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# Truncated Singular Value Decomposition Method for Mitigating Unwanted Enhancement in Active Noise Control Systems

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# Truncated Singular Value Decomposition Method for Mitigating Unwanted Enhancement in Active Noise Control Systems

\* This presentation is a part of the INTER-NOISE 2018 Student Paper Competition.

Xuchen Wang, Yangfan Liu, J. Stuart Bolton

(INCE-USA Student Associate)

Ray W. Herrick Laboratories, Purdue University



INTER-NOISE **2018**  
Impact of Noise Control Engineering

26-29 **AUGUST**  
CHICAGO, ILLINOIS



\* This project is the work of Xuchen Wang, under supervision of Dr. Yangfan Liu and Dr. J. Stuart Bolton.

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Problem  
Introduction

# Introduction

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- MIMO Active Noise Control (ANC) Problem



- Noise Control in Open Region



- Application: Range Hood, Headrest etc.



# Introduction

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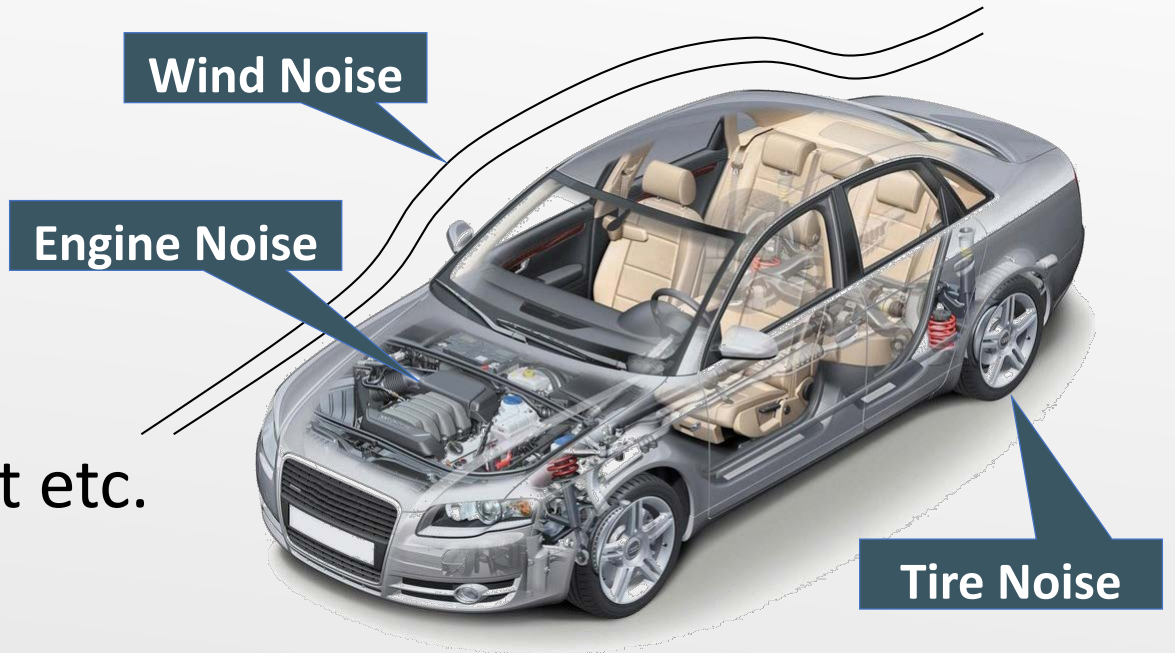
- MIMO Active Noise Control (ANC) Problem



- Noise Control in Open Region



- Application: Range Hood, Headrest etc.



# Enhancement Problem

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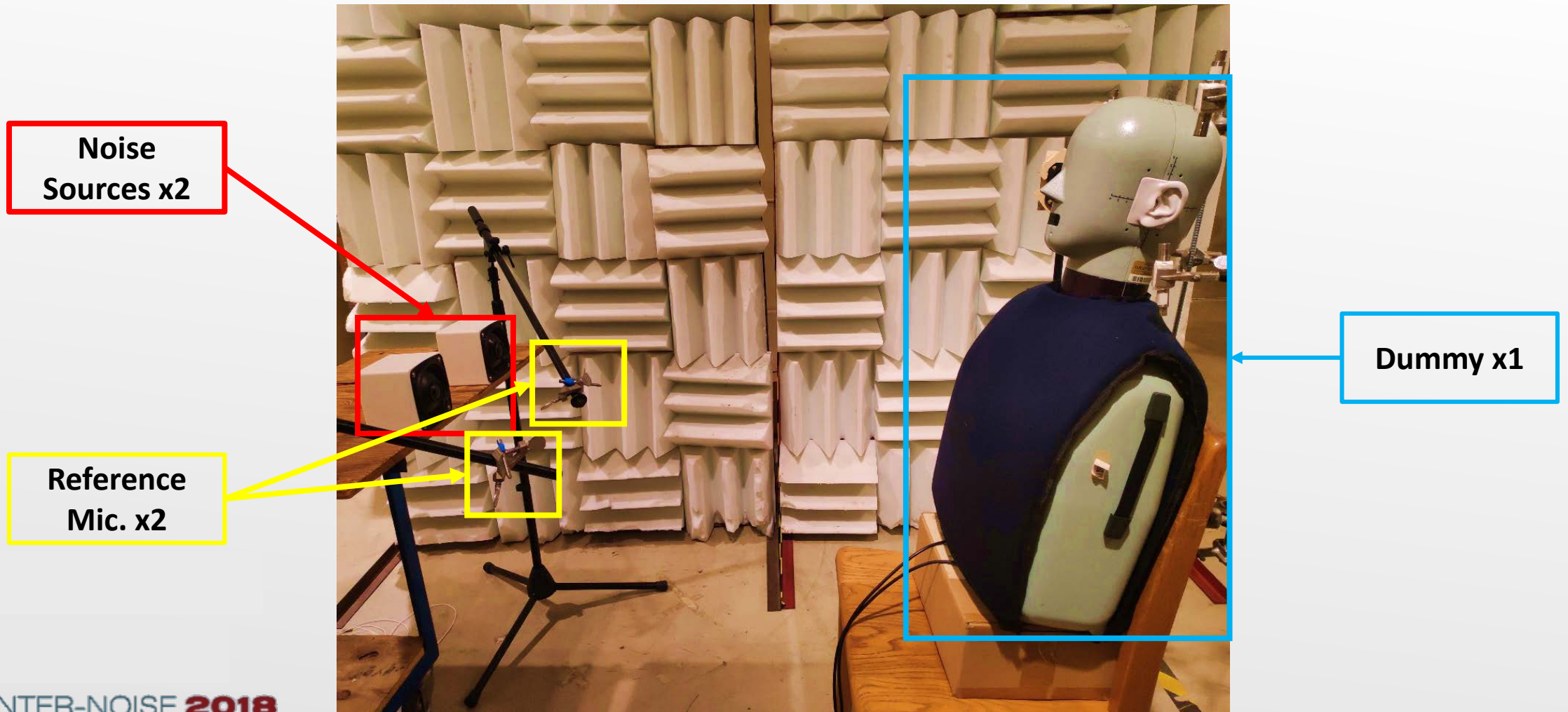
- Possible Reasons:

- System Delay
- Feedback Path Cancellation
- Correlated Reference Signals
- ...

