

# SPR-4230: Alternative Quality Assurance Methods for Compacted Subgrade

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# Presentation Layout

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- Project background
- Research approach
- Research Findings to Date
  - Laboratory Testing
  - Field Testing
- Summary
- Future Work



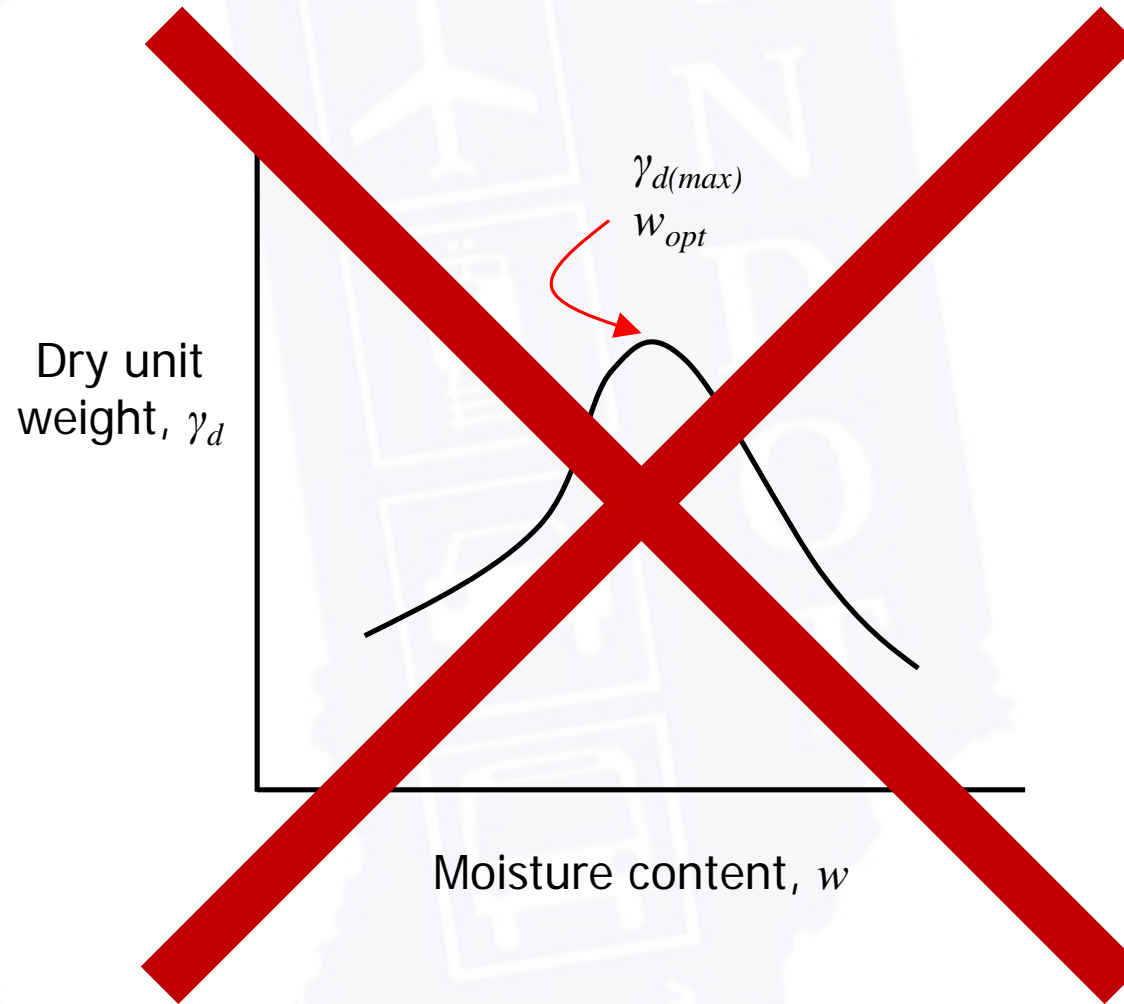
# Performance-Based Specifications

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- Type of quality assurance specification
  - Quality assurance = owner/owner's representative (i.e., INDOT)
  - Quality control = contractor
- Describes desired level(s) of engineering property(s)
  - Predictor(s) of performance
  - Appear in primary prediction relationship(s)

Doyle, G. (2003). *Major Types of Transportation Construction Specifications: A Guideline to Understanding Their Evolution and Application*. AASHTO Highway Subcommittee on Construction, Quality Construction Task Force. Washington, D.C.: American Association of State Highway and Transportation Officials.

# Traditional Subgrade Quality Assurance



Although soil strength and stiffness tends to increase with increasing dry unit weight (density), density/dry unit weight cannot be used to directly predict performance

# A More Appropriate Performance Property

**Project1:Project\***

General Information

Design type: New Pavement

Pavement type: Rlexible Pavement

Design life (years): 20

Base construction: August 2013

Pavement construction: August 2013

Traffic opening: Septen 2013

Performance Criteria	Limit	Reliability
Initial IRI (in./mile)	60	
Terminal IRI (in./mile)	200	90
AC top-down fatigue cracking (ft/mile)	2000	90
AC bottom-up fatigue cracking (percent)	20	90
AC thermal cracking (ft/mile)	700	90
Permanent deformation - total pavement (in.)	0.5	90
Permanent deformation - AC only (in.)	0.4	

Layer 5 Subgrade: A-4

Resilient modulus (psi): **9480**

Unbound: Layer thickness (in.) 0.4, Poisson's ratio 0.5, Coefficient of lateral earth pressure (K0) 0.5

Sieve: A-4

Identifiers: Display name/identifier A-4, Description of object Default material, Approver, Date approved 1/1/2011, Author AASHTO, Date created 1/1/2011, County, State, District, Direction of travel, From station (miles), To station (miles), Mileposts

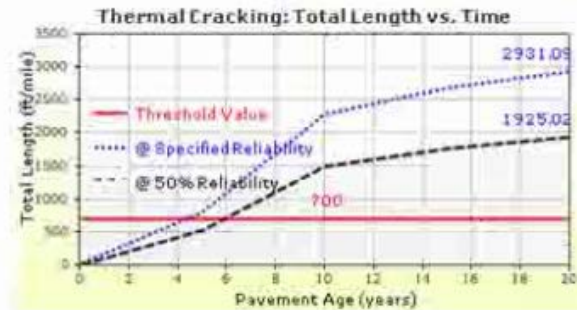
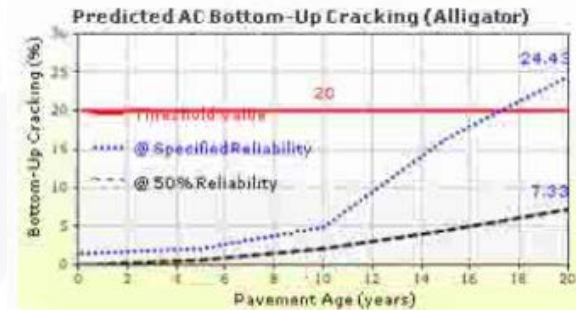
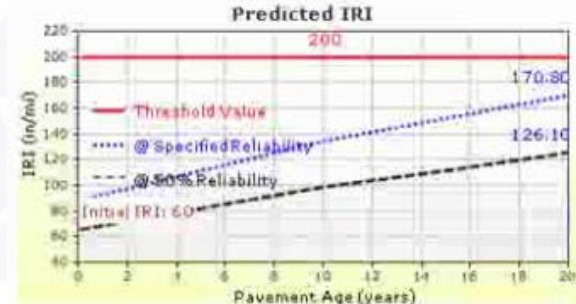
Resilient modulus (psi): Enter the resilient modulus of the unbound materials and subgrade.

Error List:

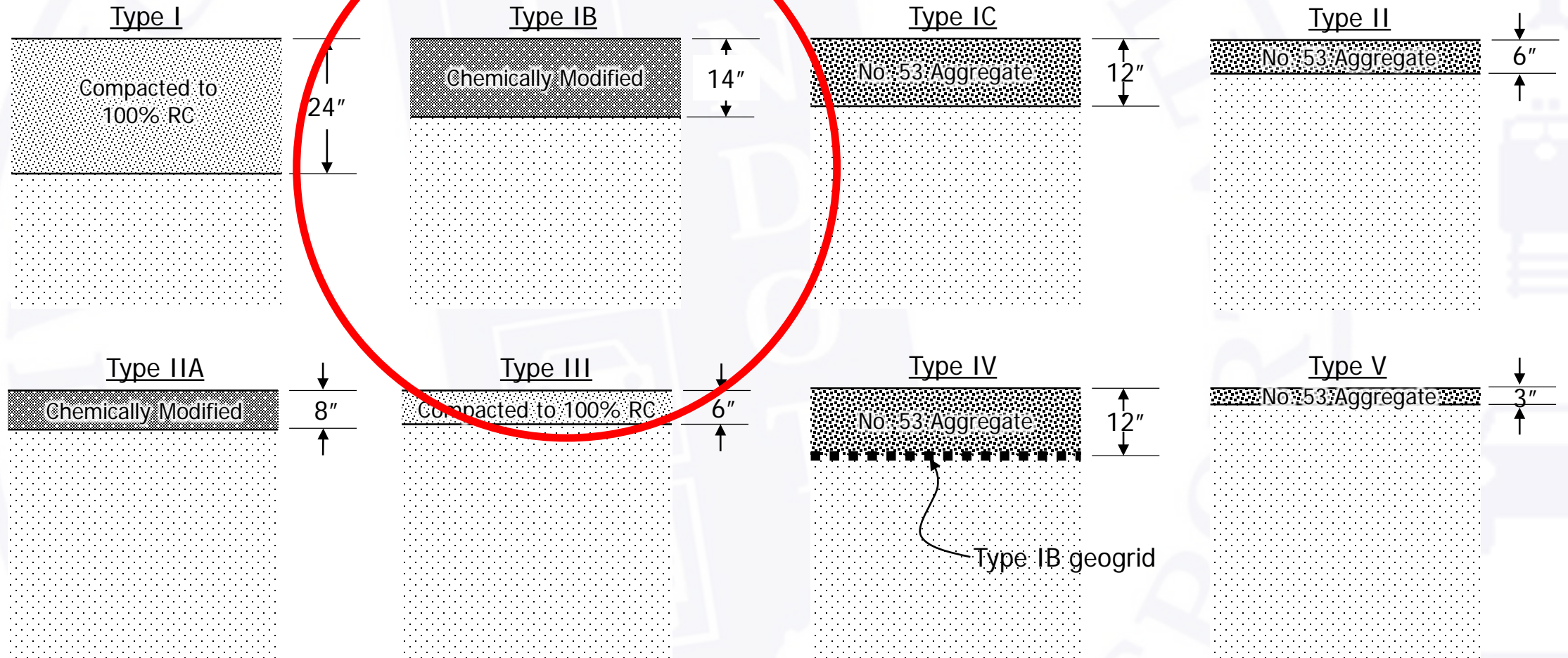
Project	Object	Property	Description
Project1	Layer 1 Asphalt Concrete:Default asphalt concrete	Asphalt binder	Asphalt binder calculation error - Asphalt Binder type must be one of PENETRATI...

**Modulus**

Resilient modulus (psi) **9480**



# INDOT Allowed Subgrade Treatment Types



# Goal of SPR-4230

Specified chemically modified subgrade resilient modulus used in design

In situ quality assurance testing

Confirm specified chemically modified subgrade resilient modulus during construction

Light weight deflectometer (LWD)

- Rapid
- Easy to use
- Provides stiffness measurement

# Light Weight Deflectometer (LWD)

10 kg drop weight  
imparting 1,589 lbf  
maximum force

Accelerometer  
measuring peak  
deflection

≈28-<sup>3</sup>/<sub>8</sub> in.  
drop height

Data  
collector

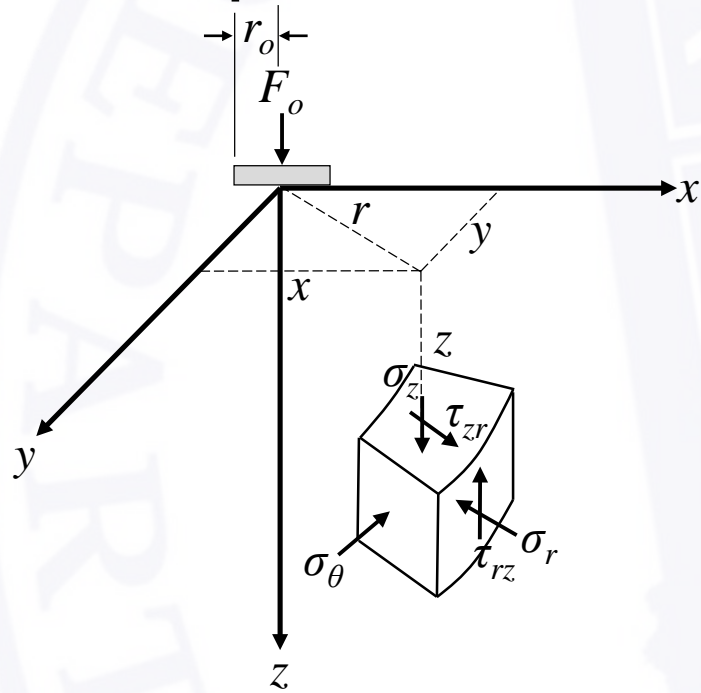
Loading plate  
(11.81 in. diameter)





# LWD Elastic Modulus Backcalculation

## Boussinesq's solution:



## In Situ Stresses:

$$\sigma_z = f(F_o, r, z) \quad \sigma_r = f(F_o, r, z) \quad \sigma_\theta = f(F_o, r, z)$$

## In Situ Vertical Strain:

$$\varepsilon_z = \frac{1}{E} [\sigma_z - \nu(\sigma_\theta + \sigma_r)]$$

$\nu$  is Poisson's ratio  
(0.2 to 0.4 typical)

## Vertical Deflection at Surface:

$$\delta_z = \int_0^\infty \varepsilon_z dz$$

$$\delta_z = \frac{F_o(1 - \nu^2)k}{\pi r_o E}$$

$k$  is applied stress shape factor

$$E_{LWD} = \frac{F_o(1 - \nu^2)k}{\pi r_o \delta_z}$$

$E$  is elastic Modulus

$F_o$  is applied force

$r_o$  is loading plate radius

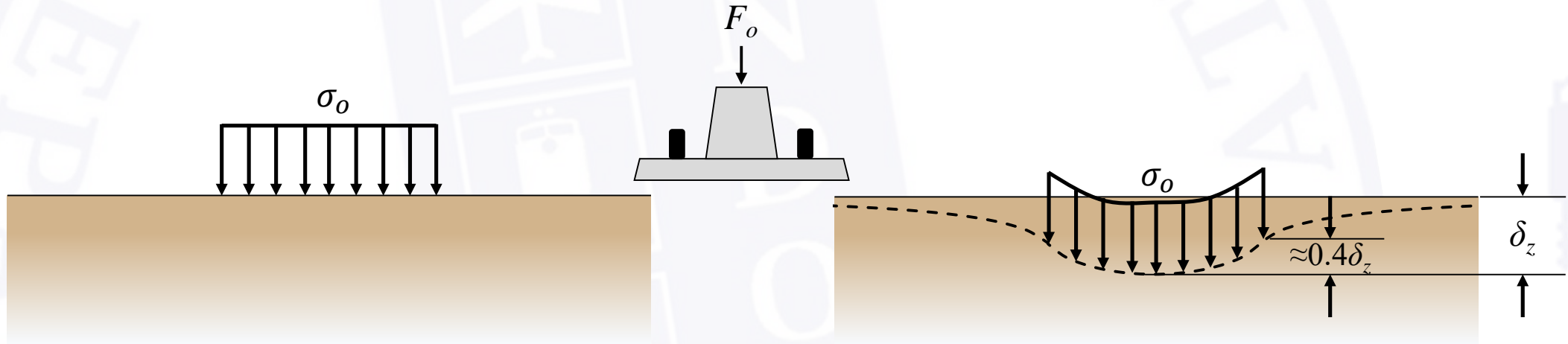
$\nu$  is Poisson's ratio

$k$  is applied stress shape factor

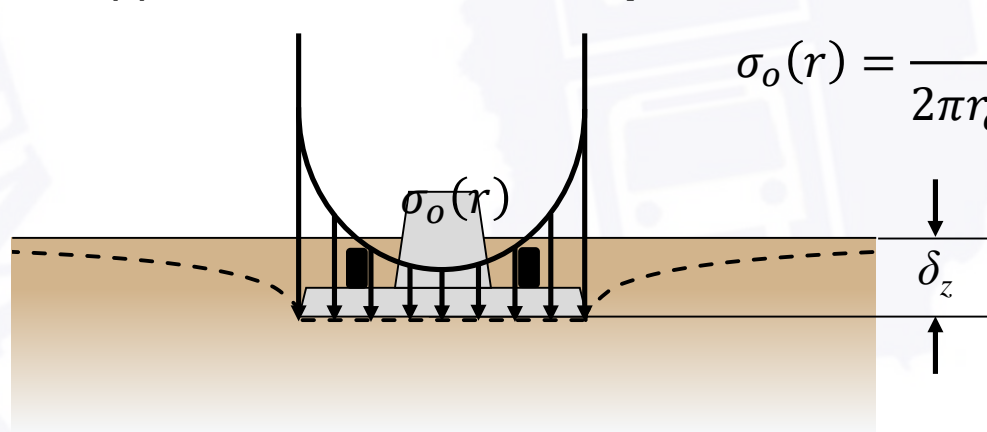
$\delta_z$  is surface deflection

# Applied Stress Shape Factor (k)

Is stress applied uniformly? **Probably not (loading plate is too stiff)**



Stress applied over an **inverse-parabolic stress distribution** is a better assumption

