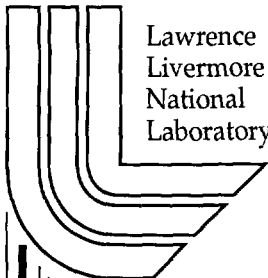


Radiative Strength Functions and Level Densities

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RADIATIVE STRENGTH FUNCTIONS AND LEVEL DENSITIES

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Radiative strength functions and level densities have been extracted from primary γ -ray spectra for $^{27,28}\text{Si}$, $^{56,57}\text{Fe}$, $^{96,97}\text{Mo}$, and several rare earth nuclei. An unexpectedly strong (~ 1 mb MeV) resonance at 3 MeV in the radiative strength function has been observed for well-deformed rare earth nuclei. The physical origin of this resonance and its connection to the scissors mode is discussed.

1. Introduction

Radiative strength functions and level densities are important quantities in low-energy nuclear structure. Since the first estimate of level densities by Bethe in 1936¹, level densities and related thermodynamical quantities like entropy and the caloric curve have been investigated in order to map out structural changes in atomic nuclei like the pairing phase transition^{2,3,4,5}. On the experimental side, level densities have been studied by a variety of methods like counting of discrete levels^{6,7} at low energies, the study of neutron resonance spacings⁸ at the neutron binding energy B_n , evaporation spectra⁹ over large energy intervals, and Erickson fluctuations¹⁰ for light nuclei ($A \leq 60$). Modern nuclear theory treats the problem of nuclear level densities by a variety of methods like relativistic mean field theory¹¹, finite temperature random phase approximation¹², finite temperature Hartree

Fock Bogoliubov method¹³ and shell model Monte Carlo calculations^{14,15}. Those methods have the advantage that realistic nucleon-nucleon interactions are taken into account.

Radiative strength functions are a measure of the average electromagnetic response of atomic nuclei. The concept of radiative strength functions was introduced by Blatt and Weisskopf¹⁶. They showed that the square of the γ -transition matrix element connecting compound states is proportional to the level spacing of the initial states with equal spin and parity. This led to the model-independent definition of the radiative strength function of multipolarity XL in terms of average partial radiative widths Γ_i , level spacing D_i and transition energy E_γ according to:

$$f_{XL} = \Gamma_i / (E_\gamma^{2L+1} D_i). \quad (1)$$

The most important radiative strength functions for the statistical decay of nuclei are the electric dipole ($E1$), the magnetic dipole ($M1$) and to a lesser extent the electric quadrupole ($E2$) strength functions. Experimentally, information about radiative strength functions has been obtained by the study of photoabsorption cross sections^{17,18}, by various methods involving radiative neutron capture like the spectrum fitting method¹⁹, the investigation of primary γ rays of different multiplicities^{20,21,22} and the two-step cascade method^{23,24}, and finally by a sequential extraction method involving charged particle reactions²⁵. Theoretical investigations of radiative strength functions improved when Axel realized that the energy independent Weisskopf estimate failed to describe the experimental $E1$ strength function²⁶. Instead, resonance models were developed for the different strength functions, including the $E1$ giant electric dipole resonance (GEDR), the $M1$ giant magnetic dipole or spin flip resonance (GMDR)^{21,27} and the weakly collective isovector $M1$ orbital resonance or scissors mode (SM)^{28,29}. Special interest remains in the investigation of the tail of the GEDR. Popov showed in his fundamental work on $(n, \gamma\alpha)$ reactions, that the $E1$ strength function in spherical nuclei like ^{144}Nd tends to approach a finite value for small transition energies³⁰. Based on this observation, temperature dependent models of the tail of the GEDR were developed^{31,32}. The exact mechanism for a temperature dependent width of the GEDR is presently still under discussion^{33,34,35,36}. Also, microscopic calculations of strength functions have been attempted in some cases^{37,38}.