- Focus:

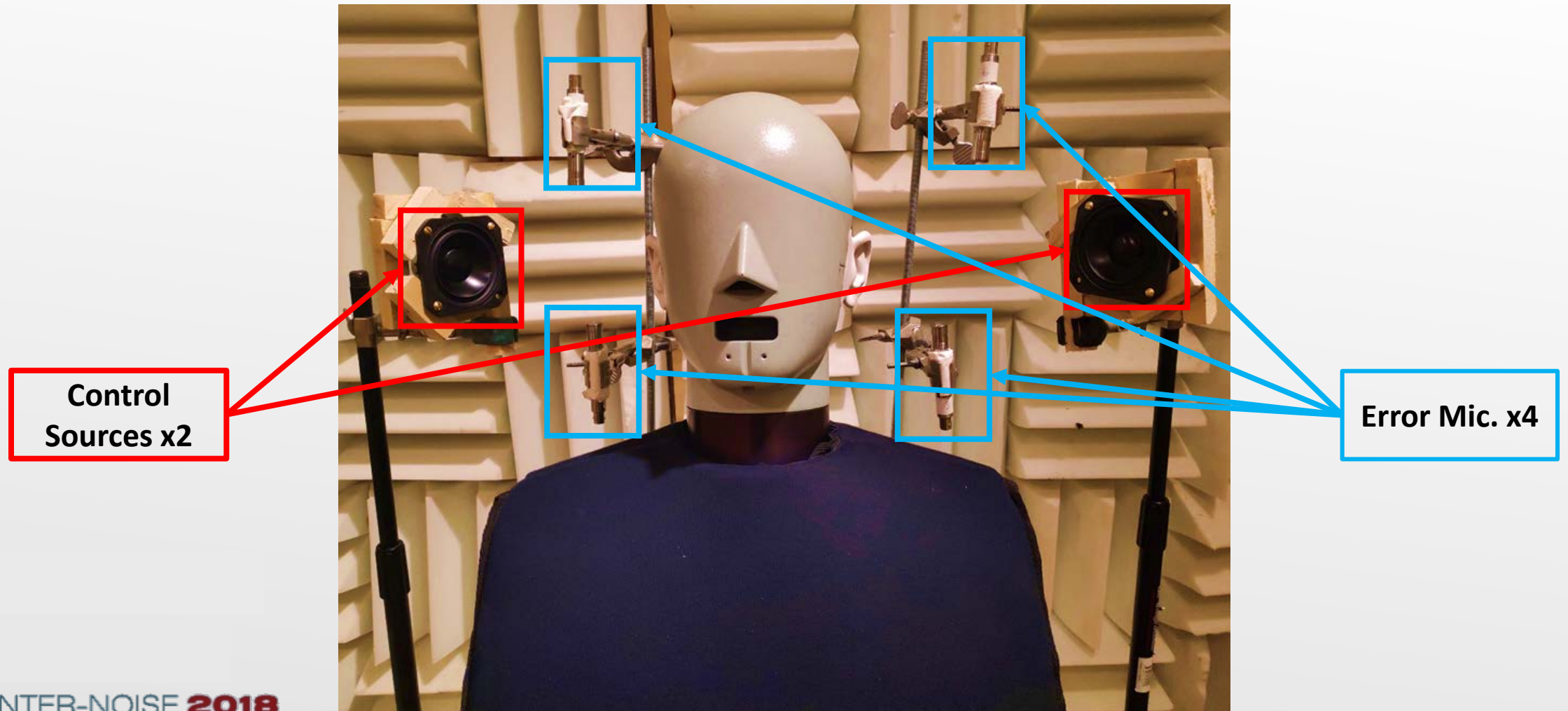
- Correlated Reference Signals Problem in MIMO Feed-forward Non-adaptive Active Noise Control System

# Experiment Setup

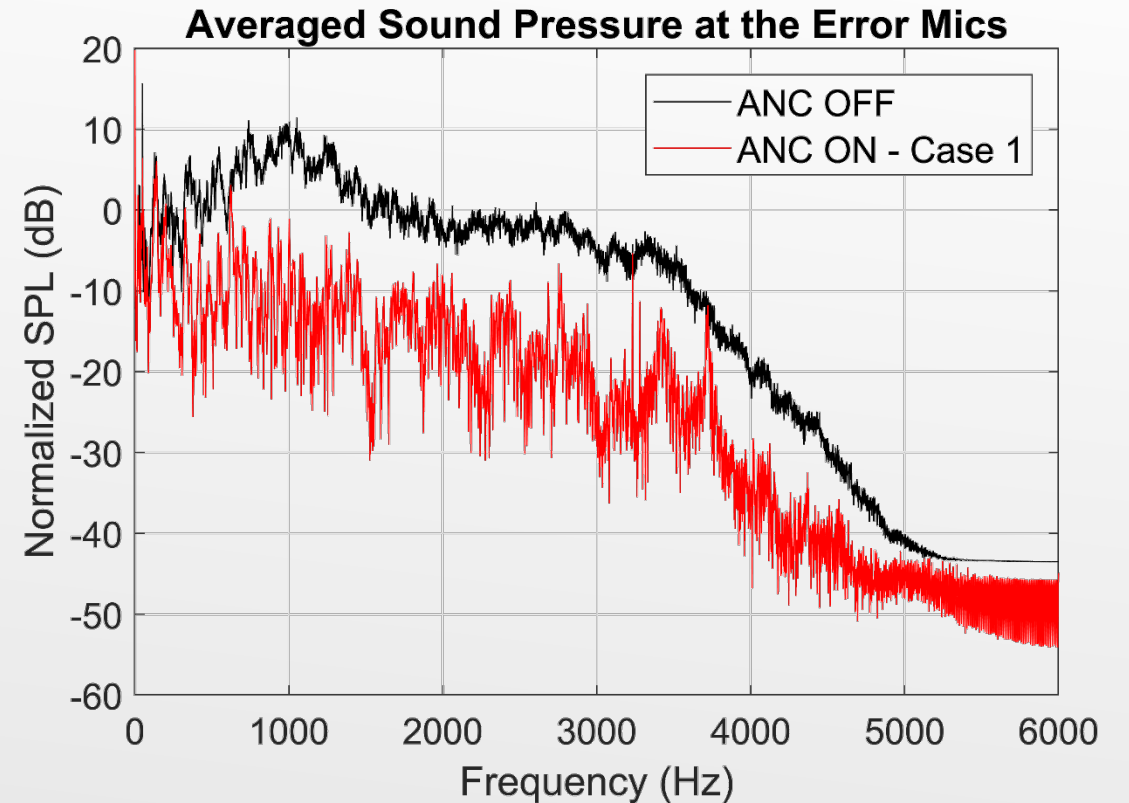
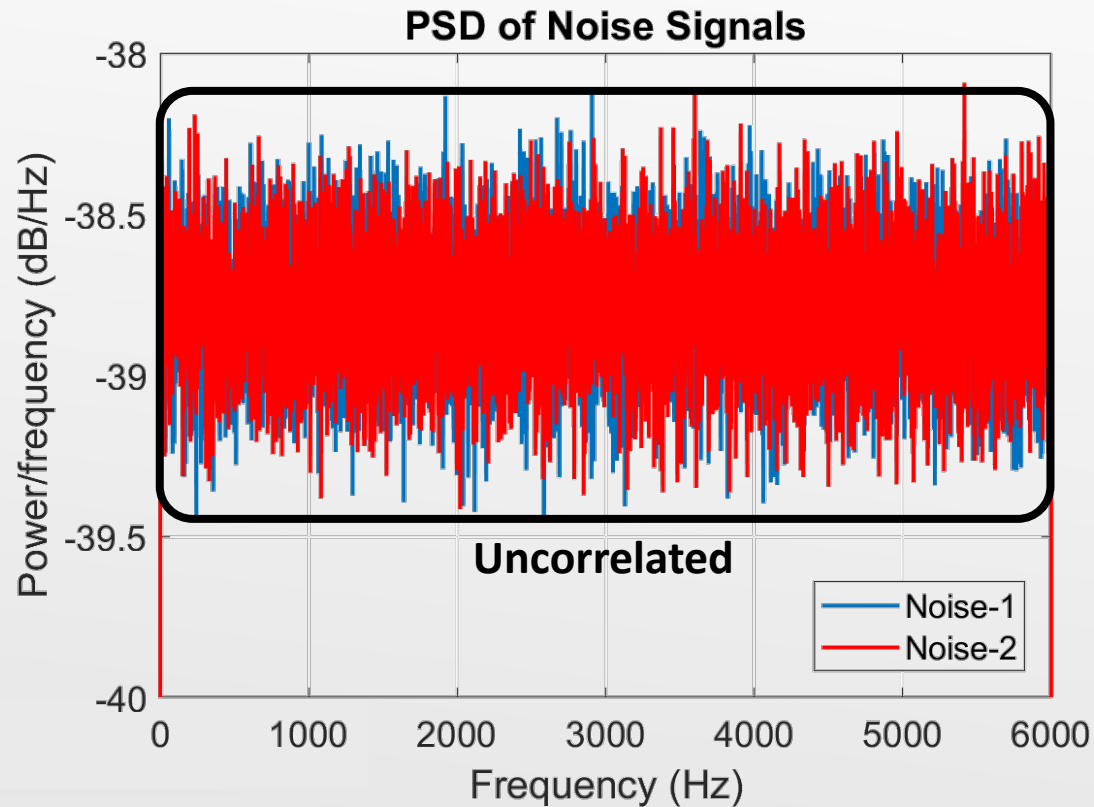




