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## **EXPERIMENTAL AND MODELING STUDY OF PARTICULATE MATTER OXIDATION UNDER LOADING CONDITIONS FOR A SCR CATALYST ON A DIESEL PARTICULATE FILTER**

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EXPERIMENTAL AND MODELING STUDY OF PARTICULATE MATTER  
OXIDATION UNDER LOADING CONDITIONS FOR A SCR CATALYST ON A  
DIESEL PARTICULATE FILTER

By

Abhishek Jadav

A THESIS

Submitted in partial fulfillment of the requirements for the degree of

MASTER OF SCIENCE

In Mechanical Engineering

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2018

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This thesis has been approved in partial fulfillment of the requirements for the Degree of MASTER OF SCIENCE in Mechanical Engineering.

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## List of Abbreviations, Notations and Symbols

A	Pre-Exponential Factor
ANR	Ammonia to NO <sub>x</sub> Ratio
API	American Petroleum Institute
CLD	Chemiluminescence Detector
CO	Carbon Monoxide
CO <sub>2</sub>	Carbon Dioxide
CPF	Catalyzed Particulate Filter
DDOC	Downstream of the DOC
DEF	Diesel Exhaust Fluid
delP	Pressure Drop across SCRF®
DOC	Diesel Oxidation Catalyst
DPF	Diesel Particulate Filter
DSCRF®	Downstream of the SCRF®
E <sub>a</sub>	Activation Energy
ECM	Engine Control Module
EPA	Environmental Protection Agency
FID	Flame Ionization Detector
FS	Full Scale
HC	Hydrocarbons
H/C	Hydrogen to Carbon Ratio
HD	Heavy Duty
HHV	Higher Heating Value
H <sub>2</sub> O	Water
IRD	Infrared Detector
IRS-MS	Infrared Spectrometry Mass Spectrometer
k	Oxidation Factor
k <sub>avg</sub>	Average Oxidation Factor
k <sub>mod</sub>	Modified Rate Constant

$k_{std}$	Standard Rate Constant
LHV	Lower Heating Value
MST	Manual Sampling Train
MTU	Michigan Technological University
$N_2$	Nitrogen
$NH_3$	Ammonia
NO	Nitrogen Oxide
$NO_2$	Nitrogen Dioxide
$NO_x$	Oxides of Nitrogen (Mainly NO and $NO_2$ )
$O_2$	Oxygen
OBD	On-Board Diagnostics
PM	Particulate Matter
PO	Passive Oxidation
$Q_{std}$	Standard Volumetric Flowrate
$RR_o/RR$	Reaction Rate
$R_u$	Universal Gas Constant
RU	Ramp Up
S1	Stage 1
S2	Stage 2
S3	Stage 3
S4	Stage 4
SCR	Selective Catalytic Reduction
SCR <sup>®</sup>	SCR catalyst coated on a DPF developed by Johnson Matthey
SCR-F	Model for a SCR on a DPF
SOF	Soluble Organic Fraction
SOL	Solid Fraction
SP	Specific
T	Temperature
UDOC	Upstream of the DOC

USCRF <sup>®</sup>	Upstream of the SCRF <sup>®</sup>
Y	Mass Fraction
W	Molecular Weight
w/o	Without
w/	With

## Abstract

The heavy-duty diesel engines use a Diesel Oxidation Catalyst (DOC), a Catalyzed Particulate Filter (CPF), a Selective Catalytic Reduction (SCR) with urea injection and a Ammonia Oxidation Catalyst (AMOX), to meet the US EPA 2010/2013 particulate matter (PM) and NO<sub>x</sub> emission standards. However, it is not possible to achieve the 2015 California low NO<sub>x</sub> standards with this arrangement. Hence, there is a need to improve the existing aftertreatment system. This can be achieved by coating the SCR catalyst on a diesel particulate filter (DPF), thus combining the PM filtration and NO<sub>x</sub> reduction functionality into a single device. This reduces the overall volume/weight of the system and provides opportunity for packaging flexibility and improved thermal management along with the possibility of higher NO<sub>x</sub> reduction with a downstream SCR system.

The SCR catalyst on a DPF used in this study is known as a SCRF<sup>®</sup> which was supplied by Johnson Matthey and Corning. Previous research on the CPF and SCRF<sup>®</sup> at MTU highlighted that the reactivity of PM retained in the CPF and SCRF<sup>®</sup> is higher during loading conditions compared to passive oxidation conditions i.e. when the flow rate of PM entering the CPF or SCRF<sup>®</sup> is higher in loading conditions compared to the low flow rate and higher PM reaction rate during passive oxidation conditions. A 2013 Cummins ISB engine with a DOC-SCRF<sup>®</sup> arrangement was used to perform twelve tests (eight tests without urea injection and four tests with urea injection) in order to determine the NO<sub>2</sub> assisted passive oxidation performance of the SCRF<sup>®</sup> under loading conditions with and without urea injection. The primary focus of this study was to carry out Loading Tests with and without Urea injection and measure species concentrations, PM mass retained, exhaust flowrates, substrate temperature distributions, pressure drop across the filter, and to determine the kinetics of NO<sub>2</sub> assisted PM oxidation under loading conditions and compare it with kinetics under passive oxidation conditions.

The NO<sub>2</sub> assisted passive oxidation performance of the SCRF<sup>®</sup> was experimentally studied by running the engine at 2400 RPM and four different loads at nominal and reduced rail pressure for 5.5 hours in two stages of loading. These conditions were intended to span the SCRF<sup>®</sup> inlet temperatures in the range of 264-364°C and inlet NO<sub>2</sub> concentrations in the range of 52-120 ppm. Four conditions out of these eight conditions were repeated with the injection of urea in the form of diesel exhaust fluid at a target ammonia to NO<sub>x</sub> ratio of 1.0 to investigate both the NO<sub>x</sub>

reduction performance, as well as the effect of urea on the NO<sub>2</sub> assisted passive oxidation performance.

From the conclusions of the study based on the experimental data, it was found that the cumulative percentage of PM oxidized in the SCRF<sup>®</sup> increases with the increase in engine load due to higher SCRF<sup>®</sup> temperatures and NO<sub>2</sub> concentrations. On average, the reactions rates with urea injection during loading conditions in the SCRF<sup>®</sup> are 25% lower compared to the reaction rates without urea injection. The reactivity of PM under loading conditions with and without urea injection is higher compared to the reactivity of PM under passive oxidation with and without urea injection. For a lumped PM oxidation model, a higher pre-exponential for NO<sub>2</sub> assisted oxidation is needed for loading as compared to passive oxidation conditions. It was not possible to determine the kinetics of NO<sub>2</sub> assisted oxidation of PM under loading conditions from the experimental data using a standard Arrhenius model which lead to the development of a different model for PM oxidation.

A PM oxidation model was developed based on the shrinking core model which keeps the identity of the incoming PM masses in the SCRF<sup>®</sup> as compared to SCR-F model being developed at MTU which is lumped model for PM oxidation. The PM oxidation model was calibrated to simulate PM oxidation in the SCRF<sup>®</sup> with a single set of kinetics under wide range of conditions including loading and passive oxidation conditions. The reaction rate results from the PM oxidation model were then applied to the SCR-F model to simulate the pressure drop across SCRF<sup>®</sup> and the PM retained in the SCRF<sup>®</sup> for the loading conditions used in this study. The SCR-F model was calibrated using experimental data from Loading Tests w/o Urea to simulate the PM retained within  $\pm 2$  g and pressure drop across SCRF<sup>®</sup> within  $\pm 0.5$  kPa of the experimental data at the end of the test. The calibrated SCR-F model was also used to estimate the cake, wall and channel pressure drop and the PM retained in the cake and wall for the Loading Tests w/o Urea to check the integrity of experimental data and the consistency of the model.

The NO<sub>2</sub> assisted kinetics for PM oxidation in the SCRF<sup>®</sup> without urea injection using the SCR-F model resulted in an activation energy of 96 kJ/gmol and pre-exponential factor of 2.6 m/K-s for the cake and 1.8 m/K-s for the wall. An analysis of the results from the SCR-F model suggests that for all the conditions, 84-92% of the total PM retained was in the PM cake layer and the oxidation in the PM cake layer accounted for 72-84% of the total PM mass oxidized during loading.

## Chapter 1. Introduction

Diesel engine emissions are being regulated by various organizations around the world. The Environmental Protection Agency (EPA) in the U.S. sets standards for engine tail pipe emissions which are becoming more stringent for heavy duty diesel engines every few years as seen in Table 1.1. Figure 1.1 shows emission standards for light duty vehicles on the FTP-75 cycle. As a result, engine manufacturers are continuously coming up with solutions and developing new technologies to meet the emission standards by controlling the oxides of nitrogen (NO, NO<sub>2</sub> and N<sub>2</sub>O) and particulate matter (PM) which are the major emissions of concern from diesel engines.

Table 1.1: US EPA Emission Standards for Heavy Duty Diesel Engines [1]

Emission Gases	EPA Standard – Implementation Year			
	2004	2007-09	2010	2015
	g/bhp-hr			
<b>NO<sub>x</sub></b>	2.00*	1.2	0.2	0.02 <sup>#</sup>
<b>NMHC</b>	0.5*	0.14	0.14	0.14
<b>CO</b>	15.5	15.5	15.5	15.5
<b>PM</b>	0.1	0.01	0.01	0.01

\*Alternative standard: NMHC+NO<sub>x</sub> = 2.5 g/bhp-hr

<sup>#</sup>Manufacturers may choose California Optional Low NO<sub>x</sub> Standard

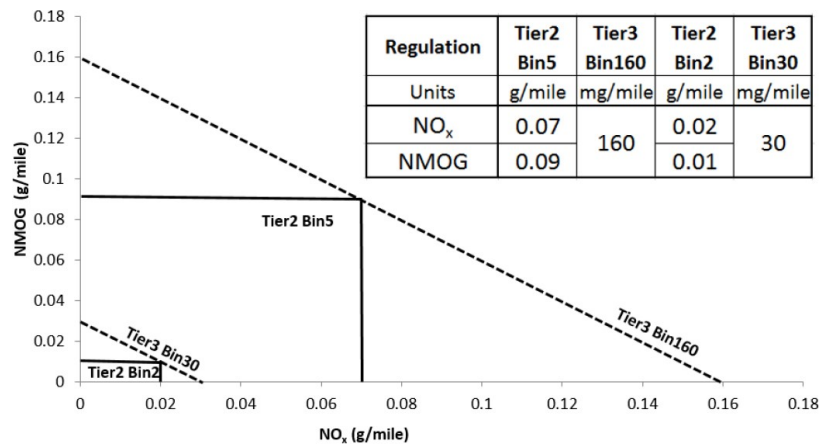


Figure 1.1: EPA Emission Standards for Light Duty Vehicles [2]

Many technologies are being implemented on diesel engine to control emissions which include exhaust gas recirculation (EGR), advanced fuel injection strategies etc. Particularly for heavy duty

diesel engines, a typical aftertreatment system consisting of a Diesel Oxidation Catalyst (DOC), a Catalyzed Particulate Filter (CPF), a Selective Catalytic Reduction (SCR) with urea injection assembly and an Ammonia Oxidation Catalyst (AMOX) is currently being used by manufacturers to meet the EPA standards for year 2010/2013 shown in Table 1.1 [3].

### 1.1 Diesel Engine Aftertreatment System Research

A typical aftertreatment system for a heavy duty diesel engine is shown in Figure 1.2. The engine exhaust flows through the DOC, CPF, decomposition tube and the SCR system. SCR-B catalyst shown in Figure 1.2 is a substrate with SCR catalyst coated in the front and AMOX catalyst at the back of the substrate.

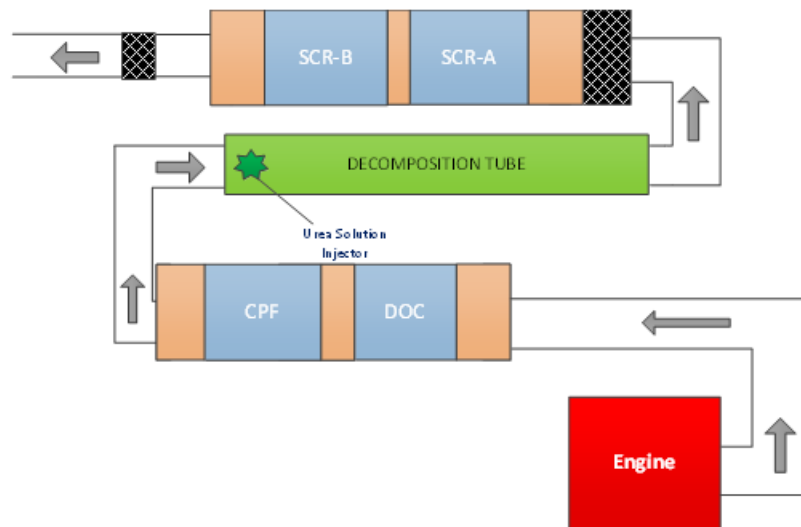


Figure 1.2: Schematic of the Cummins ISB 2013 Production Aftertreatment System [4]

The DOC is a flow through catalyst that oxidizes the nitrogen oxide (NO), carbon monoxide (CO) and hydrocarbon (HC) in the exhaust stream to nitrogen dioxide (NO<sub>2</sub>), carbon dioxide (CO<sub>2</sub>) and water (H<sub>2</sub>O). The DOC is placed upstream of the filter to increase the proportion of NO<sub>2</sub> by oxidizing the NO in the exhaust as the proportion of NO<sub>2</sub> in the diesel exhaust is relatively low (5-15% of total NO<sub>x</sub>) [5]. This promotes the NO<sub>2</sub> assisted oxidation of PM in the CPF. The NO to NO<sub>2</sub> conversion in the DOC is a function of exhaust space velocity, DOC inlet temperature, inlet NO concentration and is maximum for DOC inlet temperatures in the range of 300-350°C after which

it starts decreasing [6]. The DOC is also used to oxidize the hydrocarbons in the diesel fuel dosed late into the combustion cycle during active regeneration. The HC conversion increases with the increase in DOC inlet temperature [6].

The CPF is a wall flow device which filters the PM in the exhaust and oxidizes the PM retained in the wall and the cake layer by NO<sub>2</sub> assisted oxidation and thermal oxidation with O<sub>2</sub>. Both the mechanisms occur simultaneously although one may be the dominant mechanism at certain conditions. The NO<sub>2</sub> assisted oxidation is dominant in the temperature range 250-400°C [5] whereas the thermal oxidation is dominant in temperatures above 400°C [7].

The SCR is a flow through device with a honeycomb structure. Catalysts such as oxides of copper (Cu), iron (Fe) or vanadium (V) are coated on the channels of the substrate. The SCR is used to reduce the NO<sub>x</sub> in the exhaust to nitrogen (N<sub>2</sub>) and water (H<sub>2</sub>O). This is done by injecting a urea solution (32.5% conc. by weight) also known as Diesel Exhaust Fluid (DEF) into the exhaust stream. The urea decomposes into ammonia (NH<sub>3</sub>), carbon dioxide (CO<sub>2</sub>) and water (H<sub>2</sub>O). The ammonia produced by decomposition of urea is adsorbed and stored on the surface of the catalyst which reacts with NO and NO<sub>2</sub> and reduces the NO<sub>x</sub>.

The AMOX is placed downstream of the SCR substrate and oxidizes the ammonia that slips out of the SCR to nitrogen (N<sub>2</sub>) and water (H<sub>2</sub>O). The ammonia slip out of SCR occurs due to over injection of urea solution or low exhaust temperatures where the NH<sub>3</sub> doesn't react with the NO and NO<sub>2</sub>.

Although these systems are effective in achieving the 2010/2013 EPA standards, it is not possible to achieve the 2015 California low NO<sub>x</sub> standards with this arrangement. Hence, there is a need to improve the existing aftertreatment system by increasing the SCR catalyst volume. But this will increase the cost of the system due to the precious metal involved and also increase the weight and volume of the overall system which might cause packaging issues as well.

To solve this, the SCR catalyst can be combined with a diesel particulate filter (DPF) into a single device which is known as SCR catalyst on a DPF or SCR-on-DPF or SDPF. The SCR catalyst is coated on the DPF substrate wall thus combining both the NO<sub>x</sub> reduction and PM oxidation functionality into a single device which reduces the overall volume and weight of the system and provides the opportunity for packaging flexibility and improved thermal management [3]. The SCR catalyst on



a DPF used in this study is known as SCRF<sup>®</sup> and was supplied by Johnson Matthey and Corning. The SCRF<sup>®</sup> is a wall flow device with a Cu-zeolite based SCR catalyst coated on the substrate walls. The engine and aftertreatment research done at MTU is a part of the Consortium effort with Cummins and Isuzu as partners. Figure 1.3 shows the overall experimental program with different phases of testing. A Cummins ISB 2013 6.7 L engine was used for the experimental testing in order to collect data and characterize the performance of the CPF, SCR and SCRF<sup>®</sup>. The production or the baseline system at MTU consists of a DOC, CPF decomposition tube and SCR system as shown in Figure 1.2. In Configuration 1, the CPF is replaced with a spacer and the SCR system is replaced with the SCRF<sup>®</sup> as shown in Figure 1.4. In Configuration 2, the SCR is replaced with the SCRF<sup>®</sup> and the CPF is used in this system to remove the PM in order to determine the SCR kinetics of the SCRF<sup>®</sup>. In Configuration 3, the CPF is replaced with the SCRF<sup>®</sup> and the SCR is placed downstream of the SCRF<sup>®</sup>. Details about these three SCRF<sup>®</sup> Configurations and the experimental work performed on all the three Configurations at MTU is given in references [8,9,10].

Based on the previous research at MTU on the production system and Configuration 1, it was observed that the reactivity of PM retained in the CPF and SCRF<sup>®</sup> is higher during loading conditions compared to passive oxidation conditions i.e. when the flow rate of PM entering the CPF or SCRF<sup>®</sup> is higher in loading conditions compared to the low flow rate and higher PM reaction rate during passive oxidation conditions [4, 8]. Hence, to further understand and characterize the difference in reactivity of PM during loading conditions and passive oxidation conditions, loading tests at different engine conditions at different temperatures and PM and NO<sub>2</sub> concentrations were carried out with and without urea injection.

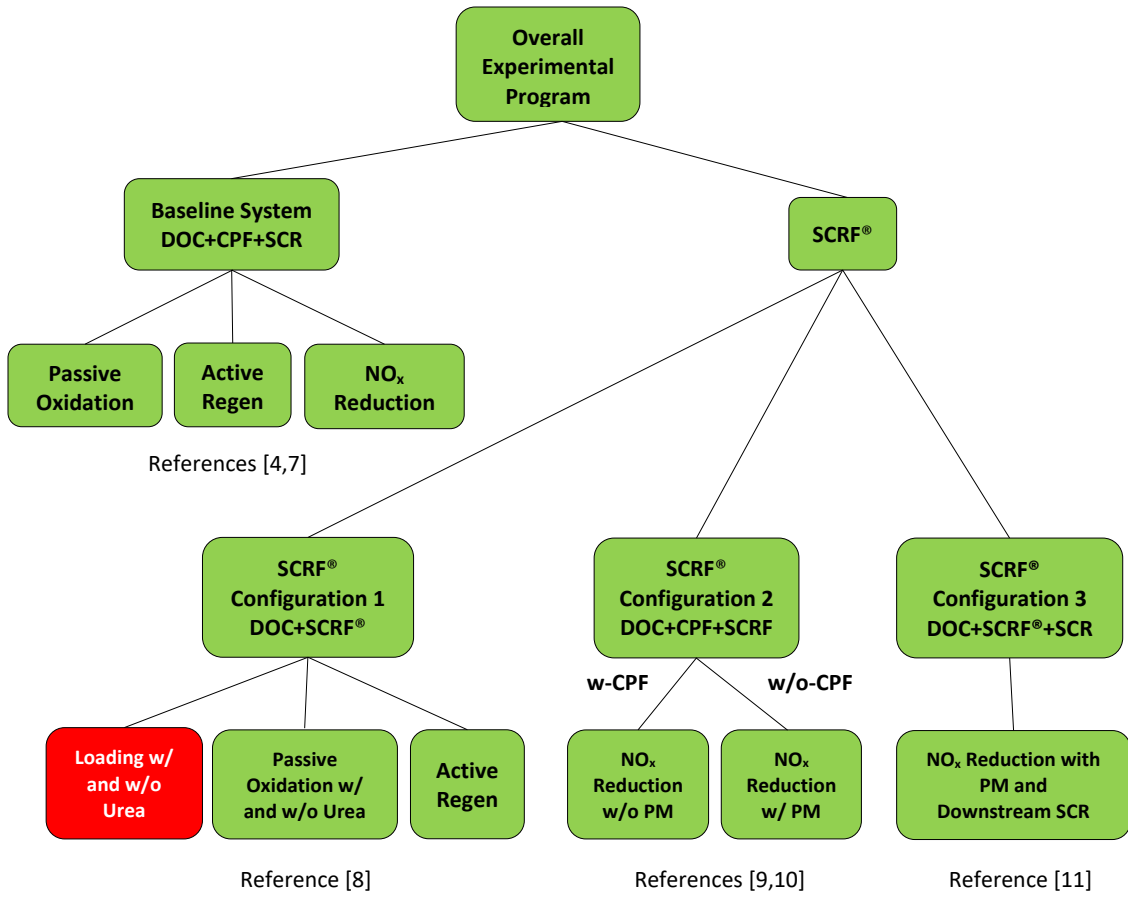


Figure 1.3: Overall Experimental Program

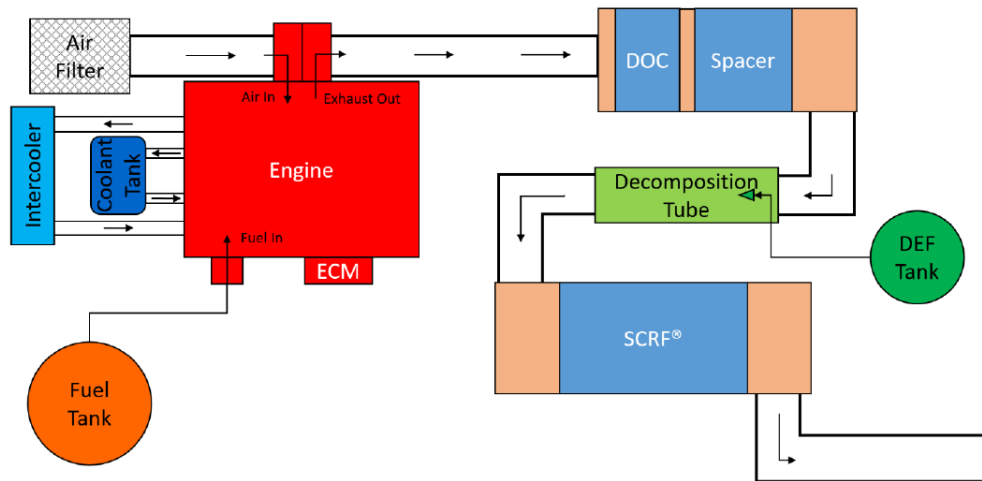


Figure 1.4: SCR Configuration 1 [8]

## 1.2 MTU SCR-F Model

The SCR-F model is being developed at MTU [12] to simulate the performance of the SCR-F<sup>®</sup> under different engine conditions. The model is capable of simulating the PM loading and oxidation via NO<sub>2</sub> assisted and thermal oxidation mechanisms, and the filtration of the PM in the cake and the substrate wall. It can simulate the total pressure drop across the SCR-F<sup>®</sup> and estimate the individual contribution of the PM cake, wall and the channel to the total pressure drop. It has the ability to simulate the reaction of chemical species - NO, NO<sub>2</sub>, CO, CO<sub>2</sub>, O<sub>2</sub> and HC across the SCR-F<sup>®</sup>. The model is also capable of predicting the temperature and PM distribution in both the radial and axial direction in the SCR-F<sup>®</sup>. The development of the model will be briefly discussed in Section 2.5.

The model has been calibrated using experimental data from the Configuration 1 passive oxidation without urea and active regeneration tests [8], and Configuration 2 without PM [9]. Currently, it is being calibrated using experimental data for passive oxidation with urea in Configuration 1 [8] and experimental data for NO<sub>x</sub> reduction with PM in Configuration 2 [9]. The procedure for the calibration and the results are being developed. The SCR-F model has been used to simulate the PM retained in the SCR-F<sup>®</sup>, the total pressure drop across SCR-F<sup>®</sup> and the temperature distribution in SCR-F<sup>®</sup> for the tests performed in this study. Also, the model values have been compared to the experimental data to help in determining the integrity of the experimental data as the model is expected to be consistent.

## 1.3 Goals and Objectives

The primary focus of this study is to experimentally determine the PM oxidation performance of the SCR-F<sup>®</sup> under loading conditions with and without urea injection and to characterize the differences in the PM oxidation kinetics for loading and passive oxidation conditions with and without urea injection. The data from this study will be used to develop and calibrate a PM oxidation model. The results of this model will be applied to the SCR-F model to simulate the oxidation characteristics of PM under loading conditions.

## Objectives:

- Conduct experimental studies in order to determine the oxidation characteristics of the PM in the SCRF<sup>®</sup> during loading with and without urea injection for various engine conditions with different temperature and NO<sub>2</sub> concentrations.
- Study the effects of different space velocities, inlet temperatures, NO<sub>2</sub> concentration and fuel rail pressure on the SCRF<sup>®</sup> pressure drop and the PM mass retained under loading conditions with and without urea injection.
- Determine the kinetics of NO<sub>2</sub> assisted PM oxidation in the SCRF<sup>®</sup> under loading conditions with and without urea injection. Characterize the difference in the PM oxidation kinetics for loading and passive oxidation conditions with and without urea injection.
- Study the effect of urea on PM oxidation in the SCRF<sup>®</sup> under loading conditions.
- Develop a model based on the microstructure of PM particles that keeps track of incoming PM mass samples into the SCRF<sup>®</sup> to simulate the PM retained in the SCRF<sup>®</sup> for a single set of kinetics for PM oxidation under loading and passive oxidation conditions.
- Calibrate the SCR-F model using experimental data as input to simulate the PM retained in the SCRF<sup>®</sup> and pressure drop across the SCRF<sup>®</sup> under loading conditions with and without urea. Validate the performance of the model by comparing the simulation results and the experimental data.

## 1.4 Overview of Thesis

As discussed in Section 1.2, the focus of this thesis is on the PM oxidation performance of the SCRF<sup>®</sup> under loading conditions with and without urea injection. This chapter presented a brief introduction on the diesel engine aftertreatment system research followed by the goals and objectives of this study.

Chapter 2 discusses the published literature related to the oxidation of PM in a SCR catalyst on a DPF with and without urea injection. There is also a discussion on the comparison of NO<sub>2</sub> assisted PM oxidation kinetics from various experimental and modeling studies along with different

models used for PM oxidation in the literature. It also provides a background and motivation for the research conducted.

Chapter 3 discusses the experimental setup and procedures used for collecting data. There is a brief introduction on the test cell setup and different instruments used followed by discussion on the test procedure and test matrix for the experiments.

Chapter 4 focuses on the development of the PM oxidation model and calibration process. It discusses the integration of the PM oxidation model into the SCR-F model followed by the process used for calibrating the SCR-F model with experimental data from the tests conducted. There is brief discussion on the process followed for calibrating the PM oxidation model using experimental data from the passive oxidation tests in reference [8].

Chapter 5 presents the data and results from the experimental tests conducted followed by the comparison of results for loading and passive oxidation conditions with and without urea injection. The performance of the calibrated SCR-F model and the PM oxidation model is discussed by comparing the simulated data with the experimental data.

Chapter 6 summarizes the results from the experimental and modeling studies and draws conclusions of the research.

This is followed by Appendices A through G which provide additional data and information that supports the various chapters.

## Chapter 2. Literature Review

The focus of this chapter is to discuss published literature related to the objectives of this study and providing a background for the research conducted. The first section discusses the mechanisms of PM oxidation in a SCR catalyst on a DPF followed by a review of the literature to understand the effect of SCR reactions on the PM oxidation in the filter. The next section provides a brief description on the kinetics of PM oxidation followed by a discussion of the different models for PM oxidation to determine the kinetics of PM oxidation. This is followed by a section pertaining to loading studies of CPFs and SCR catalysts on DPFs. The last section discusses the development of the SCR-F model.

### 2.1 Oxidation of PM With and Without Urea Injection

The SCR catalyst on a DPF has dual functionality of filtering the PM as well as reducing the  $\text{NO}_x$  in the diesel exhaust. As the PM gets loaded in the filter, the pressure drop across the filter increases which increases the backpressure on the engine. This deteriorates engine performance and increases fuel consumption and PM, CO and HC emissions [1]. To solve this problem, the PM in the filter has to be periodically oxidized by a process commonly known as ‘active regeneration’. There are two gases in the diesel exhaust –  $\text{O}_2$  and  $\text{NO}_2$  which play an important role in the oxidation of PM. There are two mechanisms for PM oxidation, the  $\text{NO}_2$  assisted and the thermal oxidation which is  $\text{O}_2$  assisted. Both the mechanisms occur simultaneously although one may be the dominant mechanism at certain temperature conditions. The  $\text{NO}_2$  assisted oxidation is dominant in the temperature range 250-400°C [5] whereas the thermal oxidation is dominant in temperatures above 400°C [7]. The temperatures in all the experimental tests performed in this study are below 400°C and therefore it is assumed that  $\text{NO}_2$  assisted oxidation is the dominant mechanism for PM oxidation. The literature pertaining to  $\text{NO}_2$  assisted oxidation is discussed further in this Chapter. The literature pertaining to thermal oxidation can be found in references [4,8].

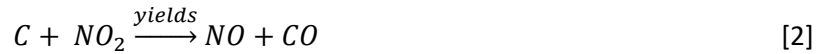
#### **$\text{NO}_2$ Assisted Oxidation**

In this mechanism, the PM retained in the filter is oxidized as a result of the reaction of  $\text{NO}_2$  with the PM. In a typical diesel aftertreatment system, an oxidation catalyst (DOC) is placed upstream of the filter to increase the proportion of  $\text{NO}_2$  by oxidizing the NO in the exhaust as the proportion

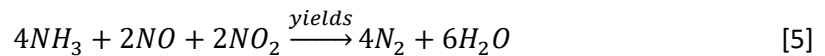
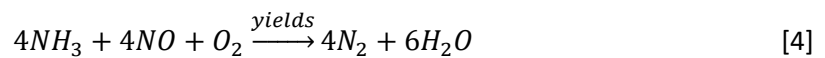
of NO<sub>2</sub> in the diesel exhaust is relatively low (5-15% of total NO<sub>x</sub>) [5]. This promotes the oxidation of PM in the filter by increasing the amount of NO<sub>2</sub> into the filter. Equation 1 describes the oxidation of NO to NO<sub>2</sub> in the DOC. As discussed earlier, the NO to NO<sub>2</sub> conversion efficiency of the DOC depends on factors such as space velocity, inlet temperatures and NO concentrations [6]. The DOC conversion efficiency peaks at temperatures in the range of 300-350°C [6].



Equations 2 and 3 describes the NO<sub>2</sub> assisted oxidation of PM in the filter. The increased proportion of NO<sub>2</sub> in the exhaust due to NO to NO<sub>2</sub> conversion in the DOC increases the PM oxidation rate [5].



As explained earlier, the SCR catalyst on a DPF can reduce NO<sub>x</sub> in the exhaust with the ammonia SCR reactions. Equations 4 and 5 describes the standard and fast SCR reactions respectively which are two important reactions [13].



In the SCR catalyst on a DPF, there is a competition between the SCR and PM oxidation reactions for consumption of NO<sub>2</sub>. This is schematically shown in Figure 2.1. A summary of published research about the effect of SCR reactions on PM oxidation is described in the following paragraphs.

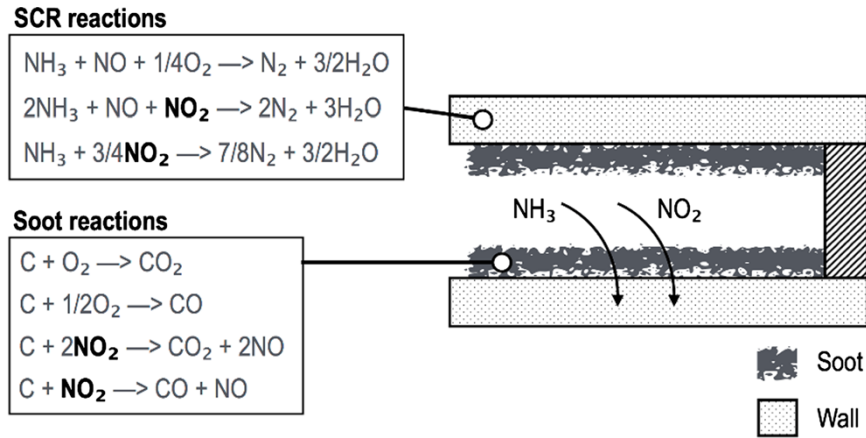


Figure 2.1: Competition Between PM Oxidation and SCR Reactions [14]

Czerwinski et al. [15] studied the passive oxidation performance of a SCR catalyst on a DPF with and without urea injection. The filter was loaded to 3 g/L (around 20 g for 5 repeated tests) with urea dosing of 36 g/h using a HD 3.0 L Iveco engine. The soot loading in the filter decreased by 81% without urea compared to 41% decrease with urea injection at ANR 1.0. This is because urea dosing hinders  $\text{NO}_2$  assisted oxidation [15].

Naseri et al. [16] studied the passive regeneration capability of a Cu-zeolite SCR catalyst on a DPF with and without urea injection after the loading it up to 3 g/L. A 2007 MY heavy-duty diesel engine was used to conduct passive oxidation experiments for 30 minutes with Engine Out  $\text{NO}_x$  4.5 g/hp-hr and DOC inlet temperature of 300°C (DOC Out  $\text{NO}_2/\text{NO}_x = 0.26$ ) and 400°C (DOC Out  $\text{NO}_2/\text{NO}_x = 0.30$ ). At 300°C, there was a net soot gain of 5% without urea as compared to net soot gain of 20% with urea injection at ANR 1.2 as shown in Figure 2.2. However, at 400°C, there was a 25% net soot oxidation without urea compared to 19% net soot oxidation with urea injection at ANR 1.2 as shown in Figure 2.2. The lower soot oxidation with urea injection at 400°C is attributed to  $\text{NO}_2$  conversion via SCR reaction in the SCR catalyst on a DPF [16].



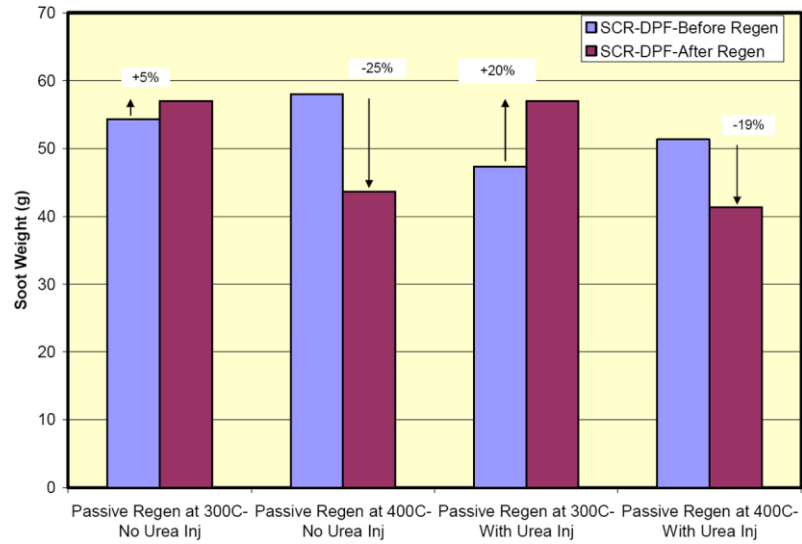


Figure 2.2: Passive Regeneration Capability of the SCR catalyst on a DPF With and Without Urea [16]

Troconi et al. [14] performed modeling and experimental studies to investigate the effect of SCR activity on passive regeneration characteristics of a Cu-zeolite SCR catalyst on a DPF. A 2.2 L Euro 4 Daimler OM 646 engine was used to perform two passive oxidation tests at 350°C and 450°C with and without NH<sub>3</sub> injection. At 350°C, the net oxidized soot mass at the end of the experiments was 6.2 g without NH<sub>3</sub> compared to 5.1 g with NH<sub>3</sub> injection. At 450°C, the net oxidized soot mass was 9.4 g without NH<sub>3</sub> compared to 8.6 g with NH<sub>3</sub> injection. It is evident that there is a negative effect of SCR reactions on the NO<sub>2</sub> assisted oxidation as the measured oxidized soot mass is lower for the cases when NH<sub>3</sub> is injected [14]. The contribution of NO<sub>2</sub> and O<sub>2</sub> to the total reaction rate for soot oxidation for each of these tests is shown in Figure 2.3. It is clearly observed that the NH<sub>3</sub> injection lowers the contribution of NO<sub>2</sub> to the soot oxidation at both the temperatures as a part of NO<sub>2</sub> is reduced by NH<sub>3</sub> before it reacts with soot resulting in lower soot oxidation rates. However, the effect of NH<sub>3</sub> on the contribution of O<sub>2</sub> to the soot oxidation is negligible.

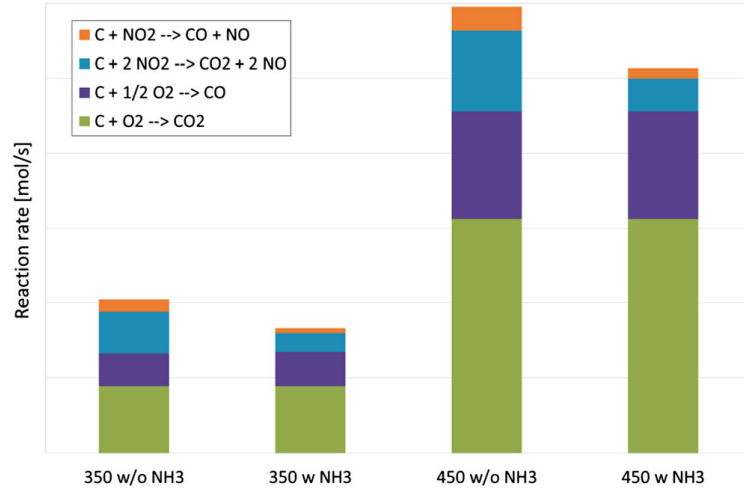


Figure 2.3: Predicted Soot Oxidation Reaction Rates for Passive Regeneration Experiments With and Without NH<sub>3</sub> Injection at 350°C and 450°C for a SCR catalyst on a DPF [14]

## 2.2 Kinetics of PM Oxidation

In this study, experimental tests were designed to determine the kinetics of NO<sub>2</sub> assisted oxidation of the PM retained in the SCR<sup>®</sup> for different loading conditions. The kinetics or the reaction rate of the PM oxidation is a function of temperature at which the reaction takes place, and the oxidant (NO<sub>2</sub> or O<sub>2</sub>) concentrations. Generally, the models used to understand the kinetics of PM oxidation are the standard Arrhenius model and the modified Arrhenius model. The equation for the standard Arrhenius model is given in Equation 6.

$$k_{std} = A * e^{-\frac{E_a}{R_u * T}} \quad [6]$$

where,

$k_{std}$  is the rate constant for the reaction [1/s],

A is the frequency factor or pre-exponential factor [1/s],

$E_a$  is the activation energy of the reaction [kJ/gmol],

$R_u$  is the universal gas constant = 8314 [kJ/gmol-K],

T is temperature of the reaction [K].

The equation for the modified Arrhenius model is similar to the standard Arrhenius model. However, the rate constant has a temperature dependent term. The equation of the modified Arrhenius model is given in Equation 7.

$$k_{mod} = B * T^n * e^{-\frac{E_a}{R_u * T}} \quad [7]$$

where,

$k_{mod}$  is the rate constant for the modified Arrhenius model [1/s],

B is the frequency factor or pre-exponential factor [1/s-K<sup>n</sup>],

T<sup>n</sup> is the temperature of the reaction to the power n, where n is the order of the reaction [K<sup>n</sup>].

Over the years, many researchers have conducted tests which includes reactor based studies or experiments on an engine with DOC-CPF (or DPF or SCR catalyst on a DPF) arrangement along with modeling efforts to determine the kinetics of NO<sub>2</sub> assisted and O<sub>2</sub> assisted oxidation. The kinetics of NO<sub>2</sub> assisted oxidation from the literature are given in Table 2.1. A range of activation energies are reported in the literature from 40-122 kJ/gmol for NO<sub>2</sub> assisted oxidation. Similarly, activation energies from various sources for NO<sub>2</sub> assisted and thermal oxidation has been summarized in references [4, 8]. Many sources have reported that activation energy for NO<sub>2</sub> or O<sub>2</sub> assisted oxidation depend on the PM composition [17], the temperature [17, 18], catalytic coating of the CPF [19] and many other factors. Hence, when comparing the activation energies from these sources, all the dependencies and testing conditions have to be taken into account. Also, it is important to note that the units for pre-exponential factor from different sources are different depending on the model and the relations used with respect to oxidant concentration. Reference [20] and reference [21] have used mole fractions and mass fractions respectively for the NO<sub>2</sub> concentrations whereas references [4, 8] have used mole concentrations in ppm respectively to determine the NO<sub>2</sub> assisted kinetics of PM oxidation.

The order of the reaction (n) used in Equation 7 is generally considered to be one (pseudo-first order) as reported by references [4, 8, 18, 19, 20, 22, 23, 24]. However, some authors have determined or referenced order of reaction for NO<sub>2</sub> or O<sub>2</sub> other than one. Reference [25] reports order of 0.76 to 0.94 for O<sub>2</sub> whereas reference [26] reports order of 0.39 for O<sub>2</sub> in thermal oxidation of Printex-U. Zero order for NO<sub>2</sub> has been reported by reference [27] in NO<sub>2</sub> assisted oxidation at around 300°C and an increasing dependence on NO<sub>2</sub> with temperature. In this study, a pseudo-first order reaction i.e. order one has been assumed for NO<sub>2</sub> assisted oxidation of PM.

Table 2.1: Kinetics of NO<sub>2</sub> Assisted Oxidation From Various References

Ref. #	Reference Name	Kinetics Model	Activation Energy	Pre-Exponential Factor	Temperature Range	NO <sub>2</sub> Range	Test Type	Notes
[-]	[-]	[-]	[kJ/gmol]	[-]	[°C]	[ppm]	[-]	[-]
[28]	Dabhoiwala et. al.	Modified Arrhenius	73	0.5-3 [m/K/s]	273-461	13-169	PM produced by a Heavy-Duty Diesel Engine (2002 Cummins ISM-330) and oxidized in CPFs with different catalyst loadings	-
[27]	Triana et. al.	Modified Arrhenius	122	100 [m/K/s]	286-429	60-128	Modeling study of a DOC-CPF using PM produced by a John Deere 8.1 L 175 kW @ 1200 rpm, 1060 N-m turbo and aftercooled HP and common rail injection engine, trapped and oxidized in a CPF	-
[23]	Messerer et. al.	Standard Arrhenius	115	1.17 [10 <sup>6</sup> /s]	275-450	0-800	Oxidation of FBR with Pt washcoat collected PM using reactor feed gas, produced by a LDV diesel engine	-
[23]	Messerer et. al.	Standard Arrhenius	98	7.36 [10 <sup>4</sup> /s]	275-450	0-710	Oxidation of FBR with Pt washcoat collected PM using reactor feed gas, produced by a HDV diesel engine	-
[24]	Kandylas et. al.	Modified Arrhenius	40	0.5 [gmol-K/m <sup>2</sup> /s <sup>2</sup> ]	165-416	200-400	PM produced by a 1.9 L, 66kW @ 4k rpm, turbocharged, DI and EGR and oxidized in a DPF	-
[20]	Premchand et. al.	Standard Arrhenius	74	0.1 [m/s] for cake and 0.35 [m/s] for wall	253-408	61-112	PM produced by a 2007 Cummins ISL 272 kW engine and oxidized in a production CPF	Activation Energy based on experimental data [22] and frequency factors estimated using a computational I-D CPF model developed at MTU
[21]	Mahadevan et. al.	Standard Arrhenius	60.8	0.007 [m/K/s] for cake and 0.007 [m/K/s] for wall	253-408	61-112		Activation Energy and frequency factors estimated using a 2-D CPF/SCR-F high fidelity model developed at MTU
[7]	Raghavan et. al.	Standard Arrhenius	87.5	8.15 [10 <sup>6</sup> /s]	302-389	330-1013	PM produced by a 2013 Cummins ISB 2013 280 hp engine and oxidized in a production CPF	Aftreatment Configuration: DOC-CPF-SCR
[4]	Raghavan et. al.	Modified Arrhenius	89	15.2*10 <sup>-3</sup> [1/K/ppm/s]	302-389	330-1013		Aftreatment Configuration: DOC-CPF-SCR
[8]	Gustafson et. al.	Standard Arrhenius	99.2	113.7 [1/ppm/s]	273-377	117-792	PM produced by a 2013 Cummins ISB 2013 280 hp engine and oxidized in the SCR-F <sup>®</sup>	Aftreatment Configuration: DOC-SCR-F <sup>®</sup> w/o urea
[8]	Gustafson et. al.	Standard Arrhenius	96	23.1 [1/ppm/s]	273-373	171-821		Aftreatment Configuration: DOC-SCR-F <sup>®</sup> w/ urea

### 2.3 Models for PM Oxidation

The rate of oxidation of carbonaceous materials or soot can be described using the general kinetic model equation described by Equation 8 [25].

$$RR_O = N_t * k(T) * f(p_{O_2}, p_{NO_2}, p_{H_2O}, \dots) \quad [8]$$

where,

$RR_o$  is the reaction rate,

$N_t$  is the total number of active carbon sites,

$k(T)$  is the temperature dependent reaction rate constant (Equation 6 and 7 in section 2.2),

$f(p_{O_2}, p_{NO_2}, p_{H_2O}, \dots)$  is a function which describes the dependency of reaction rate on partial pressure of various gas components which is generally linear as reported by references [18,29].

Several different approaches have been followed to determine the total number of active sites ( $N_t$ ). References [25,30] reports relating  $N_t$  to an active site concentration and to soot surface as described by Equation 9 [25].

$$N_t = \lambda * S_a \quad [9]$$

where,

$\lambda$  is the surface concentration of active sites,

$S_a$  is the specific surface area.

The specific surface area ( $S_a$ ) can be expressed as a function of the fraction of the soot oxidized as described by Equation 10 [25].

$$S_a = S_{a,o} * (1 - \xi_m)^n \quad [10]$$

Where,

$S_{a,o}$  is the initial specific surface area,

$\xi_m$  is the fraction of soot oxidized,

$n$  is the reaction order in carbon.

The reactivity of soot with respect to its oxidation has been investigated by many researchers over the years and it has been found that microstructure of the soot particles plays an important role in its oxidation behavior [31]. Many models have been proposed based on the microstructure of soot particles, one of which is the Bhatia and Perlmutter model [32] described by Equation 11. This model is based on growth of pores with random pore size distribution [33]. For low values of  $\xi_m$  the surface to volume ratio or specific surface area increases with  $\xi_m$  while at high value of  $\xi_m$  it decreases.  $\psi$  is a structural factor that determines the value of  $\xi_m$  at which this reversal of trend occurs.

$$S_a = S_{a,o} * (1 - \xi_m) * \sqrt{1 - \psi * \ln(1 - \xi_m)} \quad [11]$$

Another model known as the shrinking core model [33] assumes soot particles to be dense ideal spheres which implies that surface area shrinks more slowly than the mass of the soot [17]. As the soot particle oxidizes, the specific surface area increases and hence the reaction rate increases. There are contrasting reasons proposed for the increase in surface area with oxidation. Reference [34] reports the reason to be the change in density of the soot particle whereas reference [35] proposes the reason to be the increase in porosity of the soot particle. The shrinking core model is described in Equation 12 and is similar to Equation 11 with  $n=-1/3$ .

$$S_a = S_{a,o} * (1 - \xi_m)^{-\frac{1}{3}} \quad [12]$$

In the shrinking core model, the surface area of soot particle is not proportional to the mass of the particle. Hence, the fresh soot particle has less exposed surface area per unit mass than a particle already reduced by oxidation. For example, overall reactivity of 1 g of fresh soot is lower than the overall reactivity of same mass of partially oxidized soot. Hence for modeling, the age of different soot populations needs to be tracked along with the mass of the soot remaining, in order to correlate mass of the soot to the reactive surface area. A model based on the shrinking core model that can track each of incoming soot particles in the filter has been developed in this study

which is discussed in detail in section 4.1. A summary of the published research reporting varying reaction kinetics during PM oxidation in reactor studies is described in the following paragraphs.

Yezerets et al. [17] performed serial temperature programmed oxidation experiments on soot samples in a reactor with 10% O<sub>2</sub>/He feed gas. They reported a lower activation energy for oxidizing the initial 10-25% of the soot samples. It was proposed that the increased initial reactivity of soot samples was not because of hydrocarbons adsorbed on the soot particles but due to changes in the properties of particulate matter or due to formation of highly reactive species on the surface of carbon in the soot samples.

Messerer et al. [23] carried out reactor based oxidation experiments at different temperatures on LDV and HDV diesel soot samples with feed gas (150 ppm NO<sub>2</sub>, 45 ppm NO, 10% O<sub>2</sub>, and 3% H<sub>2</sub>O in N<sub>2</sub>). The variation of the reaction rates with the amount of soot oxidized in these experiments is shown in Figure 2.4. They attributed the initial high reactivity and the initial decrease of the rate of soot oxidation to the consumption of the most reactive soot components (adsorbed hydrocarbons, SFG) which account for almost 25% of the initial soot carbon mass. The linear increase in the reactivity for the region between 25% to 75% mass oxidized and non-linear increase in the reactivity for the region approaching 100% oxidation of the soot samples were explained with increasing surface-to-volume ratio and reactant accessibility using a shrinking core model expression, indicating fairly uniform reactivity and homogeneous chemical structures of the bulk material and the core of soot investigated [23].

