Cleveland State University EngagedScholarship@CSU



Mechanical Engineering Faculty Publications

Mechanical Engineering Department

10-2006

An Initial Non-Equilibrium Porous-Media Model for CFD Simulation of Stirling Regenerators

Roy C. Tew NASA Glenn Research Center

Terry Simon University of Minnesota

David Gedeon Gedeon Associates

Mounir B. Ibrahim *Cleveland State University*, m.ibrahim@csuohio.edu

Wei Rong Cleveland State University

Follow this and additional works at: https://engagedscholarship.csuohio.edu/enme_facpub Part of the <u>Mechanical Engineering Commons</u> How does access to this work benefit you? Let us know!

Recommended Citation

Tew, Roy C.; Simon, Terry; Gedeon, David; Ibrahim, Mounir B.; and Rong, Wei, "An Initial Non-Equilibrium Porous-Media Model for CFD Simulation of Stirling Regenerators" (2006). *Mechanical Engineering Faculty Publications*. 270. https://engagedscholarship.csuohio.edu/enme_facpub/270

This Report is brought to you for free and open access by the Mechanical Engineering Department at EngagedScholarship@CSU. It has been accepted for inclusion in Mechanical Engineering Faculty Publications by an authorized administrator of EngagedScholarship@CSU. For more information, please contact library.es@csuohio.edu.



An Initial Non-Equilibrium Porous-Media Model for CFD Simulation of Stirling Regenerators

Roy C. Tew Glenn Research Center, Cleveland, Ohio

Terry Simon University of Minnesota, Minneapolis, Minnesota

David Gedeon Gedeon Associates, Athens, Ohio

Mounir Ibrahim and Wei Rong Cleveland State University, Cleveland, Ohio

NASA STI Program . . . in Profile

Since its founding, NASA has been dedicated to the advancement of aeronautics and space science. The NASA Scientific and Technical Information (STI) program plays a key part in helping NASA maintain this important role.

The NASA STI Program operates under the auspices of the Agency Chief Information Officer. It collects, organizes, provides for archiving, and disseminates NASA's STI. The NASA STI program provides access to the NASA Aeronautics and Space Database and its public interface, the NASA Technical Reports Server, thus providing one of the largest collections of aeronautical and space science STI in the world. Results are published in both non-NASA channels and by NASA in the NASA STI Report Series, which includes the following report types:

- TECHNICAL PUBLICATION. Reports of completed research or a major significant phase of research that present the results of NASA programs and include extensive data or theoretical analysis. Includes compilations of significant scientific and technical data and information deemed to be of continuing reference value. NASA counterpart of peer-reviewed formal professional papers but has less stringent limitations on manuscript length and extent of graphic presentations.
- TECHNICAL MEMORANDUM. Scientific and technical findings that are preliminary or of specialized interest, e.g., quick release reports, working papers, and bibliographies that contain minimal annotation. Does not contain extensive analysis.
- CONTRACTOR REPORT. Scientific and technical findings by NASA-sponsored contractors and grantees.

- CONFERENCE PUBLICATION. Collected papers from scientific and technical conferences, symposia, seminars, or other meetings sponsored or cosponsored by NASA.
- SPECIAL PUBLICATION. Scientific, technical, or historical information from NASA programs, projects, and missions, often concerned with subjects having substantial public interest.
- TECHNICAL TRANSLATION. Englishlanguage translations of foreign scientific and technical material pertinent to NASA's mission.

Specialized services also include creating custom thesauri, building customized databases, organizing and publishing research results.

For more information about the NASA STI program, see the following:

- Access the NASA STI program home page at http://www.sti.nasa.gov
- E-mail your question via the Internet to *help@sti.nasa.gov*
- Fax your question to the NASA STI Help Desk at 301–621–0134
- Telephone the NASA STI Help Desk at 301–621–0390
- Write to:
 NASA STI Help Desk
 NASA Center for AeroSpace Information
 7121 Standard Drive
 Hanover, MD 21076–1320



An Initial Non-Equilibrium Porous-Media Model for CFD Simulation of Stirling Regenerators

Roy C. Tew Glenn Research Center, Cleveland, Ohio

Terry Simon University of Minnesota, Minneapolis, Minnesota

David Gedeon Gedeon Associates, Athens, Ohio

Mounir Ibrahim and Wei Rong Cleveland State University, Cleveland, Ohio

Prepared for the Fourth International Energy Conversion Engineering Conference and Exhibit (IECEC) sponsored by the American Institute of Aeronautics and Astronautics San Diego, California, June 26–29, 2006

National Aeronautics and Space Administration

Glenn Research Center Cleveland, Ohio 44135

Acknowledgments

The work described in this paper was performed for the NASA Science Mission Directorate (SMD) and the Radioisotope Power System (RPS) Program.

Level of Review: This material has been technically reviewed by technical management.

Available from

NASA Center for Aerospace Information 7121 Standard Drive Hanover, MD 21076–1320 National Technical Information Service 5285 Port Royal Road Springfield, VA 22161

Available electronically at http://gltrs.grc.nasa.gov

An Initial Non-Equilibrium Porous-Media Model for CFD Simulation of Stirling Regenerators

Roy C. Tew National Aeronautics and Space Administration Glenn Research Center Cleveland, Ohio 44135

> Terry Simon University of Minnesota Minneapolis, Minnesota 55455

> > David Gedeon Gedeon Associates Athens, Ohio 45701

Mounir Ibrahim and Wei Rong Cleveland State University Cleveland, Ohio 44115

Abstract

The objective of this paper is to define empirical parameters (or closure models) for an initial thermal non-equilibrium porous-media model for use in Computational Fluid Dynamics (CFD) codes for simulation of Stirling regenerators. The two CFD codes currently being used at Glenn Research Center (GRC) for Stirling engine modeling are Fluent and CFD-ACE. The porous-media models available in each of these codes are equilibrium models, which assume that the solid matrix and the fluid are in thermal equilibrium at each spatial location within the porous medium. This is believed to be a poor assumption for the oscillating-flow environment within Stirling regenerators; Stirling 1-D regenerator models, used in Stirling design, use non-equilibrium regenerator models and suggest regenerator matrix and gas average temperatures can differ by several degrees at a given axial location and time during the cycle. A NASA regenerator research grant has been providing experimental and computational results to support definition of various empirical coefficients needed in defining a non-equilibrium, macroscopic, porous-media model (i.e., to define "closure" relations). The grant effort is being led by Cleveland State University, with subcontractor assistance from the University of Minnesota, Gedeon Associates, and Sunpower, Inc. Friction-factor and heat-transfer correlations based on data taken with the NASA/Sunpower oscillating-flow test rig also provide experimentally based correlations that are useful in defining parameters for the porous-media model; these correlations are documented in Gedeon Associates' Sage Stirling-Code Manuals. These sources of experimentally based information were used to define the following terms and parameters needed in the non-equilibrium porous-media model: hydrodynamic dispersion, permeability, inertial coefficient, fluid effective thermal conductivity (including thermal dispersion and estimate of tortuosity effects), and fluid-solid heat transfer coefficient. Solid effective thermal conductivity (including the effect of tortuosity) was also estimated. Determination of the porous-media model parameters was based on planned use in a CFD model of Infinia's Stirling Technology Demonstration Convertor (TDC), which uses a random-fiber regenerator matrix. The non-equilibrium porous-media model presented is considered to be an initial, or "draft," model for possible incorporation in commercial CFD codes, with the expectation that the empirical parameters will likely need to be updated once resulting Stirling CFD model regenerator and engine results have been analyzed. The emphasis of the paper is on use of available data to define empirical parameters (and closure models) needed in a thermal non-equilibrium porous-media model for Stirling regenerator simulation. Such a model has not yet been implemented by the authors or their associates. However, it is anticipated that a thermal non-equilibrium model such as that presented here, when incorporated in the CFD codes, will improve our ability to accurately model Stirling regenerators with CFD relative to current thermal-equilibrium porous-media models.