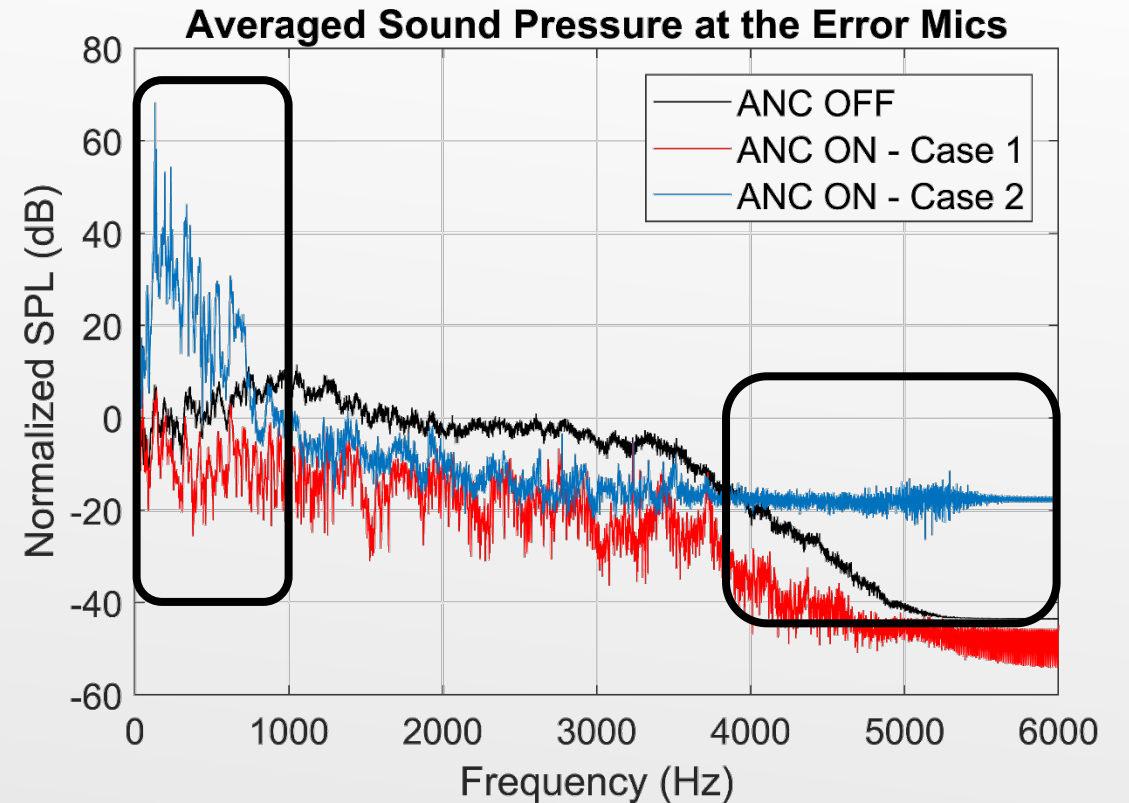
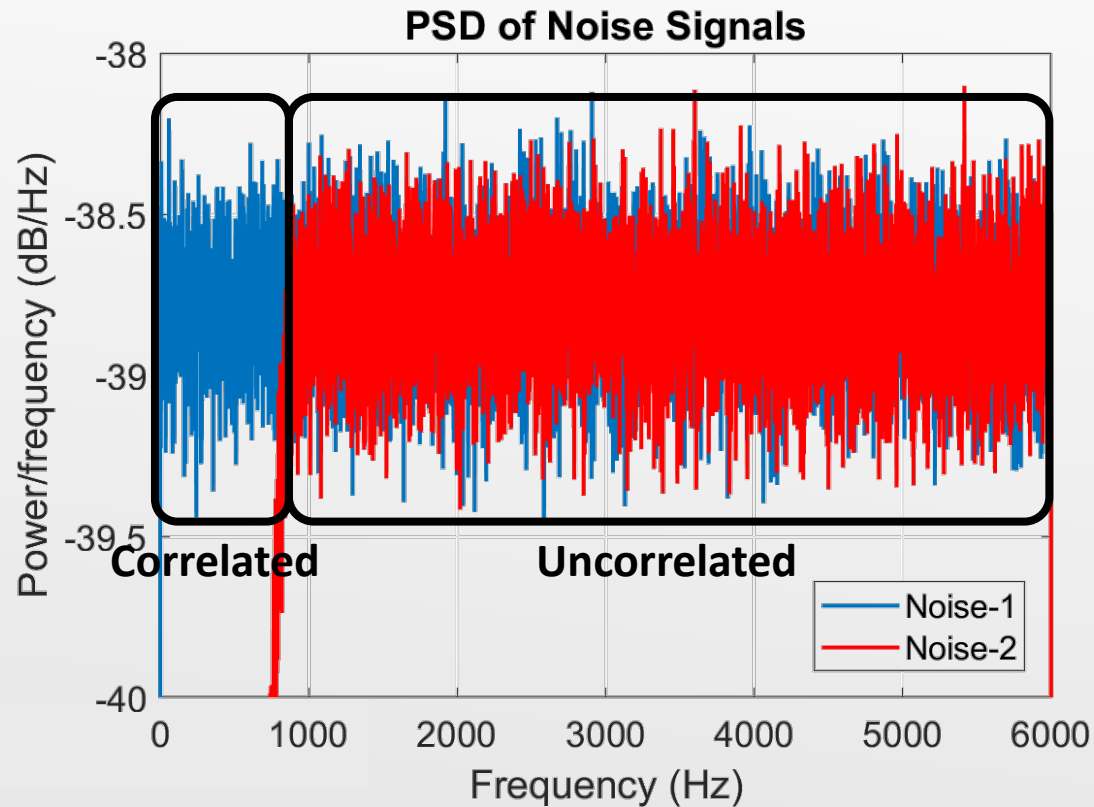
# Experiment Setup