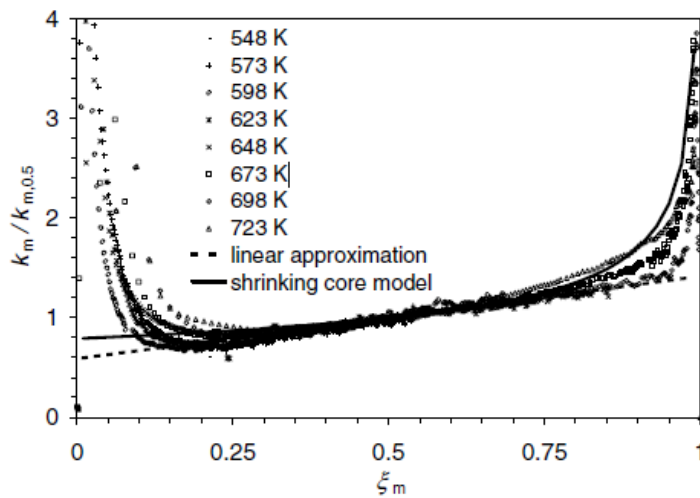


Figure 2.4: Dependence of the Pseudo First Order Rate Coefficient on Carbon Mass Conversion for LDV Soot Oxidation Experiments [23]

Konstandopoulos et al. [31] performed temperature programmed oxidation experiments by loading the soot samples generated from a common rail 1.9 L diesel engine, on a catalyst coated filter placed in a reactor. The filter samples were exposed to synthetic exhaust (10% O<sub>2</sub> in N<sub>2</sub>) at a constant volume flow rate and the temperature was increased from 250°C to 700°C at a rate of 3°C/min. A population model for different classes of soot particles in different states of contact with the catalyst was developed and applied to the experimental data. They reported three activation energies, lower activation energy (80 kJ/gmol) attributed to adsorbed organics (SOF, SFG) on the soot particles and relatively high activation energy of 120 kJ/gmol and 180 kJ/gmol corresponding to the shell and core respectively of the soot particles that are assumed to have a core-shell structure [35]. Konstandopoulos et al. [31] also performed isothermal experiments for soot oxidation on a catalyst coated filter. The variation of reactivity of soot particles with fraction of soot oxidized for these experiments is shown in Figure 2.5. The trend observed and its proposed explanation was similar to that reported by reference [23].

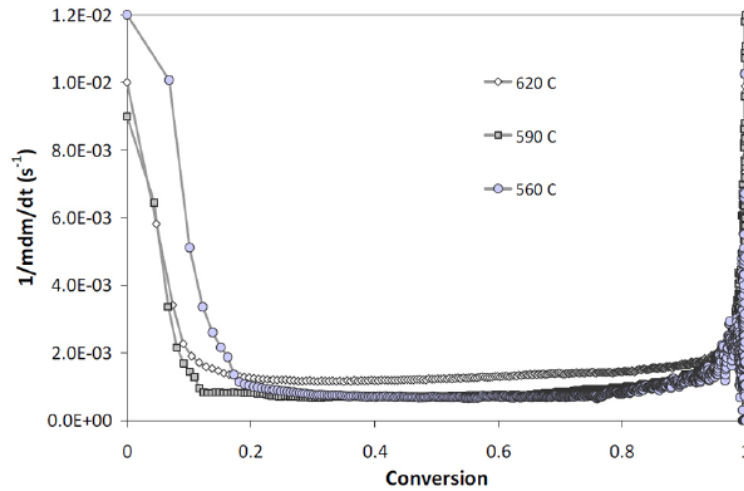


Figure 2.5: Soot Oxidation Rate on Catalyst Coated Filters at Different Temperatures [31]



## 2.4 Loading Studies of CPF and SCR Catalyst on a DPF

This section discusses the experiments performed by researchers on engine-dyno system with a CPF or SCR catalyst on a DPF to understand the characteristics of PM oxidation at different engine conditions leading to different exhaust flow rates or space velocities, NO<sub>2</sub> concentrations and inlet temperatures. A summary of the published research on this is described in the following paragraphs.

Hasan et al. [36] performed experiments on a Cummins ISM 2002 engine at rated speed (2100 RPM) and 20, 40, 60 and 75% of full load (1120 Nm) with and without a DOC upstream of the CPF to understand the effect of temperature and NO<sub>2</sub> concentrations on the PM oxidation in the catalyzed continuously regenerating trap (CCRT<sup>®</sup>). The MTU 1-D 2-layer CPF model was improved and calibrated using the experimental data to simulate and compare the evolution of pressure drop across the CPF, PM retained in the CPF and filtration efficiency with time to the experimental data. The model was also used to predict the evolution of cake, wall and channel pressure drop with time as well as the evolution of oxidation rate and PM retained in layer 1, layer 2 and wall in the CPF with time. The contribution of different components to the total pressure drop across the CPF after 5 hours of loading for 20% and 75% load test conditions is shown in Figure 2.6. Similarly, the PM oxidized in layer 1, layer 2 and wall in the CPF after 5 hours of loading along with the mechanism for PM oxidation for all the test conditions is shown in Figure 2.7. The percentage of PM oxidized increases with the increase in engine load due to higher temperatures and NO<sub>2</sub> concentrations. Also, for higher load (75%), pressure drop across CPF is lower compared to 20% load because of higher oxidation rate of PM in the wall as seen in Figure 2.6 and 2.7. Kinetics for PM oxidation in the wall were different from the kinetics for cake layers and did not change with temperature, exhaust flow rate or NO<sub>2</sub> concentrations. The same experiments and similar modeling work was performed by Dabhoiwala et al. [37] using the same engine with a different DOC and CPF. The trends in the percentage of PM oxidized and pressure drops was similar to that reported by reference [36].

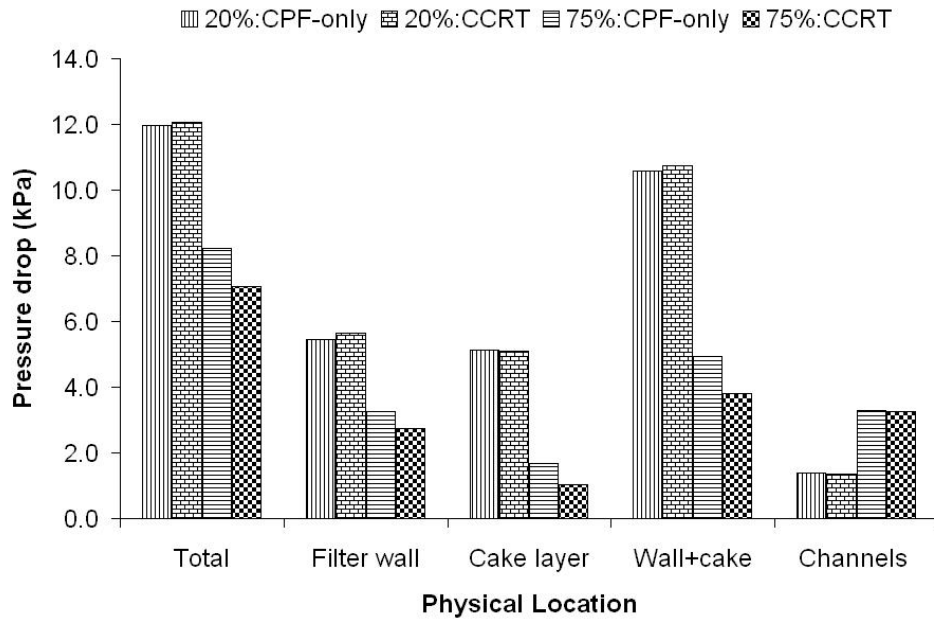


Figure 2.6: Pressure Drop Components After 5 Hours of Loading for 20% and 75% Load Test Condition [36]

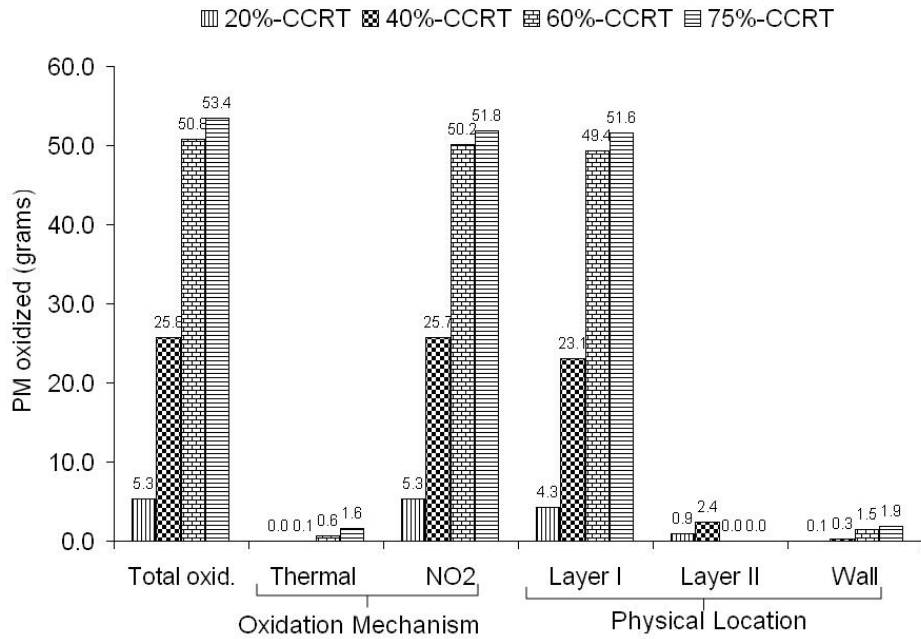


Figure 2.7: Total PM Oxidized After 5 Hours of Loading by Type and Physical Location [36]

Similar to the experiments performed by Hasan et al. [36] and Dabhoiwala et al. [37], Premchand et al. [38] performed a series of experiments on a 2004 John Deere 6.8 L engine at two engine speeds (2200 RPM and 1650 RPM) at four engine load ranging from 25% to 100% of rated torque at the respective engine speeds. The improved MTU 1-D 2-layer CPF model from reference [36] was calibrated using the experimental data for 2200 RPM tests and was used to predict the evolution of cake, wall and channel pressure drop with time as well as the evolution of oxidation rate and PM retained in layer 1, layer 2 and wall in the CPF with time. The PM oxidized in layer 1, layer 2 and wall in the CPF after 8 hours of loading for the 25% and 100% CPF and CCRT® test conditions predicted by the model is shown in Figure 2.8. It was observed that the percentage of PM oxidized by the CPF is higher at higher engine loads due to higher temperatures and NO<sub>2</sub> concentrations. The PM cake layer is the primary filter in the CPF after it is formed with filtration efficiency higher than 99%. Also, wall filtration efficiency decreases with increasing wall oxidation.

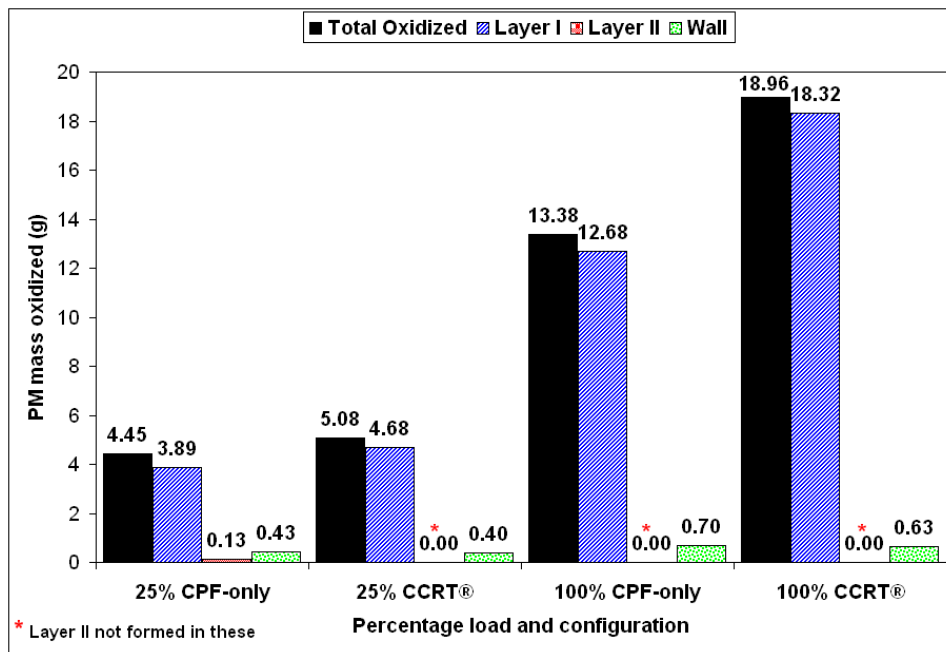


Figure 2.8: Distribution of PM Mass Oxidized by Location at 2200 RPM [38]

Raghavan et al. [4, 7] performed passive oxidation experiments to determine the kinetics of PM oxidation. The experiments consisted of first loading the CPF to a pre-determined amount of PM loading and then oxidizing the PM under selected exhaust conditions, followed by a post oxidation loading stage. A 2013 Cummins ISB 6.7 L engine was used to load 30 g of PM in the CPF at engine

condition 2400 RPM and 200 Nm and 30% reduced fuel rail pressure for 5.5 hours. The passive oxidation conditions had NO<sub>2</sub> concentrations ranging from 137 to 1013 ppm and temperatures ranging from 299 to 388°C. An Arrhenius plot of PM oxidation during the passive oxidation and loading stages is shown in Figure 2.9. As seen from Figure 2.9, the reaction rates during loading (S2) are higher compared to the passive oxidation stage (PO). The authors reported that the higher reaction rates during S2 are due to the oxidation of loosely packed topmost layers of PM cake which is thought to be more readily oxidized under relatively low NO<sub>2</sub> concentrations and temperature conditions observed during S2. Also, it was proposed that higher reactivity for S2 could be due to the nature of PM being oxidized being similar to the initially oxidized PM in reference [17] or the order of PM oxidation w.r.t NO<sub>2</sub> might be higher during loading conditions as suggested in reference [39].

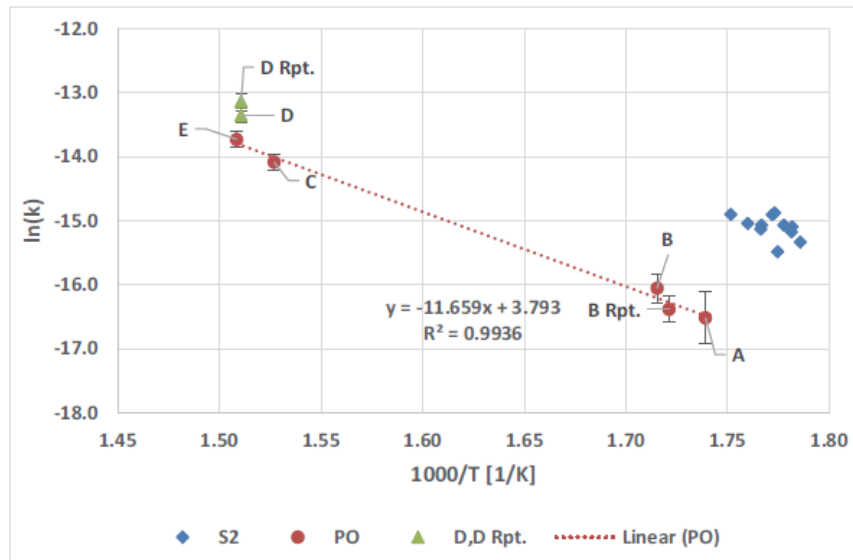


Figure 2.9: Comparison of Kinetics of PM Oxidation During Passive Oxidation and Loading Conditions in CPF [7]

Gustafson et al. [8] performed passive oxidation experiments on a SCR<sup>®</sup> with and without urea injection. The engine, loading condition, passive oxidation conditions and the test procedure were the same as used by reference [4]. An Arrhenius plot showing the comparison of PM oxidation during the passive oxidation and loading stages in CPF and SCR<sup>®</sup> w/ and w/o urea is shown in Figure 2.10. As seen from Figure 2.10, the reaction rates during loading (S2) are higher compared to the passive oxidation stage (PO) for the SCR<sup>®</sup> w/ and w/o urea. It was proposed that the lower

fuel rail pressure used in the loading stages compared to the nominal fuel rail used in the passive oxidation stage might have an influence on the oxidation rates. A similar trend was also observed by reference [4] for the CPF. Also, the reaction rate constant is reported to be 60% lower with urea injection with the SCR-F®.

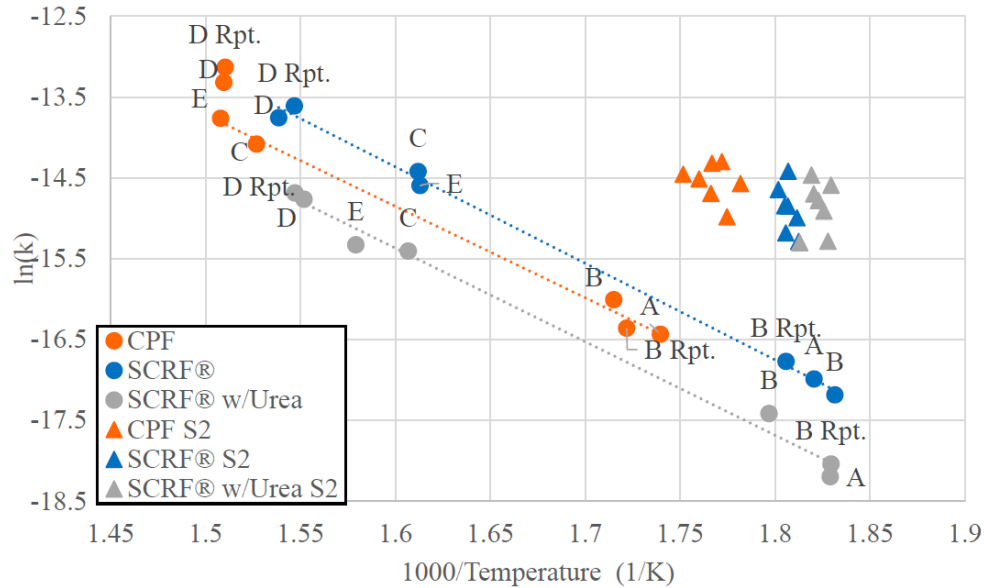


Figure 2.10: Comparison of Kinetics of PM Oxidation During Passive Oxidation and Loading Conditions in CPF, SCR-F® With and Without Urea [8]

Based on the modeling work performed by references [37, 38] using the 1-D 2 layer CPF model, a decreasing trend of pre-exponential for NO<sub>2</sub> assisted PM oxidation in the cake and wall was observed for a particular value of activation energy, with increasing engine load. Similarly, references [4, 8] reported a different set of kinetics for NO<sub>2</sub> assisted PM oxidation during loading and passive oxidation in the CPF and SCR-F® based on the experimental data. The calibration of the SCR-F model with passive oxidation data without urea for SCR-F® from reference [8] also resulted in a different set of kinetics for PM oxidation during the loading conditions and passive oxidation conditions [40]. This served as a motivation to perform the loading tests on the SCR-F® similar to that performed on the CPF by references [36, 37, 38], to understand and characterize the difference in the kinetics for NO<sub>2</sub> assisted PM oxidation during loading and passive oxidation conditions. The experimental data for these loading tests will be used to calibrate and develop a model for PM oxidation based on the shrinking core model, which is capable of simulating the PM

oxidation during loading and passive oxidation conditions for a single set of kinetics to overcome the limitations of the SCR-F model as it is a lumped model for PM oxidation as explained in the next section.

## 2.5 SCR-F Model

The focus of this section is to understand the development of the SCR-F model for PM filtration and oxidation, pressure drop and the temperature [12]. This provides a better understanding of the parameters to be calibrated in the SCR-F model to simulate the PM oxidation performance in the SCR-F<sup>®</sup> under loading conditions using the experimental data.

In the SCR-F model, the full volume of SCR-F<sup>®</sup> is divided into user configurable number of axial and radial zones wherein each zone consists of multiple inlet and outlet channels [21]. The channel geometry for each zone is illustrated by the schematic in Figure 2.11. Each zone consists of the substrate wall, PM cake and empty volume for inlet and outlet channels.

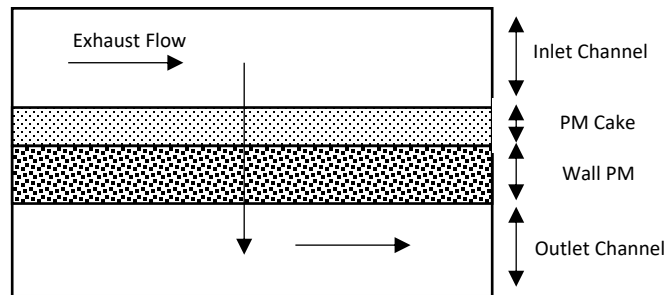


Figure 2.11: Schematic for the Channel Geometry in a Zone in the SCR-F Model

### PM Filtration and Oxidation Model

The SCR-F model takes into account the PM filtration within the substrate wall and cake separately. In each zone, the substrate wall is discretized into four slabs as shown in Figure 2.12 and the PM filtration takes place in a sequence starting from the cake through the four slabs in the wall.

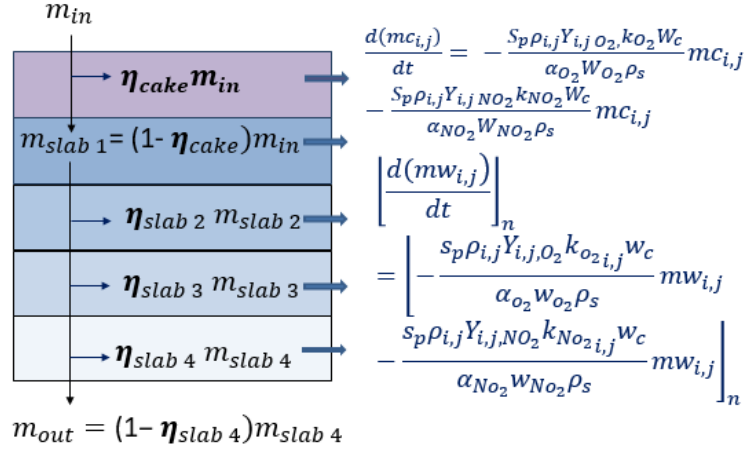


Figure 2.12: Schematic Showing Filtration of PM in the Cake and the Wall [21]

The overall filtration efficiency is calculated using Equation 13 [21].

$$\eta_{total,i,j} = 1 - [(1 - \eta_{cake,i,j}) \prod_{n=1}^{n=4} (1 - \eta_{wall,i,j \text{ slab } n})] \quad [13]$$

where,  $\eta_{cake,i,j}$  is the PM cake layer filtration efficiency and  $\eta_{wall,i,j \text{ slab } n}$  is the filtration efficiency of each slab in the substrate wall. Details about development of Equation 13 can be found in reference [20].

The PM retained in the cake layer and substrate wall is oxidized by  $\text{NO}_2$  assisted and thermal oxidation reactions. Equations 14 and 15, used in the SCR-F model, describe the reaction rate for the  $\text{NO}_2$  assisted oxidation of PM in the cake layer and substrate wall respectively within each zone. Similar equations have been used for the thermal oxidation in the model with a different set of kinetics given in reference [21].

$$RR_{NO_2,cake} = \frac{S_p * \rho_{i,j} * Y_{i,j,NO_2} * A_{cake} * T_{i,j} * e^{\left(\frac{E_{a,NO_2}}{R_u * T_{i,j}}\right)} * W_c}{\alpha_{NO_2} W_{NO_2} \rho_s} \quad [14]$$

$$RR_{NO_2,wall} = \frac{S_p * \rho_{i,j} * Y_{i,j,NO_2} * A_{wall} * T_{i,j} * e^{\left(\frac{E_{a,NO_2}}{R_u * T_{i,j}}\right)} * W_c}{\alpha_{NO_2} W_{NO_2} \rho_s} \quad [15]$$

where,  $s_p$  is the specific surface area of PM [1/m],  $\rho_{i,j}$  is the density of gas in each zone [kg/m<sup>3</sup>],  $Y_{i,j,NO_2}$  is the mass fraction of inlet NO<sub>2</sub> in each zone,  $A_{cake}$  is the pre-exponential for PM cake [m/K-s],  $A_{wall}$  is the pre-exponential for PM in the substrate wall [m/K-s],  $T_{i,j}$  is temperature of the filter in each zone [K],  $E_{a,NO_2}$  is the activation energy for NO<sub>2</sub> assisted PM oxidation [kJ/gmol],  $R_u$  is the universal gas constant [8.314 J/gmol-K],  $W_C$  is the molecular weight of carbon [kg/kmol],  $\alpha_{NO_2}$  is the NO<sub>2</sub> oxidation partial factor,  $W_{NO_2}$  is the molecular weight of NO<sub>2</sub> [kg/kmol] and  $\rho_s$  is the PM density [kg/m<sup>3</sup>].

### Pressure Drop Model

The pressure drop across the PM cake and wall in each zone has been modeled using Darcy's flow equation. Equations 16 and 17 from reference [21] show the calculation of pressure drop due to PM cake and wall respectively in the SCR-F model.

$$\Delta P_{cake,i,j} = \mu_{i,j} v_{s,i,j} \frac{w_{p,i,j}}{k_{cake,i,j}} \quad [16]$$

$$\Delta P_{wall,i,j} = \mu_{i,j} v_{w,i,j} \frac{w_s}{k_{wall,i,j}} \quad [17]$$

where,  $\Delta P_{cake,i,j}$  is the pressure drop due to PM cake at each zone,  $\Delta P_{wall,i,j}$  is the pressure drop due to the substrate wall at each zone,  $\mu_{i,j}$  is the dynamic viscosity of the exhaust gas at each zone,  $v_{w,i,j}$  is the velocity of gas through the substrate wall at each zone,  $v_{s,i,j}$  is the velocity of gas through the PM cake layer at each zone,  $w_s$  is the substrate wall thickness,  $w_{p,i,j}$  is the PM cake layer thickness at each zone,  $k_{wall,i,j}$  is the wall permeability at each zone and  $k_{cake,i,j}$  is the PM cake layer permeability at each zone. The detailed formulation of the terms used in Equations 16 and 17 and the formulae used for the channel pressure drop is given in reference [21].

### Temperature Model

The temperature model has been developed based on the resistance node terminology in reference [41]. The model takes into account the energy stored in the filter due to heat conduction along the length of the filter ( $\dot{Q}_{cond,axial}$ ), heat conduction in the radial direction of the



filter ( $\dot{Q}_{cond,radial}$ ), convection between the filter and the inlet and outlet channel gas ( $\dot{Q}_{conv1}$  and  $\dot{Q}_{conv2}$ ), energy released during the oxidation of the PM cake ( $\dot{Q}_{reac,PM}$ ), energy released during oxidation of the HC in the inlet channel gas ( $\dot{Q}_{reac,HC}$ ), enthalpy transfer by the wall-flow gas ( $\dot{Q}_{wall-flow}$ ) and heat transfer due to radiation exchange between channel surfaces ( $\dot{Q}_{rad}$ ).

Figure 2.13 shows the schematic of the mesh used for the temperature model. The model discretizes each zone into separate control volumes for inlet channels, filter and outlet channels. The energy balance equations are applied for control volume of the inlet and outlet channels and are explained in detail in reference [21].

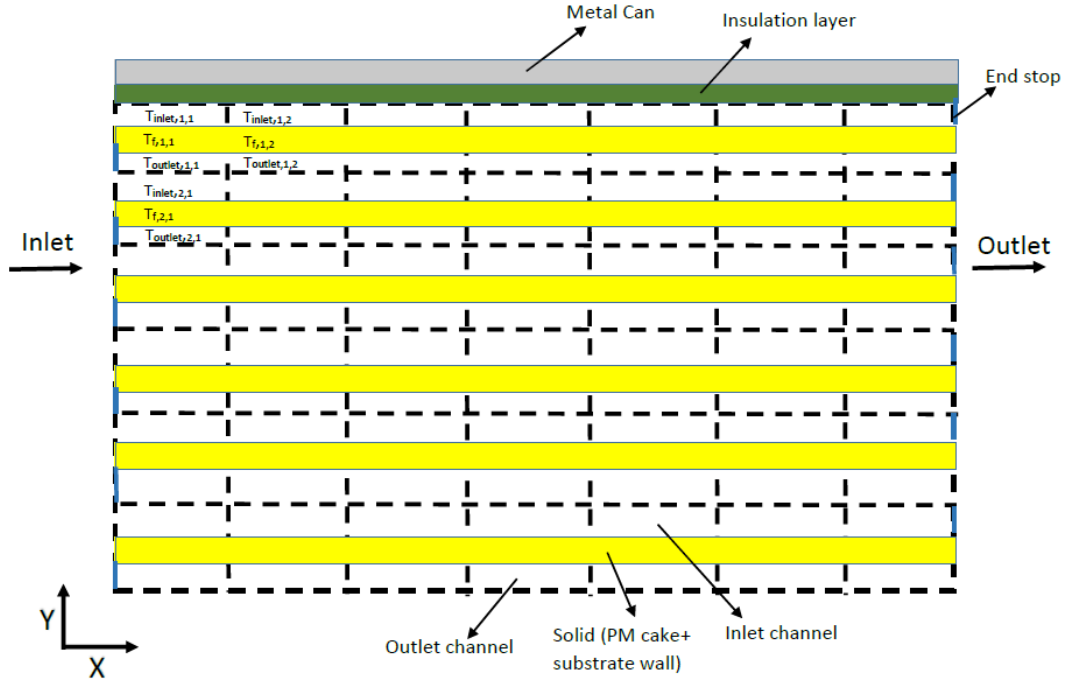


Figure 2.13: Schematic of Temperature Solver Mesh for SCR-F Model [21]

The energy equation for the control volume of filter in each zone is given by Equation 18 which is used to calculate the temperature of the filter in each zone.

$$(\rho_s c_s V s_{i,j} + \rho_f c_f V f_{i,j}) \frac{dT_{f,i,j}}{dt} = \dot{Q}_{cond,axial} + \dot{Q}_{cond,radial} + \dot{Q}_{conv1} + \dot{Q}_{conv2} + \dot{Q}_{reac,PM} + \dot{Q}_{reac,HC} + \dot{Q}_{wall-flow} + \dot{Q}_{rad}$$

[18]

where,  $T_f$  is the temperature of the filter. Again, the detailed formulae for terms in Equation 18 can be found in reference [21].

The SCR-F model, developed as discussed in the above paragraphs, has been calibrated using experimental data from passive oxidation w/o urea and active regeneration tests from reference [8]. The calibrated SCR-F model along with the PM oxidation model (Section 4.1) was used to model the PM retained, pressure drop and temperature distribution in the SCR-F<sup>®</sup> for loading conditions in this study and compared to the experimental data which is discussed in detail in Section 5.4.

## Chapter 3. Experimental Setup, Instrumentation and Test Procedures

This chapter focuses on the overall layout of the test cell, specifications of the aftertreatment components and instruments used for testing. It also provides a detailed description of the test procedures and the test matrix used for the experimental tests. A brief description of the test cell layout along with the sensors and components used is given in the next section. A detailed description of the engine, dynamometer and aftertreatment components is given in the subsequent sections. The chapter ends with a discussion of the test procedures and the test matrix for the Loading Tests along with the terms and equations used for the analysis of the data obtained from these tests.

### 3.1 Engine Test Cell Setup

This section discusses the layout of the engine, aftertreatment system (DOC and SCR<sup>®</sup>), instrumented sensors and the sampling locations within the test setup. The schematic layout of engine test cell is shown in Figure 3.1.

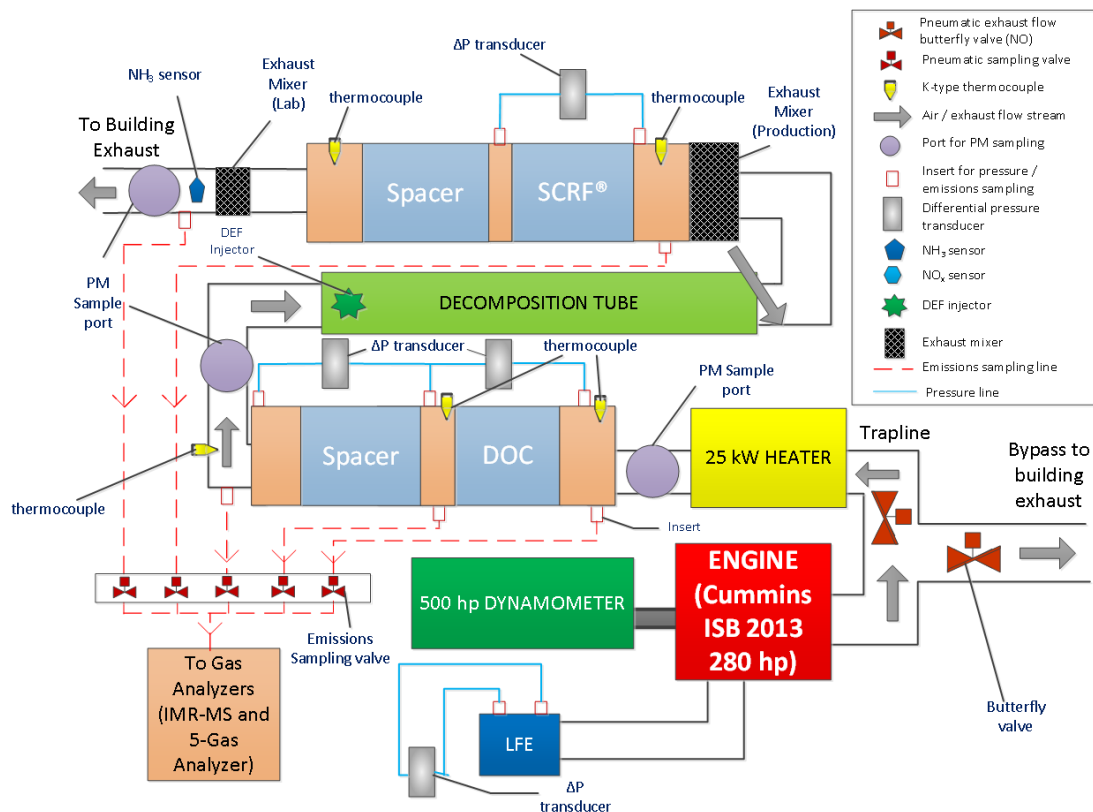


Figure 3.1: Schematic Layout of the Engine Test Cell Setup [4]

Fuel used in the engine is pumped from the fuel shed into the smaller day tank which periodically gets filled as fuel is consumed. The fuel then flows through a Coriolis flow meter which measures the rate of fuel flow. After passing through the Coriolis flow meter, it is cooled by the building water supply in a tube heat exchanger. It is then supplied to the engine after passing it through a four-micron filter and fuel water separator. The ventilation system for the test cell provides fresh air to the engine air filter which then flows through the Laminar Flow Element (LFE). The pressure drop across the LFE has been calibrated for the mass flow rate of air entering the engine using mathematical relations supplied by the manufacturer.

The exhaust from the engine flows downstream through a 4-inch diameter exhaust pipe, from where it can be directed either into the trap line, which leads through the aftertreatment system before exiting to the building exhaust, or directly through the bypass line to the building exhaust. Opening or closing the pneumatic butterfly valve corresponding to the trap line or bypass line allows us to switch the path of the exhaust flow. In the trap line, the exhaust gas flows through a 25 kW production heater which can be used to raise the temperature of the gas entering the aftertreatment system in a controlled manner without changing the engine conditions. After passing through the heater, the exhaust flows through the DOC which oxidizes NO into NO<sub>2</sub>, CO into CO<sub>2</sub> and HC into CO<sub>2</sub> and H<sub>2</sub>O. The exhaust then flows through the decomposition tube where the DEF solution, consisting of deionized water and urea, can be injected into the decomposition tube. After this, the exhaust gas flows through a mixer to allow the DEF decomposition products/droplets and the exhaust gas to form a homogeneous mixture. The exhaust gas then flows through the SCR<sup>®</sup> which is a wall flow device that has dual functionality of filtering the PM as well as reducing NO<sub>x</sub>. After the exhaust flows through the SCR<sup>®</sup>, it goes through a mixer before exiting to the building exhaust.

### 3.2 Engine and Dynamometer Specifications

A Cummins ISB 2013 heavy duty diesel engine was used for this study. A proprietary ECM software called Calterm III was supplied by Cummins along with the engine to monitor and log data from various sensors mounted on the engine and aftertreatment system. This software was also used to control important engine and aftertreatment parameters like enabling manual control of urea injection and deciding the flow rate of urea injection, or manually controlling the fuel rail injection pressure etc. The specifications of the engine are listed in Table 3.1.

Table 3.1: Specifications of the Engine

Model	Cummins ISB Heavy Duty
Year of Manufacture	2013
Cylinders	6, Inline
Bore x Stroke	107 x 124 mm
Displacement	6.7 L (409 in <sup>3</sup> )
Rated Speed and Power	2400 RPM and 208 kW
Peak Torque	895 Nm @ 1600 RPM
Fuel System	Direct Injection (Common Rail)
Aspiration	Variable Geometry Turbocharger (VGT)
EGR System	Electronically Controlled and Cooled

An eddy current dynamometer was used to control the speed and the load on the engine. The dynamometer was controlled by a Digalog Model 1022A controller with two modes of operation - Constant Speed and Constant Load. The Constant Speed mode was used for all the tests while using the throttle to control the load on the engine. The specifications for the dynamometer are listed in Table 3.2.

Table 3.2: Specifications of the Dynamometer

Manufacturer	Dynamatic
Model	DM8121HS
Type	Eddy Current
Construction	Wet Gap
Controller	Digalog Model 1022A
Load Cell	BLH Electronics U3G1C
Oiling	Constant Oiling Leveler
Maximum Torque	1501 ft-lbs at 1750 RPM
Constant Power	500 hp from 1750 – 7000 RPM

### 3.3 Fuel Properties

The properties for the ultra-low sulfur diesel (USLD) used in the experimental tests for this study are listed in Table 3.3. The same blend of fuel was used throughout testing as it was stored and consumed from a local fuel storage facility.

Table 3.3: Fuel Properties

Fuel Type	ULSD-2
API. Gravity at 15.6 °C	35.4
SP. Gravity at 15.6 °C	0.848
Viscosity at 40 °C	2.999
Total Sulfur (ppm)	7
Initial Boiling Point (°C)	184
Final Boiling Point (°C)	363
Cetane Index	48.7
Water Content (ppm)	34
Higher Heating Value <sup>1</sup> (MJ/kg)	45.68
Lower Heating Value <sup>1</sup> (MJ/kg)	42.89
H/C <sup>2</sup>	1.833

<sup>1</sup>Obtained from reference [42] where similar fuel was used

<sup>2</sup>Obtained from reference [43]

### 3.4 Aftertreatment System

The aftertreatment system used in this study consists of a Diesel Oxidation Catalyst (DOC) and SCRF<sup>®</sup> (SCR catalyst on a DPF) from Cummins, Johnson Matthey and Corning. The DOC is a flow through device capable of oxidizing CO, NO and HC in the engine exhaust. The SCRF<sup>®</sup> is a wall flow device that has dual functionality of filtering the PM as well as reducing NO<sub>x</sub>. The specifications of these components are listed in Table 3.4.

### 3.5 Test Cell Instrumentation

There were several production sensors, non-production sensors and measurement devices that were used for collecting data during the experimental tests. A schematic of these instruments along with the engine and dynamometer is shown in the Figure 3.2.

Table 3.4: Specification of Substrate

Component	DOC	SCR <sup>F</sup>
Material	Cordierite	Cordierite
Catalyst	Pt	Cu-zeolite
Diameter (in)	9	10.5
Diameter of Substrate (mm)	228.6	266.7
Length (in)	4	12
Length (mm)	101.6	304.8
Cell Geometry	Square	Square
Total Volume (L)	4.17	17.04
Open Volume (L)	3.5	10.2
Cell Density (/in <sup>2</sup> )	400	200
Cell Width (mil)	46	55
Cell Width (mm)	1.16	1.39
Filtration Area (in <sup>2</sup> )	N/A	11370
Open Frontal Area (in <sup>2</sup> )	26.92	25.9
Channel Wall Thickness (mil)	4	16
Wall Density (g/cm <sup>3</sup> )	0.91	N/A
Porosity (%)	35	50
Mean Pore Size (μm)	N/A	16
Number of Inlet Cells	25447	8659
Actual Open Surface Area (m <sup>2</sup> )	4.22	7.37
Surface Area of Cells (m <sup>2</sup> )	12.08	14.74
Perimeter of Cell (mm)	4.67	5.58

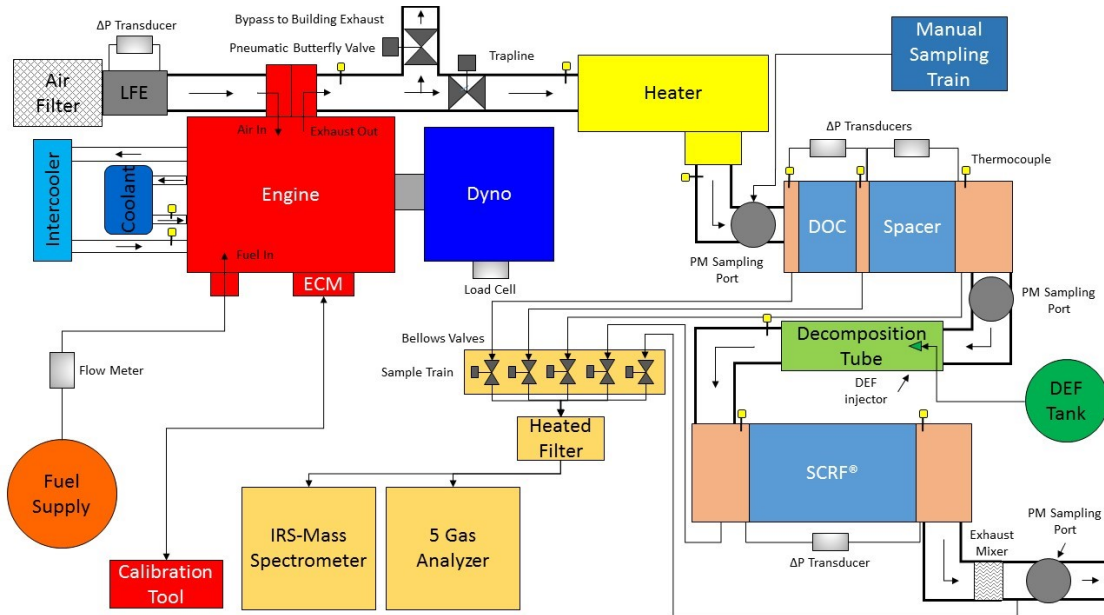


Figure 3.2: Schematic of the Instrumentation in the Test Cell [8]

The detailed specifications for each of the instruments and devices in the test cell are described in the following paragraphs.

### 3.1.1 Laminar Flow Element (LFE)

A Laminar Flow Element model 50MC2-06F from Meriam Instruments was used to determine the mass flow rate of air entering the intake manifold. This was done by measuring the pressure difference across the orifice using a differential pressure transducer and determining the volumetric air flow rate from the calibrated flow curve provided by the manufacturer which gives the relation between the flow rate in standard cubic feet per minute and differential pressure. The volumetric flow rate was then converted to mass flow rate using the density of air at the standard conditions (25 °C and 1 atm pressure).

### 3.1.2 Fuel Flow Measurement

A model CMFS015M319N2BAECZZ Micro Motion Coriolis Meter was used to measure the mass flow rate of fuel as well as the fuel density and temperature. The specifications of this instrument are listed in Table 3.5.

*Table 3.5: Coriolis Meter Specifications*

Manufacturer	Micro Motion		
Model	CMFS015M319N2BAECZZ		
Measurement	Flowrate	Density	Temperature
Accuracy	± 0.10%	± 0.5 kg/m <sup>3</sup>	± 1 °C
Repeatability	± 0.05%	± 0.2 kg/m <sup>3</sup>	± 0.2 °C

### 3.1.3 Thermocouples

K-type thermocouples were used to measure temperatures of the exhaust gas at locations upstream and downstream of the 25kW heater, DOC, Spacer, Decomposition Tube, SCRF<sup>®</sup> as well as the temperature of the coolant and air intake. Twenty thermocouples, namely S1-S20 were instrumented in the SCRF<sup>®</sup> at different axial and radial locations - S1-S10 into the inlet channels and S11-S20 into the outlet channels. The layout of the thermocouples instrumented in the SCRF<sup>®</sup> is shown in Figure 3.3. The specifications of the thermocouples used are listed in Table 3.6.



Table 3.6: Thermocouple Specifications

Manufacturer	Omega			
Part Number	KMQSS-125U-6	KMQSS-032U-12	KMQSS-020U-12	KMQSS-020U-16
Type	K	K	K	K
Length	6"	12"	12"	16"
Diameter	0.125"	0.032"	0.020"	0.020"
Accuracy	$\pm 2.2$ °C	$\pm 2.2$ °C	$\pm 2.2$ °C	$\pm 2.2$ °C
Count	13	3	16	4
Location	Exhaust, Air Intake, Coolant	Heated Sample Lines	SCRF® Channel	SCRF® Channel

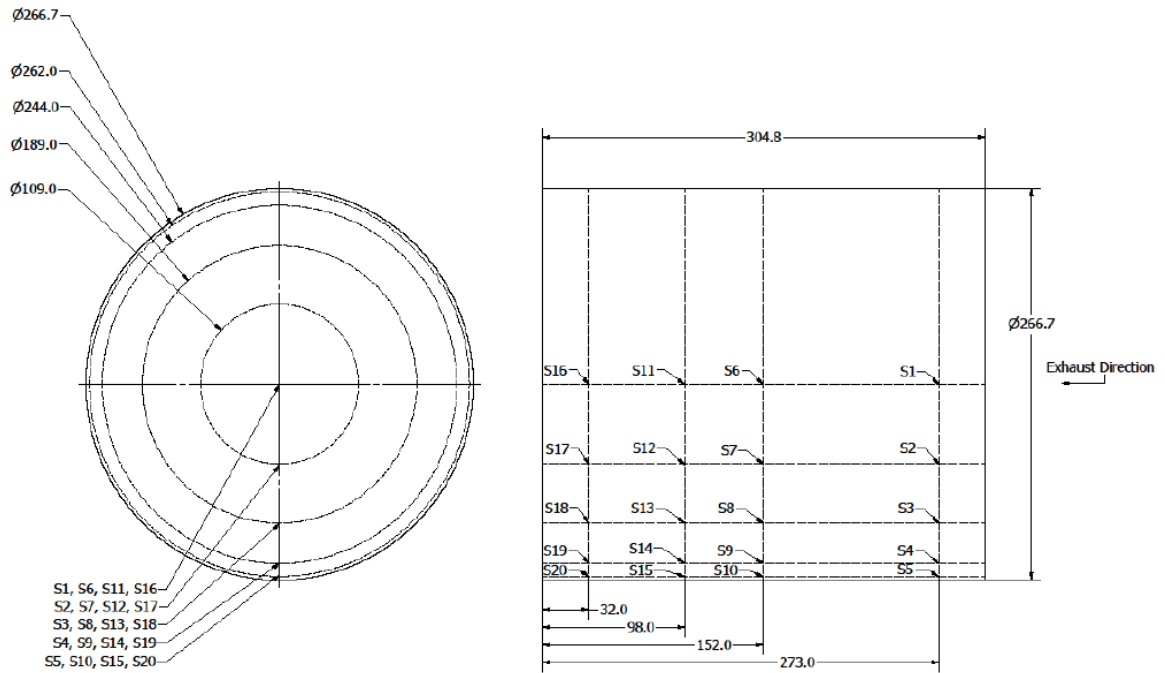


Figure 3.3: SCRF® Thermocouple Layout [9]

### 3.1.4 Pressure Transducers

Pressure Transducers were used to measure pressure drop across the LFE, DOC and SCRF®. The specifications of the pressure transducers used are listed in Table 3.7. An OMEGA HX94V Temperature and Pressure Transmitter was also used to take measurements for test cell conditions during the experimental tests.

Table 3.7: Pressure Transducers Specifications

Manufacturer	Omega			
Model	PX419-26B5V	PX429-10WDWU10V	PX409-2.5DWU5V	PX429-5DWU10V
Type	Absolute	Differential	Differential	Differential
Range	26-32 in Hg	0-10 in H <sub>2</sub> O	0-2.5 PSID	0-5 PSID
Accuracy, Linearity, Hysteresis, Repeatability	± 0.08% FS	± 0.08% FS	± 0.08% FS	± 0.08% FS
Output Voltage	0-5 VDC	0-10 VDC	0-5 VDC	0-10 VDC
Measurement	Barometric Pressure	ΔP LFE	ΔP DOC	ΔP SCRF®

### 3.1.5 Data Acquisition System

Two NI cDAQ-9178 chassis from National Instruments (NI) with different modules were used to collect engine speed, load, pressure, temperature data from different locations in the test cell and control the electro-pneumatic valves in the valvetrain to allow emission sampling at different locations in the aftertreatment system. A NI LabVIEW interface was developed to log and monitor the data from these modules on the desktop computer. The specifications for the different NI modules are listed in Table 3.8.

A PCAN service tool was used to obtain the data from the engine ECM using CAN communication (J1939 protocol) by connecting it to the desktop computer via USB. Calterm III, the proprietary software from Cummins, was used to log and monitor the engine ECM data and manually control performance parameters like fuel rail pressure, post-combustion fuel dosing, urea dosing, throttle position etc.

Table 3.8: Specification of the Data Acquisition System

Manufacturer	National Instruments				
Module	NI 9205	NI 9213	NI 9263	NI 9239	NI 9472
Signal Type	Analog Input	Analog Input	Analog Output	Analog Input	Digital Output
Signal Count	16 Differential	16 Differential	4	4 Differential	8
Quantity	1	4	1	2	1
Rate	250 kS/s	75 S/s	100 kS/s	50 kS/s	100 μs
Maximum Range	±10 V	±78.125 mV	±10 V	±10 V	6V – 30 V
Accuracy	6220 μV	38 μV	0.11 V	0.019 V	-
Measurement	Pressure Transducers	Temperature (Thermocouple)	Speed and Load	Speed and Load Control for Transients	Valvetrain Control

### 3.1.6 Particulate Matter (PM) Sampling

A manual sampling train manufactured by Anderson Instruments Inc. and a dry gas meter were used to measure the concentration of PM in the engine exhaust by hot sampling. Figure 3.4 shows the picture of the manual sampling train and the sampling probe. A/E type glass fiber filters with 47 mm diameter were used to collect the PM samples by putting the filters in the sampling probe and inserting the sampling probe into the exhaust flow through one of the three sampling ports in the aftertreatment system (Figure 3.1). The manual sampling train is used to draw the sample and measure the duration, temperature, vacuum pressure and the dry gas meter measures the volumetric flow of the exhaust gas sample. The PM concentration is then calculated using these values and the pre and post sampling weights of the glass fiber filter. The detailed information about weighing the glass fiber filter before and after the tests is given in reference [4].

