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An Initial Non-Equilibrium Porous-Media Model for CFD Simulation of Stirling Regenerators

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The objective of this paper is to define empirical parameters (or closure models) for an initial thermal non-equilibrium porous-media model for use in Computational Fluid Dynamics (CFD) codes for simulation of Stirling regenerators. The two CFD codes currently being used at Glenn Research Center (GRC) for Stirling engine modeling are Fluent and CFD-ACE. The porous-media models available in each of these codes are equilibrium models, which assume that the solid matrix and the fluid are in thermal equilibrium at each spatial location within the porous medium. This is believed to be a poor assumption for the oscillating-flow environment within Stirling regenerators; Stirling 1-D regenerator models, used in Stirling design, use non-equilibrium regenerator models and suggest regenerator matrix and gas average temperatures can differ by several degrees at a given axial location and time during the cycle. A NASA regenerator research grant has been providing experimental and computational results to support definition of various empirical coefficients needed in defining a non-equilibrium, macroscopic, porous-media model (i.e., to define "closure" relations). The grant effort is being led by Cleveland State University, with subcontractor assistance from the University of Minnesota, Gedeon Associates, and Sunpower, Inc. Friction-factor and heat-transfer correlations based on data taken with the NASA/Sunpower oscillating-flow test rig also provide experimentally based correlations that are useful in defining parameters for the porous-media model; these correlations are documented in Gedeon Associates' Sage Stirling-Code Manuals. These sources of experimentally based information were used to define the following terms and parameters needed in the non-equilibrium porous-media model: hydrodynamic dispersion, permeability, inertial coefficient, fluid effective thermal conductivity (including thermal dispersion and estimate of tortuosity effects), and fluid-solid heat transfer coefficient. Solid effective thermal conductivity (including the effect of tortuosity) was also estimated. Determination of the porous-media model parameters was based on planned use in a CFD model of Infinia's Stirling Technology Demonstration Convertor (TDC), which uses a random-fiber regenerator matrix. The non-equilibrium porous-media model presented is considered to be an initial, or "draft," model for possible incorporation in commercial CFD codes, with the expectation that the empirical parameters will likely need to be updated once resulting Stirling CFD model regenerator and engine results have been analyzed. The emphasis of the paper is on use of available data to define empirical parameters (and closure models) needed in a thermal non-equilibrium porous-media model for Stirling regenerator simulation. Such a model has not yet been implemented by the authors or their associates. However, it is anticipated that a thermal non-equilibrium model such as that presented here, when incorporated in the CFD codes, will improve our ability to accurately model Stirling regenerators with CFD relative to current thermal-equilibrium porous-media models.

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Presentation Outline	istrations of Stirling engine, 2-D simulation results, regen. Iterial	idence that assumption of gas/solid thermal equilibrium in generator not valid	r reference, thermal non-equilibrium porous-media nservation equations	rous-media model quantities in these equations needing finition or "closure"	mmary of available information for defining these quantities	ncluding remarks	1 Research Center	at Lewis Field
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Thermal-Equilibrium Porous-Media Model for Regenerator Simulation) 2-D Axisymmetric CFD Model of Infinia's TDC Stirling Engine (Using GRC Temperature Contours: Generated with Dyson's Fluent



Currently Used Regenerator Random Fiber Material



Bekaert 316 Stainless Steel Nominal 12 Micron Round Fibers Mean Eff. D.=13.4 microns & Fibers Are Not Round 90 % Porosity ---from David Gedeon memo. reporting on DOE Regenerator Research Contract Work, Photo By GRC.



Figure 1 Bekaert nominal 12 micron round fibers 316 stainless steel. Measured mean effective diameter 13.4 microns. From 90% porosity regenerator matrix made and tested under curren DOE regenerator research program. Micrograph courtesy of NASA GRC.



Evidence that Gas/Solid Thermal Equilibrium Assumption is not Valid	 UMN Tests with Engine Values of Dimensionless Variables show Significant Temperature Differences between Gas and Solid To be shown 	 Sage 1-D Model of Infinia's TDC 55 We Engine shows significant Gas/Solid Temperature Differences in Regenerator To be shown 	 Enthalpy Flux Losses through the Regenerator from the Hot to the Cold calculated by Sage are significant (to be shown) and are expected to be sensitive to thermal equilibrium/non- equilibrium assumption 	 Enthalpy Flux at Point along 1-D Flow Axis is: 	$\oint \dot{m} c_p T_{gas} dt$	Glenn Research Center	at Lewis Field
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(Considered to Yield an Approximation of Random Fiber) **UMN Wire Screen Regenerator**



- 90 % Porosity
- **Stainless Steel 304 Welded Screens**
- 200 Layers of 6.3 mm x 6.3 mm Mesh
 - Wire Diameter = 0.81 mm
- Each Screen Rotated 45 Deg. Rel. to Next
- Representative Stirling Engine (Max. Reynolds # & Valensi #) **Chosen to define Test Section Dimensionless Parameters**
 - Hot-Wire Anemometry Measurements

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(Macro-Calculations made with CFD-ACE Thermal Equilibrium Porous Media Model) CSU CFD "Micro-" and "Macro-" Calculations & UMN Test Data (Micro-Calculations made using REV of actual geometry)





at Lewis Field

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Determination of Permeability and Inertial Coefficient

