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Photoelectron Diffraction and Holography: Some New Directions

C.S. Fadley

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PHOTOELECTRON DIFFRACTION AND HOLOGRAPHY: SOME NEW DIRECTIONS

Charles S. Fadley

Materials Sciences Division Lawrence Berkeley Laboratory University of California Berkeley, California 94720 and University of California at Davis **Department of Physics** Davis, California 95616

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PHOTOELECTRON DIFFRACTION AND HOLOGRAPHY: SOME NEW DIRECTIONS⁺

CHARLES S. FADLEY

Department of Physics, University of California-Davis, Davis, CA 95616 Materials Sciences Division, Lawrence Berkeley Laboratory, Berkeley, CA 94720

ABSTRACT

Photoelectron diffraction has by now become a versatile and powerful technique for studying surface structures, with special capabilities for resolving chemical and magnetic states of atoms and deriving direct structural information from both forward scattering along bond directions and back-scattering path length differences. Further fitting experiment to theory can lead to structural accuracies in the \pm 0.03 Å range. Holographic inversions of such diffraction data also show considerable promise for deriving local three-dimensional structures around a given emitter with accuracies of $\pm 0.2 - 0.3$ Å. Resolving the photoelectron spin in some way and using circularly polarized radiation for excitation provide added dimensions for the study of magnetic systems and chiral experimental geometries. Synchrotron radiation with the highest brightness and exergy resolution, as well as variable polarization, is crucial to the full exploitation of these techniques.

INTRODUCTION

Photoelectrons emitted from core levels represent localized sources of outgoing waves which can then scatter from nearby atoms to produce diffraction patterns. We will here consider several new directions for using such diffraction patterns to determine surface atomic positions, as well as surface magnetic structures [1-5]. The analysis of such data in a more recently suggested holographic manner so as to directly image atoms in three dimensions [6,7] will also be considered. The special benefits that synchrotron radiation brings to such studies will also be pointed out.

PHOTOELECTRON DIFFRACTION-BASIC CONCEPTS

Photoelectron diffraction patterns are by now well known and much studied, and have lead to the increasing use of this technique for surface structure studies [1-5]. The fundamental measurement is illustrated in Fig. 1. A photoelectron is emitted from a core level, and its intensity is measured as a function of its direction or its energy above a single-crystal sample, yielding what can be termed scanned-angle or scanned-energy data, respectively. In terms of the electron wave vector k , this is equivalent to measuring intensity as a function of its direction $k = k / |k|$ or its magnitude $k = |k|$. Intensity variations are produced by the interference of the unscattered or direct wave component ϕ_{α} and the various scattered-wave components ϕ ¹

over initial and final magnetic quantum numbers and interference between the two final-state channels l_{final} = 1+1 and 1-1 that are allowed by the dipole selection rules $[84, 83, 9].$

Expanding the square in Eq. 3a now yields

$$
I(\underline{k}) \propto |F_0|^2 + \Sigma_j [F_0^* F_j \exp\{-i\underline{k} \cdot \underline{r}_j\} + F_0 F_j^* \exp\{i\underline{k} \cdot \underline{r}_j\}]
$$

+
$$
\Sigma_j \Sigma_k [F_j^* F_k \exp\{i\underline{k} \cdot (\underline{r}_j - \underline{r}_k)\} + F_j F_k^* \exp\{-i\underline{k} \cdot (\underline{r}_j - \underline{r}_k)\}\}.
$$
 (4)

 $|\mathbf{F}_{\text{O}}|^2$ is thus simply proportional to $I_{\text{O}}(\underline{k})$: the intensity in the absence of any scattering. A normalized intensity function $\chi(\underline{k})$ can now be calculated, very much as in the analysis of extended x-ray absorption fine structure (EXAFS), with one choice being [7a]:

$$
\chi(\underline{k}) = [I(\underline{k}) - I_0(\underline{k})]/I_0(\underline{k})^{1/2}, \qquad (5)
$$