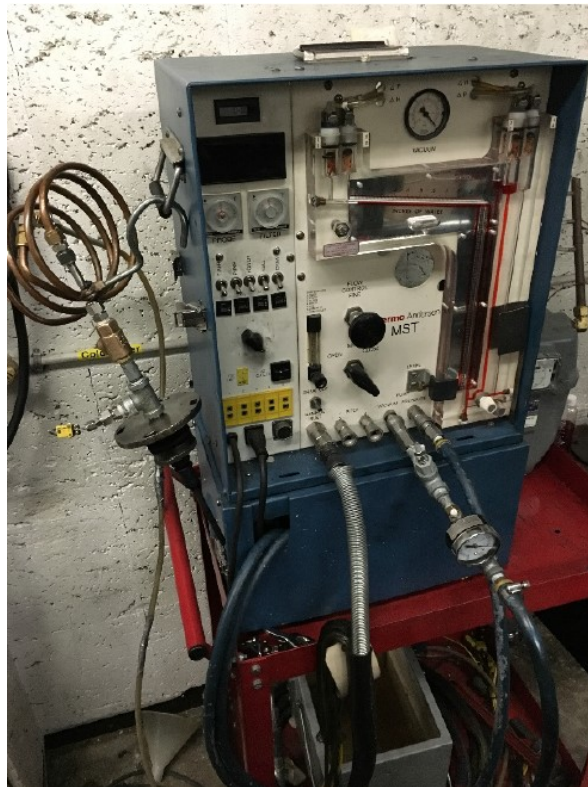


Figure 3.4: Manual Sampling Train, Sampling Probe and Dry Gas Meter [8]

### 3.1.7 Substrate Weighing Scale

A model Ranger RD35LM weighing scale manufactured by Ohaus was used to weigh the SCRF<sup>®</sup> in-between the stages during the test which is discussed in detail in section 3.6. The specifications of the weighing scale are listed in Table 3.9. The detailed procedure to weigh the SCRF<sup>®</sup> is discussed in detail in reference [4]. The PM mass retained during each stage of the test is calculated from the weight of the SCRF<sup>®</sup> at the end of each stage which is discussed in detail in section 3.9.

Table 3.9: Weighing Scale Specifications

Manufacturer	Ohaus
Model	RD35LM
Capacity	35000 g
Certified Readability	± 1.0 g
Readability	± 0.1 g
Linearity	± 0.3 g

### 3.1.8 Emission Sampling

Emission samples were collected and measured at three locations in the aftertreatment system, namely, upstream DOC (UDOC), upstream SCRF<sup>®</sup> (USCRF<sup>®</sup>) and downstream SCRF<sup>®</sup> (DSCR<sup>®</sup>). The exhaust gas from these locations was allowed to flow through stainless steel sampling lines and a heated filter before being sampled by two different instruments. One of the instruments was an Airsense Ion Molecule Reaction Mass Spectrometer (IMR-MS) from V&F Instruments Inc. and the other was the AVL AMA-4000 Pierburg Emission Bench. The temperature of the sampling lines and the heated filter was maintained at 190 °C throughout the test to avoid condensation of water vapor and to minimize adsorption of gaseous emissions on the sampling lines [44].

The Mass Spectrometer was used to measure NO, NO<sub>2</sub>, NH<sub>3</sub> and O<sub>2</sub> species concentrations in the exhaust at UDOC, USCRF<sup>®</sup> and DSCR<sup>®</sup>. The specifications of the Mass Spectrometer are listed in Table 3.10. The detailed procedure to operate and calibrate the Mass Spectrometer is discussed in reference [9].

Table 3.10: IRS-MS Specifications

Manufacturer	V&F
Model	Airsense
Accuracy	< ± 2%
Mass Range	0-500 amu
Resolution	< 1 amu
Lower Detection Limit	< 1ppb (benzene in air)
	< 10 ppm (benzene in exhaust gas)
Drift Concentration	< ± 5% over 12 hours
Reproducibility	< ± 3%
Max Humidity	80%
Measurement Type	Wet
Analysis Time	10-6500 msec/amu
Response Time	T90<50 msec

The Pierburg emission bench was used to measure concentrations of NO/NO<sub>x</sub>, THC, O<sub>2</sub>, CO and CO<sub>2</sub> in the exhaust. The NO/NO<sub>x</sub> analyzer was capable of measuring only one species at a time. The NO<sub>2</sub> concentrations were estimated by subtracting NO from the NO<sub>x</sub> concentrations. The specifications of the Pierburg emission bench are listed in Table 3.11. The Pierburg emission bench was not used for some of the initial tests due to issues with its software and touch interface which were resolved later.

Table 3.11: Pierburg Emission Bench Specifications [8]

Manufacturer	Pierburg				
Model	AMA4000				
Measurement	O <sub>2</sub>	CO	CO <sub>2</sub>	NO <sub>x</sub> /NO	THC
Range	0-25%	0-5000 ppm	0-20%	0-10000 ppm	0-20000 ppm
Detection Limit	15 ppm	125 ppb	15 ppm	35 ppb	30 ppb C <sub>3</sub>
Accuracy	N/A	N/A	N/A	N/A	N/A
Repeatability	≤ 0.5% of the measured value + 2x the detection limit	≤ 0.5% of the measured value + 2x the detection limit	≤ 0.5% of the measured value + 2x the detection limit	≤ 0.3% of the measured value + 2x the detection limit	≤ 0.5% of the measured value + 2x the detection limit
Noise	≤ 1.0% of the measured value + 2x the detection limit	≤ 1.0% of the measured value + 2x the detection limit	≤ 1.0% of the measured value + 2x the detection limit	≤ 1.0% of the measured value + 2x the detection limit	≤ 1.0% of the measured value + 2x the detection limit
Analyzer Type	Paramagnetic	IRD	IRD	CLD	FID
Measurement Type	Dry	Dry	Dry	Wet	Wet

The production aftertreatment system had two UniNO<sub>x</sub> sensors installed, one each at the engine outlet and the SCR/SCR<sup>®</sup> outlet. The sensor measured NO<sub>x</sub> concentrations in the exhaust and displayed and logged the data through Calterm via CAN communication. Each sensor consists of a zirconia based multilayer sensing element by NGK Insulators and a control unit by Continental. A NH<sub>3</sub> sensor from Delphi was also installed at the SCR<sup>®</sup> outlet to measure NH<sub>3</sub> slip (Figure 3.1). Data from the NH<sub>3</sub> sensor was monitored and logged through LabVIEW interface via CAN communication. The specifications of the sensors are listed in Table 3.12. A picture of the NO<sub>x</sub> and NH<sub>3</sub> sensor is shown in Figure 3.5 and 3.6 respectively.

Table 3.12: Specifications of NO<sub>x</sub> and NH<sub>3</sub> Sensors

Component	Range	Resolution	Accuracy	Voltage Range	Operating Temperature
NO <sub>x</sub> Sensor	0-1500 ppm	0.1 ppm	± 10 %	12-32 V	100-800 °C
NH <sub>3</sub> Sensor	0-1500 ppm	0.1 ppm	± 10 %	13.5 – 32 V	200-500 °C
λ Sensor, O <sub>2</sub> (linear)	12-21 %	0.10 %	± 0.3 - ± 1.4 %	24 V	100-800 °C



Figure 3.5: Production NO<sub>x</sub> Sensor



Figure 3.6: Delphi NH<sub>3</sub> Sensor

### 3.6 Test Procedure

Primarily, the Loading Tests were designed to determine the NO<sub>2</sub> assisted oxidation kinetics for PM retained in the SCR<sup>®</sup> for different loading conditions with and without urea injection and to characterize the differences in the reaction kinetics in loading and passive oxidation conditions and also to collect data for modeling the SCR<sup>®</sup> pressure drop and PM mass retained during loading conditions. The test procedures for the Loading Tests were developed by modifying the procedures used in reference [8]. Figure 3.7 shows the schematic of the test procedure followed

for Loading Tests w/o Urea. Each Loading Test consists of a warmup, cleanout and two loading stages as shown in Figure 3.7. The detailed explanation for each of the stages is given in later paragraphs in this chapter.



Figure 3.7: Stages of a Loading Test w/o Urea

The test procedure followed for the Loading Test w/ Urea is similar to the procedure followed for the Loading Tests w/o Urea. The only difference between the tests is the injection of DEF at ANR 1.0 during the two loading stages as shown in Figure 3.8. This is done to understand the interaction of PM oxidation and NO<sub>x</sub> reduction performance in loading conditions with urea injection.

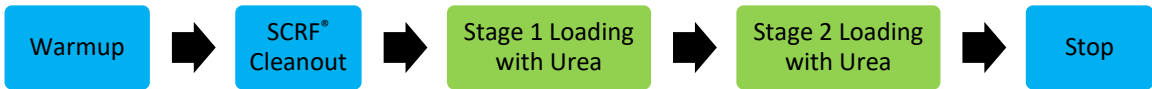


Figure 3.8: Stages of a Loading Test w/ Urea

A plot of pressure drop across SCRF<sup>®</sup> is shown in Figure 3.9 and give a graphical representation of the loading profile of a complete Loading Test. When comparing one Loading Test to another, the variable changed are engine speed, engine load and fuel rail pressure which eventually changes the SCRF<sup>®</sup> inlet temperature and PM and NO<sub>2</sub> concentrations.

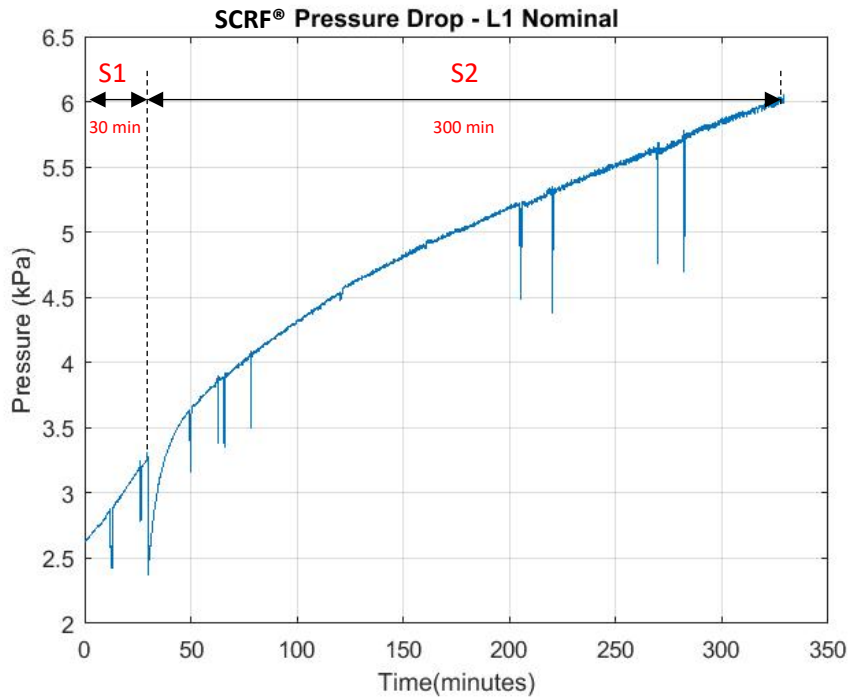


Figure 3.9: SCRF® Pressure Drop vs Time for a Typical Loading Test (Warmup and SCRF® Cleanout Stage Omitted)

## Warmup

In this stage, the engine is run at specific speeds and loads for predetermined time durations as shown in Table 3.13 to allow the oil, coolant and substrate temperature to stabilize at steady state conditions. The Mass Spectrometer is calibrated and other instruments are checked in this stage so that if there are some issues, they can be addressed before starting the next stage. At the end of this stage, the exhaust flow is switched from the bypass line to the trap line to begin the SCRF® Cleanout stage.

Table 3.13: Warmup Stage Engine Conditions

Engine Speed	Engine Load	Duration	Condition
[RPM]	[Nm]	[min]	[-]
750	20	3	Idle
1200	200	5	Warmup
1660	475	5	Baseline



### **SCRF® Cleanout**

In this stage, the SCRF® is cleaned out to remove the PM remaining in the SCRF® from the previous tests to ensure that we start the Stage 1 Loading with nearly zero PM loading in the SCRF®. This is done by running the engine at the baseline condition shown in Table 3.13 and dosing roughly 35-38 mg/stroke of fuel late in the combustion cycle. The unburnt hydrocarbons from this dosed fuel get oxidized in the DOC which results in an exothermic reaction. As a result, the temperature of the exhaust gas increases to a temperature of around 600 °C. The PM retained in the SCRF® oxidizes completely because of active regeneration at around 600 °C in 30-45 minutes depending on the amount of PM retained from the previous tests. The pressure drop across the SCRF® is observed until it approaches a balance point or where the slope of pressure drop curve becomes zero to ensure that nearly all the PM loaded in the SCRF® has been oxidized during this stage. A balance point is defined as the point at which the rate of PM oxidation is same as the rate of PM loading in the SCRF®. Once the balance point is reached, the fuel dosing is stopped and the exhaust gas temperature is allowed to stabilize for 10-15 minutes before going to the next step.

### **Stage 1 Loading**

In this stage, the PM produced by the engine is loaded into the SCRF® by running the engine at the loading condition chosen for that specific test. The details of the engine speed, load, fuel rail pressure and exhaust flowrate for each of the Loading Tests are given in Section 3.7. In Loading Tests w/ Urea, DEF is injected at target ANR 1.0 during the Stage 1 Loading. The loading conditions corresponding to the specific test is run for 30 minutes. During these 30 minutes, gaseous emission samples are collected and measured by the Mass Spectrometer for 10 minutes each at UDOC, USCRF® and DSCR®. A PM sample is also collected at UDOC for 10 minutes using the MST and Gas Flow Meter as described earlier in Section 3.1.6.

At the end of Stage 1, the path of the exhaust flow is switched from the trap line to the bypass line to prevent further loading of PM in the SCRF®. The engine is then returned to idle conditions for a few minutes before shut down. Once the engine is shut down, the SCRF® is removed from the aftertreatment system and the temperatures for the thermocouples instrumented inside the SCRF® are measured manually to ensure that the average of the readings is  $235 \pm 30$  °C. The SCRF®

is then weighed at the same condition without allowing it to cool down further because there is an increase in weight of the SCRF<sup>®</sup> as it cools down as observed in reference [45].

### **Stage 2 Loading**

After weighing the SCRF<sup>®</sup> at the end of Stage 1, the SCRF<sup>®</sup> is installed back into the aftertreatment system and the engine is brought back up to the loading condition corresponding to the specific test. The temperatures in the aftertreatment system are allowed to stabilize before switching back the path of the exhaust flow from bypass line to the trap line for the Stage 2 Loading to begin. This warmup procedure takes 5-10 minutes as the aftertreatment components are still at relatively higher temperatures. In Loading Tests w/ Urea, DEF is injected at a target ANR of 1.0 for the entire duration of Stage 2 Loading.

The Stage 2 Loading is run for 300 minutes (5 hours) during which gaseous emission samples are collected and measured by the Mass Spectrometer at UDOC, USCRF<sup>®</sup> and DSCR<sup>®</sup> for 100 minutes each. In some of the tests, 60 minute measurements were made at these locations with the Mass Spectrometer and 40 minutes with the Pierburg emission bench. Five PM samples are taken during Stage 2, out of which four PM samples are taken at UDOC for 10 minutes each and one PM sample is taken at DSCR<sup>®</sup> for 60 minutes. The PM sample at DSCR<sup>®</sup> is taken following the first two samples at UDOC to equally space out the samples across the duration of Stage 2. This is done to check if the PM concentrations in the exhaust flow vary as the SCRF<sup>®</sup> loads. After 300 minutes, the path of the exhaust flow is switched from the trap line to the bypass line to prevent further loading of PM in the SCRF<sup>®</sup> and the engine is returned to idle before being shut down. The weighing procedure is repeated as followed at the end of Stage 1 Loading.

### **3.7 Test Matrix for Loading Tests w/o Urea**

Primarily, the Loading Tests were designed to determine the NO<sub>2</sub> assisted oxidation kinetics for PM retained in the SCRF<sup>®</sup> for different loading conditions with and without urea injection and to characterize the differences in the reaction kinetics in loading and passive oxidation conditions. So, while selecting the test points for the Loading Tests, it was important to select engine conditions where more than 90% of the PM oxidation was NO<sub>2</sub> assisted with relatively low SCRF<sup>®</sup> inlet temperatures and NO<sub>2</sub> concentrations to have a sufficient mass of SCRF<sup>®</sup> PM loading. Figure

3.10 shows the map of SCR<sup>®</sup> inlet temperatures and NO<sub>2</sub> concentrations for the 2007 Cummins ISL engine and aftertreatment system from reference [20]. The blue lines represent lines of constant reaction rates and the ratios on the lines represent the contribution of NO<sub>2</sub> to the oxidation of PM. Figure 3.10 also shows the test conditions selected (marked in red) for the Loading Tests keeping the points mentioned above in consideration.

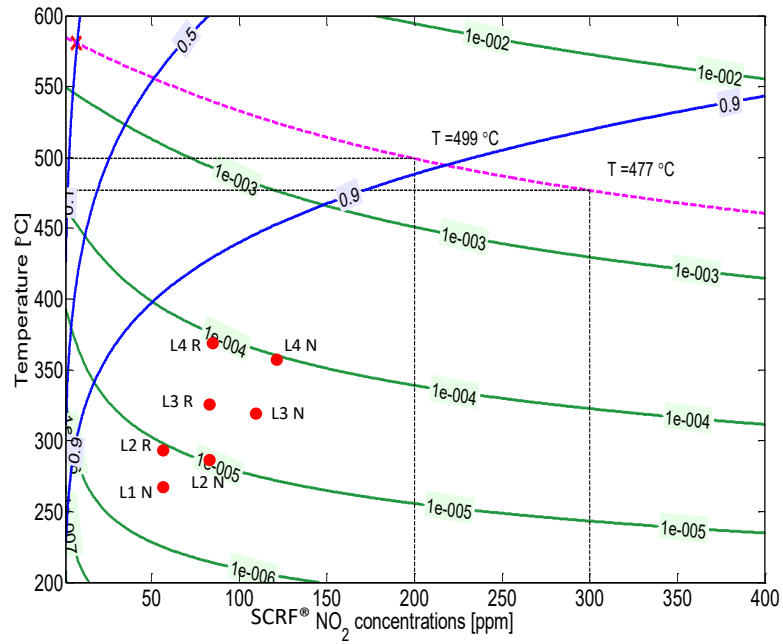


Figure 3.10: Test Conditions for Loading Tests [20]

The test matrix for the Loading Tests w/o Urea is shown in Table 3.14. Table 3.15 shows the emission data for this test matrix obtained by running point validation tests to ensure that the test conditions lie in the region in which 90% of the PM oxidation is NO<sub>2</sub> assisted as shown in Figure 3.10 and that there is a variation in the PM reaction rate.

Table 3.14: Test Matrix for Loading Tests w/o Urea

Test	FRP	Speed	Load	Exhaust Flow Rate	Std. Space Velocity	DOC Inlet Temp.	SCRF® Inlet Temp.
[-]	[Bar]	[RPM]	[Nm]	[kg/min]	[k/hr]	[°C]	[°C]
L1-Nom	1500	2400	203	10.9	33	273	270
L1-Red <sup>#</sup>	1050	2400	200	11.2	33	276	273
L2-Nom	1560	2400	271	11.4	34	293	293
L2-Red	1092	2400	271	11.5	34	302	297
L3-Nom	1575	2400	339	11.9	36	325	325
L3-Red	1103	2400	339	12.0	36	338	332
L4-Nom	1610	2400	406	12.5	37	355	355
L4-Red	1127	2400	406	12.5	37	371	364

<sup>#</sup>Data obtained from Test PO-C in reference [11]

Table 3.15: Emission Data for Loading Tests w/o Urea Obtained by Point Validation Test

Test	NO <sub>2</sub> into DOC	NO into DOC	NO <sub>2</sub> into SCRF®	NO into SCRF®	PM Conc.
[-]	[ppm]	[ppm]	[ppm]	[ppm]	[mg/scm]
L1-Nom	28	200	62	163	7.2
L1-Red <sup>#</sup>	22	161	58	128	11.5
L2-Nom	30	265	86	202	6.5
L2-Red	26	192	64	154	10.0
L3-Nom	25	305	108	208	5.8
L3-Red	22	226	80	160	9.0
L4-Nom	15	355	118	240	5.3
L4-Red	13	250	87	172	9.8

<sup>#</sup>Data obtained from Test PO-C in reference [11]

### 3.8 Test Matrix for Loading Tests w/ Urea

The test matrix for the Loading Tests w/ Urea is shown in Table 3.16. Four test conditions from the Loading Tests w/o Urea are being used with urea dosing at ANR 1.0. This is done to determine the effect of urea on NO<sub>2</sub> assisted PM oxidation kinetics as well as to understand the interaction of PM oxidation and NO<sub>x</sub> reduction with urea injection for the loading conditions. Table 3.17 shows the emission data for this test matrix obtained by running point validation tests.

Table 3.16: Test Matrix for Loading Tests w/ Urea

Test	FRP	Speed	Load	Exhaust Flow Rate	Std. Space Velocity	DOC Inlet Temp	SCRF® Inlet Temp.
[-]	[Bar]	[RPM]	[Nm]	[kg/min]	[k/hr]	[°C]	[°C]
L1-Nom w/ Urea	1500	2400	203	10.9	33	273	270
L1-Red w/ Urea <sup>#</sup>	1050	2400	203	11.2	33	276	273
L3-Nom w/ Urea	1575	2400	339	11.9	36	325	325
L3-Red w/ Urea	1103	2400	339	12.0	36	338	332

<sup>#</sup>Data obtained from Test PO-C in reference [11]

Table 3.17: Emission Data for Loading Tests w/ Urea Obtained by Point Validation Test

Test	ANR	NO <sub>2</sub> into DOC	NO into DOC	NO <sub>2</sub> into SCR®	NO into SCR®	PM Conc.
[-]	[-]	[ppm]	[ppm]	[ppm]	[ppm]	[mg/scm]
L1-Nom w/ Urea	1.0	28	200	62	163	7.2
L1-Red w/ Urea <sup>#</sup>	1.0	22	161	58	128	11.5
L3-Nom w/ Urea	1.0	25	305	108	208	5.8
L3-Red w/ Urea	1.0	22	226	40	160	9.0

<sup>#</sup>Data obtained from Test PO-C in reference [11]

### 3.9 Equations Used for Analysis of PM Data

The terms and equations used for the analysis of the experimental data are described in the following paragraphs.

The mass of the PM produced by the engine and entering the SCR® is calculated using Equation 19.

$$m_{in} = c_{in} * \frac{\dot{m}_{exhaust}}{\rho_{Std}} * \frac{t_{stage}}{1000} \quad (19)$$

where,  $c_{in}$  is the average PM concentration in the exhaust at engine out location [mg/scm],  $\dot{m}_{exhaust}$  is the mass flow rate of exhaust [kg/min] calculated as the sum of the mass air flow rate and fuel flow rate from the laminar flow element and the Coriolis meter respectively and  $t_{stage}$  is the duration of the stage [min].

The mass of the PM filtered out of the SCR® is calculated using Equation 20. This includes the PM that was filtered but not oxidized.

$$m_{out} = (1 - \eta_f) * m_{in} \quad (20)$$

where,  $\eta_f$  is the filtration efficiency of the SCRF<sup>®</sup> calculated using Equation 21.

$$\eta_f = \frac{c_{in} - c_{out}}{c_{in}} \quad (21)$$

Only one downstream concentration is taken during the test in stage 2, so an assumption is made that the filtration efficiency remains roughly constant after the cake layer forms. The estimation of Stage 1 filtration efficiency using the calibrated SCR-F model is discussed in Appendix A.

The mass of PM retained in the SCRF<sup>®</sup> at the end of the stage is calculated using Equation 22. PM retained is a cumulative value, meaning the mass of PM at the end of the Stage 2 includes the mass of PM loaded from Stage 1.

$$m_{retained} = M_S - M_{clean} \quad [22]$$

where,  $M_S$  is the weight measurement of the SCRF<sup>®</sup> taken at the end of the stage [g] and  $M_{clean}$  is the clean weight of the SCRF<sup>®</sup> at the start of the Stage 1 [g]. The calculation of the clean weight of the SCRF<sup>®</sup> is discussed in detail in Appendix A.

The mass of the PM oxidized [g] during the stage is calculated from the overall PM mass balance using Equation 23.

$$m_{ox} = m_{start} + m_{in} - m_{out} - m_{retained} \quad (23)$$

where,  $m_{start}$  is the mass of the PM in the SCRF<sup>®</sup> at the beginning of the stage [g]. The value of  $m_{start}$  for the Stage 1 is zero and for Stage 2 is equal to the  $m_{retained}$  at the end of Stage 1.

The percentage of PM oxidized [%] during the stage is calculated using Equation 24.

$$\%m_{ox} = \frac{m_{ox}}{m_{start} + m_{in}} * 100 \quad (24)$$

The exhaust flow rate through the SCRF® can also be expressed in terms of the standard space velocity [1/hr] or the reactor volumes per unit time flowed through the SCRF® as described by Equation 25. A higher space velocity indicates less time spent in the substrate.

$$SV_{Std} \left[ \frac{1}{hr} \right] = \frac{\dot{m}_{exhaust} \left[ \frac{kg}{min} \right]}{\rho_{Std} \left[ \frac{kg}{m^3} \right] * V_{Substrate} [m^3]} * 60 \left[ \frac{min}{hr} \right] \quad (25)$$

where,  $V_{Substrate}$  is the total volume of the SCRF® shown in Table 3.4 [m<sup>3</sup>].

### 3.10 Equations Used for Calculation of Experimental Reaction Rate

The procedure followed to calculate the reaction rate for PM oxidation based on the experimental data is discussed in this section. The procedure followed is similar to the procedure used by references [4, 7, 8].

The mass balance equation or the rate of change of the mass retained in a control volume (SCRF®) as shown in Equation 26 is obtained by differentiating Equation 23 and substituting the mass oxidized ( $\dot{m}_{ox}$ ) as the product of reaction rate ( $RR_o$ ) and the mass retained, and the flow rate of mass entering ( $\dot{m}_{in}$ ) as shown in Equation 27.

$$\frac{dm_{retained}}{dt} = \dot{m}_{in} - \dot{m}_{out} - m_{retained} * RR_o \quad (26)$$

$$\text{where, } \dot{m}_{in} = \frac{\dot{m}_{exhaust}}{\rho_{std}} * C_{in} \quad (27)$$

Substituting Equations 20 and 27 into Equation 26 and rearranging the terms results in a first order linear differential as shown in Equation 28.

$$\frac{dm_{retained}}{dt} + m_{retained} * RR_o = \eta_f * \frac{\dot{m}_{exhaust}}{\rho_{std}} * C_{in} \quad (28)$$

The solution of the linear differential equation (Equation 28) is shown in Equation 29 which is solved iteratively over the duration of interest using MATLAB to calculate the average reaction rate ( $RR_o$ ).

$$m_2 = \eta_f * c_{in} * \frac{Q_{Std}}{RR_o * 1000} * (1 - e^{-RR_o * t}) + m_1 * e^{-RR_o * t} \quad (29)$$

where,  $m_2$  is the mass of PM retained in the SCRF<sup>®</sup> at the end of the time step [g], and  $m_1$  is the mass of PM retained in the SCRF<sup>®</sup> at the beginning of the time step [g],  $t$  is the duration of time step [s] and  $Q_{Std}$  is the average standard volumetric flowrate of exhaust during the stage calculated using Equation 30.

$$Q_{Std} \left[ \frac{\text{scm}}{\text{s}} \right] = \frac{\dot{m}_{exhaust} \left[ \frac{\text{kg}}{\text{min}} \right]}{\rho_{Std} \left[ \frac{\text{kg}}{\text{m}^3} \right]} * \frac{1}{60 \left[ \frac{\text{s}}{\text{min}} \right]} \quad (30)$$

For the calculation of average reaction rate for Stage 2 for the Loading Tests, the PM retained at the end of Stage 1 ( $m_{retained,S1}$ ) and Stage 2 ( $m_{retained,S2}$ ) is calculated as explained in Appendix A. The mass of the PM in the SCRF<sup>®</sup> at the beginning of the Stage 2 ( $m_{start,S2}$ ) is equal to the PM retained at the end of Stage 1 ( $m_{retained,S1}$ ). Based on the  $m_{start,S2}$  and  $m_{retained,S2}$  values, the reaction rate for Stage 2 is calculated following the iterative process explained below. The reaction rate results for Stage 2 for the Loading Tests w/o and w/ Urea are discussed in detail in Section 5.1 and Section 5.2 respectively.

For the first iteration, the value of  $m_1$  is set equal to  $m_{start}$  for the stage,  $RR_o$  is assumed zero or a value close to zero (as infinity cannot be handled by MATLAB) and the value of  $m_2$  is calculated for the time step. For the next time step, the value of  $m_1$  is set equal to  $m_2$  from the previous time step and the value of  $m_2$  is calculated for the next time step. This is continued till the final time step and the value of  $m_2$  at the final time step is compared to the experimental  $m_{retained}$  value  $\pm 0.05$  g. If the value of  $m_2$  at the final time step is less than the experimental  $m_{retained} - 0.05$ g, the value of  $RR_o$  is increased by  $10^{-7} \text{ s}^{-1}$ . If the value of  $m_2$  at the final step is more than the experimental  $m_{retained} + 0.05$ g, the value of  $RR_o$  is decreased by  $10^{-7} \text{ s}^{-1}$ .



For the next iteration, the value of  $RR_o$  from the previous iteration is used. The same procedure is followed for further iterations till the value of  $m_2$  is within the tolerance limit of  $m_{retained} \pm 0.05g$ . The value of  $RR_o$  in the final iteration is taken as the average reaction rate during the duration of interest.

Once the value of the average reaction rate is estimated for a test condition, the value of reaction rate constant (k) is calculated by normalizing the reaction rate by the  $NO_2$  concentration at the SCR<sup>®</sup> inlet for that test condition. The natural logarithm of the reaction rate constant can be plotted versus the inverse of SCR<sup>®</sup> inlet temperature for all test conditions to determine the kinetics of the PM oxidation using a standard Arrhenius model as seen in Figures 2.9 and 2.10.

## Chapter 4. Model for PM Oxidation

References [4,7,8] reported higher reactivity of PM retained in the CPF and SCR-F<sup>®</sup> during loading conditions compared to passive oxidation conditions as discussed in Section 2.4. The calibration of the SCR-F model with passive oxidation data from reference [8] also resulted in a different set of kinetics for PM oxidation during the loading conditions and passive oxidation conditions [40]. Hence, to model the oxidation of PM using a single set of kinetics for a wide range of conditions including loading and passive oxidation conditions, there was a need to develop a model which takes into account the microstructure of PM particles as compared to the SCR-F model which is a lumped model for PM oxidation. Motivated by this concept, a model for PM oxidation was developed using the shrinking core model [33] which takes into account the changes in the reactivity of PM particle at the microstructure level as it oxidizes and it also keeps track of each of the incoming PM masses in the oxidation process.

The focus of this chapter is on the development of the PM oxidation model which is discussed in detailed in Section 4.1. The application of the results of the PM oxidation model to the SCR-F model in order to simulate the PM retained in the SCR-F<sup>®</sup> and the pressure drop across the SCR-F<sup>®</sup> is discussed in Section 4.2. Section 4.3 describes in detail the calibration process for the SCR-F model with the loading test data. Further, the PM oxidation model was calibrated using passive oxidation data [8] to check if the model can simulate the PM oxidation using a single set of kinetics under loading and passive oxidation conditions which is discussed in Section 4.4.

### 4.1 Model Development

The model for PM oxidation has been developed from the fundamental equation of conservation of mass and a shrinking core model for PM oxidation [23, 33]. Figure 4.1 shows a control volume (depicting a SCR-F<sup>®</sup>) at time  $t$  with some amount of mass loaded (discretized into four lumped masses with different colors) termed as  $m_{\text{retained}}(t)$ . At time  $t$ , assume that an exhaust stream containing a lumped mass ( $m_{\text{in}}$ ) enters the control volume as shown in Figure 4.1. At time  $t+\Delta t$ , a portion of the lumped mass entering ( $m_{\text{in}}$ ) is retained in the control volume while a portion of the lumped mass entering ( $m_{\text{in}}$ ) exits the control volume ( $m_{\text{out}}$ ) as the filtering efficiency is less than 100%. Also, a portion of the  $m_{\text{retained}}(t)$  gets oxidized by reacting with the  $\text{NO}_2$  in the exhaust stream. The remaining portion of  $m_{\text{retained}}(t)$  plus the portion of the incoming lumped mass ( $m_{\text{in}}$ ) retained in the control volume is collectively termed as  $m_{\text{retained}}(t+\Delta t)$  as shown in Figure 4.1.

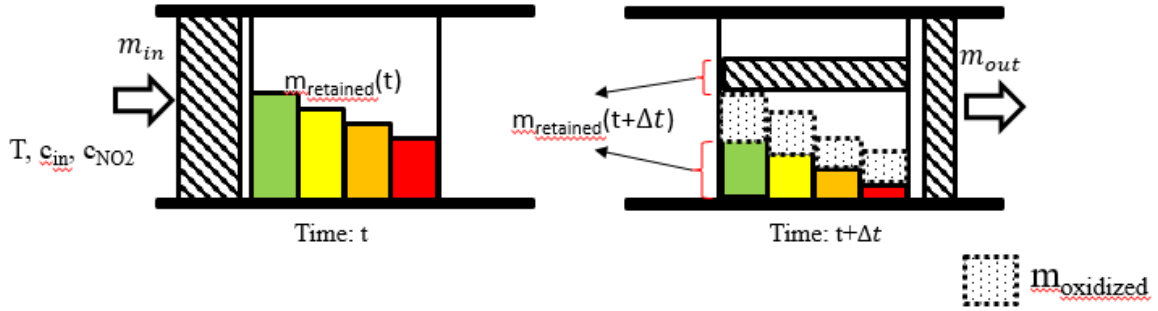


Figure 4.1: PM Mass Balance in a Control Volume at Time  $t$  and  $t+\Delta t$

The assumptions made in the development of this model are listed below.

- The exhaust flow rate ( $\dot{m}_{in}$ ), PM in ( $c_{in}$ ) and  $\text{NO}_2$  concentration ( $c_{\text{NO}_2}$ ) are assumed constant with time for a particular lumped mass entering the control volume at time  $t$ .
- The temperature for PM oxidation is assumed to be equal to the SCRF® inlet temperature and is assumed constant with time for a particular lumped mass entering the control volume at time  $t$ .
- There is no oxidation of the lumped mass entering the control volume during time  $\Delta t$  [46]. Only the PM retained in the control volume gets oxidized.
- An important point to note is that the oxidation of the different masses retained in the control volume at time  $t$  has not been uniform which is depicted by different sizes of the colored lumped masses at time  $t+\Delta t$  in Figure 4.1.

The mass balance equation and the inlet mass flow rate for a lumped mass entering the control volume (the SCRF®) at during  $\Delta t$  and exiting during time  $\Delta t$  is described by Equations 31 and 32.

$$\frac{dm_{retained}}{dt} = \dot{m}_{in} - \dot{m}_{out} - m_{retained} * RR \quad [31]$$

$$\text{where, } \dot{m}_{in} = \frac{\dot{m}_{exhaust}}{\rho_{std}} * c_{in} \quad [32]$$

Here,  $m_{retained}$  is the PM retained in the SCRF® [g],  $\dot{m}_{in}$  is the flow rate of PM entering the SCRF® [g/s],  $\dot{m}_{out}$  is the flow rate of PM exiting the SCRF® [g/s],  $RR$  is the reaction rate of oxidation of PM retained [1/s],  $\dot{m}_{exhaust}$  is the flow rate of exhaust [g/s],  $\rho_{std}$  is the standard exhaust density - 1.18 kg/m<sup>3</sup> (25°C and 101.3 kPa) and  $c_{in}$  is the PM concentration in the exhaust [g/scm].

The SCRF® is a wall flow device and the exhaust stream entering the inlet channel passes through the porous substrate wall and exits through the outlet channel. A portion of the PM in the exhaust stream entering the inlet channels is retained in the SCRF® due to filtration in the substrate wall and the cake [21] and the remaining portion of PM exits through the outlet channels. The filtration efficiency ( $\eta_f$ ) of the SCRF® as a fraction is described by Equation 33.

$$\eta_f = 1 - \frac{\dot{m}_{out}}{\dot{m}_{in}} \quad [33]$$

Equation 33 can be modified as  $\dot{m}_{in} - \dot{m}_{out} = \eta_f \dot{m}_{in}$  which when substituted in Equation 31 results in the equation 34 for PM mass balance.

$$\frac{dm_{retained}}{dt} = \eta_f \dot{m}_{in} - m_{retained} * RR \quad [34]$$

For the model development, assume that there is some mass retained in the SCRF® denoted by  $m_{retained}^i(t_j)$  at time  $t_j$  due to filtration of a lumped mass (i) in the SCRF®. At time  $t_{j+1}$ , the reduced value of the mass retained  $m_{retained}^i(t_{j+1})$  due to oxidation is calculated using Equation 35 which is obtained by discretizing Equation 34 for the for the lumped mass (i) with  $\Delta t = t_{j+1} - t_j$ .

$$\frac{m_{retained}^i(t_{j+1}) - m_{retained}^i(t_j)}{t_{j+1} - t_j} = \eta_f \dot{m}_{in}^i - \frac{m_{retained}^i(t_{j+1}) + m_{retained}^i(t_j)}{2} * RR^i(t_j) \quad [35]$$

Figure 4.2 shows the variation of mass retained with time for the different lumped masses (i, i+1, i+2....) entering the SCRF® at time ( $t_j, t_{j+1}, t_{j+2}....$ ) respectively i.e. after every assumed time step of 1 minute. The value of the mass retained decreases or increases with time as it gets oxidized as seen in Figure 4.2.

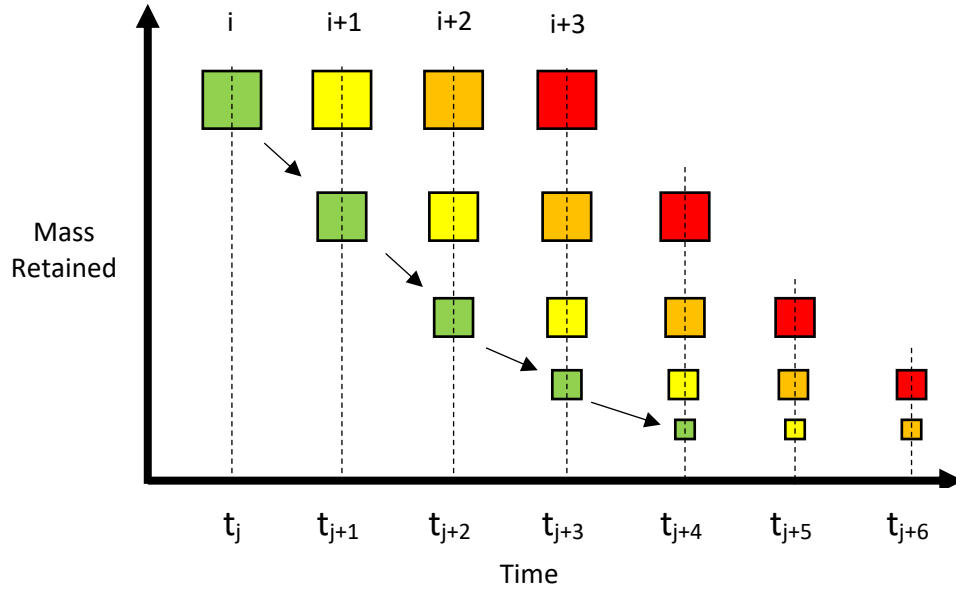


Figure 4.2: Schematic Representation of the Variation of Mass Retained in the SCRF® With Time

Once the value of  $m_{retained}^i(t_{j+1})$  is calculated using Equation 35, the percentage of PM oxidized ( $\xi$ ) is calculated at time  $t_{j+1}$  for lumped mass (i) using Equation 36 and 37.

$$\xi^i(t_{j+1}) = 1 - \frac{m_{retained}^i(t_{j+1})}{\eta_f m_{in}^i} \quad [36]$$

$$\text{where, } m_{in}^i = c_{in} * \frac{\dot{m}_{exhaust}}{\rho_{std}} * (t_{j+1} - t_j) \quad [37]$$

The value of  $\xi^i(t_{j+1})$  calculated at time  $t_{j+1}$  using Equation 36 is then used to determine the value of oxidation factor (k) to be used in calculating the reaction rate for the next time step. The value of oxidation factor (k) for a particular value of percentage of PM oxidized ( $\xi$ ) is determined by interpolating in between the specific points extracted from the trend of PM oxidized ( $\xi$ ) vs oxidation factor (k) shown in Figure 4.3. This trend is obtained from the data for the reactor studies for PM oxidation in reference [23] shown in Figure 2.4. The trend is also similar in nature to that obtained by reference [31] shown in Figure 2.5. The trend shown in Figure 4.3 was used for the initial computation in the model.

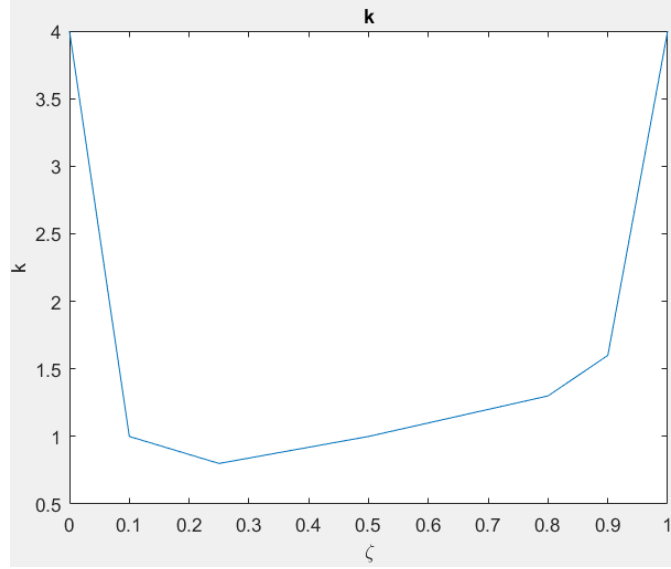


Figure 4.3: Variation of the Oxidation Factor ( $k$ ) With Percentage of PM Oxidized ( $\xi$ ) [23]

The reaction rate  $RR^i(t_{j+1})$  for the lumped mass (i) at time ( $t_{j+1}$ ) is calculated using Equations 38 and 39 by multiplying the reaction rate term ( $RR_o$ ) with the oxidation factor ( $k$ ). It is important to note that the standard Arrhenius rate constant has been used in this model.

$$RR^i(t_{j+1}) = RR_o * k(\xi^i(t_{j+1})) \quad [38]$$

$$\text{where, } RR_o = A * e^{\left(\frac{-E_a}{R_u * T}\right)} * [NO_2] \quad [39]$$

where,  $RR_o$  is the reaction rate [1/s],  $A$  is the frequency factor or pre-exponential factor [1/K-ppm-s],  $E_a$  is the activation energy of the reaction [kJ/gmol],  $R_u$  is the universal gas constant = 8314 [kJ/gmol-K],  $T$  is temperature of the reaction [K] and  $[NO_2]$  is the concentration of  $NO_2$  in ppm.

After calculating the reaction rate at time  $t_{j+1}$ , the value of mass retained  $m_{retained}^i(t_{j+2})$  at time  $t_{j+2}$  is calculated using Equation 35 and the same process is repeated using Equations 36-39 for the consequent time steps for the lumped mass (i) till the end of experimental data available. The same process is followed for the lumped masses (i+1, i+2,...) entering the SCRF® at time ( $t_{j+1}, t_{j+2}, \dots$ ) till the end of experimental data available. The process of the model development and the equations used is illustrated graphically in Figure 4.4 for a better understanding.

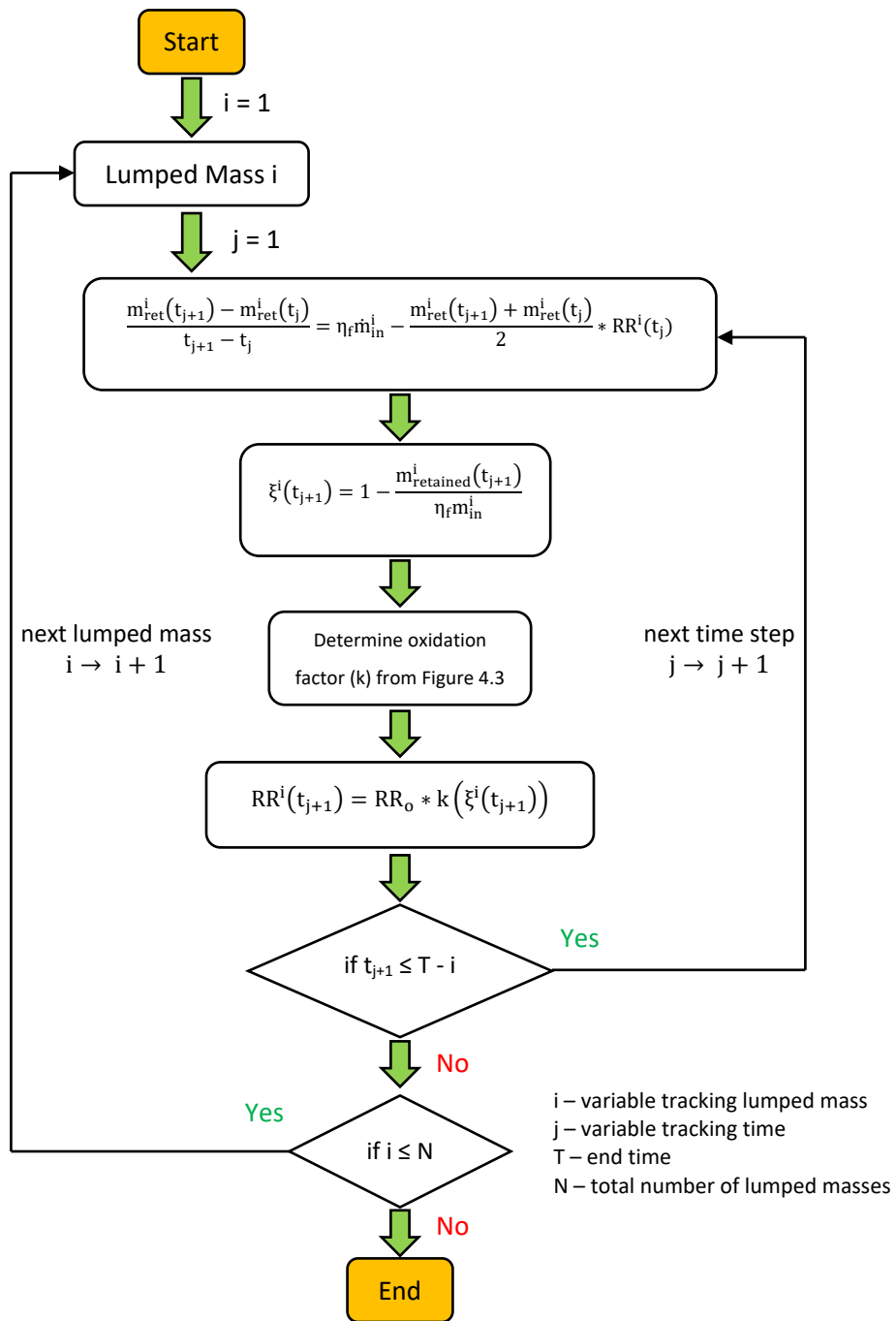


Figure 4.4: Schematic of the Model Developed for PM Oxidation

## 4.2 Application of the PM Oxidation Model's Reaction Rate Results in the SCR-F Model

This section focuses on the application of the reaction rate results from the PM oxidation model to the SCR-F model [12]. Further, the calibration of the SCR-F model with the experimental data from Loading Tests w/o Urea is discussed in the next section.

The PM oxidation model developed as discussed in Section 4.1 can simulate the PM retained in the SCR-F<sup>®</sup> with time. However, to estimate the amount of PM retained in the cake and wall, and the contribution of the cake, wall and channel to the total pressure drop across the SCR-F<sup>®</sup> as well as the evolution of filtration efficiency with time and PM loading, there is a need to integrate the calibrated PM oxidation model to the SCR-F model. This is performed by applying the reaction rate results from the PM oxidation model to the SCR-F model, specifically to simulate the pressure drop and estimate the Stage 1 filtration efficiency (Appendix A) for the Loading Tests, which is discussed in the following paragraphs.

In the PM Oxidation model, each lumped mass has an oxidation factor ( $k$ ) associated to it at each time step which is used in calculating the reaction rate for that lumped mass for the next time step. At each time step, a new term defined as the average oxidation factor ( $k_{avg}$ ) is calculated by taking the weighted average of oxidation factor ( $k$ ) of all lumped masses based on the quantity of PM in each lumped mass. The formula used to calculate the average oxidation factor ( $k_{avg}$ ) is shown in Equation 40.

$$k_{avg,t} = \frac{\sum_{i=1}^t (k_{i,t} * m_{retained,t}^i)}{\sum_{i=1}^t m_{retained,t}^i} \quad [40]$$

The average oxidation factor ( $k_{avg}$ ) calculated at each time-step from the PM Oxidation model is then applied to the reaction rate for the NO<sub>2</sub> assisted oxidation of PM in the cake and the substrate wall in the SCR-F model by modifying Equations 14 and 15 given in Section 2.5 as shown in Equation 41 and 42. The average oxidation factor ( $k_{avg}$ ) is interpolated based on the time step in the SCR-F model from the values calculated from the PM oxidation model and multiplied to the reaction rate for NO<sub>2</sub> assisted oxidation of PM in the cake and substrate wall.



$$RR_{NO_2, cake} = k_{avg} * \frac{s_p * \rho_{i,j} * Y_{i,j,NO_2} * A_{cake} * T_{i,j} * e^{\left(\frac{E_{a,NO_2}}{R_u * T_{i,j}}\right)} * W_C}{\alpha_{NO_2} W_{NO_2} \rho_s} \quad [41]$$

$$RR_{NO_2, wall} = k_{avg} * \frac{s_p * \rho_{i,j} * Y_{i,j,NO_2} * A_{wall} * T_{i,j} * e^{\left(\frac{E_{a,NO_2}}{R_u * T_{i,j}}\right)} * W_C}{\alpha_{NO_2} W_{NO_2} \rho_s} \quad [42]$$

where,  $s_p$  is the specific surface area of PM [1/m],  $\rho_{i,j}$  is the density of gas in each zone [kg/m<sup>3</sup>],  $Y_{i,j,NO_2}$  is the mass fraction of inlet NO<sub>2</sub> in each zone,  $A_{cake}$  is the pre-exponential for PM cake [m/K-s],  $A_{wall}$  is the pre-exponential for PM in the substrate wall [m/K-s],  $T_{i,j}$  is temperature of the filter in each zone [K],  $E_{a,NO_2}$  is the activation energy for NO<sub>2</sub> assisted PM oxidation [kJ/gmol],  $R_u$  is the universal gas constant [8.314 J/gmol-K],  $W_C$  is the molecular weight of carbon [kg/kmol],  $\alpha_{NO_2}$  is the NO<sub>2</sub> oxidation partial factor,  $W_{NO_2}$  is the molecular weight of NO<sub>2</sub> [kg/kmol] and  $\rho_s$  is the PM density [kg/m<sup>3</sup>].

