



1-6-2018

Real-time Decision Policies with Predictable Performance

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Recommended Citation

Houssam Abbas, Rajeev Alur, Konstantinos Mamouras, Rahul Mangharam, and Alena Rodionova, "Real-time Decision Policies with Predictable Performance", *Proceedings of the IEEE* 106(9). January 2018. <http://dx.doi.org/10.1109/JPROC.2018.2853608>

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Real-time Decision Policies with Predictable Performance

Abstract

As methods and tools for Cyber-Physical Systems grow in capabilities and use, one-size-fits-all solutions start to show their limitations. In particular, tools and languages for programming an algorithm or modeling a CPS that are specific to the application domain are typically more usable, and yield better performance, than general-purpose languages and tools. In the domain of cardiac arrhythmia monitoring, a small, implantable medical device continuously monitors the patient's cardiac rhythm and delivers electrical therapy when needed. The algorithms executed by these devices are streaming algorithms, so they are best programmed in a streaming language that allows the programmer to reason about the incoming data stream as the basic object, rather than force her to think about lower-level details like state maintenance and minimization. Because these devices are resource-constrained, it is useful if the programming language allowed predictable performance in terms of processing runtime and energy consumption, or more general costs. StreamQRE is a declarative streaming programming language, with an efficient and portable implementation and strong theoretical guarantees. In particular, its evaluation algorithm guarantees constant cost (runtime, memory, energy) per data item, and also calculates upper bounds on the per-item cost. Such an estimate of the cost allows early exploration of the algorithmic possibilities, while maintaining a handle on worst-case performance, on the basis of which hardware can be designed and algorithms can be tuned.

Keywords

Quantitative Regular Expressions, Streaming languages, Arrhythmia monitoring, Tachycardia, Real-time

Disciplines

Analytical, Diagnostic and Therapeutic Techniques and Equipment | Electrical and Computer Engineering | Programming Languages and Compilers | Theory and Algorithms

Real-time Decision Policies with Predictable Performance

Houssam Abbas, *Member, IEEE*, Rajeev Alur, *Fellow, IEEE*, Konstantinos Mamouras, *Member, IEEE*, Rahul Mangharam, *Member, IEEE*, and Alena Rodionova, *Member, IEEE*

Abstract—As methods and tools for Cyber-Physical Systems grow in capabilities and use, one-size-fits-all solutions start to show their limitations. In particular, tools and languages for programming an algorithm or modeling a CPS that are specific to the application domain are typically more usable, and yield better performance, than general-purpose languages and tools. In the domain of cardiac arrhythmia monitoring, a small, implantable medical device continuously monitors the patient’s cardiac rhythm and delivers electrical therapy when needed. The algorithms executed by these devices are *streaming algorithms*, so they are best programmed in a streaming language that allows the programmer to reason about the incoming data stream as the basic object, rather than force her to think about lower-level details like state maintenance and minimization. Because these devices are resource-constrained, it is useful if the programming language allowed predictable performance in terms of processing runtime and energy consumption, or more general costs. StreamQRE is a declarative streaming programming language, with an efficient and portable implementation and strong theoretical guarantees. In particular, its evaluation algorithm guarantees constant cost (runtime, memory, energy) per data item, and also calculates upper bounds on the per-item cost. Such an estimate of the cost allows early exploration of the algorithmic possibilities, while maintaining a handle on worst-case performance, on the basis of which hardware can be designed and algorithms can be tuned.

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I. INTRODUCTION

THE last few years have witnessed an explosion of IoT systems in applications such as smart buildings, wearable devices, and healthcare. A key component of an effective IoT system is the ability to make decisions in real-time in response to data it receives. For instance, a gateway router in a smart home should detect and respond in a timely manner to security threats based on monitored network traffic, and a healthcare system should issue alerts in real-time based on measurements collected from all the devices for all the monitored patients. Programming the desired logic as a deployable implementation is challenging due to the volume of data and hard constraints on available memory, power usage, and response time.

In current practice, a general-purpose imperative language such as C is used to program real-time decision making policies. Due to the challenges in analyzing such code, this approach does not lead to *predictable* performance and does not facilitate *exploration of design options* at early stages. A specialized language for specifying these policies in a declarative manner, with programming abstractions suitable for processing data streams with performance guarantees, can be a potential solution to both these challenges. It can play

the same role as *model-based design* does for safety-critical embedded control software [1], [2], [3], [4].

To specify the decision logic based on computing quantitative summaries of data streams we advocate *Quantitative Regular Expressions (QREs)* [5], [6]. The language allows the computation to be expressed as a streaming composition of stages. The core QRE combinators, which are quantitative extensions of operations in classical regular expressions, can be used to impart to the input data stream a logical hierarchical structure facilitating modular specifications (for instance, to view patient data as a sequence of episodes and to view network traffic as a sequence of Voice-over-IP sessions). The QRE compiler translates a high-level query into a streaming algorithm with precise complexity bounds on per-item processing time and total memory footprint. The StreamQRE library, an implementation in Java, has been shown experimentally to have superior performance compared to other existing high-performance engines for processing streaming data [6]. This experimental evaluation involved workloads that are representative of clickstream analysis (Yahoo streaming benchmark [7]) and real-time analytics for business event streams (NEXMark benchmark [8]). A variant of StreamQRE (called NetQRE) has been shown to be useful for network monitoring [9].

Medical devices offer an ideal test-bed for exploring the applications of formal methods in system design due to their safety-critical nature that demands predictable operation [10]. Recently, the implantable pacemaker has been used to illustrate the benefits of model-based design [11], [12], [13]. This involves specifying the algorithms for detecting slower-than-normal rhythms used by pacemakers using formal modeling languages, such as timed automata [14] and hybrid automata [15], and verifying correctness requirements using a model checker such as UPPAAL [16].

While this previous work dealt with pacemakers, Implantable Cardioverter Defibrillators (ICDs) and Insertable Loop Recorders (ILRs) are a more sophisticated class of implantable cardiac devices that must do *multi-beat rhythm classification*, not only detect whether a beat was missing, like pacemakers do. The goal of such an Arrhythmia Monitoring Algorithm (AMA) is to detect undesirable patterns in the (discretized) input signal being monitored. We argue that such a classification task is best viewed as a matching algorithm over streaming data, and the desired decision logic can be naturally expressed using QREs.

In particular, we program a representative AMA, used in an ICD by Boston Scientific [17], using the QRE language. The

QRE compiler then generates the low-level implementation whose space complexity and per-item processing time complexity are constant — that is, independent of the number of samples processed so far (see Section 4 of [6]). Furthermore, we show how the QRE compiler can *statically* compute an upper bound on the cost of processing each item, where the cost can be, for example, the energy consumption on a specific platform. This assures predictable real-time performance. Such estimates, provided early in the design cycle, allow one to compare design alternatives (that is, different variants of the monitoring algorithm) statically in terms of their achievable worst-case costs. Such analysis complements average-case analysis (i.e., measured performance when running the algorithm on a typical load). We demonstrate the latter type of analysis by profiling the energy consumption of the QRE on a signals database on a given hardware platform.

The paper is organized as follows. Section II gives a background on cardiac function, necessary for understanding the complexity of arrhythmia monitoring. Section III motivates the programming of AMAs in QREs, and Section IV introduces the QRE formalism and the Java library that implements it. This library is available online at [18]. Section V describes one representative AMA and Section VI details its QRE implementation. The Java library is used in Section VII to illustrate the implemented AMA on a database of arrhythmia episodes. Section VIII describes how to compute upper bounds on QRE cost, like per-item energy consumption. Section IX summarizes related work and Section X concludes the paper.

II. BACKGROUND ON CARDIAC FUNCTION

To understand the arrhythmia monitoring algorithm presented in this paper and appreciate its complexities, it is necessary to first understand some basics of cardiac electrophysiology: how the heart beats normally, why it could go into arrhythmia, and what measurements are available to an implantable device to detect this.

A. Cardiac electrophysiology

The heart has two upper chambers called the *atria* and two lower chambers called the *ventricles* (see Fig. 1). The synchronized contractions of atria and ventricles assure an adequate supply of oxygenated blood to the rest of the body. This contraction is driven by electrical activity in the heart, which originates in the right atrium, floods the atria first, then conducts down to the ventricles and floods those in turn. The cardiac muscle contracts as it is being traversed by the electrical wavefront, i.e., as it *depolarizes*. In a first approximation which is sufficient for understanding AMAs, we may consider that this contraction is an instantaneous event, and refer to it as an (atrial or ventricular) *beat*. This normal pattern of electrical activity is referred to as Normal Sinus Rhythm (NSR), after the *sino-atrial node* where the electricity normally originates. Disturbances of NSR are referred to as *arrhythmias*. They can arise because of structural defects in the cardiac muscle, like a re-entrant circuit around which the electrical waveform circulates very fast, or because of irritable tissue that starts to depolarize faster than the sino-atrial node.

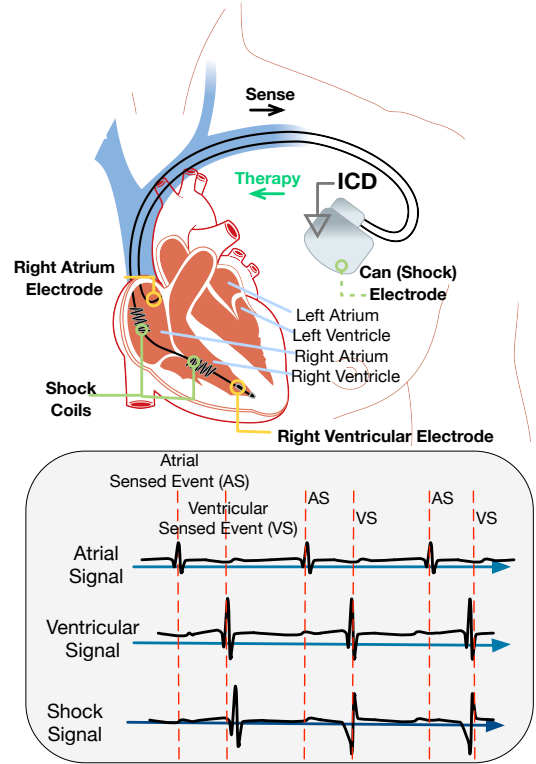


Fig. 1: ICD and its connection to the heart

Ventricular Tachycardia (VT) is an example of an arrhythmia originating in the ventricles, in which the ventricles depolarize at a very high rate and effectively drive the rhythm. This high rate of depolarization doesn't give enough time for the muscle to contract and relax properly, which can result in insufficient blood supply. If the VT is sustained, or degenerates into Ventricular Fibrillation (VF) (Fig. 2), it is fatal within a minute. An abnormally fast heart rate that originates in the atria and/or the conduction system above the ventricles is referred to as a *Supra-ventricular Tachycardia (SVT)*. An SVT causes patient discomfort but is not fatal in the short-term and does not require device treatment. Most fast arrhythmias fall under these two categories: VT or SVT.

B. Implantable devices

Two types of implantable devices monitor a heart's rhythm continuously to detect abnormally fast arrhythmias, aka *tachycardias*. The first is Implantable Cardioverter Defibrillators (ICDs). An ICD is inserted under the pectoral muscles, and has one or two leads that are directly implanted in the cardiac chambers, and through which it measures local electrical activity - see Fig. 1. The measured signals are known as *electrograms*, or EGMs, and are termed 'atrial' or 'ventricular' depending on the chamber where they are measured¹. See Fig. 3. An ICD uses EGMs to distinguish a wide range of tachycardias. If it detects a potentially fatal tachycardia, then it delivers therapy to the heart in the form of either low-energy

¹In this paper, we will ignore the so-called 'shock EGM' as it will not be used in describing arrhythmia monitoring algorithms.