and this yields

$$
\chi(\underline{k}) \propto (\left| \mathbf{F}_0 \right|)^{-1} \Sigma_j \left[\mathbf{F}_0(\underline{k})^* \mathbf{F}_j(\underline{k}) \exp\{-i\underline{k} \cdot \underline{r}_j\} + \mathbf{F}_0(\underline{k}) \mathbf{F}_j(\underline{k})^* \exp\{i\underline{k} \cdot \underline{r}_j\} \right]
$$

$$
+(\left| \mathbf{F}_0 \right|)^{-1} \Sigma_j \Sigma_k \left[\mathbf{F}_j(\underline{k})^* \mathbf{F}_k(\underline{k}) \exp\{i\underline{k} \cdot (\underline{r}_j - \underline{r}_k)\} + \mathbf{F}_j(\underline{k}) \mathbf{F}_k(\underline{k})^* \exp\{-i\underline{k} \cdot (\underline{r}_j - \underline{r}_k)\} \right],
$$
(6)

where the r_j or r_k dependence of F_j or F_k , respectively, in sphericalwave scattering have not been indicated explicitly. This form is useful in considering holographic analyses of diffraction.

Another common approximation is to assume that the scattered waves ϕ_j and ϕ_k are small in amplitude with respect to ϕ_o , so that the cross terms ϕ_o ϕ_j and $\phi_o \phi_j$ in Eq. 1 dominate the structural information. This directly leads via Eqs. 3 and 6 to

$$
\chi(\underline{k}) \propto 2\Sigma_j (\hat{\epsilon} \cdot \hat{r}_j/r_j) |f_j(\theta_j)| W_j \exp(-L_j/2\Lambda_e)
$$

$$
\cdot \cos[kr_j(1-\cos\theta_j)+\Psi_j(\theta_j,r_j)] . \qquad (7)
$$

This form directly shows that Fourier transforms of scanned-energy data along some direction k and over some interval Δk

$$
F_{\Delta k}(\hat{\mathbf{k}}, \mathbf{r}) \propto \int_{\Delta k} \chi(\underline{\mathbf{k}}) \exp\{-i\mathbf{k}\mathbf{r}\} \mathrm{d}\mathbf{k} \quad , \tag{8}
$$

should be useful for deriving path length differences $r = r_j(1-\cos\theta_j)$, a result that has been discussed and used in a number of previous studies $[4, 10]$.

There are several important characteristics of such photoelectron diffraction patterns, as summarized below. More detailed discussions with illustrative examples appear elsewhere [1-5].

-Measurement of intensities: In general, core peak intensities must be

two interfering channels of 1 ± 1 . Thus, theoretical modeling can be the most accurate for photoelectron diffraction and holography. Varying *b***oth the polarisation and energy of the ex***c***iting photon also c**an *b***e used** t**o e**m**phasize different scatterers or aspects of** t**he e**m**ission or s***c***attering** proc**ess.**

-Simple forward scattering: In measurements at photoelectron kinetic energies of about 500 eV or higher, the scattering amplitude $|f_i(\theta_i, r_i)|$ energies **o** $\mathbf{a} \cdot \mathbf{b}$ explicitly the same $\mathbf{a} \cdot \mathbf{b}$ and $\mathbf{a} \cdot \mathbf{b}$ and $\mathbf{a} \cdot \mathbf{b}$ **i**s **hi**g**h**l**y peaked in the forw**a**rd direction (**i**.**e**. near** 0j **= 0**-**).- Nany studies have by no**w s**hown that such forward sca**tt**ering or fo**rwa**rd** f**ocussin**g **peaks can he direc**tly **used to determ**i**ne** bo**nd di**r**ections** f**or** ! **adsorbed** m**o**l**e***c***u**l**e**s **[1,3] and lo**w**-index d**i**rect**i**on**s **fo**r s**in**g**le cr**y**sta**ls **and e**p**itaxial overla**y**er**s **[I, 2].** A**s** an **i**l**lustration of the sensitivit**y **of such hi**g**h-ener**gy p**atterns to different surface struc**t**ures, Fig. 2 shows** t**he full 2***x* **in**t**e**n**si**ty **dis**t**r**i**butions above three d**i**ffe**r**en**t **surfaces, in stereogra**p**hic** p**ro**j**ec**t**ion: fcc Ni(OOl) [20], hc**p **Ru(O001) [21]***,* **and the textu**r**ed su**r**face of highl**y **oriented** py**rol**y**tic** g**ra**p**hite** w**ith a preferr**ed **(0001) orien**t**ation [22]. Such** f**o**rw**ard scattering** p**eaks have also been found to be sensitive to surface** p**re-**m**elting pheno**m**ena [23]. The higher k**i**net**i**c energies requir**ed **for this kind of** m**easure**m**ent** have led **to its being performed primarily w**i**th laboratory x-ray sour**c**es** in the 1.2-1.5 keV range, but higher brightness synchrotron radiation **sources in t**h**e 5**00**-**1**5**00 **eV range would b**e **equally usefu**l **for this work.**