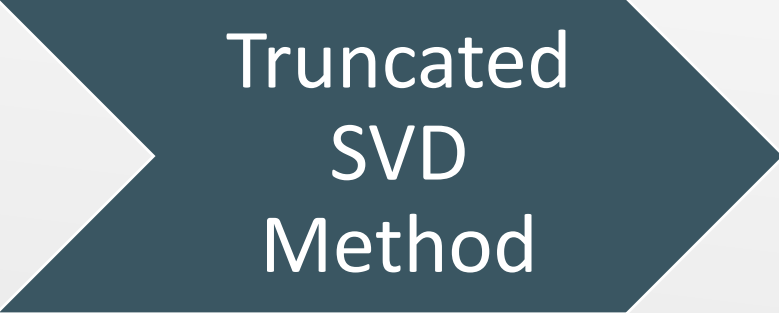


# Case 1



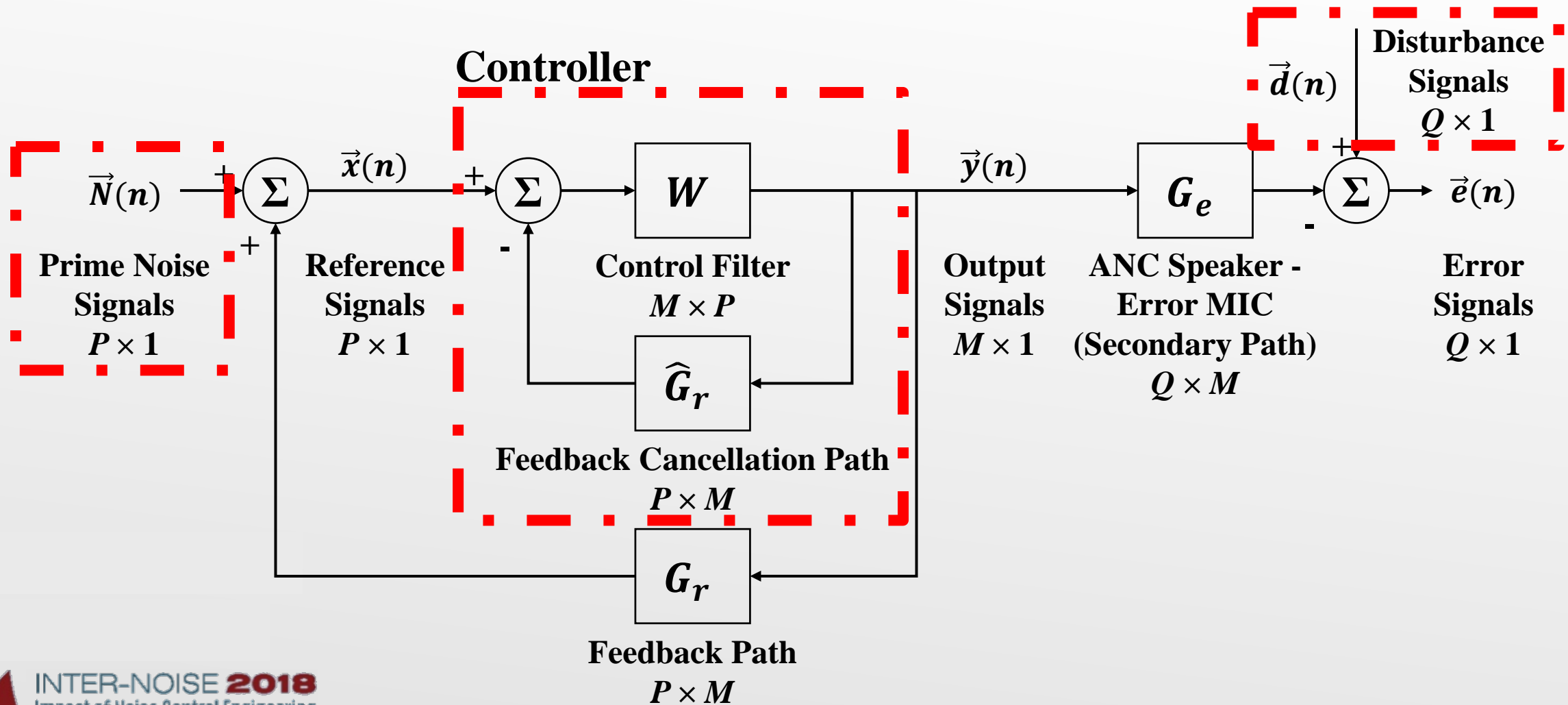
# Case 2





Truncated  
SVD  
Method

# Feed-forward Active Noise Control System



# Coefficients of Controller

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\*S. J. Elliott, *Signal processing for active control*, Elsevier, (2000).

$$J = E[\vec{e}^T(n) \cdot \vec{e}(n)] = \vec{w}^T A \vec{w} + 2\vec{w}^T \vec{b} + c$$