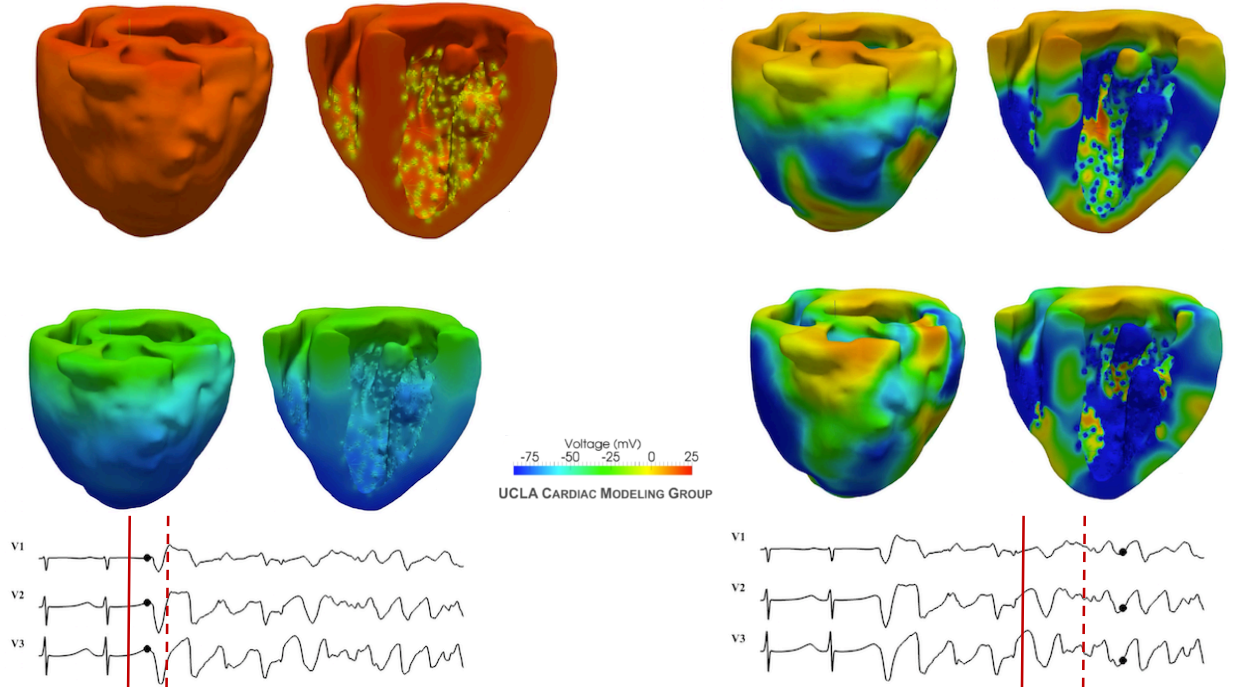


Fig. 2: Electrical activity during Normal Sinus Rhythm (NSR) and Ventricular Fibrillation (VF). The color scale runs from blue = rest state to red = excited (aka depolarized) state. (Colors in digital version). In the top left, the ventricles are shown from two different angles, during a phase of NSR. The ventricles are fully excited. The bottom left panel shows a later phase of the same beat, where the ventricles are progressively relaxing, starting with the apex (the pointed tip of the heart). This orderly propagation insures adequate muscle contraction and blood flow. Three surface ECGs are shown beneath the left column, with red bars indicating the timing of the two snapshots. Note the periodic pattern. The right column shows two snapshots during VF (earlier snapshot on top). Note the disorganized nature of the electrical activity, wavefront breakup, and the multiple regions of depolarization. Note also the change in the surface ECG from periodic and regular (early on) to disorganized. The AMA reads two such signals (obtained, however, intra-cardially and not from the surface) and tries to detect fibrillation. [Obtained from video of a simulation of the ventricles by the UCLA Cardiac Modeling Group, courtesy of Luigi Perrotti]

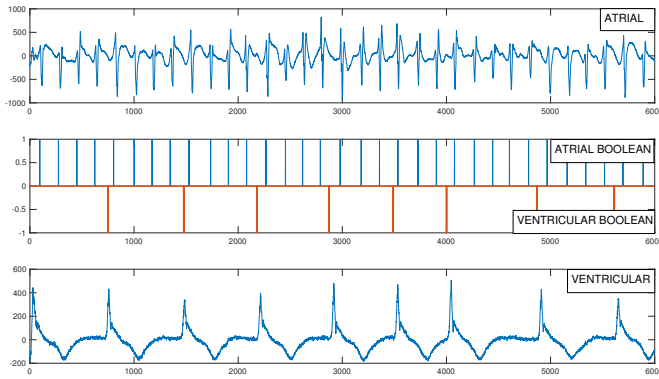


Fig. 3: EGMs (top and bottom panels) and corresponding boolean beat signals (middle) during atrial tachycardia. Beats correspond to peaks in the EGMs.

pacing sequences or (possibly more than one) very high-energy shock. Either way, the goal of the therapy is to stop the current rhythm and allow a normal rhythm to start. VTs and SVTs can share similar heart rates and other characteristics, so an SVT can be mis-diagnosed as a VT. This is problematic because shock therapy used to stop a VT can deliver between 30-60 Joules of energy at around 700 Volts in under 15ms [19], directly to the heart, which is very painful to the patient², and

²Patients compare the shock to a “horse kicking you in the chest”.

has been shown to increase morbidity [20]. Therefore, one of the biggest challenges for ICDs is to discriminate between VF and sustained VT that typically requires a shock, and SVT that typically should not be shocked [21]. This paper will present one particular ICD AMA in detail in Section V.

The second type of device that monitors tachycardias is the Insertable Loop Recorder (ILR) (also known as Implantable Cardiac Monitor). An ILR is a small device (the smallest ILR on the market is smaller than a key) that is inserted sub-cutaneously, and monitors surface ECG signals. It uses these signals to compute a number of long- and short-term statistics of the rhythm, and in particular to detect Atrial Fibrillation (AF) episodes. AF is an abnormally fast and disorganized atrial rhythm that can lead to fainting spells, and which, in the long term, contributes to blood clot formation. These clots can cause a stroke upon reaching the brain. The ILR does not have any therapeutic functions, but only monitors the heart rhythm. As an example, Biotronik’s BioMonitor [22] calculates and stores the following daily quantities, in a sliding window of 240 days where the oldest day drops out of the window. The quantities include 1) the average daily heart rate, 2) the daily minimum average heart rate, where the averages are calculated over consecutive blocks of 10 mins in the day, 3) daily heart rate variability, defined as the standard deviation of the sliding 5-minute averages, and 4) the rate histogram, where each heartbeat is binned into bins of width

10 beats-per-minute (bpm). In addition, the BioMonitor will take consecutive windows of n beats and count the number of cycle lengths that fall below a fixed value in each window.

Remote continuous monitoring has recently been shown to improve treatment outcomes [23] and to reduce time-to-treatment for patients with atrial tachycardia burden [24], so it is important to develop algorithms that can monitor over longer periods of time and/or compute more advanced statistics that can better detect the arrhythmia burden.

C. Device measurement: from real-valued to boolean signal

Formally, an EGM is a uniformly-sampled, discrete-time real-valued bounded signal. An EGM signal can be characterized by the *timing of beats* that produced it, and the *morphology of the signal itself*. To detect the beat timing (i.e., when the chamber is contracting), the peaks of the EGM are detected [25]. The output of peak detection is a discrete-time boolean signal, where a 1 indicates a beat. See Fig. 3. Beat timing is crucial to an arrhythmia's detection, since it is used in all discriminators.

The 'morphology' refers to the shape of the EGM. The so-called 'shock' EGMs during an atrially-driven rhythm look different from the shock EGMs during a ventricularly-driven rhythm. The ICD uses this to help it determine whether the current arrhythmia is an SVT or VT. In this paper, and in order to keep the exposition simple, we will only work with the beat signal, i.e., the boolean signal produced by peak detection on the local atrial and ventricular channels, as shown in Fig. 3.

III. STREAMING ALGORITHMS FOR ARRHYTHMIA DETECTION

An AMA is naturally viewed as a *pipeline of streaming algorithms*, where each node of the pipeline performs a streaming calculation on its input signal, and passes its output signal to the next node. So what is a streaming algorithm? And why view arrhythmia monitors as streaming algorithms? The main characteristics of a streaming algorithm are that it views its input as a sequence, or *stream*, of items from some data domain, arriving one at a time. It gets to process each item only once, after which it discards it and moves on to the next item in the input stream. After processing each item, the algorithm produces an output value (which might also be null). A streaming algorithm has limited memory available (much smaller than the length of the stream which, for practical purposes, may be regarded as infinite), and limited processing time. Section IV gives several examples of streaming calculations.

The following considerations, which govern the design and execution of an AMA, establish the suitability of the streaming model of calculation for AMA. First, an AMA's input is a uniformly sampled discrete-time electrical signal that arrives in real-time, one sample at a time, and thus can be viewed as a stream. Second, when running on an ICD, the AMA has a delay constraint. Namely, not much time must elapse between the onset of a fatal VT and the moment that the AMA detects it, because this delays the delivery of therapy. This requirement translates directly into a requirement of small

processing time per item of the input signal, which is a key constraint on streaming algorithms. Third, ICDs and ILRs share a power consumption concern. Indeed, power is the *main* non-functional design factor for these devices. Even for today's ICDs, which can have a battery life between 7 and 11 years, an additional 3 months of battery life are still worth pursuing [26], since they can mean the difference between having to surgically replace the ICD or not. Because most ICD and ILR recipients are older patients with health complications [27], it is desirable to prolong battery life and reduce the likelihood of a replacement [26]. The power in an ICD is consumed by the monitoring algorithms, the shock therapy, and the pacing therapy. Although shocks are the single most power-hungry event, over an average device's lifetime, they will only consume 3% of the battery, and it is exceedingly rare that they consume more than 36% [28]. The rest is shared between pacing and monitoring. Thus it is important to reduce the power cost of monitoring. For ILRs, because they do not have any therapeutic functions, most of the power is consumed by monitoring. Thus an AMA has a more general *small cost-per-item constraint*.

If AMAs are viewed as streaming algorithms, then it follows that they are best programmed using a *streaming programming language*. That is, a language that is expressly designed and optimized for describing streaming algorithms and automatically generating efficient code from the program description. Indeed, it is important to note the productivity gains achievable by using a Domain Specific Language (DSL). It is generally agreed that programming in a DSL results in greater productivity for the development teams producing the software - see, e.g., [29] and [30] where development time reductions of 5-7x are routinely reported. During the *design exploration stage* when AMAs are developed, tweaked and compared, it is helpful to program in a language that allows high-level reasoning about the stream as the basic object of manipulation and easy capture of patterns in the stream.

The StreamQRE language [18], [6] permits such a declarative way of programming. StreamQRE (pronounced 'stream query') allows the developer to create Quantitative Regular Expressions (QREs), which are a quantitative extension of regular expressions. A QRE declares how the stream should be divided up (by matching against a regular expression) and which arbitrary operations should be executed on the matching pieces. Similarly to regular expressions, QREs can be combined using quantitative extensions of regular combinators to form more complex computations. QREs are described in detail in the next section. QREs also provide theoretical guarantees on the memory, time and energy consumed to process a data item by the resulting algorithm. Specifically, a QRE has per-item memory and time complexities and energy consumption that are independent of the length of the stream, and depend only on the size of the query. Thus, a QRE program automatically gives a baseline implementation with constant cost per data item. One also automatically gets a static upper bound on the per-item cost of a QRE. This allows a cost comparison to choose between similarly-performing algorithms. Such early feedback on cost allows early design exploration, at a point in the design cycle where algorithmic

changes are easy and can be correlated to cost decrease, and where it is well-established that the most gains are possible.

Of course, during design exploration, AMAs can also be programmed in a general purpose language like C++, and in a non-streaming fashion, e.g., by keeping a sliding window big enough to store the entire signal segment of interest and repeating all computations with every new sample that enters the window. However, this requires the programmer to explicitly think of keeping state information and minimizing it, and to think of various sources of delay in her code and minimize those. Moreover, it is much harder to obtain upper bounds on cost (whether power, memory or processing time) of freeform code than the cost of QREs, which have sufficient structure to enable the above analysis. Finally, when it is possible, analysis of cost at code-level enables late-stage implementation changes whose effect on cost will typically be small compared to early-stage algorithmic changes.

In summary, the advantages of describing AMAs in a streaming language, and more specifically in StreamQRE, over describing them in a general purpose language, are:

- A more natural way to reason about the algorithm's streaming operation, which highlights opportunities to reuse computation results.
- A declarative way to program the algorithm, which enables reasoning at the stream level and how it needs to be divided hierarchically and processed, rather than get bogged down in item-level computations.
- An automatic implementation of the algorithm that guarantees bounded memory, runtime, and energy consumption per data item that is independent of the input signal length. The algorithm designer is relieved from having to explicitly maintain state.
- An automatic way to obtain an upper bound on the cost of a QRE as a function of the costs of the basic operations. This cost can model power consumption, for example.

IV. INTRODUCTION TO QRES

This section is an introduction to the language of *Quantitative Regular Expressions* (QREs). First, we present the semantic model of streaming functions for describing stateful streaming transformations. Then, we introduce the language of QREs and define some derived constructs that will be used later to specify the arrhythmia detection algorithm. Finally, we discuss an efficient implementation of QREs as a Java library.

A. Streaming functions

We introduce here the basic semantic objects for our language, called *streaming functions*, which are partial functions from sequences of input data items to an output value. Each streaming function has an associated *rate* that captures its domain, that is, as the function reads the input data stream, the rate characterizes the prefixes that trigger the production of the output. In our language, the rates are required to be *regular*, captured by symbolic regular expressions, which lead to decision procedures for constructing well-typed expressions.

