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# Quarter-wave layers with $\mathbf{5 0} \%$ reflectance for obliquely incident unpolarized light 

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#### Abstract

The conditions under which light interference in a transparent quarter-wave layer of refractive index $n_{1}$ on a transparent substrate of refractive index $n_{2}$ leads to $50 \%$ reflectance for incident unpolarized light at an angle $\varphi$ are determined. Two distinct solution branches are obtained that correspond to light reflection above and below the polarizing angle, $\varphi_{p}$, of zero reflection for $p$ polarization. The real $p$ and $s$ amplitude reflection coefficients have the same (negative) sign for the solution branch $\varphi>\varphi_{p}$ and have opposite signs for the solution branch $\varphi<\varphi_{p}$. Operation at $\varphi<\varphi_{p}$ is the basis of a $50 \%-50 \%$ beam splitter that divides an incident totally polarized light beam (with $p$ and $s$ components of equal intensity) into reflected and refracted beams of orthogonal polarizations [Opt. Lett. 31, 1525 (2006)] and requires a film refractive index $n_{1} \geqslant(\sqrt{2}+1) \sqrt{n_{2}}$. A monochromatic design that uses a high-index $\mathrm{TiO}_{2}$ thin film on a low-index $\mathrm{MgF}_{2}$ substrate at 488 nm wavelength is presented as an example. © 2007 Optical Society of America

OCIS codes: $230.1360,260.5430,260.3160,160.4330$.


## 1. INTRODUCTION

In a recent letter ${ }^{1}$ it was shown that it is possible to split a monochromatic light beam into two beams of equal power and orthogonal polarizations by reflection and refraction at the planar surface of a dielectric substrate at an angle of incidence below the Brewster angle. This requires a substrate of high refractive index, $n_{2} \geqslant 3+2 \sqrt{2}$ $=5.8284$, e.g., PbTe in the IR. It was noted that a quarterwave layer of high refractive index, which is deposited on a substrate of low refractive index, can also be used to accomplish the same novel beam splitting function. This thin-film coating design is now presented in this paper. For a succinct account of different types of beam splitters, see, e.g., the review by Dobrowolski. ${ }^{2}$

In Section 2 an analytical design procedure is presented for achieving $50 \%$ reflectance of unpolarized (or randomly polarized) light that is obliquely incident on a transparent quarter-wave coating on a transparent substrate. The algorithm developed in Section 2 is applied in Subsection 3.A to the special case of a vanishing substrate ( $n_{2}=1$ ), i.e., an unsupported quarter-wave pellicle. It is also applied to quarter-wave coatings of varying refractive index $n_{1}$ on a (glass or plastic) substrate of refractive index $n_{2}=1.5$ in Subsection 3.B.

In Section 4 a beam splitter design that uses a $\mathrm{TiO}_{2}$ high-index quarter-wave coating on a low-index $\mathrm{MgF}_{2}$ substrate for 488 nm (Ar-ion-laser) light is considered as a specific example. An error analysis shows the effect of $\pm 5^{\circ}$ shifts in the angle of incidence and of $\pm 5 \%$ shifts in wavelength or film thickness on the performance of this beam splitter. Section 5 gives a brief summary of the paper.

## 2. QUARTER-WAVE LAYERS THAT REFLECT 50\% OF UNPOLARIZED LIGHT AT OBLIQUE INCIDENCE: ANALYTICAL TREATMENT

For light reflection in air $\left(n_{0}=1\right)$ by a transparent layer of quarter-wave optical thickness (equal to half the filmthickness period) and refractive index $n_{1}$ on a transparent substrate of refractive index $n_{2}$, the amplitude reflection coefficients of the $p$ and $s$ polarizations at oblique incidence at an angle $\varphi$ are real and are given by ${ }^{3,4}$