### 4.3 Calibration of the SCR-F Model With Loading Tests w/o Urea Data

This section focuses on the calibration of the SCR-F model using experimental data from the eight Loading Tests w/o Urea performed in this study, after applying the reaction rate results from the PM Oxidation model to the SCR-F model as discussed in Section 4.2.

The objective of the calibration process is to determine the kinetics of PM oxidation in the cake and the wall to simulate the PM mass retained in the SCR-F<sup>®</sup> for the two loading stages within ± 2 g of the experimental values as well as to simulate the pressure drop across the SCR-F<sup>®</sup> within ±0.5 kPa of the experimental values. The input parameters and the calibration parameters for the SCR-F model are as follows.

#### Input Parameters:

1. Exhaust mass flow rate (kg/s)
2. SCR-F<sup>®</sup> inlet temperature (°C)

3. SCRF® inlet concentrations - NO (ppm), NO<sub>2</sub> (ppm), O<sub>2</sub> (%), CO (ppm), CO<sub>2</sub> (%), N<sub>2</sub> (ppm), HC (C<sub>12</sub>H<sub>24</sub>) (ppm) and PM concentration (mg/scm)
4. Ambient temperature (°C) and pressure (kPa)

**Calibration Parameters:**

1. PM oxidation kinetics (NO<sub>2</sub> assisted and thermal oxidation)
2. Pressure drop parameters
3. Filtration parameters
4. Cake permeability parameters
5. Thermal parameters
6. Gaseous species kinetics

The SCR-F model was already calibrated using experimental data from passive oxidation tests without urea from reference [8] as discussed in Section 2.5. The value of oxidation factor (*k*) w.r.t. percentage of PM oxidized ( $\xi$ ) in the PM oxidation model was also calibrated using experimental data from passive oxidation tests without urea from reference [8] which will be discussed in Section 4.4. Hence, for the calibration of the SCR-F model with the Loading Tests w/o Urea data, only the parameters related to PM oxidation kinetics had to be re-calibrated to take into account the changes due to varying reaction rates with time as a result of application of the PM oxidation model results to the SCR-F model.

The procedure followed for calibration and optimizing the output of the SCR-F model is explained in the following steps:

1. Initially, the value of activation energy (*E<sub>a</sub>*) and pre-exponential (*A*) obtained from the calibration of PM oxidation model with the passive oxidation data [8] which will be discussed in Section 4.4 were used for the NO<sub>2</sub> assisted oxidation kinetics of PM in the cake (*E<sub>a,NO2,cake</sub>* , *A<sub>NO2,cake</sub>*) and the wall (*E<sub>a,NO2,wall</sub>* , *A<sub>NO2,wall</sub>*) in the SCR-F model. The pre-exponential for the PM oxidation in the cake and the wall are then calibrated by comparing the simulated total PM retained with the experimental data and adding the cost function shown in Equation 43 for each of the eight Loading tests w/o Urea and minimizing the total cost.

$$Cost = \sum_{i=1}^2 (m_{retained,expt,i} - m_{retained,model,i})^2 \quad [43]$$

where, *i* stands for end of Stage 1 and Stage 2.

2. The pre-exponential for the PM oxidation in the wall ( $A_{NO_2,wall}$ ) is then calibrated by comparing the simulated total pressure drop across the SCR-F<sup>®</sup> and minimizing the total cost for all the eight Loading Tests w/o Urea. The cost functions for a single experiment is shown in Equation 44.

$$Cost = delP_{expt,i} - delP_{model,i} \quad [44]$$

where, i stands for end of Stage 2.

3. The pre-exponential for the PM oxidation in the cake ( $A_{NO_2,cake}$ ) is re-calibrated, to account for changes in the wall PM oxidation in step 2, by comparing the simulated total PM retained with the experimental data and minimizing the total cost for all the eight experiments as explained in Step 1.

The flow chart illustrating the process of calibration of the SCR-F model is shown in Figure 4.5.

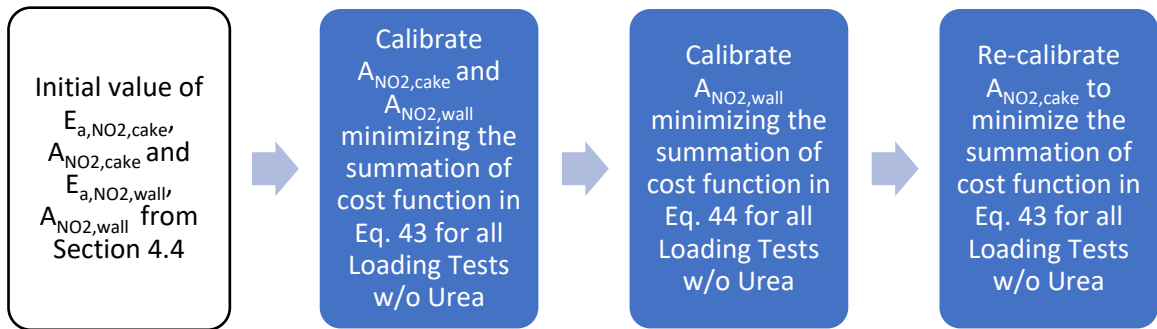


Figure 4.5: Flow Chart for the Calibration of SCR-F Model with Loading Tests w/o Urea Data

The kinetics of NO<sub>2</sub> assisted PM oxidation obtained after calibrating the SCR-F model using reaction rate results from the PM oxidation model, is given in Section 5.4. Also, the performance of the calibrated model and the analysis of the model data for the Loading Tests w/o Urea is discussed in detail in Section 5.4.

#### 4.4 Calibration of the PM Oxidation Model With Passive Oxidation w/o Urea Data

The PM oxidation model developed as discussed in Section 4.1 requires the parameters to be calibrated to simulate the kinetics of oxidation of diesel PM retained in the SCRF<sup>®</sup>. The calibration of the PM oxidation model using experimental data from the passive oxidation tests from reference [8] is discussed in detail in this section.

The passive oxidation tests [8] were designed to determine the NO<sub>2</sub> assisted oxidation kinetics of PM retained in the SCRF<sup>®</sup>. Each passive oxidation test consists of a loading Stage 1 (30 mins), Stage 2 (300 mins) and Ramp up (15 mins) followed by a passive oxidation stage and post-oxidation loading Stage 3 (30 mins) and Stage 4 (60 mins). Detailed description for each of these stages can be found in reference [8]. A plot of the loading profile of a passive oxidation test in terms of the pressure drop across the substrate is shown in Figure 4.6. The PM retained in the SCRF<sup>®</sup> at the end of each loading stage (represented by red dots in Figure 4.6) was calculated by measuring the weight of the SCRF<sup>®</sup> at the end of each loading stage and subtracting the clean weigh of the SCRF<sup>®</sup> without any PM loading which is discussed in detail in reference [8].

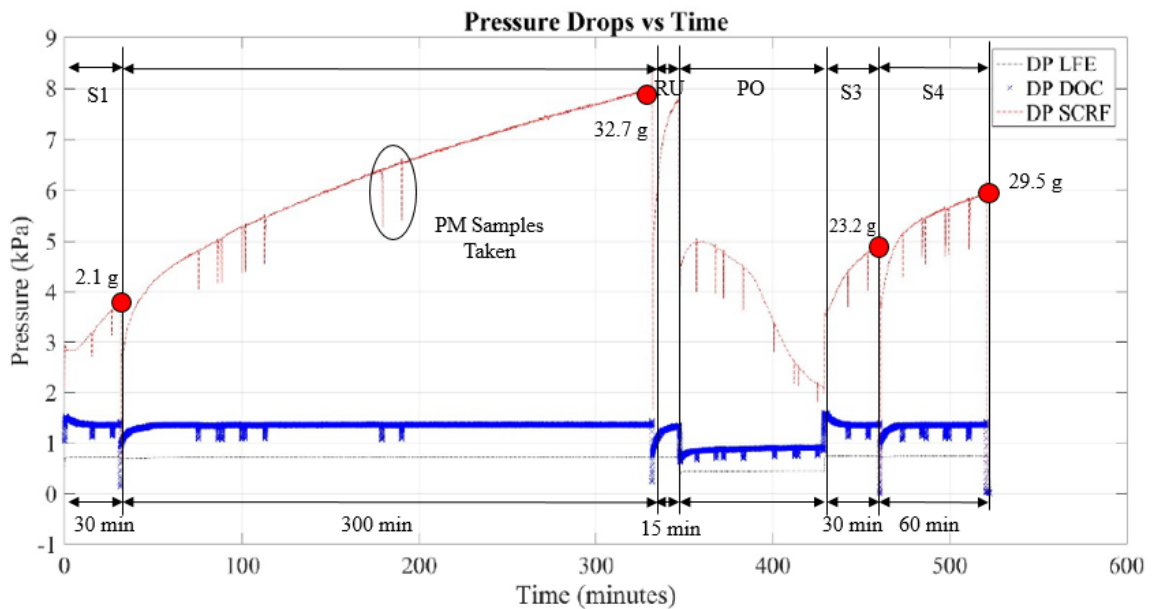


Figure 4.6: Pressure Drop vs Time for a Passive Oxidation Test PO-C [8]

The objective of this calibration process is to determine a single set of kinetics of PM oxidation to simulate the PM mass retained in the SCRF® for all the stages in the passive oxidation test within  $\pm 2$  g of the experimental values of PM retained at the end of the stages. The parameters used as inputs for the model and the parameters calibrated using experimental data are as follows.

**Input Parameters:**

1. Exhaust mass flow rate (kg/s)
2. SCRF® Inlet NO<sub>2</sub> concentration (ppm)
3. SCRF® Inlet temperature (K)
4. SCRF® Inlet PM concentration (g/scm)
5. SCRF® Filtration efficiency (-)
6. Duration of the experiment (minutes)

**Calibration Parameters:**

1. NO<sub>2</sub> Assisted PM Oxidation Kinetics (Activation Energy E<sub>a</sub> and Pre-exponential A)
2. Oxidation Factor (k)

For the calibration, initial values of activation energy (E<sub>a</sub>) and pre-exponential (A) are obtained from the Arrhenius plot of experimental reaction rates from reference [8]. Also, the same values of oxidation factor (k) w.r.t percentage of PM oxidized from reference [23] shown in Figure 4.3 are used for the initial calibration. The procedure followed for calibrating the parameters and optimizing the output of the model is explained in the following steps.

- 1) The NO<sub>2</sub> assisted PM oxidation kinetics are calibrated assuming different set of kinetics in the loading stages (E<sub>a</sub>, A<sub>loading</sub>) and passive oxidation stage (E<sub>a</sub>, A<sub>PO</sub>). This is done by maintaining the absolute difference (Equation 45) between the model PM retained and the experimental PM retained at the end of the Stage 1, 2 and 3 within  $\pm 2$  g for a single set of kinetics for the loading stages for all experiments and a single set of kinetics for passive oxidation stage for all experiments.

$$Difference_i = |m_{retained,expt,i} - m_{retained,model,i}| \quad [45]$$

where, i stands for end of stage 1, 2 or 3

2) In this step, the values of oxidation factor ( $k$ ) for the initial portion of the PM oxidized i.e. for  $\xi < 0.25$  are calibrated manually to obtain the same kinetics ( $E_a$  and  $A$ ) for the loading stages and the passive oxidation stage. The comparison of the calibrated value of oxidation factor ( $k$ ) w.r.t percentage of PM oxidized ( $\xi$ ) and that used initially from the reference [23] is shown in Figure 4.7. The calibrated value of oxidation factor ( $k$ ) w.r.t. percentage of PM oxidized ( $\xi$ ) is fitted with a sixth order polynomial shown in Equation 46 and is used in the model for further calibration in Step 3.

$$k = 1256.7\xi^6 - 4518.2\xi^5 + 6584.6\xi^4 - 4944.9\xi^3 + 2003.6\xi^2 - 411.82\xi + 33.995 \quad [46]$$

3) The pre-exponential ( $A$ ) is again re-calibrated, with the same value of activation energy ( $E_a$ ) from Step 1, to account for changes in the loading stages and passive oxidation stage due to calibration of the oxidation factor ( $k$ ). The cost function shown in Equation 47 for a single experiment is added for all experiments and the total cost is minimized while calibrating the value of pre-exponential ( $A$ ).

$$Cost = \sum_{i=1}^3 (m_{retained,expt,i} - m_{retained,model,i})^2 \quad [47]$$

where,  $i$  stands for end of stage 1, 2 or 3

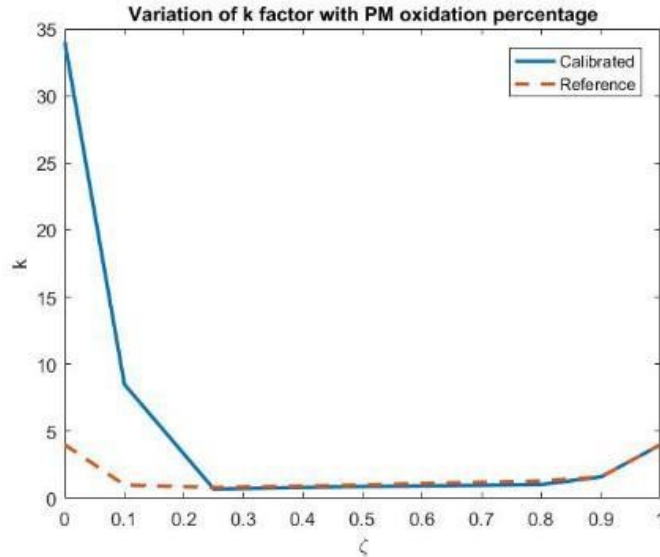


Figure 4.7: Comparison of Calibrated Oxidation Factor ( $k$ ) w.r.t Percentage of PM Oxidized With That Used Initially From Reference [23]

The flow chart illustrating the process of calibration of the PM Oxidation model is shown in Figure 4.8.

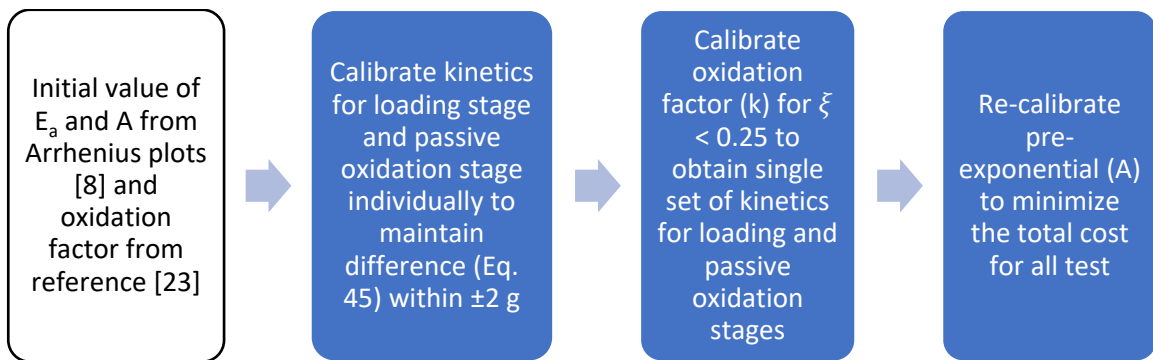


Figure 4.8: Flow Chart for the Calibration Process

The kinetics obtained after calibrating the model and the performance of the calibrated model is discussed in detail in Section 5.5.

## Chapter 5. Results and Discussion

This chapter focuses on the results and analysis of the experimental data and the modeling work carried out. Section 5.1 discusses the data and results for the Loading Tests w/o Urea in terms of the PM loading and oxidation performance of the SCRF<sup>®</sup>. This is followed by Section 5.2 which focuses on the results for the Loading Tests w/ Urea in terms of the PM loading, oxidation performance and NO<sub>x</sub> reduction performance of the SCRF<sup>®</sup>. In Section 5.3, the results for the Loading Tests w/o and w/ Urea are compared in terms of the kinetics of NO<sub>2</sub> assisted oxidation of PM retained and the pressure drop across the SCRF<sup>®</sup>. Also, there is a discussion on the comparison of the kinetics of NO<sub>2</sub> assisted PM oxidation in the SCRF<sup>®</sup> under loading and passive oxidation conditions which was the primary objective for performing the Loading Tests as discussed in Section 2.4. Further, the performance of the calibrated SCR-F model with the reaction rate results from the PM oxidation model for the loading without urea data, is discussed in Section 5.4. At the end of the chapter, there is a discussion of the performance of the PM oxidation model under loading and passive oxidation conditions for a single set of kinetics.

### 5.1 Loading Tests w/o Urea

As discussed in Chapter 3, the Loading Tests were designed to determine the NO<sub>2</sub> assisted oxidation kinetics for PM retained in the SCRF<sup>®</sup> for different loading conditions and to characterize the differences in the reaction kinetics of PM under loading and passive oxidation conditions. Also, the Loading Tests w/ Urea were designed to determine the effect of urea on NO<sub>2</sub> assisted PM oxidation kinetics as well as to understand the interaction of PM oxidation and NO<sub>x</sub> reduction with urea injection for the loading conditions.

Eight Loading Tests w/o Urea and four Loading Tests w/ Urea were performed with each test consisting of two stages of loading – Stage 1 and Stage 2. The data and the results for the Loading Tests w/o Urea performed are discussed in detail in this section. The variables changed when comparing one Loading Test to another are the engine speed, engine load and fuel rail pressure which results in changing the SCRF<sup>®</sup> inlet temperature and the PM and NO<sub>2</sub> concentrations.

To introduce the data for the Loading Tests w/o Urea, the important engine and exhaust conditions for Stage 2 Loading for each test are given in Table 5.1. There may be slight differences between the values in Table 5.1 compared to the test matrix in Section 3.7 as these are the actual



values obtained during the tests as contrasted to the values obtained from the point validation tests. It is important to note that the all the test conditions given in Table 5.1 lie in the region in which 90% of the PM oxidation is NO<sub>2</sub> assisted as discussed in Section 3.7 and that there is a significant variation in the reaction rate for PM oxidation. Therefore, for the analysis of data, an assumption was made that the PM oxidation was completely NO<sub>2</sub> assisted while calculating the kinetics of PM oxidation discussed later in this section.

Table 5.1: Engine and Exhaust Conditions for Stage 2 in Loading Tests w/o Urea

Test	FRP	Speed	Load	Exhaust Flow Rate	Std. Space Velocity	PM Conc.	DOC Inlet Temp.	SCRF <sup>®</sup> Inlet Temp.
[-]	[Bar]	[RPM]	[Nm]	[kg/min]	[k/hr]	[mg/scm]	[°C]	[°C]
<b>L1-Nominal</b>	1507	2401	203	10.9	33	7.1	273	264
<b>L1-Reduced<sup>#</sup></b>	1050	2400	203	11.2	33	11.7	278	275
<b>L2-Nominal</b>	1560	2400	271	11.4	34	6.6	300	287
<b>L2-Reduced</b>	1092	2400	271	11.5	34	11.7	302	298
<b>L3-Nominal</b>	1575	2400	339	11.9	36	5.7	324	330
<b>L3-Reduced</b>	1103	2400	339	12.0	36	11.0	337	332
<b>L4-Nominal</b>	1610	2400	406	12.5	37	5.7	353	354
<b>L4-Reduced</b>	1127	2400	406	12.5	37	10.9	369	364

<sup>#</sup>Data obtained from Test PO-C in reference [11]

The NO, NO<sub>2</sub> and NO<sub>x</sub> values at the DOC inlet and SCRFR<sup>®</sup> inlet for each test are given in Table 5.2. Theoretically, NO<sub>x</sub> should be conserved across the DOC and the SCRFR<sup>®</sup> when there is no urea injection into the system. However, as observed from Table 5.2, there is slight variation in the NO<sub>x</sub> values at the DOC inlet and SCRFR<sup>®</sup> inlet for each test. The reason for this can be attributed to the minor leakages in the aftertreatment system or the sampling system or measurement error. Also, since the UDOC, USCRF and DSCRFR samples are taken at different time intervals one after the other during the tests, there may be small discrepancies in the conservation of species. To ensure

the difference in total NO<sub>x</sub> across the DOC remained within an acceptable margin of error (<10%), the percentage difference from the inlet concentrations is calculated using Equation 48 and the data are shown in Table 5.2. Also, the NO<sub>x</sub> values at the DOC inlet and SCR<sup>F</sup>® inlet for Loading Tests without Urea shown in Table 5.2 should be theoretically equal since it is assumed there are no reactions occurring in the decomposition tube between the DOC outlet and SCR<sup>F</sup>® inlet.

$$NO_x \text{ Difference (\%)} = \frac{NO_{x,in} - NO_{x,out}}{NO_{x,in}} * 100 \quad [48]$$

Table 5.2: Emission Data Across DOC for Loading Tests w/o Urea

Test	DOC Inlet Temp.	DOC Inlet			DOC NO Conv.	SCR <sup>F</sup> ® Inlet			NO <sub>x</sub> Diff.
		NO <sub>2</sub>	NO	NO <sub>x</sub>		NO <sub>2</sub>	NO	NO <sub>x</sub>	
	[°C]	[ppm]	[ppm]	[ppm]	[%]	[ppm]	[ppm]	[ppm]	[%]
<b>L1 Nominal</b>	277	30	186	216	10	62	167	229	-6
<b>L1 Reduced<sup>#</sup></b>	278	26	162	188	20	59	129	188	0
<b>L2 Nominal</b>	300	29	261	290	22	88	203	291	0
<b>L2 Reduced</b>	302	22	193	215	24	61	147	208	3
<b>L3 Nominal</b>	324	24	315	339	28	93	227	320	6
<b>L3 Reduced</b>	337	0	191	192	26	52	142	194	-1
<b>L4 Nominal</b>	353	15	333	348	31	120	230	350	-1
<b>L4 Reduced</b>	369	7	250	257	32	82	169	251	2

<sup>#</sup>Data obtained from Test PO-C in reference [11]

The percentage of NO conversion across the DOC is also calculated using Equation 49 for each test and the NO conversion percentage are given in Table 5.2. For this calculation, the NO values at the DOC outlet have been assumed equal to the NO values at the SCR<sup>F</sup>® inlet since it is assumed there are no reactions occurring in the decomposition tube between the DOC outlet and SCR<sup>F</sup>® inlet.

$$NO \text{ Conversion (\%)} = \frac{NO_{in} - NO_{out}}{NO_{in}} \quad [46]$$

where, the DOC inlet and outlet NO concentration are in ppm.

The NO conversion across the DOC is plotted against the DOC inlet temperature as shown in Figure 5.1. The trend for NO conversion across the DOC is in agreement with that observed in the literature. However, the value of NO conversion observed for test L1 Nominal and L1 Reduced is relatively low ( $\leq 20\%$ ) when compared to the other Loading Tests. Hence, to check proper functioning of the DOC in converting NO to NO<sub>2</sub>, another validation test was performed which is described in detail in Appendix B.

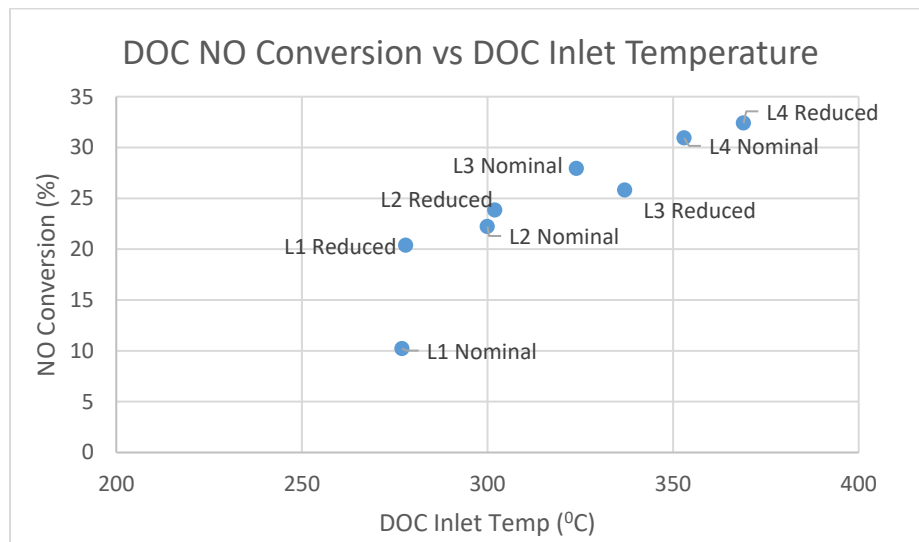


Figure 5.1: NO Conversion Across DOC vs DOC Inlet Temperature for Loading Tests w/o Urea

Next, the NO, NO<sub>2</sub> and NO<sub>x</sub> values at the SCR<sup>®</sup> outlet for each test are given in Table 5.3 along with the NO, NO<sub>2</sub> and NO<sub>x</sub> values at the SCR<sup>®</sup> inlet from Table 5.2 for comparison. As observed from Table 5.3, the NO<sub>2</sub> value decreases across the SCR<sup>®</sup> and the NO value increases across the SCR<sup>®</sup> as NO<sub>2</sub> is converted to NO while oxidizing the PM retained in the SCR<sup>®</sup>. The percentage difference in the NO<sub>x</sub> values at the inlet and outlet of the SCR<sup>®</sup> was calculated using Equation 48 to ensure conservation of mass in terms of NO<sub>x</sub> across the SCR<sup>®</sup>. The percentage difference in the NO<sub>x</sub> values at the inlet and outlet of the SCR<sup>®</sup> for each test was within the acceptable range (<10%) as seen in Table 5.3.

Table 5.3: Emission Data Across SCRF® for Loading Tests w/o Urea

Test	SCRF® Inlet Temp.	SCRF® Inlet			SCRF® Outlet			NO <sub>x</sub> Difference
		NO <sub>2</sub>	NO	NO <sub>x</sub>	NO <sub>2</sub>	NO	NO <sub>x</sub>	
	[°C]	[ppm]	[ppm]	[ppm]	[ppm]	[ppm]	[ppm]	[%]
<b>L1 Nominal</b>	264	62	167	229	45	171	216	6
<b>L1 Reduced<sup>#</sup></b>	275	59	129	188	33	150	183	3
<b>L2 Nominal</b>	287	88	203	291	68	207	275	5
<b>L2 Reduced</b>	298	61	147	208	37	155	193	7
<b>L3 Nominal</b>	330	93	227	320	72	256	329	-3
<b>L3 Reduced</b>	332	52	142	194	36	143	179	8
<b>L4 Nominal</b>	354	120	230	350	94	248	342	2
<b>L4 Reduced</b>	364	82	169	251	57	195	253	-1

<sup>#</sup>Data obtained from Test PO-C in reference [11]

Further, to validate the NO<sub>x</sub> values from Mass Spectrometer (MS) shown in Table 5.2 and Table 5.3, they were compared to the NO<sub>x</sub> values from the Calterm. The comparison of NO<sub>x</sub> values at UDOC and USCRF® from the MS and the Calterm for all the tests is shown in Figure 5.2 and 5.3 respectively. The NO<sub>x</sub> value at UDOC and USCRF® from the MS and the Calterm seem to be in agreement for all the tests except the test L3 Reduced which is the outlier point as observed from Figure 5.2 and 5.3. For test L3 Reduced, the NO<sub>x</sub> value at UDOC and USCRF® from the MS is lower compared to that from Calterm. The NO<sub>x</sub> value at UDOC and USCRF® from MS seems incorrect as the value from Calterm agrees with the values obtained during the point validation tests (Table 3.15). The incorrect reading from the MS might be due to the filter getting plugged in the heated filter during the test and thus giving incorrect NO<sub>x</sub> values. The emission data from Calterm for test L3 Reduced was used for further analysis.

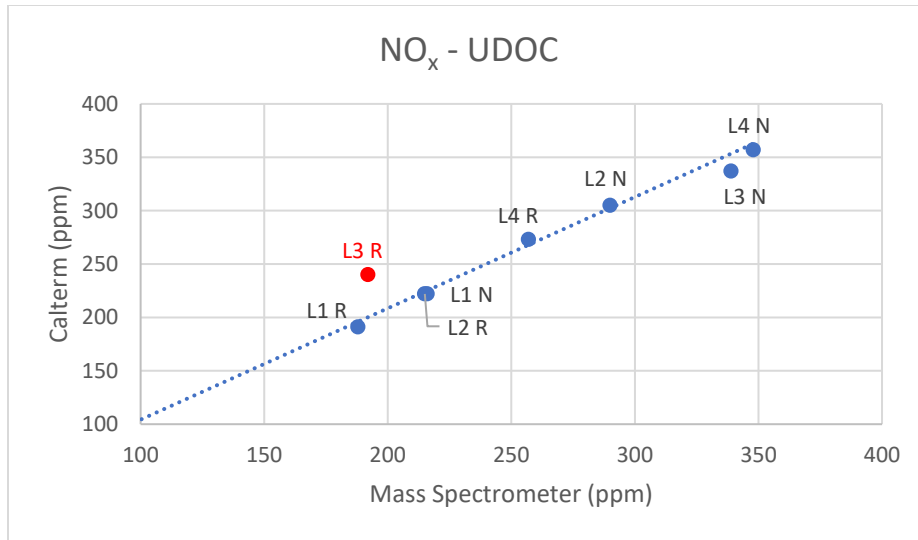


Figure 5.2: Comparison of NO<sub>x</sub> Data From Calterm and Mass Spectrometer at UDOC

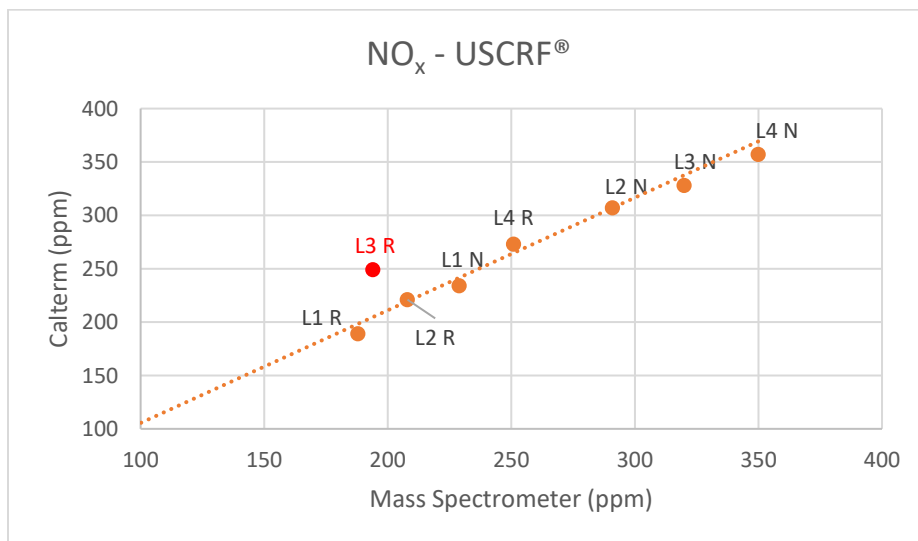


Figure 5.3: Comparison of NO<sub>x</sub> Data From Calterm and Mass Spectrometer at USCRF®

Similarly, the NO<sub>x</sub> values at DSCR® from the MS is compared to that from Calterm for all the tests as shown in Figure 5.4. Tests L3 Reduced and L4 Nominal are observed to be the outlier points. For L3 Reduced, the NO<sub>x</sub> value at DSCR® from Calterm agrees with the value obtained during the point validation test (Table 3.15) and so Calterm value was used for further analysis. However, for test L4 Nominal, the NO<sub>x</sub> value from Mass Spectrometer agrees with the value obtained during the point validation test and so the Calterm value was assumed incorrect.

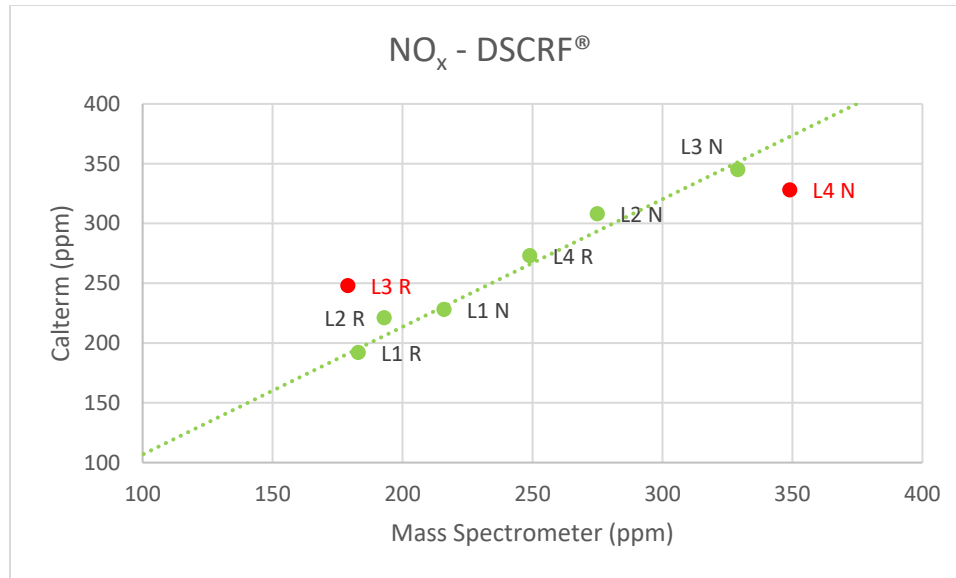


Figure 5.4: Comparison of NO<sub>x</sub> Data From Calterm and Mass Spectrometer at DSCR®

The PM mass balance for Stage 1 and Stage 2 for these tests is shown in Table 5.4 and Table 5.5 respectively. The factors that affect PM loaded into the SCR® are exhaust flowrate, fuel rail pressure, SCR® inlet temperature and NO<sub>2</sub> concentrations into the SCR®. An increase in NO<sub>2</sub> and/or temperature results in a higher amount of PM oxidized and will affect the amount of PM retained in the SCR®. The parameters given in Table 5.4 and Table 5.5 are calculated using formulae discussed in Section 3.9. The calculation of the clean weight of the SCR® is discussed in detail in Appendix A. The filtration efficiency during Stage 1 was not measured physically but was estimated based on results from the calibrated SCR-F model which is also discussed in detail in Appendix A.

During the test L3 Nominal, an active regeneration event was started by the ECU on its own during the last hour of Stage 2 as the manual control of the in-cylinder fuel dosing late into the combustion cycle was not enabled. However, the active regeneration was stopped midway, but still the values highlighted in Table 5.4 and Table 5.5 for L3 Nominal cannot be compared to other tests as the actual PM retained would be slightly higher and PM oxidized would be slightly lower than the values shown in the Table 5.4 and Table 5.5.

Table 5.4: PM Balance for Stage 1 for Loading Tests w/o Urea

Test	PM Conc.	PM <sub>in</sub>	Filtration Efficiency**	PM <sub>out</sub>	PM <sub>start</sub>	PM <sub>retained</sub>	PM <sub>oxidized</sub>	PM <sub>oxidized</sub>
	[mg/scm]	[g]	[%]	[g]	[g]	[g]	[g]	[%]
L1 Nominal	7.2	1.96	61.6	0.75	0	1.14	0.06	3.3
L1 Reduced <sup>#</sup>	11.6	3.57	66.3	1.20	0	2.04	0.33	9.2
L2 Nominal	6.4	1.86	59.8	0.75	0	0.76	0.35	18.8
L2 Reduced	11.7	3.44	64.3	1.23	0	2.06	0.15	4.5
L3 Nominal	5.7	1.77	57.0	0.76	0	0.55*	0.46*	26.1*
L3 Reduced	11.3	3.61	61.9	1.38	0	1.72	0.52	14.4
L4 Nominal	5.5	1.76	55.4	0.78	0	0.77	0.20	11.5
L4 Reduced	11.0	3.57	59.6	1.44	0	1.47	0.65	18.3

<sup>#</sup>Data obtained from Test PO-C in reference [11]

\*Cannot compare with other tests due to unexpected active regeneration in Stage 2

\*\*Average filtration efficiency estimated using calibrated SCR-F model discussed in Appendix A

Table 5.5: PM Balance for Stage 2 for Loading Tests w/o Urea

Test	PM Conc.	PM <sub>in</sub>	Filtration Efficiency	PM <sub>out</sub>	PM <sub>start</sub>	PM <sub>retained</sub>	PM <sub>oxidized</sub>	PM <sub>oxidized</sub>
	[mg/scm]	[g]	[%]	[g]	[g]	[g]	[g]	[%]
L1 Nominal	7.1	19.7	97.5	0.50	1.14	16.1	4.22	20.3
L1 Reduced <sup>#</sup>	11.7	33.4	98.4	0.53	2.04	25.4	9.47	26.7
L2 Nominal	6.6	19.2	96.7	0.63	0.76	11.5	7.87	39.4
L2 Reduced	11.7	34.3	97.2	0.95	2.06	26.8	8.62	23.7
L3 Nominal	5.7	16.8	97.0	0.50	0.55*	7.7*	9.21*	53.0*
L3 Reduced	11.0	33.7	97.1	0.98	1.72	20.1	14.3	40.4
L4 Nominal	5.7	18.3	96.0	0.74	0.77	8.5	9.86	51.6
L4 Reduced	10.9	34.8	97.3	0.94	1.47	15.0	20.30	58.4

<sup>#</sup>Data obtained from Test PO-C in reference [11]

\*Cannot compare with other tests due to unexpected active regeneration in Stage 2

The cumulative PM mass balance at the end of Stage 2 for all the tests is illustrated graphically in Figures 5.5 and 5.6. It is observed that the percentage of PM oxidized increases with increase in engine load. This is because at higher engine load, the SCR<sup>®</sup> temperature and NO<sub>2</sub> concentrations are higher compared to the values at lower engine load. The PM oxidized percentage increases while moving from L1 Nominal to L4 Nominal or L1 Reduced to L4 Reduced except for L3 Nominal and L1 Reduced. For L3 Nominal, the actual PM oxidized should have been lower and PM retained higher because of an unexpected active regeneration event as discussed before. For L1 Reduced, there is a possibility that the Stage 2 filtration efficiency (98.4%) is higher than the filtration efficiency for other tests because of which the percentage of PM out is lower compared to other tests as seen in Figure 5.5. A decreasing trend in the percentage of PM mass retained is observed as we move from L1 Nominal to L4 Nominal or L1 Reduced to L4 Reduced except L3 Nominal and L1 Reduced. Difference in percentage of PM oxidized or PM retained while comparing tests at nominal and reduced fuel rail pressure is due to major difference in the PM concentrations and minor differences in the SCR<sup>®</sup> temperature and NO<sub>2</sub> concentrations.

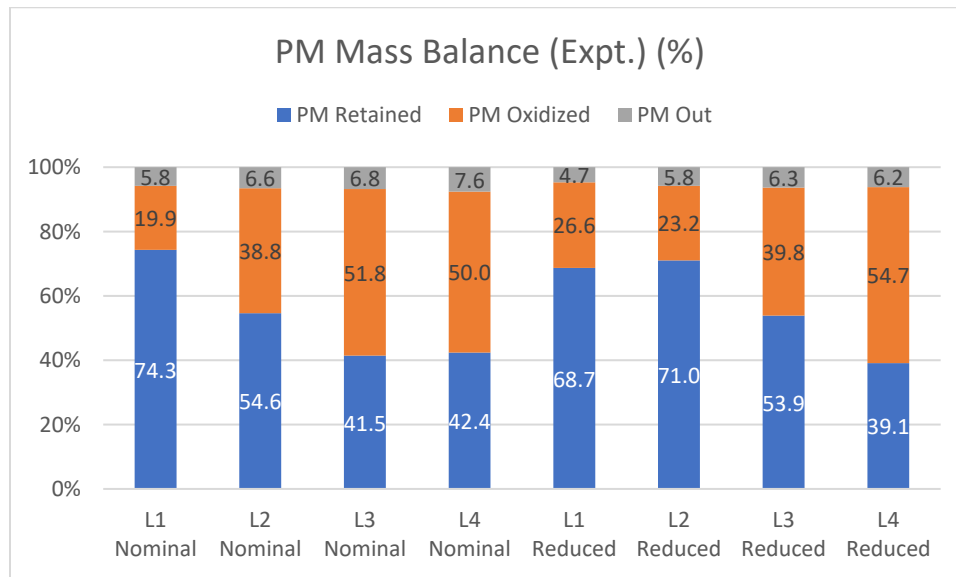


Figure 5.5: PM Mass Balance as Percentage of PM In (Expt.) for Loading Tests w/o Urea

As discussed earlier, the primary objective of the Loading Tests was to determine the NO<sub>2</sub> assisted oxidation kinetics for PM retained in the SCR<sup>®</sup> for different loading conditions and to characterize the differences in the reaction kinetics in loading and passive oxidation conditions. The average reaction rate for NO<sub>2</sub> assisted PM oxidation during Stage 2 is calculated as explained in Section



3.10 for all the tests and is given in Table 5.6. It is important to note that the reaction rate depends on the SCR<sup>®</sup> temperature, NO<sub>2</sub> concentrations and the duration and so these values are also given in Table 5.6. The reaction rate constant (k) calculated by normalizing the average reaction rate by the NO<sub>2</sub> concentration is also given in Table 5.6.

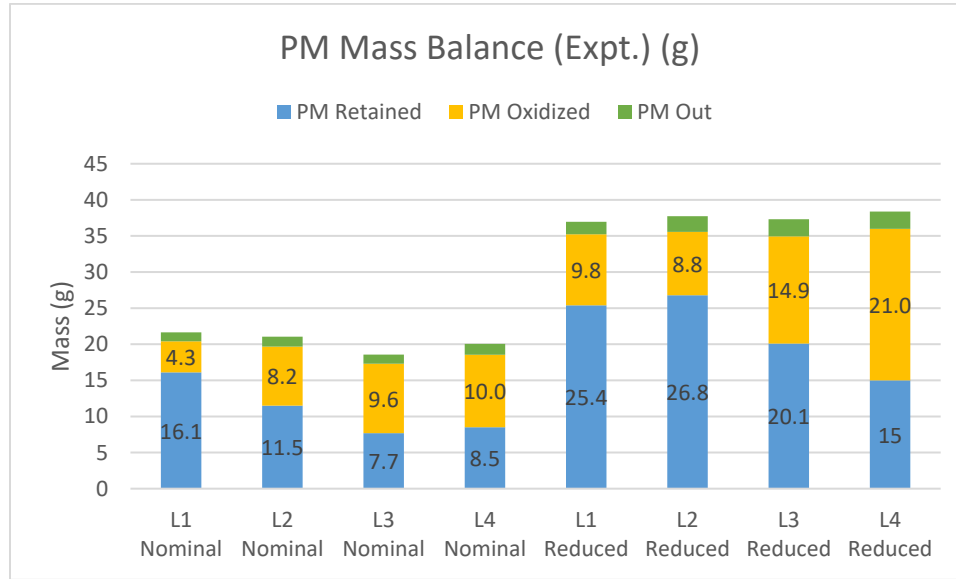


Figure 5.6: PM Mass Balance (Expt.) for Loading Tests w/o Urea

Table 5.6: Variables to Compare Kinetics of NO<sub>2</sub> Assisted PM Oxidation Without Urea

Test	Expt. Reaction Rate (RR <sub>0</sub> )	Stage 2 Duration	SCR <sup>®</sup> Inlet Temp	NO <sub>2</sub> into SCR <sup>®</sup>	PM Retained	PM Oxidized	k = RR <sub>0</sub> /NO <sub>2</sub>
[-]	[1/s]	[min]	[°C]	[ppm]	[g]	[%]	[10 <sup>6</sup> /ppm/s]
<b>L1 Nominal</b>	2.53E-05	299	264	62	16.1	20.3	0.405
<b>L1 Reduced<sup>#</sup></b>	3.50E-05	300	275	59	25.4	26.7	0.592
<b>L2 Nominal</b>	6.11E-05	300	287	88	11.5	39.4	0.694
<b>L2 Reduced</b>	3.07E-05	299	298	61	26.8	23.7	0.505
<b>L3 Nominal</b>	-	300	330	93	7.7*	53.0*	-
<b>L3 Reduced</b>	6.24E-05	302	332	80	20.1	40.4	0.780
<b>L4 Nominal</b>	9.51E-05	300	352	120	8.5	51.6	0.793
<b>L4 Reduced</b>	1.08E-04	302	364	82	15.0	58.4	1.320

<sup>#</sup>Data obtained from Test PO-C in reference [11]

\*Cannot compare with other tests due to unexpected active regeneration in Stage 2

The natural log of reaction rate constant ( $k$ ) from Table 5.6 is plotted against the inverse of SCRF<sup>®</sup> inlet temperature for all the tests and is shown in Figure 5.7. The variation of  $k$  with the inverse of SCRF<sup>®</sup> average temperature determined from the experimental data from passive oxidation tests w/o Urea [8] is also plotted in Figure 5.7 for comparison. As observed from Figure 5.7, the reaction rate kinetics for NO<sub>2</sub> assisted PM oxidation during loading is higher compared to that during passive oxidation. A similar trend was also reported in reference [4] and reference [8] for PM oxidation in a CPF and a SCRF<sup>®</sup> respectively as discussed in Section 2.4. Also, the average reaction rate and reaction rate constant is higher for tests at higher engine load compared to tests at lower engine load. The average reaction rate for L3 Nominal was not calculated as the value of PM retained and PM oxidized computed is not consistent due to an unexpected active regeneration in Stage 2 as explained earlier.

A standard Arrhenius model is used to fit the passive oxidation data from reference [8] which results in a line with slope and y intercept which corresponds to activation energy ( $E_a$ ) and pre-exponential ( $A$ ) respectively. The value of activation energy obtained is the minimum energy required for the oxidation of PM with NO<sub>2</sub>. The pre-exponential factor relates to how likely two or more molecules collide in the right orientation for the reaction to occur. The line of best fit for determining  $E_a$  and  $A$  for the passive oxidation data is plotted in Figure 5.7.

It is important to note that it is not possible to fit the data for Loading Tests w/o Urea using a standard Arrhenius model as observed from Figure 5.7. Hence, a model for PM oxidation was developed in this study to simulate the reaction kinetics during loading and passive oxidation conditions for a single set of kinetics. The development of this model is discussed in detail in Section 4.1 along with its application to the SCR-F model in Section 4.2. The performance of the SCR-F model with reaction rate results from PM oxidation model for the Loading Tests w/o Urea is discussed in detail in Section 5.4. The PM oxidation model is able to simulate the reaction kinetics during passive oxidation conditions along with the loading conditions for a single set of kinetics and the results will be discussed in Section 5.5.

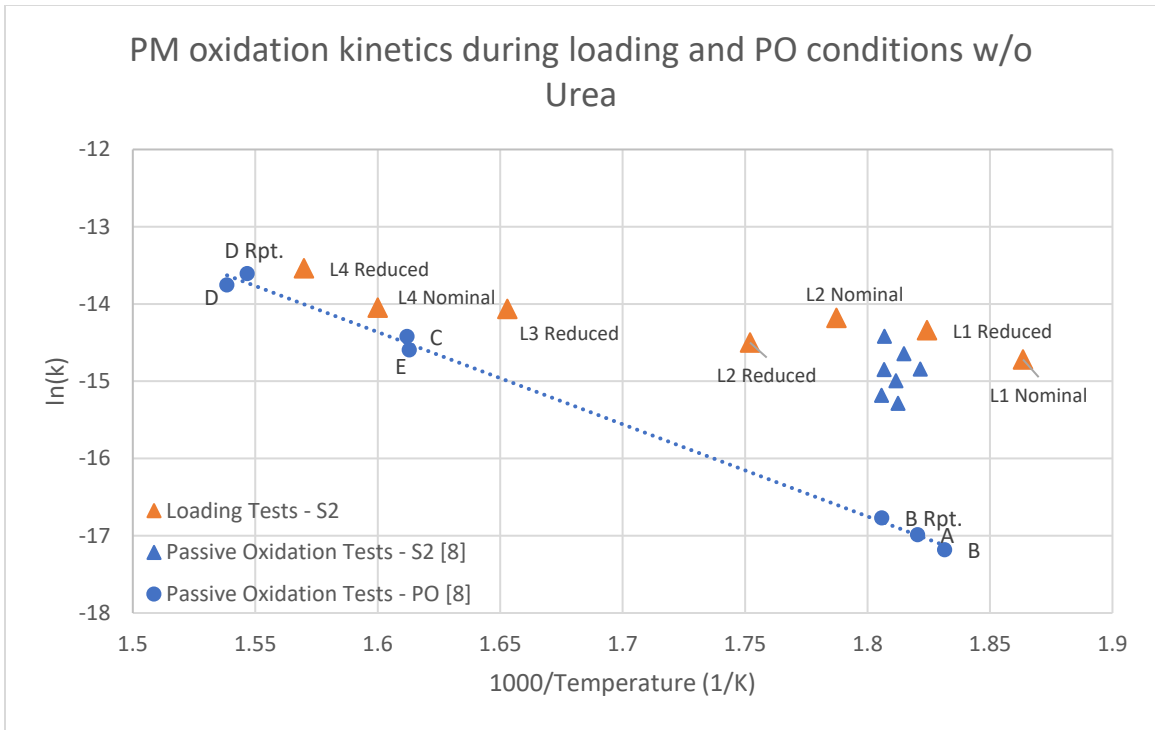


Figure 5.7: Comparison of PM Oxidation Kinetics for Passive Oxidation [8] and Loading Conditions w/o Urea in SCRF®

## 5.2 Loading Tests w/ Urea

The results for the Loading Tests w/ Urea will be presented in a similar fashion to the Loading Tests w/o Urea. Since the focus of this thesis is to compare and characterize the difference in reaction kinetics under loading and passive oxidation conditions, it is important to study kinetics of PM oxidation in loading conditions with urea so that the difference in kinetics with urea injection can be quantified. As discussed earlier, all the Loading Test w/ Urea were performed at a target ANR of 1.0. The actual ANR will be discussed later in this section. To introduce the results for the Loading Tests w/ Urea, the engine and exhaust conditions for Stage 2 for each test are given in Table 5.7.