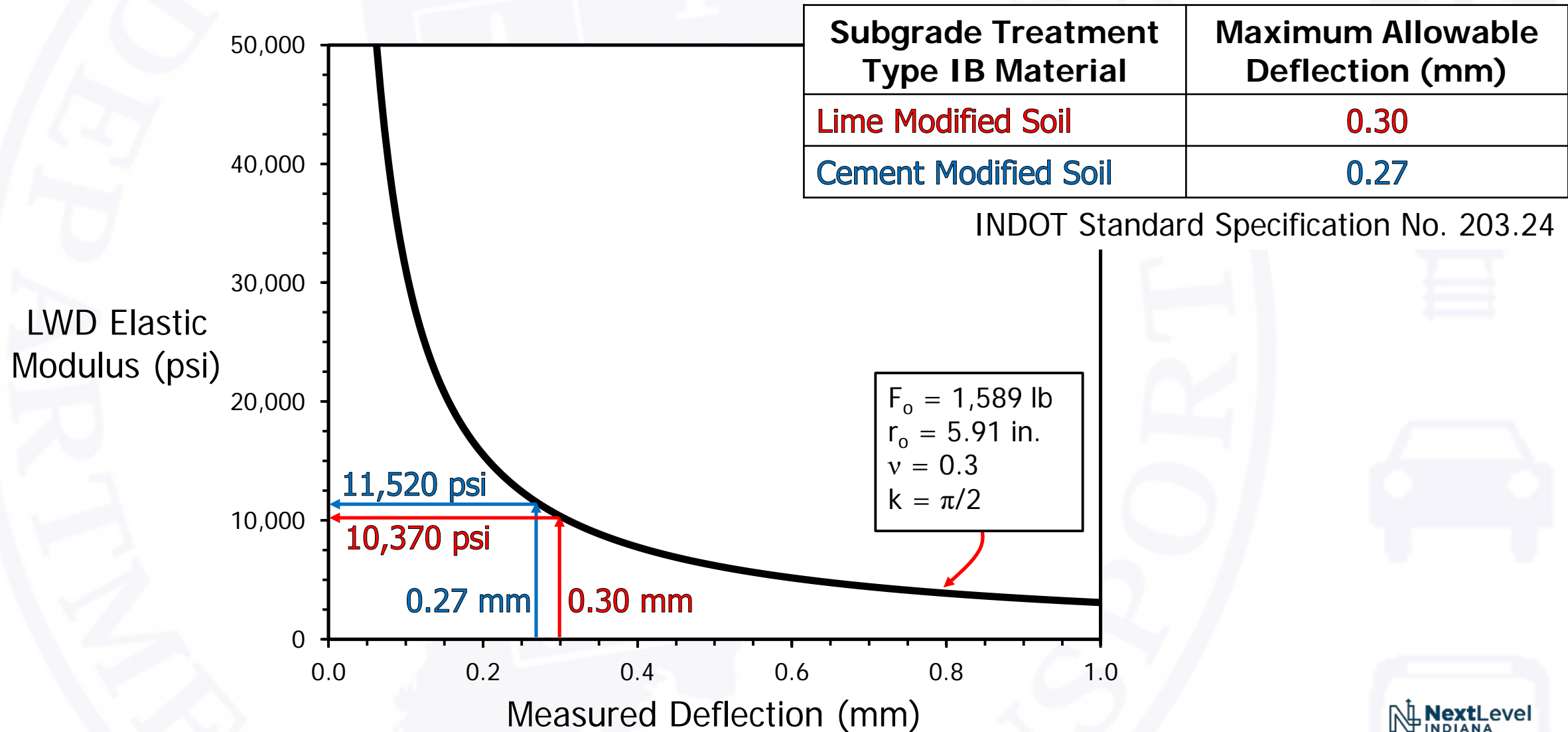


$$\sigma_o(r) = \frac{F_o}{2\pi r_o \sqrt{r_o^2 - r^2}}$$

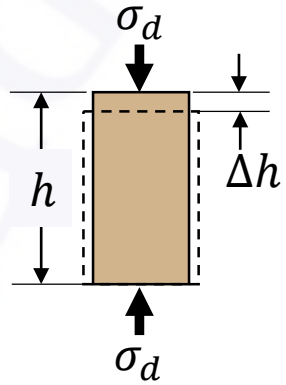
$$E_{LWD} = \frac{F_o (1 - \nu^2) k}{\pi r_o \delta_z}$$

$$k = \frac{\pi}{2}$$

# LWD Elastic Modulus



# LWD Elastic Modulus $\neq$ Resilient Modulus (Strain)



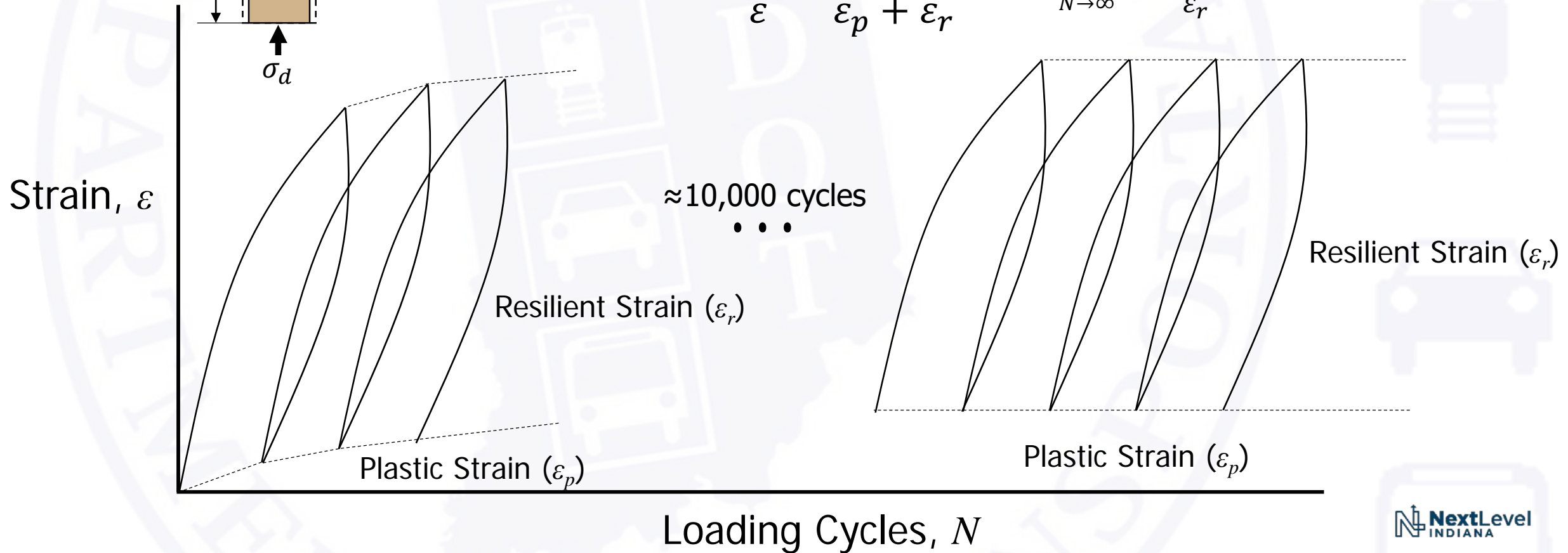
$$\varepsilon = \frac{\Delta h}{h}$$

$$\varepsilon = \varepsilon_p + \varepsilon_r$$

$$E = \frac{\sigma_d}{\varepsilon} = \frac{\sigma_d}{\varepsilon_p + \varepsilon_r}$$

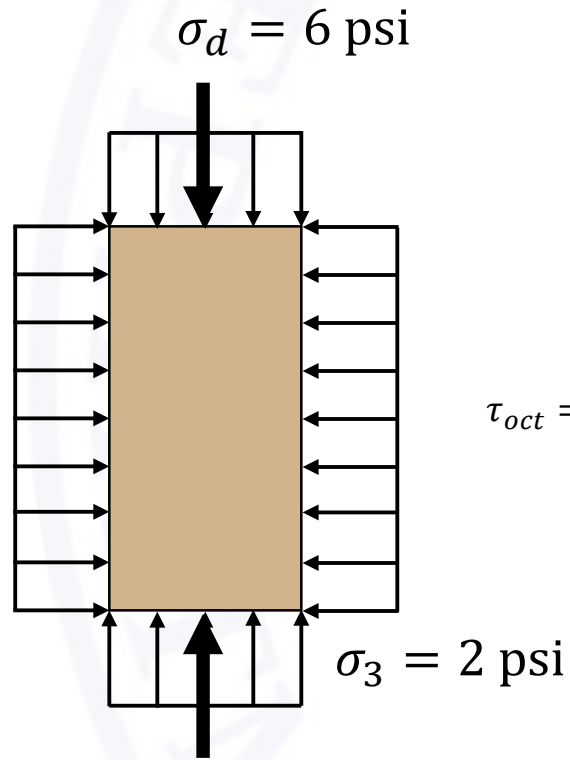
$$\lim_{N \rightarrow \infty} \varepsilon_p = 0$$

$$\lim_{N \rightarrow \infty} E = \frac{\sigma_d}{\varepsilon_r} = M_r$$



# LWD Elastic Modulus $\neq$ Resilient Modulus (Stress)

AASHTO T 307  
(Resilient Modulus Lab Test)



$$M_r = k_1 p_a \left( \frac{\theta}{p_a} \right)^{k_2} \left( \frac{\tau_{oct}}{p_a} + 1 \right)^{k_3}$$

$$\theta = \sigma_1 + \sigma_2 + \sigma_3$$

$$\tau_{oct} = \frac{1}{3} \sqrt{(\sigma_1 - \sigma_2)^2 + (\sigma_1 - \sigma_3)^2 + (\sigma_2 - \sigma_3)^2}$$

