

7-10-2018

# Finite Element Study of Acoustic Mode Force Transmission in a Loaded, Structural-Acoustical Tire Model

Rui Cao

*Purdue University*, cao101@purdue.edu

J Stuart Bolton

*Purdue University*, bolton@purdue.edu

Follow this and additional works at: <https://docs.lib.purdue.edu/herrick>

---

Cao, Rui and Bolton, J Stuart, "Finite Element Study of Acoustic Mode Force Transmission in a Loaded, Structural-Acoustical Tire Model" (2018). *Publications of the Ray W. Herrick Laboratories*. Paper 175.  
<https://docs.lib.purdue.edu/herrick/175>

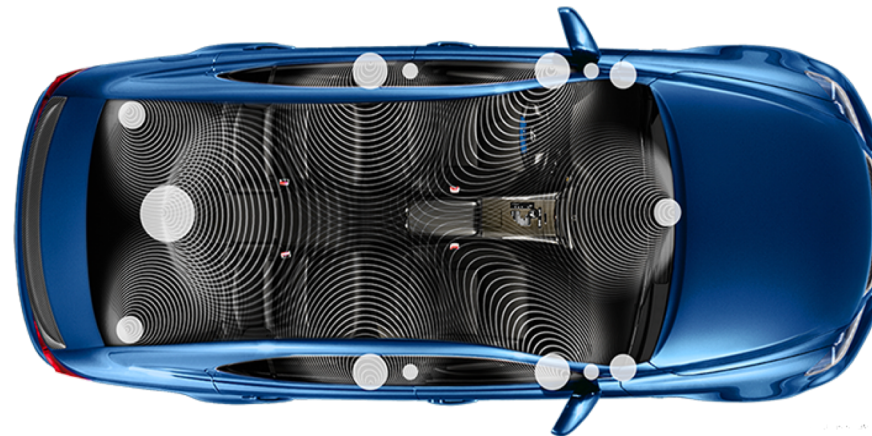
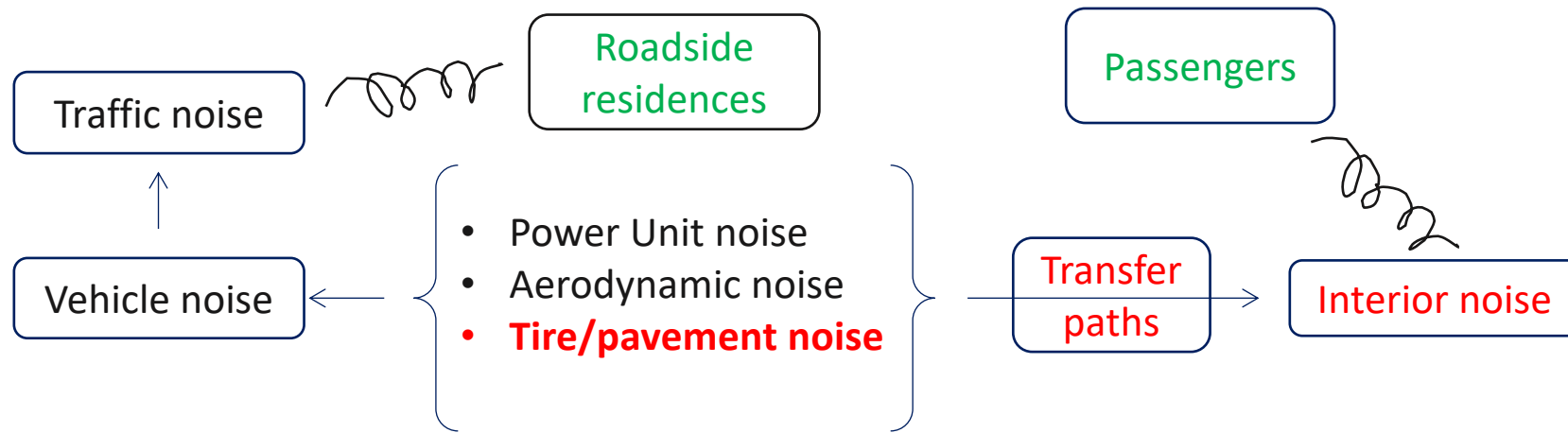
This document has been made available through Purdue e-Pubs, a service of the Purdue University Libraries. Please contact [epubs@purdue.edu](mailto:epubs@purdue.edu) for additional information.

# Force transmission characteristics for a loaded structural-acoustic tire model

Ray W. Herrick Laboratories,  
Purdue University, USA  
Rui Cao and J. Stuart Bolton  
07/10 2018



# I. Introduction



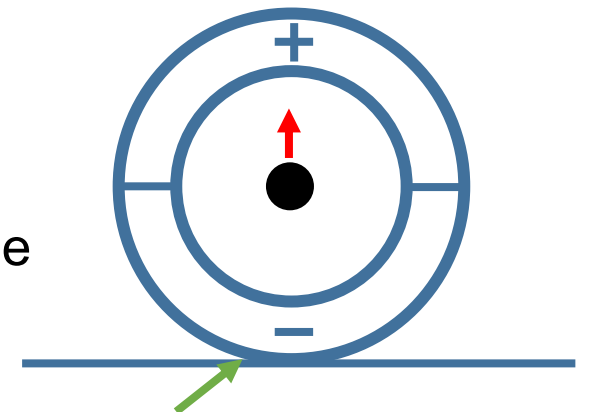
# I. Introduction

---

- High frequency interior noise is mostly airborne and usually is not associated with structural vibration from road excitation. However, low frequency noise, has a strong association with structural vibration and can be perceived by the passengers.
- A major component of structure-borne noise comes from the tire's acoustic cavity mode near 200 Hz

**Why do two tires of same size and geometry, from different manufacturers, have very different responses, in terms of cavity noise perception?**

- Study force transmission from contact patch excitation to rim center
- How the cavity resonance may affect force transmission
- Ways of identifying bad tires/good tires, in terms of structure-borne noise





## II. Finite element tire model

---

**A Finite Element structural-acoustical tire model was created to investigate the tire cavity-induced structure-borne noise**

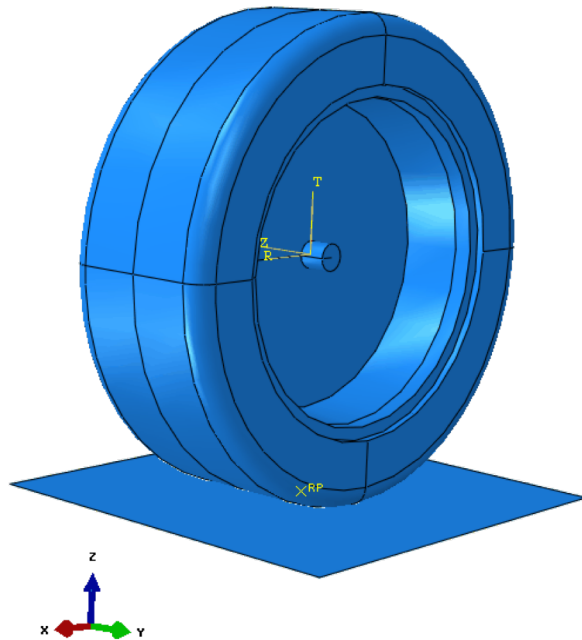
- Create realistic tire-road contact patch
- Point excitation at the contact patch edge
- Calculate dispersion relation in tire tread to identify vibration modes, as from test results
- Calculate force transmission from excitation location to the rim center, to act as input for full vehicle analysis
- Comparison study to identify the influencing factors

## II. Finite element tire model

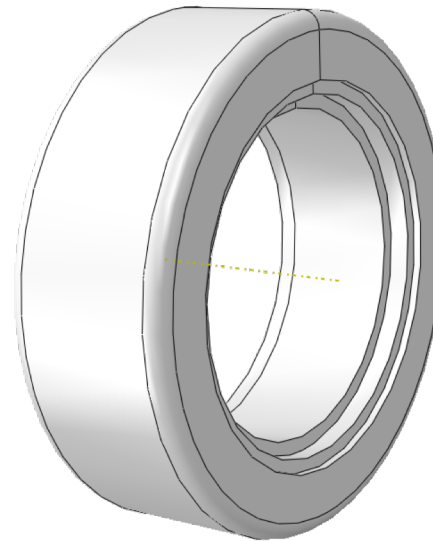
---

**All modeling was performed in Abaqus 6.13**

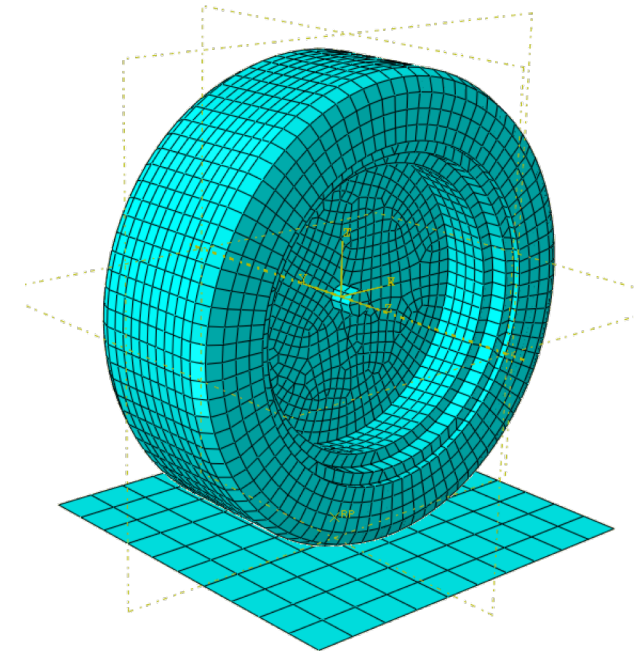
Assembled model



Air cavity model



Meshed assembled model



A 245/40R20 tire was used for dimension

## II. Finite element tire model

---

All parts are using homogeneous material

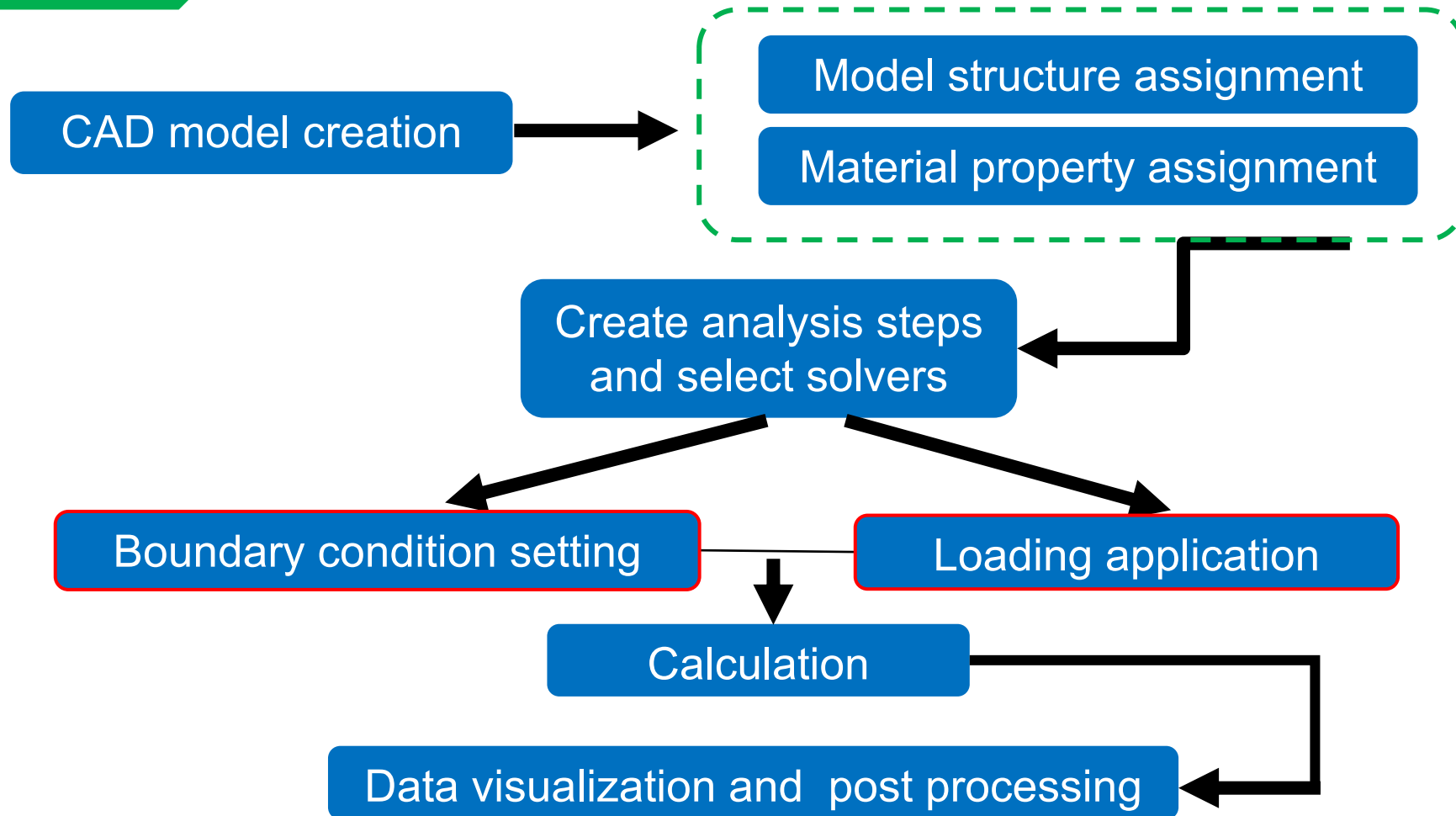
Part	Density [kg/m <sup>3</sup> ]	Modulus [Pa]	Thickness [mm]	Poisson's ratio
Rim	2700	$7 \times 10^{12}$	10	0.3
Tread	1200	$7.5 \times 10^8$	10	0.45
Sidewall	800	$5 \times 10^7$	8	0.45
Air	1.204	149180	N/A	N/A

- ❖ Material properties were simplified and approximated
- ❖ Rim was set to be very stiff, so its resonances were above the frequency of interest in this study
- ❖ Air bulk modulus was given at 97 °F