Nomenclature

A = heat transfer area (m^2) $A_{sf} = solid-fluid interfacial area (m²)$ a = cross-sectional area (m²) C_f = inertial coefficient c_p = specific heat (J/kg-K) d_h = hydraulic diameter (m) d_w = wire diameter (m) f =friction-factor h = heat transfer coefficient (J/m^2-s-K) $K = permeability (m^2)$ k = thermal conductivity (W/m-K) k_{tor} = thermal tortuosity conduct. tensor (W/m-K) k_{dis} = thermal dispersion conduct. tensor (W/m-K) L = length(m) \dot{m} = mass flow rate (kg/s) $Nu = h d_h / k$, Nusselt No. p = pressure (Pa)Pe = Re Pr, Peclet No. $Pr = c_p \mu / k$, Prandtl No. Re = ρ u d_h/ μ , Reynolds No. t = time(s) $r_{\rm h}$ = hydraulic radius (m) = $d_{\rm h}/4$ T = temperature (K) $U = \langle u \rangle$, superficial, Darcian, or approach velocity u = average-flow-channel, or local, velocity V = volume (m^3)

Greek Symbols

 β = porosity

 $\rho = \text{density} (\text{kg/m}^3)$

 μ = absolute viscosity (kg/m-s)

 $v = dynamic viscosity (m^2/s)$

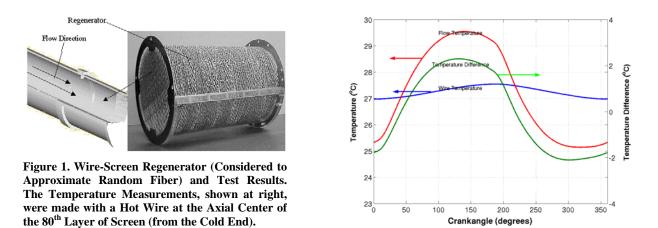
I. Introduction

The Advanced Stirling Convertor (ASC) is being developed as a light-weight, high-efficiency Advanced Stirling Radioisotope Generator (SRG) for use on potential NASA Space Science missions. Potential missions include providing spacecraft onboard-electric power for deep-space missions or power for lunar applications, or un-piloted Mars rovers. Advanced Stirling convertors would provide substantial performance and mass benefits for these missions and could also allow the use of Stirling radioisotope power systems for radioisotope electric propulsion. A combined Stirling convertor/cooler based on a high temperature heater head may enable an extended-duration Venus surface mission. Therefore, GRC is also developing advanced technology for Stirling convertors, aimed at improving specific power and efficiency of the convertor and the overall power system, and confirming and enhancing reliability. Performance and mass improvement goals have been established for these next generation

Stirling radioisotope power systems. Efforts are underway to achieve these goals, both in-house at GRC and via grants and contracts. These efforts include use of multi-dimensional (multi-D) Stirling computational-fluid-dynamics (CFD) models to enhance knowledge of component performance details and reliability, high-temperature materials, advanced controllers, low-vibration techniques, advanced regenerators, and a lightweight convertor.^{1, 2}

The objective of this paper is to report on definition of empirical parameters for an initial thermal nonequilibrium porous-media model intended for use in multi-D Stirling codes³⁻⁵ for simulation of regenerators. Experimental data from a regenerator research grant⁶⁻⁸ and experimentally based correlations derived from oscillating-flow rig test data⁹ were used in defining parameters needed in the non-equilibrium porous-media model. The grant is led by Cleveland State University (CSU) with subcontractor assistance from the University of Minnesota (UMN), Gedeon Associates and Sunpower Inc. Determination of the particular porous media model parameters presented was based on planned use in a CFD model of Infinia's Stirling Technology Demonstration Convertor (TDC). The thermal non-equilibrium porous-media model presented is considered to be an initial, or "draft," model for possible incorporation in commercial CFD codes (which now contain thermal equilibrium porousmedia models), with the expectation that empirical parameters or heuristic terms in the equations may need to be updated once resulting Stirling CFD model regenerator and engine results have been analyzed. The emphasis of the paper is on use of available data to define the empirical parameters (or closure models) needed in non-equilibrium porous-media models for Stirling regenerator simulation. Such a porous-media model has not yet been implemented in a Stirling CFD model by the authors or their associates.

Two CFD codes, Fluent^{††} and CFD-ACE^{‡‡}, have been used at Glenn Research Center (GRC) for modeling of Infinia's Stirling TDC. The porous-media models available in each of these codes are thermal equilibrium models, which assume that the solid matrix and the fluid are in local thermal equilibrium (thus at the same temperature) at each spatial interface between them within the porous medium. This is believed to be a poor assumption for the oscillating-flow environment within Stirling regenerators; some results supporting this belief are: (1) Experimental measurements in a large-scale replica of such a regenerator show solid and fluid temperatures differ by as much as 2 degrees C over an engine cycle, as shown in Fig. 1^{§§}. Characteristics of this large-scale replica and the tests were: 90% porosity, stainless steel 304 welded screens, 200 layers of 6.3 mm x 6.3 mm mesh, 0.81 mm wire diameter; test section dimensionless parameters were similar to those of the TDC (the temperature measurements were made with



hot-wire anemometry). (2) This same experimental data is shown in Figure 2, along with (a) a "microscopic" CFD simulation of the non-equilibrium temperatures of one layer of the test rig welded screen and adjacent fluid¹⁰, and (b) a CFD-ACE "macroscopic" equilibrium porous-media model simulation of the "lumped" solid plus fluid temperature over a cycle. Note that the variation of the calculated macroscopic thermal-equilibrium-model lumped solid/fluid temperature over the cycle (lying between the CFD microscopic and the measured solid temperatures in Fig. 2), is almost the same as that of the non-equilibrium solid temperature variations—due to the much greater specific heat of the solid. (3) Fig. 3 shows Sage 1-D TDC model predictions of the regenerator solid and fluid

^{††} Internet website <u>www.fluent.com</u> or do internet search on "Fluent"

^{‡‡} Internet website <u>www.esi-group.com/SimulationSoftware/CFD-ACE/</u> or do internet search on "CFD-ACE"

^{§§} Simon, T., "Contributions to Regenerator Modeling," Presentation for Regenerator Modeling Panel Discussion,

^{2&}lt;sup>nd</sup> International Energy Conversion Engineering Conference, Providence, RI, August 18, 2004.

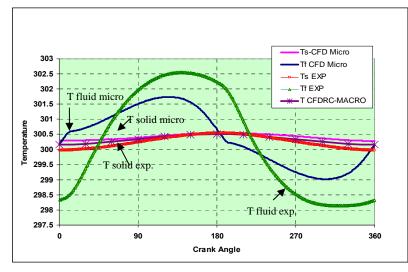


Figure 2. CFD Microscopic Calculations of Solid and Fluid Temperatures, and Macroscopic Equilibrium Solid+Fluid Temperature, deg. K--superimposed on the UMN Experimental Temperatures from Fig. 1

temperatures***. Differences in solid and fluid temperatures range up ~ 20 degrees K at the ends of the regenerator and ~1-2 degrees at the center of the regenerator. These calculations, made by the first author at GRC, yielded an enthalpy flux loss over the cycle of about 22 W, or approximately 8% of the predicted 288 W of heat into the hot-end of the convertor (predicted electrical power was about 56 W at ~83 Hz frequency); one would expect that neglect of the temperature difference between the regenerator solid and fluid, and the consequent entropy generation, would produce underestimation of regenerator enthalpy-flux losses. Therefore these results. both measurements and CFD simulations, suggest the assumption of solid-

matrix/fluid thermal equilibrium would be inappropriate for the Stirling TDC regenerator.