- (1) U. of Minn. Large-Scale Wire Screen Measurements
- Use NASA/Sunpower Oscillating-Flow Rig Darcy Friction-Factor Data Assume Quasi-Steady Flow, Equate Darcy-Forchheimer Steady 1-D Momentum Equation with Darcy Friction Factor Momentum Eq. & (7)







Coefficient		UMN Large-S (d _w =8.11	cale Screens E-4 m)		TDC Rar	ndom Fiber
	UMN Old, Experimental	UMN New, Experimental	CSU Calcs.	Sage Cor.	Sage Cor.	Unidirectional Flow Tests
K (m ²)	1.07E-7	1.86E-7	8.9E-7	8.24E-7	4.08E-10	3.52E-10
$\mathbf{K/d_w}^2$	0.163	0.283	1.36	1.26	I	I
Cf	0.049	0.052	0.14	0.13-0.11 Re=25-100	0.19-0.17 Re=25-100	0.154-0.095 Re=25-100

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Fluid & Solid Effective Thermal Conductivity Tensors

- Assume only diagonal elements of tensors are non-zero
- Then, in terms of 3-D cylindrical coordinates--



Experimental Values of Fluid Thermal Dispersion Conductivity

and axial thermal dispersion conductivities determined by various , respectively, are the radial , $k_{dis,xx}$ experimental measurements - In Table below, $k_{{\scriptstyle dis,yy}}$

	Estimated Thermal Dispersion	Porous media
Current Direct Measurements at UMN, Niu ⁷	$\varepsilon_{M,eddy} = \frac{k_{dis,yy}}{\rho_f c_p} = 0.02 d_h U$ or $\frac{k_{dis,yy}}{k_f} = 0.02 Pe$	Welded Screen
Hunt and Tien ²²	$\frac{k_{dis,yy}}{k_f} = 0.0011 Pe$	Fibrous Media
Metzger, Didierjean, and Maillet ²³	$\frac{k_{dis,yy}}{k_f} = (0.03 - 0.05)Pe \text{ and } \frac{k_{dis,xx}}{k_f} = 0.073Pe^{1.59}$	Packed Spheres
Gedeon ⁹	$\frac{k_{dis,xx}}{k_f} = 0.50Pe^{0.62}\beta^{-2.91} \text{ or } \frac{k_{dis,xx}}{k_f} \approx 0.06Pe \text{ for }\beta = 0.9, Pe = 560$	Woven Screen





Estimates of Fluid-Stagnant and Solid-Effective Thermal Conductivities for 90% porosity wire screen or random fiber matrix#2	 For the axial direction use a modification of the series model A lumped effective solid + fluid effective thermal conductivity (not including thermal dispersion), based on the series model is 	$k eff_{,s+f} = \left(\frac{1}{k_f + \frac{1}{k_s}}\right) = \left(\frac{1}{0.90} + \frac{1}{10.1}\right) = 0.0289 W / mK$	 Only slightly larger than molecular fluid cond. of 0.026 W/m-K & likely too small since series model implies wires not touching in axial direction 	 3-D CFD microscopic simulation of REV of the UMN welded screen by by Rong of CSU suggests above series value should be multiplied by 2.157 	$\therefore k_{eff, s+f} = (0.0289 W / mK) (2.157) = 0.0623 W / mK$	 The above would be appropriate for an equilibrium model. Seeing no obvious way to separate values for a fluid & solid in the axial direction— propose using the same value for fluid-stagnant and solid-effective cond. in the axial direction, hoping that overall effect will be reasonable. 	Glenn Research Center	at Lewis Field
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Heat Transfer Coefficients Between Fluid & Solid Matrix

- Technical Memorandums containing NASA/Sunpower oscillating-flow Good sources of heat transfer coefficient correlations for wire screen and random fiber matrices are Gedeon's Sage manuals and NASA rig data.
- The following correlations are in terms of Nusselt No., Peclet Number (Reynolds No. x Prandtl No.), and porosity:
- $Nu = (1.+0.99 \ Pe^{0.66}) \ \beta^{1.79}$ For wire screen:
- For random fiber: $Nu = (1.+1.16 Pe^{0.66}) \beta^{2.61}$
- where--

$$abla u = rac{hd_h}{k}, \quad Pe = Re \ Pr = rac{\rho u d_h}{\mu} \frac{c_p \mu}{k}$$

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Oscillating-Flow Rig







Concluding Remarks

- replace the existing thermal equilibrium models in CFD codes for A thermal-non-equilibrium porous-media model is needed to accurate simulation of Stirling regenerators
- parameters needing definition for a macroscopic, thermal-nonsummarized for reference in discussing porous-media model Transient, compressible-flow, conservation equations are equilibrium porous-media model
- the hydrodynamic-dispersion term and the permeability & inertial Available experimental information is discussed for definition of coefficient & thermal dispersion terms in the energy equations coefficients in the momentum equation, and the heat transfer
- Methods are outlined for estimating fluid-stagnant and solideffective thermal conductivities
- the regenerator of a TDC Stirling engine. Still need to implement. Adequate information is given for definition of an initial thermal non-equilibrium porous-media model for use in a CFD model of
- Application of this model in Stirling CFD codes may demonstrate that further refinement of these parameters, or of the model itself may be required