$\theta$  is bulk stress

$\tau_{oct}$  is octahedral shear stress

$p_a$  is atmospheric pressure

$k_1, k_2, k_3$  are material constants

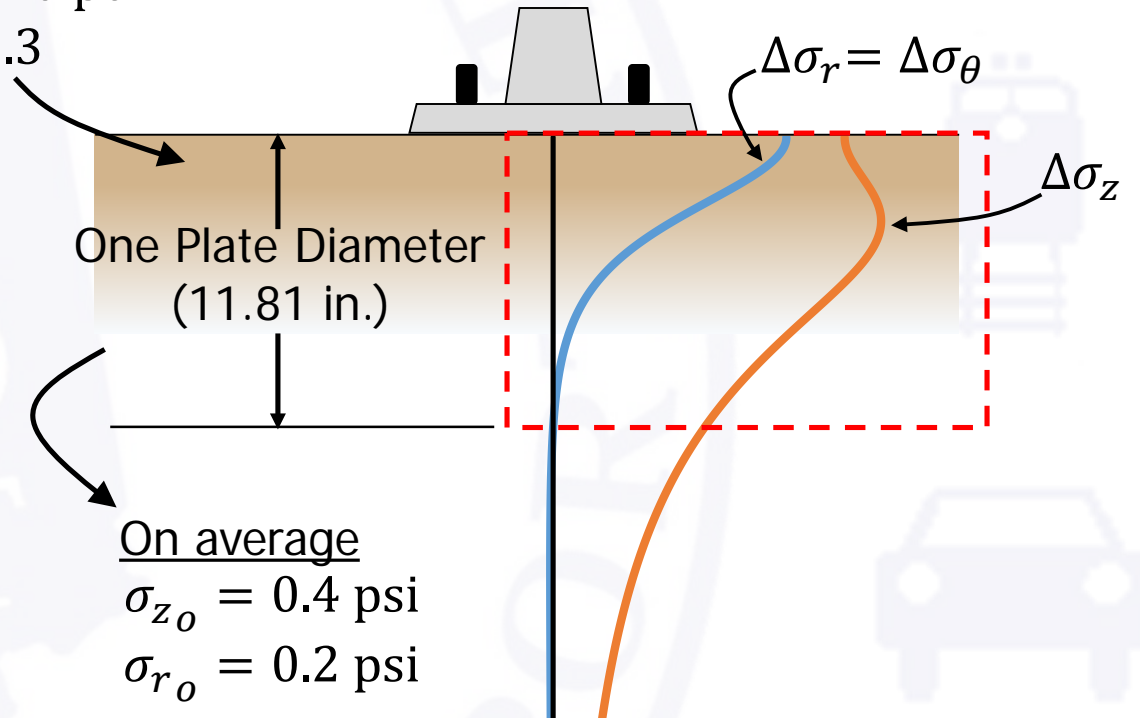
$$\sigma_2 = \sigma_3 = 2 \text{ psi}$$

$$\sigma_1 = 8 \text{ psi}$$

Light Weight Deflectometer

$$\gamma = 120 \text{ pcf}$$

$$\nu = 0.3$$



On average

$$\sigma_{z0} = 0.4 \text{ psi}$$

$$\sigma_{r0} = 0.2 \text{ psi}$$

$$\Delta\sigma_z = 6.5 \text{ psi}$$

$$\Delta\sigma_r = 1.9 \text{ psi}$$

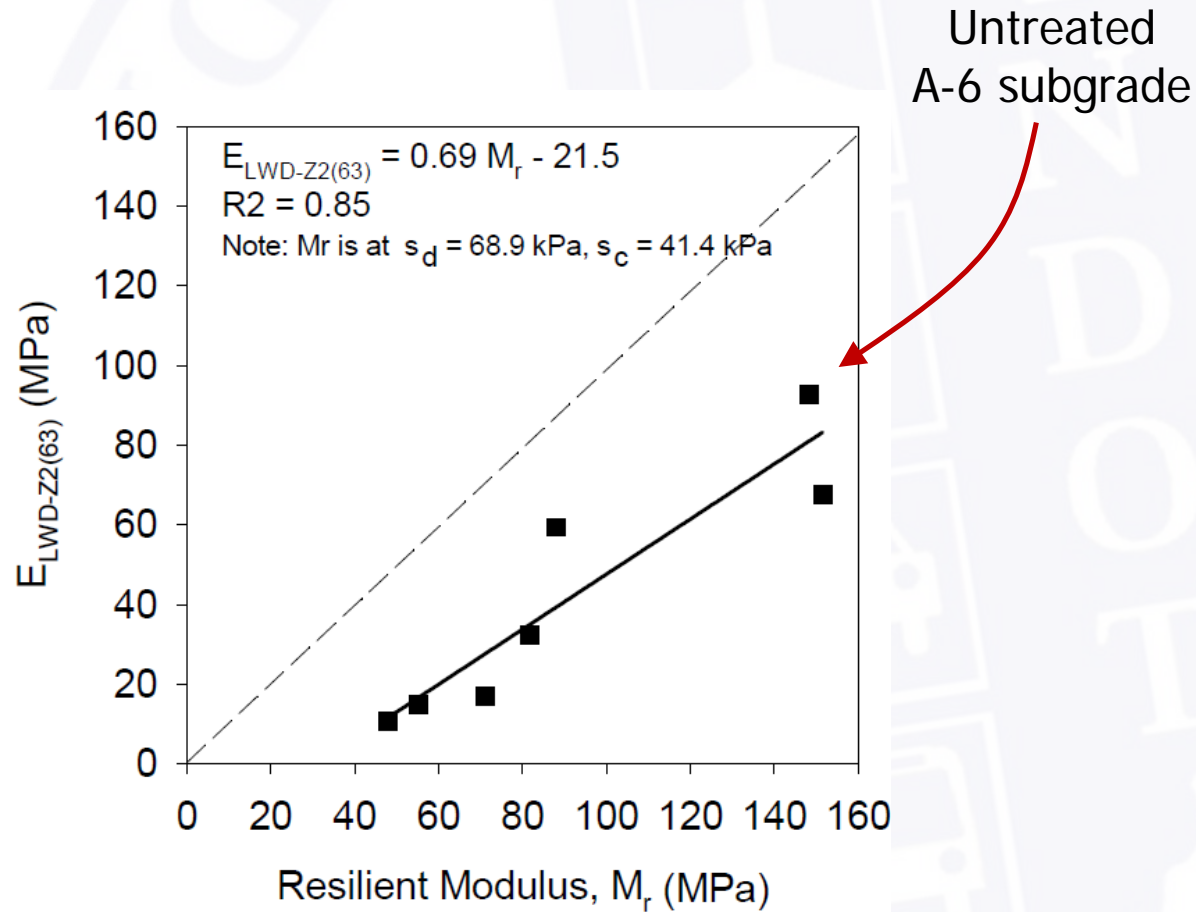
$$\sigma_{zf} = 6.9 \text{ psi}$$

$$\sigma_{rf} = 2.1 \text{ psi}$$

$$\sigma_2 = \sigma_3 = 2.1 \text{ psi}$$

$$\sigma_1 = 9.0 \text{ psi}$$

# Previously Established $E_{LWD}$ and $M_r$ Correlations



D. J. White, M. Thompson, and P. Vennapusa, "Field validation of intelligent compaction monitoring technology for unbound materials," Final Report MN/RC-2007-10, Minnesota DOT, St. Paul, Minn, USA, 2007.

Untreated A-4 and A-7-5 subgrades

$$M_r = k_1 p_a \left( \frac{\theta}{p_a} \right)^{k_2} \left( \frac{\tau_{oct}}{p_a} + 1 \right)^{k_3}$$

$$k_i = C_1 + C_2 \left( \frac{\sigma}{\delta} \right) \quad i = 1, 2, 3$$

	$C_1$	$C_2$
$k_1$	480	1040
$k_2$	1.0	-0.9
$k_3$	-3.7	2.8

S. H. Mousavi, A. G. Gabr, and R. H. Borden, "Subgrade resilient modulus prediction using light-weight deflectometer data," Canadian Geotechnical Journal, 54(3), 2017.