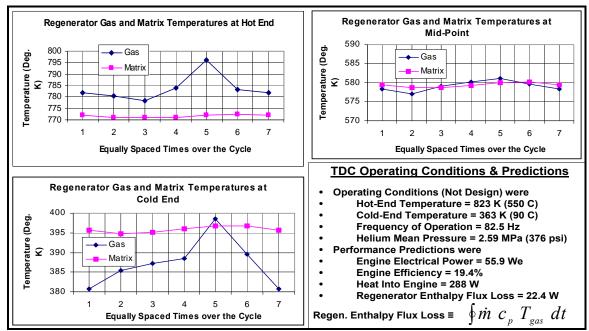


Figure 3. Sage 1-D Thermal Non-Equilibrium Regenerator Model, Fluid & Solid Temperature Predictions for TDC

A survey of the porous-media literature supports the need for thermal non-equilibrium porous-media models for thermal storage applications, as in Stirling regenerators. In Singh¹¹ it is noted that in a thermal storage system, heat transfer between the solid and fluid phases is a key phenomenon and both the phases are inherently in thermal non-equilibrium. Hence the corresponding models of heat transfer will necessarily be of the 2-energy-equation type, one equation each for the fluid and solid phase temperature. Results are shown in the paper of 1- and 2-energy-equation temperature calculations (i.e. using thermal- equilbrium and non-equilibrium models) for steady-flow through

^{****} Tew, R., "Overview of Stirling Regenerator (Porous Media) CFD Modeling Problems," Presentation for Workshop on Convective Heat Transfer in Porous Media, Hosted by NASA Glenn Research Center, North Olmsted, OH, April 28-29, 2004.

porous-media with thermal fields which evolve with time; 1- and 2-energy-equation temperature profiles are compared for glass/water and metal/air porous-media systems over ranges of Reynolds number and porous-media flow lengths.

Amiri and Vafai¹² examined the validity of the thermal-equilibrium assumption via a one-dimensional study of incompressible flow through a packed bed. They noted that the transient response of the solid structure is crucial to the performance of packed beds when used for thermal storage applications, and the solid-to-fluid heat transfer coefficient is a major resistance to heat transfer at the interface between the fluid and the solid matrix. The "microscopic" governing equations were volume averaged over a representative elementary volume to arrive at the "macroscopic" transport equations, including separate fluid and solid phases; the resulting 1-D, incompressible, volume-averaged macroscopic equations used by Amiri and Vafai are a reduced form of the more general macroscopic equations given below in this paper. Temperature differences between fluid and solid were calculated for a range of Reynolds No.'s and Darcy No.'s (dimensionless permeability). It was found that the ratio of fluid-to-solid thermal conductivity was an important parameter in determining local temperature difference between fluid and solid, for a given set of operating conditions. This analysis was also for steady flow through the porous media (packed beds) with developing thermal fields.

Minkowycz¹³ analyzes departure from local thermal equilibrium in porous media due to a rapidly changing heat source. The analysis is done for a sinusoidally-varying imposed heat-flux at one of the boundaries for the cases of no-flow and steady-flow in the same direction as the imposed heat-flux. It is noted that local thermal equilibrium is an often-used hypothesis when studying heat transfer in porous media, but examination of non-equilibrium phenomena show that this hypothesis is usually not valid during rapid heating and cooling. Oscillatory plots of fluid and solid dimensionless temperatures as a function of dimensionless time over the cycle are shown for various combinations of dimensionless frequency, fluid and solid heat capacities, and dimensionless "Sparrow No.'s;" Sparrow No. is defined to be a product of one form of the more familiar Biot number and a dimensionless ratio of lengths. It is noted that in the presence of rapid surface heat input variations, local thermal equilibrium fails to exist and large errors can be realized, depending on the value of the thermophysical properties; and the value of the Sparrow number appears to be indicative of the presence, or not, of local thermal equilibrium for applications dealing with rapidly changing heat inputs.

Muralidhar¹⁴ analyzed the effect of pulsating flow of gas and the accompanying heat transfer within a regenerator made from wire-mesh screens, of the type used in Stirling cycle devices. A harmonic analysis was used to examine fully-developed but unsteady gas flow in a regenerator assuming a non-Darcy, thermally non-equilibrium porous medium. It is noted that one assumption often adopted in the published literature is the thermal equilibrium between fluid in the pores and the solid material of the porous medium; however, thermal performance of regenerators totally depends on heat transfer between fluid and solid phases. Therefore, the individual phases should have a local temperature difference from one to the other. Unfortunately, although temperature profiles and regenerator effectiveness are explored as functions of Reynolds No., pulsating frequency, thermal properties of gas and solid, and the mesh structure—the local temperature differences between gas and solid do not appear to be given in the paper.

Gedeon¹⁵ developed a 2-D CFD "Manifest" (for "manifold estimate") computer code for simulation of Stirling regenerators and their manifolds (that was capable of extension to other Stirling components). In the process of developing this code, he derived a non-equilibrium macroscopic porous-media model, starting from the generalized Navier-Stokes equations. These integral-form porous-media equations were also converted to curvilinear form for use in Manifest. Gedeon used Manifest to study jetting into the porous matrix (as from adjacent heat exchangers) and the effect of side-inlet regenerator manifolds. Side-inlet manifolds appeared to greatly enhance the possibility that flow through the regenerator would be non-uniform and thus decrease regenerator performance. The form of Gedeon's integral-form non-equilibrium porous-media equations differs from the differential form shown in this paper.

Thermal equilibrium porous-media models, or 1-energy-equation models, are consistent with the assumption of infinite heat-transfer coefficients between fluid and solid phases and completely neglect entropy generation due to the radial heat transfer between the fluid and solid phases (since the local temperature difference between the phases is zero). However, unless the solid heat capacity of the porous-medium is essentially infinite relative to that of the fluid, thermal-equilibrium-model hot-end and cold-end regenerator fluid exit temperatures can still vary over the cycle; so, in general, thermal equilibrium porous-media models of Stirling regenerators will still yield non-zero regenerator enthalpy flux losses over the cycle, though one would expect that these losses would be underestimated.

II. A Compressible-Flow Non-Equilibrium Porous-Media Model for CFD Codes

Initial values of parameters needed for a macroscopic non-equilibrium porous-media model are defined below for use in modeling Technology Demonstration Convertor (TDC) regenerators in CFD codes. Fluid continuity, momentum and energy equations, and a solid-energy equation, are stated for reference in defining the parameters needed. Experimental and computational data generated under a regenerator research grant⁶⁻⁸, and data from an oscillating-flow test rig⁹ are used in defining this initial set of parameters (i.e., in defining closure models).

First define superficial (Darcian), approach, velocity as $U = \langle u \rangle = ua / a_{total} = u \beta$. This is also the volume-flow rate through a unit cross-sectional area of the solid-plus-fluid. It is determined by averaging the velocity over a region that is small with respect to the macroscopic flow dimension but large with respect to the matrix-flow-channel size. In the above equation for superficial velocity, "a" is the average fluid-flow area within the total solid-plus-fluid cross-sectional area, a_{total} , that the velocity is averaged over to determine the superficial velocity, U. The porosity is β . The average-flow-channel fluid velocity (or local porous-media velocity) is u, corresponding to the

A. Non-Equilibrium Porous-Media Conservation Equations

superficial velocity, $U = \langle u \rangle$, and $u = \langle u \rangle / \beta$.