As a motivating example, consider a stream that consists of integers and special separator symbols #:

3 -5 4 1 -3 # 7 -2 9 # 1 -4

Given such an input data stream, suppose we want to specify the transformation illustrated below that outputs at every occurrence of the # symbol the sum of all integers from the start of the stream.

input : 3 -5 4 1 -3 # 7 -2 9 # 1 -4
output : 0 14

This transformation can be modeled by a streaming function, i.e. a partial function $f : D^* \rightarrow \mathbb{Z}$, where $D = \mathbb{Z} \cup \{\#\}$ is the set of input data items. For example, $f(3 -5 4 1 -3 \#) = 0$ and $f(3 -5 4 1 -3 \# 7 -2 9 \#) = 14$. The rate of f is the set of all finite sequences over D that end with #, which is denoted by the regular expression $D^* \cdot \#$. This rate is also captured by the equivalent expression $(\mathbb{Z}^* \cdot \#)^+$, where $\mathbb{Z}^* \cdot \#$ matches a block of integers terminated by a # symbol.

Suppose now that we want to process further the output stream produced by f in order to emit at every occurrence of a negative output of f the count of all negative outputs of f so far. This second processing state is described by a streaming function $g : \mathbb{Z}^* \rightarrow \mathbb{N}$, whose rate is denoted by the regular expression $\mathbb{Z}^* \cdot \mathbb{Z}^{<0}$, that counts the number of negative input elements and emits the count at every occurrence of a negative input item. We write $\mathbb{Z}^{<0}$ for the set of negative integers. The overall computation is described by the *streaming composition* $f \gg g$, which supplies the stream of outputs produced by f as the input stream to g .

B. Quantitative Regular Expressions

We will introduce now the language of *Quantitative Regular Expressions* (QREs) for representing stream transformations. For brevity, we also call these expressions *queries*. A query represents a streaming transformation whose domain is a regular set over the input data type.

To define queries, we first choose a typed signature which describes the basic data types and operations for manipulating them. We fix a collection of *basic types*, and we write A, B, \dots to range over them. This collection contains the type \mathbb{B} of boolean values, and the unit type \mathbb{U} whose unique inhabitant is denoted by `def`. It is also closed under the cartesian product operation \times for forming pairs of values. Typical examples of basic types are the natural numbers \mathbb{N} , the integers \mathbb{Z} , the rationals \mathbb{Q} , and the real numbers \mathbb{R} . We write $a : A$ to mean that a is of type A . For example, we have `def` : \mathbb{U} .

We also fix a collection of *basic operations* on the basic types, for example the k -ary operation $op : A_1 \times \dots \times A_k \rightarrow B$. The identity function on D is written as $\text{id}_D : D \rightarrow D$, and the operations $\pi_1 : A \times B \rightarrow A$ and $\pi_2 : A \times B \rightarrow B$ are the left and right projection respectively. We assume that the collection of operations contains all identities and projections, and is closed under pairing and function composition. To describe derived operations we use a variant of lambda notation that is similar to Java's lambda expressions [31]. That is, we write $(A x) \rightarrow t(x)$ to mean $\lambda x:A.t(x)$, which is an

(anonymous) function that takes an argument x of type A and returns the value $t(x)$. We write $(A\ x, B\ y, C\ z) \rightarrow t(x, y, z)$ to mean $\lambda x:A, y:B, z:C. t(x, y, z)$. For example, the identity function on D is $(D\ x) \rightarrow x$, the left projection on $A \times B$ is $(A\ x, B\ y) \rightarrow x$, the right projection on $A \times B$ is $(A\ x, B\ y) \rightarrow y$, and $(D\ x) \rightarrow \text{def}$ is the unique function from D to \mathbb{U} . We will typically use lambda expressions in the context of queries from which the types of the input variables can be inferred, so we will omit the types as in $(x, y) \rightarrow x$.

For every basic type D , assume that we have fixed a collection of *atomic predicates*, so that the satisfiability of their Boolean combinations (built up using the Boolean operations: and, or, not) is decidable. We write $\varphi : D \rightarrow \mathbb{B}$ to indicate that φ is a predicate on D , and we denote by $\text{true}_D : D \rightarrow \mathbb{B}$ the predicate that is always true. The predicate $((\mathbb{Z}\ x) \rightarrow x > 0) : \mathbb{Z} \rightarrow \mathbb{B}$ is true of the strictly positive integers.

Example 4.1: We consider a Boolean ventricular heart signal, where the data items are values of type $\mathbb{B} = \{0, 1\}$. A value 1 indicates a ventricular contraction of the heart, and a value 0 indicates the absence of a contraction. The signal is sampled uniformly with a sampling rate of f Hz. The predicates $\neg \text{isV}$ and isV test if a Boolean value is zero or one respectively. \square

For a type D , we define the set of *symbolic regular expressions over D* [32], denoted $\text{RE}\langle D \rangle$, with the grammar:

$r ::= \varphi$	[predicate on D]
ε	[empty sequence]
$r \sqcup r$	[nondeterministic choice]
$r \cdot r$	[concatenation]
r^*	[iteration].

The concatenation symbol \cdot is sometimes omitted, that is, we write rs instead of $r \cdot s$. The expression r^+ (iteration at least once) abbreviates $r \cdot r^*$. We write $r : \text{RE}\langle D \rangle$ to indicate the r is a regular expression over D . Every expression $r : \text{RE}\langle D \rangle$ is interpreted as a set $\llbracket r \rrbracket \subseteq D^*$ of finite sequences over D :

$$\llbracket \varphi \rrbracket \triangleq \{d \in D \mid \varphi(d) \text{ is true}\}$$

and the rest of the regular construct have their usual interpretations. Two expressions are said to be *equivalent* if they denote the same language.

Example 4.2: The symbolic regular expression $(\neg \text{isV})^* \cdot \text{isV}$ denotes sequences of samples that contain a single ventricular beat (contraction) at the end. \square

A string can be matched efficiently against a regular expression if there's only one way in which it could match the expression. Intuitively, this reduces the number of possible matches that have to be kept track of. The notion of *unambiguity* for regular expressions [33] is a way of formalizing the requirement of uniqueness of parsing. The languages L_1, L_2 are said to be *unambiguously concatenable* if for every word $w \in L_1 \cdot L_2$ there are unique $w_1 \in L_1$ and $w_2 \in L_2$ with $w = w_1 w_2$. The language L is said to be *unambiguously iterable* if for every word $w \in L^*$ there is a unique integer $n \geq 0$ and unique $w_i \in L$ with $w = w_1 \cdots w_n$. The definitions of unambiguously concatenability and unambiguous iterability

extend to regular expressions in the obvious way. Now, a regular expression is said to be *unambiguous* if it satisfies the following:

- 1) For every subexpression $e_1 \sqcup e_2$, e_1 and e_2 are *disjoint*.
- 2) For every subexpression $e_1 \cdot e_2$, e_1 and e_2 are *unambiguously concatenable*.
- 3) For every subexpression e^* , e is *unambiguously iterable*.

Example 4.3: Consider the finite alphabet $\Sigma = \{a, b\}$. The regular expression $r = (a \sqcup b)^* b (a \sqcup b)^*$ denotes the set of sequences with at least one occurrence of b . It is ambiguous, because the subexpressions $(a \sqcup b)^* b$ and $(a \sqcup b)^*$ are not unambiguously concatenable: the word $w = ababa$ matches r , but there are two different splits $w = ab \cdot aba$ and $w = abab \cdot a$ that witness the ambiguity of parsing. The regular expressions $a^* b (a \sqcup b)^*$ and $(a \sqcup b)^* b a^*$ are both equivalent to r , and they are unambiguous. \square

Checking whether a regular expression is unambiguous can be done in polynomial time. For the case of symbolic regular expressions this results still holds, under the assumption that satisfiability of the predicates can be decided in unit time [34].

After these preliminaries, we now define quantitative regular expressions, or queries, recursively. Informally, a query f is a symbolic regular expression, called the *rate* of f and written $R(f)$, with a way to compute quantities over the strings that match the expression. The rate denotes the domain of the transformation that f represents. The definition of the query language has to be given simultaneously with the definition of rates (by mutual induction), since the query constructs have typing restrictions that involve the rates. We annotate a query f with a type $\text{QRE}\langle D, C \rangle$ to denote that the input stream has elements of type D and the outputs are values of type C .

1) *Atomic queries:* The basic building blocks of queries are expressions that describe the processing of a single data item. Suppose $\varphi : D \rightarrow \mathbb{B}$ is a predicate over the data item type D and $op : D \rightarrow C$ is an operation from D to the output type C . Then, the *atomic query* $\text{atom}(\varphi, op) : \text{QRE}\langle D, C \rangle$, with rate φ , is defined on single-item streams that satisfy the predicate φ . The output is the value of op on the input element.

Notation: It is very common for op to be the identity function, and φ to be the always-true predicate. So, we abbreviate the query $\text{atom}(\varphi, \text{id}_D)$ by $\text{atom}(\varphi)$, and the query $\text{atom}(\text{true}_D)$ by $\text{atom}()$.

Example 4.4: For the Boolean ventricular heart signal, the query that matches a single item that is a heartbeat and returns nothing is $f = \text{atom}(\text{isV}, x \rightarrow \text{def})$. The type of f is $\text{QRE}\langle \mathbb{B}, \mathbb{U} \rangle$ and its rate is isV . \square

2) *Empty sequence:* The query $\text{eps}(c) : \text{QRE}\langle D, C \rangle$, where c is a value of type C , is only defined on the empty sequence ε and it returns the output c .

3) *Iteration:* Suppose that we want to iterate a computation $f : \text{QRE}\langle D, A \rangle$ over consecutive subsequences of the input stream and aggregate all these output values sequentially using an initial value $c : B$ and an aggregation operation $op : B \times A \rightarrow B$. The iteration query

$$\text{iter}(f, c, op) : \text{QRE}\langle D, B \rangle$$

describes this computation. More specifically, we split the input stream w into subsequences $w = w_1 w_2 \dots w_n$, where

each w_i matches f . The output values $a_1 a_2 \dots a_n$ with $a_i = f(w_i)$ are combined using the list iterator *left fold* with start value $c : B$ and aggregation operation $op : B \times A \rightarrow B$. This can be formalized with the combinator

$$\text{fold} : B \times (B \times A \rightarrow B) \times A^* \rightarrow B,$$

which takes an initial value $b : B$ and a stepping map $op : B \times A \rightarrow B$, and iterates through a sequence of values of A :

$$\begin{aligned} \text{fold}(b, op, \varepsilon) &= b \\ \text{fold}(b, op, \gamma a) &= op(\text{fold}(b, op, \gamma), a) \end{aligned}$$

for all sequences $\gamma \in A^*$ and all values $a \in A$. For example, $\text{fold}(b, op, a_1 a_2) = op(op(b, a_1), a_2)$.

In order for $\text{iter}(f, c, op)$ to be well-defined as a function, every input stream w that matches $\text{iter}(f, c, op)$ must be uniquely decomposable into $w = w_1 w_2 \dots w_n$ with each w_i matching f . This requirement can be expressed equivalently as: the rate $R(f)$ is unambiguously iterable.

Example 4.5: For the Boolean heart signal, the query g below matches a sequence of data items that are not heartbeats and returns their count:

$$\begin{aligned} f : \text{QRE}(\mathbb{B}, \mathbb{B}) &= \text{atom}(\neg \text{isV}) \\ g : \text{QRE}(\mathbb{B}, \mathbb{N}) &= \text{iter}(f, 0, (x, y) \rightarrow x + 1) \end{aligned}$$

The rate of f is $\neg \text{isV}$, and the rate of g is $(\neg \text{isV})^*$. \square

4) **Combination and application:** Assume the queries f and g describe stream transformations with outputs of type A and B respectively that process the same set of input sequences, and op is a function of type $A \times B \rightarrow C$. Then,

$$\text{combine}(f, g, op) : \text{QRE}(D, C)$$

describes the computation where the input is processed according to both f and g in parallel and their results are combined using op . This computation is meaningful only when both f and g are defined on the input sequence. So, we demand w.l.o.g. that the rates of f and g are equivalent.

This binary combination construct generalizes to an arbitrary number of queries. For example, we write

$$\text{combine}(f, g, h, (x, y, z) \rightarrow op(x, y, z))$$

for the ternary variant. In particular, we write $\text{apply}(f, op)$ for the case of one argument.

Example 4.6: For the Boolean heart signal, suppose g counts all heartbeats seen so far and h counts all data items. Then, the query k below computes the ratio of these values.

$$\begin{aligned} f : \text{QRE}(\mathbb{B}, \mathbb{N}) &= \text{atom}(\text{true}_{\mathbb{B}}, x \rightarrow \text{if } x \text{ then } 1 \text{ else } 0), \\ g : \text{QRE}(\mathbb{B}, \mathbb{N}) &= \text{iter}(f, 0, (x, y) \rightarrow x + y) \\ h : \text{QRE}(\mathbb{B}, \mathbb{N}) &= \text{iter}(\text{atom}(), 0, (x, y) \rightarrow x + 1) \\ k : \text{QRE}(\mathbb{B}, \mathbb{Q}) &= \text{combine}(g, h, (x, y) \rightarrow x/y) \end{aligned}$$

The rate of f is true and the rates of the queries g , h and k are all equal to true^* . \square

5) **Quantitative concatenation:** Suppose that we want to perform two streaming computations in sequence: first execute the query $f : \text{QRE}(D, A)$, then the query $g : \text{QRE}(D, B)$, and finally combine the two results using the operation $op : A \times B \rightarrow C$. The query

$$\text{split}(f, g, op) : \text{QRE}(D, C)$$

describes this computation. More specifically, we split the input into two parts $w = w_1 w_2$, process the first part w_1 according to f with output $f(w_1)$, process the second part w_2 according to g with output $g(w_2)$, and produce the final result $op(f(w_1), g(w_2))$ by applying op to the intermediate results.