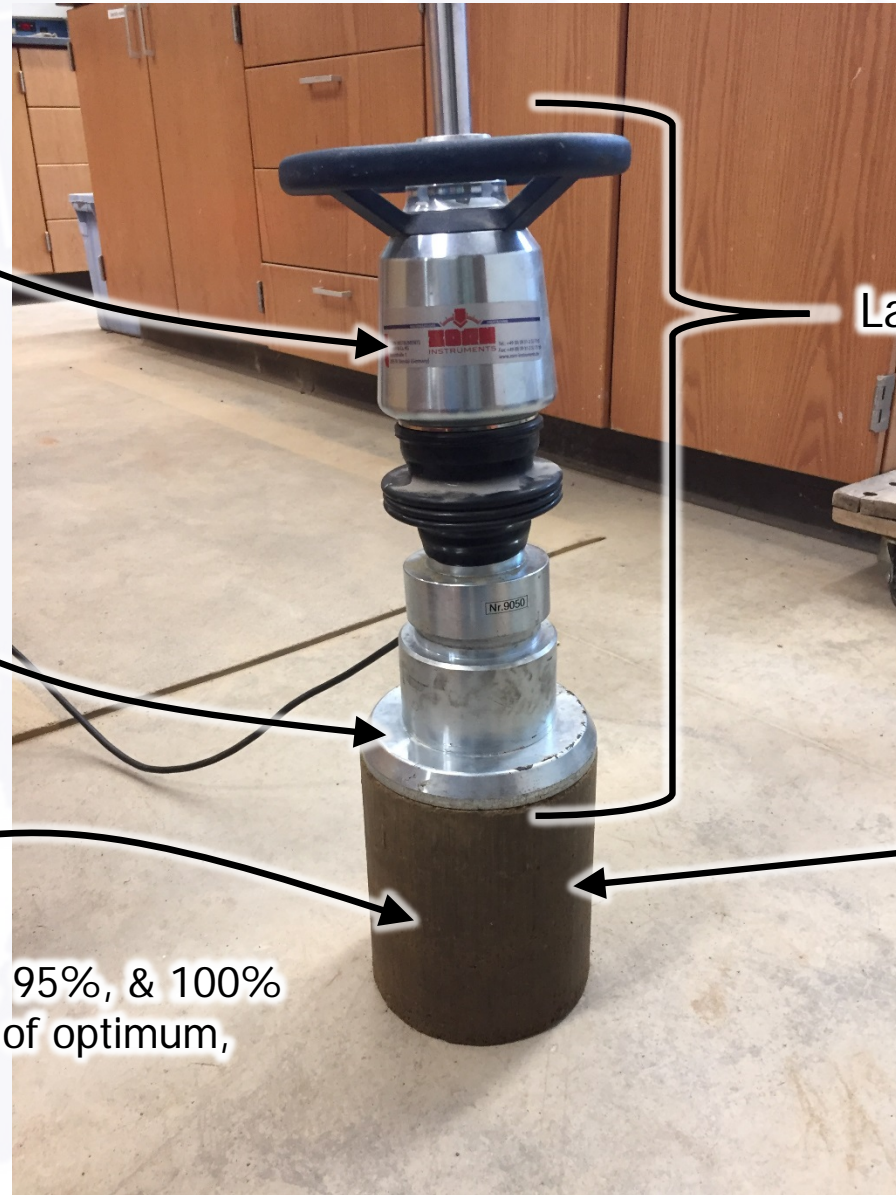
# This Study's $E_{LWD}$ and $M_r$ Correlation

5 kg drop weight  
imparting up to 871 lbf  
maximum force

Loading plate  
(5.91 in. diameter)

A-6 subgrade

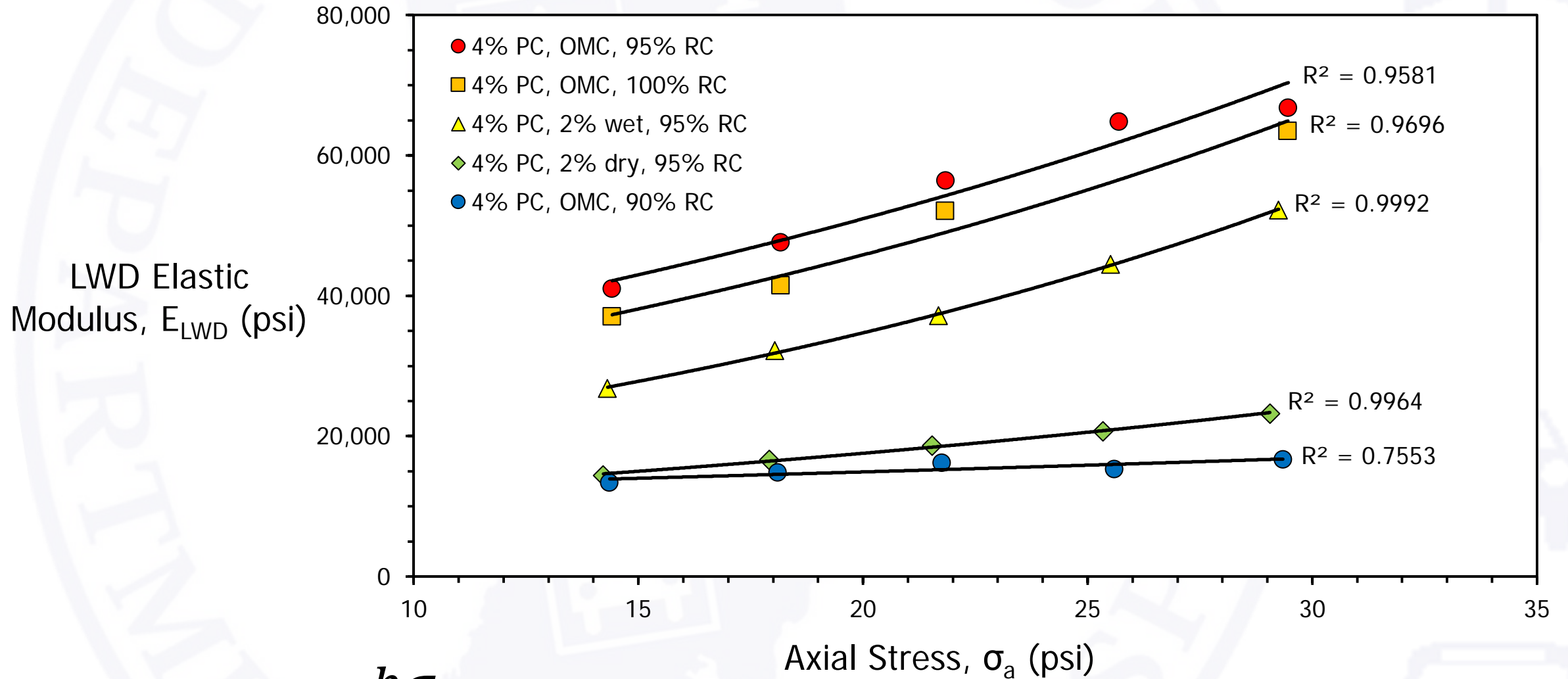
- Nominal 4% cement content
- Nominal relative compactions of 90%, 95%, & 100%
- Nominal moisture contents of 2% dry of optimum, optimum, & wet of optimum



Laboratory LWD

CBR-sized sample  
(7 in. high, 6 in. diameter)

# Relationship Between $E_{LWD}$ and Axial Stress ( $\sigma_a$ )

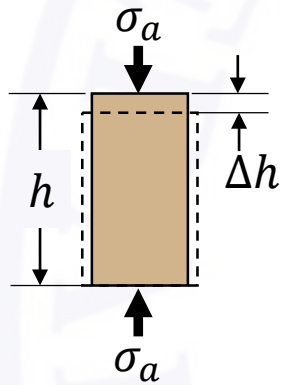


$$E_{LWD} = ae^{b\sigma_a}$$



# Predicting In Situ $E_{LWD}$

In the lab...



$$E_{LWD} = a e^{b \sigma_a}$$

$$\sigma_a = (\varepsilon_{LWD})(E_{LWD})$$

$$E_{LWD} = a \exp[b(\varepsilon_{LWD})(E_{LWD})]$$

$$\varepsilon_{LWD} = \frac{\Delta h}{h}$$

In the field...

$$\varepsilon_{LWD} = \frac{1}{E_{LWD}} [\sigma_z - \nu(\sigma_r + \sigma_\theta)]$$

$$(\varepsilon_{LWD})(E_{LWD}) = \sigma_z - \nu(\sigma_r + \sigma_\theta)$$

For symmetric loading...

$$\sigma_r = \sigma_\theta$$

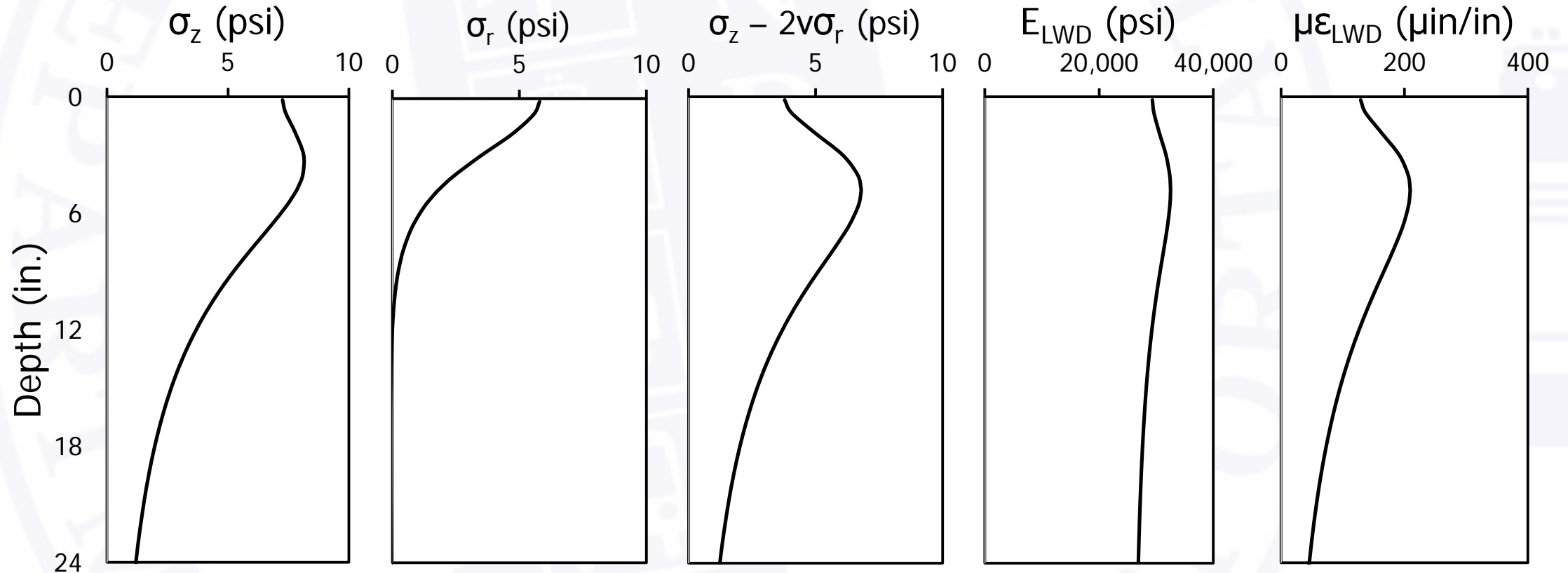
$$(\varepsilon_{LWD})(E_{LWD}) = \sigma_z - 2\nu\sigma_r$$

$$E_{LWD} = a e^{b(\sigma_z - 2\nu\sigma_r)}$$

# Predicting In Situ $E_{LWD}$

Example: 4% cement; optimum moisture content; 95% relative compaction;  $\nu = 0.3$  (assumed)  
 $F_o = 1,589$  lb;  $r_o = 5.91$  in.