Table 5.7: Engine and Exhaust Conditions for Stage 2 in Loading Tests w/ Urea

Test	FRP	Speed	Load	Exhaust Flow Rate	Std. Space Velocity	PM Conc.	DOC Inlet Temp.	SCR <sup>F</sup> ® Inlet Temp.	ANR
[-]	[Bar]	[RPM]	[Nm]	[kg/min]	[k/hr]	[mg/scm]	[°C]	[°C]	[-]
L1-Nom w/ Urea	1513	2399	200	10.9	33	7.2	273	268	1.00
L1-Red w/ Urea	1050	2404	203	11.0	33	14.1	287	283	0.98
L3-Nom w/ Urea	1593	2399	340	12.1	36	6.9	328	321	1.09
L3-Red w/ Urea	1103	2402	340	12.1	36	11.3	347	334	1.01

It is important to note that the injection of urea should not have any effect on the engine and exhaust conditions given in Table 5.7. The difference between the values in Table 5.7 and 5.1 for the same test conditions are due to minor day to day variations in the performance of the engine. The major difference observed is in the PM concentrations for these tests with and without urea.

The NO, NO<sub>2</sub> and NO<sub>x</sub> values at the DOC inlet and SCR<sup>F</sup>® inlet for each Loading Test w/ Urea are given in Table 5.8. Theoretically, NO<sub>x</sub> should be conserved across the DOC and NO<sub>x</sub> is reduced across the SCR<sup>F</sup>® when there is urea injection into the system. However, as observed from Table 5.8, there is slight variation in the NO<sub>x</sub> values at the DOC inlet and SCR<sup>F</sup>® inlet for each test. The conservation of mass in terms of NO<sub>x</sub> was checked again using Equation 48 with the maximum difference of 4% which is within an acceptable margin of error (<10%). The reason for this difference in the NO<sub>x</sub> values has been discussed earlier for Loading Tests w/o Urea. Also, there is

variation in the NO<sub>x</sub> values at the DOC inlet and SCRF<sup>®</sup> inlet when comparing one Loading Test w/o Urea (Table 5.2) to the Loading Test w/ Urea (Table 5.8). This difference might be due to the day to day variation in calibration process of the Mass Spectrometer.

Table 5.8: Emission Data Across DOC for Loading Tests w/ Urea

Test	DOC Inlet Temp.	DOC Inlet			NO Conv.	SCRF <sup>®</sup> Inlet			NO <sub>x</sub> Diff.
		NO <sub>2</sub>	NO	NO <sub>x</sub>		NO <sub>2</sub>	NO	NO <sub>x</sub>	
	[°C]	[ppm]	[ppm]	[ppm]	[%]	[ppm]	[ppm]	[ppm]	[%]
L1 Nominal w/ Urea	272	21	161	182	11	41	143	184	-1
L1 Reduced w/ Urea	287	23	142	165	15	45	121	166	-1
L3 Nominal w/ Urea	328	16	293	309	32	98	200	298	4
L3 Reduced w/ Urea	347	12	245	257	29	76	174	250	3

The percentage of NO conversion across the DOC is also calculated for these tests using Equation 49, the values of which are given in Table 5.8. Again, it is assumed that there are no reactions occurring in the decomposition tube between the DOC outlet and SCRF<sup>®</sup> inlet and so NO values at the DOC outlet are equal to the NO values at the SCRF<sup>®</sup> inlet. The NO<sub>x</sub> reduction reactions occur only in the SCRF<sup>®</sup> and not in the decomposition tube. The NO conversion across the DOC is plotted against the DOC inlet temperature and is shown in Figure 5.8.

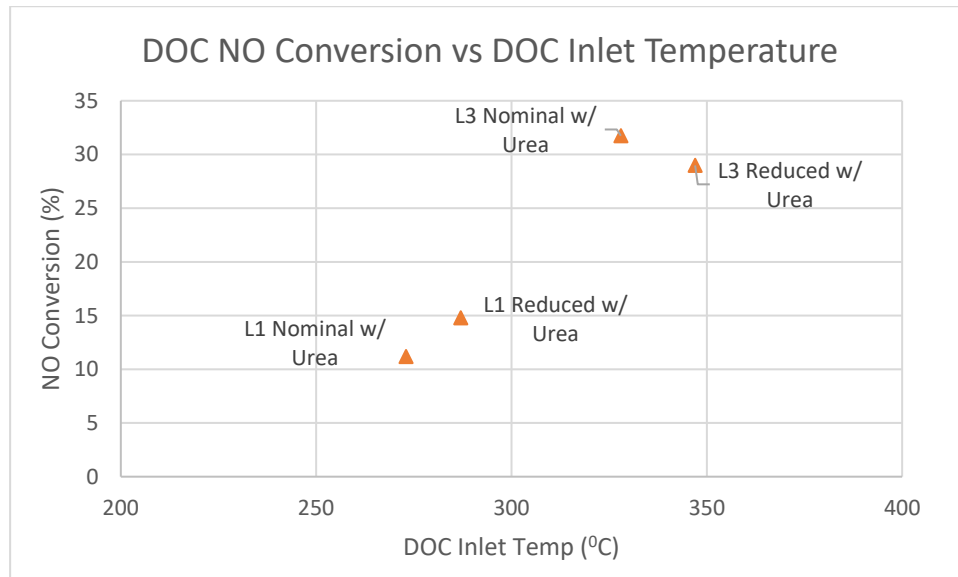


Figure 5.8: NO Conversion Across DOC vs DOC Inlet Temperature for Loading Tests w/ Urea

Further, the NO, NO<sub>2</sub> and NO<sub>x</sub> values at the SCR<sup>®</sup> outlet are given in Table 5.9 along with the values at the inlet for comparison. Since urea was injected into the system at ANR of 1.0, we see a significant reduction in the NO<sub>x</sub> values across the SCR<sup>®</sup>. The value of NO<sub>x</sub> reduction in percentage of inlet value is also given in Table 5.9 for each test.

Table 5.9: Emission Data Across SCR<sup>®</sup> for Loading Tests w/ Urea

Test	SCR <sup>®</sup> Inlet Temp.	SCR <sup>®</sup> Inlet			SCR <sup>®</sup> Outlet			NO <sub>x</sub> Conv.
		NO <sub>2</sub>	NO	NO <sub>x</sub>	NO <sub>2</sub>	NO	NO <sub>x</sub>	
	[°C]	[ppm]	[ppm]	[ppm]	[ppm]	[ppm]	[ppm]	[%]
L1 Nominal w/ Urea	268	41	143	184	0	36	36	80
L1 Reduced w/ Urea	283	45	121	166	0	34	34	80
L3 Nominal w/ Urea	321	98	200	298	1	18	19	94
L3 Reduced w/ Urea	340	76	174	250	1	14	15	94

Similar to the Loading Tests w/o Urea, the NO<sub>x</sub> values from Mass Spectrometer (MS) shown in Tables 5.8 and 5.9 were compared to the NO<sub>x</sub> values from the Calterm for Loading Tests w/ Urea. The comparison of NO<sub>x</sub> values at UDOC and USCR<sup>®</sup> and DSCR<sup>®</sup> from the MS and the Calterm for all the tests is shown in Figures 5.9, 5.10 and 5.11 respectively. The NO<sub>x</sub> value at UDOC and USCR<sup>®</sup> and DSCR<sup>®</sup> from the MS and the Calterm seem to be in agreement for all the tests as they are within the acceptable margin of error at all the three locations.

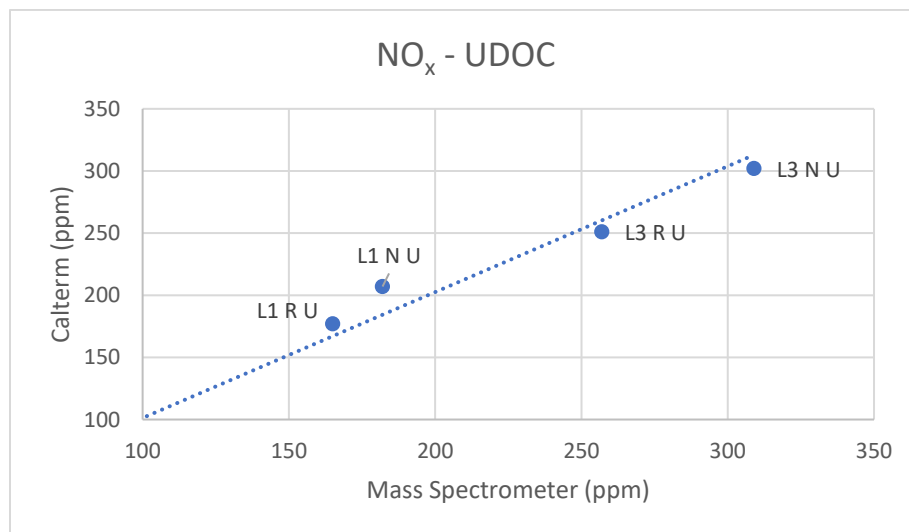


Figure 5.9: Comparison of NO<sub>x</sub> Data From Calterm and Mass Spectrometer at UDOC

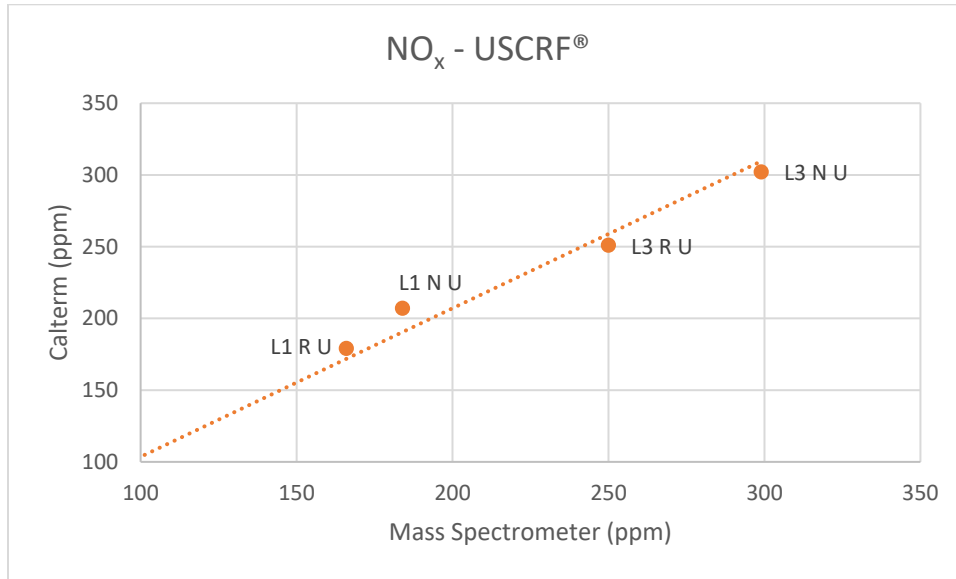


Figure 5.10: Comparison of NO<sub>x</sub> Data From Calterm and Mass Spectrometer at USCRF®

Figure 5.11 also shows the NO<sub>x</sub> values from the Loading Tests w/o Urea at DSCR® as compared to the NO<sub>x</sub> values from the Loading Tests w/ Urea. As there is NO<sub>x</sub> reduction across the SCR® due to the NH<sub>3</sub>, NO and NO<sub>2</sub> reactions, the NO<sub>x</sub> values at DSCR® are significantly lower in concentrations which is clearly seen in Figure 5.11.

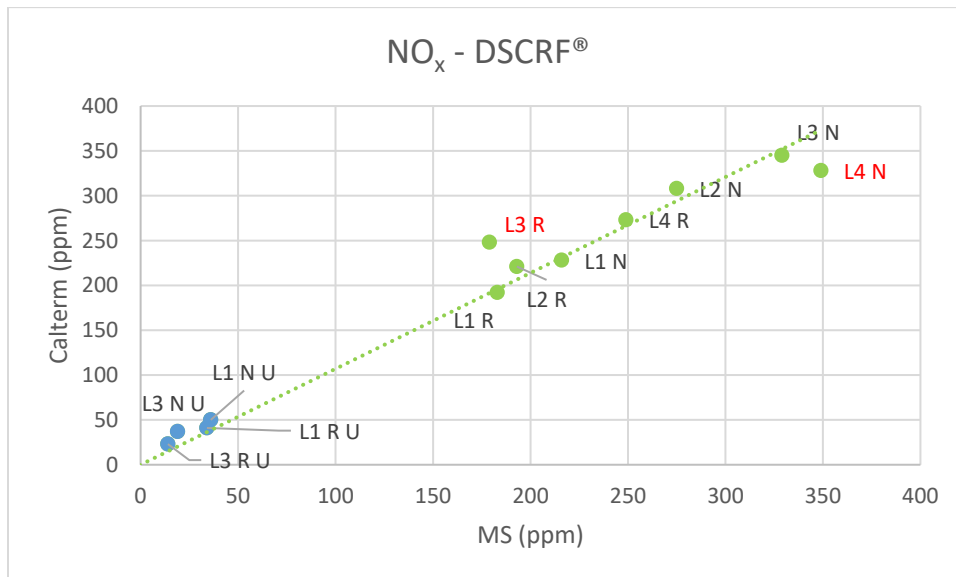


Figure 5.11: Comparison of NO<sub>x</sub> Data From Calterm and Mass Spectrometer at DSCR®

The NO<sub>x</sub> reduction performance of the SCRF® for Loading Tests w/ Urea is shown in Table 5.10. For these tests, the target ANR was 1.0. However, the values of ANR shown in Table 5.10 are the actual values used in the tests.

Table 5.10: NO<sub>x</sub> Reduction Performance of SCRF® at ANR 1.0 During Stage 2 for Loading Tests w/ Urea

Test	ANR	NH <sub>3</sub> Injected	NH <sub>3</sub> Slip	NO <sub>x</sub> Into SCRF®	NO <sub>x</sub> Out of SCRF®	NO <sub>x</sub> Conversion
[-]	[-]	[ppm]	[ppm]	[ppm]	[ppm]	[%]
L1 Nominal w/ Urea	1.00	184	1	184	36	80
L1 Reduced w/ Urea	0.98	163	16	166	34	80
L3 Nominal w/ Urea	1.09	325	23	298	19	94
L3 Reduced w/ Urea	1.01	253	15	250	15	94

Further, the PM mass balance for Stage 1 and Stage 2 for these tests is shown in Tables 5.11 and 5.12 respectively. It is important to note that the percentage of PM oxidized in Stage 1 and Stage 2 is low compared to the percentage of PM oxidized in Loading Test w/o Urea with similar conditions as the duration for both the tests with and without urea was the same. This difference in the percentage of PM oxidized due to urea injection has been discussed in detail in Section 5.3. The calculation of the clean weight of the SCRF® is discussed in detail in Appendix A. The filtration efficiency during Stage 1 was not measured physically but was estimated based on results from the calibrated SCR-F model which is also discussed in detail in Appendix A.

Table 5.11: PM Balance for Stage 1 for Loading Tests w/ Urea

Test	PM Conc.	PM <sub>in</sub>	Filtration Efficiency*	PM <sub>out</sub>	PM <sub>start</sub>	PM <sub>retained</sub>	PM <sub>oxidized</sub>	PM <sub>oxidized</sub>
	[mg/scm]	[g]	[%]	[g]	[g]	[g]	[g]	[%]
L1 Nominal w/ Urea	6.7	1.83	61.6	0.70	0	1.12	0.01	0.3
L1 Reduced w/ Urea	14.1	3.84	65.0	1.34	0	2.29	0.20	5.3
L3 Nominal w/ Urea	7.4	2.29	57.0	0.98	0	0.95	0.35	15.4
L3 Reduced w/ Urea	12.0	3.73	61.9	1.42	0	2.12	0.19	5.2

\*Average filtration efficiency estimated using calibrated SCR-F model discussed in Appendix A



Table 5.12: PM Balance for Stage 2 for Loading Tests w/ Urea

Test	PM Conc.	PM <sub>in</sub>	Filtration Efficiency	PM <sub>out</sub>	PM <sub>start</sub>	PM <sub>retained</sub>	PM <sub>oxidized</sub>	PM <sub>oxidized</sub>
	[mg/scm]	[g]	[%]	[g]	[g]	[g]	[g]	[%]
L1 Nominal w/ Urea	7.2	20.1	98.2	0.36	1.12	17.6	3.27	15.4
L1 Reduced w/ Urea	14.1	39.8	99.4	0.23	2.29	31.8	10.1	23.9
L3 Nominal w/ Urea	6.9	21.2	98.0	0.43	0.95	12.4	9.34	42.1
L3 Reduced w/ Urea	11.3	34.8	97.9	0.74	2.12	24.6	11.6	31.3

The cumulative PM mass balance at the end of Stage 2 for all the tests is illustrated graphically in Figures 5.12 and 5.13. It is observed that the percentage of PM oxidized is higher for L3 compared to L1. This is because at higher engine load, the SCR<sup>®</sup> temperature and NO<sub>2</sub> concentrations are higher compared to lower engine load. A decreasing trend in the percentage of PM mass retained is observed as we move from L1 to L3. The difference in percentage of PM oxidized or PM retained while comparing tests at nominal and reduced fuel rail pressure is due to major difference in PM concentration and minor difference in the SCR<sup>®</sup> temperature and NO<sub>2</sub> concentrations.

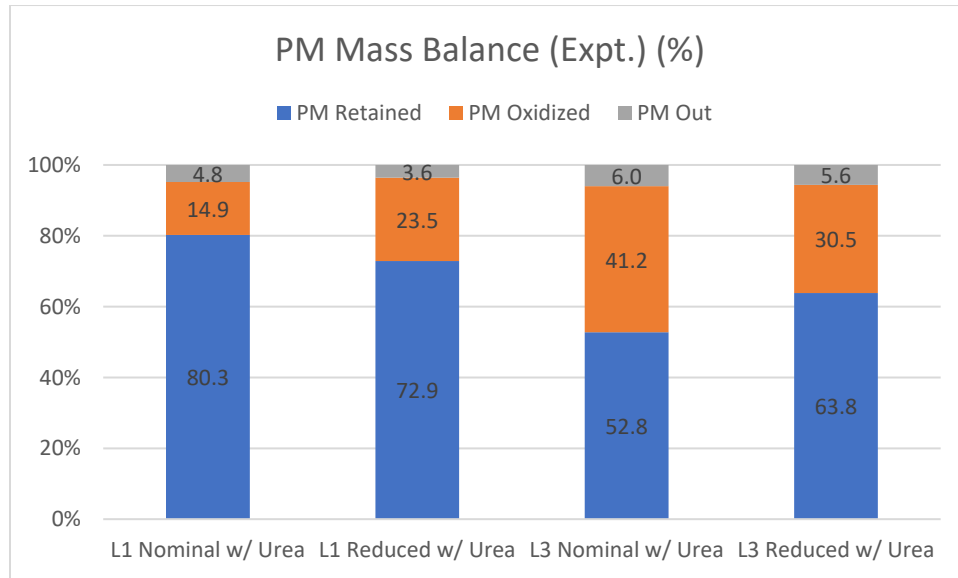


Figure 5.12: PM Mass Balance (Expt.) as % of PM In for Loading Tests w/ Urea

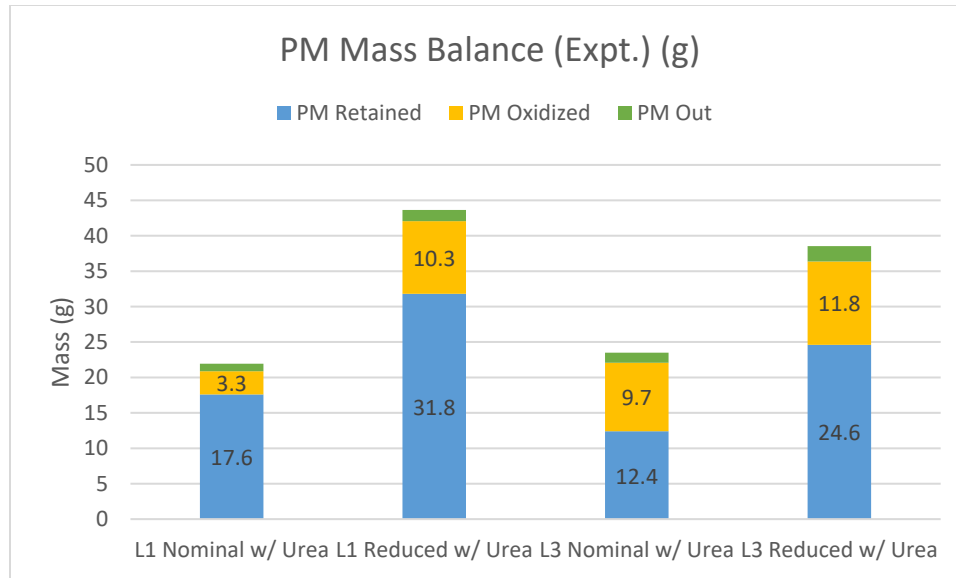


Figure 5.13: PM Mass Balance (Expt.) for Loading Tests w/ Urea

Next, the average reaction rate for NO<sub>2</sub> assisted PM oxidation during Stage 2 is calculated as explained in Section 3.10 for all the tests and is given in Table 5.13. The SCR<sup>®</sup> temperature, NO<sub>2</sub> concentrations, duration and the reaction rate constant (k) are also given in Table 5.13. The average reaction rate and reaction rate constant is higher for tests L3 Nominal and Reduced w/ Urea compared to L1 Nominal and Reduced w/ Urea due to higher SCR<sup>®</sup> temperature and NO<sub>2</sub> concentrations.

Table 5.13: Variables to Compare Kinetics of NO<sub>2</sub> Assisted PM Oxidation With Urea

Test	Expt. Reaction Rate (RR <sub>o</sub> )	Stage 2 Duration	SCR <sup>®</sup> Inlet Temp	NO <sub>2</sub> into SCR <sup>®</sup>	PM Retained	PM Oxidized	k = RR <sub>o</sub> /NO <sub>2</sub>
[-]	[1/s]	[min]	[°C]	[ppm]	[g]	[%]	[10 <sup>6</sup> /ppm/s]
<b>L1 Nominal w/ Urea</b>	1.81E-05	302	268	41	17.6	15.4	0.442
<b>L1 Reduced w/ Urea</b>	3.01E-05	301	283	45	31.8	23.9	0.669
<b>L3 Nominal w/ Urea</b>	6.58E-05	301	321	98	12.4	42.1	0.672
<b>L3 Reduced w/Urea</b>	4.32E-05	300	340	76	24.6	31.3	0.569

Again, the natural log of reaction rate constant ( $k$ ) from Table 5.13 is plotted against the inverse of SCRF<sup>®</sup> inlet temperature for all the tests and is shown in Figure 5.14. A similar plot from the experimental data from passive oxidation tests with urea [8] is shown in Figure 5.14 for comparing the kinetics during loading and passive oxidation conditions with urea injection. Similar to the trend observed in Loading Tests w/o Urea, the reaction rate kinetics for NO<sub>2</sub> assisted PM oxidation during loading with urea injection is higher compared to that during passive oxidation with urea injection. Also, it is not possible to fit the loading with urea data (with a R<sup>2</sup> value greater than 0.95) from Figure 5.14 with a single set of kinetics unlike the data for passive oxidation for which a single set of kinetics exists which is calculated using a standard Arrhenius model.

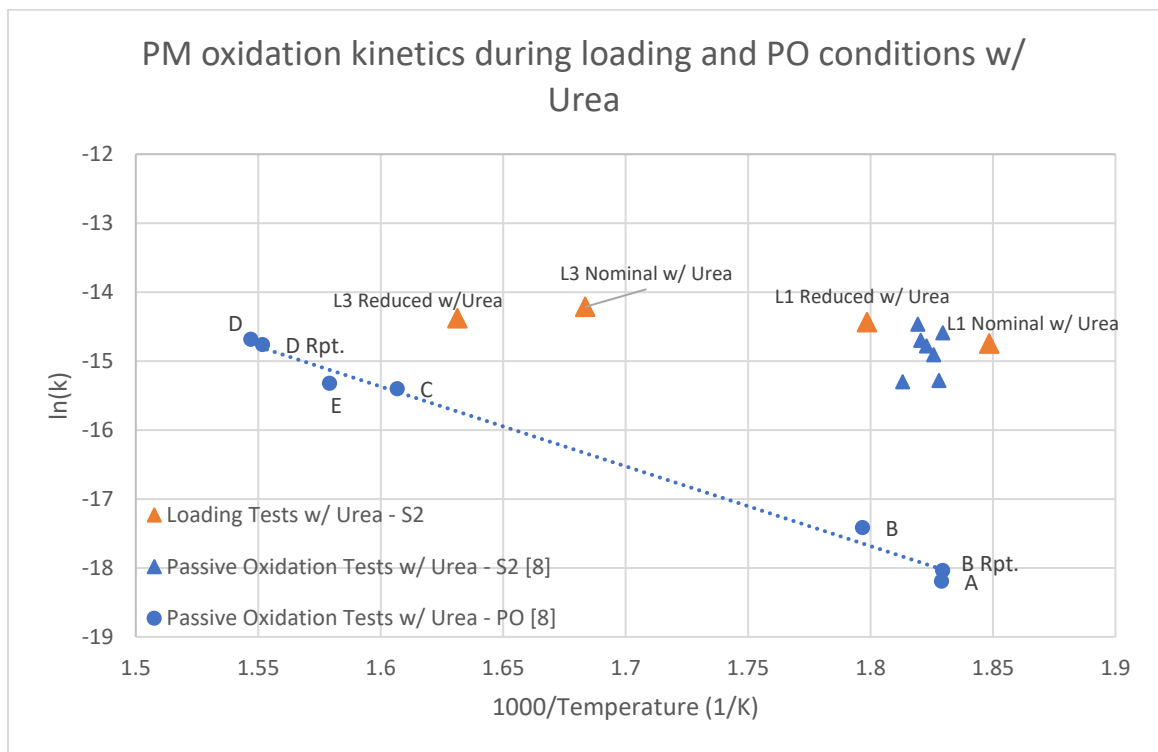


Figure 5.14: Comparison of SCRF<sup>®</sup> PM Oxidation Kinetics for Passive Oxidation [8] and Loading Conditions With Urea

### 5.3 Comparison of Results for Loading Tests w/o and w/ Urea

The data and results for the Loading Tests w/o Urea and w/ Urea have been presented in Section 5.1 and Section 5.2 respectively. However, it is important to compare the experimental data from both these sets of tests which is focus of this section. A comparison of the NO<sub>2</sub> assisted PM oxidation kinetics, PM oxidized, PM retained and SCR<sup>®</sup> pressure drop for loading with and without urea injection will be presented and discussed.

#### Kinetics Comparison

The variables necessary to compare the NO<sub>2</sub> assisted PM oxidation kinetics with and without urea are given in Table 5.14. The average reaction rate, PM retained and PM oxidized are compared for each of the Loading tests w/o and w/ Urea.

Table 5.14: Variables to Compare NO<sub>2</sub> Assisted PM Oxidation With and Without Urea Injection

Test	Expt. Reaction Rate (RR <sub>o</sub> )	SCR <sup>®</sup> Inlet Temp	NO <sub>2</sub> into SCR <sup>®</sup>	PM Retained	PM Oxidized	k = RR <sub>o</sub> /NO <sub>2</sub>
[-]	[1/s]	[°C]	[ppm]	[g]	[%]	[10 <sup>6</sup> /ppm/s]
L1 Nominal	2.53E-05	264	62	16.1	20.3	0.405
L1 Nominal w/ Urea	1.81E-05	268	46 <sup>1</sup>	17.6	15.4	0.394
L1 Reduced <sup>#</sup>	3.50E-05	275	59	25.4	26.7	0.592
L1 Reduced w/ Urea	3.01E-05	283	56 <sup>1</sup>	31.8	23.9	0.538
L3 Nominal	-	330	93	7.7*	53.0*	-
L3 Nominal w/ Urea	6.58E-05	321	98	12.4	42.1	0.672
L3 Reduced	6.24E-05	332	80	20.1	40.4	0.780
L3 Reduced w/Urea	4.32E-05	340	76	24.6	31.3	0.569

<sup>#</sup>Data obtained from Test PO-C in reference [11]

\*Cannot compare with other tests due to unexpected active regeneration in Stage 2

<sup>1</sup>NO<sub>2</sub> values estimated from Calterm

The average reaction rate for PM oxidation for each Loading Test w/o and w/ Urea from Table 5.14 has been compared in Figure 5.15. As observed from Figure 5.15, the average reaction rate for tests with urea injection is lower compared to tests without urea injection for the same engine conditions. This is due to decrease in available NO<sub>2</sub> in the PM cake caused by forward diffusion of NO<sub>2</sub> as a result of the concentration gradient caused by the consumption of NO and NO<sub>2</sub> by the SCR reactions in the substrate wall [12]. The reaction rate constant for tests with urea is also lower

compared to tests without urea as observed from Figure 5.15. The average reaction rate for L3 Nominal was not calculated as the value of PM retained and PM oxidized computed is incorrect due to an unexpected active regeneration in Stage 2 as explained earlier.

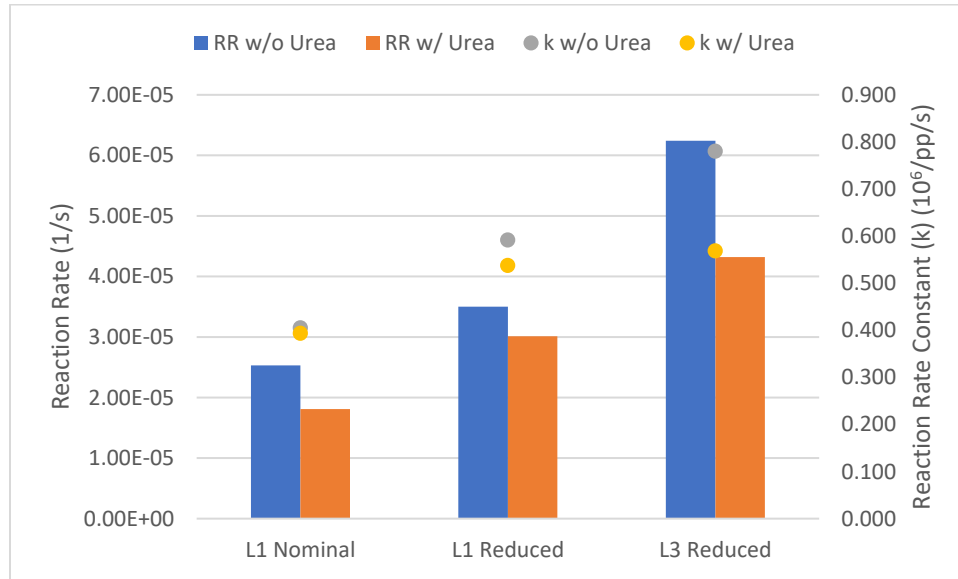


Figure 5.15: Reaction Rate Comparison for Loading Tests w/o and w/ Urea

When comparing one test without urea injection to another test with urea injection, the test with urea injection is expected to have higher value of PM retained in the SCRF<sup>®</sup>. This is because of the competition between PM oxidation and the SCR reactions and hence less oxidation of the PM retained by NO<sub>2</sub> which results in a higher PM retained. The same trend is observed for percentage of cumulative PM retained w.r.t. to cumulative PM entering when comparing a Loading Test w/o Urea to a Loading Test w/ Urea as shown in Figure 5.16. Figure 5.16 shows the comparison of cumulative PM oxidized for Loading Tests w/o and w/ Urea. As expected, the cumulative percentage of PM oxidized is higher for tests without urea compared to tests with urea. Similarly, Figure 5.17 shows the comparison of cumulative PM retained and PM oxidized in grams for the Loading Tests w/o and w/ Urea.

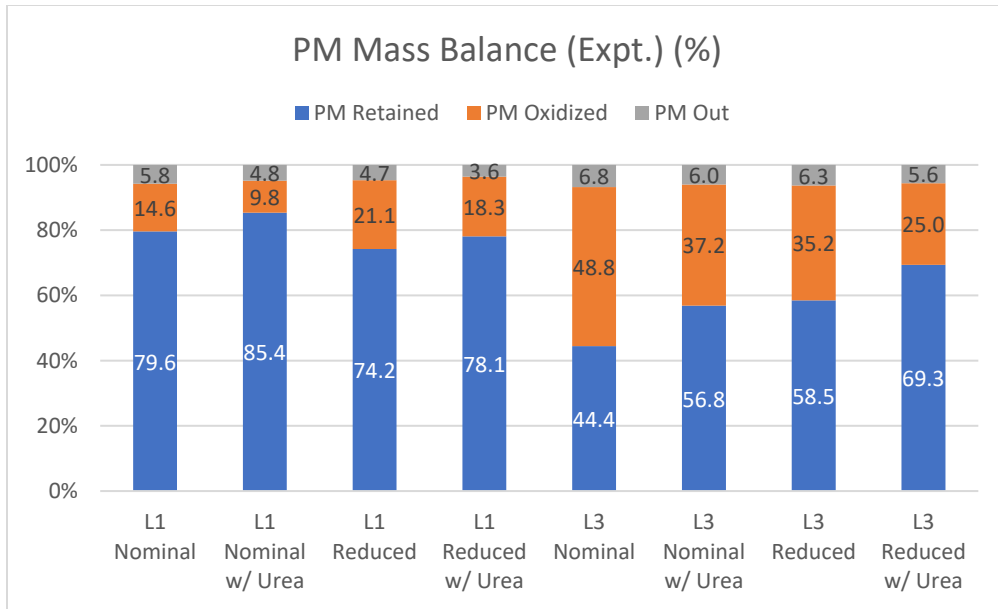


Figure 5.16: Comparison of Cumulative PM Retained and PM Oxidized as Percentage of PM In for Loading Tests w/o and w/ Urea

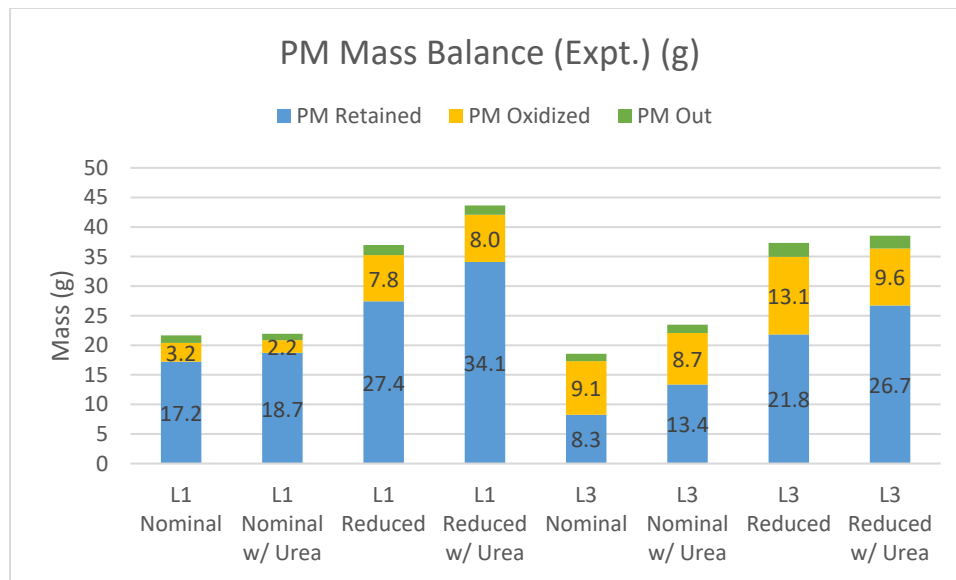


Figure 5.17: Comparison of Cumulative PM Retained and PM Oxidized for Loading Tests w/o and w/ Urea

Further, to compare the kinetics of PM oxidation during loading and passive oxidation conditions which is the primary objective of this study, the natural log of the reaction rate constant ( $k$ ) was plotted against the inverse of SCRF<sup>®</sup> inlet temperature for all the Loading Tests w/o and w/ Urea and all the Passive Oxidation Tests from reference [8] which is shown in Figure 5.18. The kinetics

of PM oxidation during loading conditions are higher than that during passive oxidation conditions as observed from Figure 5.18. A kinetic model is needed to explain the PM oxidation under passive oxidation and loading conditions. Hence, a PM oxidation model was developed based on the shrinking core model which is able to simulate the reaction kinetics using a single set of kinetics for PM oxidation under loading and passive oxidation conditions.

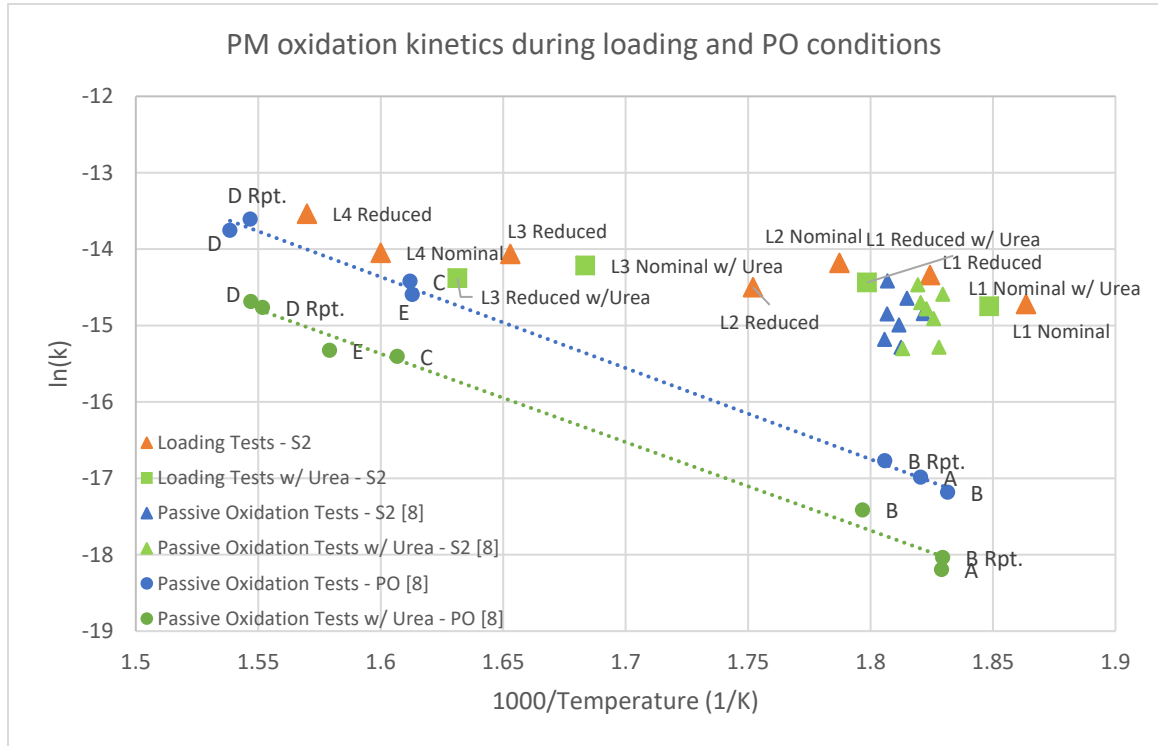


Figure 5.18: Comparison of PM Oxidation Kinetics for Passive Oxidation [8] and Loading Conditions With and Without Urea in SCRF®

### SCRF® Pressure Drop Comparison

To further understand the difference in the kinetics of PM oxidation with and without urea under loading conditions, the pressure drop across the SCRF® was studied for the Loading Tests w/o Urea and the Loading Tests w/ Urea. Figure 5.19 shows the pressure drop across SCRF® vs time for test L3 Reduced without Urea and L3 Reduced with Urea. The pressure drop for all other tests are given in Appendix C.

As discussed earlier, the PM retained in tests with urea injection is higher compared to that for the same test conditions without urea injection. The pressure drop across the SCRF<sup>®</sup> depends on the PM retained in the SCRF<sup>®</sup> cake and wall, the exhaust flow rate and the cake permeability. For the tests L3 Reduced and L3 Reduced with Urea, the exhaust flow rate is similar as shown in Table 5.16. However, the PM retained for L3 Reduced is 20.1 g compared to 24.6 g for L3 Reduced w/ Urea. Since the PM retained for L3 Reduced w/ Urea is higher, the pressure for this test should be higher compared to the test L3 Reduced. This trend is observed clearly in Figure 5.19 where the pressure drop for L3 Reduced with Urea is higher compared to L3 Reduced due to higher PM retained in the SCRF<sup>®</sup> and lower PM oxidized. The SCRF<sup>®</sup> inlet temperature, NO<sub>2</sub> concentration into the SCRF<sup>®</sup>, PM retained and PM oxidized are also given in Table 5.15 for better comparison between the two tests.

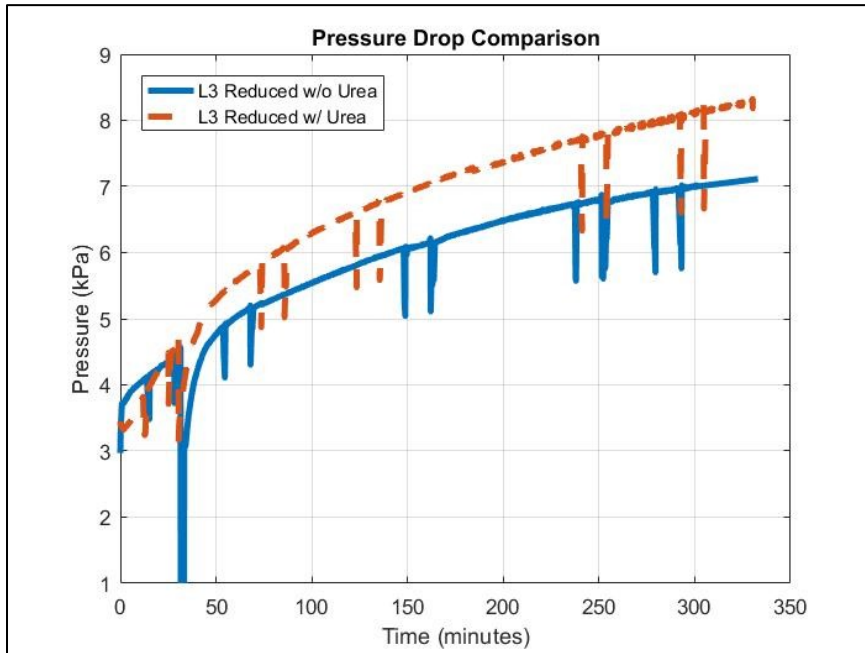


Figure 5.19: Comparison of Pressure Drop Across SCRF<sup>®</sup> vs Time Plots for L3 Reduced w/o and w/ Urea

Table 5.15: Variables Important for Comparing Pressure Drop Across SCRF<sup>®</sup> for L3 Reduced w/o and w/ Urea

Test	Duration	Exhaust Flow Rate	SCRF <sup>®</sup> Inlet Temp	NO <sub>2</sub> into SCRF <sup>®</sup>	PM Retained	Cumulative PM Oxidized
[-]	[min]	[kg/min]	[°C]	[ppm]	[g]	[%]
L3 Reduced	334	12.0	332	80	20.1	35.2
L3 Reduced w/Urea	330	12.1	340	76	24.6	25.0



Next, the test L3 Nominal and L3 Nominal w/ Urea will be compared in a similar way. Figure 5.20 shows the pressure drop across SCR<sup>F</sup>® vs time for test L3 Nominal and L3 Nominal w/ Urea. For L3 Nominal, there was an unexpected active regeneration at the end of Stage 2 as discussed earlier which is clearly seen in Figure 5.20 as a spike in the pressure drop between 250-300 minutes.

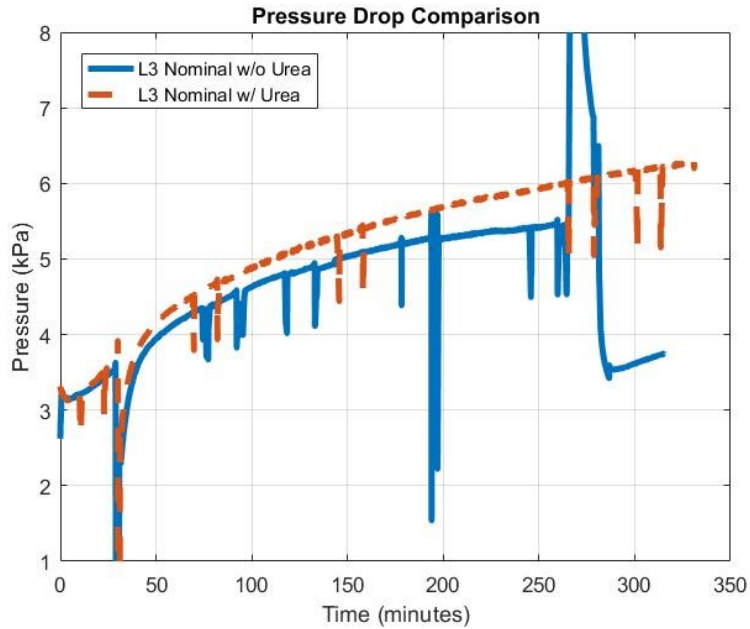


Figure 5.20: Comparison of Pressure Drop Across SCR<sup>F</sup>® vs Time plots for L3 Nominal w/o and w/ Urea

The pressure drop for L3 Nominal w/ Urea is higher than the pressure drop for L3 Nominal at all time as seen in Figure 5.20. This is because the cumulative PM oxidized is lower for L3 Nominal w/ Urea compared to L3 Nominal and so the PM retained for L3 Nominal w/ Urea is higher compared to L3 Nominal as seen in Table 5.16. Other parameters which affect the pressure drop such as the exhaust flow rate and the cake permeability are the same for the tests compared as shown in Table 5.16. The SCR<sup>F</sup>® inlet temperature, NO<sub>2</sub> concentrations into the SCR<sup>F</sup>® and duration of the tests are also given in Table 5.16 for better comparison between the two tests.

Table 5.16: Variables Important for Comparing Pressure Drop Across SCR<sup>F</sup>® for L3 Nominal w/o and w/ Urea

Test	Duration	Exhaust Flow Rate	SCR <sup>F</sup> ® Inlet Temp	NO <sub>2</sub> into SCR <sup>F</sup> ®	PM Retained	Cumulative PM Oxidized
[-]	[min]	[kg/min]	[°C]	[ppm]	[g]	[%]
L3 Nominal	331	12.1	330	93	10.0*	48.8
L3 Nominal w/Urea	331	12.1	321	98	12.4	37.2

\*Estimated from SCR-F model [Section 5.4]

## 5.4 Calibration of SCR-F Model With Reaction Rate Data From the PM Oxidation Model for the Loading Tests w/o Urea

This section focuses on the results of the calibration of the SCR-F model using experimental data from the eight Loading Tests w/o Urea, after applying the reaction rate data from the PM oxidation model to the SCR-F model as discussed in Section 4.2.

The kinetics of NO<sub>2</sub> assisted PM oxidation in the cake and the wall and the pressure drop parameters obtained after calibrating the SCR-F model using the reaction rate data from the PM oxidation model for the Loading Tests w/o Urea is shown in Tables 5.17 and 5.18 respectively.

Table 5.17: Cake and Wall PM Oxidation Kinetics From Calibration of Loading Test w/o Urea Data

	Symbol	Value	Units
Pre Exponential of NO <sub>2</sub> assisted PM oxidation	$A_{NO_2, \text{cake}}$	2.6	m/K-s
Activation energy of NO <sub>2</sub> assisted PM oxidation	$E_{a, NO_2, \text{cake}}$	96	kJ/gmol
Pre Exponential of NO <sub>2</sub> assisted PM oxidation	$A_{NO_2, \text{wall}}$	1.8	m/K-s
Activation energy of NO <sub>2</sub> assisted PM oxidation	$E_{a, NO_2, \text{wall}}$	96	kJ/gmol

Table 5.18: SCR-F Model Pressure Drop Parameters From Calibration of Loading Test w/o Urea Data

Parameter	Description	SCR-F	Units
<b>Substrate Wall</b>			
$k_{o,w}$	Initial permeability of substrate wall	1.04E-13	(m <sup>2</sup> )
$k_{o,trans}$	Transition permeability of substrate wall	8.00E-13	(m <sup>2</sup> )
<b>Wall PM</b>			
$C_{1wpm}$	First constant for wall packing density calculation	2.35	(1/m <sup>3</sup> )
$C_{2wpm}$	Second constant for wall packing density	0.723	(kg/m <sup>3</sup> )
$C_3$	Ref. pressure for wall permeability correction	103.2	(kPa)
$C_4$	Wall permeability correction factor	110	(-)
<b>PM cake layer</b>			
$\alpha_{0,cake}$	Initial solidosity of PM cake layer	0.05	(-)
$k_{o,cake}$	Initial / ref. permeability of PM cake layer	7.01E-15	(m <sup>2</sup> )
$A_{eff,cake}$	PM cake maximum filtration efficiency parameter	0.95	(-)
$C_5$	Cake permeability correction factor	1.43E-13	(kg m <sup>-1</sup> )
$C_6$	Ref. pressure for lambda correction	100	(kPa)
$C_7$	Ref. temperature for lambda correction	300	(K)
$C_{10}$	Slope for post loading cake permeability	0	(-)
$C_{11}$	Constant for post loading cake permeability	1.485	(-)
$C_{13}$	Constant for oxidation cake permeability	0.664	(-)

The performance of the SCR-F model for the Loading Tests w/o Urea is given in Tables 5.19 and 5.20. Table 5.19 shows the comparison of the model PM retained values to the experimental values at the end of Stage 1 and Stage 2. Table 5.19 data shows that the model PM retained data are within  $\pm 2$  g of the experimental values at the end of Stage 1 and Stage 2 for all the tests except L2 Nominal as the experimental value of PM retained is inconsistent with the trend followed by other tests (Figure 5.21). The experimental PM retained values for L3 Nominal shown in Table 5.19 should be higher as there was more PM oxidized due to an unexpected active regeneration in Stage 2 which is already discussed in Section 5.1. The plots showing the simulated PM retained in the SCR-F<sup>®</sup> versus time for all the Loading Test w/o Urea are given in Appendix E.