In order for this construction to be well-defined as a function, every input w that matches $\text{split}(f, g, op)$ must be uniquely decomposable into $w = w_1 w_2$ with w_1 matching f and w_2 matching g . In other words, the rates of f and g must be unambiguously concatenable.

The binary split construct extends naturally to more than two arguments. For example, the ternary version would be $\text{split}(f, g, h, (x, y, z) \rightarrow op(x, y, z))$.

Example 4.7: For the Boolean heart signal, suppose that g matches sequences that end with a heartbeat and h counts the size of sequences without any heartbeat. Then, the query k below outputs the time that has elapsed since the last heartbeat.

$$\begin{aligned} f : \text{QRE}(\mathbb{B}, \text{Ut}) &= \text{iter}(\text{atom}(), \text{def}, (x, y) \rightarrow \text{def}) \\ g : \text{QRE}(\mathbb{B}, \text{Ut}) &= \text{split}(f, \text{atom}(\text{isV}), (x, y) \rightarrow \text{def}) \\ h : \text{QRE}(\mathbb{B}, \mathbb{N}) &= \text{iter}(\text{atom}(\neg \text{isV}), 0, (x, y) \rightarrow x + 1) \\ k : \text{QRE}(\mathbb{B}, \mathbb{N}) &= \text{split}(g, h, (x, y) \rightarrow y) \end{aligned}$$

The rate of f is true^* , that of g is $\text{true}^* \cdot \text{isV}$, the rate of h is $(\neg \text{isV})^*$, and the rate of k is $\text{true}^* \cdot \text{isV} \cdot (\neg \text{isV})^*$. \square

6) **Streaming composition:** A natural operation for query languages over streaming data is streaming composition: given two streaming queries f and g , $f \gg g$ represents the computation in which the stream of outputs produced by f is supplied as the input stream to g . Such a composition is useful in setting up the query as a pipeline of several stages. We allow the operation \gg to appear *only at the top-level* of a query. So, a general query is a pipeline of \gg -free queries. At the top level, no type checking needs to be done for the rates, so we do not define the function $R()$ for queries $f \gg g$.

Example 4.8: For the Boolean heart signal, suppose we want to emit at every heartbeat the average heart rate over the entire stream. We will describe this computation as a two-stage pipeline. The first stage (query h below) produces a sequence of natural numbers which correspond to the number of 0's between two consecutive 1's (heartbeats).

$$\begin{aligned} f : \text{QRE}(\mathbb{B}, \mathbb{N}) &= \text{iter}(\text{atom}(\neg \text{isV}), 0, (x, y) \rightarrow x + 1) \\ g : \text{QRE}(\mathbb{B}, \mathbb{N}) &= \text{split}(f, \text{atom}(\text{isV}), (x, y) \rightarrow x) \\ h : \text{QRE}(\mathbb{B}, \mathbb{N}) &= \text{split}(\text{iter}(g, \text{def}, (x, y) \rightarrow \text{def}), \\ &\quad g, (x, y) \rightarrow y) \end{aligned}$$

The rate of f is $(\neg \text{isV})^*$, the rate of g is $(\neg \text{isV})^* \cdot \text{isV}$, and the rate of h is $((\neg \text{isV})^* \cdot \text{isV})^+$. The second stage (query n

below) processes a stream of these numbers to compute the average heart rate in beats per minute.

$$\begin{aligned} \mathbf{k} : \text{QRE}(\mathbb{N}, \mathbb{N}) &= \text{iter}(\text{atom}(), 0, (x, y) \rightarrow x + y) \\ \mathbf{l} : \text{QRE}(\mathbb{N}, \mathbb{N}) &= \text{iter}(\text{atom}(), 0, (x, y) \rightarrow x + 1) \\ \mathbf{m} : \text{QRE}(\mathbb{N}, \mathbb{Q}) &= \text{combine}(\mathbf{k}, \mathbf{l}, (x, y) \rightarrow x/y) \\ \mathbf{n} : \text{QRE}(\mathbb{Q}, \mathbb{Q}) &= \text{apply}(\mathbf{m}, x \rightarrow (60 \cdot f)/x) \end{aligned}$$

where f is the sampling rate in Hz. The query \mathbf{m} computes the average number of samples between two consecutive heartbeats. The top-level query is the pipeline $\mathbf{h} \gg \mathbf{n}$. \square

7) **Global choice:** Given queries \mathbf{f} and \mathbf{g} of the same type with disjoint rates r and s , the query $\text{or}(\mathbf{f}, \mathbf{g})$ applies either \mathbf{f} or \mathbf{g} to the input stream depending on which one is defined. The rate of $\text{or}(\mathbf{f}, \mathbf{g})$ is the union $r \sqcup s$. This *choice* construction allows a case analysis based on a global regular property of the input stream.

Example 4.9: In our Boolean heart example, suppose we want to compute a statistic across days, where the contribution of each day is computed differently depending on whether or not an abnormally short interval between consecutive heartbeats occurred or not. Then, we can write a query summarizing the daily activity with a rate capturing normal days (the ones without any short interval) and a different query with a rate capturing abnormal days, and iterate over their disjoint union.

Consider the stream of interval lengths between consecutive heartbeats, i.e. the output stream of query \mathbf{h} defined in Example 4.8. We assume that T is the threshold for an abnormally short interval between two consecutive heartbeats. Query \mathbf{h} below computes the smallest interval length for sequences with at least one abnormally short interval:

$$\begin{aligned} \mathbf{f} : \text{QRE}(\mathbb{N}, \mathbb{Q}) &= \text{iter}(\text{atom}(x \rightarrow x > T), \infty, \min) \\ \mathbf{g} : \text{QRE}(\mathbb{N}, \mathbb{Q}) &= \text{iter}(\text{atom}(), \infty, \min) \\ \mathbf{h} : \text{QRE}(\mathbb{N}, \mathbb{Q}) &= \text{split}(\mathbf{f}, \text{atom}(x \rightarrow x \leq T), \mathbf{g}, \min) \end{aligned}$$

The rate of \mathbf{f} is $(x > T)^*$, the rate of \mathbf{g} is true^* , and the rate of \mathbf{h} is $(x > T)^* \cdot (x \leq T) \cdot \text{true}^*$. Query \mathbf{m} below computes the average interval length for sequences with no abnormally short interval:

$$\begin{aligned} \mathbf{k} : \text{QRE}(\mathbb{N}, \mathbb{N}) &= \text{iter}(\text{atom}(x \rightarrow x > T), 0, (x, y) \rightarrow x + y) \\ \mathbf{l} : \text{QRE}(\mathbb{N}, \mathbb{N}) &= \text{iter}(\text{atom}(x \rightarrow x > T), 0, (x, y) \rightarrow x + 1) \\ \mathbf{m} : \text{QRE}(\mathbb{N}, \mathbb{Q}) &= \text{combine}(\mathbf{k}, \mathbf{l}, (x, y) \rightarrow x/y) \end{aligned}$$

The rates of \mathbf{k} , \mathbf{l} and \mathbf{m} are all equal to $(x > T)^*$. The top-level query is then $\text{or}(\mathbf{h}, \mathbf{m})$. \square

C. Derived constructs

The core language of Section IV-B is expressive enough to describe many common stream transformations. We present below several derived constructs.

1) **Matching without output:** Suppose r is an unambiguous symbolic regular expression over the data item type D . The query $\text{match}(r)$, whose rate is equal to r , does not produce any output when it matches. This is essentially the same as

producing def as output for a match. The match construct can be encoded as follows:

$$\begin{aligned} \text{match}(\varphi) &\triangleq \text{atom}(\varphi, x \rightarrow \text{def}) \\ \text{match}(r_1 \sqcup r_2) &\triangleq \text{or}(\text{match}(r_1), \text{match}(r_2)) \\ \text{match}(r_1 \cdot r_2) &\triangleq \text{split}(\text{match}(r_1), \text{match}(r_2), (x, y) \rightarrow \text{def}) \\ \text{match}(r^*) &\triangleq \text{iter}(\text{match}(r), \text{def}, (x, y) \rightarrow \text{def}) \end{aligned}$$

An easy induction establishes that $R(\text{match}(r)) = r$.

2) **“Until” Iteration:** Suppose that ϕ and ψ are disjoint predicates on the input data type D , the function $op : C \times D \rightarrow C$ is an aggregation operation, and $c : C$ is the initial aggregate. The query $\text{iterUntil}(\phi, \psi, c, op)$ aggregates a sequence of data items that satisfy ϕ and stops when an item that satisfies ψ is found. It is encoded as:

$$\text{iterUntil}(\phi, \psi, c, op) \triangleq \text{split}(\text{iter}(\text{atom}(\phi), c, op), \text{atom}(\psi), (x, y) \rightarrow x)$$

The query has type $\text{QRE}(D, C)$ and rate $\phi^* \cdot \psi$.

3) **Stream Annotation:** Suppose that the input stream has items of type D , \mathbf{f} is a query of type $\text{QRE}(D, C)$, and we want to produce an output stream with items of type E in the following way: when the query \mathbf{f} produces an output (upon consumption of the input stream) apply $op_2 : D \times C \rightarrow E$ to the last input element and its output to get the final result, and when the query \mathbf{f} is undefined apply $op_1 : D \rightarrow E$ to the last input element. This computation is described by the query $\text{annt}(\mathbf{f}, op_1, op_2) : \text{QRE}(D, E)$ with rate D^+ . This annotation query can be encoded using the regular constructs of Section IV-B, but the encoding is complex and inefficient, so we provide a custom efficient implementation.

a) **Tumbling windows:** The term tumbling windows is used to describe the splitting of the stream into contiguous non-overlapping subsequences [35]. Suppose we want to describe the streaming function that iterates \mathbf{f} at least once and reports the result given by \mathbf{f} at every match. The following query expresses this behavior:

$$\text{iterLast}(\mathbf{f}) \triangleq \text{split}(\text{match}(R(\mathbf{f})^*), \mathbf{f}, (x, y) \rightarrow y).$$

The rate of $\text{iterLast}(\mathbf{f})$ is equal to $R(\mathbf{f})^+$.

4) **Efficient Sliding Windows:** Suppose we want to apply the query $\mathbf{f} : \text{QRE}(D, A)$ to consecutive nonoverlapping parts of the input, and efficiently aggregate the intermediate results over a sliding window of size W . That is, the W most recent output values of \mathbf{f} are aggregated to produce the final output. The aggregation is described by an initial aggregate $c : B$ and three functions: an *insertion* operation $\text{ins} : B \times A \rightarrow B$ describes how to add a new value of type A to the aggregate (of type B), the *removal* operation $\text{rmv} : B \times A \rightarrow B$ describes how to remove a value from the aggregate, and the *finalization* operation $op : B \rightarrow C$ computes the final result from the aggregate. This computation is described by the query

$$\text{wnd}(\mathbf{f}, W, c, \text{ins}, \text{rmv}, op) : \text{QRE}(D, C),$$

whose rate is equal to $R(\mathbf{f})^+$. This query can be encoded using the regular constructs of Section IV-B and an additional data type for FIFO queues (in order to maintain the buffer of values of type A that are currently in the active window).

```

// Process a single value: rate Double
QRe<Double, Double> f =
    Q.atomic(x -> true, x -> x);

// Sum of sequence of values: rate Double*
QRe<Double, Double> sum =
    Q.iter(f, 0.0, (x,y) -> x+y);

// Length of sequence of values: rate Double*
QRe<Double, Long> count =
    Q.iter(f, 0L, (x,y) -> x+1);

// Average of sequence of values: rate Double*
QRe<Double, Double> avg =
    Q.combine(sum, count, (x,y) -> x/y);

Iterator<Double> stream = ... // input stream

// evaluator for the query
Eval<Double, Double> e = avg.getEval();

// execution loop
Double output = e.start();
// e.start() returns null, if undefined
while (stream.hasNext()) {
    Double d = stream.next();
    output = e.next(d);
    // e.next(d) returns null, if undefined
}

```

Fig. 4: StreamQRE Library in Java: Computing the average of a sequence of values.

D. A Java Library of QREs

StreamQRE has been implemented as a Java library [18] in order to facilitate the easy integration with user-defined types and operations. The implementation covers all the core constructs of Section IV-B, and also provides optimizations for the derived constructs of Section IV-C (matching without output, “until” iteration, stream annotation, etc.).