An important application of level densities and radiative strength functions are Hauser-Feshbach calculations of reaction cross-sections³⁹. The knowledge of such cross-sections is important for astrophysical applications⁴⁰, accelerator driven transmutation of radioactive nuclear

waste and the production of radioisotopes⁴¹.

Recently, the group at the Oslo Cyclotron Laboratory (OCL) substantially improved the sequential extraction method. They achieved the simultaneous extraction of radiative strength functions and level densities without making *a priori* assumptions on the functional form of either quantity⁴². This progress has spawned several articles on level densities, thermodynamical properties and radiative strength functions of different nuclei^{43,44,45,46,47,48,49,50,51,52,53}. The present work recapitulates the most exciting findings of this work and gives examples of several new investigations.

2. Method

Experiments were carried out with 45-MeV ^3He projectiles at the OCL. Particle- γ coincidences were measured with the CACTUS multidetector array⁵⁴ using the $(^3\text{He},\alpha\gamma)$ and $(^3\text{He},^3\text{He}'\gamma)$ reaction on ~ 1.5 mg/cm², self supporting targets of high isotopic enrichment ($\sim 95\%$). The light charged particles were detected with eight particle telescopes placed at an angle of 45° relative to the beam axis. An array of 28 NaI γ -ray detectors with a total efficiency of $\sim 15\%$ of 4π surrounded the target and particle detectors.

Total γ cascade spectra can be sorted out with respect to the initial excitation energy E from measured particle- γ coincidences, since the nuclear reaction can be fully reconstructed kinematically. These spectra are unfolded using a Compton-subtraction method⁵⁵. A subtraction procedure is then applied to extract the primary γ -ray spectra $P(E, E_\gamma)$ ⁵⁶ which is subsequently factorized according to the Axel-Brink hypothesis^{26,57}:

$$P(E, E_\gamma) \propto T(E_\gamma)\rho(E - E_\gamma). \quad (2)$$

Here, T is the γ -ray transmission coefficient and ρ is the level density at the final state. Both quantities can now be derived simultaneously by a least χ^2 method without *a priori* assuming a specific functional form for either of them⁴². Unfortunately, the structural form of Eq. (2) is such that an infinite number of solutions to the problem yield exactly the same, minimal χ^2 . All of these infinitely many solutions can be obtained⁴² by transforming one randomly picked solution by:

$$\begin{aligned} \tilde{\rho}(E - E_\gamma) &= A\rho(E - E_\gamma) \exp(\alpha[E - E_\gamma]), \\ \tilde{T}(E_\gamma) &= BT(E_\gamma) \exp(\alpha E_\gamma). \end{aligned} \quad (3)$$

The parameters A , B and α have therefore to be determined by additional physics input outside our experimental method. Only with this additional

information can unambiguous values for ρ and F be obtained. The parameters A and α are usually determined with the help of two anchor points of the level density which are derived from counting of discrete levels at low excitation energies and from neutron resonance spacing data at B_n ⁴⁸. The parameter B can then be determined using the average total radiative width $\langle\Gamma\rangle$ of neutron resonances⁵⁰.

3. Experimental results

The OCL group emphasized measurement and interpretation of the level densities of rare earth nuclei. A common finding for all nuclei has been step-structures in the level density curves at energies where the breaking of Cooper pairs is expected⁴³. A schematic microscopic calculation supports this interpretation as due to breaking of one or several pairs⁴⁶. One of the most recent findings was the observation of step structures in the level densities of ^{56,57}Fe isotopes⁵⁸ (see Fig. 1). These results extend our investigations into regions where microscopic calculations with realistic interactions become possible.