$$E_{LWD} = 25800 e^{0.034(\sigma_z - 2\nu\sigma_r)}$$



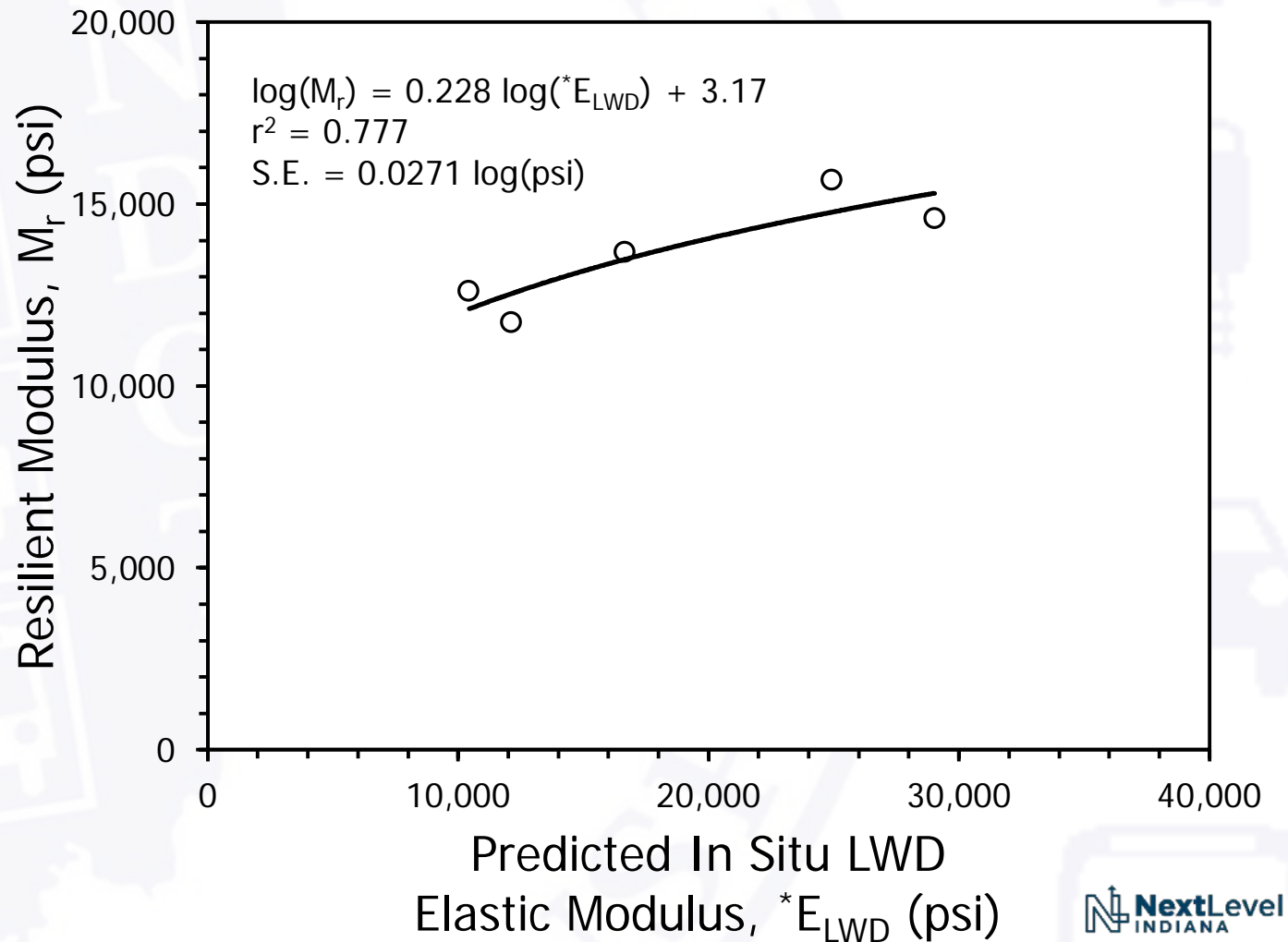
$$\delta_{LWD} = \int_0^{\infty} \epsilon_{LWD} dz = 0.107 \text{ mm}$$

$$* E_{LWD} = \frac{F_o(1 - \nu^2)}{2r_o\delta_z} = 29,033 \text{ psi}$$

# Correlating Predicted In Situ $E_{LWD}$ with $M_r$

Resilient Modulus per AASHTO T 307

$\sigma_3 = 2$  psi,  $\sigma_d = 6$  psi



# Field Testing (2018 construction season)

## I-65 near Frankfort (Crawfordsville District)

- Target 4% cement
- A-4 and A-2-4 subgrades
- 4 test sections

## I-469 near Fort Wayne (Fort Wayne District)

- Target 5% cement
- A-6 subgrade
- 2 test sections

## US-6 near Brimfield (Fort Wayne District)

- Target 4% cement
- A-1-b and A-4 subgrade
- 1 test section

## Cleveland Road in South Bend (La Porte District)

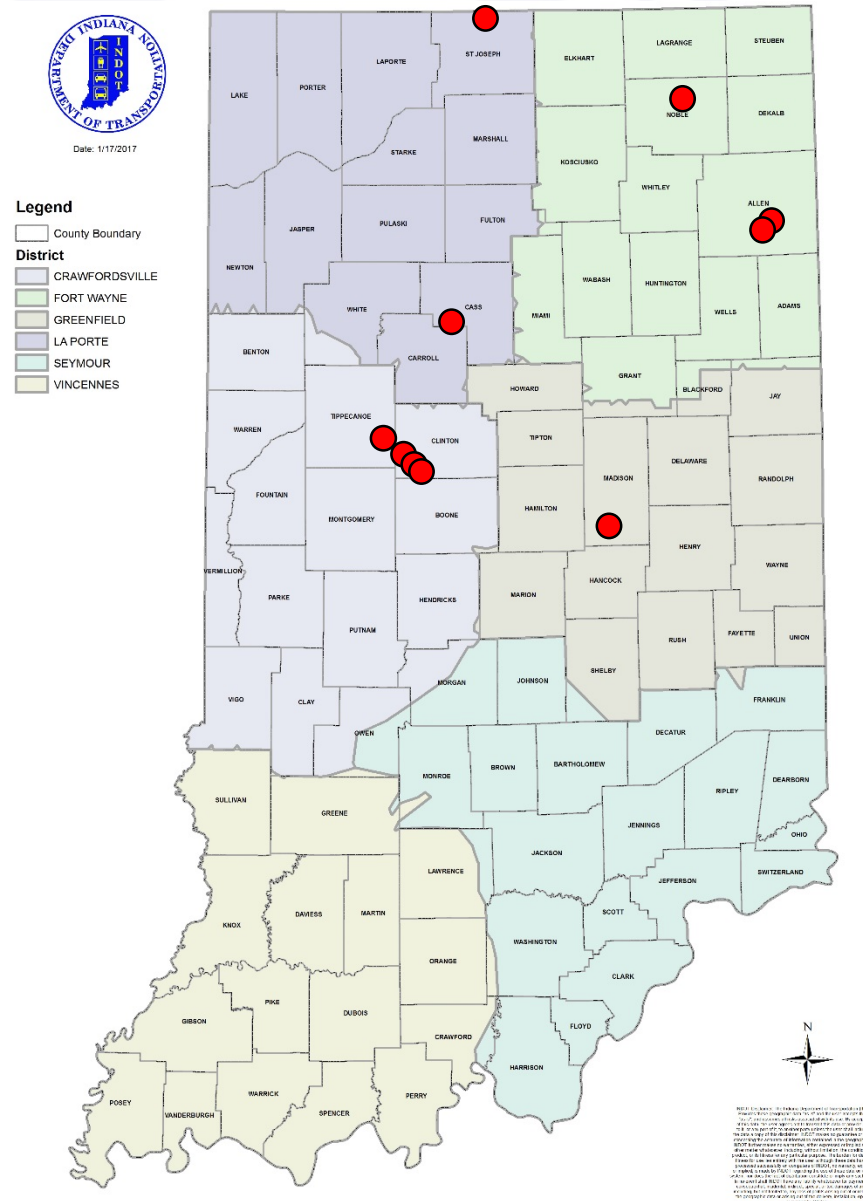
- Target 4% cement
- A-1-b
- 1 test section