Figure 4 gives a simple example that illustrates how to program with the StreamQRE Java library. The query `avg` describes the computation of the average of a sequence of values of type `Double`. The method `getEval`, which stands for “get evaluator”, is used to obtain an object that encapsulates the evaluation algorithm for the query. On this evaluator object, the methods `start` and `next` are used to initialize the algorithm and consume data items respectively.

V. AN ICD ARRHYTHMIA MONITORING ALGORITHM

We now describe in details an Arrhythmia Monitoring Algorithm (AMA) found in one of the ICDs on the market today [17]. All ICD AMAs on the market today take the form of a decision tree, such as the one in Fig. 5. Each node in the tree is a *discriminator*, which computes one feature of the input signal and decides, on its basis, how to branch. Thus, each discriminator returns a decision, Yes or No. We chose to present this particular AMA because variants on its discriminators can be found in the AMAs of all devices on the market. For example, all devices measure average heart rate, compare atrial and ventricular rates, measure rate

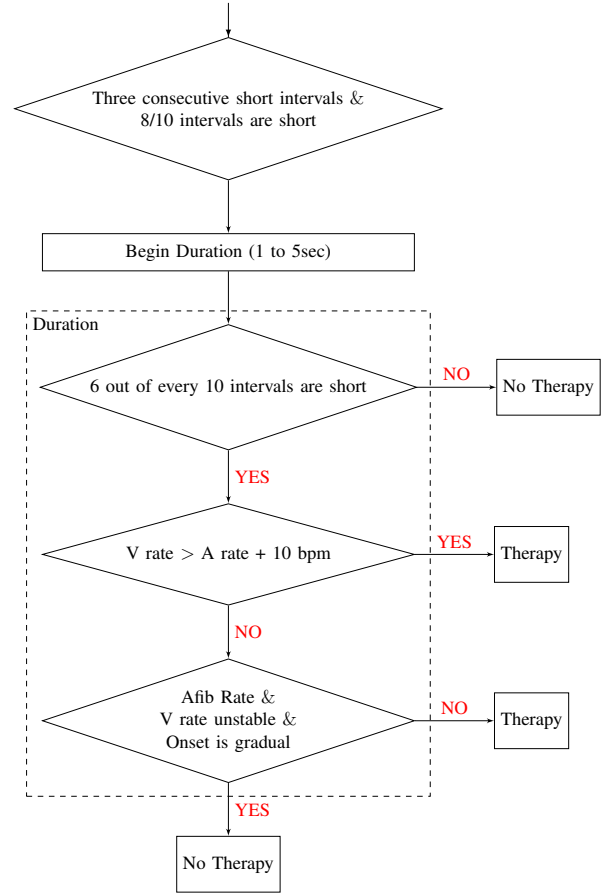


Fig. 5: Boston Scientific discrimination algorithm

variability, onset of arrhythmia, etc. The differences are in how variability is defined (variance or sum of absolute differences, for example), the size of windows for computing quantities, the way they are combined in the decision tree, etc.

A. Discriminators

Recall that the input to the AMA is a discrete-time boolean signal, which is obtained by running a peak detector on the discrete-time real-valued EGM signal. The peak detector outputs a 1 at peaks, and 0 otherwise. The signals we work with in this paper have a sampling period of 1ms. Formally, let $\mathbb{B} = \{0, 1\}$. At every time $t \in \mathbb{N}$, the AMA receives a data item s of the following form

$$s = (V, A, t) \in D := \mathbb{B} \times \mathbb{B} \times \mathbb{N} \quad (1)$$

where $V = 1$ indicates there is a ventricular beat at time t (and $V = 0$ indicates that there is not). Similarly for A . We will find the need to refer to the ventricular boolean signal separately, and we write $\mathbf{V} \in \mathbb{B}^*$ to denote it. It will also be called the ventricular *channel*. Similarly, $\mathbf{A} \in \mathbb{B}^*$ is the atrial *channel*. See Fig. 6. Given an item s , the function call `s.V` returns its first element; similarly for `s.A` and `s.t`.

An (atrial or ventricular) *interval* in a given channel is the interval of time between two consecutive beats. Its length is denoted by I , and is always an integer measured in milliseconds (ms). The average (atrial or ventricular) *rate* is the inverse of the average interval length.

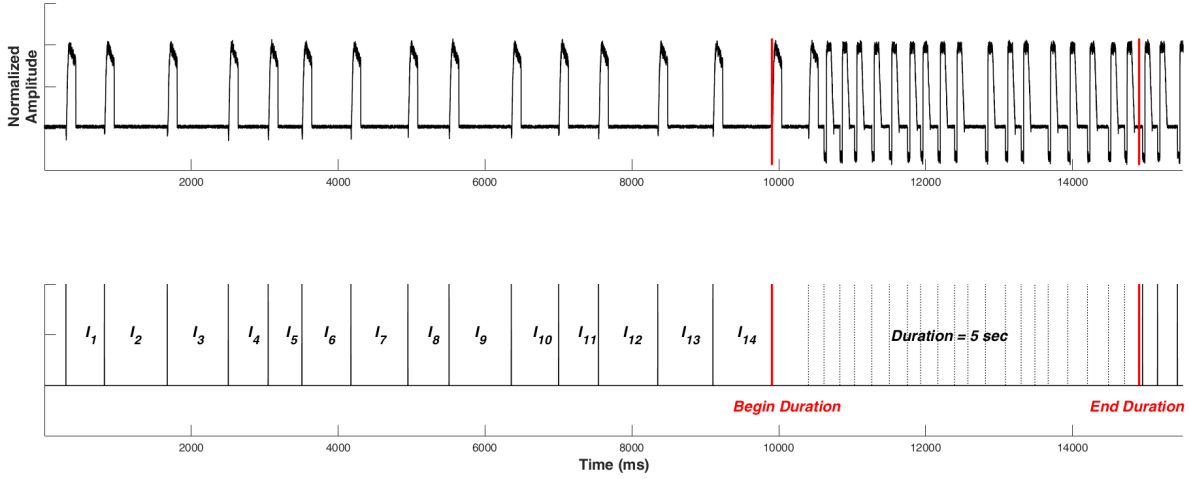


Fig. 6: Input stream from one channel. Measured electrogram (top figure) and corresponding Boolean stream (bottom figure). In the Boolean stream, spikes represent beats, and I_k is an interval of time between beats. Duration is a fixed time period, here set to 5 seconds.

The decision tree of the AMA we describe is shown in Fig. 5. It is made up of the following discriminators.

1) **Three Consecutive Short Intervals:** Three consecutive short intervals are required to initiate rhythm analysis, as they indicate a potentially accelerating rhythm. Therefore, this discriminator checks if three consecutive intervals are shorter than some pre-specified threshold T_{csi} . Referring to Fig. 6:

$$CSI := (I_5 < T_{csi}) \wedge (I_6 < T_{csi}) \wedge (I_7 < T_{csi}) \quad (2)$$

2) **8/10 Short Intervals:** A rhythm that becomes fast for a few beats then slows down again is not fatal and so should not cause therapy to be delivered. To estimate whether the current rhythm is sustained, this discriminator checks whether 8 out of 10 intervals are shorter than some threshold $T_{8/10}$. Referring to Fig. 6:

$$\text{Short8outof10} := |\{I_k : 5 \leq k \leq 14, I_k < T_{8/10}\}| \geq 8 \quad (3)$$

3) **Sudden Onset:** Ventricular Fibrillation (VF), which is fatal, usually occurs suddenly, whereas a tachycardia that accelerates gradually is usually non-fatal. The Onset discriminator quantifies the suddenness of tachycardia onset as follows. It operates in two steps, which process a window of $2m$ intervals. To help explain this discriminator using Fig. 6, we will assume $m = 4$. In the first step, it detects the ventricular beat in the first 4 intervals (I_1, \dots, I_4) at which the interval length decreased the most. This is the *pivot* beat. If the amount of decrease is greater than some threshold, Step I declares Onset. In the second step, the algorithm computes the differences between the average of 4 pre-pivot beats ($(I_1 + \dots + I_4)/4 := \mu$) and each of 4 post-pivot beats (I_5, \dots, I_8). I.e., it computes $d_5 = \mu - I_5, \dots, d_8 = \mu - I_8$. If at least 3 of these 4 differences d_5, \dots, d_8 is greater than a threshold, Step II declares Onset. If both stages declare Onset, the discriminator declares Sudden Onset. In our implementation, we simplify things by taking

the pivot to be the middle beat in the window of $2m = 8$ intervals. So SuddenOnset is computed as:

$$\text{SO-StepI} := I_{\text{post-pivot}} < \alpha \cdot I_{\text{pre-pivot}} \quad (4)$$

$$\text{SO-StepII} := |\{d_k : d_k > T_{o2}\}| \geq 3 \quad (5)$$

$$\text{SuddenOnset} := \text{SO-StepI} \wedge \text{SO-StepII}$$

When both Three Consecutive Short Intervals and 8/10 Short Intervals match, then a *Duration* is started. A *Duration* is a fixed-length time period (e.g., 5sec) during which the algorithm will continue to monitor the rhythm to see whether the arrhythmia is sustained, or it slows down and dies out. In the latter case, no therapy is delivered. See Fig. 6. During *Duration*, the following four discriminators are evaluated.

4) **A/V Rate Comparison:** If the ventricles have more beats than the atria, this is an almost sure sign that the arrhythmia is ventricular in origin (i.e., the ventricles are driving the atria and not the other way around). This discriminator compares the average ventricular heart rate r_V with the average atrial heart rate r_A , where the average is computed over the last 10 intervals in the *Duration* window:

$$\text{AVRate} := r_V > r_A + 10\text{bpm}$$

5) **Sliding 6/10:** Sometimes an arrhythmia terminates on its own, which is preferable to having the device terminate it with a shock. This discriminator continuously checks whether 6 out of every 10 intervals are short; if any 10 intervals fails this check, the discriminator declares No Therapy.

$$\text{Sliding6outof10} := \text{For every 10 intervals } I_1, \dots, I_{10} \\ |\{I_k : I_k < T_{6/10}\}| \geq 6$$

6) **Stability:** VF is an unstable rhythm, meaning that the interval lengths during fibrillation vary greatly. The Stability discriminator defines rhythm stability as being the variance in ventricular intervals' lengths during *Duration*. If variance is

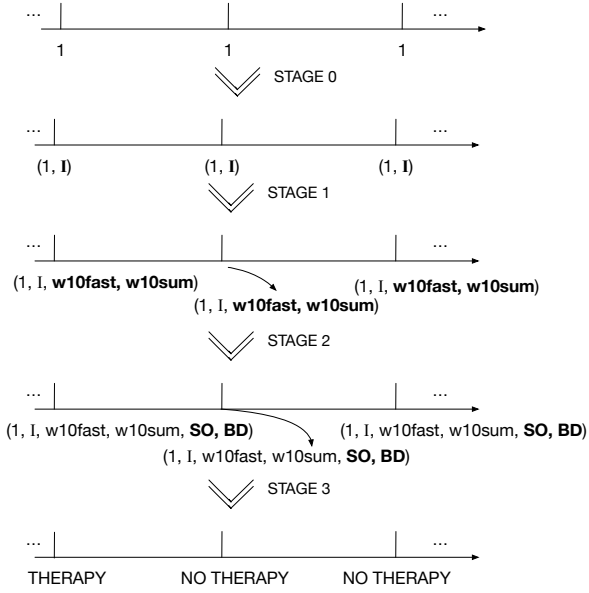


Fig. 7: The overall detection algorithm, shown for the ventricular channel and with the timestamp sequence omitted. The top stream gives the input boolean signal. Streams below it are annotated with the information in bold font. I = Interval Length, $w10fast$ = number of last 10 intervals that are short, $w10sum$ = sum of last 10 interval lengths, SO = Sudden Onset flag, BD = Begin Duration flag.

below a threshold T_{stab} , then the rhythm is deemed stable. With \bar{I} denoting the average interval length,

$$\text{Stability} := \frac{1}{n} \sum_{k=1}^n (I_k - \bar{I})^2 \leq T_{stab}$$

7) **AFib Rate**: Atrial Fibrillation (AF) is an atrially-driven rhythm with a high rate, and is one possible source of misclassification for the AMA. To circumvent this issue, this discriminator measures the atrial rate throughout the Duration. As long as at least 4/10 intervals are shorter than the AF threshold T_{af} , this discriminator decides that the current rhythm is in fact AF and therapy should be withheld.

SlidingAFib := For every 10 interval lengths I_1, \dots, I_{10}
 $|\{I_k : I_k < T_{af}\}| \geq 4$

VI. QRE IMPLEMENTATION OF THE ARRHYTHMIA MONITORING ALGORITHM

The QRE implementation of the BSC algorithm of Section V is divided into four main stages. The first two stages annotate the input signal with additional information: the lengths of the intervals between heartbeats, and some sliding-window statistics over them. The annotated stream is passed to the later stages in order to compute the discriminators for deciding whether therapy should be delivered or not. We give a high-level overview of each stage in Section VI-A, as well as more detailed descriptions and QREs implementations in Sections VI-B to VI-E.