The incompressible-flow, non-equilibrium, porous-media equations from Ibrahim and Rong¹⁰ were used as a starting point; they used the volume-averaging approach described in Whitaker¹⁶ in deriving their macroscopic porous-media equations. Rewritten for compressible flow²⁶, and including a hydrodynamic dispersion term from Ayyaswamy^{†††}, the fluid continuity, momentum, and energy equations, respectively, written in terms of the superficial, or approach, or Darcian velocity are (where the brackets, <>>, denote volume averaging):

$$\frac{\partial \langle \rho \rangle^{f}}{\partial t} + \frac{1}{\beta} \nabla \bullet \left[\langle \rho \rangle^{f} \langle \mathbf{u} \rangle \right] = 0$$
⁽¹⁾

$$\frac{1}{\beta} \frac{\partial \left(\langle \rho \rangle^{f} \langle \mathbf{u} \rangle \right)}{\partial t} + \frac{1}{\beta^{2}} \nabla \bullet \left[\langle \rho \rangle^{f} \langle \mathbf{u} \rangle \langle \mathbf{u} \rangle \right] = -\nabla \langle \rho \rangle^{f} + \nabla \bullet \left(\frac{\langle v_{eff} \rangle^{f}}{\beta} \langle \rho \rangle^{f} \nabla \langle \mathbf{u} \rangle - \frac{\langle \rho \rangle^{f}}{\beta} \langle \tilde{\mathbf{u}} \tilde{\mathbf{u}} \rangle \right) - \frac{\langle \mu \rangle^{f}}{K} \langle \mathbf{u} \rangle - \langle \rho \rangle^{f} \frac{C_{f}}{\sqrt{K}} |\langle \mathbf{u} \rangle| \langle \mathbf{u} \rangle$$

$$(2)^{\ddagger \ddagger \ddagger 1}$$

$$\frac{\partial \left(\langle \rho \rangle^{f} \langle h \rangle^{f}\right)}{\partial t} + \frac{1}{\beta} \nabla \bullet \left[\langle \rho \rangle^{f} \langle \mathbf{u} \rangle \langle h \rangle^{f}\right] = \nabla \bullet \left[\overline{k}_{fe} \bullet \nabla \langle T \rangle^{f}\right] + \left(\frac{\mu}{K} + \langle \rho \rangle^{f} \frac{C_{f}}{\sqrt{K}} |\mathbf{u}|\right) \mathbf{u} \cdot \mathbf{u} + h_{sf} \frac{dA_{sf}}{dV_{f}} \left(\langle T \rangle^{s} - \langle T \rangle^{f}\right) + \frac{d\langle p \rangle^{f}}{dt}$$
(3)^{§§§},****

where the wetted area per unit fluid volume, $\frac{dA_{sf}}{dV_f} = \frac{1}{r_h}$ (and $r_h =$ hydraulic radius) and $\frac{d\langle p \rangle^f}{dt}$ is a substantial or material derivative. Finally, the solid energy equation is:

^{\$\$\$} The pressure-work term, $\frac{d\langle p \rangle^f}{dt}$, is the form for an ideal gas (helium, here). In general it should be written

 $\beta_{cte}T \frac{d\langle p \rangle^{f}}{dt}$. For an ideal gas, the coefficient of thermal expansion, $\beta_{cte} = \frac{1}{T}$.

**** Burmeister¹⁷ suggests the form of the fluid energy viscous dissipation terms, $\left(\frac{\mu}{K} + \langle \rho \rangle^{f} \frac{C_{f}}{\sqrt{K}} |\mathbf{u}|\right) \mathbf{u} \cdot \mathbf{u}$, here—which is consistent with the Darcy-Forchheimer terms in the momentum equation, (2).

^{†††} Ayyaswamy, P. S., University of Pennsylvania, Private Communication, 2004. Ayyaswamy described this $\tilde{u}\tilde{u}$ term as representing "the additional stresses due to the correlation between the velocity fluctuations associated with the hydrodynamic dispersion due to the solid matrix." A closure model for the term is discussed later in this paper.

^{‡‡‡} The effective viscosity used in the "Brinkman term" of this momentum equation is different than the molecular viscosity, in general, as a result of the solid/fluid interfaces within the matrix. The Brinkman term computes momentum transport where there are velocity gradients within the flow. Examples would be the jetting of fluid from adjacent heat exchanger passages into the matrix, etc.

$$\frac{\partial \left(\rho_{s} C_{s} \langle T \rangle^{s}\right)}{\partial t} = \nabla \bullet \left[\bar{\bar{k}}_{se} \bullet \nabla \langle T \rangle^{s}\right] - h_{sf} \frac{dA_{sf}}{dV_{s}} \left(\langle T \rangle^{s} - \langle T \rangle^{f}\right)$$
(4)

where the wetted area per unit solid volume, $\frac{dA_{sf}}{dV_s} = \frac{1}{r_h} \frac{1}{1-\beta}$.

Kaviany¹⁸ has described a momentum equation very similar to equation (2) as a "semiheuristic" equation. That is, most of the terms are multi-dimensional terms based on derivation from fundamentals. However, the last two terms of equation (2) are based on a "heuristic" extension from a 1D momentum equation (i.e., this is a "speculative extension" of an experimentally based 1D equation to serve as a guide in study of multi-dimensional problems, that has not been experimentally verified for multi-dimensional problems). Thus, in this initial or "draft" non-equilibrium porous-media model, we will assume that permeability is isotropic (Even though we know that the wirescreen used in engines and the UMN experiments is not isotropic, and because of the method of fabrication of random fiber material used in modern engines, it is believed that most of the lengths of those fibers, also, lie in planes perpendicular to the flow direction). Thus, as this porous-media model is improved upon, it may be desirable in the future to use anisotropic permeability. There are forms of Equation (2) with terms similar to the last two in equation (2), but in which the permeability is a tensor quantity¹⁶. But, in equation (2), permeability is a scalar quantity assumed to be the same for all directions. Similar statements can be made for the inertial term multiplier of

equation (2), i.e. C_f / \sqrt{K} .

The expressions or parameters in the above equations needing definition, for use in modeling Stirling regenerators, are: (1) the hydrodynamic dispersion term in the momentum equation; (2) scalar permeability, K, and (3) scalar inertial coefficient, C_f , in the momentum equation; (4) the fluid effective thermal conductivity, \overline{k}_{fe} , in the fluid-energy equation; (5) the solid effective thermal conductivity, \overline{k}_{se} , in the solid-energy equation, and (6) the heat-transfer coefficient between fluid and solid, h_{sf} , appearing in both fluid and solid energy equations. Note that the thermal conductivity expressions in the energy equations are tensors, though they are expected to have non-zero values only on the diagonals. The products of velocity vectors in the momentum equation are also tensors.

1.Hydrodynamic Dispersion

In the fluid momentum equation, equation (2) above, there is a hydrodynamic dispersion term:

$$\frac{1}{\beta} \langle \tilde{\mathbf{u}} \tilde{\mathbf{u}} \rangle \cong \tilde{\mathbf{u}} \tilde{\mathbf{u}}$$
(5)

where β is porosity; **u** is the average-channel fluid, or local, velocity inside the matrix, and $\tilde{\mathbf{u}}$ is the spatial-variation of the average-channel fluid velocity inside the matrix. $\tilde{\mathbf{u}}\tilde{\mathbf{u}}$ is a tensor quantity which can be expanded in the form:

$$i\tilde{\mathbf{u}} = \mathbf{i}i\tilde{u}\tilde{u} + \mathbf{i}j\tilde{u}\tilde{v} + \mathbf{i}k\tilde{u}\tilde{w} + \mathbf{j}i\tilde{v}\tilde{u} + \mathbf{j}j\tilde{v}\tilde{v} + \mathbf{j}k\tilde{v}\tilde{w} + \mathbf{k}i\tilde{w}\tilde{u} + \mathbf{k}j\tilde{w}\tilde{v} + \mathbf{k}k\tilde{w}\tilde{w}$$
(6)

For transport normal to the principal flow direction which is assumed to be the axial, **i**, direction, the mean velocity gradient is in the radial, **j**, direction and the term of interest (i.e. of significance) is $\tilde{u} \tilde{v}$, where v is the velocity component in that direction, = $|\mathbf{u}|\mathbf{j}$. Therefore the term from the above expression for transport normal to the flow is $|\tilde{u} \tilde{v}|$ or $|\tilde{v} \tilde{u}|$. The dispersion represented by this term is of axial momentum, ρu , but this term is in the direction normal to u (in the direction of v).