# III. Analysis process

---

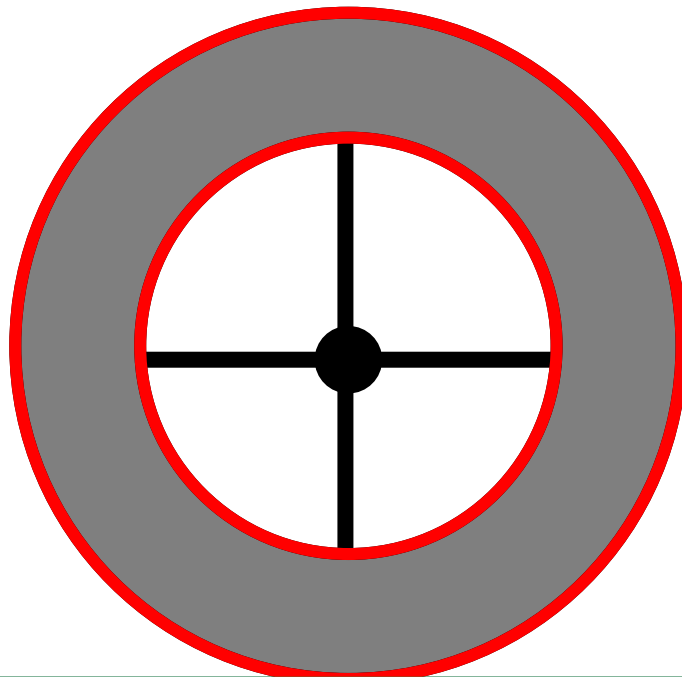
## Overview



# III. Analysis process

---

## Boundary conditions



### ***Continuity boundary***

Tread – Air Cavity

Sidewall – Air Cavity

Rim – Air Cavity

“TIE” function was applied to enforce the two surfaces stay in contact at all times

### ***Contact boundary:***

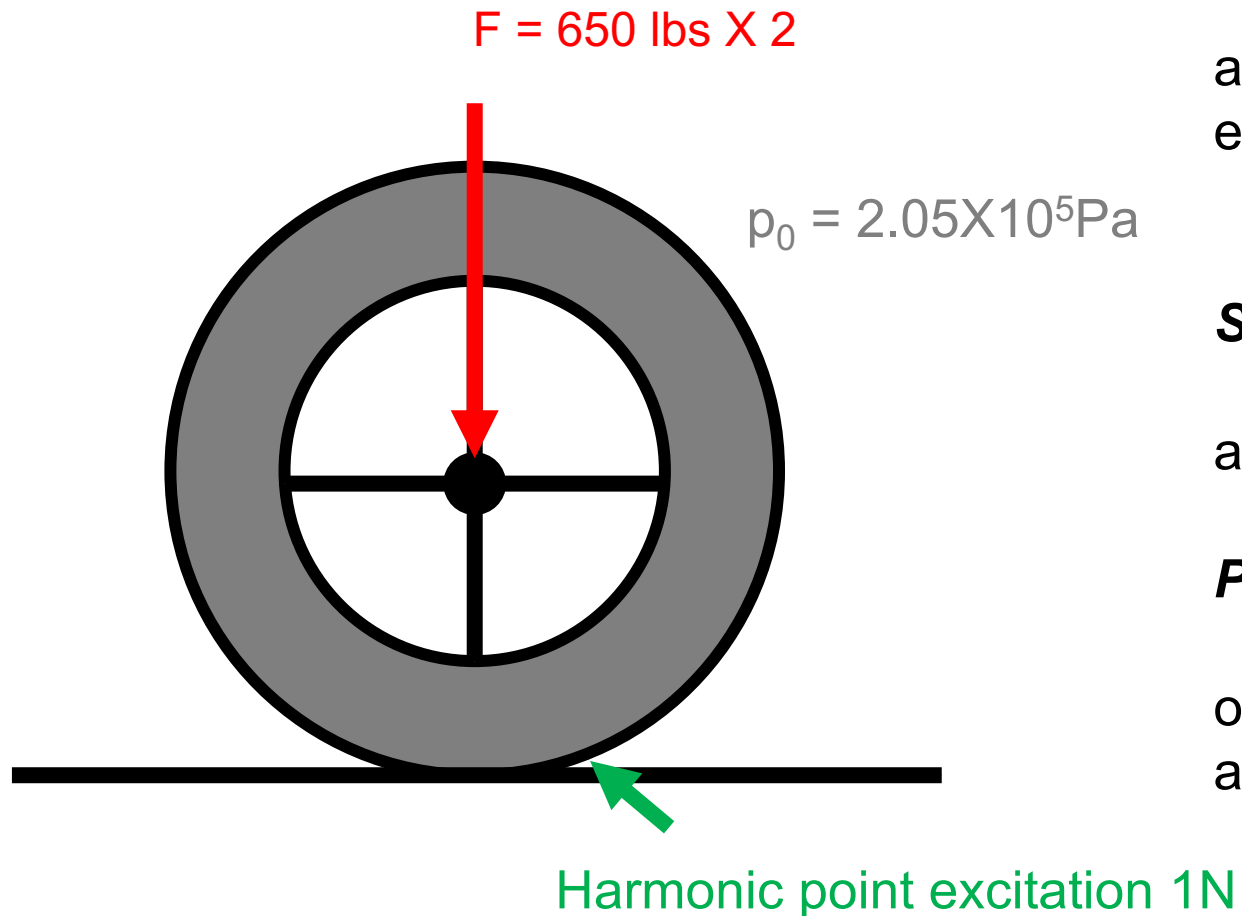
Tread surface – rigid ground

Ground is considered rigid in the normal direction; a small friction coefficient is added to increase solution robustness (prevent tire sliding horizontally as the contact starts)

### III. Analysis process

---

#### Excitations



#### ***Vertical static loads***

1300 lbs (approximately 6000 N) applied at the rim center – with 650 lbs on each side

#### ***Static inflation pressure***

A  $2.05 \times 10^5 \text{ Pa}$  inflation pressure was applied to all tire interior cavity surfaces

#### ***Point harmonic excitation***

A 1 N point harmonic point excitation over the investigated frequency range was applied at the contact patch leading edge

# III. Analysis process

---

## Analysis Steps

Initial step – fix rim center

Step 1 – Tire inflation

- rim center is still fixed

Step 2 – Apply vertical load

- rim center is released
- require adaptive mesh of the air cavity

Step 3 – Modal analysis

- extract modes from 10 Hz to 320 Hz

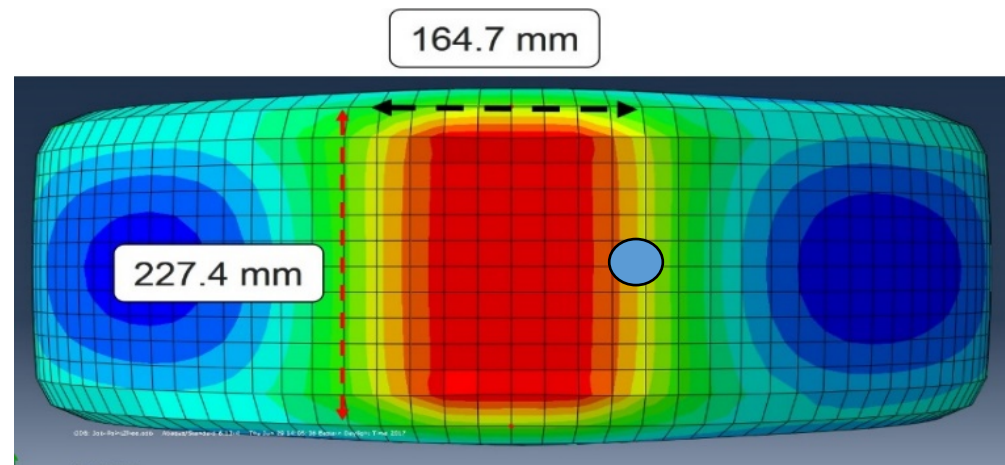
Step 4 – Forced response calculation

- direct approach
- 0.5 Hz increment

## IV. Data visualization and comparison study

---

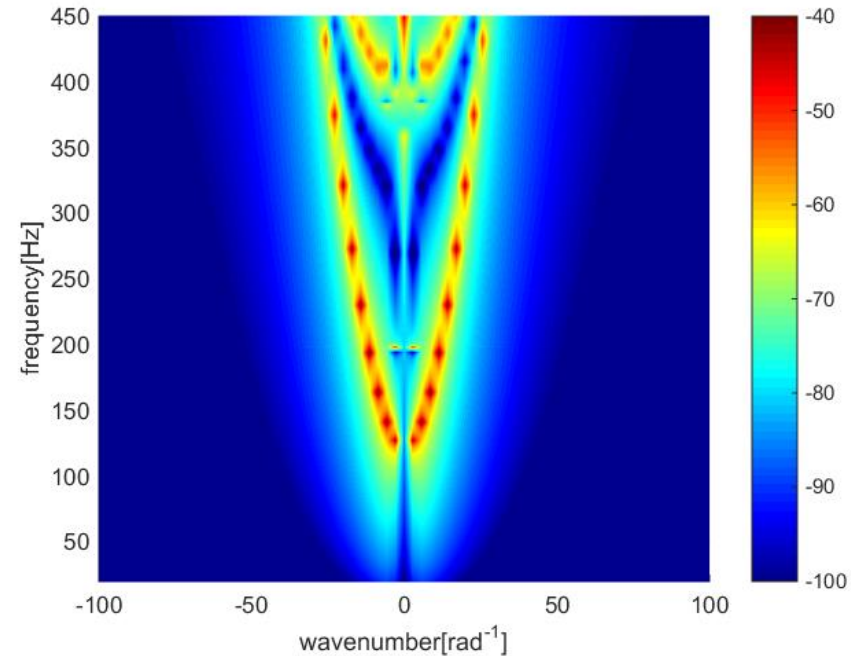
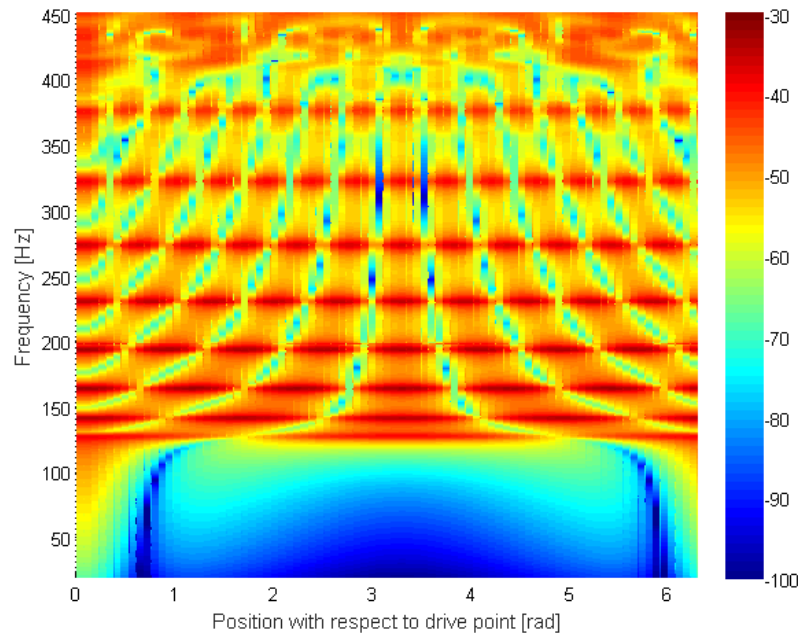
- What to expect from the results
  - Surface velocity of the tire tread – identify vibration modes
  - Dispersion relation of the tire tread – identify wave types
  - Rim center acceleration – force transmissibility study
  - Cavity and structural mode shapes



Contact patch area



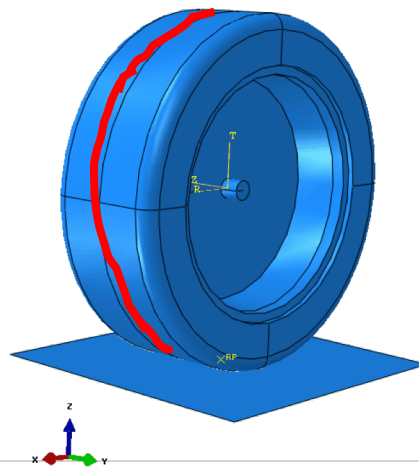
# IV. Data visualization and comparison study



Spatial Surface velocity  
- unloaded tire

Drive point

Velocity was measured at points  
along the tire tread centerline



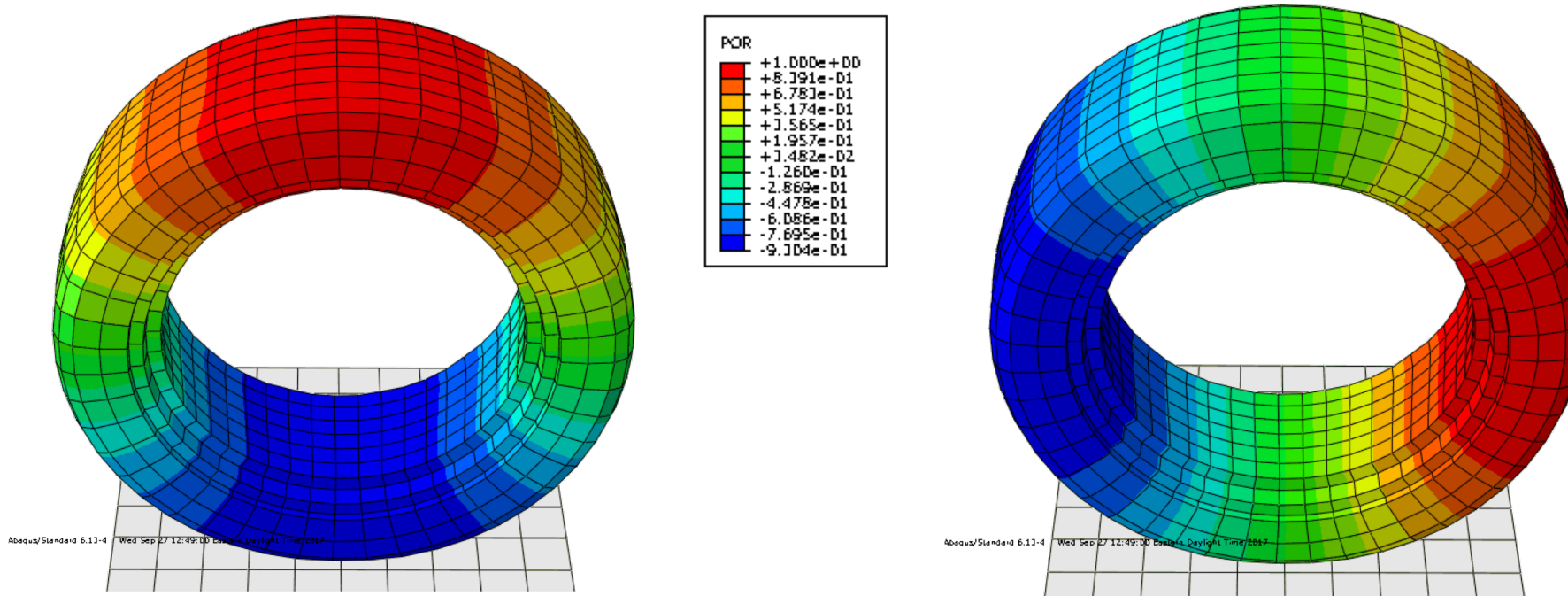
Dispersion relations  
- unloaded tire

Dispersion was based on the  
wavenumber decomposition of  
the surface mobility data