Table 5.19: Comparison of Experimental and Model PM Retained at the End of Stage 1 and Stage 2

Test	PM Retained					
	Stage 1			Stage 2		
	Expt.	Model	Diff.	Expt.	Model	Diff.
	[g]	[g]	[g]	[g]	[g]	[g]
<b>L1 Nom</b>	1.1	1.1	0.0	16.1	15.7	0.4
<b>L1 Red<sup>#</sup></b>	2.0	2.1	-0.1	25.4	26.9	-1.5
<b>L2 Nom</b>	0.8 <sup>[1]</sup>	1.0	-0.2	11.5 <sup>1</sup>	13.9	-2.4
<b>L2 Red</b>	2.1	1.9	0.2	26.8	25.8	1.0
<b>L3 Nom</b>	0.6*	0.8	-0.2	7.8*	10.0	-
<b>L3 Red</b>	1.7	1.6	0.1	20.0	20.2	-0.2
<b>L4 Nom</b>	0.8	0.7	0.1	8.5	6.9	1.6
<b>L4 Red</b>	1.5	1.4	0.1	15.0	14.6	0.4

<sup>#</sup>Data obtained from Test PO-C in reference [11]

\* The experimental value is lower than the expected PM retained due to unexpected active regeneration in Stage 2

<sup>1</sup>The experimental value is lower than the expected PM retained for the pressure drop value (Figure 5.21)

Table 5.20 shows the comparison between the model SCR-F<sup>®</sup> pressure drop values and the experimental values at the end of Stage 2. The model pressure drop across the SCR-F<sup>®</sup> is within  $\pm 0.5$  kPa of the experimental value at the end of Stage 2 for all the tests except L4 Reduced as the experimental pressure drop value is inconsistent with the trend followed by other tests (Figure

5.21). For the test L3 Nominal, the pressure drop value just before the start of the unexpected active regeneration in Stage 2 was compared to the model pressure drop value. The plots showing the simulated pressure drop across SCR<sup>®</sup> versus time for all the Loading Test w/o Urea are given in Appendix F.

Table 5.20: Comparison of Experimental and Model Pressure Drop at the End of Stage 2

Test	Stage 2 Pressure Drop		
	Expt.	Model	Diff.
	[kPa]	[kPa]	[kPa]
<b>L1 Nom</b>	6.1	5.8	0.3
<b>L1 Red<sup>#</sup></b>	7.9	7.8	0.1
<b>L2 Nom</b>	6.1	5.9	0.2
<b>L2 Red</b>	7.8	8.0	-0.2
<b>L3 Nom</b>	5.5*	5.7 (5.5*)	0.0*
<b>L3 Red</b>	7.1	7.5	-0.4
<b>L4 Nom</b>	5.1	5.3	-0.2
<b>L4 Red</b>	6.0 <sup>1</sup>	6.9	-0.9

#Data obtained from Test PO-C in reference [3]

\*Pressure drop before the unexpected active regeneration in Stage 2

<sup>1</sup>The experimental value is lower than expected pressure drop for the amount of PM retained

Further, the experimental pressure drop across the SCR<sup>®</sup> normalized by the exhaust mass flow rate is plotted against the experimental PM retained at the end of Stage 2 for all the tests as shown in Figure 5.21 to ensure the integrity of the experimental data collected. A line has been plotted to fit the data as seen in Figure 5.21. All the tests follow a similar trend along the line except the tests L2 Nominal and L4 Reduced which are identified as the outlier points. This means that the experimental pressure drop value should be higher or lower for the amount of PM retained or vice versa for these two test points.

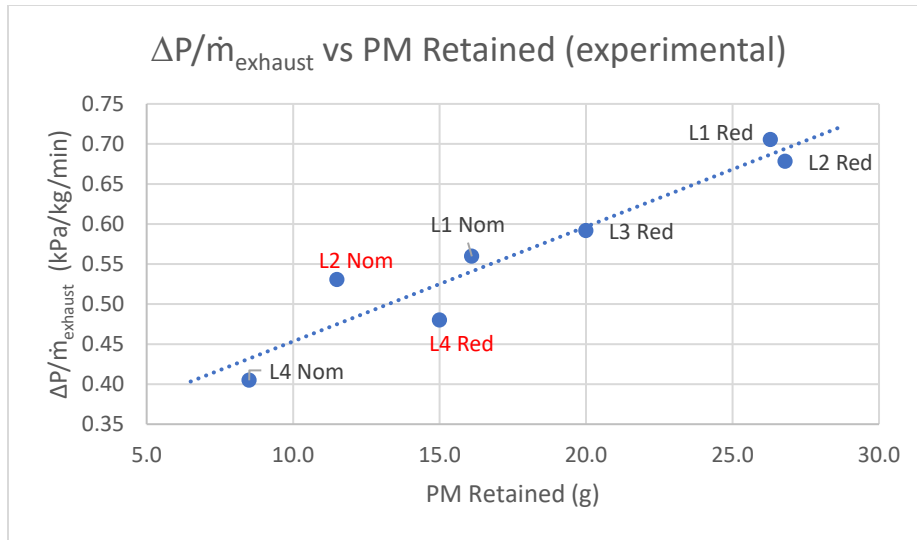


Figure 5.21: Expt. Pressure Drop Normalized by Exhaust Flow Rate vs Expt. PM Retained for Loading Tests w/o Urea

The model pressure drop across SCR-F<sup>®</sup> normalized by the exhaust mass flow rate is plotted against the model PM retained at the end of Stage 2 for all the tests as shown in Figure 5.22. The cake permeability is assumed constant in the SCR-F model shown in Table 5.18 has been used in the calibrated SCR-F model. Again, a line is plotted to fit the data. All the tests follow a similar trend along the line as compared to two outlier points based on the experimental plot in Figure 5.21. Hence, either the pressure drop or PM retained data for tests L2 Nominal and L4 Reduced could be incorrect due to measurement inaccuracy. The value of pressure drop and PM retained from the model for test L3 Nominal is also consistent with the model data from other tests as it was simulated without the active regeneration that occurred with the experimental data.

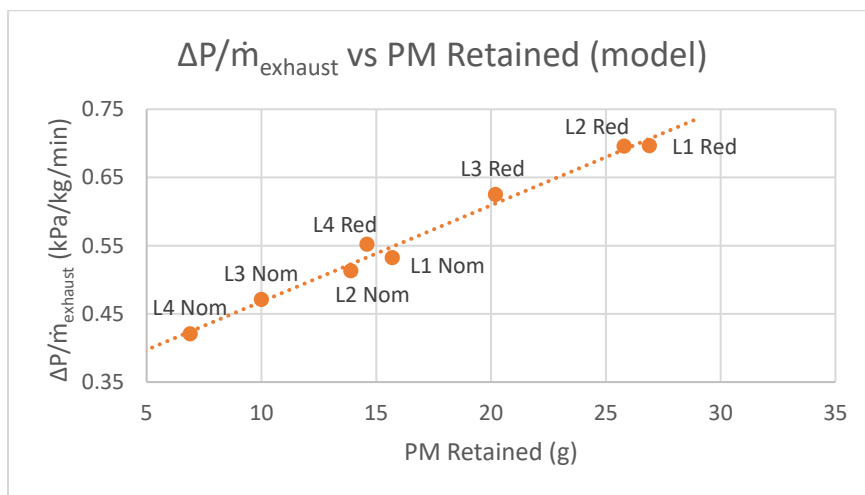


Figure 5.22: Model Pressure Drop Normalized by Exhaust Flow Rate vs Model PM Retained for Loading Tests w/o Urea

The total model pressure drop across the SCR-F<sup>®</sup> is the sum of the pressure drop across the cake, wall and channel. This is clearly observed in the model pressure drop plots in Appendix F. Similarly, the SCR-F model predicts the amount of PM retained in the cake and the wall as observed from the plots in Appendix E. The cake pressure drop normalized by the exhaust mass flow rate is plotted versus the PM retained in the cake at the end of Stage 2 for all the tests as shown in Figure 5.23. As observed from Figure 5.23, all the tests follow a similar trend along the line which implies that the amount of PM retained in the cake predicted by the model is in agreement with the cake pressure drop. Also, the wall pressure drop normalized by the exhaust mass flow rate is plotted versus the PM retained in the wall at the end of Stage 2 for all the tests as shown in Figure 5.24 to check the consistency of the SCR-F model.

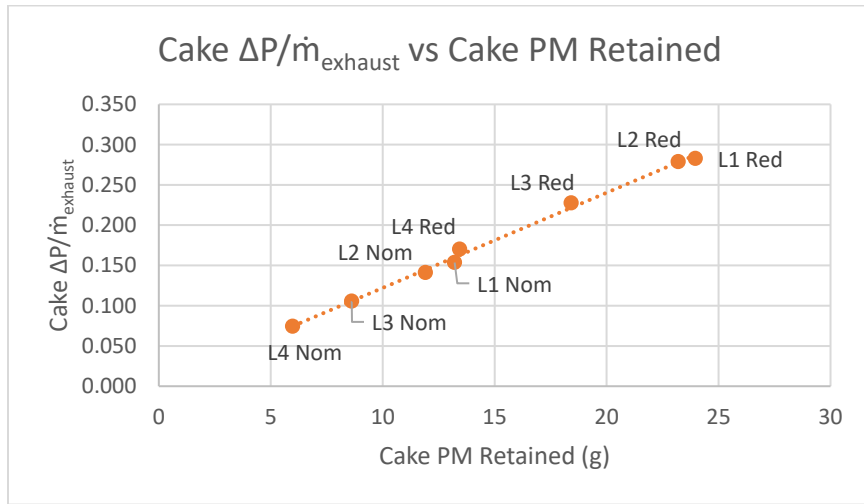


Figure 5.23: Cake Pressure Drop Normalized by Exhaust Flow Rate vs Cake PM Retained for Loading Tests w/o Urea

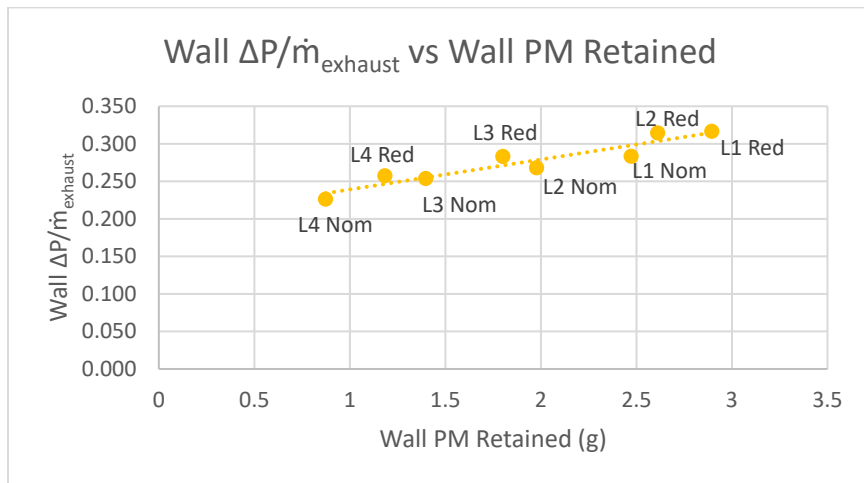


Figure 5.24: Wall Pressure Drop Normalized by Exhaust Flow Rate vs Wall PM Retained for Loading Tests w/o Urea

The PM mass balance is analyzed for the values obtained from the model for all the tests. Figure 5.25 shows the cumulative mass balance in terms of percentage of cumulative PM entering the SCR-F<sup>®</sup> using the SCR-F model for all the tests. As observed from Figure 5.25, the percentage of PM oxidized increases and the percentage of PM retained decreases with increase in engine load which is as expected. L3 Nominal and L1 Reduced also follow the expected trend which was not observed with the experimental data shown in Figures 5.5 and 5.6. The difference in the % PM oxidized and PM retained while comparing tests at nominal and reduced fuel rail pressure is due to major differences in PM concentrations and minor differences in the SCR-F<sup>®</sup> temperature and NO<sub>2</sub> concentrations.

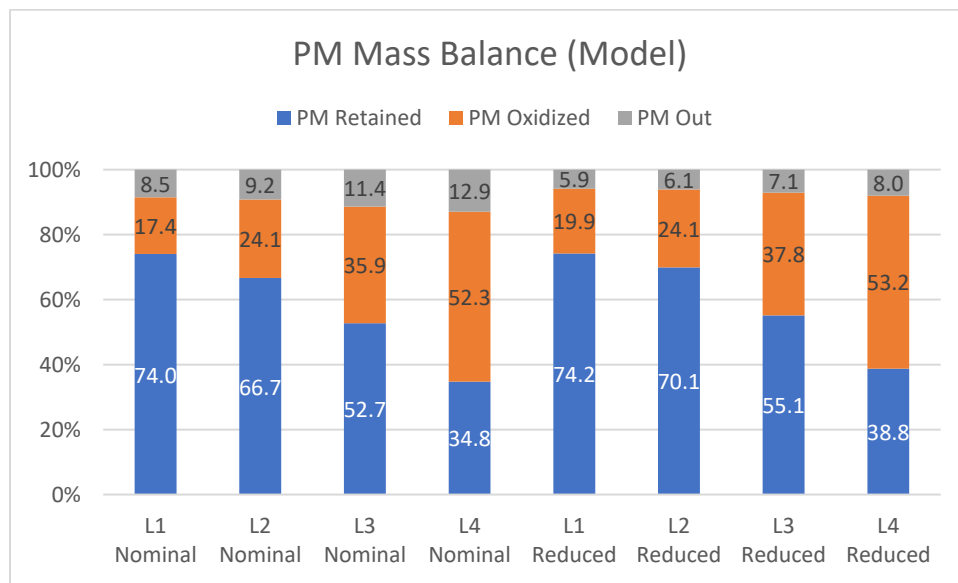


Figure 5.25: PM Mass Balance(Model) as % of PM In for Loading Tests w/o Urea

Further, the calibrated SCR-F model was used to estimate the cumulative amount of PM retained in the cake and the wall at the end of Stage 2 for all the tests. The comparison of the PM retained in the cake and wall is illustrated graphically as shown in Figure 5.26. The PM retained in the cake and the wall decreases in going from L1 to L4 for nominal or reduced rail pressure as observed from Figure 5.26. This is due to higher PM oxidation at higher engine loads due to higher SCR-F<sup>®</sup> temperature and NO<sub>2</sub> concentrations leading to lower PM retained. Also, the PM retained for tests at reduced rail pressure is higher compared to tests at nominal rail pressure because of higher PM entering the SCR-F<sup>®</sup> due to relatively high PM concentrations at reduced rail pressure.

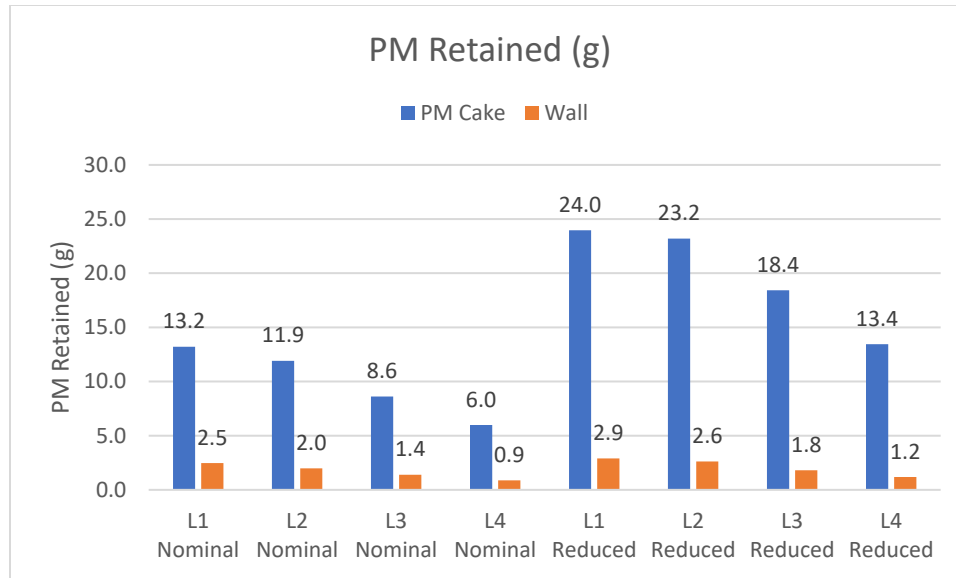


Figure 5.26: PM Retained in the Cake and the Wall

Figure 5.27 shows the distribution of PM retained in the cake and the wall in terms of percentage of the total PM retained for all the tests. It is observed that the majority of PM is retained in the cake as seen in Figure 5.27. Also, the percentage of PM retained in the cake increases with increase in engine load (L1 to L4).

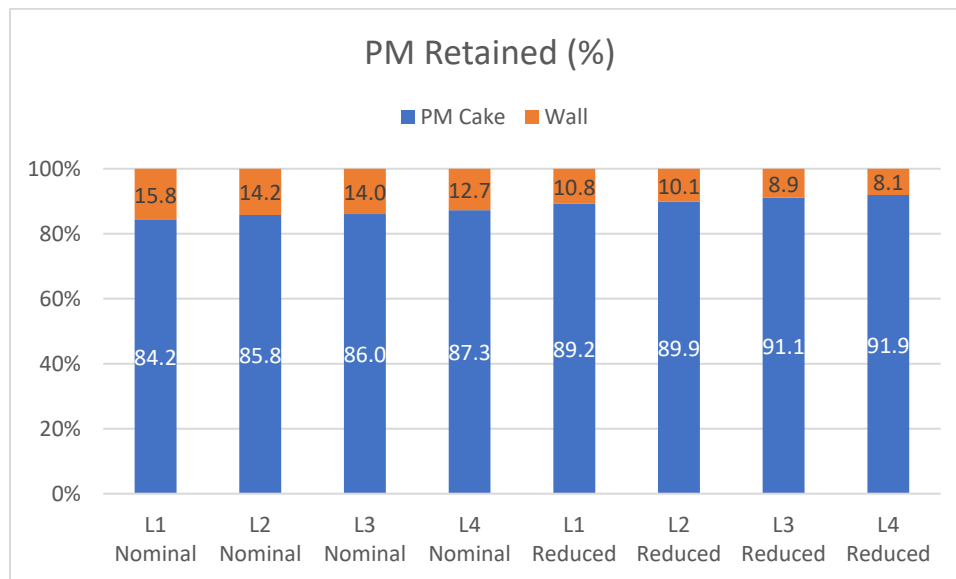


Figure 5.27: PM Retained in the Cake and the Wall as % of Total PM Retained



Figure 5.28 shows the PM oxidized in the cake and the wall for all the tests. It is observed that the PM oxidized in the cake and the wall increases with the increase in engine load (L1 to L4) due to increased temperature and NO<sub>2</sub> concentrations.

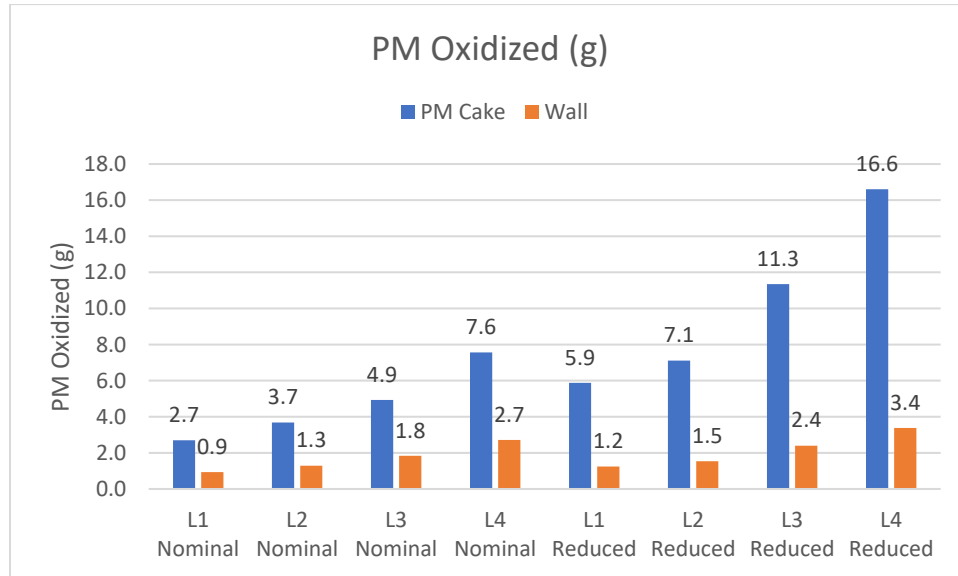


Figure 5.28: PM Oxidized in the Cake and the Wall

The distribution of PM oxidized in the cake and the wall in terms of percentage of the total PM oxidized for all the tests is given in Figure 5.29. Although no trend is observed in the percentage of PM oxidized in the cake and the wall, it is observed that the majority of PM oxidized in the cake for all the tests.

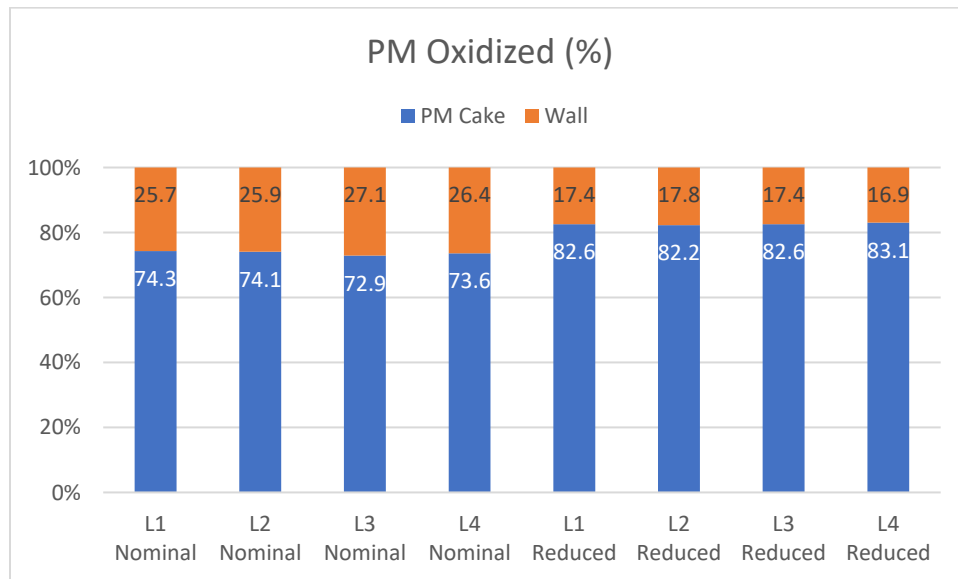


Figure 5.29: PM Oxidized in the Cake and the Wall as % of Total PM Oxidized

## 5.5 Calibration of the PM Oxidation Model with Passive Oxidation w/o Urea Data

The reaction rate results from the PM oxidation model were used in the SCR-F model to simulate the kinetics of PM oxidation in the cake and wall for all the Loading Tests w/o Urea. The performance of SCR-F model along with the PM oxidation model is evaluated only on the kinetics of PM oxidation in loading conditions. However, there is need to ensure that the PM oxidation model can simulate the PM oxidation using a single set of kinetics under a wide range of conditions including loading and passive oxidation conditions. This is done by calibrating the PM oxidation model with experimental data from reference [8] which is already discussed in Section 4.4. The performance of the PM oxidation model on the passive oxidation data from reference [8] is the focus of this section.

As discussed in Section 4.4, each passive oxidation test from reference [8] consists of two loading stages (Stage 1 and Stage 2) followed by a 15 min Ramp up stage, passive oxidation stage and post oxidation loading stages (Stage 3 and Stage 4). The experimental data for loading Stage 2 and passive oxidation stage is shown in Table 5.21 and 5.22. The experimental data obtained from each stage of the passive oxidation test i.e. Stage 1, Stage 2, Ramp up, Passive Oxidation Stage and Stage 3 of the test are used as input parameters for the model.

*Table 5.21: Loading Conditions for Stage 2 in Configuration 1 Tests w/o Urea [8]*

Test	Engine Speed	Engine Load	Exhaust Flow Rate	SCR-F <sup>®</sup> In Temp	NO <sub>2</sub> into SCR-F <sup>®</sup>	PM Conc.
	RPM	Nm	kg/min	°C	ppm	mg/scm
<b>PO-A</b>	2403	202	11.2	279	61	13.5
<b>PO-C</b>	2401	201	11.2	278	64	12.7
<b>PO-E</b>	2401	201	11.2	274	66	12.2
<b>PO-B</b>	2406	198	11.0	276	39	13.3
<b>PO-B Rpt</b>	2401	201	11.3	279	77	13.6
<b>PO-D</b>	2402	195	11.2	278	52	13.1
<b>PO-D Rpt</b>	2402	202	11.3	279	68	13.9

Table 5.22: Passive Oxidation Conditions for Configuration 1 Tests w/o Urea [8]

Test	Engine Speed	Engine Load	Duration	Exhaust Flow Rate	SCRF® Inlet Temp.	NO <sub>2</sub> into SCRF®	PM Conc.
	RPM	Nm	Minutes	kg/min	°C	ppm	mg/scm
<b>PO-A</b>	1300	300	421	5.6	276	263	2.5
<b>PO-C</b>	1400	550	81	7.0	347	228	3.7
<b>PO-E</b>	1200	650	36	7.3	347	523	2.2
<b>PO-B</b>	900	450	240	3.8	273	674	1.7
<b>PO-B Rpt</b>	900	450	220	3.4	281	792	1.7
<b>PO-D</b>	2100	600	153	13.0	377	117	4.2
<b>PO-D Rpt</b>	2100	600	122	12.8	374	147	5.0

The kinetics of PM oxidation obtained after calibrating the PM oxidation model as discussed in Section 4.4 is shown in Table 5.23. It is important to note that the same set of kinetics was used for all stages in the test i.e. Stage 1, Stage 2, Ramp up, passive oxidation stage and Stage 3.

Table 5.23: Calibrated NO<sub>2</sub> Assisted PM Oxidation Kinetics From the PM Oxidation Model

NO <sub>2</sub> assisted kinetics	Value	Units
<b>Activation Energy (E<sub>a</sub>)</b>	96	kJ/gmol
<b>Pre-exponential (A)</b>	77	1/K-ppm-s

The performance of the PM oxidation model with the same set of kinetics is given in Table 5.24. Table 5.24 shows the comparison of the model PM retained values to the experimental values at the end of Stage 1, Stage 2 and Stage 3. As observed from Table 5.24, the model PM retained values are within ±2 g of the experimental values at the end of Stage 1 and Stage 2 for all the tests.

Table 5.24: Comparison of Experimental and Model PM Retained at the End of Stage 1, Stage 2 and Stage 3

Test	Stage 1			Stage 2			Stage 3		
	Expt.	Model	Diff.	Expt.	Model	Diff	Expt.	Model	Diff
	[g]	[g]	[g]	[g]	[g]	[g]	[g]	[g]	[g]
PO-A	3.1	3.3	-0.2	35.1	33.9	1.2	35.1	33.9	1.2
PO-C	2.1	2.4	-0.3	32.7	31.9	0.8	23.2	23.9	-0.7
PO-E	3.6	3.4	0.2	33.5	31.6	1.9	22.9	22.2	0.7
PO-B	1.9	2.1	-0.2	32.7	33.2	-0.5	28.9	28.1	0.8
PO-B Rpt	2.2	2.9	-0.7	31.7	33.7	-2.0	23	24.5	-1.5
PO-D	2	2.4	-0.4	32.5	32.8	-0.3	18	16.2	1.8
PO-D Rpt	1.8	2.6	-0.8	29.2 (32.5*)	34.1	(-1.6)	14.5 (15.5*)	17.5	(-2.0)

\*estimated value [40]

The shrinking core model used in the development of PM oxidation model is capable of simulating the NO<sub>2</sub> assisted oxidation of PM with a single set of kinetics under a wide range of conditions including loading and passive oxidation conditions as discussed in this section for data from passive oxidation tests from reference [8].

## Chapter 6. Summary and Conclusions

This chapter summarizes the findings and accomplishments from this study. It also provides conclusions from the results for the experimental and modeling work.

### 6.1 Summary

The primary objective of this study was to carry out Loading Tests w/o and w/ Urea and measure species concentrations, PM mass retained, flowrates, substrate temperature distributions, pressure drop across the filter, and to determine the kinetics of NO<sub>2</sub> assisted PM oxidation under loading conditions and compare it with kinetics under passive oxidation conditions from reference [8]. A total of 12 tests were performed in this study: eight tests without urea injection, and four tests with urea injection. The summary of the findings in this study is divided into Loading Test w/o Urea, Loading Test w/ Urea, and the modeling work.

#### **Loading Test w/o Urea**

Eight tests were performed to study the characteristics of PM oxidation in the SCRF<sup>®</sup> under loading conditions without urea injection. The exhaust flow rates and standard space velocities ranged from 10.9-12.5 kg/min and 33-37 k/hr respectively. The NO<sub>2</sub> concentrations at the SCRF<sup>®</sup> inlet varied from 52-120 ppm and SCRF<sup>®</sup> inlet temperature varied from 264-374°C. The cumulative percentage of PM oxidized varied from 19.9% to 54.5% during the 5.5-hour Loading Tests w/o Urea. The average reaction rate for Stage 2 varied from 2.53E-05 to 1.08E-04 s<sup>-1</sup> while the reaction rate constant ranged from 0.405-1.320\*10<sup>6</sup>/ppm/s. It is not possible to fit the experimental data using an Arrhenius model to determine the kinetics of NO<sub>2</sub> assisted passive oxidation because the reactivity of PM under loading without urea was compared to the reactivity of PM under passive oxidation conditions without urea.

#### **Loading Test w/ Urea**

Four tests were performed to study the characteristics of PM oxidation in the SCRF<sup>®</sup> under loading conditions with urea injection. The average ANR for tests was 1.02 with one test having an ANR of 1.09 (L3 Nominal w/ Urea). The NO<sub>x</sub> conversion varied from 80-94%. The average NH<sub>3</sub> slip ranged from 1-12 ppm. The exhaust flow rates and standard space velocities ranged from 10.9-12.1 kg/min and 33-36 k/hr respectively. The NO<sub>2</sub> concentrations at the SCRF<sup>®</sup> inlet varied from

41-98 ppm and the SCRF<sup>®</sup> inlet temperature varied from 268-334°C. The average filtration efficiency for Stage 2 was 98.4%. The cumulative percentage of PM oxidized varied from 14.9 to 41.2%. The average reaction rate for Stage 2 varied from 1.81E-05 to 6.58E-05 s<sup>-1</sup> while the reaction rate constant ranged from 0.442-0.672\*10<sup>6</sup>/ppm/s. It is not possible to fit the experimental data using an Arrhenius model to determine the kinetics of NO<sub>2</sub> assisted passive oxidation with urea injection because the reactivity of PM under loading with urea was compared to the reactivity of PM under passive oxidation conditions with urea. A comparison of the results for these tests was done with the results for the corresponding tests without urea injection in terms of average reaction rate, reaction rate constant, cumulative PM oxidized, cumulative PM retained and SCRF<sup>®</sup> pressure drop.

### **PM Oxidation Model and SCR-F Model**

A PM oxidation model was developed based on the shrinking core model which maintains the identity of the incoming PM masses retained in the SCRF<sup>®</sup> as compared to the SCR-F model which assumes a lumped model for the incoming PM without keeping the identity of the PM masses retained in the SCRF<sup>®</sup>. The PM oxidation model was calibrated to simulate PM oxidation with a single set of kinetics under a wide range of conditions including loading and passive oxidation conditions. The reaction rate results from the PM oxidation model were applied to the SCR-F model to simulate the pressure drop across the SCRF<sup>®</sup> and the PM retained in the SCRF<sup>®</sup>. The SCR-F model was calibrated using experimental data from Loading Tests w/o Urea to simulate the PM retained within ±2 g and pressure drop across SCRF<sup>®</sup> within ±0.5 kPa of the experimental values at the end of Stage 2. The SCR-F model was also used to estimate the cake, wall and channel pressure drop and the PM retained in the cake and wall for the Loading Tests w/o Urea to check the integrity of experimental data and the consistency of the model and the experimental data.

## **6.2 Conclusions**

The conclusions with respect to the goals and objectives of this study are given below.

- The reactivity of PM under loading conditions with and without urea injection is higher compared to the reactivity under passive oxidation with and without urea injection. As a

result, a different set of kinetics for NO<sub>2</sub> assisted oxidation is needed for loading and passive oxidation conditions using a lumped PM retained model.

- Based on the experimental data, the percentage of PM oxidized in the SCRF<sup>®</sup> increases with increasing engine load due to higher SCRF<sup>®</sup> temperatures and higher NO<sub>2</sub> concentrations. The percentage of PM retained in the SCRF<sup>®</sup> follows a decreasing trend with increasing engine load. Tests L3 Nominal and L1 Reduced do not follow this trend due to measurement errors.
- The higher PM oxidation rate without urea injection compared to with urea injection during loading conditions is attributed to the competition for NO<sub>2</sub> between the SCR reduction reactions and the PM oxidation reactions.
- On average, the reaction rate with urea injection during loading conditions in the SCRF<sup>®</sup> are 25% lower than the reaction rates without urea injection.
- The NO<sub>2</sub> assisted kinetics for PM oxidation in the SCRF<sup>®</sup> without urea injection are obtained from the SCR-F model with an activation energy of 96 kJ/gmol and pre-exponential factor of 2.6 m/K-s for the cake and 1.8 m/K-s for the wall.
- The shrinking core model used in the development of the PM oxidation model is capable of simulating PM oxidation under loading and passive oxidation conditions using a single set of kinetics. This is not possible with the standard Arrhenius model used for PM oxidation in the SCR-F model since a higher pre-exponential (A) is needed for loading conditions as compared to passive oxidation conditions.
- The SCR-F model along with the reaction rate results from the PM oxidation model is able to simulate the PM retained and SCRF<sup>®</sup> pressure drop within  $\pm 2$  g and  $\pm 0.5$  kPa respectively of the experimental values at the end of Stage 2 for the loading conditions without urea injection.

- Based on the modeling work performed, the percentage of PM oxidized in the SCRF<sup>®</sup> increases with increasing engine load due to higher SCRF<sup>®</sup> temperatures and higher NO<sub>2</sub> concentrations. The percentage of PM retained in the SCRF<sup>®</sup> follows a decreasing trend with increasing engine load. All the tests follow this trend for modeling while there are two tests that do not follow this trend for the experimental data.
- The percentage of PM oxidized in the cake and the wall also increases with the increase in engine load (increasing temperature and NO<sub>2</sub> concentrations) while PM retained in the cake and the wall follow a decreasing trend with increasing engine load. The majority of PM oxidation occurs in the PM cake and the majority of the PM is retained in the PM cake.



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## Appendix A: Mass Balance Equations and Data Analysis

This appendix discusses the equations used for the analysis of experimental data from the Loading Tests w/o and w/ Urea. The first part of this appendix focuses on the equations and assumptions used for the calculation of the clean weight of the SCRF® i.e. without any PM loading. Further, there is a discussion on the estimation of filtration efficiency during Stage 1 from the calibrated SCR-F model. The appendix ends with a detailed description of the equations used for the mass balance for the analysis of the experimental data during Stage 1 and Stage 2 of the Loading Tests.

### Clean Weight of the SCRF®

The equations used for the estimation of clean weight of the SCRF® from reference [47] for all the tests are given in the following paragraphs. The PM retained in the SCRF® at the end of Stage 1 ( $m_{retained,S1}$ ) and Stage 2 ( $m_{retained,S2}$ ) is calculated by subtracting the clean weight of the SCRF® ( $M_{clean}$ ) from the weight measurements of the SCRF® taken at the end of Stage 1 ( $M_{S1}$ ) and Stage 2 ( $M_{S2}$ ) as shown in Equations 50 and 51.

$$m_{retained,S1} = M_{S1} - M_{clean} \quad [50]$$

$$m_{retained,S2} = M_{S2} - M_{clean} \quad [51]$$

The cumulative mass balance for Stage 1 and Stage 2 can be mathematically expressed as shown in Equations 52 and 53 respectively.

$$m_{in,S1} - m_{retained,S1} - m_{ox,S1} - m_{out,S1} = 0 \quad [52]$$

$$m_{retained,S1} + m_{in,S2} - m_{retained,S2} - m_{ox,S2} - m_{out,S2} = 0 \quad [53]$$

where,  $m_{in,S1}$  and  $m_{in,S2}$  is the cumulative PM entering the SCRF® (g),  $m_{ox,S1}$  and  $m_{ox,S2}$  is the cumulative PM oxidized (g),  $m_{retained,S1}$  and  $m_{retained,S2}$  is the PM retained (g),  $m_{out,S1}$  and  $m_{out,S2}$  is the cumulative PM exiting the SCRF® (g) during Stage 1 and Stage 2 respectively.

The average filtration efficiency during Stage 1 and Stage 2 is given by Equations 54 and 55 respectively.

$$\bar{\eta}_{S1} = \frac{m_{in,S1} - m_{out,S1}}{m_{in,S1}} \quad [54]$$

$$\bar{\eta}_{S2} = \frac{m_{in,S2} - m_{out,S2}}{m_{in,S2}} \quad [55]$$

Substituting Equation 50 into Equation 52 and rearranging the terms, results in the following equation.

$$m_{retained,S1} = m_{in,S1} - m_{ox,S1} - m_{out,S1} = M_{S1} - M_{clean}$$

or

$$(m_{in,S1} - m_{out,S1}) - m_{ox,S1} = M_{S1} - M_{clean} \quad [56]$$

Substituting Equation 54 in Equation 56, results in the following equation.

$$\bar{\eta}_{S1} m_{in,S1} - m_{ox,S1} = M_{S1} - M_{clean}$$

or

$$M_{clean} = M_{S1} - \bar{\eta}_{S1} m_{in,S1} + m_{ox,S1}$$

or

$$m_{ox,S1} = \bar{\eta}_{S1} m_{in,S1} - (M_{S1} - M_{clean})$$

or

$$\frac{m_{ox,S1}}{m_{in,S1}} = \bar{\eta}_{S1} - \frac{(M_{S1} - M_{clean})}{m_{in,S1}} \quad [57]$$

Rearranging the terms in Equation 53, results in the following equation.

$$m_{ox,S2} = (m_{in,S2} - m_{out,S2}) + m_{retained,S1} - m_{retained,S2} \quad [58]$$

Now, substituting Equation 55 into Equation 58, results in the following equation.

$$m_{ox,S2} = \bar{\eta}_{S2}m_{in,S2} + m_{retained,S1} - m_{retained,S2} \quad [59]$$

Again, substituting Equations 50 and 51 into Equation 59, results in the following equation.

$$m_{ox,S2} = \bar{\eta}_{S2}m_{in,S2} - (M_{S1} - M_{clean}) - (M_{S2} - M_{clean})$$

or

$$m_{ox,S2} = \bar{\eta}_{S2}m_{in,S2} - (M_{S2} - M_{S1})$$

or

$$\frac{m_{ox,S2}}{m_{in,S2}} = \bar{\eta}_{S2} - \frac{(M_{S2} - M_{S1})}{m_{in,S2}} \quad [60]$$

Now, subtracting Equation 57 from Equation 60, results in the following equation.

$$\frac{m_{ox,S2}}{m_{in,S2}} - \frac{m_{ox,S1}}{m_{in,S1}} = \bar{\eta}_{S2} - \frac{(M_{S2} - M_{S1})}{m_{in,S2}} - \bar{\eta}_{S1} + \frac{(M_{S1} - M_{clean})}{m_{in,S1}}$$

Rearranging the terms, results in Equation 61 which is used for the calculation of clean weight of the SCRF®.

$$M_{clean} = M_{S1} - \left( \bar{\eta}_{S1}m_{in,S1} - \left( \bar{\eta}_{S2} - \frac{M_{S2} - M_{S1}}{m_{in,S2}} \right) m_{in,S1} \right) - \left( \frac{m_{ox,S2}}{m_{in,S2}} - \frac{m_{ox,S1}}{m_{in,S1}} \right) m_{in,S1} \quad [61]$$

In the Equations 54 to 61, the cumulative PM mass entering the SCRF® during Stage 1 ( $m_{in,S1}$ ) and Stage 2 ( $m_{in,S2}$ ) is calculated using Equation 62 and 63.



$$m_{in,S1} = \frac{c_{in,S1}}{1000} * \frac{\dot{m}_{exhaust,S1}}{\rho_{Std}} * t_{S1} \quad [62]$$

$$m_{in,S2} = \frac{c_{in,S2}}{1000} * \frac{\dot{m}_{exhaust,S2}}{\rho_{Std}} * t_{S2} \quad [63]$$

where,  $c_{in,S1}$  and  $c_{in,S2}$  is the PM concentration (mg/scm),  $\dot{m}_{exhaust,S1}$  and  $\dot{m}_{exhaust,S2}$  is the exhaust flow rate (kg/min),  $t_{S1}$  and  $t_{S2}$  is the duration (min) of Stage 1 and Stage 2 and  $\rho_{Std}$  is the exhaust density at standard atmospheric conditions.

For the calculation of  $M_{clean}$  according to Equation 61, the average filtration efficiency for Stage 1 ( $\bar{\eta}_{S1}$ ) and the ratio of PM oxidized and PM entering during Stage 1 ( $m_{ox,S1}/m_{in,S1}$ ) and Stage 2 ( $m_{ox,S2}/m_{in,S2}$ ) are estimated from the calibrated SCR-F model. Experimental values are used for all the other variables in Equation 61. Equation 61 is used to calculate the clean weight of SCR-F<sup>®</sup> which is then used in Equations 50 and 51 along with the SCR-F<sup>®</sup> weight measurements i.e.  $M_{S1}$  and  $M_{S2}$  to calculate the PM mass retained at the end of Stage 1 and Stage 2 respectively.

### **Stage 1 Average Filtration Efficiency and $m_{ox}/m_{in}$ Ratio for Stage 1 and Stage 2**

The value of average filtration efficiency during Stage 1 for all the Loading Tests was estimated from the calibrated SCR-F model with an iterative process explained in the following paragraph.

For the first iteration, the filtration efficiency for Stage 1 was assumed to be 58.6% based on the previous modeling data from the MTU 1-D model [48]. Also, the ratio of cumulative PM oxidized and cumulative PM entering during Stage 1 ( $m_{ox,S1}/m_{in,S1}$ ) and Stage 2 ( $m_{ox,S2}/m_{in,S2}$ ) was assumed equal, to calculate the  $M_{clean}$  using Equation 61. However, this ratio is not equal as observed from the modeling data which is discussed later. The values of PM retained at the end of Stage 1 and Stage 2 for all the Loading Tests were then calculated using these two assumptions.

Next, the SCR-F model was calibrated to model the PM retained at the end of Stage 1 and Stage 2 within  $\pm 2$  g of the experimental values. Once the SCR-F model was calibrated, the average filtration efficiency for Stage 1 was estimated as the average of the filtration efficiency from the

SCR-F model for the duration of Stage 1 for each Loading Test. Also, the ratio of cumulative PM oxidized and cumulative PM entering during Stage 1 ( $m_{ox,S1}/m_{in,S1}$ ) and Stage 2 ( $m_{ox,S2}/m_{in,S2}$ ) was calculated using the SCR-F model for each Loading Test.

Table A.1 gives the values of average filtration efficiency for Stage 1, and the ratio of cumulative PM oxidized and cumulative PM entering for Stage 1 and Stage 2 which are not equal, for all the Loading Tests without Urea. The same values were assumed for the Loading Tests w/ Urea.

*Table A.1: Estimation of Stage 1 Filtration Efficiency and Ratio of PM Oxidized and PM Entering for Stage 1 and Stage 2 Using Calibrated SCR-F Model*

Test	Stage 1 Filt. Eff. ( $\bar{\eta}_{S1}$ )	Stage 1			Stage 2		
		$m_{ox}$	$m_{in}$	$m_{ox}/m_{in}$	$m_{ox}$	$m_{in}$	$m_{ox}/m_{in}$
[-]	[%]	[g]	[g]	[-]	[g]	[g]	[-]
<b>L1 Nom</b>	61.6	0.08	1.93	0.042	4.3	19.3	0.225
<b>L1 Red</b>	66.3	0.21	3.49	0.060	8.24	32.7	0.252
<b>L2 Nom</b>	59.8	0.14	1.89	0.075	5.6	18.9	0.296
<b>L2 Red</b>	64.3	0.28	3.36	0.084	9.8	33.5	0.292
<b>L3 Nom</b>	57.0	0.22	1.78	0.126	7.1	17.2	0.413
<b>L3 Red</b>	61.9	0.54	3.51	0.153	14.4	33.2	0.434
<b>L4 Nom</b>	55.4	0.29	1.79	0.159	10.4	17.9	0.582
<b>L4 Red</b>	59.6	0.60	3.51	0.169	19.5	34.2	0.570

In the next iteration, the value of Stage 1 filtration efficiency and  $m_{ox}/m_{in}$  for Stage 1 and Stage 2 from Table A.1 are used to calculate the clean weight of the SCR-F<sup>®</sup> using Equation 61. The calculated value of  $M_{clean}$ , the SCR-F<sup>®</sup> weight measurements and the PM retained at the end of Stage 1 and Stage 2 for all the tests are listed in Table A.2.

It is important to note that the value of SCR-F<sup>®</sup> clean weight is different for each test as seen in Table A.2. This difference is due to breaking of thermocouple probes on the SCR-F<sup>®</sup> in between the tests which affects the SCR-F<sup>®</sup> weight measurements. Any SCR-F<sup>®</sup> thermocouple that broke in between the stages in a particular test was noted down and placed on the scale while weighing the SCR-F<sup>®</sup> to ensure correct difference in weight measurements between Stage 1 and Stage 2.

Table A.2: SCRF® Weights and PM Retained in Stage 1 and Stage 2

Test	M <sub>clean</sub>	M <sub>S1</sub>	M <sub>S2</sub>	m <sub>retained,S1</sub>	m <sub>retained,S2</sub>
[-]	[g]	[g]	[g]	[g]	[g]
L1 Nominal	19693.0	19694.1	19709.1	1.1	16.1
L1 Nominal w/ Urea	19714.4	19715.5	19732.0	1.1	17.6
L1 Reduced <sup>#</sup>	19710.2	19712.2	19735.6	2.0	25.4
L1 Reduced w/ Urea	19712.1	19714.4	19743.9	2.3	31.8
L2 Nominal	19718.4	19719.2	19729.9	0.8	11.5
L2 Reduced	19718.3	19720.4	19745.1	2.1	26.8
L3 Nominal	19704.4	19704.9	19712.1	0.6	7.8
L3 Nominal w/ Urea	19706.2	19707.1	19718.6	0.9	12.4
L3 Reduced	19710.5	19712.2	19730.5	1.7	20.0
L3 Reduced w/ Urea	19691.8	19693.9	19716.4	2.1	24.6
L4 Nominal	19690.9	19691.7	19699.4	0.8	8.5
L4 Reduced	19681.1	19682.6	19696.1	1.5	15.0

<sup>#</sup>Data obtained from Test PO-C in reference [11]

## Appendix B: Validation Test for NO Conversion across DOC

This appendix discusses about the validation test which was performed to ensure proper functioning of the DOC since some of the Loading Test had a relatively low NO conversion (<20%).

The validation test was performed at fixed engine conditions - engine speed (1200 RPM), load (120 Nm) and exhaust flow rate (5 kg/min). The 25 kW Exhaust Heater was used to increase the temperature of the exhaust in steps of 20°C and the DOC inlet temperature was allowed to stabilize. Once stabilized, emission samples were taken using the Mass Spectrometer for a period of 15 min each at UDOC and DDOC for each of the heater temperature set points at steady state conditions.

Table B.1 shows the NO, NO<sub>2</sub>, and NO<sub>x</sub> values at the DOC inlet and outlet which are used to calculate the NO conversion across the DOC. The NO conversion and NO<sub>2</sub>/NO<sub>x</sub> ratio is given in Table B.1 for all set points.

*Table B.1: NO Conversion Across DOC – Validation Test*

Heater Temp.	DOC In Temp.	DOC Out Temp.	DOC Inlet			DOC Outlet			NO Conv.	NO <sub>2</sub> /NO <sub>x</sub> Ratio
			NO <sub>2</sub>	NO	NO <sub>x</sub>	NO <sub>2</sub>	NO	NO <sub>x</sub>		
[°C]	[°C]	[°C]	[ppm]	[ppm]	[ppm]	[ppm]	[ppm]	[ppm]	[%]	[-]
200	180	193	20	170	190	16	169	185	1	0.09
220	199	213	21	173	194	40	145	185	16	0.22
240	216	231	22	173	195	58	124	182	28	0.32
260	232	251	22	178	200	77	111	188	38	0.41
280	250	270	20	181	201	85	96	181	47	0.47
300	267	289	20	183	203	92	94	186	49	0.49
320	285	308	19	187	206	99	89	188	52	0.53
340	302	327	18	193	211	104	85	189	56	0.55
360	319	346	17	196	213	106	86	192	56	0.55
380	337	366	15	196	211	102	88	190	55	0.54
400	354	384	14	193	207	94	97	191	50	0.49
420	368	400	12	190	202	87	104	191	45	0.46

The NO conversion across DOC is plotted against the DOC inlet temperature as shown in Figure B.1. The trend of NO conversion with DOC inlet temperature shown in Figure B.1 is in agreement with references in the literature where the peak NO conversion is in the range of 300-350 °C DOC inlet temperature. Hence, it was confirmed that the DOC is performing its function properly and so there was no need to change the DOC for further Loading Tests as was done by reference [8].

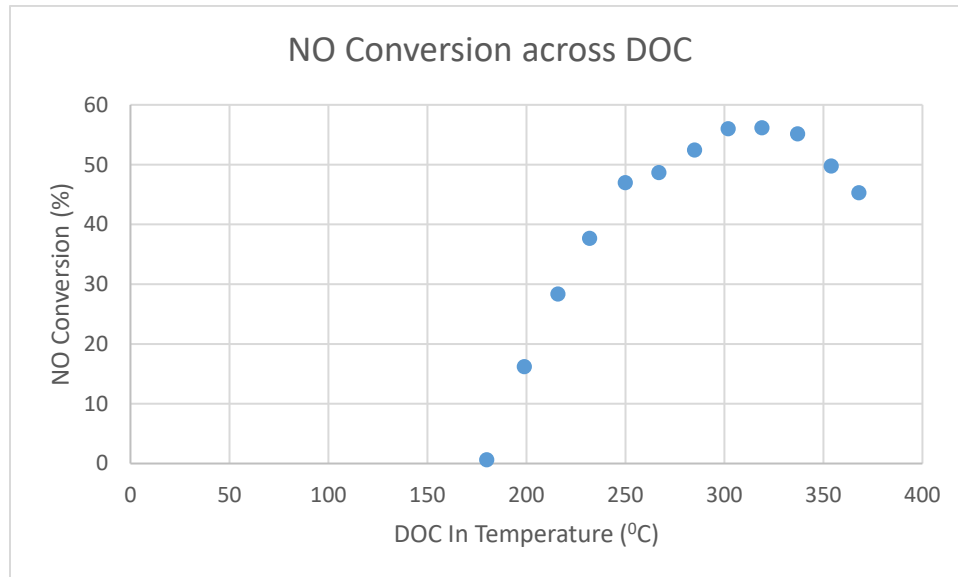


Figure B.1: NO Conversion Across DOC vs DOC Inlet Temperature

## Appendix C: Experimental Pressure Drop Plots

This appendix contains the plots for pressure drop across SCRF® vs time for each of the Loading Tests performed in this study. It also shows the comparison of pressure drop across SCRF® for Loading Tests w/o and w/ Urea in Figure C.9 to Figure C.12.