-Back scatt**erin**g**:** In m**ea**s**ure**m**ents at lower** p**hotoele**ct**ron kinetic energies of** l**es**s **t**h**an** a**bou**t **300 eV, there is a**ls**o a** s**ignificant degree of ba**c**k s**c**attering, an**d **this** c**an be used in** se**v**e**r**a**l wa**ys **to extra**c**t st**ruc**tura**l **informa**t**ion** c**on**c**ern**ing **ato**ms **that are "behind" the emitter as viewed b**y **t**h**e** 4**erector [1,4,5,**10**,24]. Syn**c**hrotron radiation is again** n**e**c**essary to insure sufficien**tly l**ow kinetic ene**rg**ie**s i**n s**uc**h studies.**

-Sin@le scatterin@ and multiDie scatterin G analysis: In a nu**mber of prior studies, it ha**s **been** f**o**u**nd that a s**im**ple single** s**catter**in**g** m**odel such a**s **that outlined above** is **able** to **predi**c**t** m**o**s**t of th**e **stru**c**ture in diffraction pattern**s**, and t**h**u**s **it** als**o can** be **u**se**fu**l **for deriving** s**o**m**e stru**c**tura**l **infor**m**ation.** H**owever,** m**u**l**tip**l**e** sc**attering effects can he strong in both forward s**c**attering a**l**on**g **hig**h**-**d**en**s**it**y **rows of** a**to**ms **(where events o**f o**rder** u**p to the n**u**mb**e**r of** s**catterer**s **between** em**itt**e**r and s**c**atterer ma**y **have t**o **h**e **considered [8d]) and back scattering at** l**ower energies (where events** u**p to third o**rd**er** a**r**e **fo**u**n**d t**o b**e **e**sse**nti**al **for pr**ed**icting a**ll **diffractio**n **features [Sd,e]). Th**is is **i**ll**u**s**tra**t**ed in Fi**g**. 3, w**h**ere experimental and ca**l**cu**l**ated fu**ll **diffraction pattern**s **ab**o**ve a Ni(**00**1) surface ar**e s**hown [2**0**]. The experi**m**ental pattern awa**y **from** l**ow-index** d**irect**i**on**s **i**s **rea**s**onab**ly **w**el**l predicted by** s**ingle scattering th**e**or**y**, but both the int**e**n**s**it**y **and width of the** l**ow-index fo**rw**ard** s**cattering peak**s **ar**e mu**c**h **overe**s**timated in t**h**is** s**i**m**ple** m**odel. Multiple scattering** th**eor**y **b**y **contrast predi**c**t**s **al**l **aspects of** t**h**e **diffraction patte**rn **very we**ll**, even t**h**o**u**gh on**l**y five** em**itter** l**a**ye**r**s **were in**clu**ded in t**h**is si**m**ulation**.

 $-$ **Path-length differences:** Another direct form of structural information **that** c**an be obtained b¥ virtue of the strong** s**in**g**le scattering chara**c**ter** o*c***curr**i**ng near the or**i**g**i**n,** a **total number of data p***o*i**nts of about 1000 is thus needed for such a structure esti**m**ate. K** m**ore rigorously derivable** method for summing such Fourier transforms of scanned-energy **data so a**s **to derive ato**mi**c** p**os**i**tio**n**s** i**n three di**me**nsions will be dis**_**ssed under photoelectron holograph**y **below.**