# IV. Data visualization and comparison study

Vertical cavity mode (pressure distribution)

Horizontal cavity mode (pressure distribution)



- ❖ Deformation causes cavity resonance split
- ❖ One occurs below undeformed cavity resonance (horizontal)
- ❖ One occurs above undeformed cavity resonance (vertical)

Undeformed resonance: 200.1 Hz; vertical mode: 201.4 Hz; horizontal mode: 199.3 Hz

## IV. Data visualization and comparison study

---

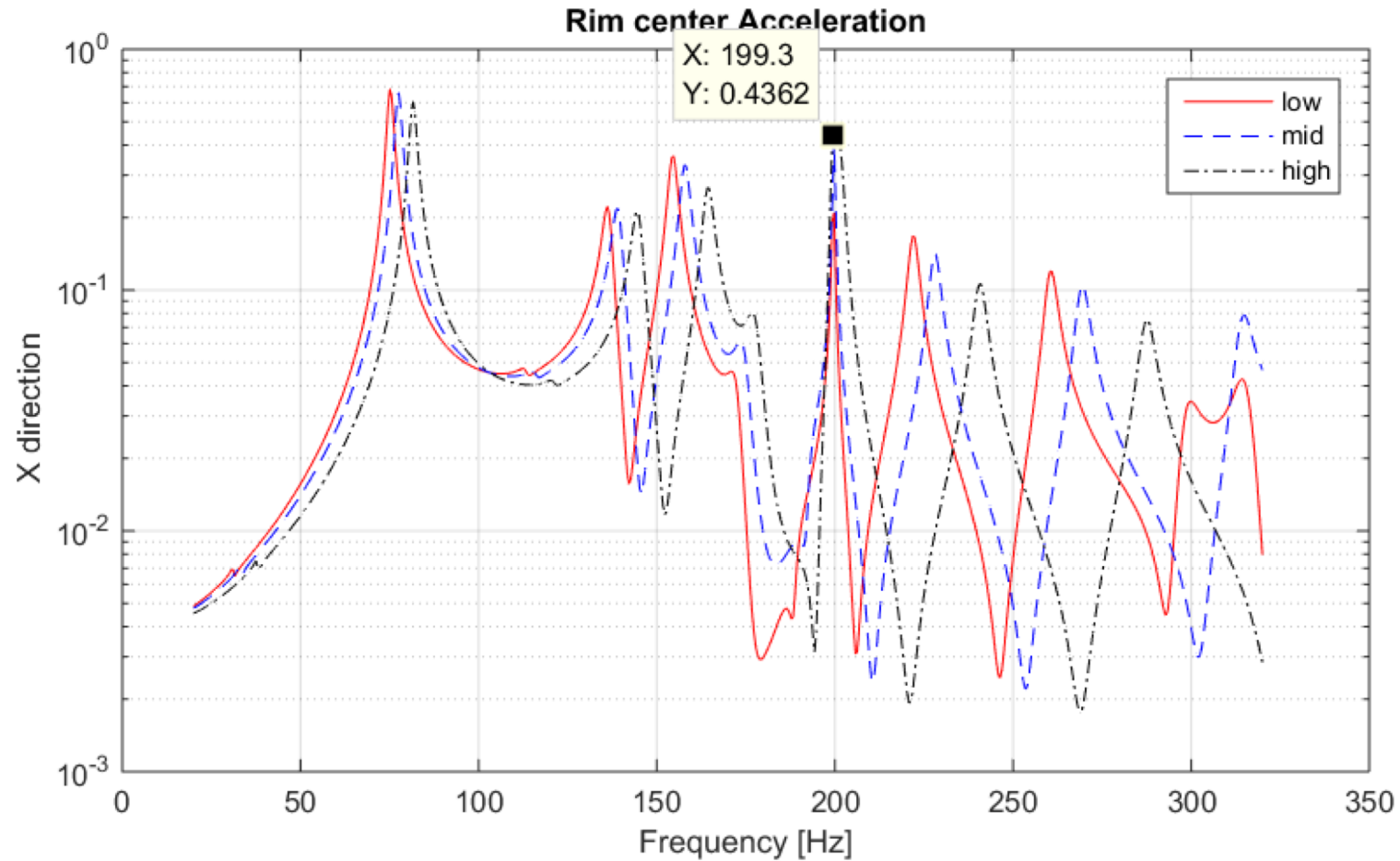
For GY245/40R20 tire, the material property of the tread was modified to be **soft (low stiffness)**, **medium (medium stiffness)** and **stiff (high stiffness)** to align the ***vertical cavity resonance*** to either the symmetric circumferential 8<sup>th</sup> mode or the asymmetric circumferential 9<sup>th</sup> mode of the treadband.

Status	Modulus	Alignment
Soft	4.5e <sup>8</sup>	9 <sup>th</sup> mode
Medium	6.0e <sup>8</sup>	In between
Stiff	10.0e <sup>8</sup>	8 <sup>th</sup> mode

Point excitation located at the contact patch on the tread centerline, toward the rim center. Most forcing component is in the vertical direction (+Z)