$$\vec{w}_{opt} = -A^{-1} \vec{b}$$

$A$  – Autocorrelation function of the filtered reference signals

$\vec{b}$  – Cross-correlation function between the filtered reference signals and the disturbance signals

$c$  – Autocorrelation function of the disturbance signals

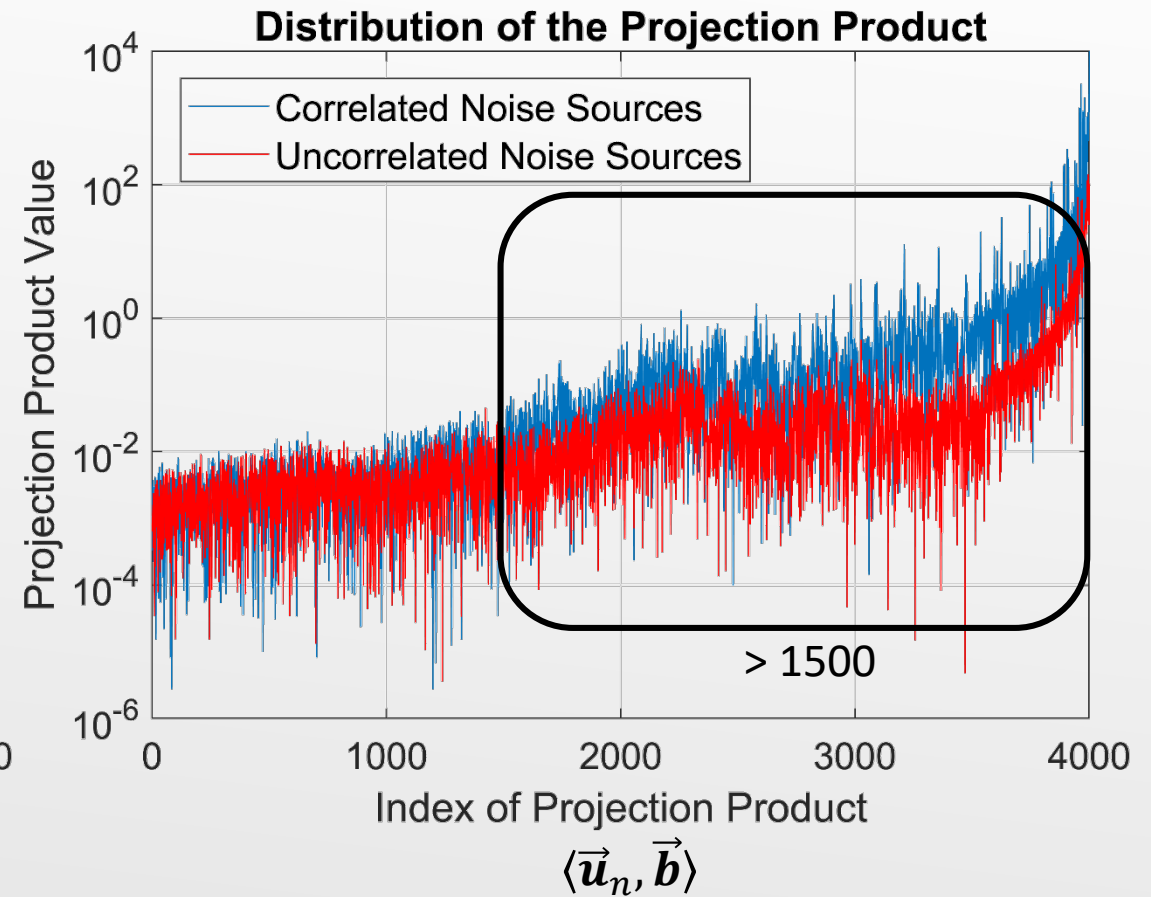
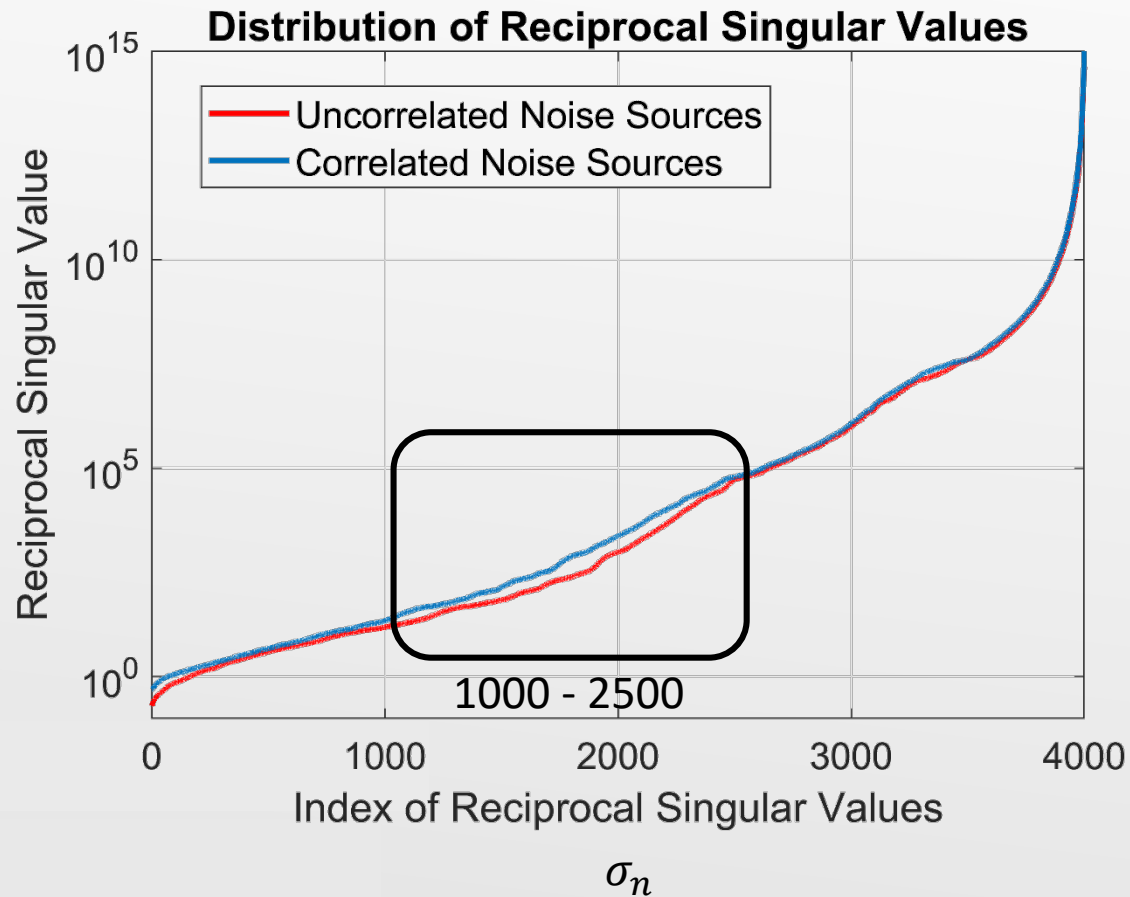
# Singular Value Decomposition Analysis