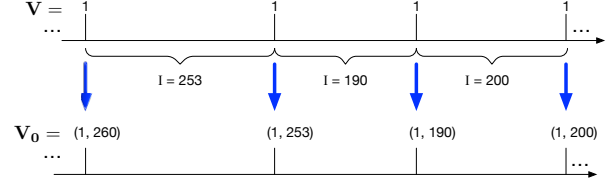


Fig. 8: Stage 0 annotates both channels V and A with interval lengths, i.e. the number of 0s between 1s. Here it is shown operating on the ventricular channel.

A. Overview of Implementation Stages

All discriminators described in Section V use the interval lengths between consecutive heartbeats. In order to simplify the later computations, it is useful to annotate the stream with this extra information so that it is readily available in the next processing steps. Similarly, there are some sliding-window statistics that are required for the discriminators “A/V Rate Comparison”, “Sliding 6/10” and “AFib Rate”. These quantities require looking at the 10 previous intervals to be computed. The specification of the algorithm is much easier if this information is already present in the stream, which obviates the need to look back 10 intervals into the past. This motivates our design choice to always annotate the stream with these useful sliding-window statistics.

The ICD’s AMA receives beats from the atrium and the ventricle. The input stream consists of data items that are of the form shown in (1). The implementation is a multi-stage pipeline, where each stage is a QRE. Each stage feeds its output stream to the following stage for further annotation and processing. They are:

- **Stage 0**: pre-processing stage which annotates the input stream s with the lengths of the ventricular and atrial intervals. See Figure 8. The output from this stage will be used in all subsequent stages. Call the output stream of this stage s_0 .
- **Stage 1**: augments its input stream s_0 with two pieces of information. The first is the total duration of every window of 10 consecutive intervals, in both channels. This will be used for the A/V Rate Comparison discriminator. The second piece of information is the number of short³ intervals in every window of 10 consecutive intervals, in both channels. This will be used for the Sliding 6/10 and AFib Rate Comparison discriminators. See Figure 9 for the computation of both quantities on the V channel. Call the output stream of this stage s_1 .
- **Stage 2**: detects the beginning of Duration, the period of time during which the rhythm is monitored for a fixed amount of time to confirm whether a suspected arrhythmia is indeed sustained and ventricular in origin. For Duration to be declared and monitored, both the Three Consecutive Short Intervals and 8/10 Short Intervals discriminators must return Yes. If Duration is

³I.e., those that are shorter than a pre-defined threshold $T_{6/10}$.

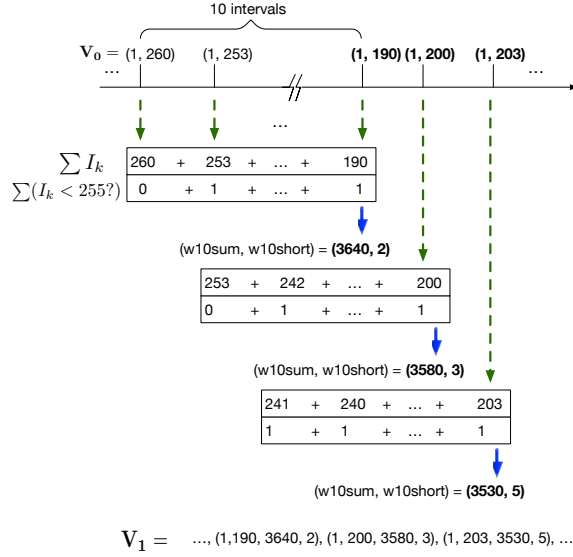


Fig. 9: Stage 1, shown acting on the V channel, augments V_0 with the total duration counter $w10sum$ and the short intervals counter $w10short$, computed over the last 10 intervals. Here, the threshold $T_{6/10} = 255$.

initiated as a result, the input stream s_1 is annotated with a **BD** marker to indicate the start of Duration. See Fig. 10. This stage also computes the Onset discriminator and annotates the stream with flag $SO = 1$ if it is met. Call the output stream of this stage s_2 .

- **Stage 3:** final stage, has input stream s_2 . It computes all discriminators in Duration: Stability, Sliding 6/10, AV Rate Comparison, and AFib Rate. Based on all these and the value of Onset, the stage makes a final decision of Therapy or No Therapy. See Figure 10.

REMARK. Because a QRE describes a streaming algorithm, each of the above stages operates continuously and issues an output with every new data item (including \perp if the string so far doesn't match). So for example, it is possible for Stage 2 to declare the start of Duration several times in a row, i.e., to output $BD = 1$ several times. See Fig. 14 for an example. The first Duration to end in a Therapy decision in Stage 3 will cause therapy to be scheduled, and the other Durations in progress are aborted. On the other hand, if the first Duration does not end in therapy, the subsequent ones continue to be monitored to their conclusion. Thus one important consequence of this streaming implementation is that it is possible for the QRE to track *multiple simultaneous* potential arrhythmias. In this way, no potentially fatal arrhythmia is missed.

We will explain now each stage in detail, and present the precise implementation in the StreamQRE language. Recall the QRE constructs of Section IV and the type of the input data items (1). Some computations are performed in the same way both on the atrial and the ventricular channel. In such cases we will only give the queries that describe the processing of the ventricular channel for the sake of brevity.

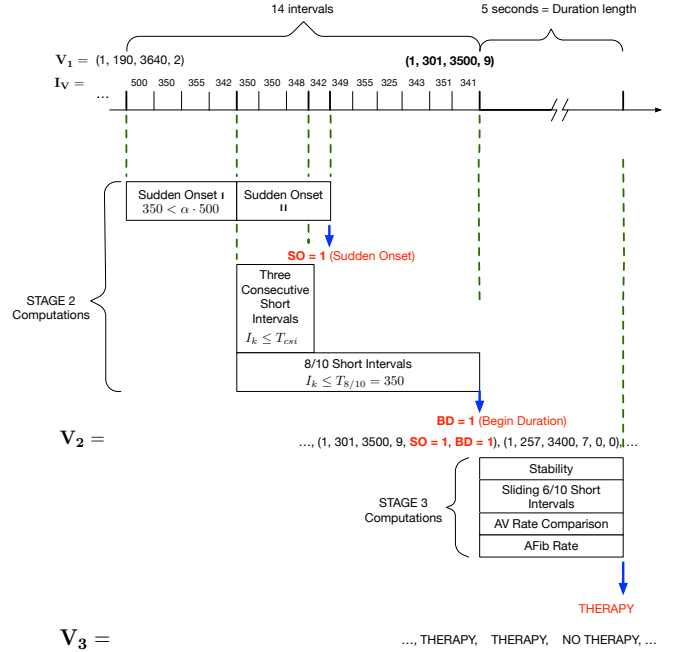


Fig. 10: Stages 2 and 3. The rectangles show the computed discriminators, and their width covers the part of the input stream used in the computation. E.g., “8/10 Short Intervals” uses the 10 intervals above its box, while Stability uses all intervals in the Duration window. Downward blue arrows indicate when a quantity is computed. E.g., the BD marker is computed every 14 intervals. SO and BD are added to stream V_1 to obtain stream V_2 . The A channel is not shown, though it enters in the calculation of AV Rate Comparison discriminator.

B. Stage 0: Annotate interval lengths

This stage annotates the stream with heartbeat interval lengths, that is, the lengths of the sequences between two consecutive heartbeats. So, the length of an interval of the form $100 \dots 001$ is the number of 0s between the 1s. This computation is performed both for the ventricular and atrial channel. The regular expression that describes a signal that has a single heartbeat at the end is 0^*1 . The query for computing the ventricular interval lengths is the following:

```

lincr = (x, y) -> x + 1, of type  $\mathbb{N} \times \mathbb{N} \rightarrow \mathbb{N}$ 
intV = iterUntil( $\neg isV$ , isV, 0, lincr)
allIntV = iterLast(intV) // rate ( $(\neg isV)^* \cdot isV$ )+
annt0V = annt(allIntV, x -> x, (x, c) -> x[IV := c])
stage0 = annt0V  $\gg$  annt0A

```

The query `intV` iterates over the 0s of the ventricular channel (predicate $\neg isV$) while incrementing a counter until it encounters a 1 (predicate `isV`). The query `allIntV` iterates `intV` over consecutive nonoverlapping subsequences, thus processing all ventricular intervals. The query `annt0V` annotates the input elements with the interval values I_V calculated by `allIntV`, and `annt0A` does the same with the atrial channel. See Fig. 8. Therefore, the output stream s_0 from this stage consists of

data items of the following form:

$$s_0 = (V, I_V, A, I_A, t) \in D_0 = (\mathbb{B} \times \mathbb{N})^2 \times \mathbb{N} \quad (6)$$

C. Stage 1: Sudden Onset and Short Intervals

The input stream for this stage consists of items of the form shown in (6). In this state, we first calculate the sum of interval lengths over a sliding window that consists of 10 intervals, and we annotate the stream with this information (see Fig. 9):

```
blockV = split(match((-isV)*), isV, (x, y) -> y.I_V)
wndSumV = wnd(blockV, 10, 0, (x, y) -> x + y)
stg1SumV = annt(wndSumV, x -> x, (x, c) -> x[SumV := c])
```

The query `blockV` matches 0^*1 in the ventricular channel and returns the length of the interval that ends with the matched 1. The query `wndSumV` executes `blockV` over a sliding window of size 10 and accumulates the interval lengths by summing them up. The query `stg1SumV` annotates the stream with all these sliding-window sums.

In the second part of this stage we also calculate the number of short ventricular intervals over a sliding window of size 10, where “short” is defined as being of length less than $T_{6/10}$.

```
shortV = apply(blockV,
               x -> if (x ≤ T6/10) then 1 else 0)
wndShortV = wnd(shortV, 10, 0, (x, y) -> x + y)
stg1ShortV = annt(wndShortV, x -> x,
                 (x, y) -> x[ShrtV := c])
```

The query `shortV` applies a thresholding operator to the output of `blockV`. As before, `shortV` is run in a sliding-window fashion using the `wnd` construct, and the output is annotated onto the stream using `annt`.

The same two computations are performed on the atrial channel, but with a different threshold, T_{afib} , for `stg1ShortA`. The final query for this state is the streaming composition of the above channel-specific computations:

```
stage1 =
  stg1SumV >> stg1ShortV >> stg1SumA >> stg1ShortA
```

The output stream s_1 of this stage consists of items (with re-arrangement) of the following form:

$$s_1 = (V, I_V, SumV, ShrtV, A, I_A, SumA, ShrtA, t) \in D_1 = (\mathbb{B} \times \mathbb{N}^3)^2 \times \mathbb{N} \quad (7)$$

D. Stage 2: Sudden Onset and Begin Duration

This stage computes the Sudden Onset discriminator and Begin Duration (**BD**) marker at every ventricular beat. In order to do this, the last 14 ventricular intervals I_1, I_2, \dots, I_{14} have to be considered, as shown in Fig. 10.

- The first 4 intervals I_1, I_2, I_3 and I_4 are used for Step I of “Sudden Onset”, defined in (4).
- The next 4 intervals I_5, I_6, I_7 and I_8 are used for Step II of “Sudden Onset”, defined in (5).
- The intervals I_5, I_6, I_7 are used for the “Three Consecutive Intervals” discriminator, defined in (2).

- The last 10 intervals I_5, I_6, \dots, I_{14} are used for the “8/10 Short Intervals” discriminator, defined in (3).

This stage splits the stream into consecutive intervals, and evaluates all the relevant discriminators over the last 14 intervals using the operation $opStage2 : \mathbb{N}^{14} \rightarrow \mathbb{B} \times \mathbb{B}$. The input to $opStage2$ is a vector of 14 ventricular interval lengths, and the output is a pair of Boolean values: the first component indicates the presence of “Sudden Onset” (SO), and the second component indicates the presence of “Begin Duration” (BD).

```
sobd = split(blockV, ..., blockV,
             (x1, ..., x14) -> opStage2(x1, ..., x14))
wndsobd = split(match(R(blockV)*), sobd, π2)
stage2 = annt(wndsobd, x -> x,
             (x, (c1, c2)) -> x[SO := c1, BD := c2])
```

The query `sobd` : $QRE\langle D_1, \mathbb{B}^2 \rangle$ matches 14 consecutive ventricular intervals, and applies the function $opStage2$ to their lengths in order to compute the Boolean flags for “Sudden Onset” and “Begin Duration”. This computation is executed in a sliding-window fashion and the output is used to annotate the stream. The output stream s_2 from Stage 2 contains data items of the following form:

$$s_2 = (s_1, SO, BD) \in D_2 = D_1 \times \mathbb{B}^2$$

E. Stage 3: Therapy Decision

This stage uses the four discriminators shown in Fig. 10 to make the final decision whether to apply therapy or not. Whenever “Begin Duration” (**BD**) is detected by the previous stage, the algorithm considers the window of N data items following **BD**, and the discriminators are computed using the information contained within this window. For example, if the Duration window is programmed to be 5 seconds, and the sampling rate is 256Hz, then the window contains $N = 5 \times 256 = 1280$ items. The query

```
stage3 = wnd(atom(), N, 0, ins, rmv, discr)
```

describes a sliding-window computation that maintains a buffer with all ventricular and atrial beats of the duration period. The function `ins` adds a new item to the buffer, the function `rmv` removes an expiring item from the buffer, and the operation `discr` computes the discriminators and the final therapy decision using only the items contained in the buffer.