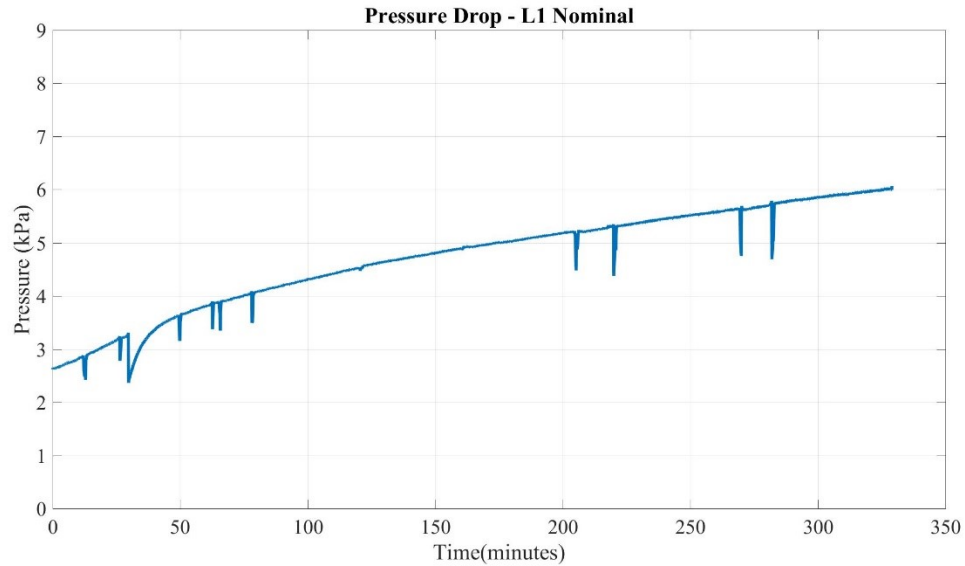


Figure C.1: SCRF® Pressure Drop vs Time for L1 Nominal

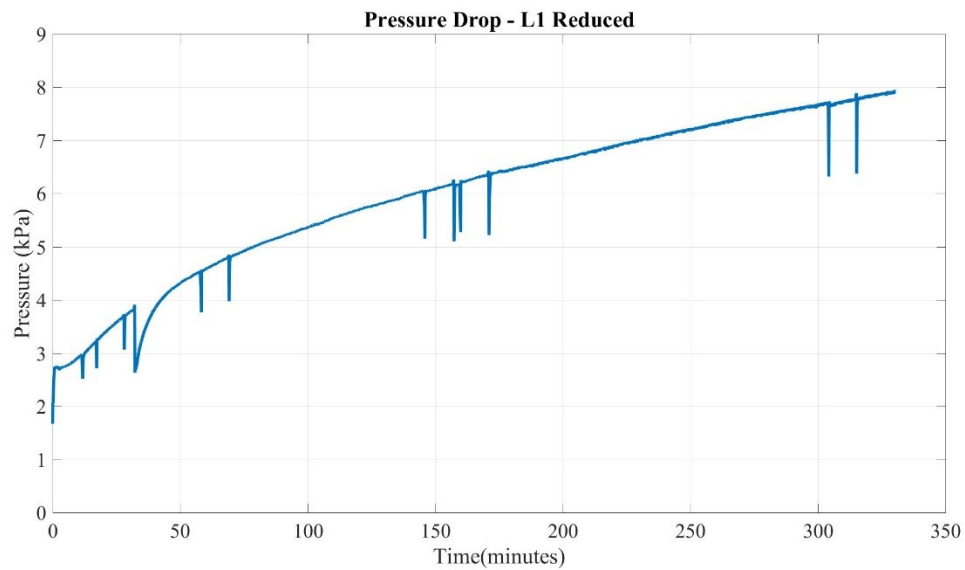


Figure C.2: SCRF® Pressure Drop vs Time for L1 Reduced [11]

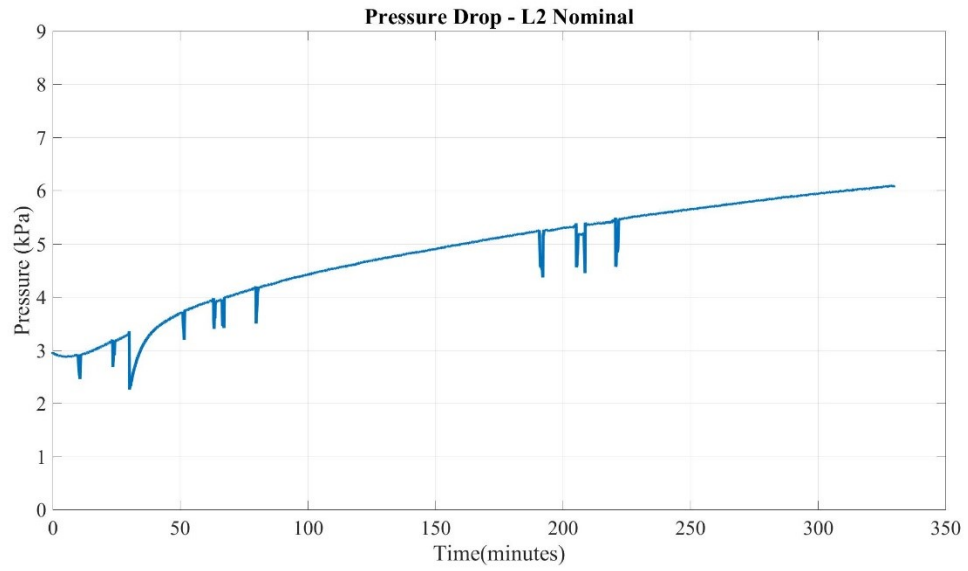


Figure C.3: SCRF® Pressure Drop vs Time for L2 Nominal

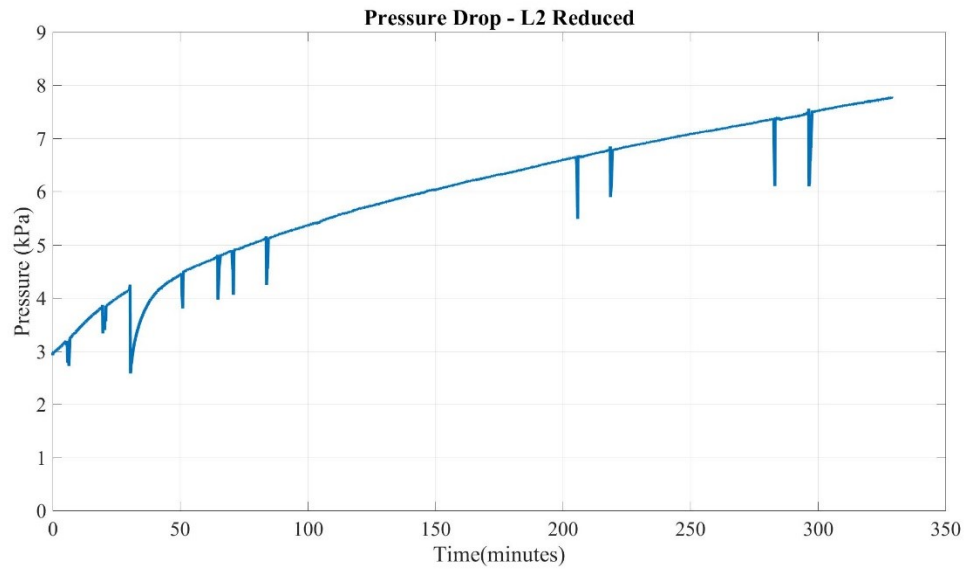


Figure C.4: SCRF® Pressure Drop vs Time for L2 Reduced

The peak in pressure drop across SCRF® towards the end of Stage 2 in between 250-300 mins for L3 Nominal shown in Figure C.5 is because of the unexpected active regeneration event explained earlier.

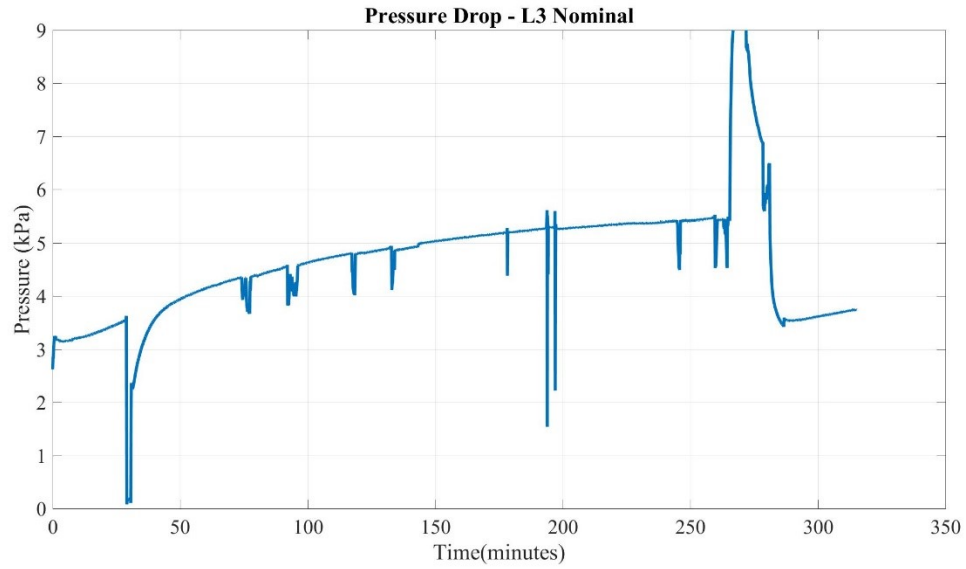


Figure C.5: SCRF® Pressure Drop vs Time for L3 Nominal

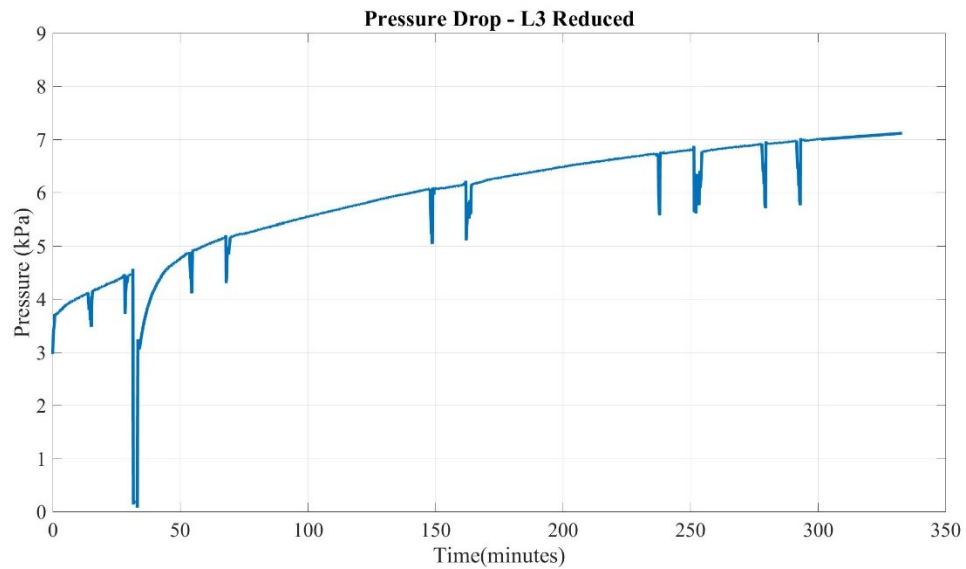


Figure C.6: SCRF® Pressure Drop vs Time for L3 Reduced



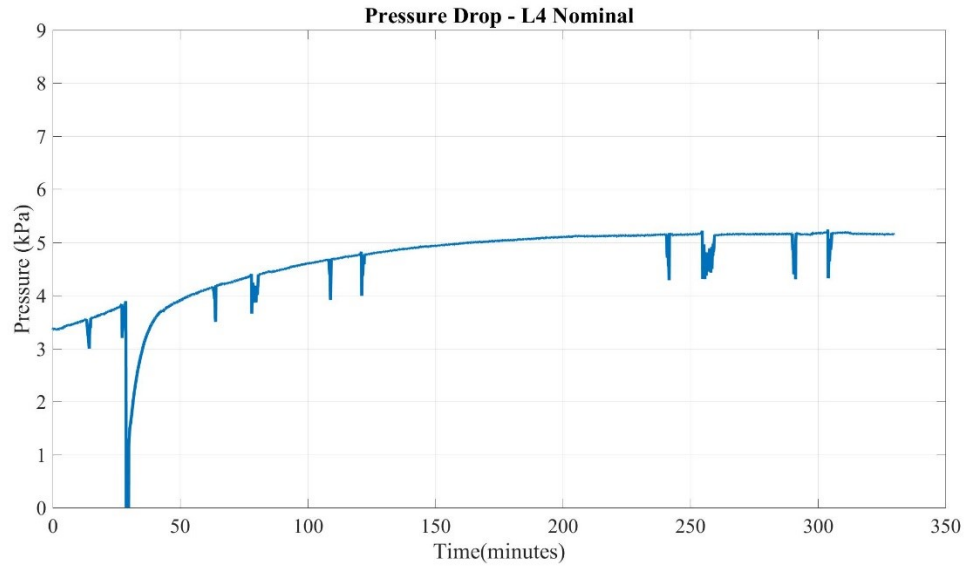


Figure C.7: SCRF® Pressure Drop vs Time for L4 Nominal

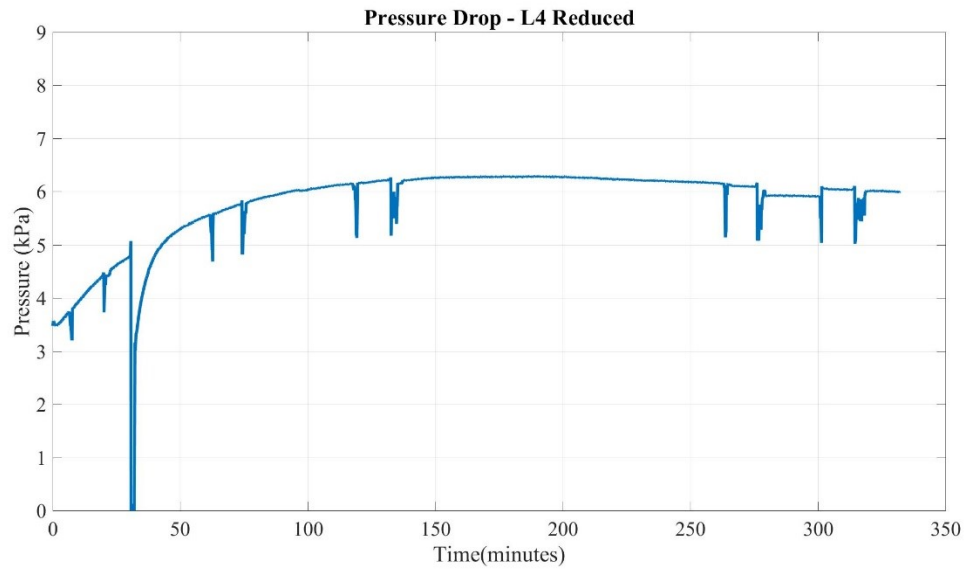


Figure C.8: SCRF® Pressure Drop vs Time for L4 Reduced

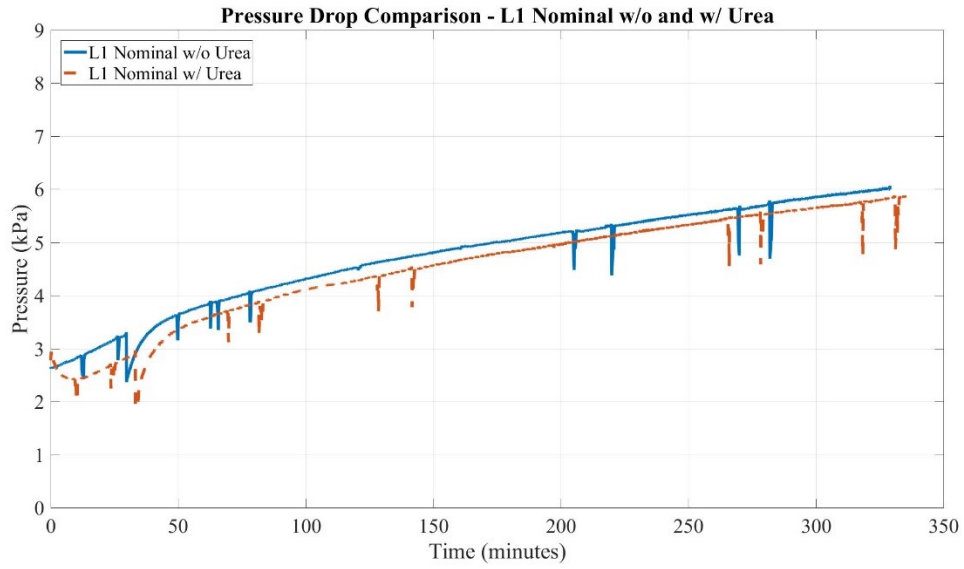


Figure C.9: SCRF® Pressure Drop Comparison for L1 Nominal w/o and w/ Urea

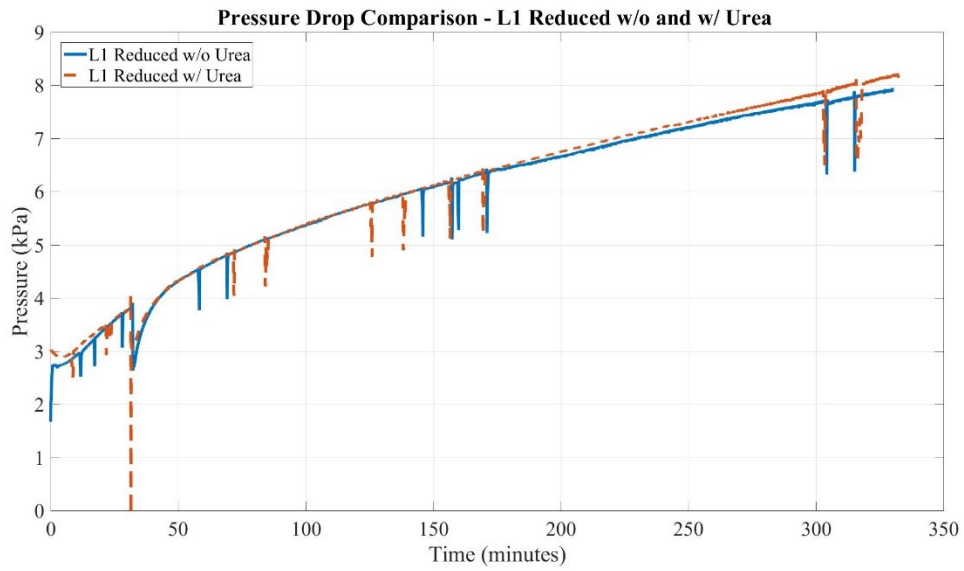


Figure C.10: SCRF® Pressure Drop Comparison for L1 Reduced w/o and w/ Urea

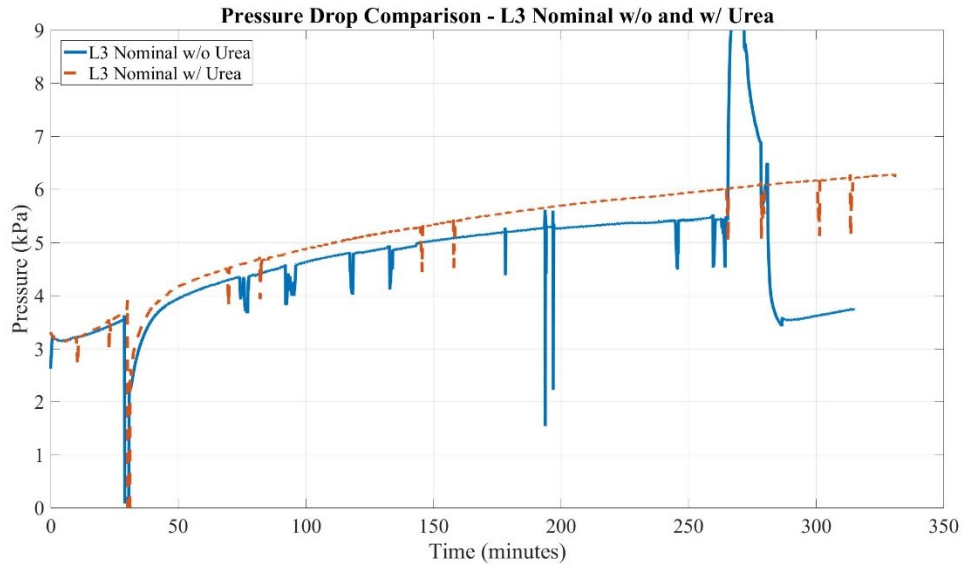


Figure C.11: SCR® Pressure Drop Comparison for L3 Nominal w/o and w/ Urea

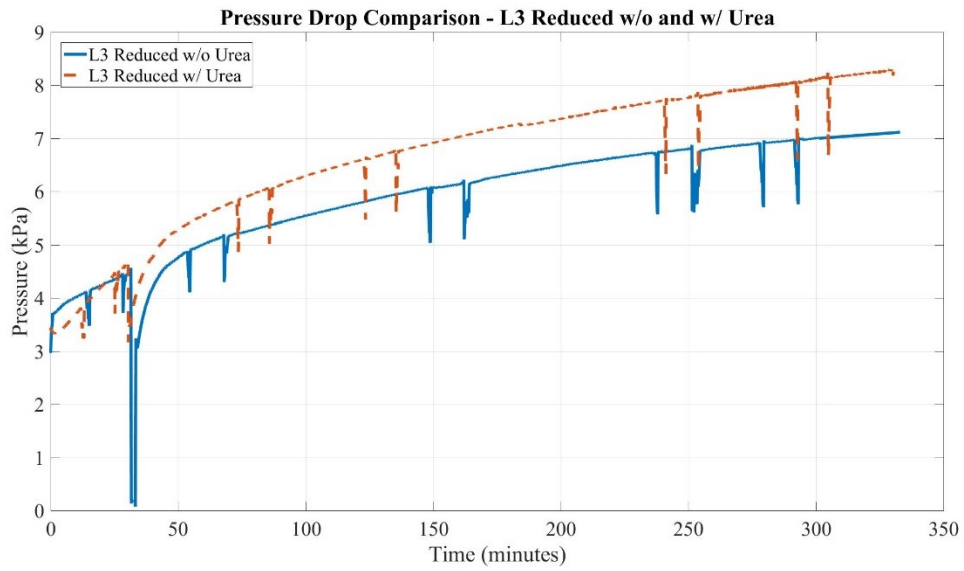


Figure C.12: SCR® Pressure Drop Comparison for L3 Reduced w/o and w/ Urea

## Appendix D: Temperature Distribution Plots

This appendix presents plots for experimental temperature distribution in the SCRF<sup>®</sup> for all the tests for Stage 2 at a time when the temperatures have stabilized. The plots for temperature distribution in the SCRF<sup>®</sup> predicted by SCR-F model are also given for all the tests for comparison with the experimental temperature data.

As discussed earlier in subsection 3.1.3, twenty thermocouples, namely S1-S20 were instrumented in the SCRF<sup>®</sup> at different axial and radial locations according to the layout shown in Figure 3.3. Each plot shows the temperature distribution in the SCRF<sup>®</sup> generated using the temperature data collected from these twenty thermocouples. The X-axis represents the axial length (mm) from the start of the SCRF<sup>®</sup> and the Y-axis represents the radial distance (mm) from the center of the SCRF<sup>®</sup>. The lines on the plot represent isotherms which divide the SCRF<sup>®</sup> into different temperature zones. The thermocouples were instrumented only in one half of the SCRF<sup>®</sup> and so the temperature distribution in top half has been mirrored about the X-axis to generate the temperature distribution for the entire volume of SCRF<sup>®</sup>. The white circles on the experimental plots represent broken thermocouple at that location where the temperature data has been estimated using linear interpolation/extrapolation within the axial zone.

For Loading Tests w/o Urea, the difference in temperature along the length of the SCRF<sup>®</sup> is negligible as observed from the experimental plots. However, there is decrease in temperature radially moving out from the center of the SCRF<sup>®</sup>. The reason for this is the heat transfer to the ambient at the outer surface of the SCRF<sup>®</sup>. The plots from the SCR-F model show similar trend where the temperature is decreasing radially from the center for the Loading Tests w/o Urea. The differences in the value of temperature at certain locations when comparing the experimental plot to the plot from SCR-F model might be due to incorrect estimation of the temperature for the broken thermocouple. However, the overall trend between the experimental and SCR-F model plot is similar.

For Loading Tests w/ Urea, it is observed that the temperature increases along the length of the SCRF<sup>®</sup>. Similar trend was also observed by references [8, 11] for passive oxidation with urea injection. The increase in the temperature along the length in the second half of the SCRF<sup>®</sup> is because of the exothermic reactions taking place due to urea injection. Also, there is a decrease

in temperature radially from the center due to heat transfer to the ambient. The experimental plots for L1 Nominal and L3 Reduced with Urea are not shown here since the temperature at some locations could not be estimated due to the fact that there were a higher number of broken thermocouples in a single axial zone in the SCRF®.

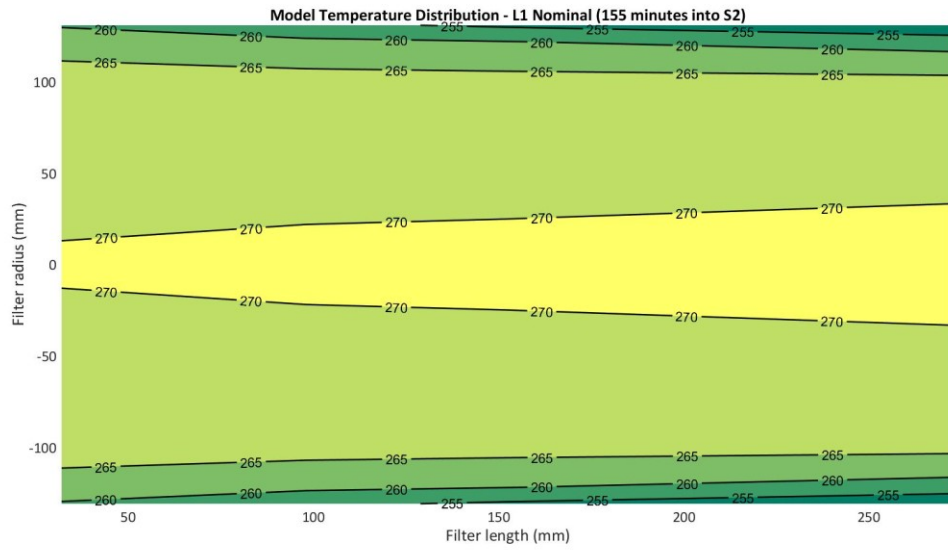


Figure D.1: SCRF® Model Temperature Distribution for L1 Nominal (155 minutes into S2)

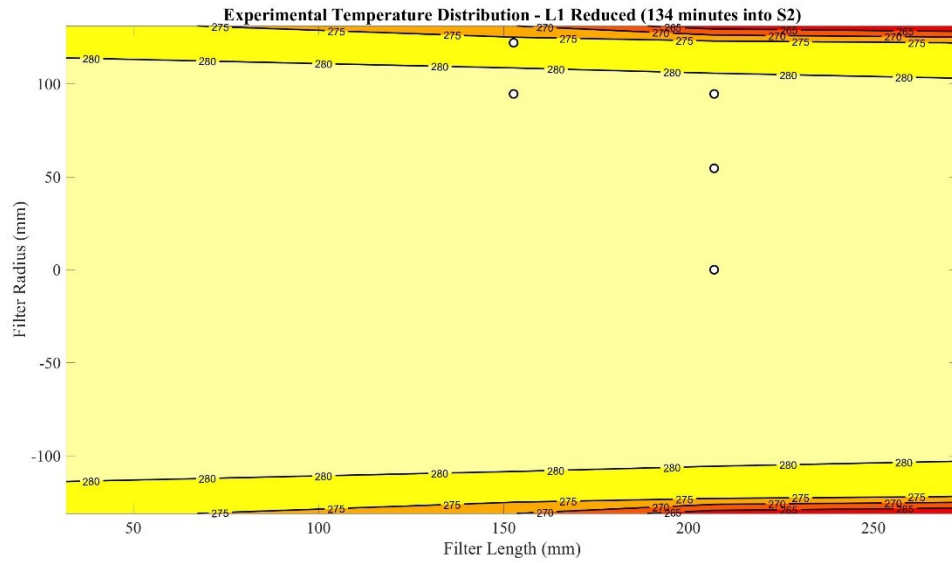


Figure D.2: SCRF® Experimental Temperature Distribution for L1 Reduced (134 minutes into S2)

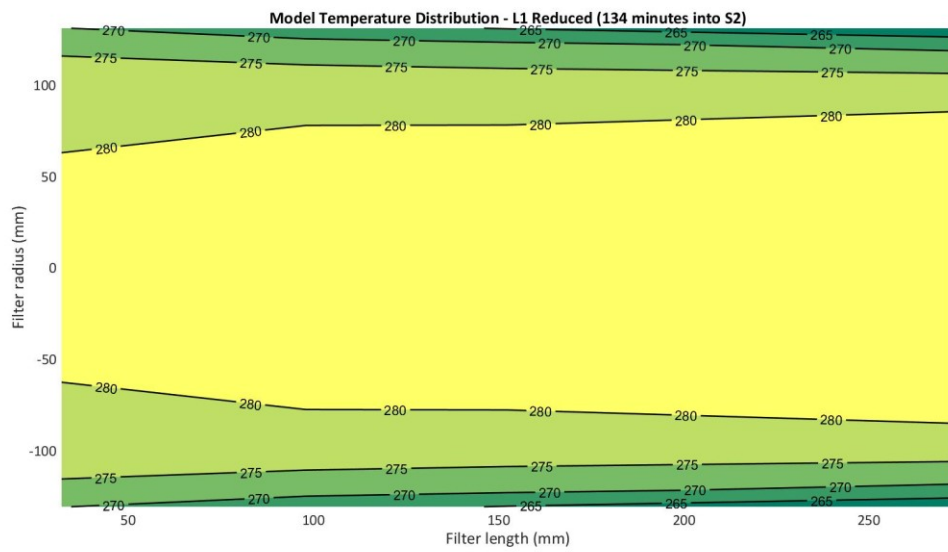


Figure D.3: SCRF® Model Temperature Distribution for L1 Reduced (134 minutes into S2)

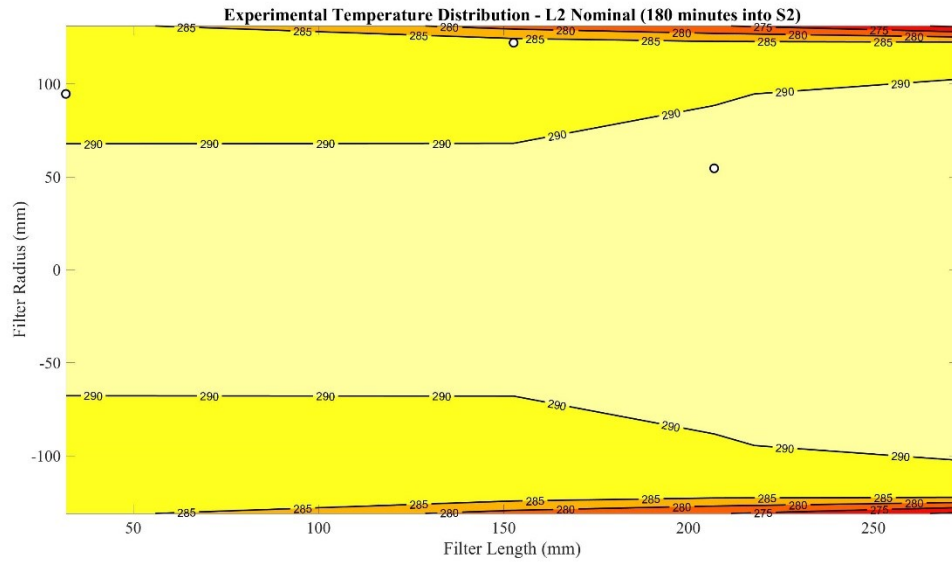


Figure D.4: SCRF® Experimental Temperature Distribution for L2 Nominal (180 minutes into S2)

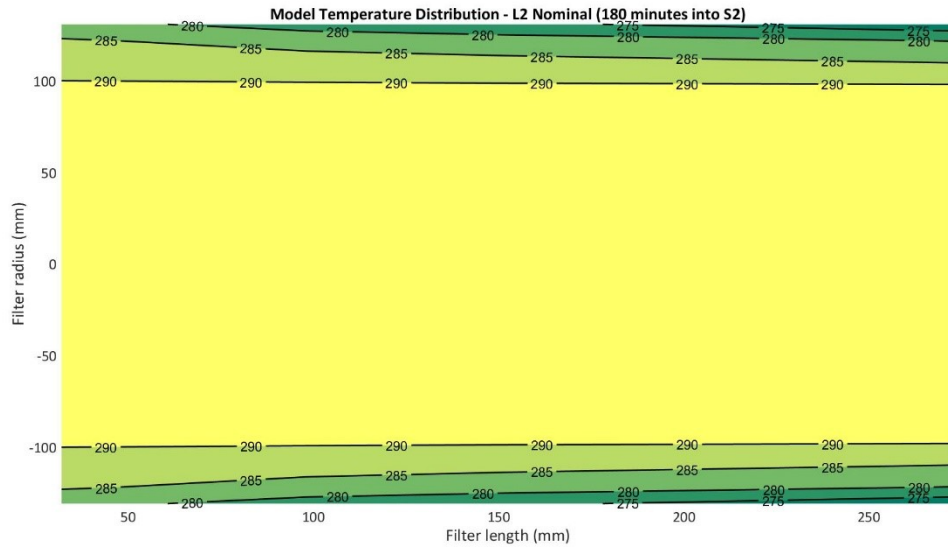


Figure D.5: SCRF® Model Temperature Distribution for L2 Nominal (180 minutes into S2)

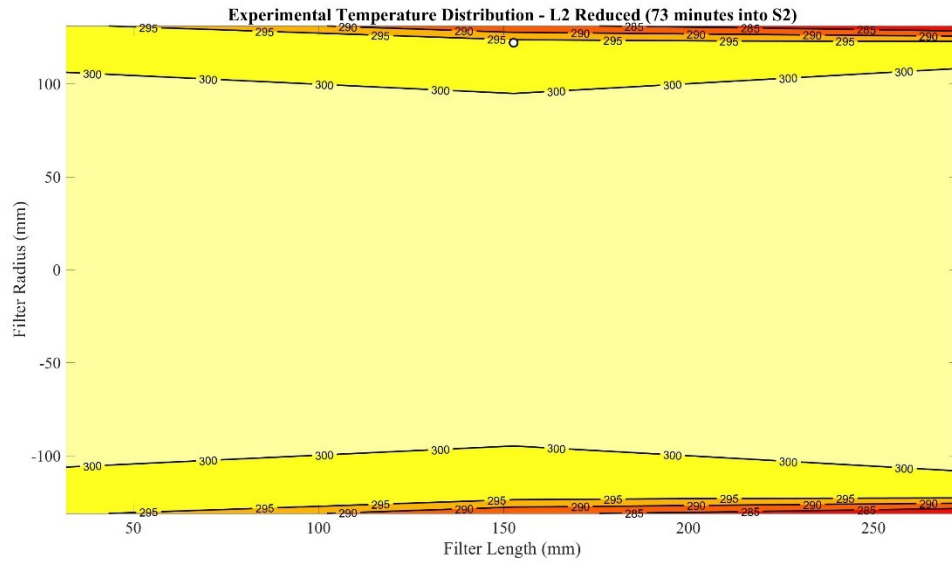


Figure D.6: SCRF® Experimental Temperature Distribution for L2 Reduced (73 minutes into S2)

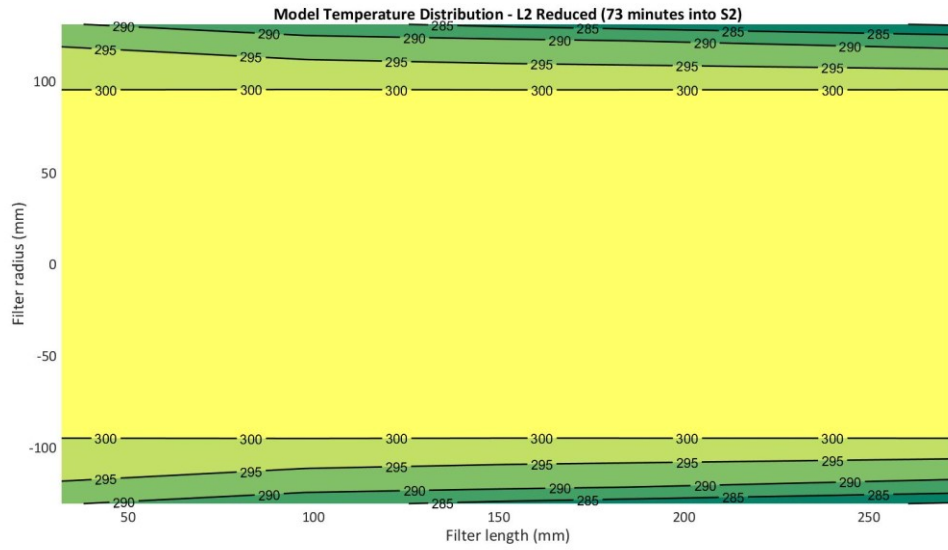


Figure D.7: SCRF® Model Temperature Distribution for L2 Reduced (73 minutes into S2)



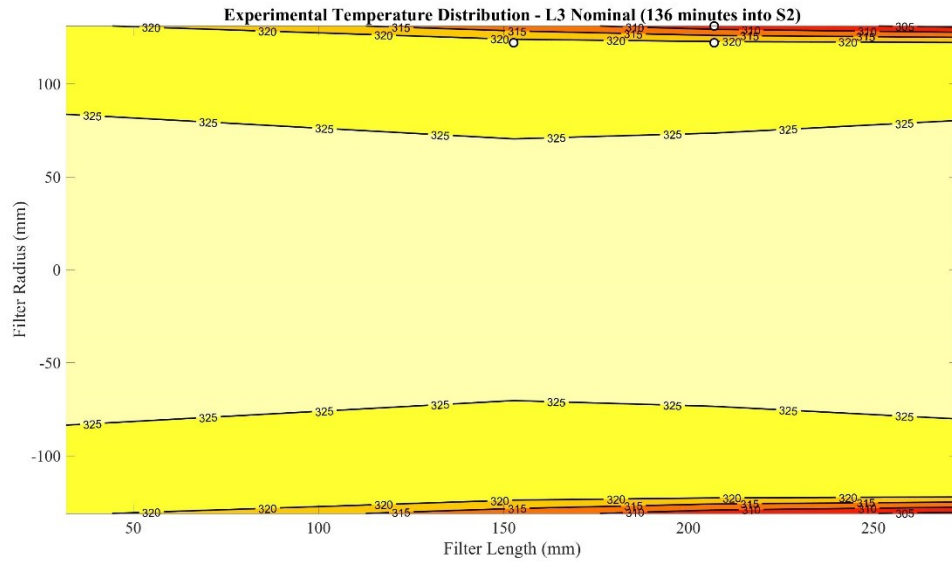


Figure D.8: SCRF® Experimental Temperature Distribution for L3 Nominal (136 minutes into S2)

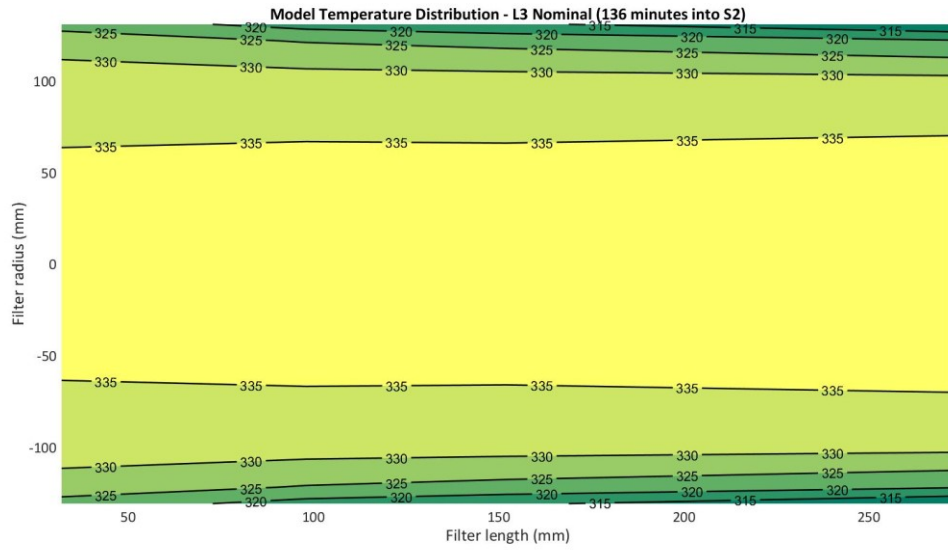


Figure D.9: SCRF® Model Temperature Distribution for L3 Nominal (136 minutes into S2)

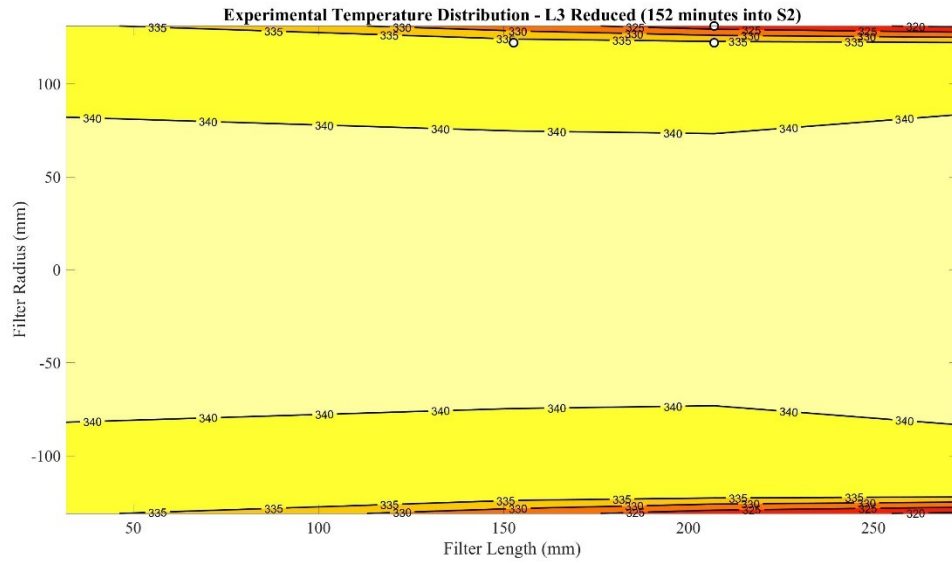


Figure D.10: SCRF® Experimental Temperature Distribution for L3 Reduced (152 minutes into S2)

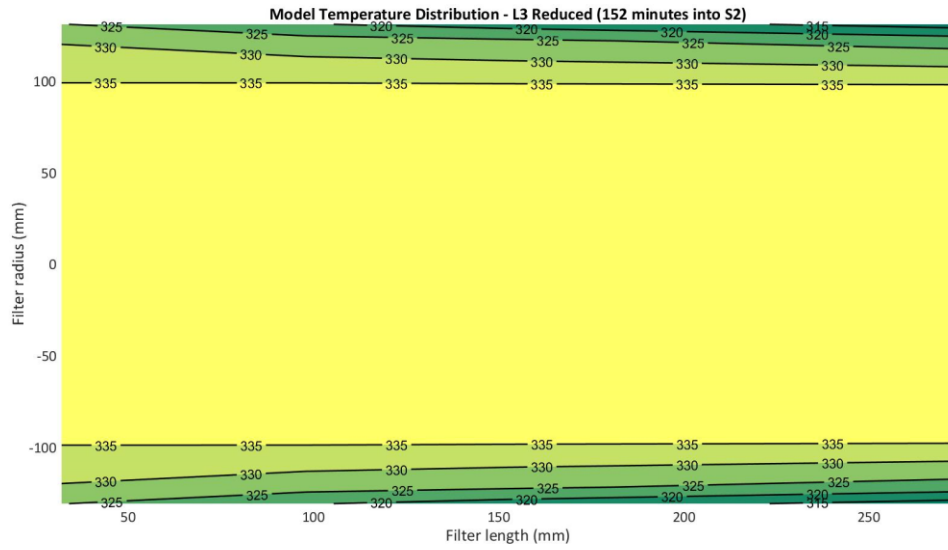


Figure D.11: SCRF® Model Temperature Distribution for L3 Reduced (152 minutes into S2)

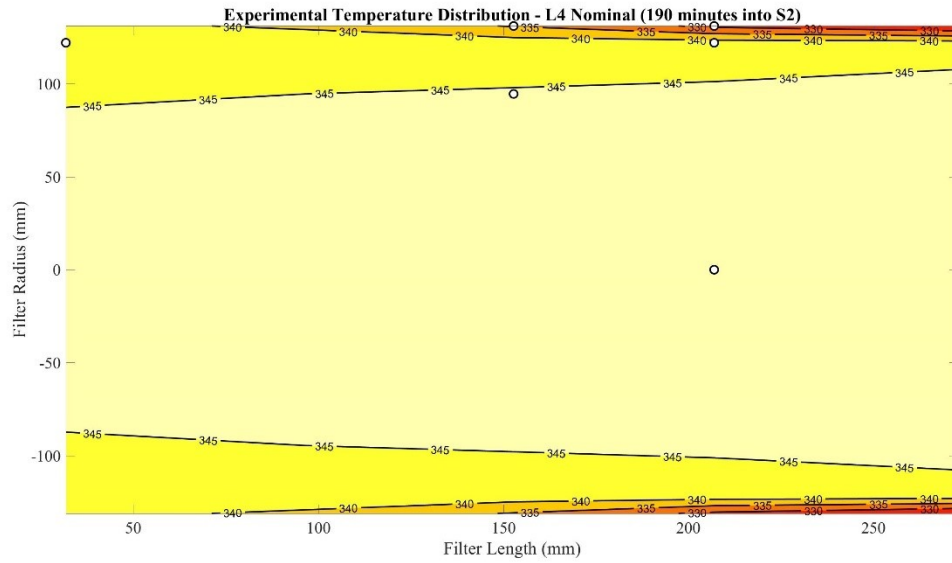


Figure D.12: SCRF® Experimental Temperature Distribution for L4 Nominal (190 minutes into S2)

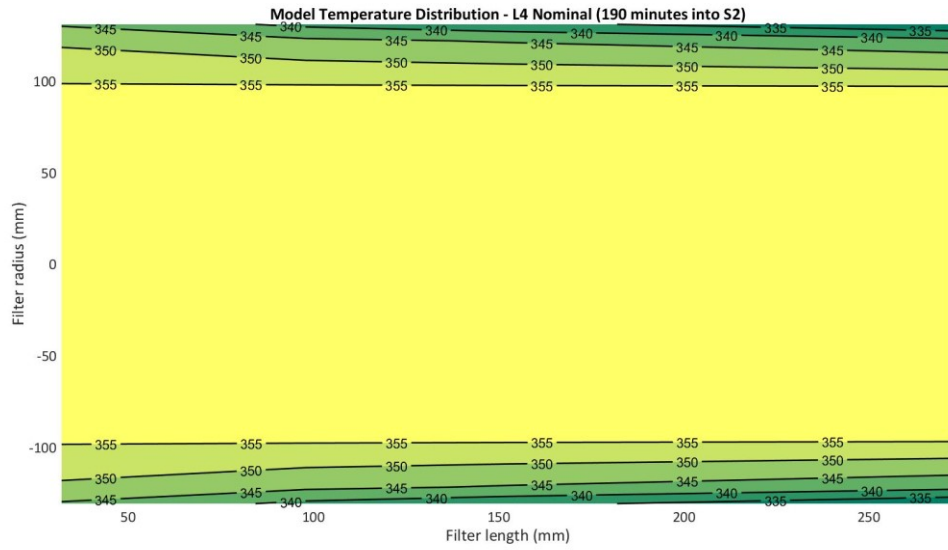


Figure D.13: SCRF® Model Temperature Distribution for L4 Nominal (190 minutes into S2)

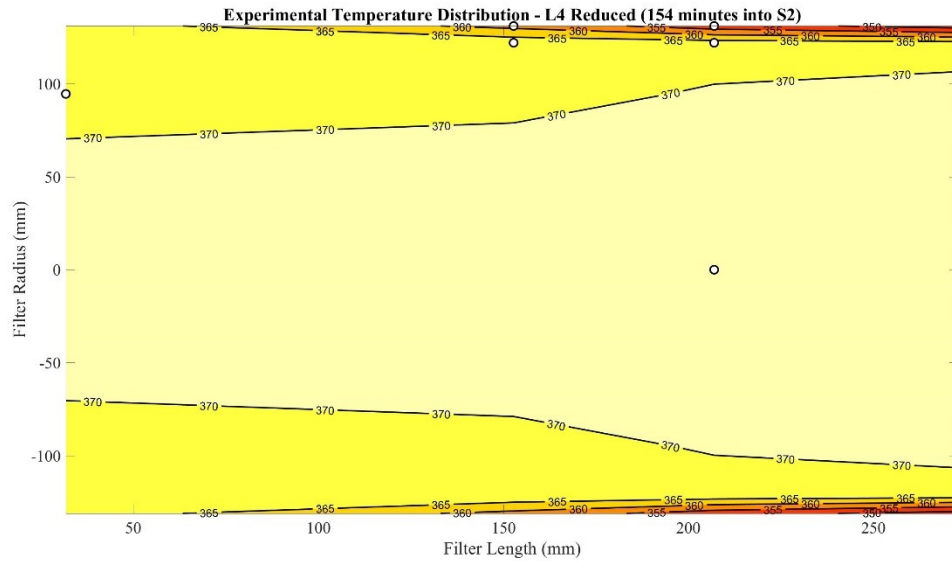


Figure D.14: SCRF® Experimental Temperature Distribution for L4 Reduced (154 minutes into S2)