-A_esur_ce .\$_ure\$: In a growi**ng nu**m**ber of stud**i**es to date, it has been po**ssi**ble also to detemin**e m**or**e **d**e**ta**i**l**e**d surface structur**e**s b**y **f**i**tt**i**n**g e**x**pe**r**ime**ntal d£ffract**i**on** p**at**te**rn**s **of** e**ither th**e **scann**e**d-an**g**le or scanned-**e**nerg**y **t**y**pe** t**o th**e**ore**t**ical s**_**ulations for var**i**ous** p**oss**i**bl**e **trial geometr**i**es [l,2a,4,5,**a**b,24]. Direct structural** i**nformat**i**on from forwa**r**d sca**t**t**e**r**i**n**g **or back-scatter**ing p**a**th **length d**i**ff**e**renc**e**s can often be use**d **to el**_i**nate various** p**o**ssi**ble s**t**ru***c***tur**es **and arr**i**ve a**t **a very good guess for** t**he final trial-and-**e**rror search. Th**e**oretical calculations have been carri**ed **out at both the s**i**n**g**l**e **scatter**ing **[1,2a] and** m**ore accurate** m**ulti**p**le scatter**i**n**g **[1**,**4,5,**8**] levels. With careful an**alys**i**s **of such fit**s**, e.**g**., via R f**a**c**t**or**s**, accurac**i**es in the approx**i**mately** _.+O.03J_ **range have been obta**i**ned. However, further work is ne**ed**ed to** sp**eed up such st**ru**cture searches** an**d the multiple scattering calculation**s **needed for the h**i**ghest ult**i**mate accurac**y**. Finall**y**,** n**ote rapid data acquisit**i**on me**t**ho**d**s are also call**ed **for**; **these will benefit** f**ro**m **ne***x***t-generation higher-briqhtness synchrotron sources as well.**

PHOTOELECTRON HOLOGRAPHY

More recently*,* **it has been suggested b**y **S**s*6***ke [6] that su***c***h** p**hotoelect**ro**n d**i**f**f**ra**c**t**i**on** pa**ttern**s *c*an **be tr**e**at**ed **a**s **hol**og**r**am**s***,* **with the** unscattered wave ϕ_o being identified as the reference wave of the hologram, and the scattered waves ϕ_j being identified as the object **hologram, and the scattered waves** _**j being iden**ti**fied a**s **the object waves, a diffraction pattern t**ha**t i**s s**omehow measur**ed **over a relatively large numb**e**r of** p**o**in**ts** i**n k space wh**i**ch nay in**v**o**l**ve var**y**ing both direct**i**on and energy** i**s then conve**rte**d** in**to a direct three-di**me**n**si**onal** image of the atoms surrounding a given atom using a Fourier-transform**like integral. The holog**r**a**l i8 i**n thi**s **in**t**e**r**pr**e**ta**ti**on** j**u**s**t the** intensity $I(\underline{k})$, or **more** conveniently the normalized function $\chi(\underline{k})$. The **hol**og**raphic** ana**ly**s**i**s **of diffraction dat**a i8 i**n a much mor**e **dev**e**lopmental stage, but several encou**r**ag**i**ng exper**im**en**t**al** s**tud**ie**s** ha**ve been carri**ed **out to** dat**e [12**,**26-31].**

The **first holographic** im**aging procedure to be demonstrated quantit**a**tively i**8 **du**e **to Barton [7a]. It** m**ak**es **u**se **o**f s*c***anned-**an**gle data at** a **s**i**ngle en**e**rg**y**, for** w**hich the Helnholtz-**Ki**rchoff theore**m **from op**ti**cs** is **u**s**ed** t**o calcu**l**ate the atom**i**c** i**mage U(E) (actual**ly **the source** w**avefield) f**rom**:**

$$
\mathbf{U}(\mathbf{x},\mathbf{y},\mathbf{z}) \propto \left| \iint_{S} \chi(\mathbf{k}) \exp[i \mathbf{k} \cdot \mathbf{z}] d\sigma_{\mathbf{k}} \right| , \qquad (9)
$$