**SVD** is used to analysis the autocorrelation function of the filtered reference signals.

$$A = U\Sigma U^T = [\vec{u}_1 \cdots \vec{u}_N] \begin{bmatrix} \sigma_1 & \cdots & 0 \\ \vdots & \ddots & \vdots \\ 0 & \cdots & \sigma_N \end{bmatrix} \begin{bmatrix} \vec{u}_1 \\ \vdots \\ \vec{u}_N \end{bmatrix}$$

$$\vec{w}_{opt} = -[\vec{u}_1 \cdots \vec{u}_N] \begin{bmatrix} \sigma_1^{-1} & \cdots & 0 \\ \vdots & \ddots & \vdots \\ 0 & \cdots & \sigma_N^{-1} \end{bmatrix} \begin{bmatrix} \vec{u}_1 \\ \vdots \\ \vec{u}_N \end{bmatrix} \vec{b} = -\sum_{n=1}^N \sigma_n^{-1} \langle \vec{u}_n, \vec{b} \rangle \vec{u}_n$$

# Singular Values & Projection Product





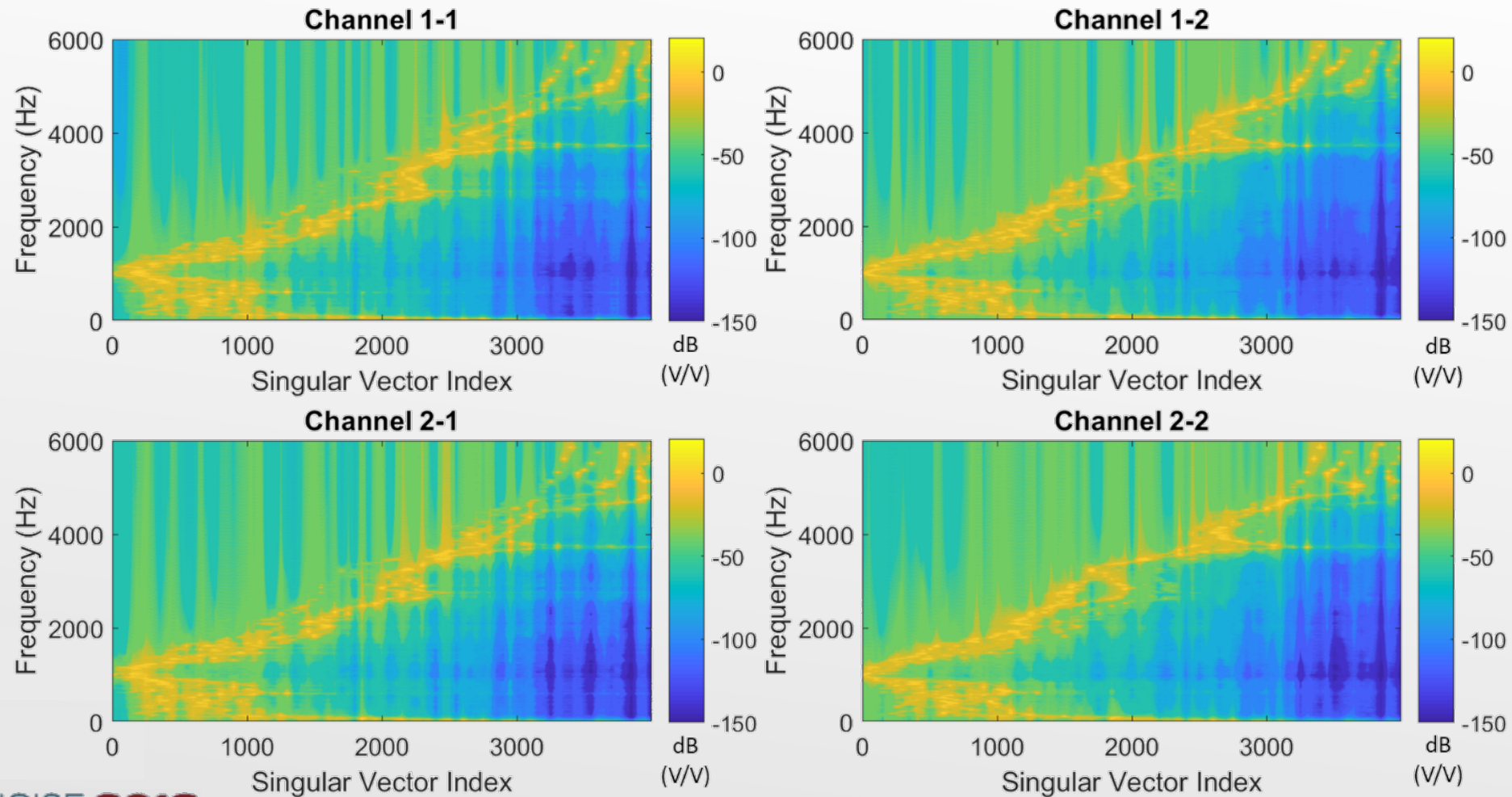
# Singular Value Decomposition Analysis

**SVD** is used to analysis the autocorrelation function of the filtered reference signals.

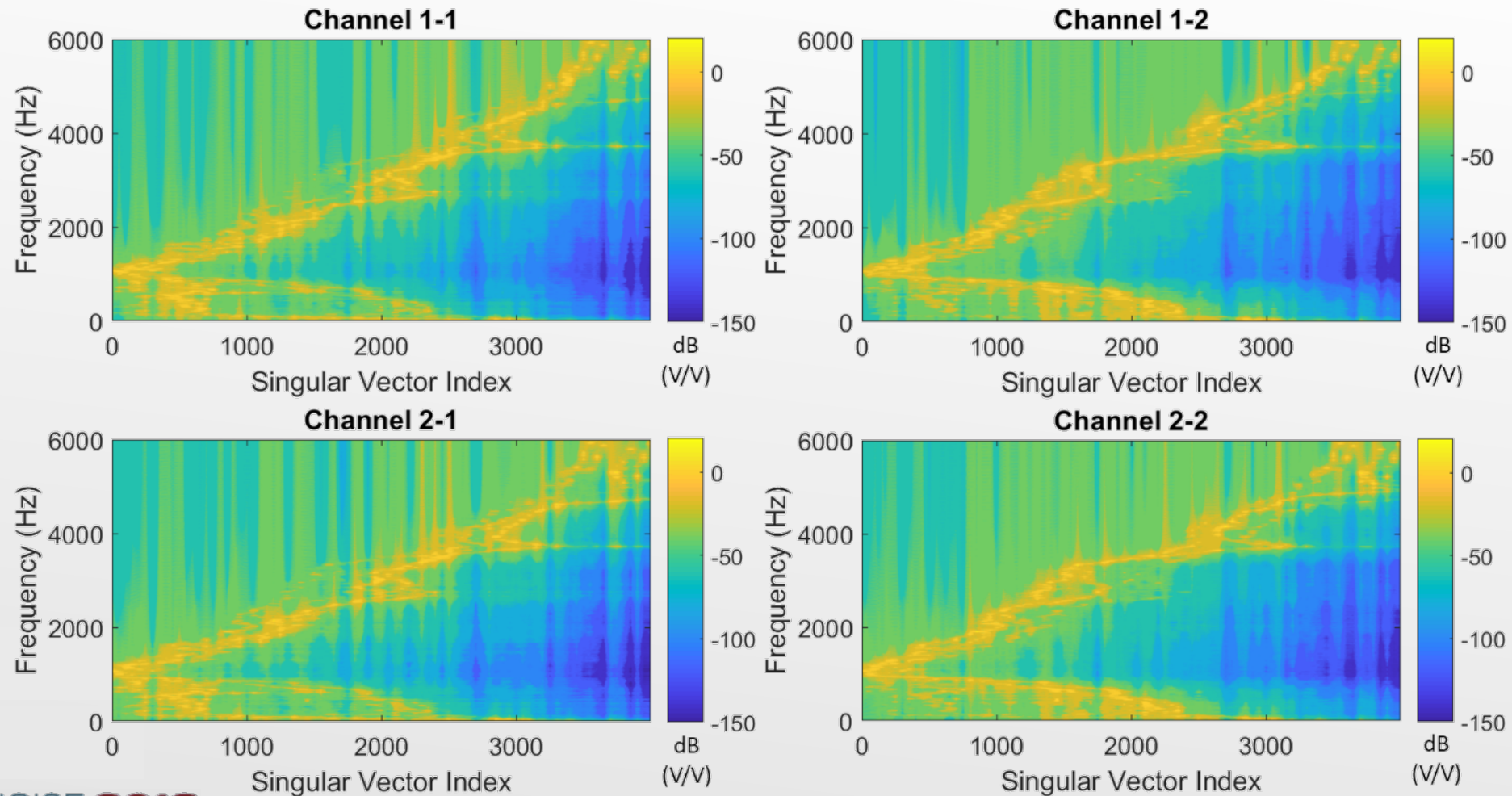
$$A = U\Sigma U^T = [\vec{u}_1 \cdots \vec{u}_N] \begin{bmatrix} \sigma_1 & \cdots & 0 \\ \vdots & \ddots & \vdots \\ 0 & \cdots & \sigma_N \end{bmatrix} \begin{bmatrix} \vec{u}_1 \\ \vdots \\ \vec{u}_N \end{bmatrix}$$

$$\vec{w}_{opt} = -[\vec{u}_1 \cdots \vec{u}_N] \begin{bmatrix} \sigma_1^{-1} & \cdots & 0 \\ \vdots & \ddots & \vdots \\ 0 & \cdots & \sigma_N^{-1} \end{bmatrix} \begin{bmatrix} \vec{u}_1 \\ \vdots \\ \vec{u}_N \end{bmatrix} \vec{b} = -\sum_{n=1}^N \sigma_n^{-1} \langle \vec{u}_n, \vec{b} \rangle \vec{u}_n$$