$$
\begin{align*}
& R_{s}=\frac{S_{0} S_{2}-S_{1}^{2}}{S_{0} S_{2}+S_{1}^{2}}  \tag{1}\\
& R_{p}=\frac{n_{1}^{4} S_{0} S_{2}-n_{2}^{2} S_{1}^{2}}{n_{1}^{4} S_{0} S_{2}+n_{2}^{2} S_{1}^{2}} \tag{2}
\end{align*}
$$

where

$$
\begin{align*}
S_{i} & =\left(n_{i}^{2}-u\right)^{1 / 2}, \quad i=0,1,2  \tag{3}\\
u & =\sin ^{2} \varphi \tag{4}
\end{align*}
$$

All materials are assumed to be optically isotropic and are separated by parallel plane boundaries.

In terms of the quantity

$$
\begin{equation*}
P=S_{0} S_{2} / S_{1}^{2} \tag{5}
\end{equation*}
$$

Eqs. (1) and (2) are rewritten as

$$
\begin{equation*}
R_{s}=\frac{P-1}{P+1}, \quad R_{p}=\frac{n_{1}^{4} P-n_{2}^{2}}{n_{1}{ }^{4} P+n_{2}{ }^{2}} . \tag{6}
\end{equation*}
$$

To achieve $50 \%$ intensity reflectance for incident unpolarized light, the amplitude reflection coefficients of the $p$ and $s$ polarizations must satisfy the following condition:

$$
\begin{equation*}
R_{p}{ }^{2}+R_{s}{ }^{2}=1 \tag{7}
\end{equation*}
$$

If Eqs. (6) are substituted into Eq. (7), a quartic equation in $P$ is obtained,

$$
\begin{equation*}
a_{4} P^{4}+a_{3} P^{3}+a_{2} P^{2}+a_{1} P+a_{0}=0 \tag{8}
\end{equation*}
$$

with coefficients given by

$$
\begin{align*}
& a_{4}=n_{1}^{8} \\
& a_{3}=-2 n_{1}^{4}\left(n_{1}^{4}+n_{2}^{2}\right), \\
& a_{2}=n_{1}^{4}\left(n_{1}^{4}-12 n_{2}^{2}\right)+n_{2}^{4}, \\
& a_{1}=-2 n_{2}^{2}\left(n_{1}^{4}+n_{2}^{2}\right), \\
& a_{0}=n_{2}^{4} \tag{9}
\end{align*}
$$

For a high-index transparent film on a low-index transparent substrate it is apparent from Eqs. (3)-(5) that $P$ is real and positive and in the range $0<P<1$, hence, only roots of Eq. (8) that satisfy this condition are accepted.

From Eqs. (3)-(5) we also obtain

$$
\begin{equation*}
P^{2}=(1-u)\left(n_{2}^{2}-u\right) /\left(n_{1}^{2}-u\right)^{2} . \tag{10}
\end{equation*}
$$

Equation (10) can be rewritten as a quadratic equation in u:

$$
\begin{equation*}
b_{2} u^{2}+b_{1} u+b_{0}=0 \tag{11}
\end{equation*}
$$

with coefficients given by

$$
\begin{align*}
& b_{2}=P^{2}-1, \\
& b_{1}=\left(n_{2}^{2}+1\right)-2 n_{1}^{2} P^{2}, \\
& b_{0}=n_{1}^{4} P^{2}-n_{2}{ }^{2} . \tag{12}
\end{align*}
$$

The only acceptable roots of Eq. (11) are those for which $0 \leqslant u<1$. Finally, the angle of incidence $\varphi$ at which the $50 \%$ reflectance for incident unpolarized light is achieved, for given $n_{1}$ and $n_{2}$, is given by

$$
\begin{equation*}
\varphi=\arcsin \left(u^{1 / 2}\right) . \tag{13}
\end{equation*}
$$

## 3. QUARTER-WAVE LAYERS THAT REFLECT 50\% OF UNPOLARIZED LIGHT AT OBLIQUE INCIDENCE: NUMERICAL RESULTS

A. Case of a Vanishing Substrate, $\boldsymbol{n}_{2}=1$

The algorithm of Section 2 is applied to determine the constraint between $n_{1}$ and $\varphi$ such that Eq. (7) is satisfied when $n_{2}=1$ (i.e., for an unsupported quarter-wave layer
or pellicle), by assigning values to $n_{1}$ between 1 and 6 in steps of 0.01 and solving for the corresponding values of $\varphi$.