where the integr**a**l **on the direction of k** i8 **over** t**he** s**pherical surface** on which the hologram is measured. Note that $\chi(\underline{k})$ has here been m**ultiplied b**y **the complex con**j**ugate of** t**he d**i**rection-dependent** pa**rt of th**e **phase factor due to** p**ath len**gt**h difference** exp**[-**i**k._r**]*,* **and that the**

generali**zed sca**tt**e**red**-wave s**tr**ength F**j **dur**i**ng** t**he** i**n**t**e**g**r**ati**on, wh**i**ch y**i**e**l**ds a new** i**mag**e **funct**i**on U':**

$$
U'(x,y,z) \propto \iiint \{ \chi(\underline{k}) \exp[i k_z z] / F_j(\underline{k},\underline{r}) \} \exp[i(k_x x + k_y y)] dk_x dk_y \quad . \quad (11)
$$

T**h**is **has been t**e**nt**e**d** t**he** s**ca**tt**ered-wave-**i**nc**l**uded Four**i**e**r t**ran**s**form** (**SWIFT) method. In pract**i**ce***,* **th**i**s procedure ha**s **to date** g**enerally** i**nvo**l**ved s**i**mpl**y **d**i**v**i**d**i**ng b**y **a** p**lan**e**-wav**e **or** sphe**r**i**cal-**w**ave** s**catt**e**r**i**n**g **factor, wh**i**ch may then have to be adju**s**ted w**it**h po**siti**on** i**n** s**pace** s**o a**s **to allow fo**r **th**e **d**i**fferent type**s **of scatterers** p**r**ese**nt [27a-**c**,34]. The latter ad**j**u**s**tmen**t **thus requ**ir**es some advance kno**w**ledge of the structure, or an** i**ter**a**t**i**ve approach. F**j **a**ls**o can** i**n p**ri**nc**i**ple a**l**lo**w f**o**r t**he an**i**so**t**rop**y i**n the outgo**i**ng reference wave,** a**s** i**s** i**mpl**_**c**i**t** i**n the** _a**c**t**or •** _j i**n Eq. 3c; th**i**s mo**r**e general t**y**pe of cor**r**ect**i**on ha**s **been** applied for the first time to experimental data from $\cos i_2(111)$ by Zhou **e**t **al. [28].**

The overlap of real and twi**n** im**age**s i**s a problem shared w**i**th opt**i**cal holo**g**raph**y**, bu**t i**t** i**s poten**ti**all**y **more ser**i**ous** i**n** i**mag**e**s of surface structures, s**i**nce the surface** i**nherentl**y **breaks the** i**nve**r**s**i**on s**y**mmetry along** i**ts normal, and** t**hu**s t**he tw**i**n**s **of** s**ub**s**trate a**t**o**m**s may overlap the** r**eg**i**ons** i**n** spa**ce occup**i**ed b**y **adsorbate or overla**y**er atoms. One** s**olu**ti**on to** this **problem** i**s to note t**hat**, for some ca**s**e**s, **the reg**i**on of** t**he hologram most s**t**rongly affected b**y **some a**t**o**m **a**t **r** i**s well** l**ocal**i**zed** i**n a sol**i**d-an**g**le reg**i**on cen**t**ered on r; th**i**s was f**i**rst de**m**on**st**ra**te**d** i**n** t**heo**r**et**i**ca**l **s**im**ul**ati**on**s **b**y **Sald**i**n e**t **a**l**. [35]. Anal**y**z**i**ng only th**i**s** Po**rt**i**on of** t**he hologram then ma**y **lead to an** i**mage** i**n wh**i**ch the t**wi**n** f**rom ano**t**her atom at -r** i**s suppre**s**sed**, **a**s s**ugge**s**ted by Sa**i**k**i e**t a**l**.** fo**r** sc**ann**ed**-ang**l**e data** f**rom cases do**mi**n**ate**d b**y f**orward scat**t**er**i**n**g **[3**6]**. For back-scatter**i**n**g **cases at lower energ**i**es, Tong et al. [34b] have a**l**so pro**po**sed anal**y**z**i**ng** s**c**a**nned-**e**n**e**rg**y **data over only small w**i**ndow**s i**n d**i**rect**i**on** i**n order to e**m**pha**si**se a** 8i**ng.e scatterer** be**h**i**nd** th**e** emi**tter.**