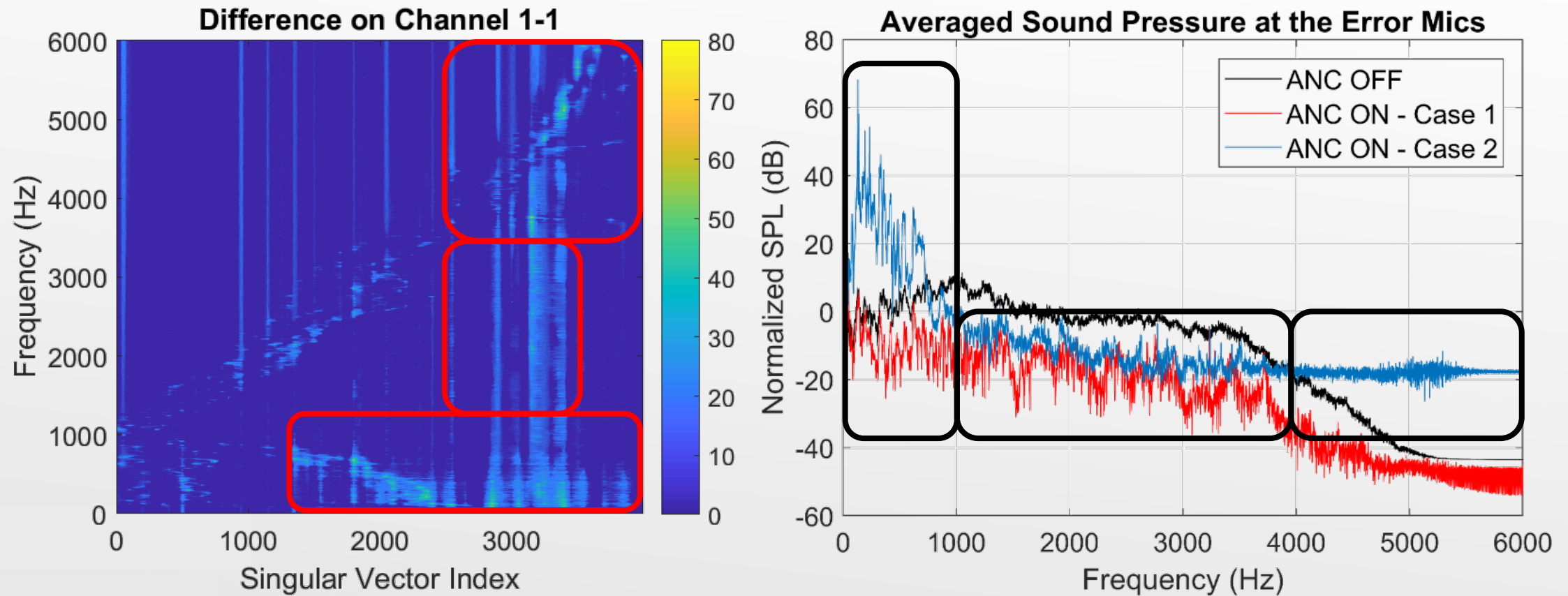
# Uncorrelated Noise Sources Case



# Correlated Noise Sources Case



# Comparison of Two Cases

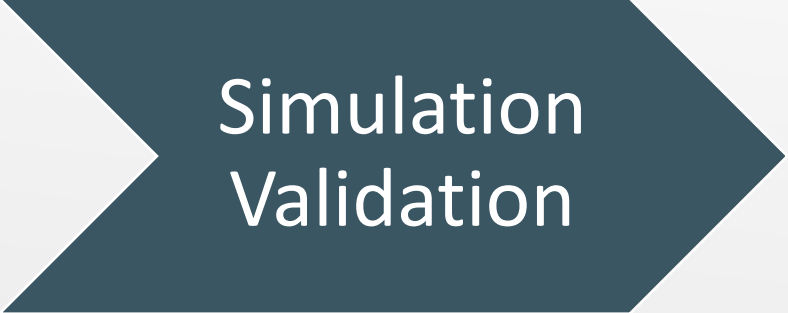


# Truncated Singular Value Decomposition Method

$l$  : Truncation Point

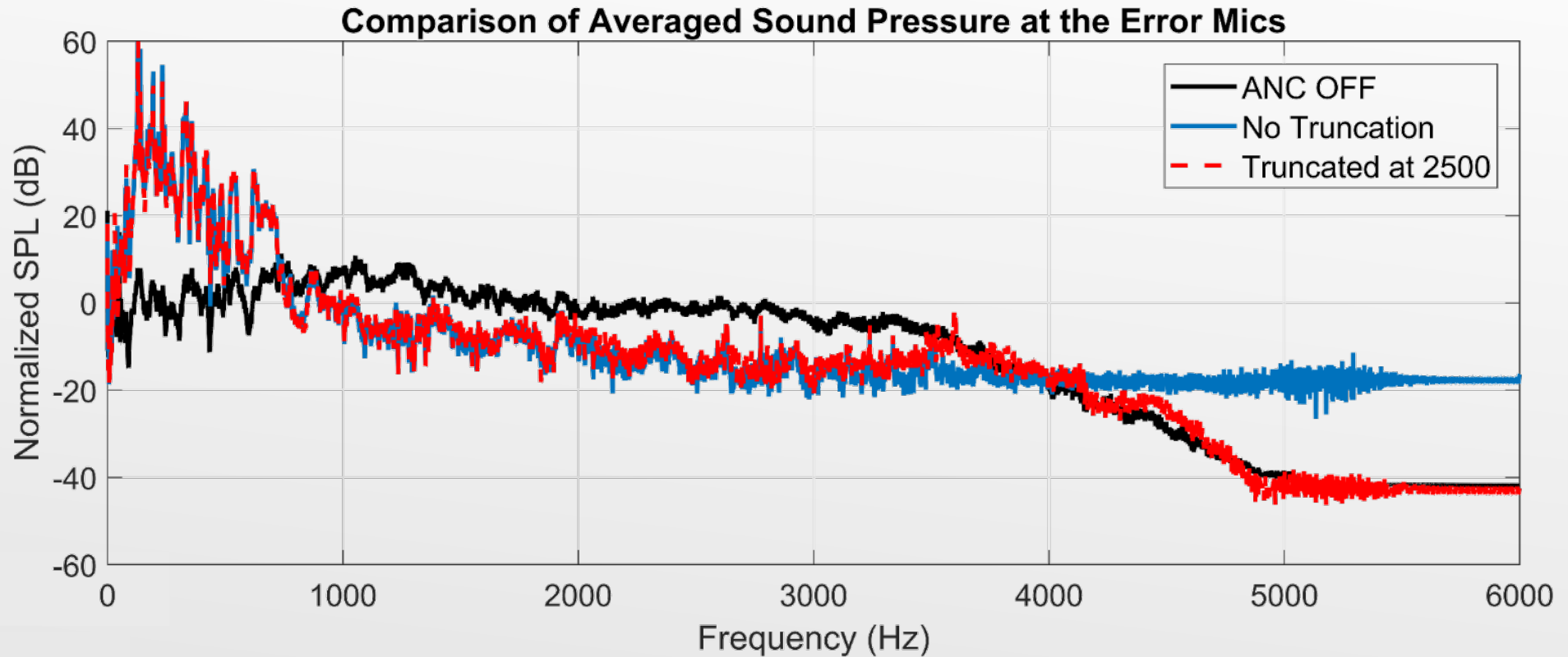
$$\vec{w}_{opt} = -[\vec{u}_1 \cdots \vec{u}_N] \begin{bmatrix} \sigma_1^{-1} & \cdots & 0 \\ \vdots & \ddots & \vdots \\ 0 & \cdots & \sigma_N^{-1} \end{bmatrix} \begin{bmatrix} \vec{u}_1 \\ \vdots \\ \vec{u}_N \end{bmatrix} \vec{b} = -\sum_{n=1}^N \sigma_n^{-1} \langle \vec{u}_n, \vec{b} \rangle \vec{u}_n$$

$$\vec{w}_{opt}^* = -[\vec{u}_1 \cdots \vec{u}_l] \begin{bmatrix} \sigma_1^{-1} & \cdots & 0 \\ \vdots & \ddots & \vdots \\ 0 & \cdots & \sigma_l^{-1} \end{bmatrix} \begin{bmatrix} \vec{u}_1 \\ \vdots \\ \vec{u}_l \end{bmatrix} \vec{b} = -\sum_{n=1}^l \sigma_n^{-1} \langle \vec{u}_n, \vec{b} \rangle \vec{u}_n$$