Figure 1 shows the two solution branches that we obtain: a high-angle branch (HAB), or solution 1, which is represented by the continuous line, and a low-angle branch (LAB), or solution 2, which is represented by the dashed line. The dash-dot curve in the middle represents the polarizing (Brewster) angle, $\varphi_{p}=\varphi_{B}=\tan ^{-1} n_{1}$.

Figures 2 and 3 show the real amplitude reflection coefficients $R_{p}$ and $R_{s}$ that are associated with the HAB and LAB, respectively, as functions of the film refractive index $n_{1} . R_{p}$ and $R_{s}$ are both negative for the HAB, Fig. 2, and have opposite signs ( $R_{p}>0, R_{s}<0$ ) for the LAB, Fig. 3.

Figure 4 is a plot of $R_{p}$ versus $R_{s}$ and shows two separate arcs of the unit circle, Eq. (7), in the third and fourth quadrants, respectively. Points A and B correspond to the similarly marked points in Fig. 1.


Fig. 1. Angle of incidence $\varphi$ versus film refractive index $n_{1}$ such that $50 \%$ of incident unpolarized light is reflected by a quarterwave pellicle. The continuous and dashed curves represent two independent solution branches. The middle curve gives the Brewster angle as a function of $n_{1}, \varphi_{B}=\tan ^{-1} n_{1}$.


Fig. 2. Amplitude reflection coefficients $R_{p}$ and $R_{s}$ that are associated with the HAB of Fig. 1 plotted as functions of the film refractive index $n_{1}$.


Fig. 3. Amplitude reflection coefficients $R_{p}$ and $R_{s}$ that are associated with the LAB of Fig. 1 plotted as functions of the film refractive index $n_{1}$.


Fig. 4. Plot of $R_{p}$ versus $R_{s}$ associated with the high- and lowangle branches (Figs. 2 and 3) yields two arcs of the unit circle in the third and fourth quadrants, respectively. The arrows indicate the direction of increasing $n_{1}$, and points A and B correspond to the similarly marked points in Fig. 1.

Figures 5 and 6 show the intensity reflectances $R_{p}{ }^{2}$ and $R_{s}{ }^{2}$ for the HAB and LAB, respectively, as functions of $n_{1}$. The average value of $R_{p}{ }^{2}$ and $R_{s}{ }^{2}$ is constant ( $=0.5$ ), independent of $n_{1}$ as is required by Eq. (7).

An interesting feature of Fig. 1 is that $\varphi$ of the HAB reaches a minimum, $\varphi_{\min }=71.8225^{\circ}$, at point A where $n_{1}$ $=1.78$. Therefore, a pellicle of 1.78 refractive index and quarter-wave optical thickness (or an odd integral multiple thereof) functions as a $50 \%-50 \% \mathrm{BS}$ for incident unpolarized light at $\approx 72^{\circ}$ angle of incidence. The starting point B of the LAB in Fig. 1 is at $\varphi=0$ and corresponds to $n_{1}=\sqrt{2}+1=2.414$. Film materials that have this refractive index include diamond in the visible and ZnSe in the IR. ${ }^{5,6}$

## B. General Case of $\boldsymbol{n}_{\mathbf{2}}>\mathbf{1}$

For an arbitrary substrate of refractive index $n_{2}$, the starting value of $n_{1}$ for the LAB is obtained by noting that at $\varphi=0, R_{p}{ }^{2}=R_{s}{ }^{2}=1 / 2$. It follows from Eqs. (6) that

$$
\begin{align*}
R_{s} & =(P-1) /(P+1)=-1 / \sqrt{2},  \tag{14}\\
P & =(\sqrt{2}-1)^{2} . \tag{15}
\end{align*}
$$