In Niu⁷ it was argued that this hydrodynamic dispersion could be equated to turbulent shear stress when the dispersion of interest is not in the direction of the mean flow, or $\langle \tilde{u}\tilde{v} \rangle = \langle \overline{u'v'} \rangle$ (where the prime refers to temporal variations about the temporal average, the overbar refers to a temporal average, and <> refers to spatial average) and that $\langle \overline{u'v'} \rangle$ could be modeled as $\varepsilon_{\rm M} = \lambda d_{\rm h} U$ where $\langle \overline{u'v'} \rangle = -\varepsilon_{\rm M} \frac{\partial U}{\partial r}$ and $\lambda \approx 0.02$, and where $d_{\rm h} =$ the hydraulic diameter, u = the in-matrix average velocity, and $U = \langle u \rangle$ is the superficial, Darcian, or approach velocity. Therefore, for use in equation (6), and in the momentum equation, (2):

$$\frac{\overline{\langle \tilde{u}\tilde{v} \rangle}}{\beta^2} = \frac{\overline{\langle \tilde{v}\tilde{u} \rangle}}{\beta^2} \approx \frac{\langle u'v' \rangle}{\beta^2} = -\frac{1}{\beta^2} \varepsilon_M \frac{\partial U}{\partial r} = -\frac{1}{\beta^2} 0.02 d_h U \frac{\partial U}{\partial r} = -\frac{1}{\beta^2} \lambda d_h U \frac{\partial U}{\partial r}$$
(7)

2. Permeability and Inertial Coefficient

In the fluid momentum equation, (2), the permeability, K, and the inertial coefficient, C_f , need evaluation for

each type of porous medium. These coefficients can be evaluated for particular types of Stirling engine regenerator porous media via use of the friction-factor data from the oscillating-flow test rig given in Gedeon⁹ under the assumption that the flow is quasi-steady^{††††, 19}. The Darcy-Forchheimer steady-flow form of the 1-D fluid momentum equation, and a similar pressure-drop equation, but in terms of the Darcy friction factor, can be written, respectively:

$$\frac{\nabla p}{L} = \frac{\mu}{K} u + \frac{C_f}{\sqrt{K}} \left\langle \rho \right\rangle^f u^2 \tag{8}$$

$$\frac{\nabla p}{L} = \frac{f_D}{d_h} \frac{1}{2} \left\langle \rho \right\rangle^f u^2 \tag{9}$$

From the oscillating-flow test rig data, as summarized by correlations given in the Sage manuals⁹, it was determined that friction-factor correlations for random fiber and wire screen are of the form:

$$f_D = \frac{\alpha}{\text{Re}} + \delta \text{Re}^{\gamma}$$
 where Reynolds #, Re = $\frac{\rho_f u d_h}{\mu}$ (10)

And where, for random fiber, $\alpha = 192$, $\delta = 4.53$, $\gamma = -0.067$, and for woven screen, $\alpha = 129$, $\delta = 2.91$, $\gamma = -0.103$. Substituting the expression for friction-factor and the definition of Reynolds number from equations (10), into equation (9), and then equating the right-hand sides of equations (8) and (9), it can be determined that:

$$\frac{K}{d_h^2} = \frac{2}{\alpha} \quad \text{and} \quad C_f = \frac{\delta \operatorname{Re}^{\gamma}}{\sqrt{2\alpha}} \tag{11}$$

A frequently used expression for hydraulic diameter of random fiber and wire screen, in terms of porosity and wire diameter is:

$$d_h = \frac{\beta}{1-\beta} d_w \tag{12}$$

For the welded stacked-screens used in the UMN regenerator test module⁶ where $\beta = 0.9$ and $d_{w} = 0.81$ mm or

8.1E-4 m, then $d_h = 7.29E-3$ m. If it is also assumed that Reynolds No.'s are in the range from 25-100, as expected

in the TDC regenerators, then equations (11) can be used to calculate values of permeability and inertial coefficient for TDC random fiber and the large screens used in the test module. The resulting TDC random fiber values are given in Table 1. The TDC random fiber results given in Table 1, in the rightmost column, are based on unidirectional flow tests of the entire TDC heater head (including heater, regenerator and cooler), taken from Wilson¹⁹ The "UMN old" and "UMN new" values of permeability, in Table 1, are experimentally determined values of permeability and inertial coefficient, determined at an earlier and a later time^{‡‡‡‡‡}. The "CSU Calcs." are calculated values determined via microscopic CFD modeling of the UMN steady-flow test module^{§§§§§}. For the large scale-screens (see Table 1), results derived from the Sage empirical correlations and the microscopic CFD calculations are seen to be in relatively close agreement. The substantially greater differences of these values from the UMN test results have not been explained. The significance of differences such as these should be examined via a sensitivity study using a macroscopic porous-media model; this has not yet been done.

3. Effective Fluid and Solid Thermal Conductivities

In the fluid energy equation, (3), $\bar{k}_{fe} \equiv$ an effective fluid conductivity tensor, each element of which is, in

general, a sum of components due to molecular conductivity, thermal tortuosity conductivity and thermal dispersion conductivity. It can be broken down into these components as follows: From equation (3),

$$\bar{\bar{k}}_{fe} \bullet \nabla \langle T \rangle^{f} = \bar{\bar{k}}_{f} \bullet \nabla \langle T \rangle^{f} + \frac{1}{V_{f}} [_{Asf} \bar{\bar{k}}_{f} T dA - \rho_{f} C_{p} \langle \tilde{T} \tilde{\mathbf{u}} \rangle$$
(13)

^{††††} Tew, R. C., Private Communication, 2005.

^{‡‡‡‡} Simon, T., University of Minnesota, Private Communication, ~2003.

^{\$\$\$\$} Ibrahim, M. B., Cleveland State University, Private Communication, 2003.

Coefficient		UMN Large-S (d _w =8.11	TDC Random Fiber			
	UMN Old, Experimental	UMN New, Experimental	CSU Calcs.	Sage Cor.	Sage Cor.	Unidirectional Flow Tests
K (m ²)	1.07E-7	1.86E-7	8.9E-7	8.24E-7	4.08E-10	3.52E-10
K/d_W^2	0.163	0.283	1.36	1.26	-	-
C _f	0.049	0.052	0.14	0.13-0.11 Re=25-100	0.19-0.17 Re=25-100	0.154-0.095 Re=25-100

 Table 1.
 Values of Permeability, K, and Inertial Coefficient, C_f, for the Large-Scale UMN Wire Screen and TDC Random Fiber Regenerator Materials.

where:

$$\frac{1}{V_f} \int_{Asf} \bar{\bar{k}}_f T \, dA = \bar{\bar{k}}_{tor} \cdot \nabla \langle T \rangle^f \tag{14}$$

Equation (14) defines the thermal tortuosity thermal conductivity, \bar{k}_{tor} .

$$-\rho_{f}C_{p}\langle \tilde{T}\tilde{\mathbf{u}}\rangle \equiv \bar{k}_{dis} \bullet \nabla \langle T \rangle^{f}$$
(15)

Equation (15) defines the thermal dispersion thermal conductivity, \bar{k}_{dis} .

$$\cdot \quad \overline{\bar{k}}_{fe} \bullet \nabla \langle T \rangle^{f} = \overline{\bar{k}}_{f} \bullet \nabla \langle T \rangle^{f} + \overline{\bar{k}}_{tor} \bullet \nabla \langle T \rangle^{f} + \overline{\bar{k}}_{dis} \bullet \nabla \langle T \rangle^{f}$$
(16)

Equation (16) defines the effective fluid thermal conductivity, \overline{k}_{fe} .

and
$$\bar{\bar{k}}_{fe} = \bar{\bar{k}}_{f} + \bar{\bar{k}}_{f,tor} + \bar{\bar{k}}_{dis} = \bar{\bar{k}}_{f,stag} + \bar{\bar{k}}_{dis}$$
 (17)

Where, in the above equation, the sum of the fluid molecular and thermal tortuosity conductivities are lumped together and called the fluid stagnant thermal conductivity.