## IV. Data visualization and comparison study

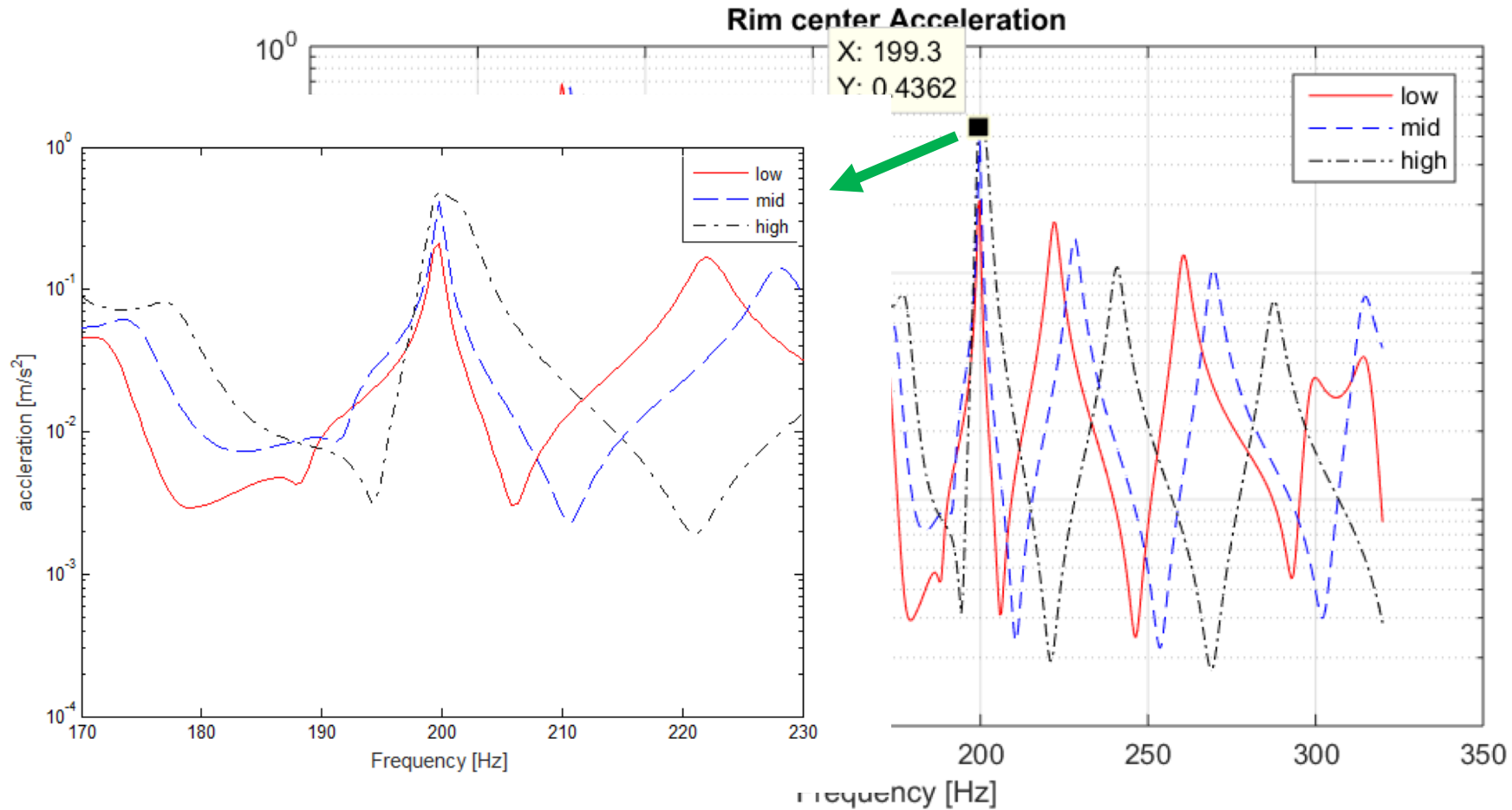
### Rim center acceleration comparison



Peak at frequency corresponding to horizontal acoustic cavity mode

# IV. Data visualization and comparison study

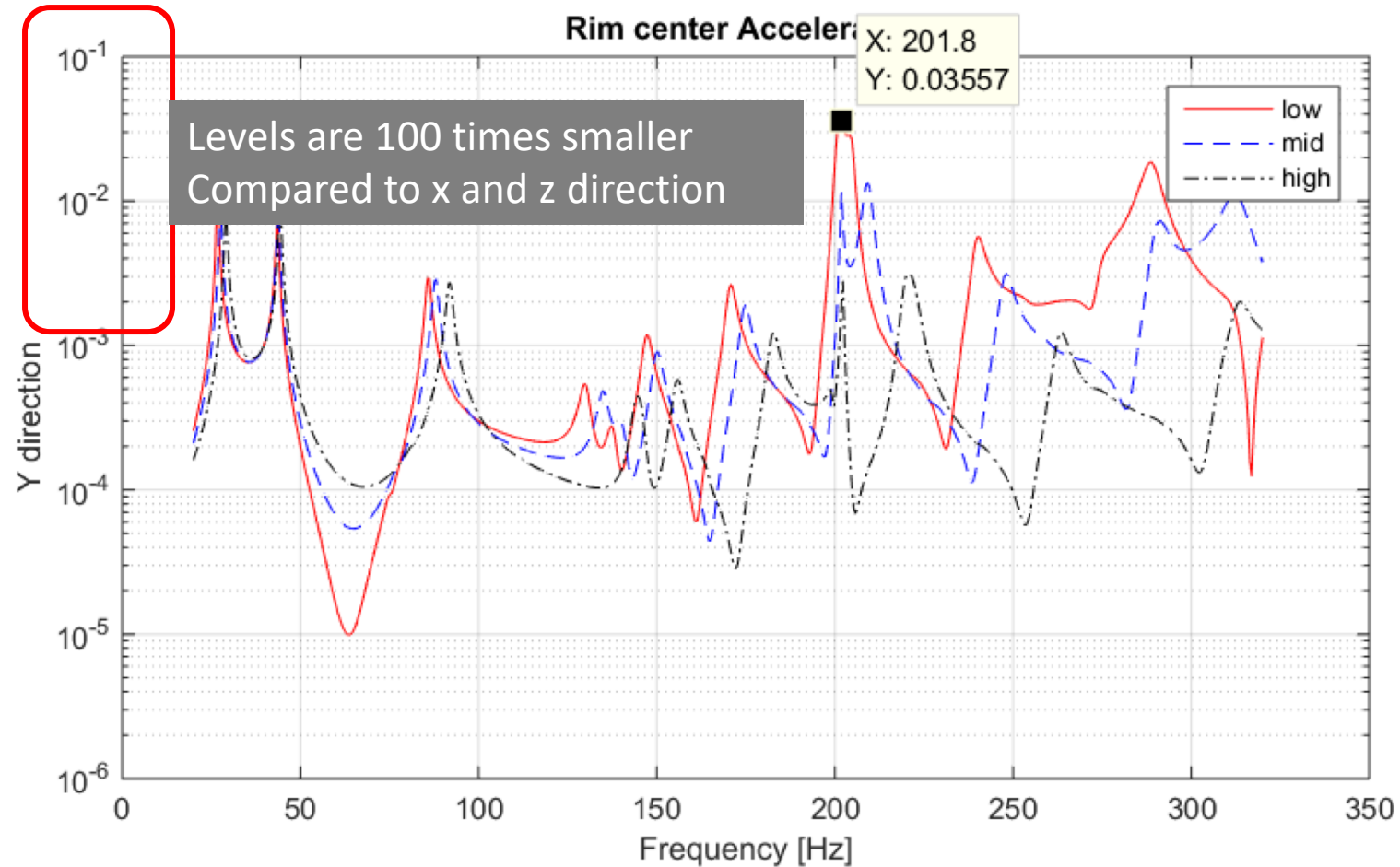
## Rim center acceleration comparison



Peak at frequency corresponding to horizontal acoustic cavity mode

# IV. Data visualization and comparison study

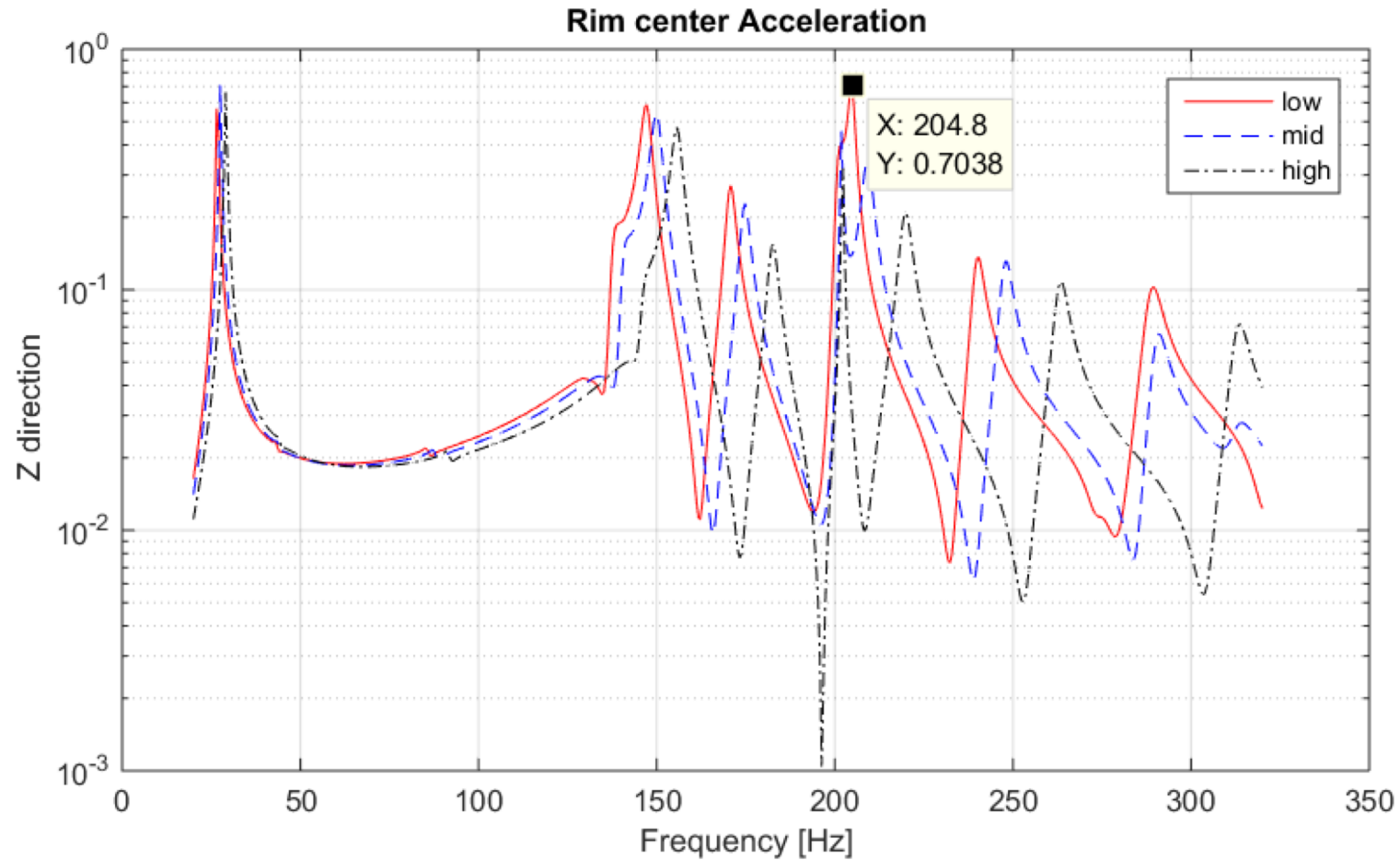
## Rim center acceleration comparison



Very low levels in the y-direction – some axial component due to the rim profile

# IV. Data visualization and comparison study

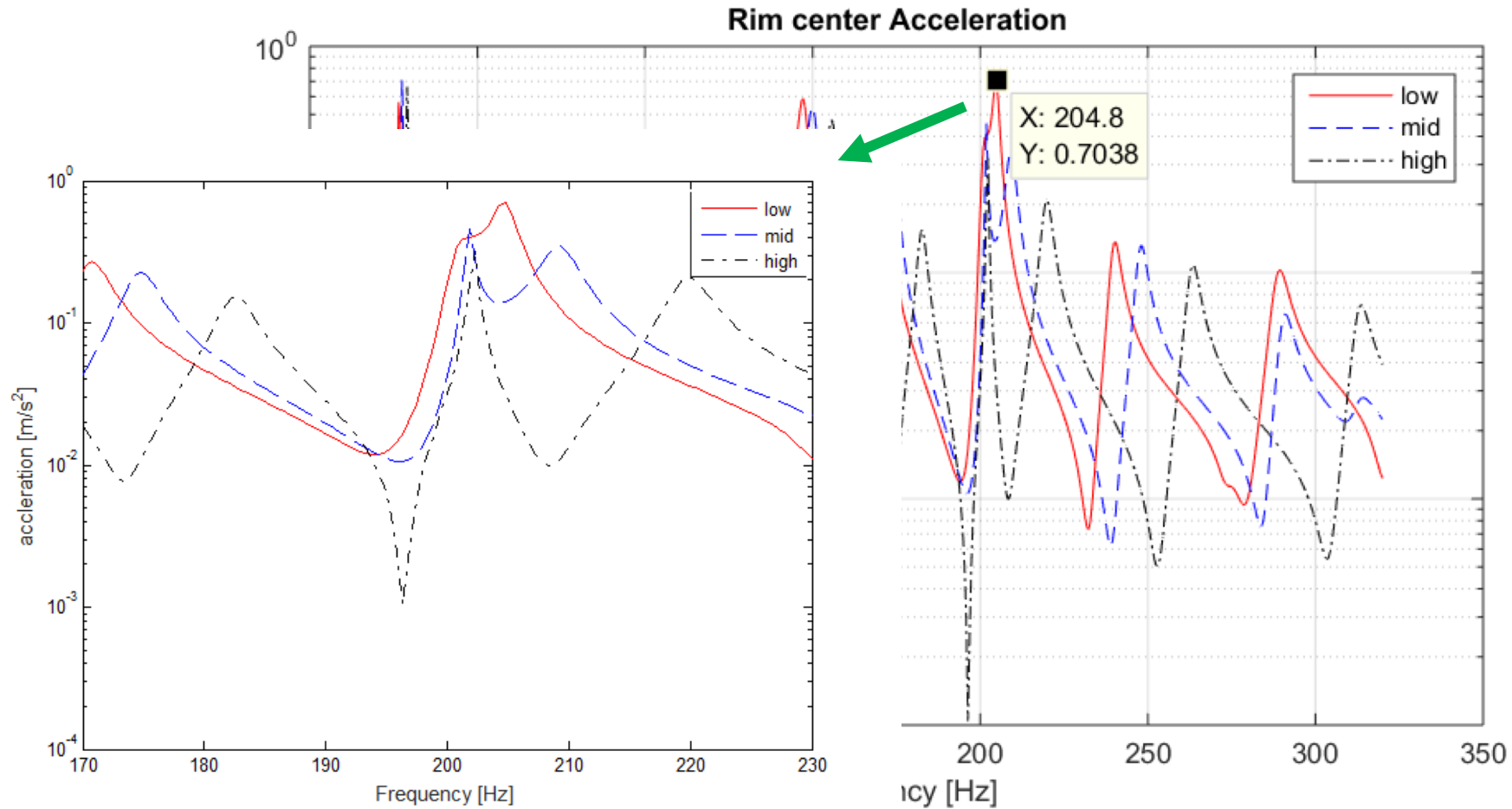
## Rim center acceleration comparison



Peak at frequency corresponding to vertical acoustic cavity mode

# IV. Data visualization and comparison study

## Rim center acceleration comparison

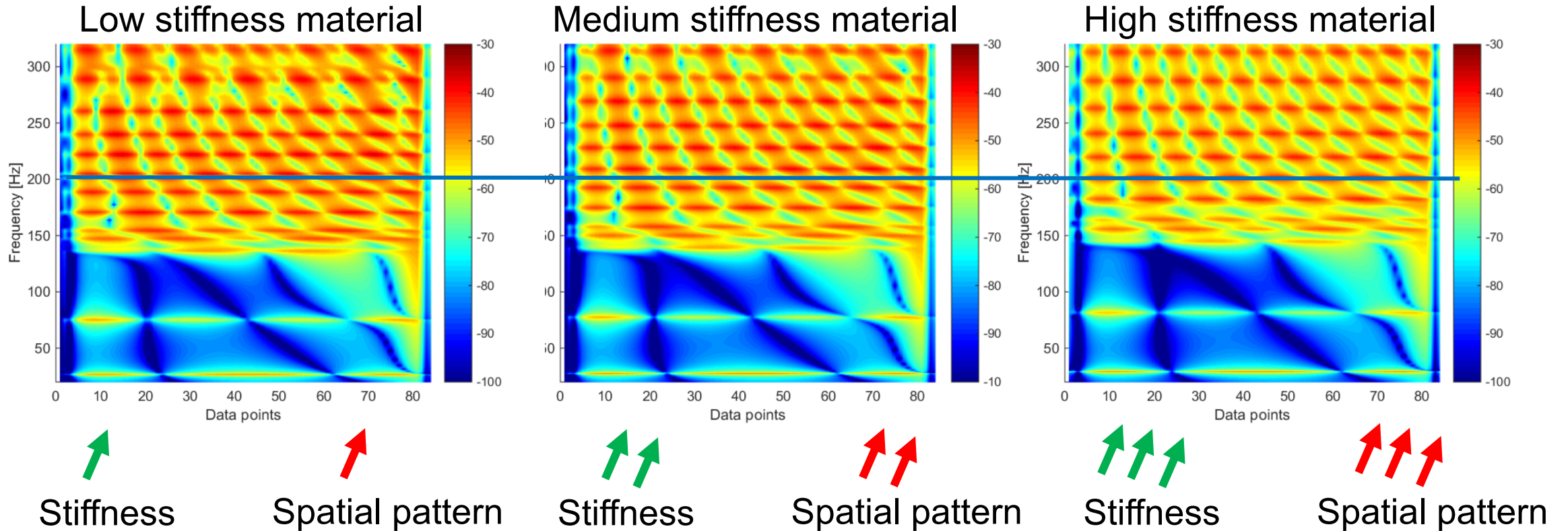


Peak at frequency corresponding to vertical acoustic cavity mode



# IV. Data visualization and comparison study

## Spatial mobility comparison

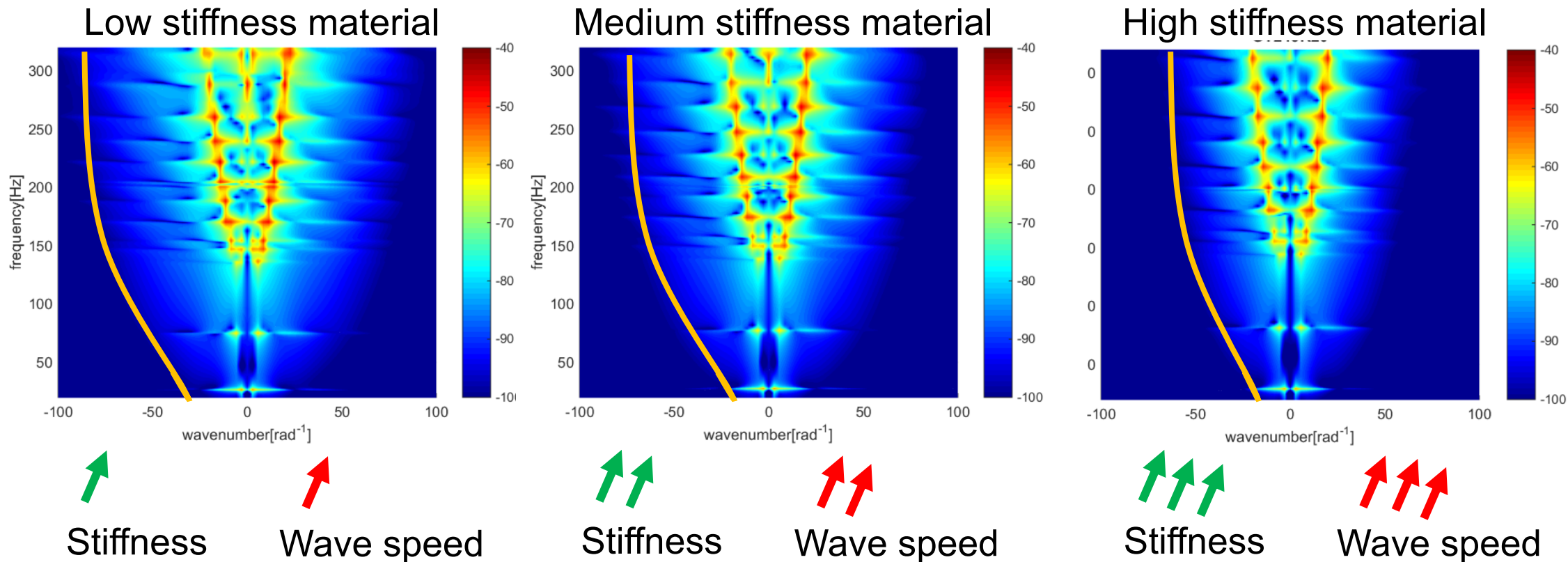


***As stiffness increase, the spatial patterns move toward high frequency region***

- Low stiffness – cavity mode matches 9<sup>th</sup> structural mode
- High stiffness – cavity mode matches 8<sup>th</sup> structural mode