## CR 400 S near Clymers (La Porte District)

- Target 4% cement
- A-4
- 1 test section

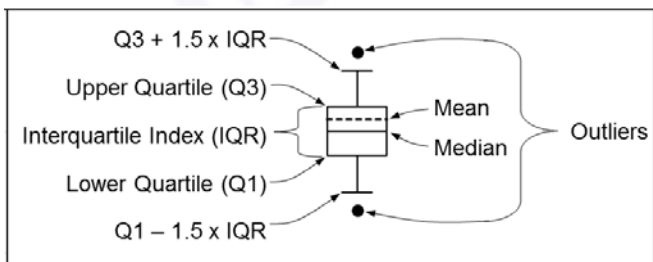
## I-69 near Anderson (Greenfield District)

- Target 4% cement
- A-6
- 1 test section



# Results of LWD Field Testing (LWD Deflection)

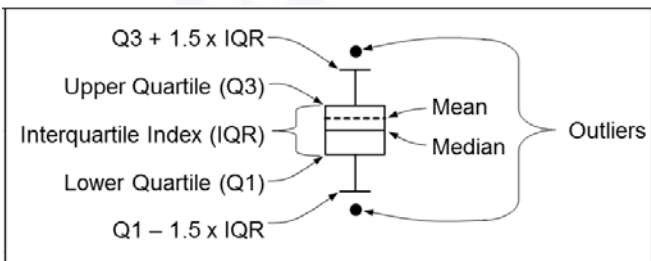
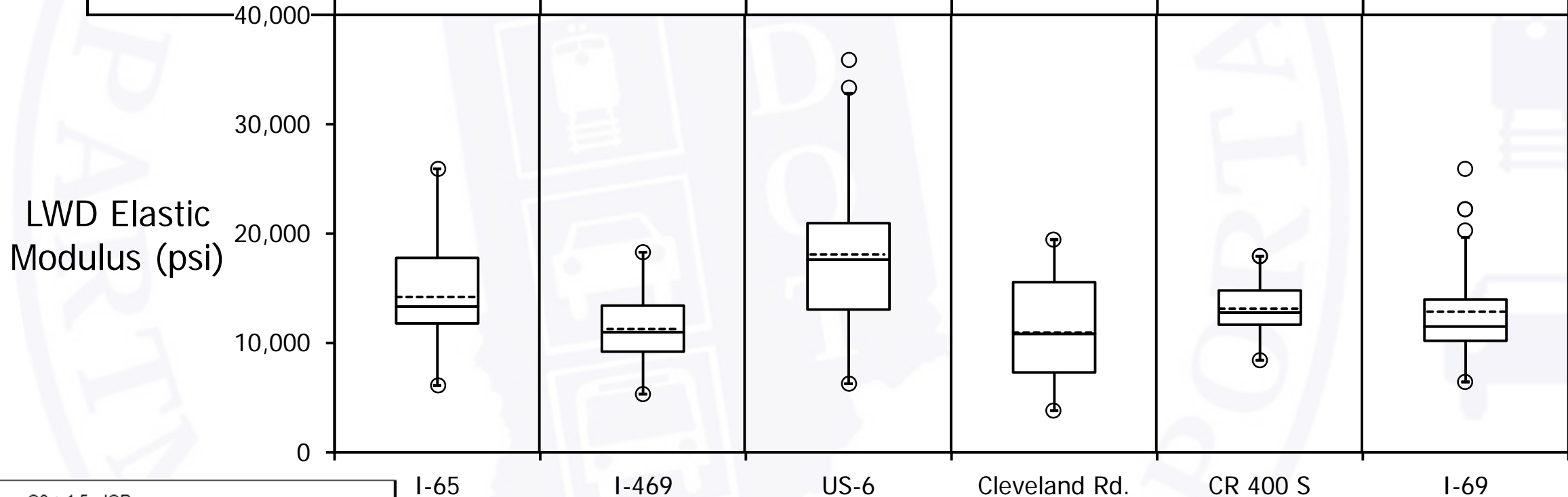
Average	0.239 mm	0.301 mm	0.206 mm	0.356 mm	0.249 mm	0.268 mm
Standard Deviation	0.076 mm	0.098 mm	0.102 mm	0.184 mm	0.059 mm	0.082 mm
Count	40	39	20	17	25	34



Average of all sections: 0.267 mm  
Standard Deviation of all sections: 0.105 mm

# Results of LWD Field Testing(LWD Elastic Modulus)

Average	14,213 psi	11,266 psi	18,081 psi	10,967 psi	13,150 psi	12,857 psi
Standard Deviation	4,147 psi	3,147 psi	7,396 psi	5,066 psi	2,894 psi	4,514
Count	40	39	20	17	25	34

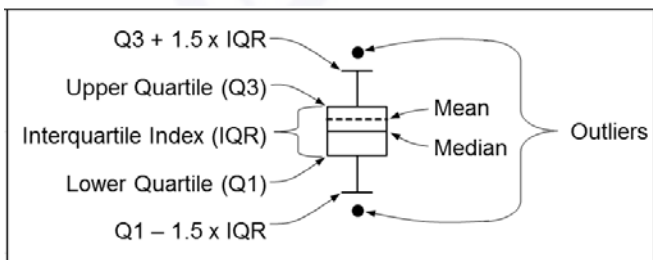
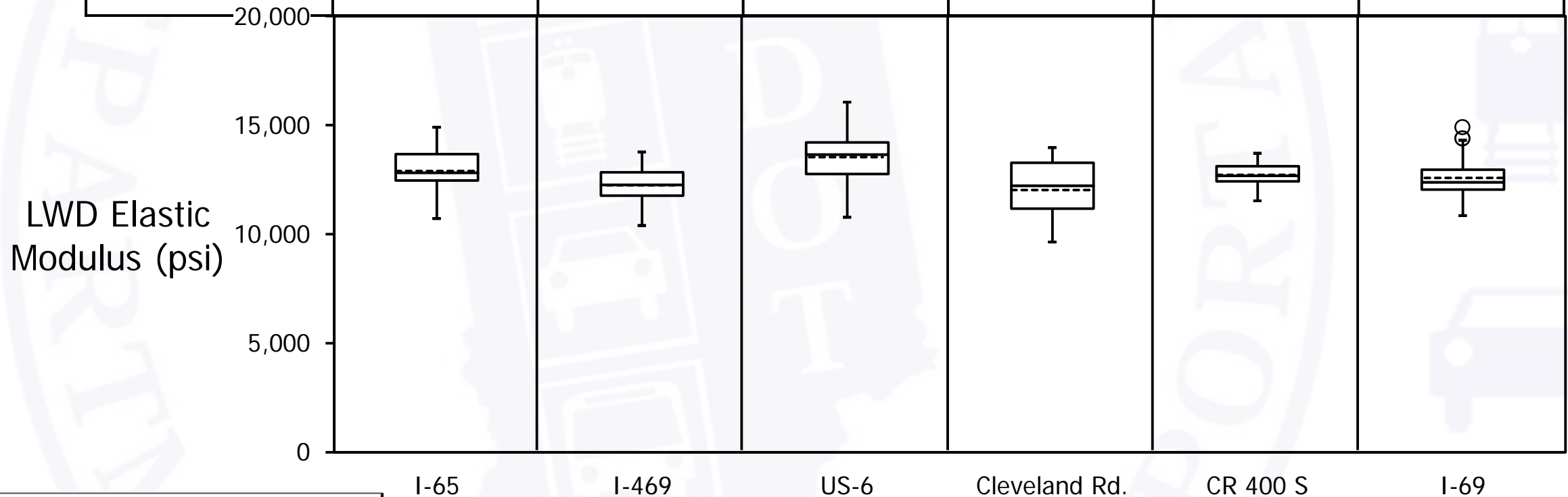


$$E_{LWD} = \frac{F_o(1 - \nu^2)}{2r_o \delta_z}$$

Average of all sections: 13,268 psi  
Standard Deviation of all sections: 4,867 psi

# Results of LWD Field Testing (LWD correlated resilient modulus)

Average	12,903 psi	12,241 psi	13,535 psi	12,020 psi	12,716 psi	12,586 psi
Standard Deviation	873 psi	813 psi	1,309 psi	1,347 psi	657 psi	940 psi
Count	40	39	20	17	25	34