It is assumed that only the diagonal elements of the effective fluid conductivity tensor are non-zero. Then in terms of 3-D cylindrical coordinates which are appropriate for Stirling engine simulation, it is further assumed that:

$$\overline{k}_{fe} = \begin{bmatrix} k_{fe,rr} & 0 & 0 \\ 0 & k_{fe,99} & 0 \\ 0 & 0 & k_{fe,xx} \end{bmatrix} = \begin{bmatrix} k_{f}+k_{f,tor,rr}+k_{dis,rr} & 0 & 0 \\ 0 & k_{f}+k_{f,tor,99}+k_{dis,99} & 0 \\ 0 & 0 & k_{f}+k_{f,tor,xx}+k_{dis,xx} \end{bmatrix} =$$

$$\begin{bmatrix} k_{f,stag,rr}+k_{dis,rr} & 0 & 0 \\ 0 & k_{f,stag,99}+k_{dis,99} & 0 \\ 0 & 0 & k_{f,stag,xx}+k_{dis,xx} \end{bmatrix}$$
(18)

In the above tensor equation for fluid effective thermal conductivity, (18), molecular conductivity is isotropic, and fluid tortuosity and dispersion conductivities will be assumed anisotropic. In general, the tortuosity conductivity is different in different directions when the alternating fluid/solid geometry is different when looking in different directions. Therefore, when fluid molecular and thermal tortuosity conductivities are lumped together to form the stagnant thermal conductivity is also, in general, different in different directions—as dictated by the geometry of the matrix. The thermal dispersion conductivity has contributions from an advective term and an eddy term. In the flow direction there would be both. Normal to the flow direction, there is only the eddy dispersion term.

In the solid energy equation, (4), the effective solid conductivity, $\overline{\overline{k}}_{se}$, is defined:

$$\bar{\bar{k}}_{se} = \begin{bmatrix} k_{se,rr} & 0 & 0\\ 0 & k_{se,99} & 0\\ 0 & 0 & k_{se,xx} \end{bmatrix} = \begin{bmatrix} f(k_s,k_{s,tor,rr}) & 0 & 0\\ 0 & f(k_s,k_{s,tor,99}) & 0\\ 0 & 0 & f(k_s,k_{s,tor,xx}) \end{bmatrix}$$
(19)

The molecular thermal conductivities can be assumed to be well known. That leaves to be determined: (1) fluid thermal dispersion and (2) fluid stagnant conductivities and solid effective conductivities—which are each functions of the molecular conductivity and the thermal tortuosity conductivity, for the fluid or solid; thus the form of the last matrix of equation (19).

4. Thermal Dispersion Conductivity

Niu⁷ and other researchers, have measured eddy diffusivity (or transport) in, or very close to, porous media. If it is assumed that this is also equivalent to thermal dispersion due to eddies, as in Niu⁷, based on the Reynolds Analogy, then values for thermal dispersion due to eddies are given in Table 2, below, in terms of porous media hydraulic diameter, d_h , and superficial, approach, or Darcian velocity, $U = \langle u \rangle$. Although in general thermal dispersion by eddies is expected to be anisotropic, for this initial model it may be adequate to use the same relationship to calculate eddy dispersion in all directions. It should be noted, however, that in the flow direction, total dispersion is only by eddies. To explore further possible differences of eddy dispersion in different directions refer to Niu⁶⁻⁸, McFadden²⁰ and Simon²¹. Once a macroscopic thermal non-equilibrium model is implemented in a Stirling CFD code, the significance of the differences in Table 2 can be explored via a sensitivity study.

Table 2. A Comparison of Therman Dispersion Coefficients from Several Methods. Taken from Nu .					
	Estimated Thermal Dispersion	Porous media			
Current Direct Measurements at UMN, Niu ⁷	$\varepsilon_{M,eddy} = \frac{k_{dis,yy}}{\rho_f c_p} = 0.02 d_h U \text{ or } \frac{k_{dis,yy}}{k_f} = 0.02 Pe$	Welded Screen			
Hunt and Tien ²²	$\frac{k_{dis,yy}}{k_f} = 0.0011 Pe$	Fibrous Media			
Metzger, Didierjean, and Maillet ²³	$\frac{k_{dis,yy}}{k_f} = (0.03 - 0.05)Pe \text{ and } \frac{k_{dis,xx}}{k_f} = 0.073 Pe^{1.59}$	Packed Spheres			
Gedeon ⁹	$\frac{k_{dis,xx}}{k_f} = 0.50 P e^{0.62} \beta^{-2.91} \text{ or } \frac{k_{dis,xx}}{k_f} \approx 0.06 P e \text{ for } \beta = 0.9, P e = 560$	Woven Screen			

Table 2. A Comparison of Thermal Dispersion Coefficients from Several Methods. Taken from Niu⁷.

5. Fluid-Stagnant and Solid-Effective Thermal Conductivity

The fluid-stagnant and solid-effective thermal conductivities (each a function of the appropriate molecular and thermal tortuosity conductivities) are estimated based on the geometry of the matrix of interest. McFadden²⁰ calculated a radial stagnant conductivity for the welded screens based on considerations of the geometry of the large-scale wire screens. Similar calculations are made for a fluid-saturated metal foam in Boomsma²⁴. In the case of the Stirling TDC that has been modeled with CFD codes, a random fiber matrix is used in the regenerator. Since the details of the geometry for such a matrix are random, some assumptions must be made, as discussed below.

For comparison with the calculations of McFadden²⁰, mentioned above, the same molecular thermal conductivities used by McFadden will be used here (i.e. for air and stainless steel): So, assume that: $k_s = 13.4$ W/m-

K for Stainless Steel 316, $k_f = 0.026$ W/m-K for air at standard temperature, and $\beta = 0.90$.

In the random fiber matrix most of the lengths of the fibers are believed to lie in planes perpendicular to the main flow axis. Therefore, initially make the assumption that for a 3-D CFD model, the effective solid+fluid conductivity in the radial and azimuthal directions (that would be appropriate for use in an equilibrium porous-media model) follows the parallel model defined below, and the effective solid+fluid conductivity in the axial direction follows the series model, also defined below.

The parallel model for this lumped effective conductivity for fluid and solid, assuming all of the fibers run in the same direction (not including the fluid thermal dispersion) is:

$$k_{eff,s+f} = k_f \beta + k_s (1-\beta)$$
⁽²⁰⁾

Therefore, this effective solid+fluid conductivity for air and stainless steel combined, for a 90% porosity matrix, would be:

$$k_{eff,s+f} = (26x10^{-3} W / mK) (0.90) + (13.4 W / mK) (0.1)$$

= 0.0234 W / mK + 1.34 W / mK = 1.36 W / mK

As already mentioned, the above would be an appropriate effective solid+fluid thermal conductivity for an equilibrium porous media model. However for a non-equilibrium porous media model, assume that the two terms on the right of the above equation represent the fluid stagnant thermal conductivity and the solid effective conductivity, respectively. That is, assume:

$$k_{f,stag} = k_{f} \beta = (26 \times 10^{-3} W / mK) (0.90) = 0.0234 W / mK$$
$$k_{se} = k_{s} (1 - \beta) = (13.4 W / mK) (0.1) = 1.34 W / mK$$

However, in accordance with McFadden²⁰:

$$k_s / k_f = 13.4 / 26 x 10^{-3} = 515$$
 and $k_{eff,s+f} / k_f = 1.36 / 26 x 10^{-3} = 52$

The value 52 is considerably larger than the 32.5 estimated by UMN for their wire screen in McFadden²⁰, based on average geometrical considerations, rather than the parallel model. Since wire screen and random fiber are thought to have similar heat transfer properties, perhaps the solid part of the parallel model should be corrected to the UMN wire screen value by multiplication by the correction factor:

Then the corrected parallel values for use for random fiber in the radial and azimuthal directions would be:

$$k_{eff,s+f} = 0.0234 + 1.36 \times 0.625 = 0.873$$
 (for equil., model)
 $k_{se} = k_s (1-\beta) 0.625 = 1.34 W / mK \times 0.625 = 0.838$ (for non – equil. model, radial & azimuthal directions)

For the axial direction, the lumped effective solid + fluid effective conductivity, $k_{eff,s+f}$, (which also doesn't include thermal dispersion) should be substantially less than in the radial and azimuthal directions. Initially assume the series model mentioned in Ref. 14. That is:

$$k_{eff,s+f} = \left(\frac{1}{\frac{\beta}{k_f} + \frac{1-\beta}{k_s}}\right) = \left(\frac{1}{\frac{0.90}{26 \times 10^{-3}} + \frac{0.1}{13.4}}\right) = 0.0289 \, W \, / \, mK \tag{21}$$

This axial effective solid+fluid thermal conductivity (not including thermal dispersion) is just slightly larger than the molecular fluid conductivity for air of 0.026 W/m-K and is probably too small since this series model assumes that the wires are not touching in the axial direction. 3-D CFD microscopic simulations of a representative elementary volume of the UMN regenerator by Rong^{******}, suggest that the value shown in equation (21) should be increased by a factor of 2.157. Therefore assume that:

$$k_{eff,s+f} = \left(\frac{2.157}{\frac{\beta}{k_f} + \frac{1-\beta}{k_s}}\right) = \left(\frac{2.157}{\frac{0.90}{26 \times 10^{-3}} + \frac{0.1}{13.4}}\right) = \left(0.0289 \, W \,/\, mK\right) \left(2.157\right) = 0.0623 \, W \,/\, mK \ (axial \ direction)$$
(22)

This resulting effective solid+fluid thermal conductivity in the axial direction would be appropriate for an equilibrium model. Seeing no obvious way to separate values for fluid and solid for a non-equilibrium macroscopic porous media model, based on the series model, we propose initially using this same value for both the fluid-stagnant and solid-effective conductivities in the axial direction in the non-equilibrium model, also—hoping that the overall axial effect might be reasonable.