# IV. Data visualization and comparison study

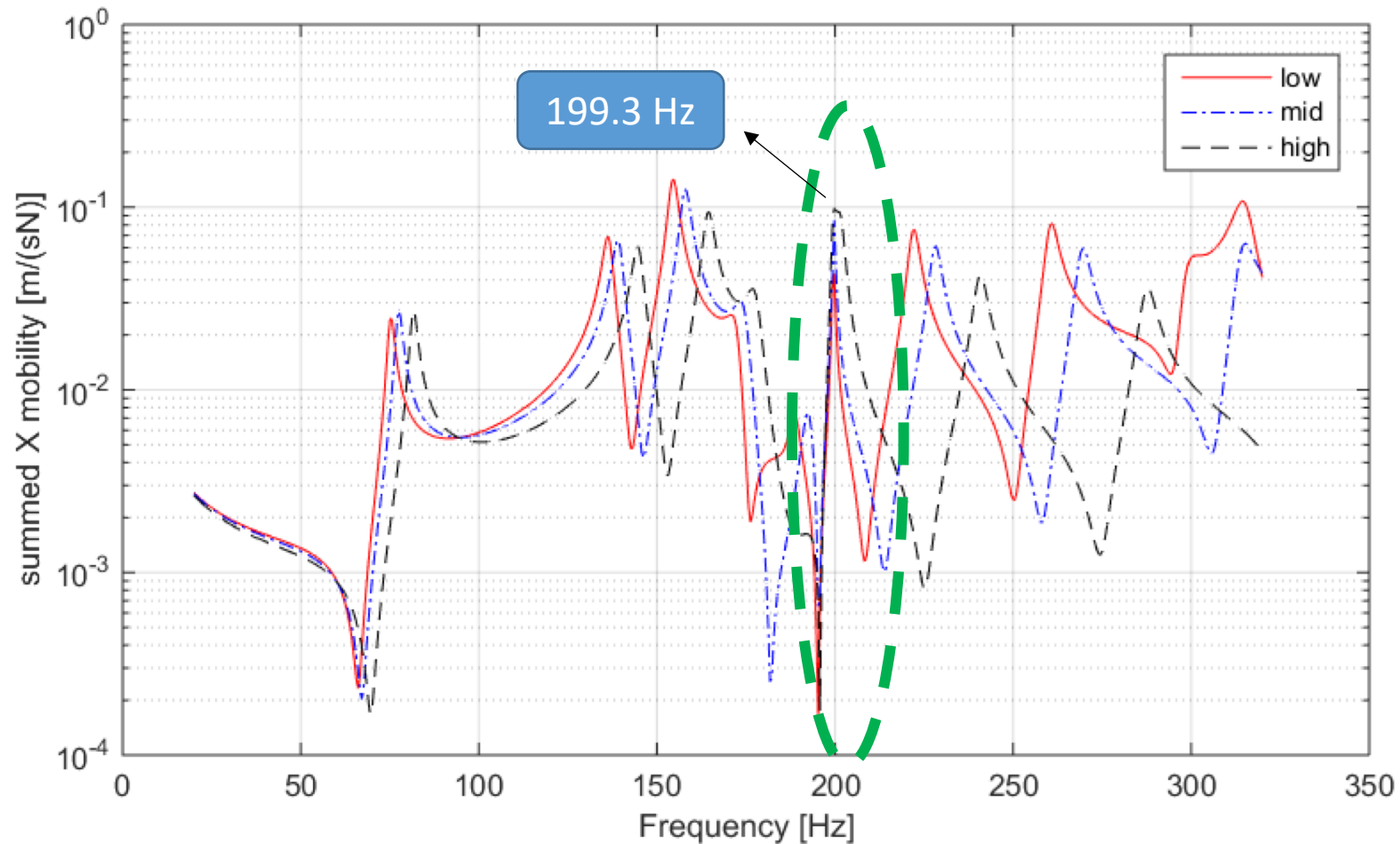
## Dispersion comparison



***As stiffness increase, the dispersion curve becomes narrower, indicating faster waves***

## IV. Data visualization and comparison study

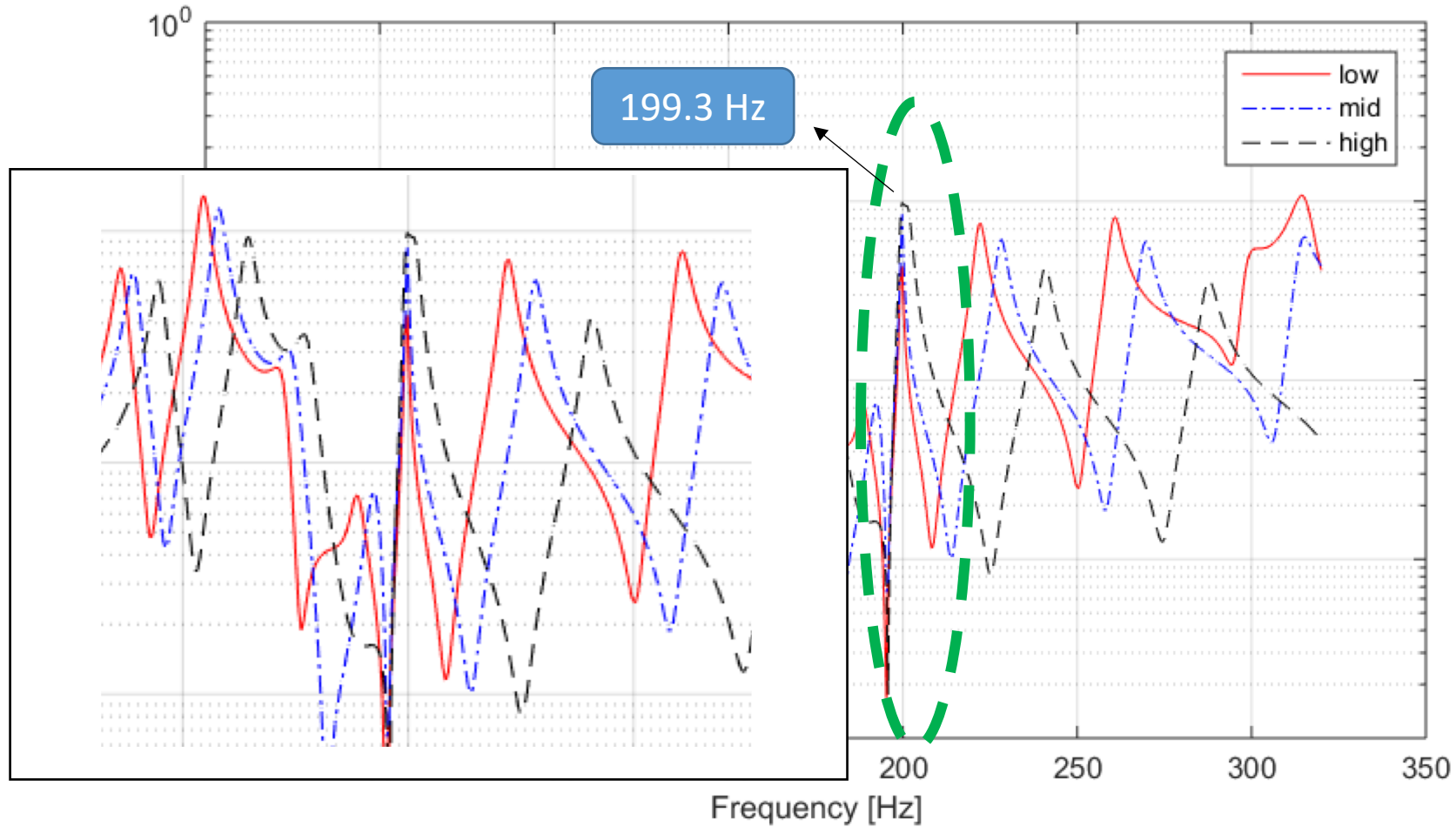
### Resultant mobility in X direction



Resultant mobility – vector sum of mobility around tire in horizontal direction

# IV. Data visualization and comparison study

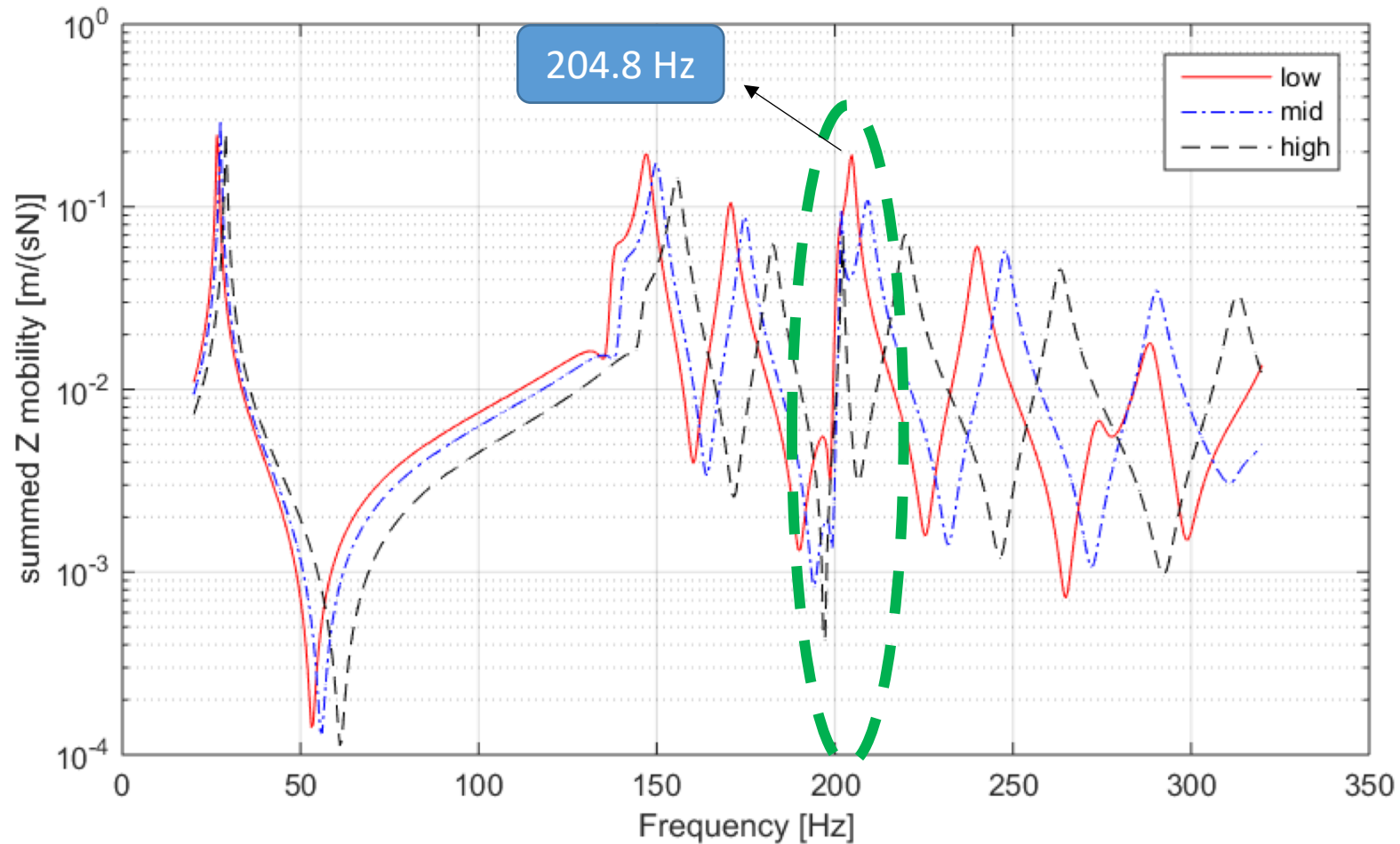
## Resultant mobility in X direction



Resultant mobility – vector sum of mobility around tire in horizontal direction

## IV. Data visualization and comparison study

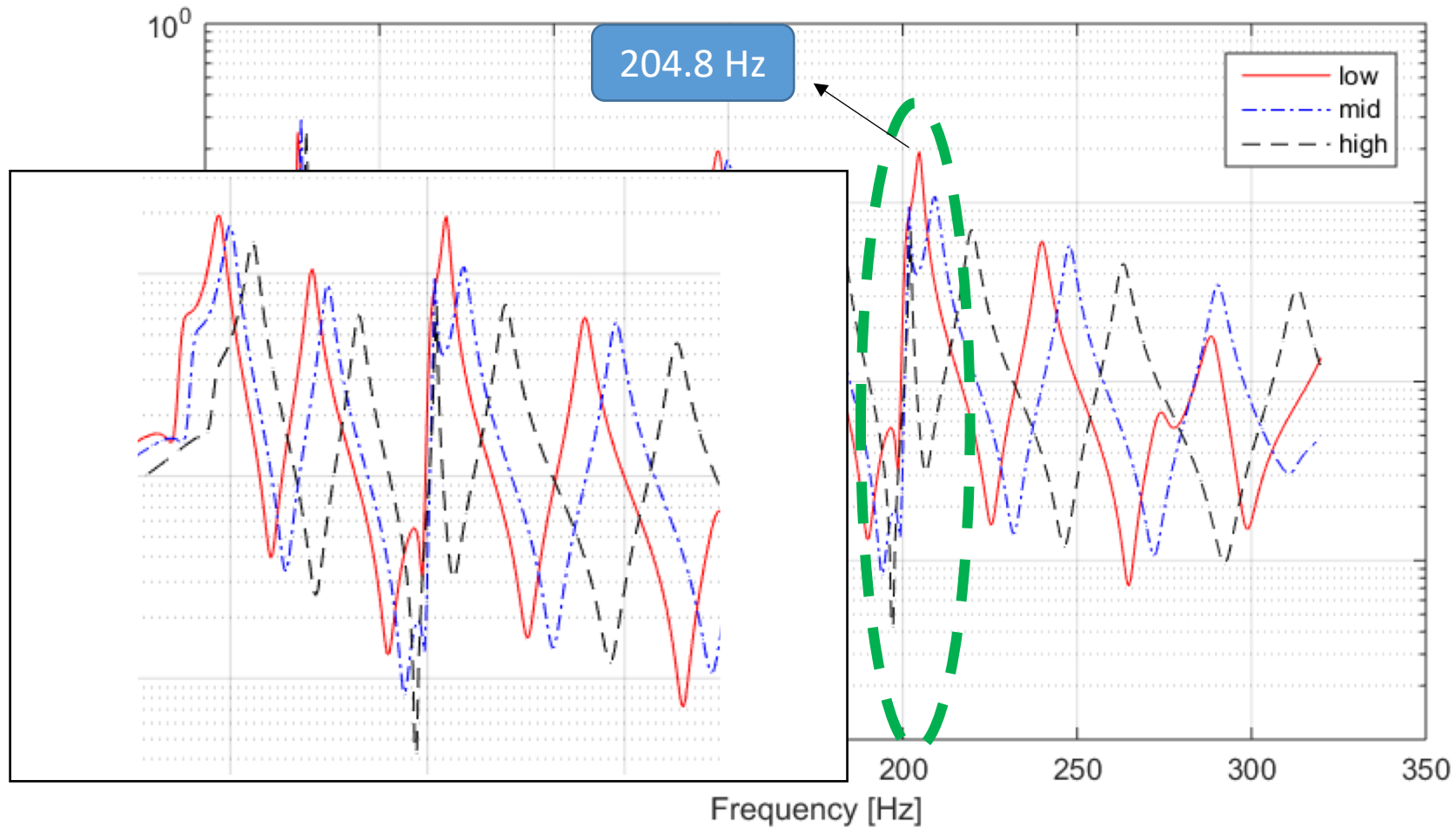
### Resultant mobility in Z direction



Resultant mobility – vector sum of mobility around tire in vertical direction

# IV. Data visualization and comparison study

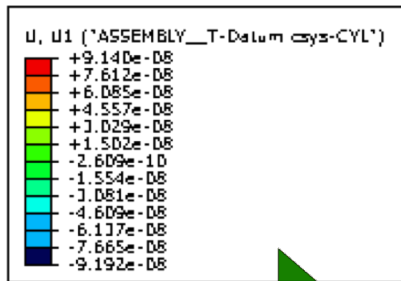
## Resultant mobility in Z direction



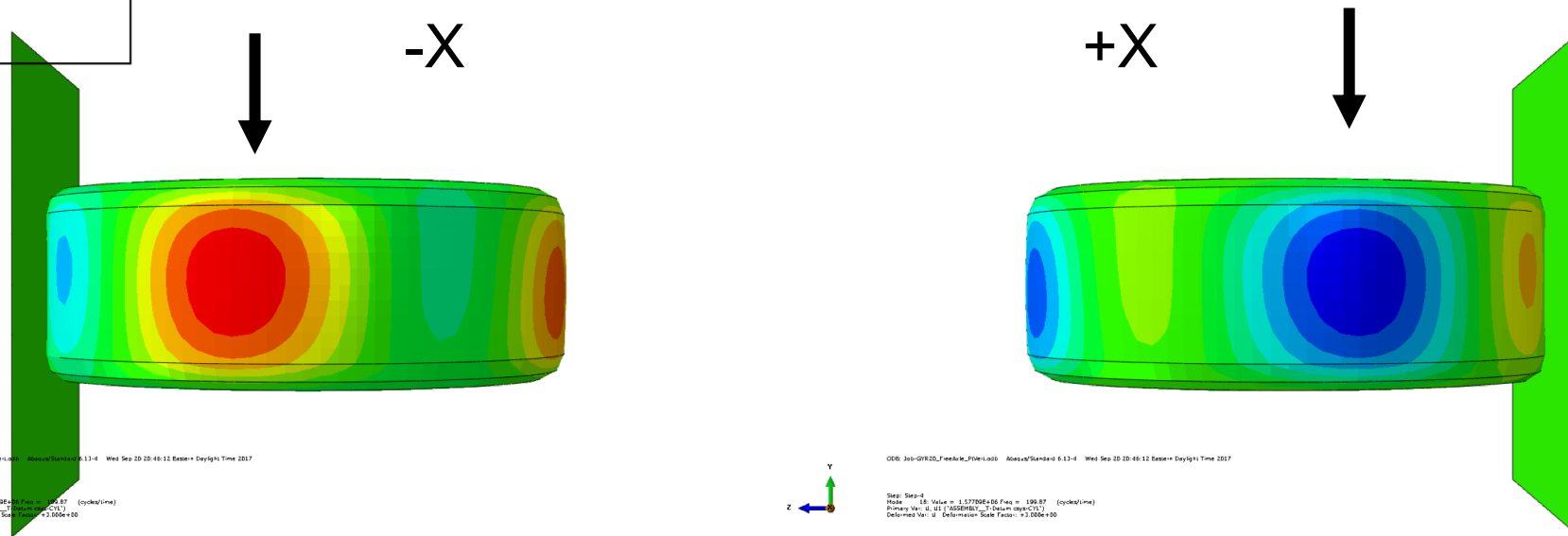
Resultant mobility – vector sum of mobility around tire in vertical direction

# V. Modal analysis

## 1<sup>st</sup> cavity mode - horizontal



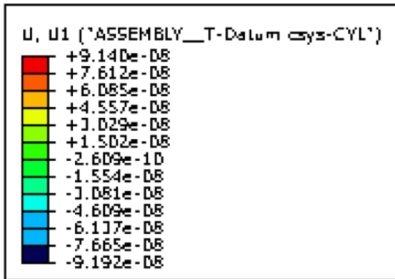
Side views



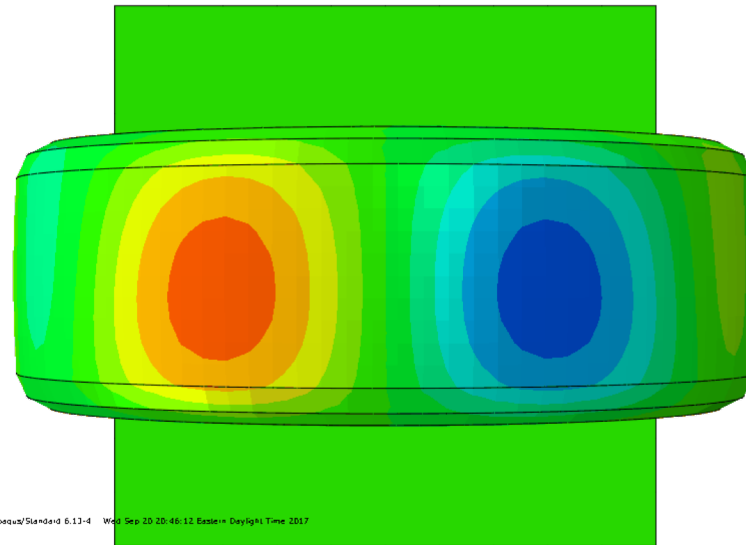
Radial displacement

# V. Modal analysis

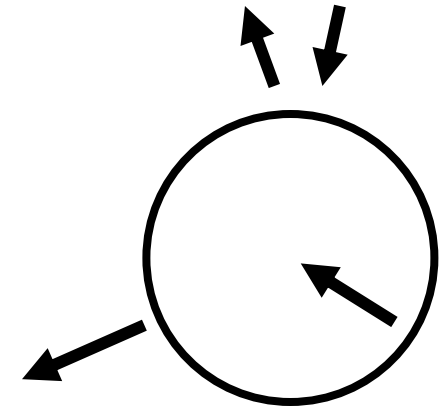