If $u=0$ is substituted in Eq. (10), we get

$$
\begin{equation*}
n_{1}=\left(n_{2} / P\right)^{1 / 2} \tag{16}
\end{equation*}
$$

When Eqs. (15) and (16) are combined, we obtain

$$
\begin{equation*}
n_{1}=(\sqrt{2}+1) \sqrt{n_{2}} \tag{17}
\end{equation*}
$$

As a specific example we take quarter-wave layers on a (glass or plastic) substrate with $n_{2}=1.5$. Figure 7 shows the two solution branches that we obtain using the algorithm of Sec. 2. When compared with Fig. 1 (for $n_{2}=1$ ), the HAB in Fig. 7 is displaced upward to higher angles,


Fig. 5. Intensity reflectances $R_{p}{ }^{2}$ and $R_{s}{ }^{2}$ that are associated with the HAB of Fig. 1 plotted as functions of the film refractive index $n_{1}$. The average reflectance, $\left(R_{p}{ }^{2}+R_{s}{ }^{2}\right) / 2$, is constant at 0.5 .


Fig. 6. Intensity reflectances $R_{p}{ }^{2}$ and $R_{s}{ }^{2}$ that are associated with the LAB of Fig. 1 plotted as functions of the film refractive index $n_{1}$. The average reflectance, $\left(R_{p}{ }^{2}+R_{s}{ }^{2}\right) / 2$, is constant at 0.5 .


Fig. 7. Angle of incidence $\varphi$ versus the refractive index $n_{1}$ of a transparent quarter-wave coating on a transparent substrate ( $n_{2}=1.5$ ) that reflects $50 \%$ of incident unpolarized light. The continuous and dashed curves represent two distinct solution branches. The middle dash-dot curve gives the polarizing angle $\varphi_{p}$ as a function of $n_{1}$ as obtained from Eqs. (19) and (20).


Fig. 8. Amplitude reflection coefficients $R_{p}$ and $R_{s}$ that are associated with the HAB of Fig. 7 plotted as functions of the film refractive index $n_{1}$. The significance of the point of intersection C is discussed in the text.
and its minimum at point A now occurs at $\varphi_{\text {min }}$ $=81.6208^{\circ}, n_{1}=1.98$. The starting value $n_{1}=2.9568$ of the LAB at point B is predicted by Eq. (17).

In Fig. 7 the middle (dash-dot) curve gives the polarizing angle $\varphi_{p}$ of the film-substrate system at which $R_{p}=0$ as a function of the film refractive index $n_{1}$ with $n_{2}=1.5$. To calculate the polarizing angle $\varphi_{p}$ we note from Eqs. (6) that $R_{p}=0$ if

$$
\begin{equation*}
P=n_{2}^{2} / n_{1}^{4} . \tag{18}
\end{equation*}
$$

Substitution of $P$ from Eq. (18) into Eq. (10) gives a quadratic equation,

$$
\begin{equation*}
c_{2} u^{2}+c_{1} u+c_{0}=0 \tag{19}
\end{equation*}
$$

in $u=\sin ^{2} \varphi_{p}$ with coefficients given by

$$
c_{2}=n_{1}^{8}-n_{2}^{8},
$$



Fig. 9. Amplitude reflection coefficients $R_{p}$ and $R_{s}$ that are associated with the LAB of Fig. 7 plotted as functions of the film refractive index $n_{1}$.


Fig. 10. Intensity reflectances $R_{p}{ }^{2}$ and $R_{s}{ }^{2}$ that are associated with the HAB of Fig. 7 plotted as functions of the film refractive index $n_{1}$. The average reflectance, $\left(R_{p}{ }^{2}+R_{s}{ }^{2}\right) / 2$, is constant at 0.5 .