Recall that to get the total effective fluid conductivities in different directions, the thermal dispersion conductivity should be added to the fluid stagnant conductivities in the radial, azimuthal and axial directions. Also, for use in modeling the TDC regenerator, the above effective conductivities must be recalculated using the thermal conductivity of helium instead of air.

^{*****} Rong, W., Cleveland State University, Private Communication, 2005.

Literature searches for experimental effective fluid+solid effective thermal conductivities (appropriate for an equilibrium porous-media model) might prove useful. One attempt to locate such information via the website of the National Institute of Standards and Technology (NIST) was not successful.

6. Heat Transfer Coefficient between Fluid and Solid Matrix Elements

A good source of heat transfer correlations for wire screen and random fiber Stirling regenerator materials is Gedeon⁹. These correlations are based on experimental data from the NASA/Sunpower oscillating-flow test rig; this rig was designed and fabricated specifically for the purpose of determining friction-factor and heat-transfer correlations for use in Stirling device design and modeling. Heat transfer correlations in terms of Nusselt No., Peclet Number (Reynolds No. x Prandtl No.), and porosity are:

For wire screen, $Nu = (1.+0.99 Pe^{0.66}) \beta^{1.79}$ and for random fiber, $Nu = (1.+1.16 Pe^{0.66}) \beta^{2.61}$ where

$$Nu = \frac{hd_h}{k}, \quad Pe = Re \ Pr = \frac{\rho u d_h}{\mu} \frac{c_p \mu}{k}$$

Measurements by Niu²⁵ indicated that the above correlation and its application in a quasi-steady fashion is suitable for the portion of an oscillatory cycle when the acceleration is sufficiently weak or the flow is decelerating, but during strong acceleration, the unsteady measurements indicate a violation of the quasi-steady-flow assumption characterized by a lag between the heat flux from one phase of the matrix to the other and the temperature difference between phases. The measurements also showed an apparently poor mixing of the flow in the pore during the strong acceleration portions of the cycle. The Valensi number based on molecular (rather than eddy) viscosity) of the flow was 2.1, which is a bit higher than values in the general operating range of an engine regenerator (~0.23 for one engine). Thus, this unsteady effect may have been overestimated. The data also indicate that over the full cycle, an estimate given by the correlation above and applied as if the flow were quasi-steady is a reasonable approach for this initial or "draft" model.

III. Concluding Remarks

A set of transient, compressible-flow, conservation equations is summarized for reference in defining the parameters whose values are needed for a macroscopic, thermal-non-equilibrium porous-media model. Such a porous-media model is needed in existing commercial CFD codes (such as CFD-ACE and Fluent) in order to more accurately model the regenerator heat exchanger in Stirling engine devices (since only equilibrium porous-media models are now available in the Fluent and CFD-ACE codes). Available experimental information from large-scale wire-screen testing is used to define a hydrodynamic-dispersion term in the momentum equation. Experimental information is also used for definition of the permeability and inertial coefficients in the momentum equation and for the thermal-dispersion conductivity for the regenerator fluid. Methods are also outlined for estimating the stagnant-fluid and effective-solid thermal conductivities. Thus adequate information is presented for definition of an initial, or "draft," non-equilibrium porous media model for use in CFD regenerator modeling of Stirling devices. It is anticipated that use of this initial model in CFD codes may demonstrate that further work on refinement of the non-equilibrium porous-media model and its parameters will be needed.

References

¹Schreiber, J. G. and Thieme, L.G., "Accomplishments of the NASA GRC Stirling Technology Development Project," in proceedings of 2ndInternational Energy Conversion Engineering Conference, AIAA-2004-5517, Providence, RI, 2004.

²Thieme, L. G. and Schreiber, J. G., "Advanced Technology Development for Stirling Convertors," in proceedings of *Space Technology and Applications International Forum (STAIF 2004)*, edited by M. El-Genk, AIP Conference Proceedings 654, Melville, New York, pp. 432-439, 2004.

³Dyson, R. W., Wilson, S. D., and Demko, R., "On the Need for Multidimensional Stirling Simulations," in proceedings of 3rd International Energy Conversion Engineering Conference, Paper No. AIAA-2005-5557, San Francisco, CA, 2005.

⁴Dyson, R. W., Wilson, S. D., and Demko, R., "Fast Whole-Engine Stirling Analysis," in proceedings of 3rd International Energy Conversion Engineering Conference, Paper No. AIAA-2005-5558, San Francisco, CA, 2005.

⁵Ibrahim, M., Mittal, M., Jiang, N., and Simon, T., "Validation of Multi-Dimensional Stirling Engine Codes: Modeling of the Heater Head," in proceedings of 3rd International Energy Conversion Engineering Conference, Paper No. AIAA-2005-5654, San Francisco, CA, 2005.

⁶Niu, Y., Simon, T.W., Ibrahim, M.B., Tew, R., and Gedeon, D., "JET Penetration into a Stirling Engine Regenerator Matrix with Various Regenerator-to-Cooler Spacings," in proceedings of *1st International Energy Conversion Engineering Conference*, Paper No. AIAA-2003-6014, Portsmouth, VA, 2003.

⁷Niu, Y., Simon, T., Gedeon, D. and Ibrahim, M., "On Experimental Evaluation of Eddy Transport and Thermal Dispersion in Stirling Regenerators," in proceedings of 2nd International Energy Conversion Engineering Conference, Paper No. AIAA-2004-5646, Providence, RI, 2004.

⁸Niu, Y., McFadden, G., Simon, T., Ibrahim, M. and Wei, R., "Measurements and Computation of Thermal Dispersion in a Porous Medium," in proceedings of 3rd International Energy Conversion Engineering Conference, Paper No. AIAA-2005-5578, San Francisco, CA, 2005.

⁹Gedeon, D., "Sage Stirling Cycle Model Class Reference Guide," 3rd Edition, Gedeon Associates, Athens, OH, 1999.

¹⁰Ibrahim, M. B., Rong, W., Simon, T., Tew, R., and Gedeon, D., "Simulations of Flow and Heat Transfer inside Regenerators Made of Stacked Welded Screens Using Periodic Cell Structures," in proceedings of 2nd International Energy Conversion Engineering Conference, Paper No. AIAA-2004-5599, Providence, RI, 2004.

¹¹Singh, C., Tathgir, R. G., and Muralidhar, K., "Comparison of 1-equation and 2-equation Models for Convective Heat Transfer in Saturated Porous Media," *The Institution of Engineers (India) Journal*, Vol. 84, MC 3, pp. 104-113, October 2003.

¹²Amiri, A. and Vafai, K., "Transient Analysis of Incompressible Flow through a Packed Bed," *Int. J. Heat Mass Transfer*, Vol. 41, pp. 4259-4279, 1998.