## 1<sup>st</sup> cavity mode - horizontal



Top view



Vertical motion components were canceled, leaving only horizontal motions



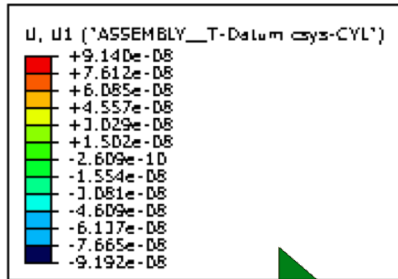
ODB: Job-GYR2D\_FreeAble\_PVW.t.odb Abaqus/Standard 6.13.4 Wed Sep 20 20:46:13 Eastern Daylight Time 2017

Step: Step-1  
Mode: 18; Value = 1.57709E+00 Freq = 199.87 (cycles/time)  
Primary Var: U, U1 ('ASSEMBLY\_\_T-Datum csys-CYL')  
Deformed Var: U; Deformation Scale Factor: +3.000e+00



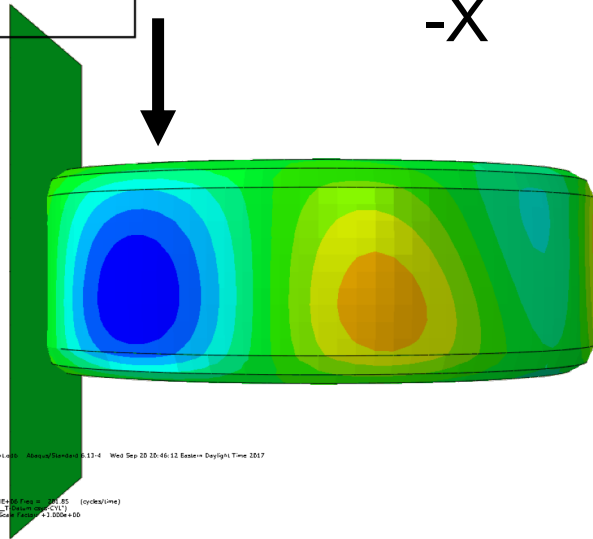
# V. Modal analysis

## 1<sup>st</sup> cavity mode - vertical

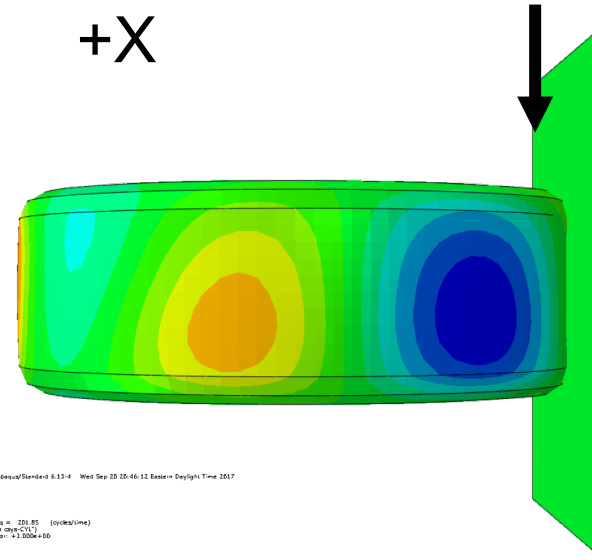


Side views

-X

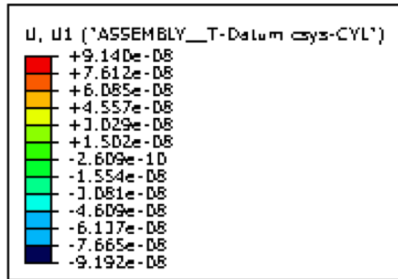


+X

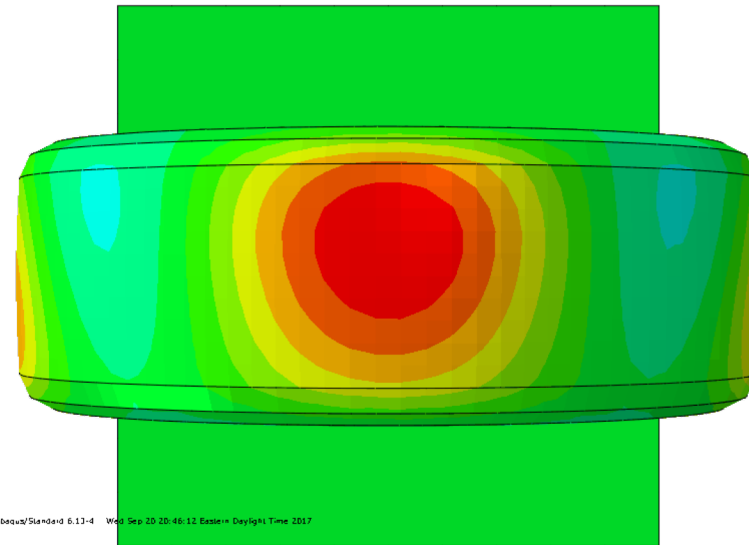


# V. Modal analysis

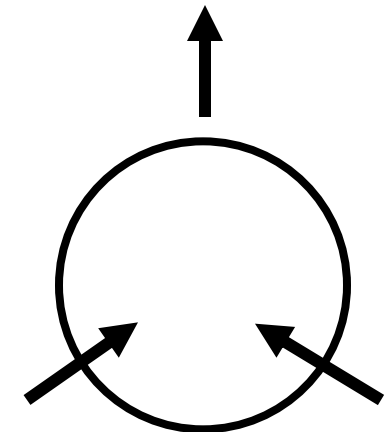
## 1<sup>st</sup> cavity mode - vertical



Top view



Horizontal motion components were canceled, leaving only vertical motion

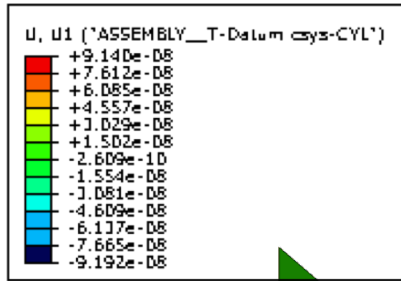


ODB: Job-GYR2D\_FreeAble\_PVW.t.odb Abaqus/Standard 6.13-4 Wed Sep 20 20:46:12 Eastern Daylight Time 2017

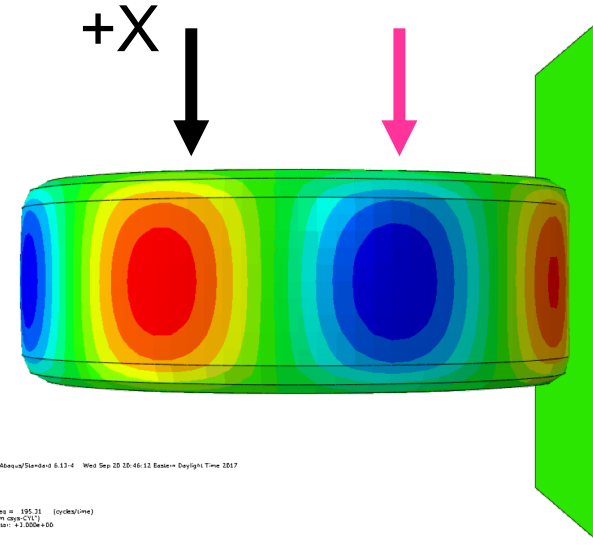
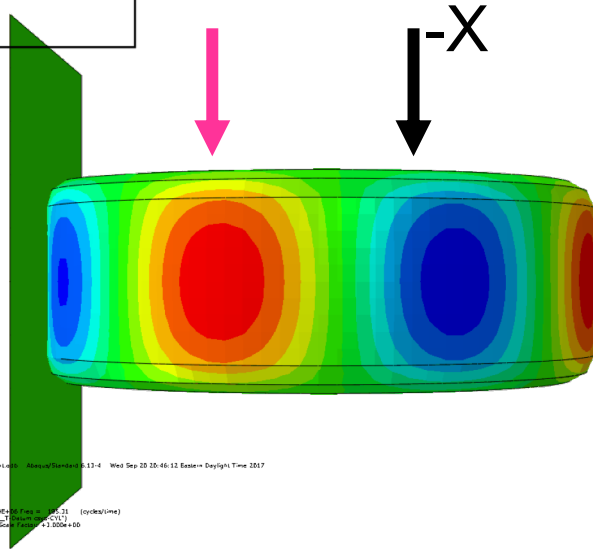
Step: Step-1  
Mode: 19; Value = 1.00053E+00 Freq = 201.85 (cycles/time)  
Primary Var: U, U1 ('ASSEMBLY\_\_T-Datum csys-CYL')  
Deformed Var: U; Deformation Scale Factor: +3.000e+00