In Fig. 5, we show the effects of simultaneously using these last **two** i**mage** i**mprovement procedures, aga**i**n for the case of c(**2**x2)S***/***N**i**(001) [27c].** n**n**ly **the** ri**gh**t ha**lf of the ho**l**ogram ha**s **been** an**a**lys**ed** t**o focus on** t**he po**si**t**i**on of** t**he neare**st **n**ei**ghbor along +x, and the SW**I**FT** p**ro**c**ed**u**re has been appl**ied i**n** d**o**i**ng** t**he** i**m***a***ge format**i**on**. **Th**e **ag**r**eemen**t **between exper**i**ment** a**nd theory** is **aga**i**n exc**el**l**e**nt**, an**d** t**he peak** Posi**t**i**ons hav**e im**p**r**oved** t**o w**it**h**i**n abo**u**t 0.3** A **of** t**he known structure. Th**i**s ex**amp**l**e **thus sugge**st**s** t**ha**t **even** si**ng**l**e**-**energ**y **holo**g*r***aph**i**c** i**m**a**ges for ad**s**orbate overla**y**ers or th**i**n e**pi_**ax**i**al** l**ayers can be ob**t**a**i_ **w**i**th** s**uf**fi**c**ie**nt accu**,**_**;**ac**y **to be used for rul**i**ng out** ma**n**y **poss**i**bl**e **s**t**ructure**s and providing excellent starting points for more accurate final trial**and-**e**rror ref**i**nements. Other** s£**ng**l**e-**e**n**e**rgy, SWIFT-corr**e**ct**e**d results f**o**r bulk CoS**£ **2 at 700 eV are also encourag**i**ng [28]. However, p**r**ev**i**ous s**t**ud**i**e**s **on mult**i**la**y**er bulk spec**i**mens of Cu [2**6**a], S**i **[27a], and N**i **[20] a**t **h**i**gher** si**ng**l**e ene**r**g**ies **suggest** t**ha**t t**h**e **presence o**f i**nequ**i**valen**t **e**mi**tte**r**s** i**n** s**e**v**era**l **layers can lead** t**o** s**trong** i**mage d**ist**ort**i**on**s **along forward** s**ca**tt**er**i**ng d**ir**ec**ti**on**s**.**

i**nteratom**ic **d**i**s**t**ances that are** t**o be** st**ud**i**e**d**. Th**e **behav**i**or of these art**i**facts** i**s** i**llustrated** i**n F**i**g. 2,** w**here** i**mages** i**n the x**y **plane of** c**(2x**2**)S***/***N**i**(001) are shown for d**i**fferent nu**m**bers of energ**i**es spanning** th**e range from 862 to 1324 eV. On**ly **the r**i**ght half of** th**e hologram** has **been** analyz**ed (as in Fi**g**. 5) to** e_p**ha**s**i**z**e** the **real ima**ge **d**u**e** t**o** th**e nearestn**e**i**g**hbor a**l**ong +x**. **In goin**g **from I to 3 to 5 to 7** to **13 ene**rg**ies, we** se**e a gradual** s**up**p**r**ess**ion of tw**in**-rel**a**t**ed **feature**s **in th**e **left half of th**e **i**m**age, a**s e**x**p**e**c**ted. But an**om**alo**us **f**ea**tures re**m**ain in circles at** x ultiples of π/δ k away from the origin and these are fully **moved** out of **th**e **r**e**gion** of interes**t onl**y in **th**e **la**s**t** p**an**e**l wi**th **13 ene**rgies**.** Th**u**s**,** s**u**ch **cri**te**ria on the choic**e **of** 6**k** a**r**e **crucial if** im**age** a**rt**i**f**ac**t**s a**r**e to **b**e supp**r**essed**.**