F. Overall AMA Query

The top-level query for this Arrhythmia Monitoring Algorithm is the streaming composition of all stages (see Fig. 7):

$$AMA = stage0 \gg stage1 \gg stage2 \gg stage3.$$

VII. ILLUSTRATIVE EXAMPLES

A. Sample executions

Two examples will serve to illustrate the details of the query execution. Fig. 11 shows a Ventricular Fibrillation (VF) EGM signal along with the corresponding boolean beat stream. The results of running `stage2` on this signal are presented

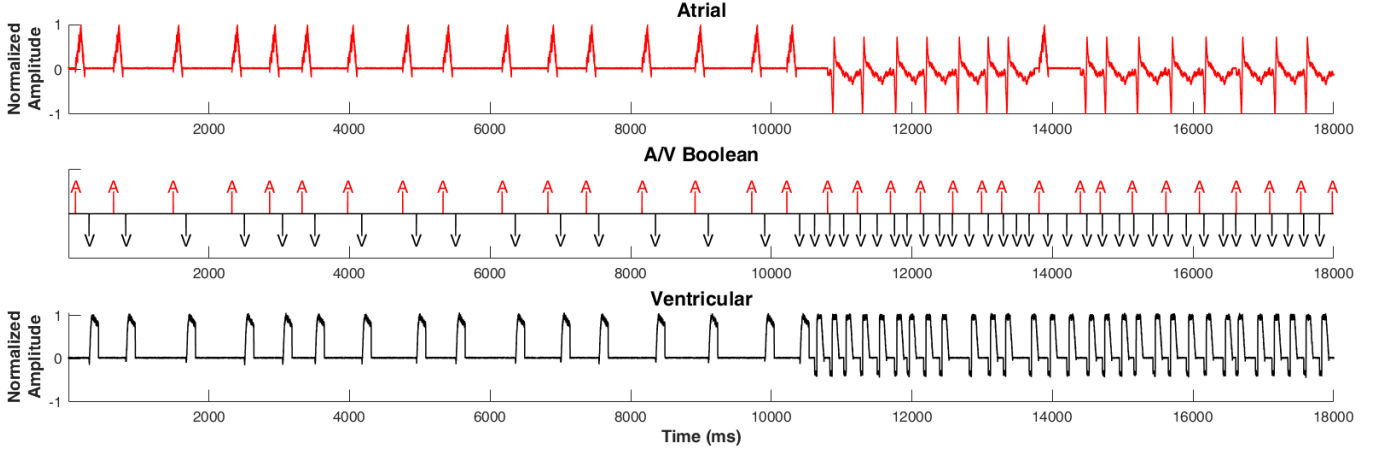


Fig. 11: EGM during a VF. Top panel shows the atrial EGM. Bottom panel shows the ventricular EGM. The middle panel shows the sensed boolean signal that is part of the input stream s to the AMA. Spikes above the x-axis indicate atrial beats, and spikes below it are the ventricular beats.

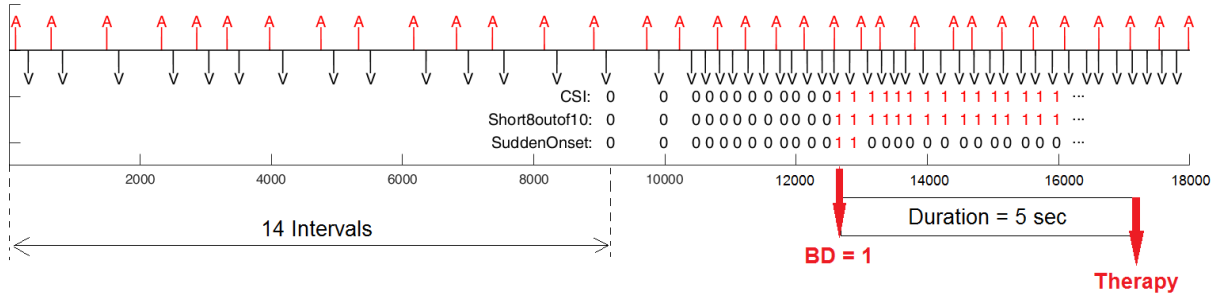


Fig. 12: Boolean beat stream from Fig. 11 and the streaming output of QRE stage2 (which calculates CSI, Short8outof10 and SuddenOnset).

in a Fig. 12. At times 12,572 ms and 12,811 ms the start of Duration is detected ($BD = 1$). At the end of the first initiated Duration (at 17,572 ms), the A/V Rate Comparison discriminator and Sliding 6/10 discriminator are satisfied and the AMA outputs Therapy. This is consistent with the decision tree in Fig 5.

Fig 14 shows an Atrial Fibrillation (AF) signal. The algorithm never outputs therapy. Before time 15,529 ms the rhythm is not determined to be fast (Three Consecutive Short Intervals and 8/10 Short Intervals are never satisfied together). The first time when the fast rhythm is detected is at 15,529ms. Therefore, the first $BD = 1$ flag happens at time 15,529 ms and Duration starts. At the end of this Duration (20,529 ms), A/V Rate Comparison is not satisfied. Moreover, the rhythm is determined to be unstable with gradual onset and AFib Rate condition is satisfied. Therefore, no therapy is delivered at this point. The same thing occurs for the next ventricular beat time point (15,867 ms), and no therapy is detected again.

B. Validation of the QRE Implementation

To validate the correctness of our QRE implementations, we created three versions of the AMA in Fig. 5. These three versions will also be used in the power analysis of Section VIII. The baseline version, presented in Section V, includes all

discriminators and has a Duration length of 5sec. The second version does not use the Sudden Onset discriminator. This discriminator is Off by default when the device ships. The third version reduces Duration length to 1sec. Accuracy is measured using the Specificity and Sensitivity of detection, defined respectively as

$$\text{Specificity} = \frac{\# \text{ correctly detected SVTs}}{\# \text{ true SVTs}} \times 100\%$$

$$\text{Sensitivity} = \frac{\# \text{ correctly detected VTs}}{\# \text{ true VTs}} \times 100\%$$

where the denominators are the number of true SVTs and VT, respectively.

The three versions were run on a database of 960 EGMs, equally divided into 480 SVTs and 480 VTs. The beat timing in the EGMs (in other words, the boolean stream s) was generated by the heart model of [36],[37]. Briefly, this model can simulate beat generation and propagation at different rates, from different locations in the heart. E.g., it can simulate a Normal Sinus Rhythm (NSR) which originates in the sinoatrial node and conducts down, or a fast ventricular rhythm that starts in the ventricles and conducts up to the atria. The model can also simulate different conduction pathways and conduction delays between locations. In this manner, it is

most ICD and ILR recipients are older patients with various health issues [27], so reducing the likelihood of a replacement by prolonging battery life is highly desirable [26].

It is generally true that the higher the abstraction level at which power consumption is estimated, then the easier it is to correlate algorithmic changes to power changes and the more questions can be answered analytically. However, the estimates are then less accurate in absolute terms. Conversely, at a lower abstraction level, the power model is more accurate, but is much harder to correlate to algorithmic changes, especially if it is tied to a particular target processor.

In this section, we provide a way to compute an *upper bound* on the energy consumed by a QRE per data item. The per-item consumption is the appropriate unit of measurement since a stream can be arbitrarily long. Being an upper bound, it allows the algorithm developers to compare design options very early on based on worst-case cost, and hardware engineers to provision battery capacity and electronics that are suitable for the expected worst-case energy draw. The upper bound is obtained by first measuring the per-item energy consumption of all the predicates and *ops* that appear in the QRE. These will be referred to as the *basic costs*. Then the QRE evaluator itself is used to combine these basic costs into the worst-case cost of the query. It is possible to do this for programs written in the StreamQRE language because of the well-understood syntactical restrictions it imposes, in particular, the restriction that computation results cannot be used in predicates. Note that these analyses apply trivially to any other additive cost, such as processing time, and not just power.

The upper-bound energy analysis described in the previous paragraph is meant to provide only a crude estimate of energy consumption for early design space exploration. It is not meant to replace a more fine-grained analysis (such as a WCET analysis) that takes the hardware and the input data into account. Such a high-precision analysis is useful for finetuning the performance of a production implementation, but a more rough analysis is still useful in the early design stage.

A. An upper bound based on the evaluator

We first need to understand roughly how the QRE evaluator works. The evaluator is the algorithm that evaluates a QRE on a given stream. For a query q , the evaluator first invokes a query-specific *start* routine to initialize the internal data structures appropriately. With every new data item that arrives, the evaluator invokes a query-specific *next* routine to process it. Moreover, *next* might have to pass the item to sub-queries: e.g., $\text{split}(f, g)$ will pass the item to g everytime the string seen so far matches f . In such a case, *next* will need to invoke the *start* method of g . Therefore, the cost of processing a data item is the cost of calling the QRE's *next* routine.

1) *From basic cost to QRE cost:* Let $\text{cost}(\varphi)$ and $\text{cost}(op)$ be the cost of evaluating the predicate φ and operation op respectively. It is assumed that these costs are data-independent, which is true for the queries that appear in AMA. Let $\text{start}(q)$ and $\text{next}(q)$ be functions that return the cost of executing *start* and *next* methods of query q . The per-item cost of a

QRE q can be upper-bounded using the following recursion on its structure.

```

q = atom( $\varphi$ , op) :
  start(q) = 0
  next(q) = cost( $\varphi$ ) + cost(op)

q = split(f, g, op) :
  start(q) = start(f) + start(g) + cost(op)
  next(q) = next(f) + next(g) + start(g) + cost(op)

q = iter(f, init, op, out) :
  start(q) = start(f) + cost(out)
  next(q) = next(f) + cost(op) + start(f) + cost(out)

q = iterLast(f) :
  start(q) = start(f)
  next(q) = next(f) + start(f)

q = iterUntil( $\varphi$ ,  $\psi$ , init, op) :
  start(q) = 0
  next(q) = cost( $\varphi$ ) + cost( $\psi$ ) + cost(op)

q = wnd(f, size, init, ins, rmv, out) :
  start(q) = start(f)
  next(q) = next(f) + cost(ins) + cost(rmv) +
    cost(out) + start(f)

q = annt(f, op1, op2) :
  start(q) = start(f)
  next(q) = next(f) + max(cost(op1), cost(op2))

q = f >> g :
  start(q) = start(f) + start(g) + next(g)
  next(q) = next(f) + next(g)

```

To understand this recursion, consider the case $q = \text{atom}(\varphi, op)$. Starting the evaluator doesn't cost anything in this case. When the data item arrives and it matches φ , then op is executed and we pay $\text{cost}(\varphi) + \text{cost}(op)$. Otherwise, we only pay $\text{cost}(\varphi)$. Thus an upper-bound on cost is $\text{cost}(\varphi) + \text{cost}(op)$, as indicated.

For a more involved example, consider the case $q = \text{split}(f, g, op)$. *start*-ing q involves *start*-ing f and g , and we pay the corresponding costs. If both of them match the empty string, then we also pay $\text{cost}(op)$. So worst-case cost of *start* is as shown. When a data item arrives, it is passed to both f and g : f might match the string in multiple positions, and it is not possible to know ahead of time which will be the right split point, so the string is always fed to f , and we pay $\text{next}(f)$. If the string seen so far matches f then the item is also passed to g to see if the string suffix will match it, and we pay $\text{start}(g)$. g might also be in the middle of matching a previous suffix (remember the evaluator maintains all possible matches). In that case, it will also process the new item using its *next* routine, and we pay $\text{next}(g)$. Finally, if both f and g match, then $op(\llbracket f \rrbracket w, \llbracket g \rrbracket w)$ is evaluated and we pay $\text{cost}(op)$. Thus in the worst-case, the cost of *next*(q) is $\text{next}(f) + \text{next}(g) + \text{start}(g) + \text{cost}(op)$, as shown.

TABLE II: jRAPL-reported values for basic costs (Obtained by averaging over 20M execution of the operation (= 1 experiment), and over 125 experiments after a 25-experiment warm up.