Fig. 11. Intensity reflectances $R_{p}{ }^{2}$ and $R_{s}{ }^{2}$ that are associated with the LAB of Fig. 7 plotted as functions of the film refractive index $n_{1}$. The average reflectance, $\left(R_{p}{ }^{2}+R_{s}{ }^{2}\right) / 2$, is constant at 0.5 .


Fig. 12. Average reflectance $\left(R_{p}{ }^{2}+R_{s}{ }^{2}\right) / 2$ and ellipsometric parameters $\psi_{r}, \psi_{t}, \Delta_{r}, \Delta_{t}$ as functions of the angle of incidence $\varphi$ for a beam splitter that consists of a quarter-wave ( 43.51 nm ) thin film of $\mathrm{TiO}_{2}$ on a $\mathrm{MgF}_{2}$ substrate at 488 nm wavelength. The angle of incidence is varied by $\pm 5^{\circ}$ around the design angle $\varphi$ $=46.04^{\circ}$.

$$
\begin{align*}
& c_{1}=2 n_{1}^{2} n_{2}^{4}-n_{1}^{8}\left(n_{2}^{2}+1\right), \\
& c_{0}=n_{1}^{4} n_{2}^{2}\left(n_{1}^{4}-n_{2}^{2}\right) \tag{20}
\end{align*}
$$

Figures 8 and 9 show the amplitude refection coefficients $R_{p}$ and $R_{s}$ as functions of $n_{1}$ for the HAB and LAB of Fig. 7, respectively. Again, $R_{p}$ and $R_{s}$ are both negative for the HAB, Fig. 8, and have opposite signs $\left(R_{p}>0, R_{s}\right.$ $<0)$ for the LAB, Fig. 9.

The point of intersection C of the curves of $R_{p}$ and $R_{s}$ in Fig. 8 is located at

$$
R_{p}=R_{s}=-1 / \sqrt{2}=-0.7071, \quad n_{1}=\sqrt{n_{2}}=1.2247
$$

This corresponds to a polarization-preserving (or polarization-independent) $50 \%-50 \%$ beam splitter in both reflection and transmission. ${ }^{3}$

The associated intensity reflections $R_{p}{ }^{2}$ and $R_{s}{ }^{2}$ as functions of $n_{1}$ are shown in Figs. 10 and 11 for the HAB and LAB, respectively. Again, the average of $R_{p}{ }^{2}$ and $R_{s}{ }^{2}$ is constant ( $=0.5$ ) independent of $n_{1}$ as required by Eq. (7).

## 4. BEAM SPLITTER FOR PRODUCING REFLECTED AND TRANSMITTED BEAMS OF EQUAL POWER AND ORTHOGONAL POLARIZATIONS IN THE VISIBLE

Consider a high-index ( $n_{1}=2.895$ ) thin film of $\mathrm{TiO}_{2}$ on a low-index ( $n_{2}=1.386$ ) $\mathrm{MgF}_{2}$ substrate at wavelength $\lambda$
$=488 \mathrm{~nm}$. (Because we assume isotropic phases, the refractive indices are taken as averages of the ordinary and extraordinary indices $n_{0}$ and $n_{\mathrm{e}}$ published in Ref. 6.) By use of the algorithm of Section 2, the operating angle of incidence $\varphi=46.037^{\circ}$ is obtained. The film-thickness pe$\operatorname{riod} D_{1}$ and quarter-wave metric film thickness $d_{1}$ are determined by

$$
\begin{align*}
D_{1} & =(\lambda / 2)\left(n_{1}^{2}-\sin ^{2} \varphi\right)^{-1 / 2} \\
d_{1} & =D_{1} / 2 \tag{22}
\end{align*}
$$

which give $D_{1}=87.02 \mathrm{~nm}$ and $d_{1}=43.51 \mathrm{~nm}$. Under the ideal operating conditions, the average reflectance for incident unpolarized light is $1 / 2$ and the reflection and transmission ellipsometric parameters ${ }^{4}$ satisfy the following relations: ${ }^{1,7}$

$$
\begin{gather*}
\Delta_{r}=\pi, \Delta_{t}=0 \\
\psi_{r}+\psi_{t}=\pi / 2 \tag{23}
\end{gather*}
$$