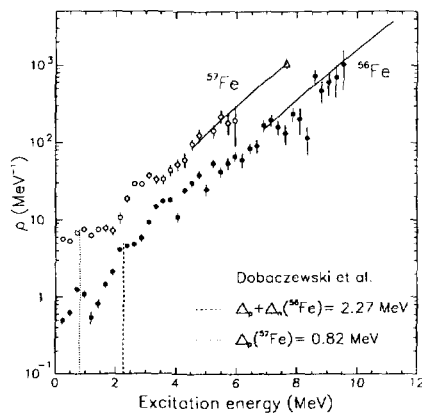


Figure 1. Step structures at 2 and 3 MeV in the level density of ⁵⁷Fe and ⁵⁶Fe, respectively, are just above the pairing gap calculated according to Ref.⁵⁹ (dotted and dashed lines respectively). This difference is to be expected since breaking a pair requires also to promote the unpaired nucleons to available single-particle levels somehow removed from the Fermi surface. The bumps and steps at 1 and 2 MeV in the level density of ⁵⁶Fe denote the first and second excited state. Solid lines are Fermi-gas models forced through the neutron resonance spacing data (triangle).

Thermodynamical quantities derived from level densities have mostly

been discussed within the statistical canonical ensemble. It has been found that the heat capacity shows a characteristic S-shape in the region of the first pair breaking⁴⁷, interpreted as the signature of a second-order phase transition. A simple, phenomenological model has been developed by the OCL group in order to account for this observation^{48,51}. A different analysis of this model in terms of the distribution of zeros in the complex temperature plane supports the finding of a second-order phase transition for rare earth nuclei⁵³.

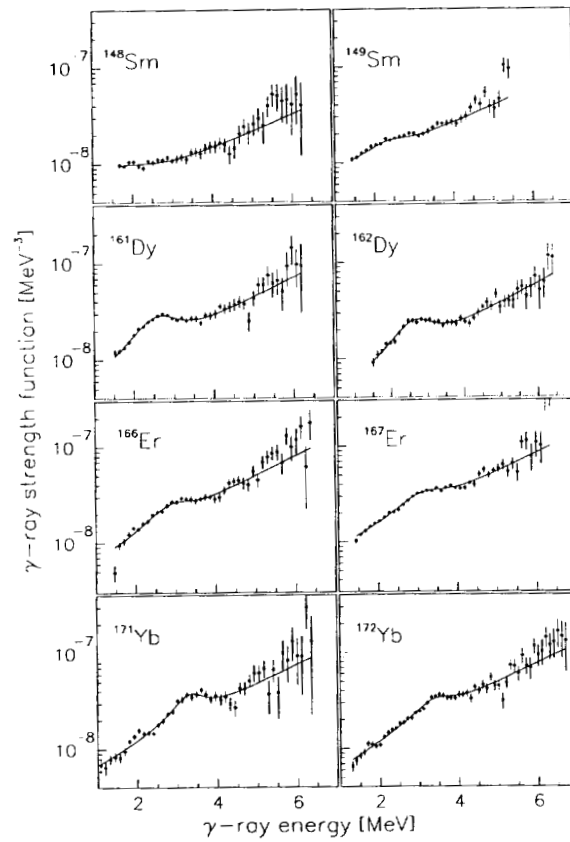


Figure 2. Radiative strength functions in different rare earth isotopes from experiments (data points) and model calculation (lines). Details on the models are given in the text. The Figure is taken from⁵².

Investigation of level densities has now entered a new phase with a Gam-

masphere experiment on ^{157}Gd which yielded a unique dataset of ($^3\text{He}, \alpha\gamma\gamma$) coincidences with at least one γ ray detected in a high-resolution Ge(HP) detector. The experiment has benefited from the development of a new, segmented charged particle detector with ten times higher solid angle coverage than the previous detectors⁶⁰. The goal of this experiment is to look for statistical γ spectra feeding discrete states with particular spin, parity and K quantum numbers and eventually to extract spin and K -dependent level densities. Analysis is in progress.

In the field of radiative strength functions it has been shown that contrary to the general belief, the tail of the GEDR in deformed rare earth nuclei can be described by the Kadmskiĭ-Markushev-Furman (KMF) model. However, the temperature parameter in the KMF model was assumed to be a constant fit parameter independent of final state energy and therefore it is not representative for the actual nuclear temperature. In the description of our data, we also took into account a Lorentzian GMDR model. Further, conclusive evidence has been given for the existence of a Lorentzian pygmy resonance with a centroid of around ~ 3 MeV and a width of ~ 1 MeV^{50,49,52} (see Fig. 2).