	Basic operation	
Measurements:	$x \rightarrow \text{True}$	$x \rightarrow x$
DRAM [J-e-5]	0.000003244	0.00004134
CPU [J-e-5]	0.0000045418	0.0001023086
Package [J-e-5]	0.00001155	0.0002180939
Total [J-e-5]	0.000019336	0.000361745

2) *Measuring the basic costs*: To start the above recursion, we need knowledge of $\text{cost}(\varphi)$ and $\text{cost}(op)$. For example, consider query `stage3` defined in Section VI-E and its associated costs:

`stage3 = wnd(atom(), N, 0, ins, rmv, discr)`

```

start(stage3) = start(atom()) = 0
next(stage3) = next(atom()) + cost(ins) + cost(rmv)
               + cost(discr) + start(atom())
               = cost(x → True) + cost(x → x)
               + cost(ins) + cost(rmv) + cost(discr)

```

Therefore, it is necessary to measure the following:

$$\begin{aligned}
 C_1 &= \text{cost}(x \rightarrow \text{True}) \\
 C_2 &= \text{cost}(x \rightarrow x) \\
 C_3 &= \text{cost}(\text{ins}) + \text{cost}(\text{rmv}) + \text{cost}(\text{discr})
 \end{aligned}$$

The costs of predicates and *ops* can be measured using jRAPL [38] for example. jRAPL provides a mean to measure the energy consumption of any snippet of Java code by enclosing it between `getEnergyStats` function calls. The `getEnergyStats` function accesses Machine-Specific Registers (MSRs) that store the energy consumed since a pre-defined datum. Thus we can measure the energy consumed by a given piece of code by comparing the register contents before and after invoking that code, e.g. as shown below:

```

EnergyCheckUtils ec = new
    EnergyCheckUtils();
double[] before = ec.getEnergyStats();
long duration =
    Queries.execute(streamlength, stream,
        myquery); //nano-sec
double[] after = ec.getEnergyStats();
double[] energy = after - before;
System.out.println("Consumed energy = "
    + energy);

```

Internally, jRAPL is a Java wrapper around the RAPL library. RAPL (Running Average Power Limit) is a suite of low-level interfaces to the MSRs with the ability to monitor and control energy and power consumption of different hardware levels, and is widely supported in Intel architectures. RAPL allows energy/power consumption to be reported separately from the CPU core, package (L3 cache, on-chip GPUs, and interconnects), and DRAM.

TABLE III: jRAPL-reported energy values for $C_3 = \text{cost}(\text{ins}) + \text{cost}(\text{rmv}) + \text{cost}(\text{discr})$, for three versions of AMA. Obtained as average of 100 experiments after a 25-experiment warm-up, each experiment having 1M runs.

Measurements:	Baseline	No Onset	Duration = 1s
DRAM [J-e-5]	0.55755	0.54573	0.182398
CPU [J-e-5]	0.549273	0.502224	0.23123
Package [J-e-5]	2.2693036	2.21987	0.726192
Total [J-e-5]	3.376137	3.267839	1.13983

For the example of `stage3`, Table II shows the energy values C_1 and C_2 reported by jRAPL. These operations are extremely cheap and their measurement can be non-deterministically affected by irrelevant processes running on the hardware (like page swaps), compiler optimizations (like discarding of unused outputs, which is why in the code listing above we print out `duration`). Therefore, and to account for this variability, we compute cost by running the same operation 20M times and averaging the energy over the runs. We call this an experiment. We run 125 such experiments in a row, and discard the first 25 experiments to take into account background noise caused by the warm up, and average the last 100 experiments. The final reported number is then the energy per predicate or *op*.

REMARK. As noted, measuring the cost of simple basic operations is affected by irrelevant sources of energy consumption. When the objective is to compare algorithms, it is reasonable to assume unit costs for the cheap basic operations, and proportionally larger cost to more complex operations, and compare the QREs on the basis of this cost model. The results, of course, are as good as our guess of the relative magnitudes of the various basic costs.

Table III shows the energy value C_3 , when running as part of the three versions of AMA described in section VII-B: the Baseline algorithm, version with no Sudden Onset discriminator, and version with a Duration of 1sec. The energy consumption of `discr` depends on which algorithm it is running in because, for example, a shorter Duration implies that `discr` is operating on fewer items, while no Onset means that the value of Sudden Onset is not used in the decision making of `discr`.

Equipped with these numbers we can upper-bound the per-item energy consumption of `stage3` by $C_1 + C_2 + C_3$. On this basis, the Duration=1sec version is the cheapest in the worst-case, and Baseline is the most expensive. On the other hand, No Onset has a per-item cost which is only slightly smaller than that of Baseline. This can be explained by the fact that Baseline only performs one extra AND relative to No Onset, which is a cheap operation (and even that is sometimes not executed, depending on the ordering of arguments). The fact that disabling Onset does not yield meaningful energy savings suggests that for patients that might benefit from Sudden Onset discrimination (like patients who have low frequency of SVTs), it can be enabled without any loss in device longevity.

B. Measured Energy Consumption of Entire Algorithm

In addition to the upper bounds, it is of course possible to measure the cost of a QRE on a typical workload, e.g., when

TABLE IV: Database-averaged jRAPL-reported energy for three version of entire algorithm. Obtained as average of 40 experiments after a warm-up of 10 experiments, each experiment having 1 run.

Measurements:	Algorithm		
	Baseline	No Onset	Duration = 1s
DRAM [J-e-5]	1.7177	1.5836	1.1813
CPU [J-e-5]	2.7648	2.0992	1.6067
Package [J-e-5]	6.7009	5.9251	4.4322
Total [J-e-5]	11.1834	9.6078	7.2203

processing the signals in the EGM database. The three versions of AMA and the signals database were described in Section VII. The energy is measured again using jRAPL. Because the AMA is a sufficiently costly operation and its energy measurements will not vary significantly between repeated runs, each experiment consists of a single run of the QRE on the database of signals. We still run and discard some initial experiments as warm-up.

Table IV reports the per-item energy consumption, averaged over the signals in the database. The energy numbers match expectations: the baseline version consumes the most energy. Version No Onset is second most expensive, because eliminating Sudden Onset reduces the costs of Stage 2 (which computes the Onset decision SO – see Fig. 10 and QRE stage2), and Stage 3 (which uses the SO value in an AND statement). Finally, Shortening Duration saves the most energy, since it implies shorter computations for 4 discriminators (Fig. 10).

IX. RELATED WORK

Medical device algorithms. Most of the literature on formal methods for medical device algorithms focuses on verifying and testing the functionality of the algorithm - see [39], [40], [41], [42] for examples in the specific context of implantable cardiac devices. These concerns are orthogonal to ours: the focus of this paper is the description of a *programming language* that is suitable for arrhythmia monitoring, and the *meta-functional* characteristics it automatically guarantees. It is worth noting that the U.S. Food and Drug Administration (FDA), which regulates medical devices in the U.S.A., does not mandate particular types of validation, such as model checking [43]. Rather, it describes in generic terms the kind of evidence that should be provided. For example, it stipulates that “Software quality assurance needs to focus on preventing the introduction of defects into the software development process”, and that “software developers should use a mixture of methods and techniques to prevent software errors and to detect software errors that do occur.” [43, Section 4.2].

The FDA Guidance does not explicitly address meta-functional properties. Works in quantitative verification, such as [44] and [45], model the heart and pacemaker to verify statistically or through simulations whether some quantitative properties are satisfied. This contrasts with our approach which is model-free, and provides cost upper bounds based on the QRE code itself, not a model of it. An application of QREs to arrhythmia monitoring appeared in [25] where a peak detector is coded in an early variant of the language.

QREs are a Domain-Specific Language (DSL): they are meant for programming queries on arbitrary data streams, with strong theoretical foundations [5] and a flexible programming environment [6], [18]. DSLs have been developed for medical device development, albeit these are usually meant for the creation of the entire device, including hardware, and focus on capturing object-oriented aspects of the domain (i.e., identifying the main objects in the domain and modeling them and their relations). E.g., [46] develops a graphical language for modeling blood separator machines, along with code generators and lock-step simulators of the model and its generated code. No work has appeared in the literature on a DSL for ICDs or ILR algorithms, and more generally, rhythm monitoring algorithms.

Streaming languages. There is a large body of work on streaming database languages and systems such as Aurora [47], Borealis [48], STREAM [49], and StreamInsight [50], [51]. The query language supported by these systems (for example, CQL [52]) is typically a version of SQL with additional constructs for splitting the stream into finite windows (e.g., tumbling or sliding windows, count-based or time-based). This allows for rich relational queries, including set-aggregations (e.g. sum, maximum, minimum, average, count) and joins over multiple data streams. Such SQL-based languages are, however, limited in their ability to express properties and computations that rely on the sequence of the events such as: sequence-based pattern-matching, and numerical computation based on list-iteration when the order of the data items is significant. There are streaming engines such as IBM’s Stream Processing Language (SPL) [53], [54], ReactiveX [55], Esper [56] and Flink [57], which support user-defined types and operations, and allow for both relational and stateful sequential computation. However, none of these engines provides support for decomposing the stream in a regular fashion and performing incremental computations that reflect the structure of the parse tree, which is a central feature of the QRE language. LOLA [58] allows arbitrary computations on streams and incremental computation of statistics, but does not support regular decomposition of the stream to define the computation domains. Finally, Timed Regular Expressions [59] allow the specification of time windows during which the timed string must match a regular expression. As such they are a specification language rather than a programming language and do not support the rich computations and quantitative combinators that QREs support.

Power estimation. Since QREs are aimed at high-level programming and the cost analysis is aimed at early design exploration, we don’t review the vast literature on low-level power estimation techniques (anything below C program level), nor do we review analyses that focus on the impact of particular hardware choices like [60]. Such analyses occur later in the design cycle and require the availability of low-level artifacts like circuits. The interested reader can consult [61] for a recent review of such techniques.

In [62],[63] and [61], a *functional level power model* is used for estimating the power consumption of a C program without compiling it. It requires partitioning the target processor into functional units, and estimating some key parameters like the

cache miss rate, external data memory access rate and the processing rate. It also depends on the user providing low-level execution details like the data mapping. This target-specific code-level analysis complements our presented bounds, which occur earlier in the design cycle and are at the algorithm level.

The approach in [64] estimates battery dissipation. It treats the processor as a black box and instead decomposes *the program* into types of basic instructions, similar to what we did to obtain the upper bounds in Section VIII. However, the basic instructions in [64] are at the instruction-set level, like integer and floating point loads and stores. And while we exploit the fact that we have a uniform evaluation algorithm for any QRE to infer bounds on the entire program's cost, the authors in [64] must establish empirically, for a given processor and program, that the program's cost is the weighted sum of the dissipations for basic instructions.

A static analysis of energy consumption of XC programs is presented in [65].⁴ After building an ISA-level power model using hardware measurements of a test suite, the XC program is translated to Horn clauses in the Ciao programming language [66]. The Ciao pre-processor can then bound the power consumption as a function of input data sizes. This technique was later extended to use a power model at the level of the compiler's intermediate representation rather than the ISA level [67]. This approach applies to programs that can be translated into a logic program. Another static analysis technique [68] uses integer linear programming to compute the worst case energy consumption, given estimates of dynamic and leakage power contributions of basic blocks in a program's control flow graph. This is inspired by well-known Worst-Case Execution Time estimation techniques.

X. CONCLUSION

This paper has argued that arrhythmia monitoring algorithms are best viewed as streaming algorithms, and that they are best programmed in the StreamQRE language. Unlike traditional streaming applications where throughput is a prime concern, here energy consumption is the primary design factor. A program written in StreamQRE automatically gets a baseline implementation with a constant memory, processing time and energy consumption per item. Moreover, the QRE evaluator automatically provides upper bounds on the per-item cost of the query, which can be used early in the design cycle to guide the choice of algorithm, and to decide whether some discriminators are worth having at all. We showed how the StreamQRE Java Library can be used to program and evaluate a query and to obtain cost upper bounds, and how these bounds correlate to actual power measurements. We believe this approach to exploring and programming arrhythmia monitors, and other medical device algorithms, has the potential to greatly alleviate the device development burden. In particular, it opens the possibility of designing ILR algorithms that collect statistics over longer time durations than is currently done. Other applications that might benefit from StreamQRE include glucose monitoring [69], [70], where a mobile device periodically or continuously measures a diabetic's blood glucose and performs

various filtering operations to predict hypo- or hyperglycemic episodes.

The theoretical basis of StreamQRE raises the possibility of performing static (formal) analysis of its performance. It is already possible, for queries written in a subset of the language, to answer questions such as "Does the worst-case peak power consumed by the algorithm exceed some threshold?", "Could the long-term average power consumed by the algorithm exceed some threshold?", and "Does algorithm A consume less peak/average power than algorithm B?". Answers to these questions impact the choice of electronics that must withstand the peak power draw, and the capacity of the device battery.

On the tools side, two projects are worth exploring: first, implementing the decision procedures that perform the above-described static analysis. Second, creating a compiler that compiles a QRE into C or assembly code targeting a given hardware platform. This would complete the path from algorithm to code to implementation, and would allow a reliable comparison of upper-bounds to actual energy consumption of the compiled code. In niche areas, expert coders might be able to squeeze more performance per Watt from hand-written code than a compiler could from automatically generated code. However, it is to be expected in the long run that medical devices will follow the arc of semiconductors, where automation has gradually out-performed humans, or has yielded such productivity gains that small performance losses are more than made up for by the reduced time-to-market, reproducibility and scalability of the design process, and automatic guarantees of correctness and performance.

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⁴XC is a high-level C-based programming language.

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