To couple the refracted light out of the substrate into air, a prismatic substrate with prism angle equal to the angle of refraction ( $31.287^{\circ}$ ) can be used, so that light leaves the prism normal to its exit face which is antireflection coated. ${ }^{8}$

When the wavelength of light and metric film thickness are kept constant, and the angle of incidence is varied by up to $\pm 5^{\circ}$, the average reflectance and ellipsometric pa-


Fig. 13. Average reflectance $\left(R_{p}{ }^{2}+R_{s}{ }^{2}\right) / 2$ and ellipsometric parameters $\psi_{r}, \psi_{t}, \Delta_{r}, \Delta_{t}$ of a beam splitter as functions of the thickness $d_{1}$ of a $\mathrm{TiO}_{2}$ film on a $\mathrm{MgF}_{2}$ substrate at $\lambda=488 \mathrm{~nm}$ and $\varphi$ $=46.04^{\circ}$. The film thickness is varied by $\pm 5 \%$ around the design value of 43.5 nm .


Fig. 14. Average reflectance $\left(R_{p}{ }^{2}+R_{s}{ }^{2}\right) / 2$ and ellipsometric parameters $\psi_{r}, \psi_{t}, \Delta_{r}, \Delta_{t}$ as functions of the wavelength $\lambda$ (in nanometers) for a beam splitter that consists of a $43.51 \mathrm{~nm} \mathrm{TiO}_{2}$ thin film on a $\mathrm{MgF}_{2}$ substrate at an angle of incidence of $\varphi=46.04^{\circ}$. The wavelength $\lambda$ is changed by $\pm 5 \%$ around 488 nm .
rameters change in the manner shown in Fig. 12. From Fig. 12, it is apparent that the ideal conditions of Eqs. (23) are nearly maintained; hence, this novel beam splitter is tolerant to small angle-of-incidence errors.

If the wavelength of light and angle of incidence are fixed, but the film thickness is varied by $\pm 5 \%$ around its design value ( $d_{1}=43.51 \mathrm{~nm}$ ), the average reflectance and ellipsometric parameters change in the manner shown in Fig. 13. Again, the ideal conditions of Eqs. (23) are approximately satisfied, to within a small error, and the coating design is not overly sensitive to small filmthickness errors around the quarter-wave thickness.

Finally, when the angle of incidence and metric thickness of the coating are kept constant, and the wavelength
is shifted by $\pm 5 \%$ around $\lambda=488 \mathrm{~nm}$, the average reflectance and ellipsometric parameters change in the manner shown in Fig. 14. In Fig. 14, the deviations from the ideal conditions of Eqs. (23) are more pronounced; hence, the beam splitter is not considered achromatic.

## 5. SUMMARY

A transparent layer of quarter-wave optical thickness, a pellicle or a coating deposited on a transparent substrate, reflects $50 \%$ of incident unpolarized light under certain conditions that are completely determined. Two distinct solution branches are obtained that correspond to incidence below and above the $p$-suppressing polarizing angle of the film-substrate system. Operation below the polarizing angle makes possible a novel thin-film beam splitter ${ }^{1}$ that divides incident totally polarized light into reflected and refracted beams of equal power ( $50 \%$ each) and orthogonal polarizations. The performance of one such device that uses a high-index $\mathrm{TiO}_{2}$ quarter-wave coating on a low-index $\mathrm{MgF}_{2}$ substrate at 488 nm wavelength is presented.
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