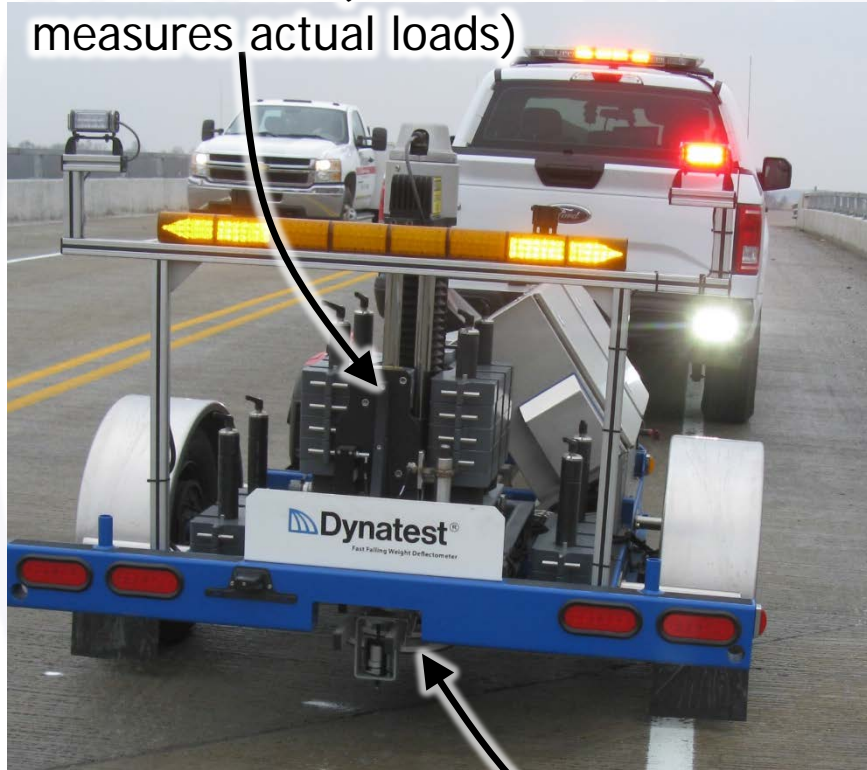
$$M_r = 1480 * E_{LWD}^{0.228}$$

Average of all sections: 12,654 psi

Standard Deviation of all sections: 1,039 psi

# Falling Weight Deflectometer (FWD)

Applies 7 kip, 9 kip, & 11 kip nominal loads (load cell measures actual loads)



11.81 in. diameter loading plate



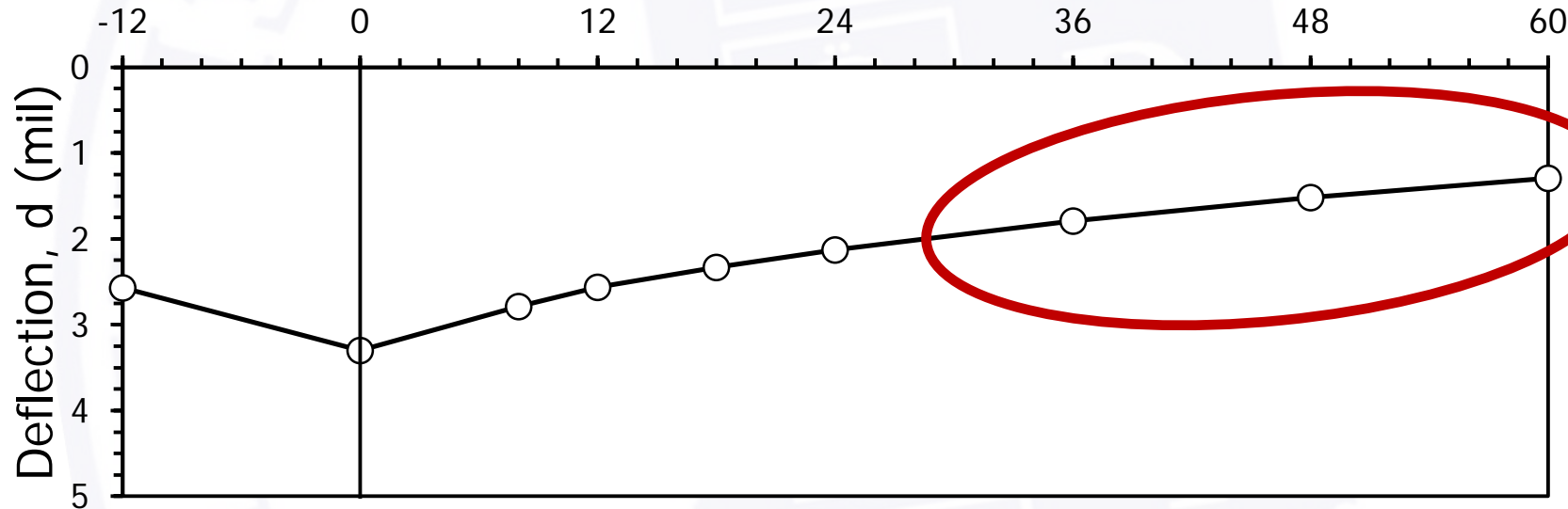
Geophones measuring surface deflection basin to nearest 0.01 mil



# Backcalculation of Subgrade Resilient Modulus from FWD

Example: I-469 NB STA 707+00

Distance from loading plate,  $r$  (in.)



Subgrade is primary source of deflection far away from the loading plate ( $\approx 36$  in.)

$$M_r = C \frac{0.24F_o}{d r}$$

AASHTO (1993)

$M_r$  is resilient Modulus

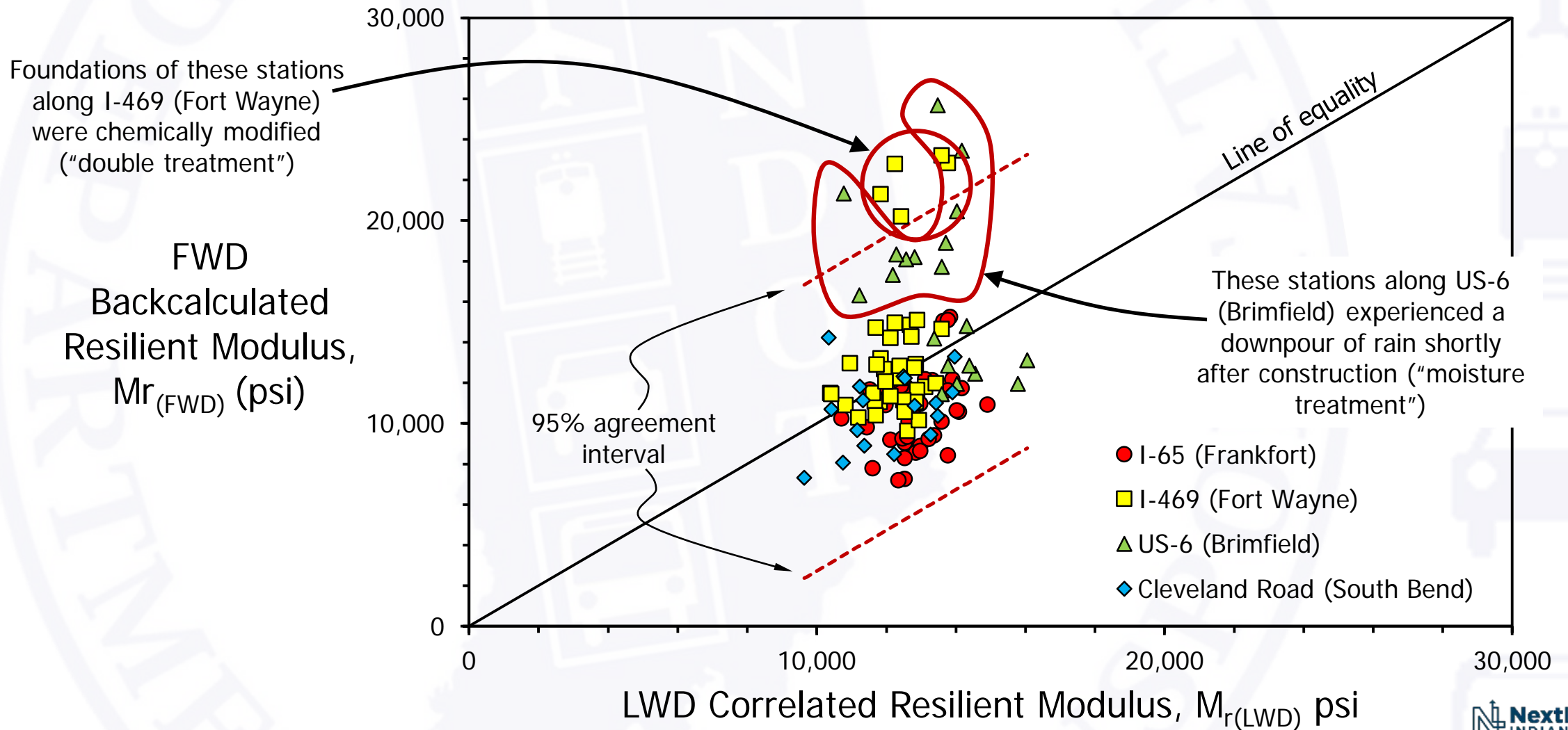
$F_o$  is applied force

$r$  is distance from loading plate

$d$  is surface deflection

$C$  is a correction factor (equals 0.33)

# LWD and FWD Resilient Modulus Agreement



# Key Findings

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- The LWD measures in situ soil stiffness (LWD elastic modulus) that relate to pavement subgrade performance
- Although LWD elastic modulus and resilient modulus are not one and the same, they do correlate well with one another
- Field LWD tests provide validation of proposed LWD elastic modulus and resilient modulus correlation
- Resilient moduli correlated from LWD testing are in agreement with resilient moduli backcalculated from FWD testing

# Future Work

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- Improve correlation between predicted LWD deflection and resilient modulus (more samples from more soil types)
- LWD and FWD measurements from INDOT contracts during the 2019 construction season
  - Use better model for backcalculating resilient modulus from FWD
- Provide recommendations for subgrade construction acceptance
  - Maximum LWD deflection
  - Testing frequency
  - Effect of curing time
- Publish findings in JTRP technical report

# Acknowledgements

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Thank you for your attention

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