# V. Modal analysis

## 8<sup>th</sup> structural mode

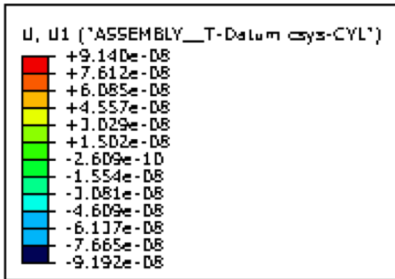


Side views

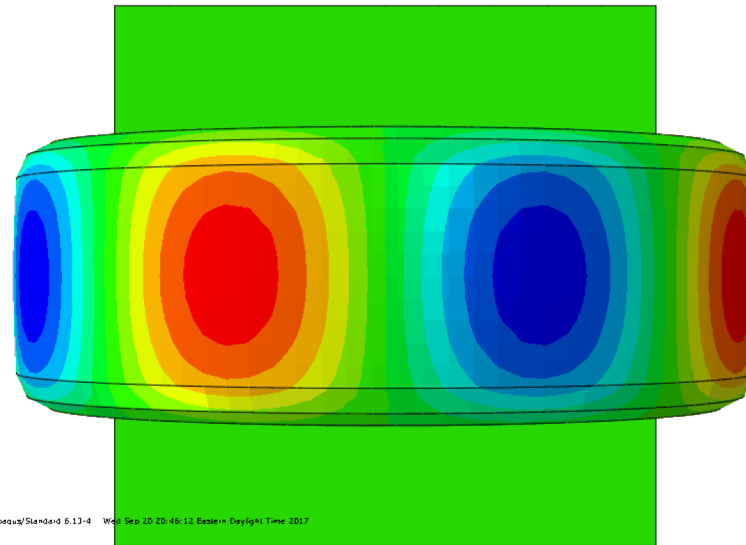


# V. Modal analysis

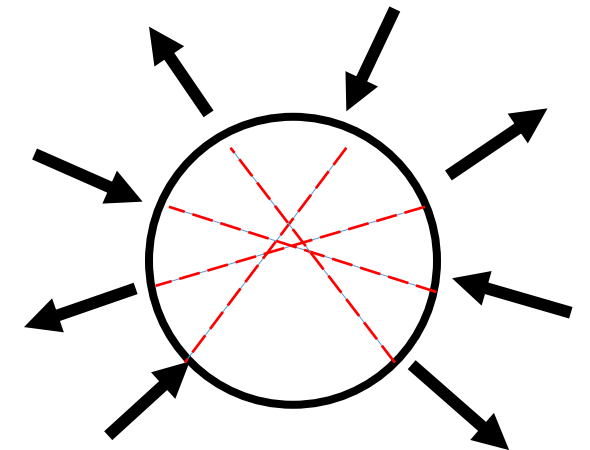
## 8<sup>th</sup> structural mode



Top view



Motion on two sides cancel each other

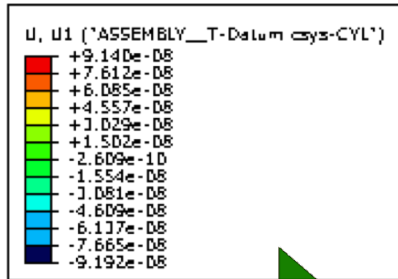


ODB: Job-GYR2D\_FreeAble\_PVW.t.odb Abaqus/Standard 6.13-4 Wed Sep 20 20:46:13 Eastern Daylight Time 2017

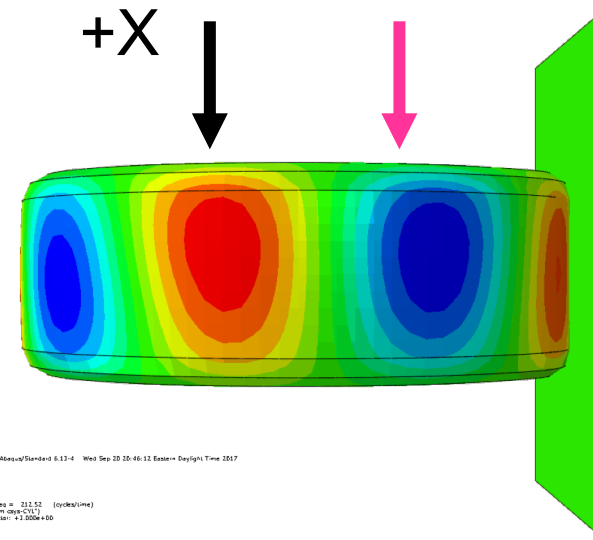
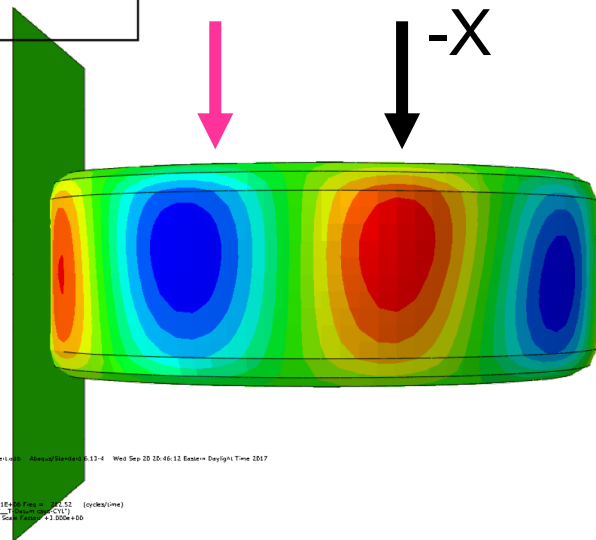
Step: Step-1  
Mode: 17; Value = 1.30099E+00 Freq = 195.31 (cycles/time)  
Primary Var: U, U1 ('ASSEMBLY\_\_T-Datum csys-CYL')  
Deformed Var: U Deformation Scale Factor: +3.000e+00

# V. Modal analysis

## 9<sup>th</sup> structural mode



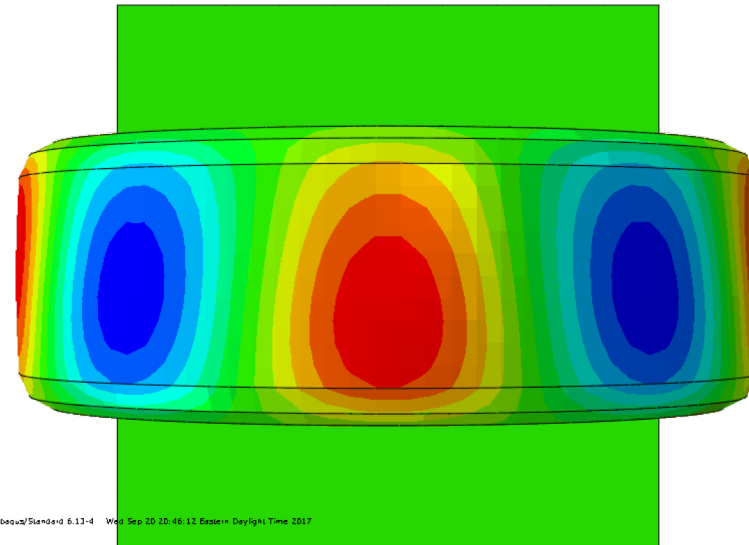
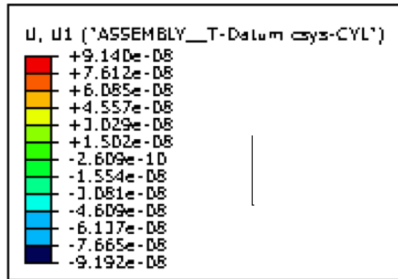
Side views



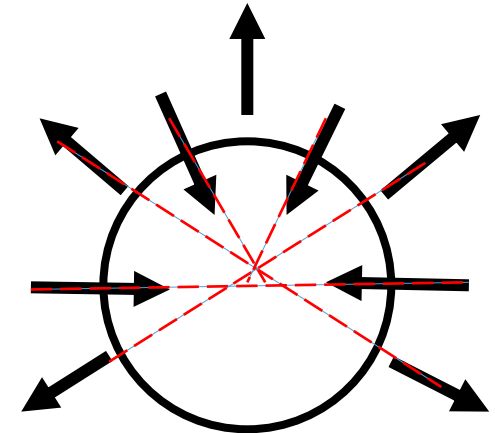
# V. Modal analysis

## 9<sup>th</sup> structural mode

Top view



Motion on two sides cancel each other, except for the peak on top



ODB: Job-GYR20\_FreeAble\_PVW1.odb Abaqus/Standard 6.13-4 Wed Sep 20 10:46:12 Eastern Daylight Time 2017

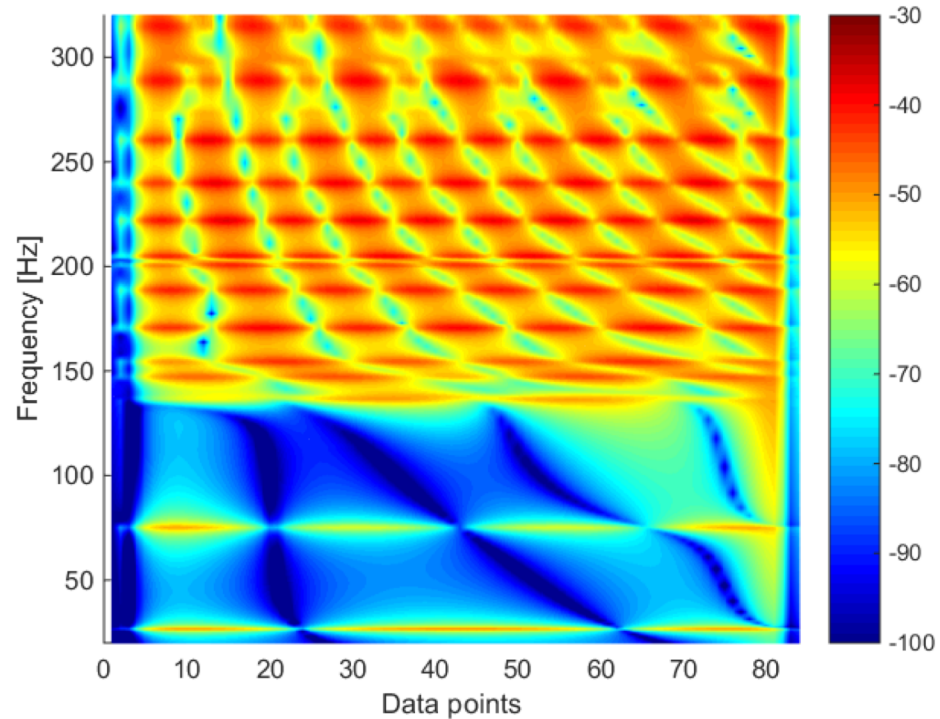
Step: Step-1  
Mode: 20; Value = 1.78211E+06 Freq = 212.52 (cycles/time)  
Primary Var: U, U1 ('ASSEMBLY\_\_T-Datum csys-CYL')  
Deformed Var: U; Deformation Scale Factor: +3.000e+00

When 9<sup>th</sup> circumferential structural mode has same frequency as the vertical cavity mode, large response is observed