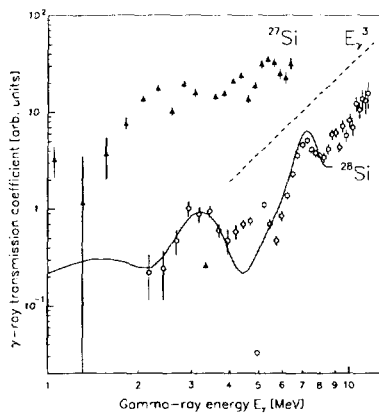


Figure 3. Experimental γ -ray transmission coefficient $T(E_\gamma)$ (data points) compared to converted lifetimes from literature (solid line)⁶¹. The dashed line shows the expected E_γ dependence in the single-particle model.

We have shown that experimental data on radiative strength functions

are in excellent agreement with previous literature data where those two datasets overlap (see, e.g., Fig. 3 of Ref.⁵⁰ or Fig. 12 of Ref.⁵²). Of special interest is here the case of ^{28}Si , where the radiative strength function can be obtained from literature data on lifetimes which can be converted to partial radiative widths⁶¹ (see Fig. 3). Further, Monte Carlo simulations have been carried out to calculate the total γ cascade spectra after average resonance neutron capture using experimental level densities and radiative strength functions. Also these results agree very well with experimental data (see, e.g., Fig. 5 of Ref.⁵⁰ or Fig. 5 of Ref.⁵²).

It is tempting to interpret the pygmy resonance in the present data as the observation of the SM in the quasicontinuum⁶². This argument is mainly based on the general agreement of resonance energy and width and the fact that no other resonances are expected in this γ -ray energy region. On the other hand, the mass-dependence of the resonance energy in the present data (see Fig. 2) and in other literature data on the pygmy resonance⁶³, i.e., a steady increase with mass^a, is different from the observation for the SM (constant or slightly decreasing with A)²⁸. Also, the resonance strength in the present data is about twice the strength observed in photon scattering experiments^{28,29}. Unfortunately, it is not possible with the present method to measure the multipolarity of the pygmy resonance directly. However, it has been suggested⁶⁴ that the combination of present data and the investigation of $(n, 2\gamma)$ spectra might yield the electromagnetic character of the pygmy resonance unambiguously. To this end, a $^{171}\text{Yb}(n, 2\gamma)$ experiment at the Los Alamos Neutron Science Center (LAN-SCC) has been carried out. Already, Bečvář could demonstrate that $(n, 2\gamma)$ experiments are sensitive to the presence of the pygmy resonance²⁴, and he has claimed the observation of the SM on excited states⁶⁵. Our investigation, however, will have the advantage that the level density and radiative strength function are already known experimentally and do not have to be taken from models.

4. Conclusions and Outlook

The OCL group has developed a new method to obtain level densities and radiative strength functions. This method has been shown to work in a wide range of the nuclear chart from Si and Fe to Mo and rare earth nuclei.

^aAlso the transition in $(n, 2\gamma)$ experiments from double-humped spectra in Gd isotopes to single-humped spectra in Dy and Yb isotopes might be tentatively explained by the presence of a pygmy resonance with a resonance energy which is increasing with mass number.

From level density curves, thermodynamical properties and the evidence of a second-order pairing phase transition could be extracted. The gap in the present data for Gd isotopes is currently being filled by a Gammasphere experiment on ^{157}Gd .

The radiative strength function is shown to agree with available data from literature and can be understood in terms of temperature-dependent models. The pygmy resonance is the subject of ongoing investigations. Hopefully, the combination of $(n, 2\gamma)$ experiments with the present data will shed light on the electromagnetic character of the pygmy resonance and whether the pygmy resonance in the present data is equivalent to the scissors mode seen in photon scattering.

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