¹³Minkowcyz, W. J., Haji-Sheikh, A. and Vafai, K., "On Departure from Local Thermal Equilibrium in Porous Media due to a Rapidly Changine Heat Source: The Sparrow Number," *Int. J. Heat Mass Transfer*, Vol. 42, pp. 3373-3385, 1999.

¹⁴Muralidhar, K. and Suzuki, K., "Analysis of Flow and Heat Transfer in a Regenerator Mesh using a Non-Darcy Thermally Non-Equilibrium Model," *Int. J. Heat Mass Transfer*, Vol. 44, pp. 2493-2504, 2001.

¹⁵Gedeon, D., "Mainifest: A Computer Program for 2-D Flow Modeling in Stirling Machines," NASA CR 182290, 1989.

¹⁶Whitaker, S., "The Forchheimer Equation: A Theoretical Development," *Transport in Porous Media*, Vol. 25, pp.27-61, 1996.

¹⁷Burmeister, L. C., *Convective Heat Transfer*, 2nd Ed., pp 48-50, Wiley, 1993.

¹⁸Kaviany, M., *Principles of Heat Transfer in Porous Media*, Spring-Verlag, Mechanical Engineering Series, 2nd Edition, pp 66-67 and 47, 1995.

¹⁹Wilson, S. D., Dyson, R. W., Tew, R. C., and Demko, R., "Experimental and Computational Analysis of Unidirectional Flow through Stirling Engine Heater Head," 3rd International Energy Conversion Engineering Conference, Paper No. AIAA-2005-5539, San Francisco, CA, 2005.

²⁰McFadden, G., "Forced Thermal Dispersion Within a Representative Stirling Engine Regenerator," University of Minnesota Master's Thesis, 2005.

²¹Simon, T., McFadden, G. and Ibrahim, M., "Thermal Dispersion within a Porous Medium Near a Solid Wall," To be Presented at *International Heat Transfer Conference*, Sydney, Australia, Aug. 13-18, 2006.

²²Hunt, M. L. and Tien, C. L., "Effects of Thermal Dispersion on Forced Convection in Fibrous Media," *Int. J. Heat Mass Transfer*, Vol. **31**, pp. 301-308, 1988.

²³Metzger, T., Didierjean, S. and Maillet, D., "Optimal Experimental Estimation of Thermal Dispersion Coefficients in Porous Media," *Int. J. Heat Mass Transfer*, Vol. **47**, pp. 3341-3353, 2004.

²⁴Boomsma, K., and Poulikakos, D., "On the Effective Thermal Conductivity of a Three-Dimensionally Structured Fluid-Saturated Metal Foam," *Int. J. of Heat & Mass Transfer*, Vol. **44**, pp. 827-836, 2001.

²⁵Niu, Y., Simon, T.W., Ibrahim, M.B., Tew, R., and Gedeon, D., "Measurements of Unsteady Convective Heat Transfer Rates within a Stirling Regenerator Matrix Subjected to Oscillatory Flow," in proceedings of *1st International Energy Conversion Engineering Conference*, Paper No. AIAA-2003-6013, Portsmouth, VA, 2003.

²⁶Bird, R. B., Steward, W. E., and Lightfoot, E. N., *Transport Phenomena*, 1st Ed., Chapter 3 for Continuity and Momentum Equations, Chapter 10 for Fluid Energy Equation, Wiley, 1960.

REPORT DOCUMENTATION PAGE

Form Approved OMB No. 0704-0188

Public reporting burden for this collection of informa gathering and maintaining the data needed, and cor collection of information, including suggestions for re Davis Highway, Suite 1204, Arlington, VA 22202-43	mpleting and reviewing the collection of in educing this burden, to Washington Heado	formation. Send comments regardi quarters Services, Directorate for In	ing this burden estimate or any other aspect of this formation Operations and Reports, 1215 Jefferson	
1. AGENCY USE ONLY (Leave blank)				
4. TITLE AND SUBTITLE			5. FUNDING NUMBERS	
An Initial Non-Equilibrium Po Stirling Regenerators	rous-Media Model for CFD S		WBS 138494.04.01.01	
6. AUTHOR(S)	WD3 130494.04.01.01			
Roy C. Tew, Terry Simon, Dav	id Gedeon, Mounir Ibrahim,	and Wei Rong		
7. PERFORMING ORGANIZATION NAME	3. PERFORMING ORGANIZATION REPORT NUMBER			
National Aeronautics and Space	e Administration			
John H. Glenn Research Center	E-15669			
Cleveland, Ohio 44135–3191		E-13009		
9. SPONSORING/MONITORING AGENCY	10. SPONSORING/MONITORING AGENCY REPORT NUMBER			
National Aeronautics and Space	e Administration			
Washington, DC 20546–0001	NASA TM-2006-214391			
Washington, DC 20340-0001			NASA IM—2000-214391	
11. SUPPLEMENTARY NOTES				
Simon, Department of Mechanical David Gedeon, Gedeon Associates	l Engineering, University of Min s, 16922 South Canaan Road, Atl ad State University, 1960 East 24	nesota, 111 Church Street, hens, Ohio 45701; Mounir 1 th Street, Cleveland, Ohio 4	ew, NASA Glenn Research Center; Terry S.E., Minneapolis, Minnesota 55455; Ibrahim and Wei Rong, Department of 44115. Responsible person, Roy C. Tew,	
12a. DISTRIBUTION/AVAILABILITY STA			12b. DISTRIBUTION CODE	
Unclassified - Unlimited				
Subject Category: 20				
Available electronically at <u>http://gltr</u>	s.grc.nasa.gov			
This publication is available from the	e NASA Center for AeroSpace Inf	Formation, 301–621–0390.		
13. ABSTRACT (Maximum 200 words)				
for use in Computational Fluid used at Glenn Research Center equilibrium models, which assu assumption for Stirling regener regenerator models and sugges axial location and time during t permeability, inertial coefficien effective thermal conductivity	Dynamics (CFD) codes for s for Stirling modeling are Flu ume solid matrix and fluid are rators; Stirling 1–D regenerate t regenerator matrix and gas a the cycle. Experimentally bas at, fluid effective thermal con	simulation of Stirling reg nent and CFD-ACE. The e in thermal equilibrium. or models, used in Stirlir average temperatures car sed information was used ductivity, and fluid-solid	ng design, use non-equilibrium n differ by several degrees at a given l to define: hydrodynamic dispersion, l heat transfer coefficient. Solid	
matrix. Emphasis is on use of a	g Technology Demonstration available data to define empir	Converter (TDC), which ical parameters needed in	ers was based on planned use in a a uses a random-fiber regenerator n a thermal non-equilibrium porous- lemented by the authors or their	
matrix. Emphasis is on use of a media model for Stirling regen	g Technology Demonstration available data to define empir	Converter (TDC), which ical parameters needed in	n uses a random-fiber regenerator n a thermal non-equilibrium porous-	
matrix. Emphasis is on use of a media model for Stirling regenerassociates.	g Technology Demonstration available data to define empir erator simulation. Such a mo	Converter (TDC), which ical parameters needed in del has not yet been impl	a uses a random-fiber regenerator n a thermal non-equilibrium porous- lemented by the authors or their	
 matrix. Emphasis is on use of a media model for Stirling regeneration associates. 14. SUBJECT TERMS Stirling engines; Porous media	g Technology Demonstration available data to define empir erator simulation. Such a mo	Converter (TDC), which ical parameters needed in del has not yet been impl	a uses a random-fiber regenerator n a thermal non-equilibrium porous- lemented by the authors or their 15. NUMBER OF PAGES 19 16. PRICE CODE	
 matrix. Emphasis is on use of a media model for Stirling regeneration associates. 14. SUBJECT TERMS Stirling engines; Porous media 17. SECURITY CLASSIFICATION 18. 	g Technology Demonstration available data to define empir erator simulation. Such a mod model; Regenerator; Compu SECURITY CLASSIFICATION	Converter (TDC), which ical parameters needed in del has not yet been impl terized simulation; CFD	a uses a random-fiber regenerator n a thermal non-equilibrium porous- lemented by the authors or their 15. NUMBER OF PAGES <u>19</u> 16. PRICE CODE	