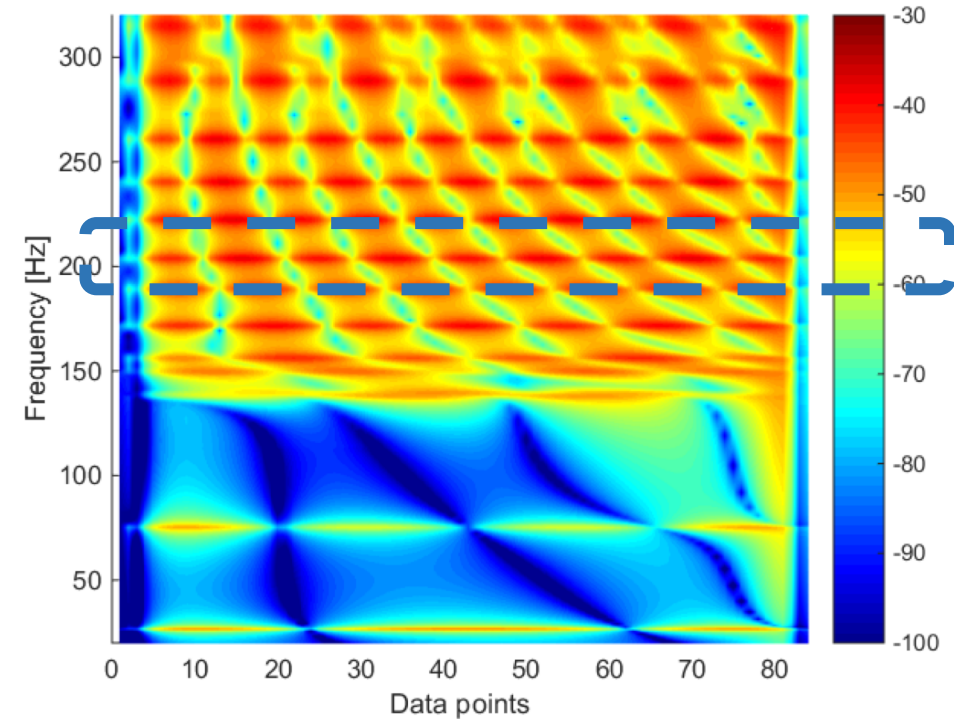
# VI. Compare with airless case

## *Compare with a model without air cavity*

Low stiffness material with air cavity

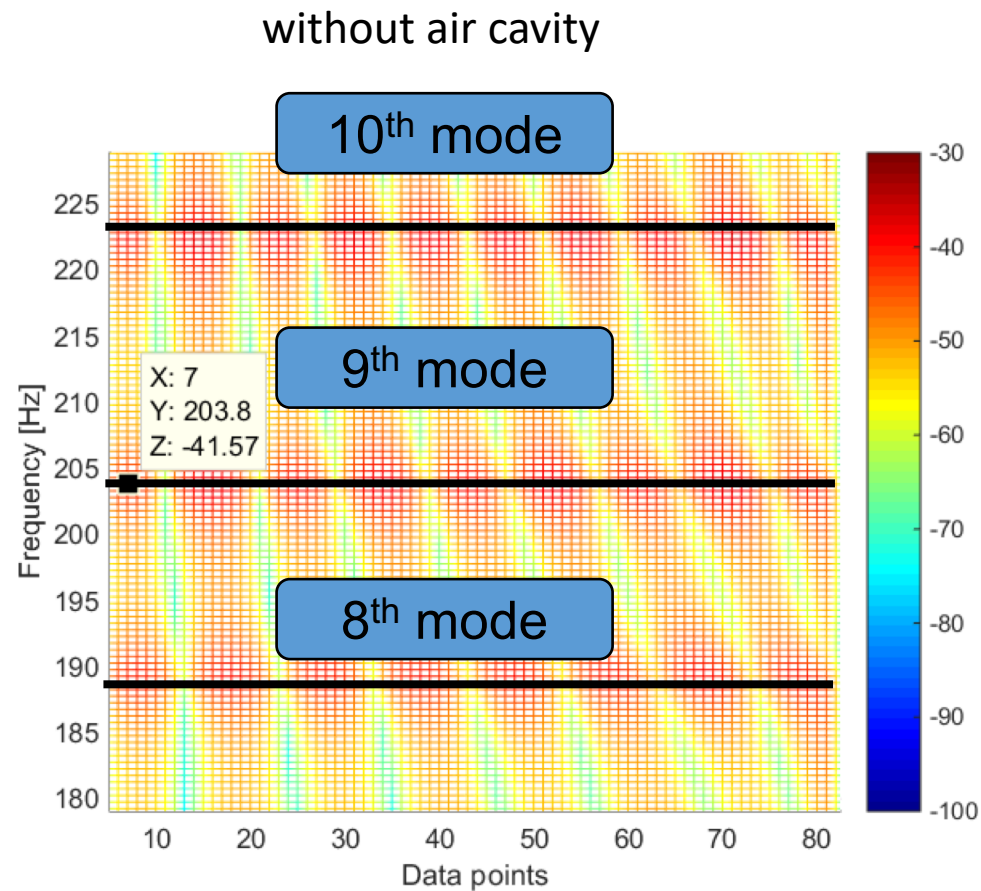
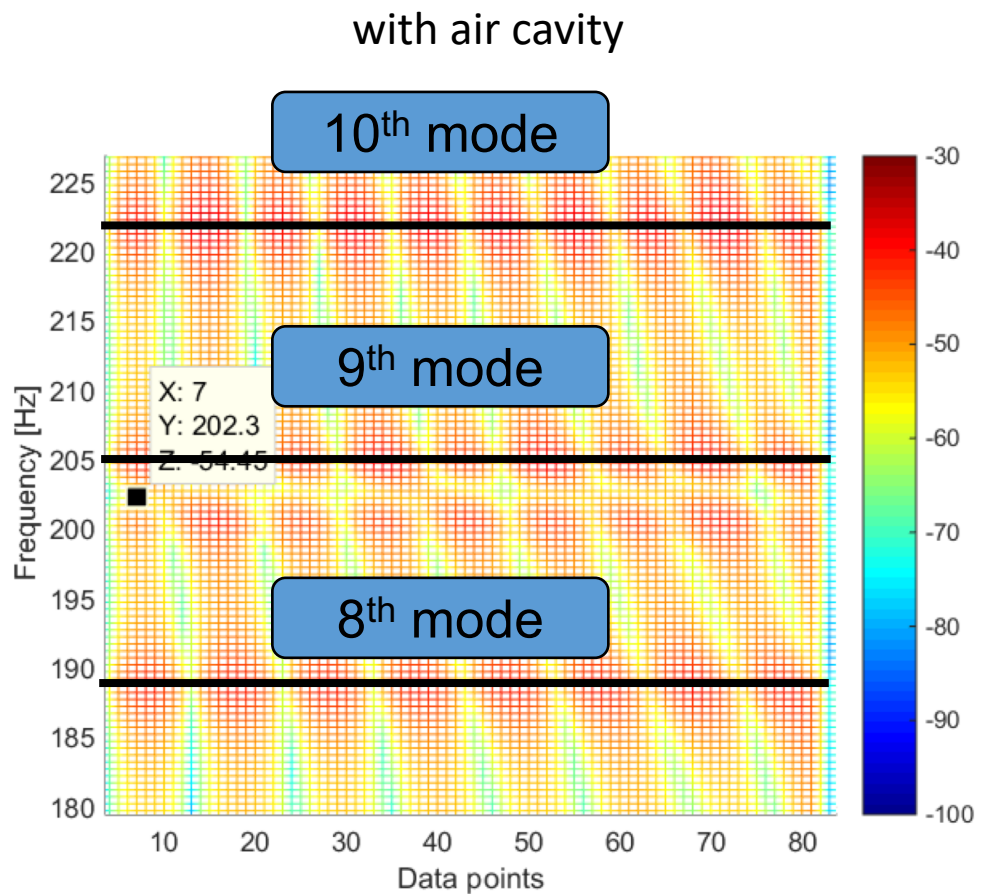


Low stiffness material without air cavity



# VI. Compare with airless case

## Compare with a model without air cavity

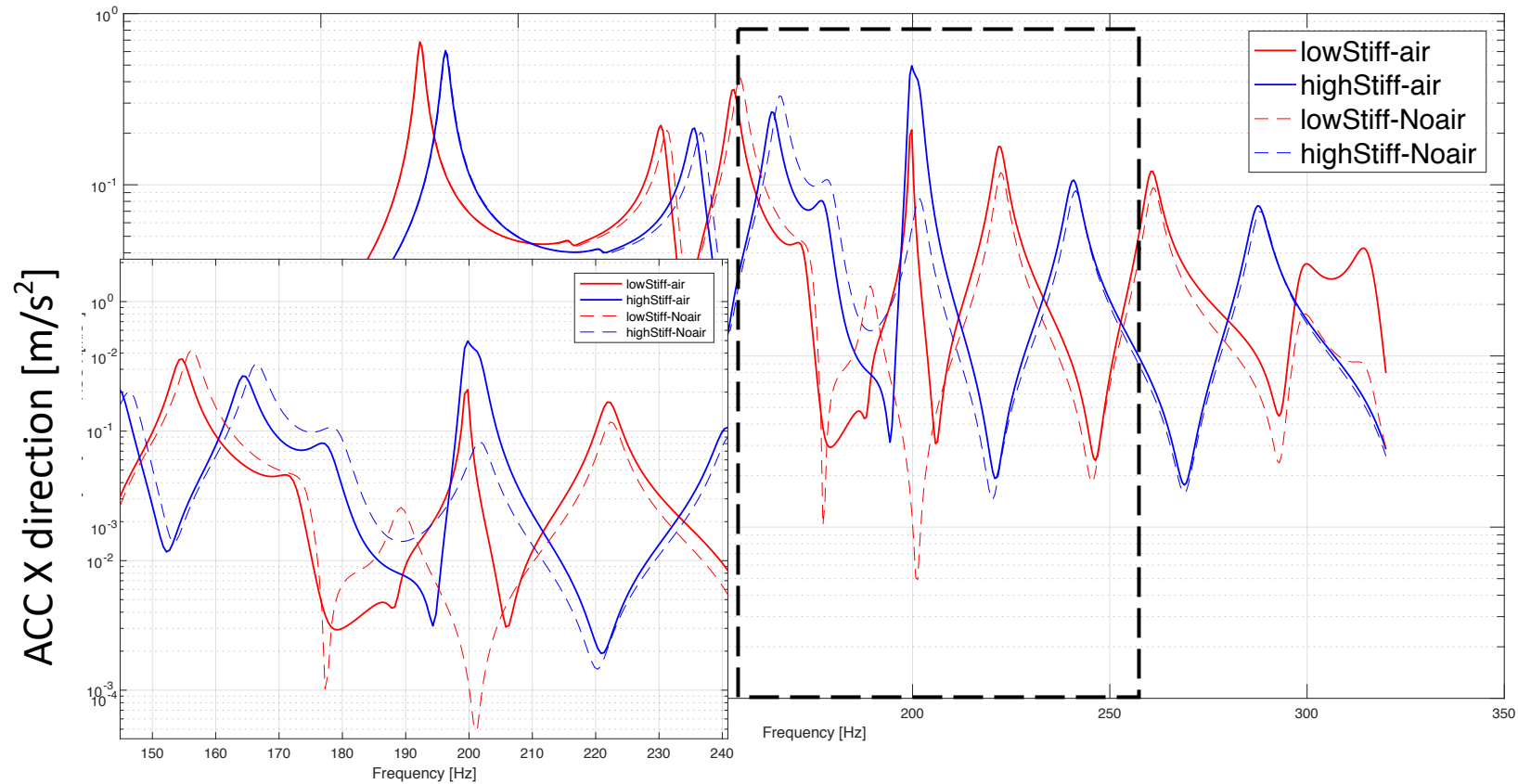


Zoom view of the cavity resonance frequency region



## VI. Compare with airless case

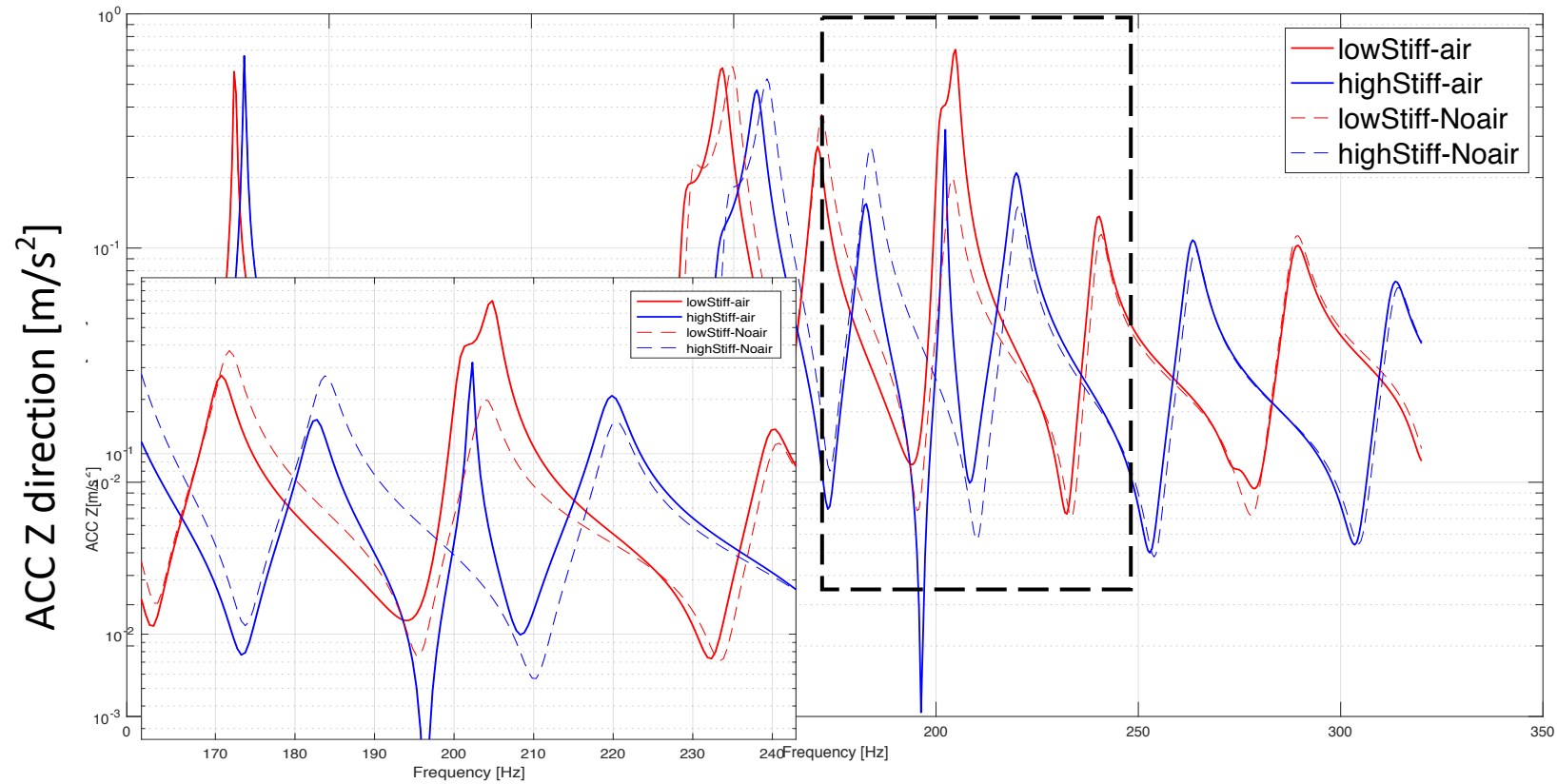
### *Compare with a model without air cavity*



Without air – fore-aft motion is substantially reduced near 200 Hz

## VI. Compare with airless case

### *Compare with a model without air cavity*



Without air vertical motion is substantially reduced near 200 Hz

## VII. Conclusion

---

### ***Conclusion***

- ❑ A finite element tire model was created, which simulated tire inflation, static loading toward a rigid surface and modal analysis.
- ❑ Reaction forces/acceleration at rim center were obtained, along with tread surface mobility and dispersion relations
- ❑ The coupling relation between cavity resonances and structural resonances were studied and odd-number structural modes were found to couple well with the vertical cavity mode due to similar mode shapes
- ❑ Force transmission was related to whether a net motion of the tire tread was created at a particular frequency
- ❑ A case without internal air cavity was simulated as an additional verification

## ***Reference***

Rui Cao, J. Stuart Bolton, Force transmission characteristics for a loaded structural-acoustic tire model, *SAE International Journal of Passenger Cars-Mechanical Systems*, 2018 (under review)

Rui Cao, J. Stuart Bolton, Tire cavity induced structure-borne noise study with experimental verification, *INTER-NOISE and NOISE-CON Congress and Conference Proceedings* , 2018 (Conference submission)

## ***Acknowledgement***

Financial support provided by Ford Motor Company, Matt Black, contract monitor.