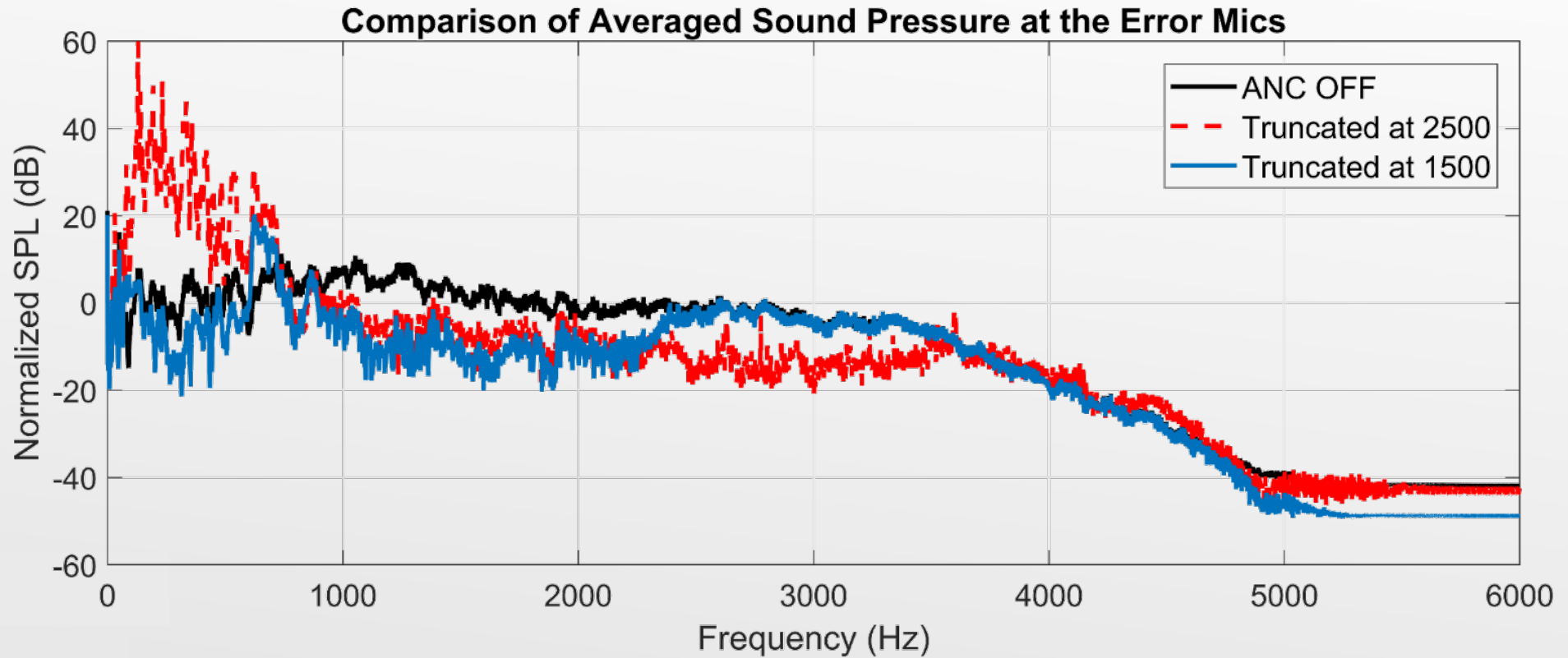


Simulation  
Validation

# Simulation Validation

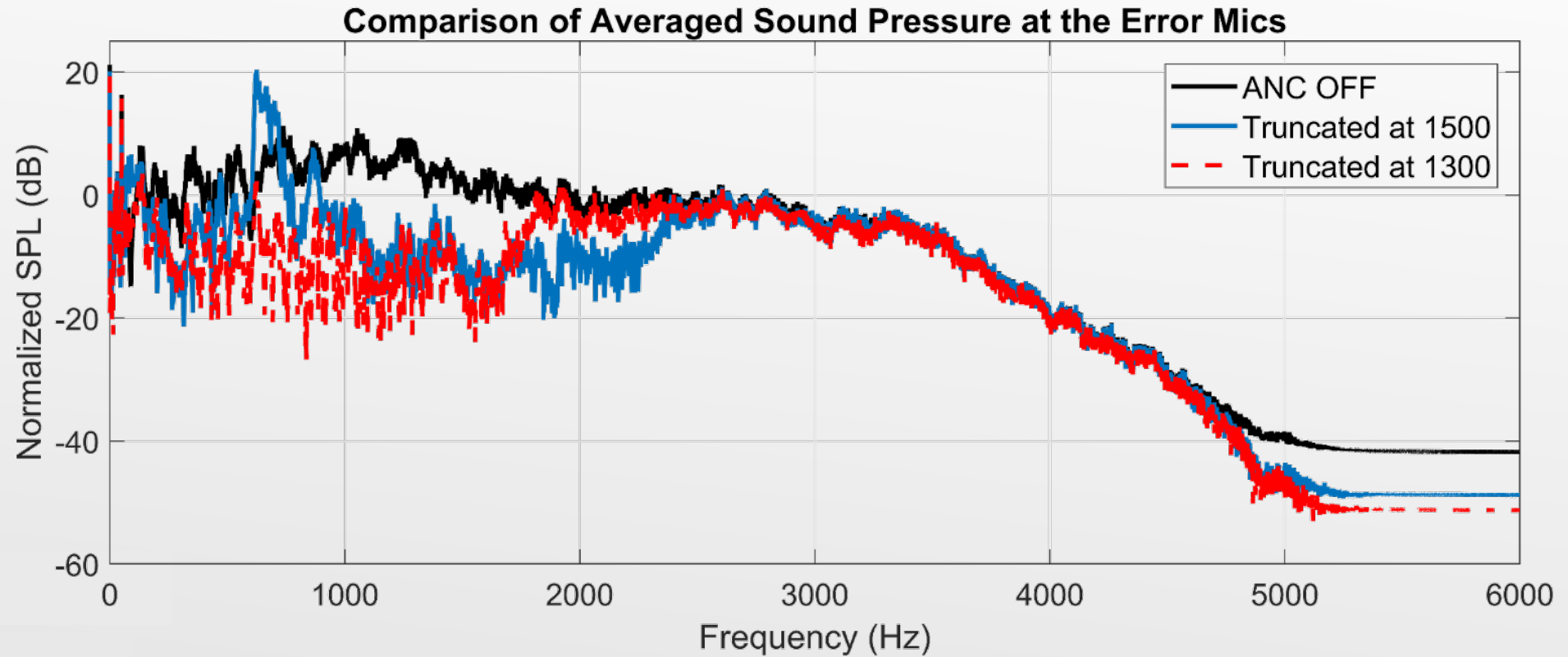


# Simulation Validation

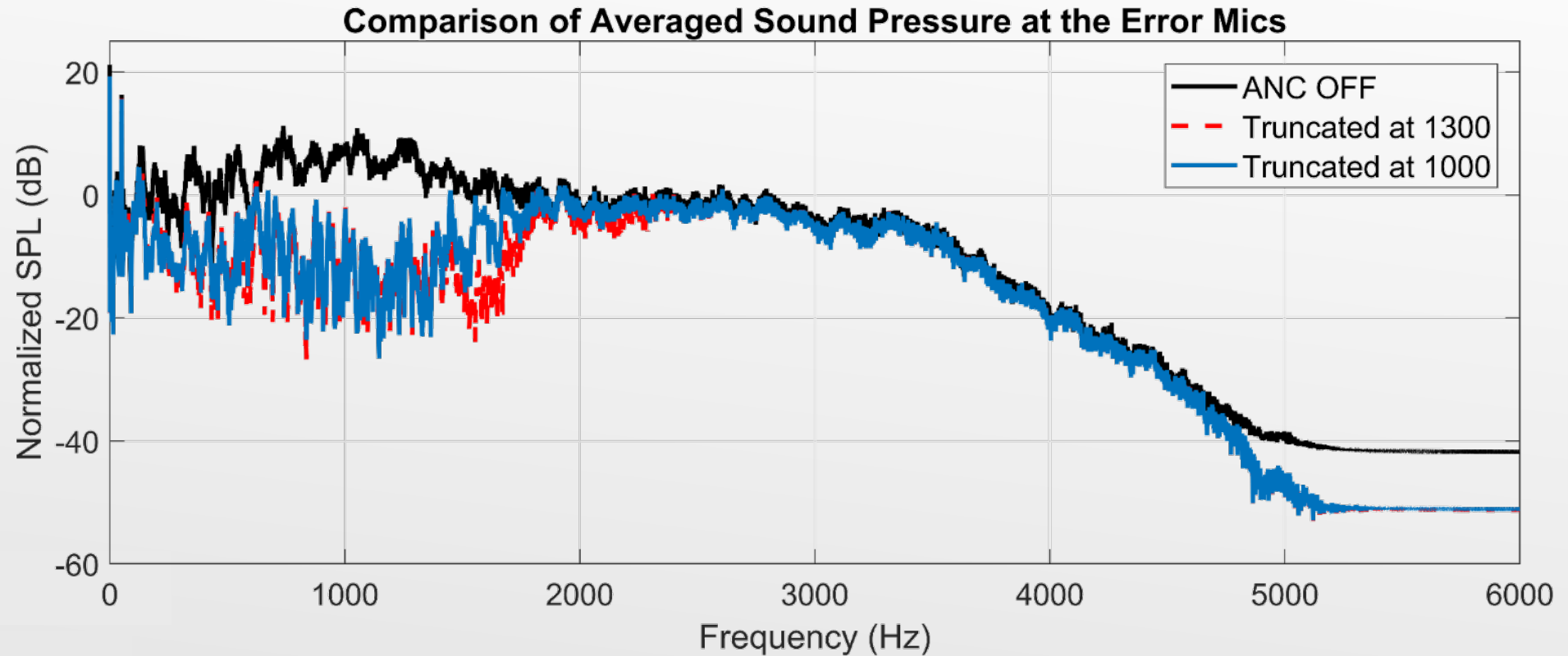




# Simulation Validation



# Simulation Validation



# Conclusions

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- The large reciprocal of singular values  $\sigma_n^{-1}$  and the projection product of  $\langle \vec{u}_n, \vec{b} \rangle$  are two causes of the noise enhancement.
- The singular vectors of some indices contribute to both noise enhancement and noise cancellation.
- Still need more tries to find the best index for truncation point to improve the performance or mitigate the unwanted enhancement.

*Thank you!*