. Schematics styled after Davis (1928) sector diagrams.

3.3, 3.6, 4.0 and 4.9 Ma correspond closely with widespread observational evidence (e.g., ice-rafted debris) of Northern Hemisphere ice expansion during the Pliocene (De Schepper et al., 2014). Similarly, dissolution through most of Enewetak's accumulated late Pliocene section, indicated by a subaerial exposure horizon separating unconforming mid–late Pliocene (>2.5 Ma) and mid Pleistocene (1.6 Ma) carbonates, is consistent with dissolution during expansion of large-scale Northern Hemisphere ice sheets after 2.7 Ma (Bailey et al., 2010). Net erosion of almost 50 m of lagoon sediment occurs in our synthetic stratigraphy between 3.1 and 1.5 Ma (Fig. 3a). Our best-fit model suggests that this lagoon deepening requires sediments to dissolve at rates considerably faster than reef framework on the rim (Lagoon $F_{dl} = 10.4 \times 10^{-5}$; Rim $F_{dr} = 7.5 \times 10^{-5}$), compensating for the lagoon being exposed less frequently than the atoll rim.

3.3. Atoll morphology

Model results suggest the intensification of glacial–interglacial sealevel cycles during the Pleistocene drove a change in Enewetak's morphology from a Pliocene full-bucket to the empty-bucket morphology we see today, consistent with paleoenvironmental reconstructions from Enewetak, which show the dominance of ostracod lagoon species such as *Loxoconcha* and *Hermanites* during the Quaternary (Cronin et al., 1991). Over the past 8.5 Ma, model and ostracod data (Cronin et al., 1991) suggest that Enewetak, and by extension most large atolls, have oscillated between empty and full-bucket morphology, with a deep lagoon present throughout the Pleistocene and also around the Miocene/Pliocene transition (Figs. 3, 5). Together, the paleo-environmental data and model results suggests that differential dissolution and constructional rim growth through large-amplitude late Pliocene to early Pleistocene glacial sea-level cycles created the empty-bucket morphology we see today at Enewetak (Figs. 3, 5).

Bathymetric soundings from atoll lagoons in the western Pacific Ocean suggest that the modern empty-bucket morphology of atoll lagoons is also strongly influenced by sedimentation and island geometry. For instance, small atolls (Fig. 4), even in areas of high rainfall, have relatively shallow lagoons due to rapid infilling from the atoll rim during sea-level highstands. With increasing island size, the relative contribution of rim-derived sediment decreases, resulting in deeper lagoons. However, deeper lagoons are also less frequently exposed over a typical glacial-interglacial cycle, limiting the time-averaged dissolution rate and therefore preventing further lagoon deepening. The balance of these two effects-deeper lagoons with larger atoll size but also slower effective dissolution-restricts average lagoon depth to less than ~50 m. Our model is able to capture this interaction of island size with dissolution rate and, using our best-fit sea-level curve, closely matches observations of mean lagoon depth from 14 atolls across the Marshall Islands (Pearson's r = 0.84, p < 0.01, n = 14) (Fig. 4a).

Subsidence rate has a minor impact on modern lagoon relief. For example, simulations for an island with the same size and mean rainfall as Enewetak but subsidence rates between 0 and 100 m/Myr (~5 times estimates in Section 3.1), produce a relatively narrow range of modern lagoon depths (30.4–37 mbsl). More substantial relief (Fig. 6) is generated only with very fast uplift (vertical motion (VM) >100 m/Myr), positioning the island well above sea level or when rapid subsidence (VM < -175 m/Myr) causes rim submergence during deglacial transgressions.

4. Conclusions

Altogether, our results show a considerably different pattern of sealevel variability over the past 8.5 Ma than implied by deep-sea oxygen isotope records, suggesting persistent bipolar glaciation and low sea level during the late Miocene, super-interglacials and higher sea level during the Pliocene, and intensification of glacial–interglacial oscillations during the Pleistocene. The widespread occurrence of modern empty-bucket atolls bears the imprint of these large-scale sea-level cycles. Using a simple numerical model we show that geographic changes in rainfall (dissolution) and island geometry (sedimentation) best explain the variability of atoll morphology in the modern Pacific.

Acknowledgments

Support for this work was provided through a Jackson School Distinguished Postdoctoral Fellowship to Michael Toomey. We appreciated the helpful feedback on an earlier version of this manuscript from Tom Cronin and Bruce Wardlaw as well as thoughtful reviews by Sam Purkis and an anonymous reviewer. Any use of trade, firm, or product names is for descriptive purposes only and does not imply endorsement by the U.S. Government.

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