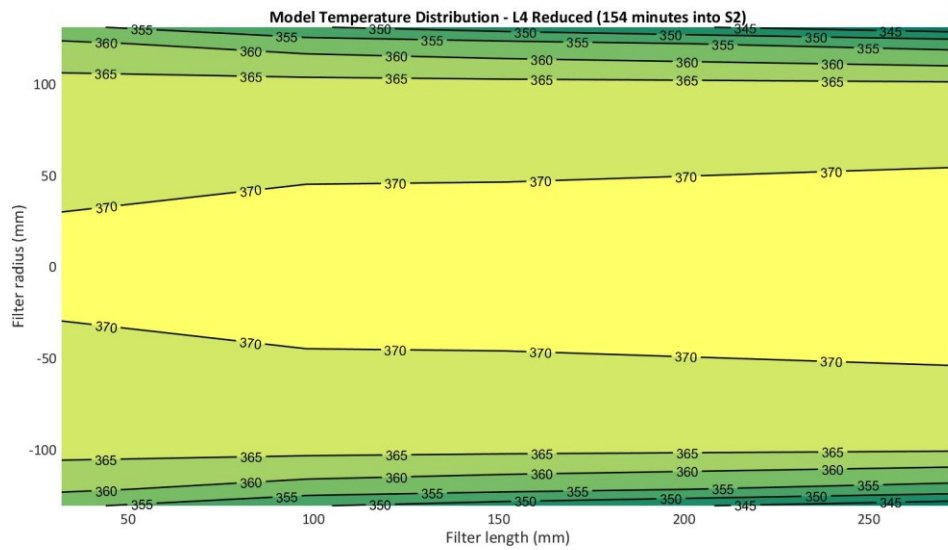


Figure D.15: SCRF® Model Temperature Distribution for L4 Reduced (154 minutes into S2)

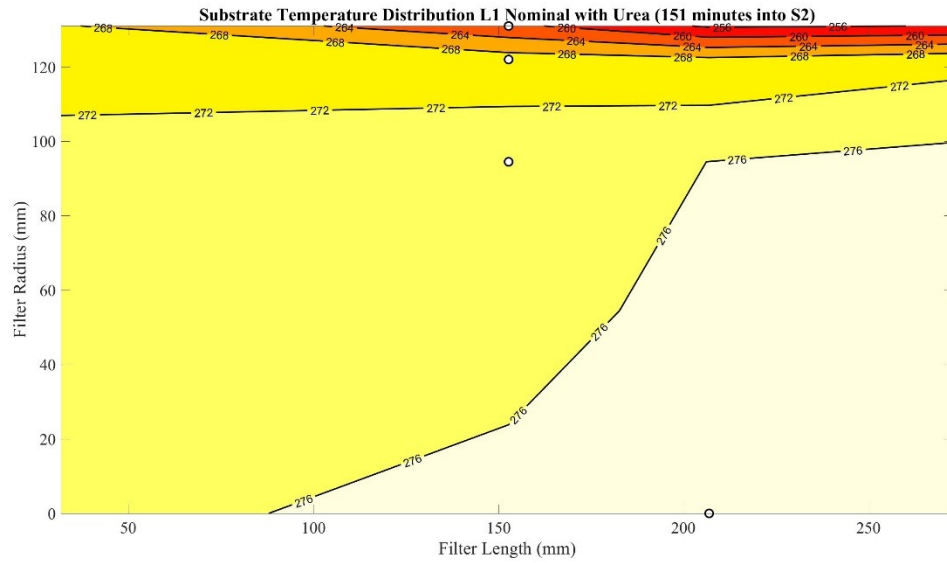


Figure D.16: SCRF® Experimental Temperature Distribution for L1 Nominal with Urea (151 minutes into S2)

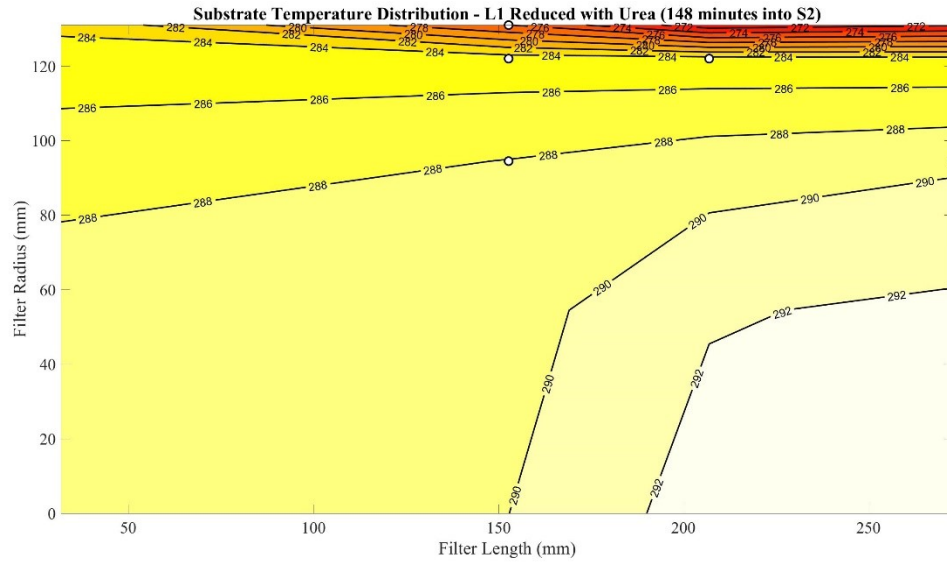


Figure D.17: SCRF® Experimental Temperature Distribution for L1 Reduced with Urea (148 minutes into S2)

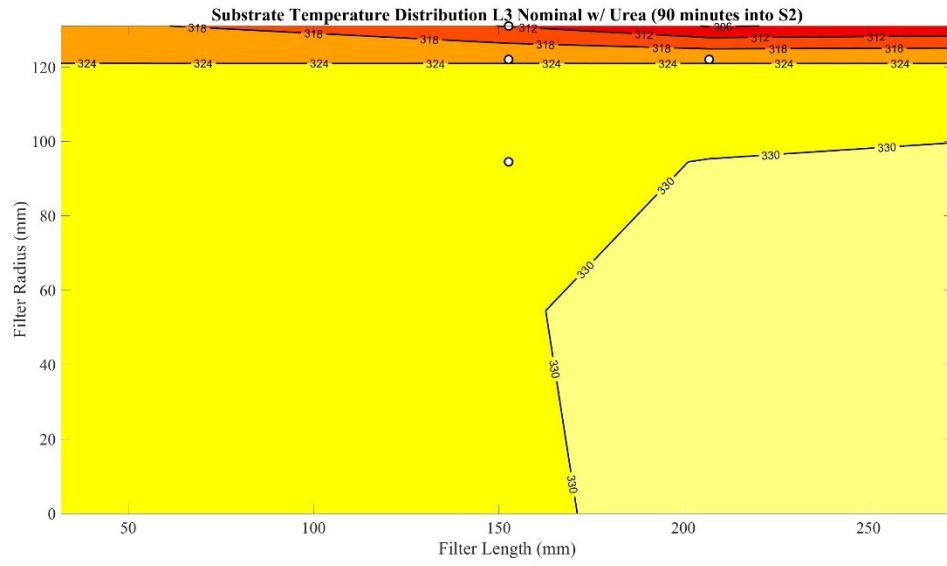


Figure D.18: SCRF® Experimental Temperature Distribution for L3 Nominal with Urea (90 minutes into S2)

## Appendix E: Model PM Mass Retained Plots for Loading Tests w/o Urea Data

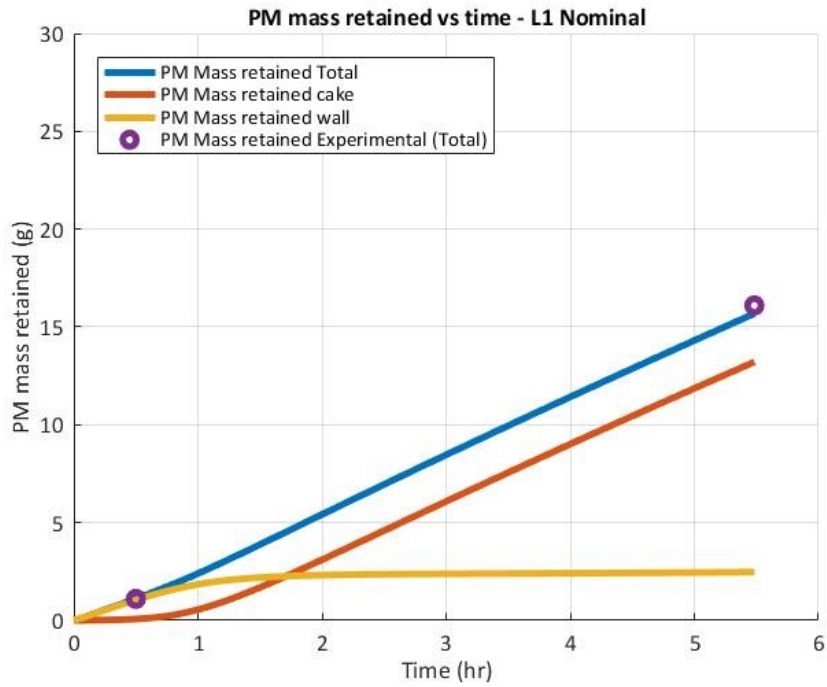


Figure E.1: PM Mass Retained vs Time for L1 Nominal

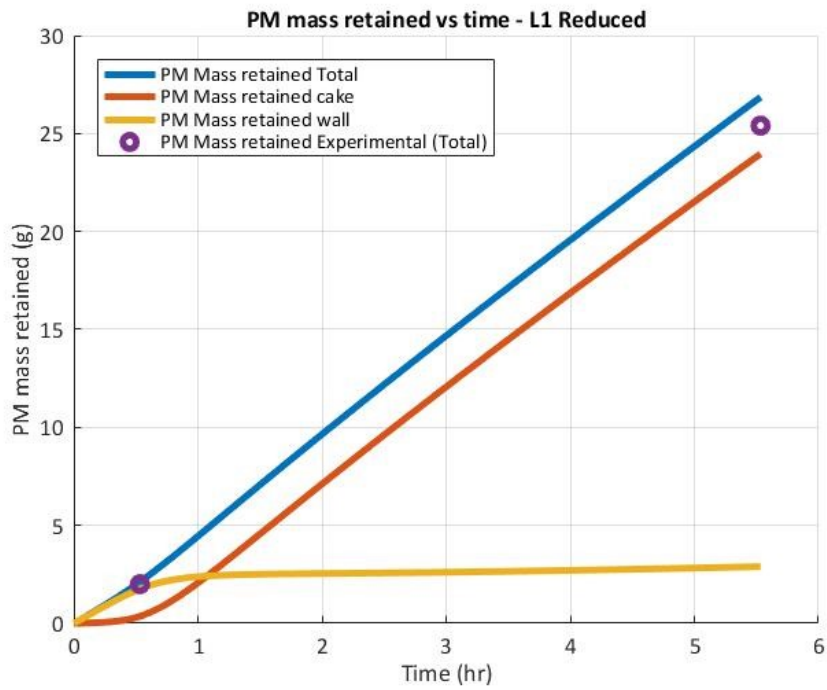


Figure E.2: PM Mass Retained vs Time for L1 Reduced

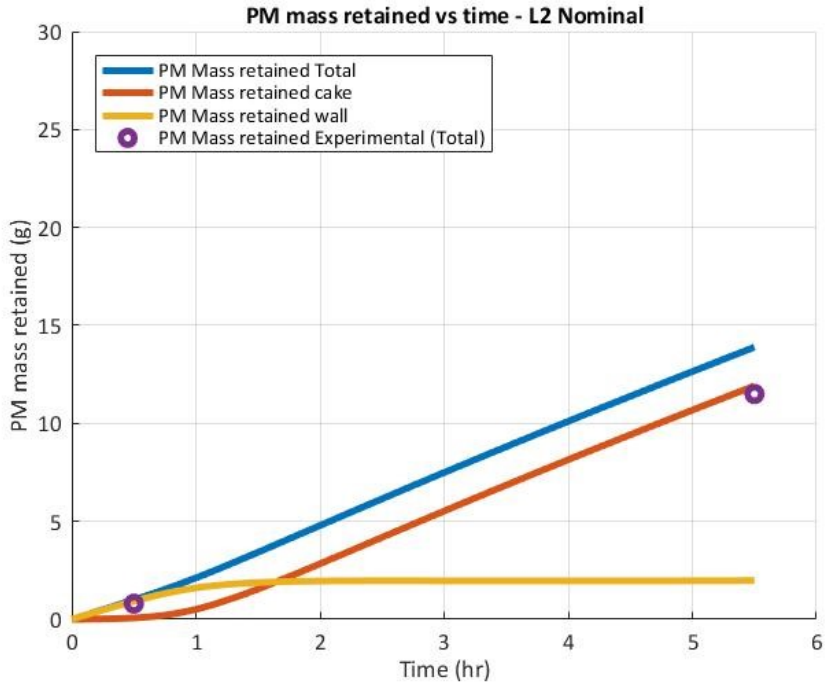


Figure E.3: PM Mass Retained vs Time for L2 Nominal

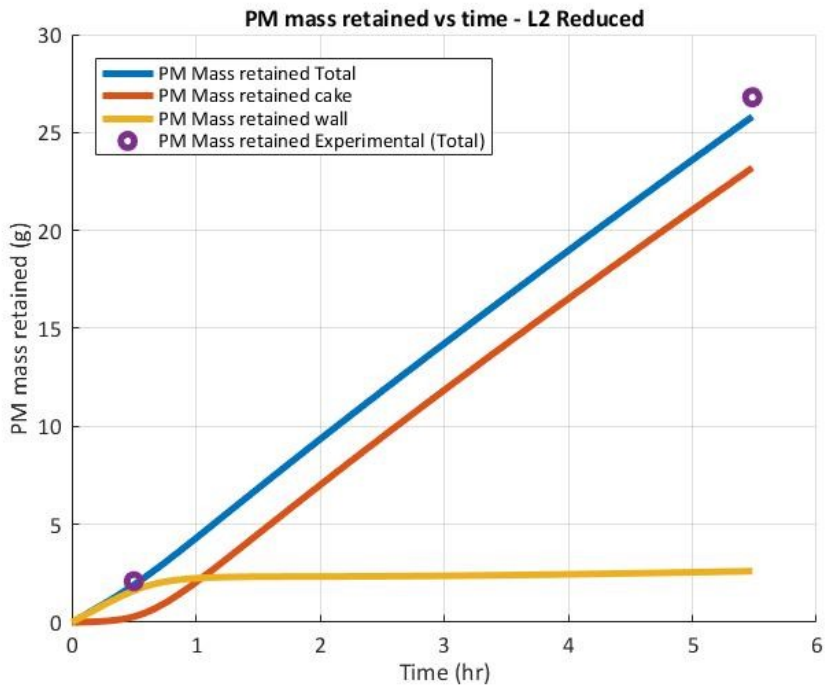


Figure E.4: PM Mass Retained vs Time for L2 Reduced



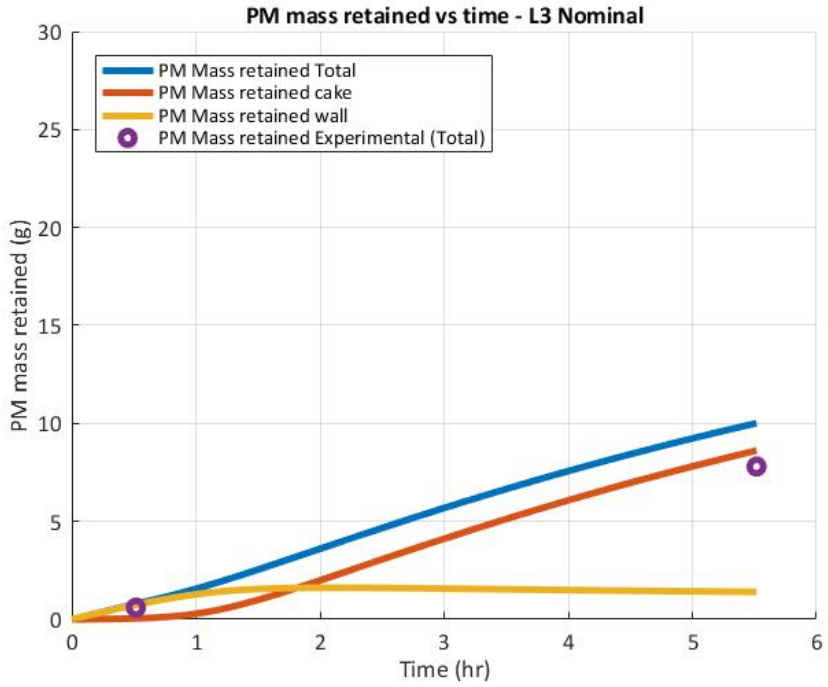


Figure E.5: PM Mass Retained vs Time for L3 Nominal

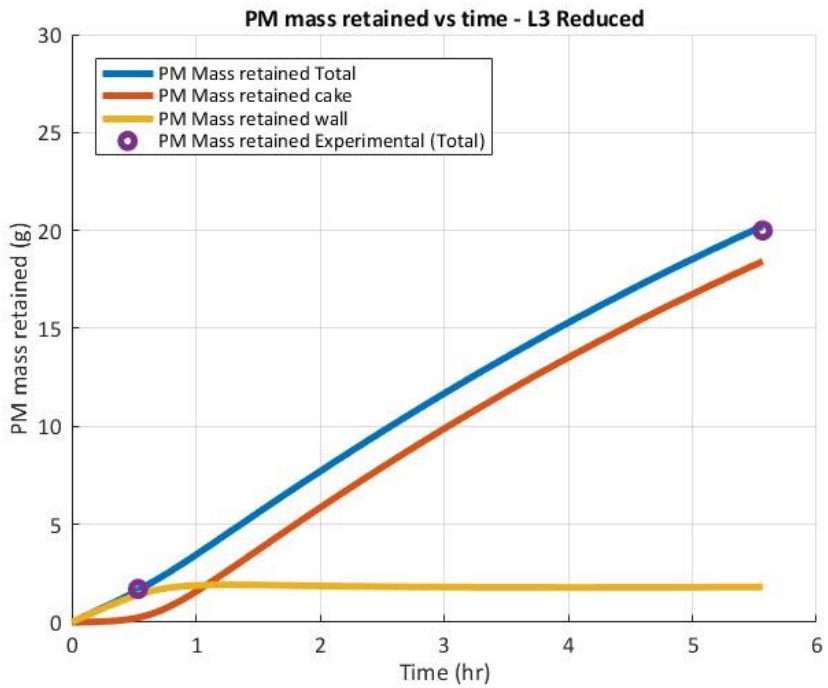


Figure E.6: PM Mass Retained vs Time for L3 Reduced

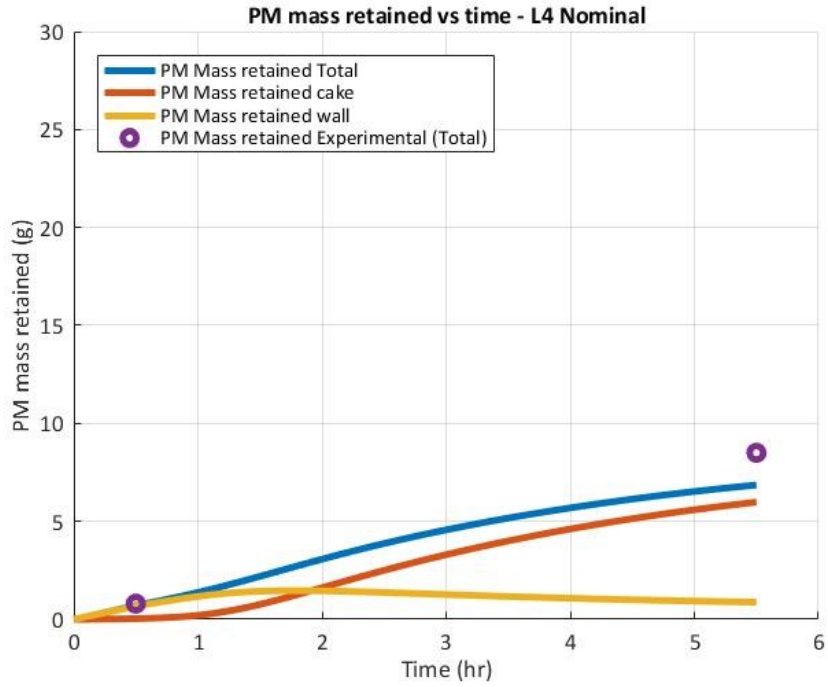


Figure E.7: PM Mass Retained vs Time for L4 Nominal

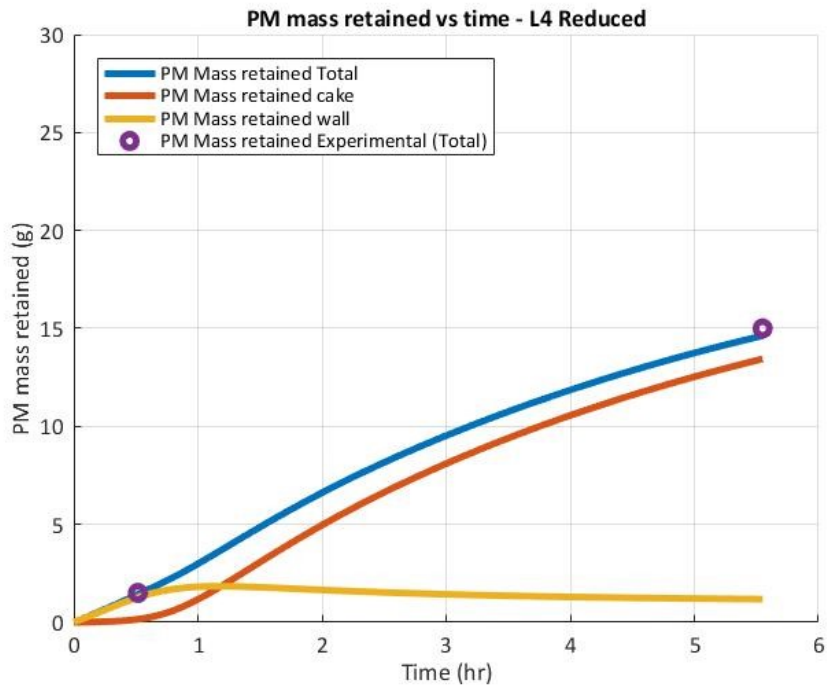


Figure E.8: PM Mass Retained vs Time for L4 Reduced

## Appendix F: Model Pressure Drop Plots for Loading Tests w/o Urea Data

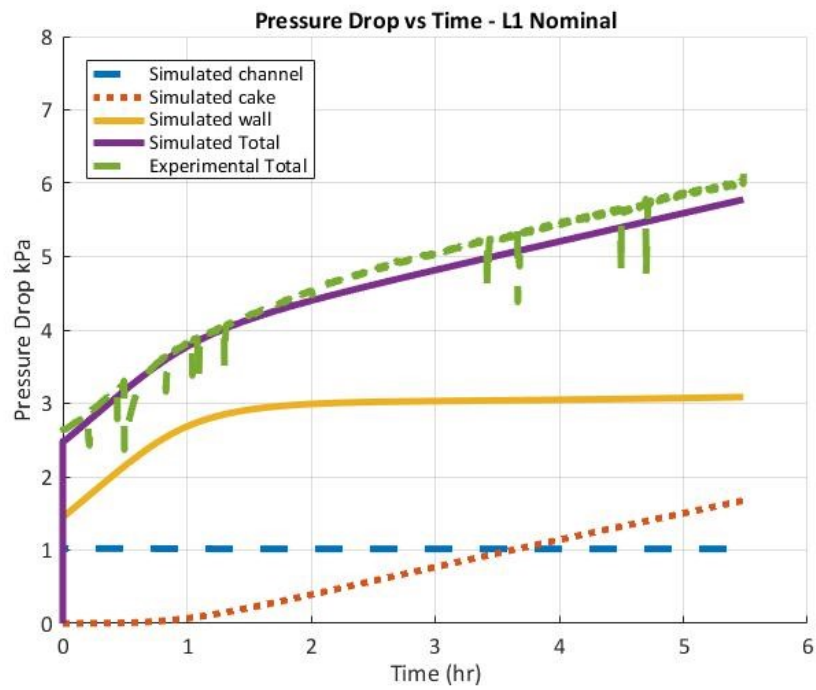


Figure F.1: Pressure Drop vs Time for L1 Nominal

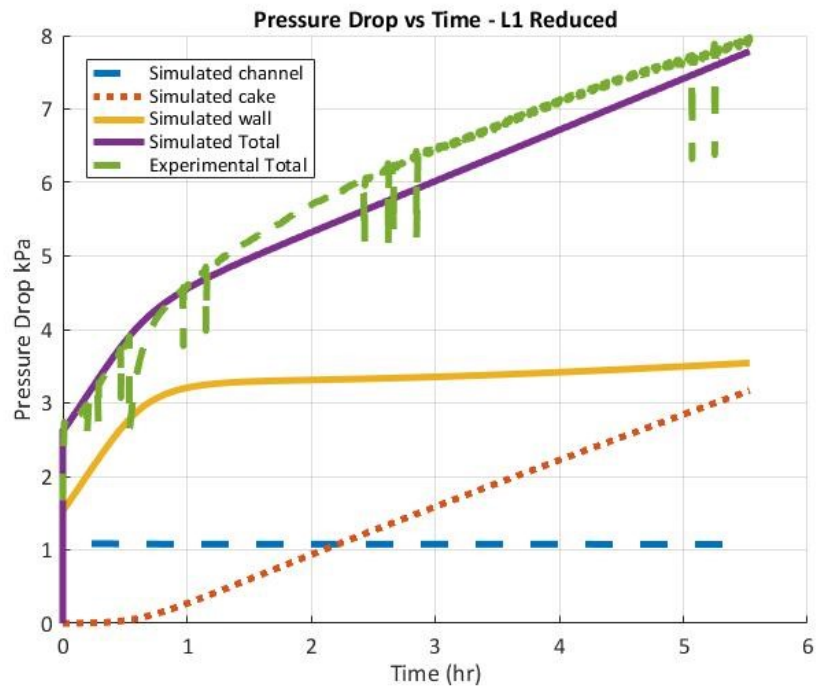


Figure F.2: Pressure Drop vs Time for L1 Reduced

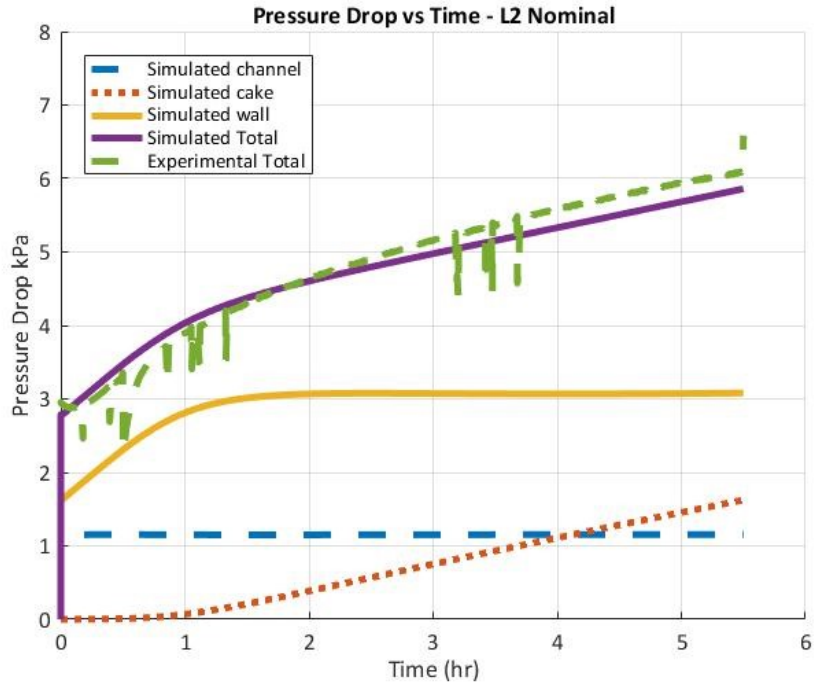


Figure F.3: Pressure Drop vs Time for L2 Nominal

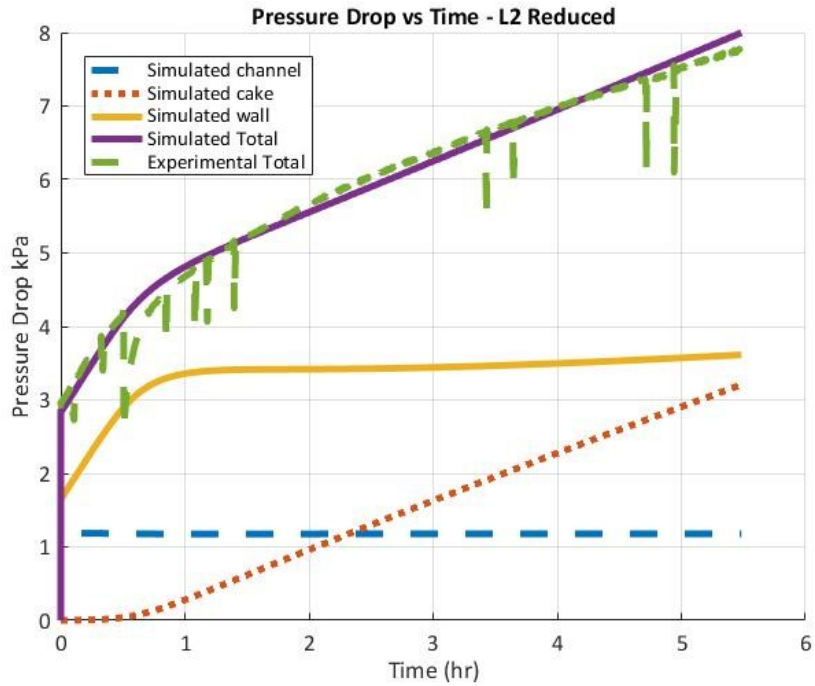


Figure F.4: Pressure Drop vs Time for L2 Reduced

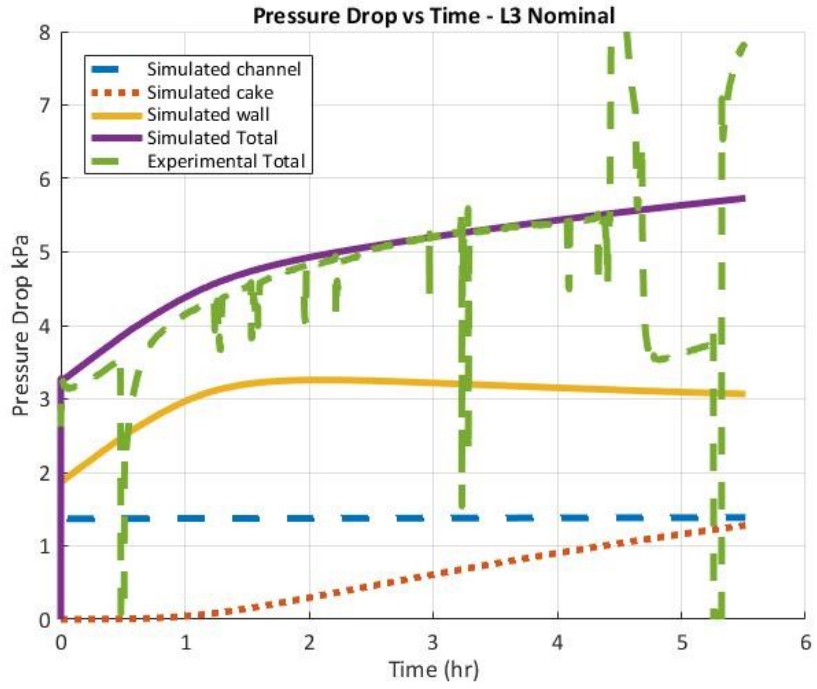


Figure F.5: Pressure Drop vs Time for L3 Nominal

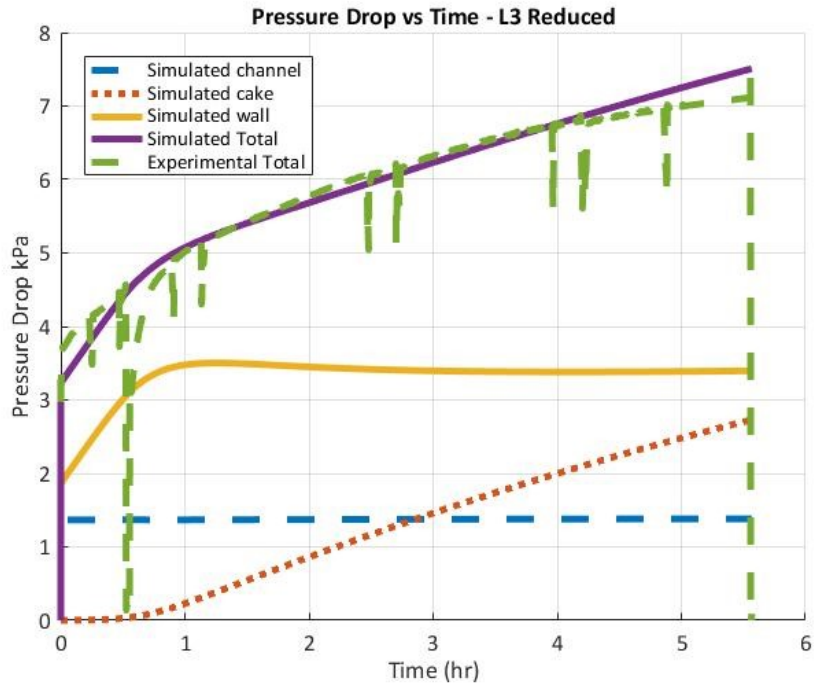


Figure F.6: Pressure Drop vs Time for L3 Reduced

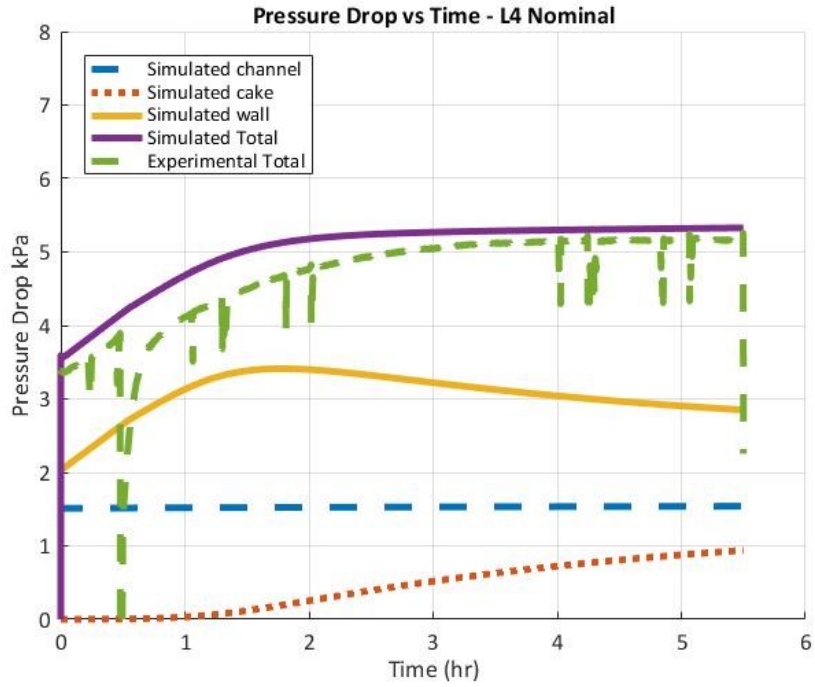


Figure F.7: Pressure Drop vs Time for L4 Nominal

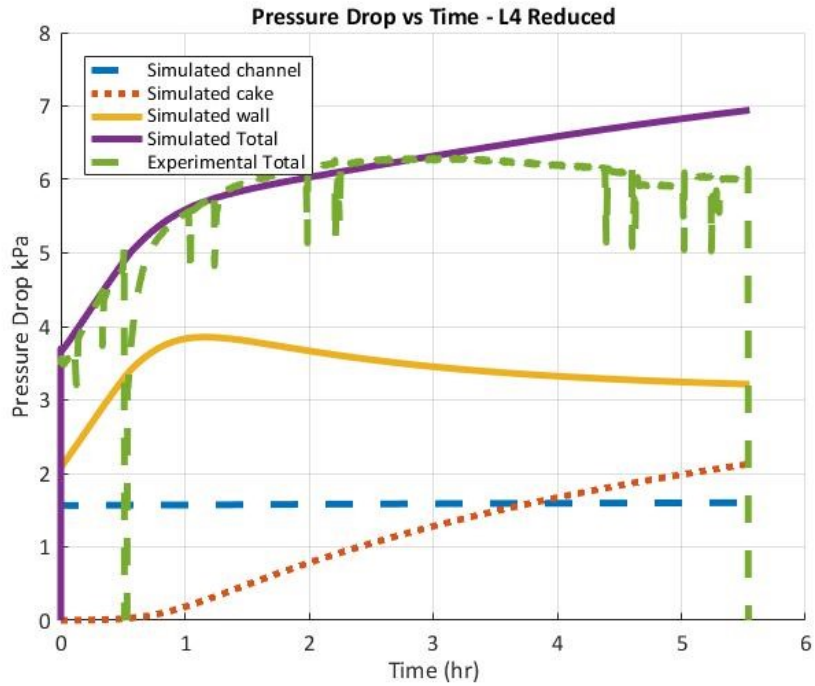


Figure F.8: Pressure Drop vs Time for L4 Reduced

## Appendix G: Model PM Mass Retained Plots for Passive Oxidation w/o Urea Data [8]

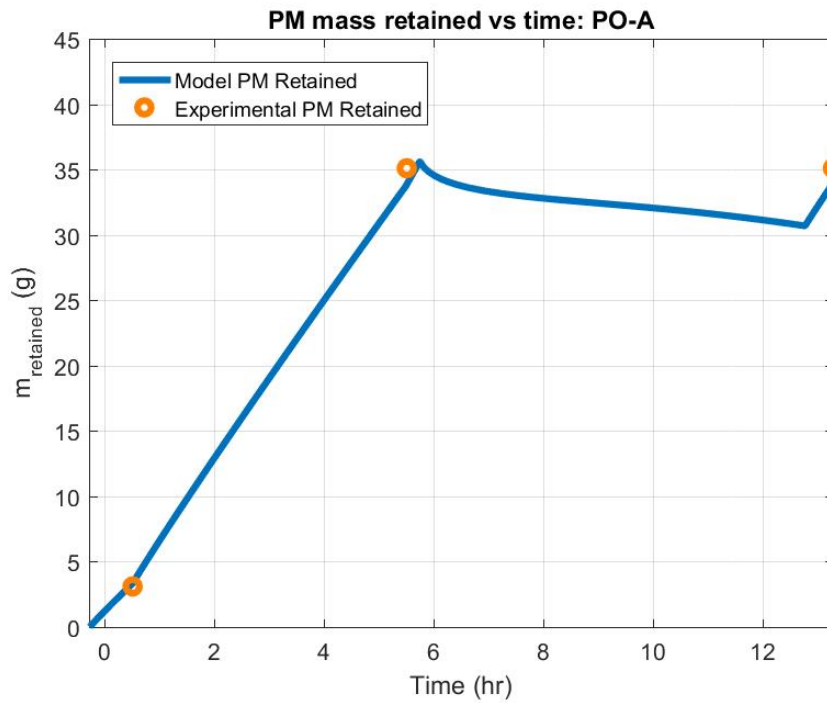


Figure G.1: PM Mass Retained vs Time for PO-A

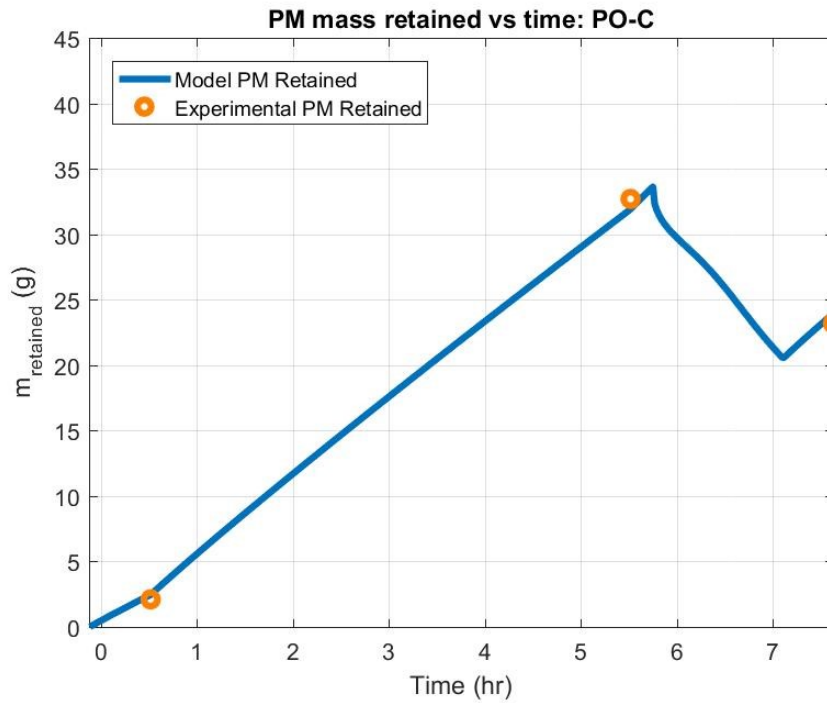


Figure G.2 PM Mass Retained vs Time for PO-C

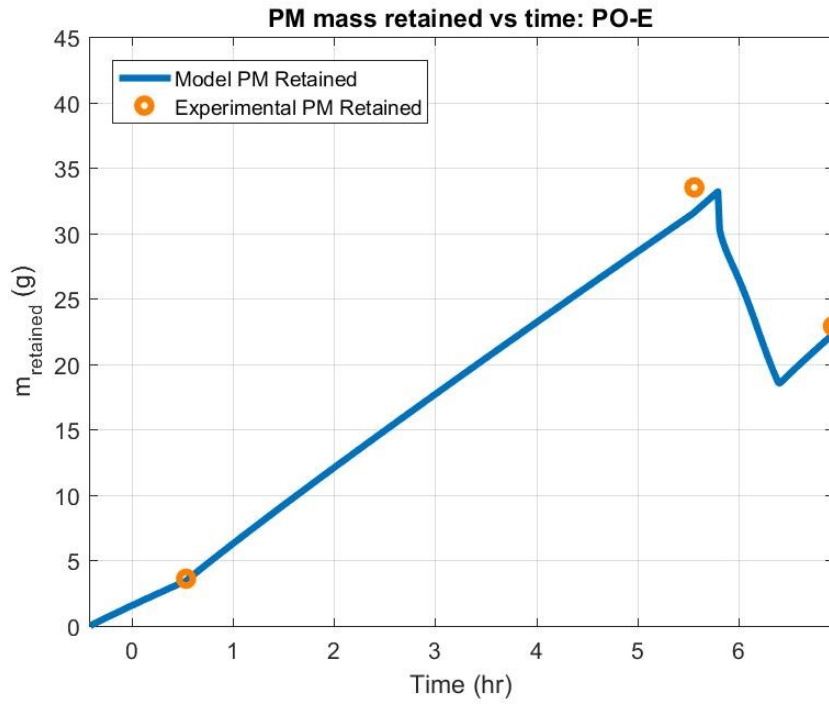


Figure G.3 PM Mass Retained vs Time for PO-E

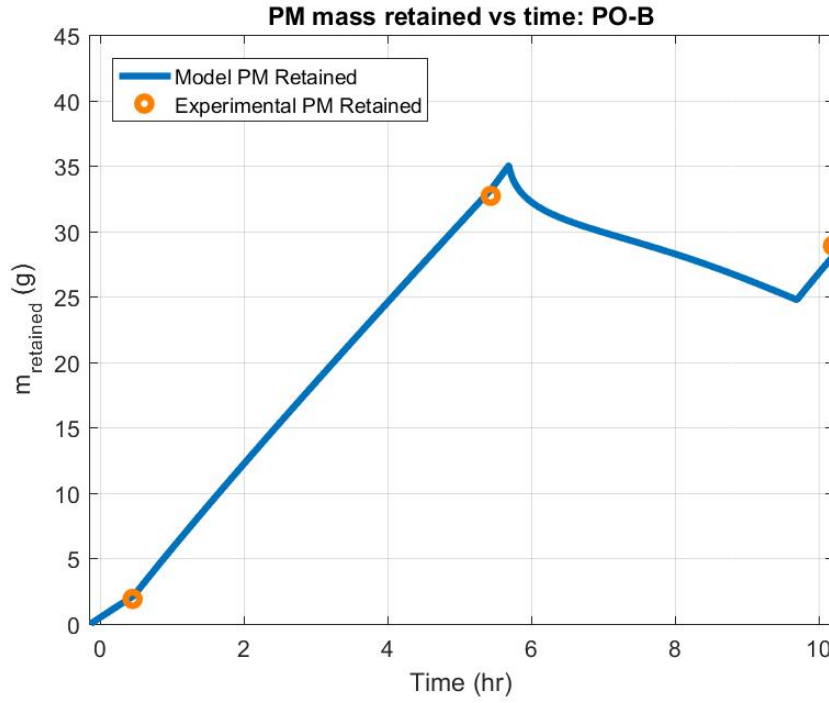


Figure G.4 PM Mass Retained vs Time for PO-B



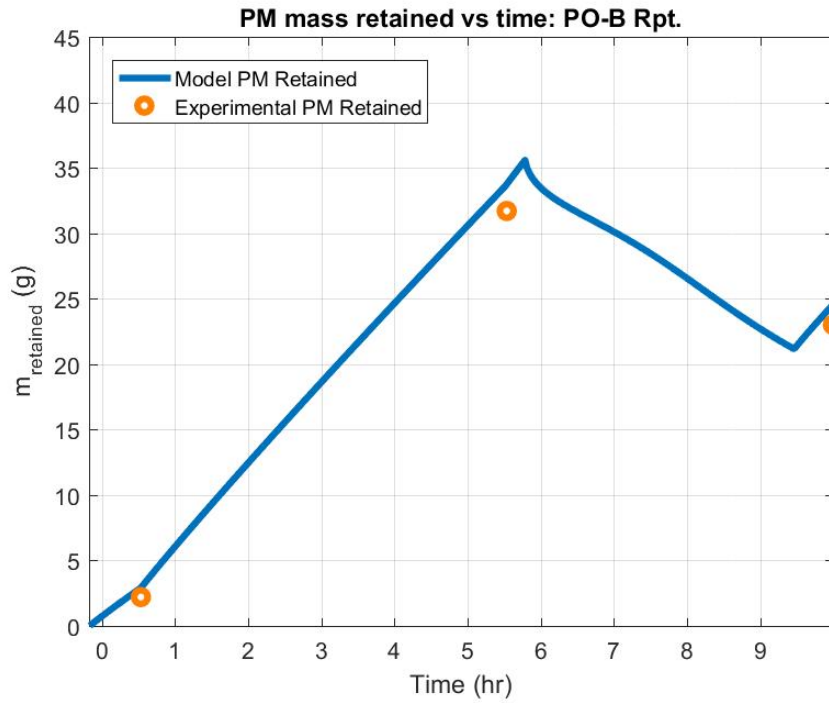


Figure G.5 PM Mass Retained vs Time for PO-B Rpt.

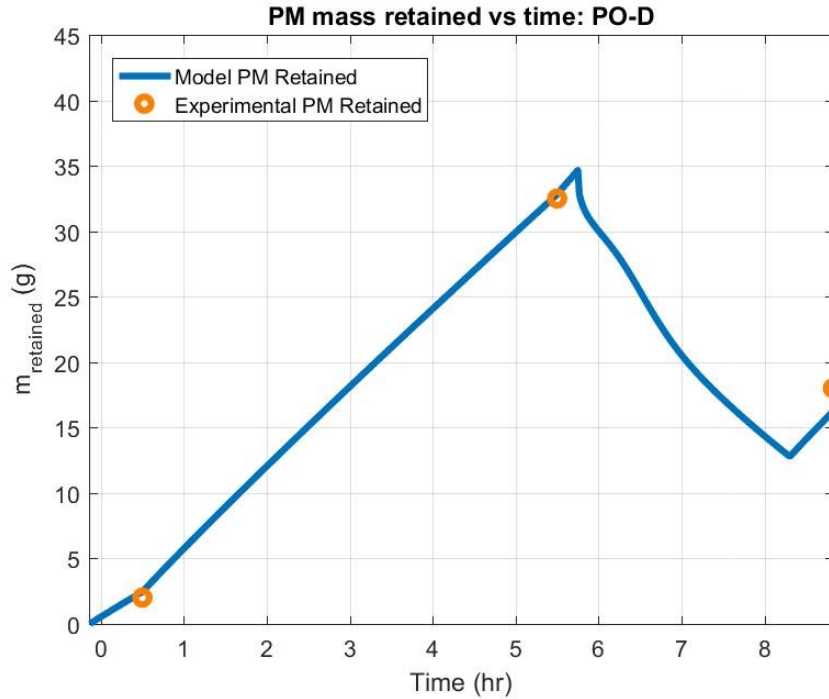


Figure G.6 PM Mass Retained vs Time for PO-D

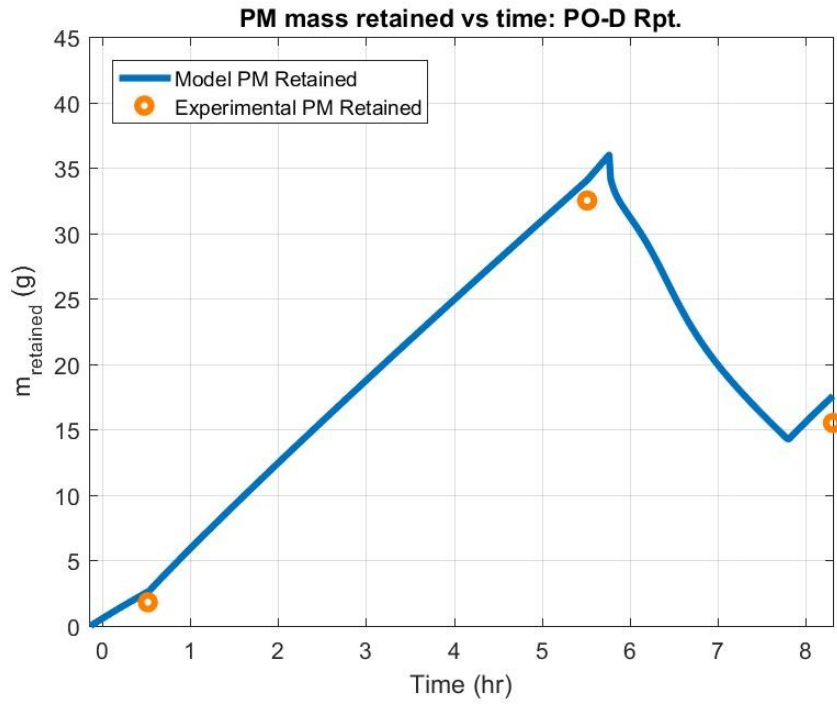


Figure G.7 PM Mass Retained vs Time for PO-D Rpt.

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