Tong **and co-work**e**r**s **[**3**7**] **hav**e **a**ls**o pr**op**o**s**e**d **a si**m**ilar holographic approa**c**h f**or **ana**ly**zing scanned-enerq**y d**ata** s**o a**s **to** s**i**m**u**l**tan**e**ou**sly **corr**ec**t f**_ **•** s**catt**e**r**ed**-wa**ve **ani**s**ot**ropies **and** el**iminat**e **twin and multip**l**es**c**attering eff**ec**ts. Thi**s **met**h**od mak**es **u**se **of a numb**er **of** sc**ann**ed**-**e**n**e**rgy diffra**c**tion** c**urv**es t**hat** a**r**e **then Fouri**e**r tr**ans**forme**d**,** s**u**m**m**e**d,** and **u**sed **to** det**ermine** t**h**e re**a**l**-ima**ge pos**it**i**on**s **of c**ert**ain** a**to**ms**. What i**s **bein**g done in this procedure is to **Fourier** transform a $\chi(\underline{k}_q)$ obtained along **th**e d**ire**c**tion kq o**ve**r s**mall s**tep**s **in k**q **f**i**r**s**t** and **th**e**n to** c**arry out** a **pha**s**e**d s**un o**ve**r** se**veral larger st**e**p**s **in-**d**ire**c**tion, a**s sh**own b**el**owz**

$$
U^{\bullet\bullet}(x,y,z) \propto \left[\Sigma_q \exp[i\underline{k}_q \cdot \underline{r}]\right]_{\Delta k_q} \chi(k_q) \exp[-ik_q r] dk_q \quad . \tag{13}
$$

Correc**tion**s **for** sc**attering a**m**pl**i**tudes** an**d**/**or pha**se sh**ift**s c**an a**ls**o** be **included in th**is **int**e**gra**l**, in** t**h**e sam**e** s**pirit** as in**di**c**ated** in E**q.** 1**2.** E**n**c**ou**r**a**gin**g ato**m**i**c **i**ma**ges have be**e**n obta**in**ed u**s**ing thi**s **a**ppro**a**ch **for (**/**3** $x \sqrt{3}$)Al on Si(111) by Wu et al. [30]. This equation is similar to Eq. **8**b**, ex**c**ept that** t**h**e s**u**l **on dir**e**ct**i**on**s **no**w **h**as a **pha**s**e that i**s **mor**e **c**le**ar**ly **r**ela**ted to a three-dim**e**n**s**iona**l **ho**l**ogr**a**phi**c **tran**s**fo**rm**.**

Comp**ari**s**on of Bq**s**. 12a and 1**3 **mak**es **it** clea**r t**hat **tk**a **app**ro**ach**es **of Bar**_**on** a**nd Tong** a**re funda**m**en**tally e**qu**i**v**ale**n**t**, in that th**ey j**u**s**t inter**ch**ange th**e **order of integration and** su**m**Aa**tion, with th**e same **overall pha**s**e fa**c**tor o**f exp**[-ikr**]**e**x**p[**i**k-r**] **-** e**xp[-ikr(l-co**sa**)]**. H**ow**e**v**e**r, th**e **fir**s**t** em**ph**as**iz**e**s finer** s**tep**s **in k** a**nd th**e **other fin**e**r** s**teps An k. Thus,** i**f bo**t**h ar**e c**ar**r**ied out ov**e**r e**q**uiv**ale**nt r**anges **of** Δk_x , Δk_y , and Δk_z , one would expect corresponding resolutions in the c**oordinat**es **x, y,** a**nd z, provided that** t**h**e **k** s**t**eps a**r**e s**uffici**e**nt**ly sma**l**l **in all dir**e**ct**i**on**s **to a**void s**p**u**r**ious **f**e**atures du**e **to th**e **noncan**cell**ation of tw**in and **mu**l**tip**le scat**t**e**r**ing **f**e**ature**s **(cf. Fi**g**. 7). If applied corr**ec**t**ly**,** bo**th** m**ethods** s**hou**l**d b**e **equa**lly **c**a**pab**le **of** s**up**p**r**essin**g twin and** mu**l**t**ipl**e m**c**a**t**te**ring** e**ff**ec**t**s**. For** a **g**i**v**e**n** im**ag**e **a**c**curacy and** sc**ope An r_** s**pac**e**, it i**s**. a**ls**o** expe**c**t**ed that th**ese t**wo approache**s **wou**l**d r**eq**uir**e **about** t**h**e same si**z**e **of data** se**t:** s**o**met**hing** l**ike** 3**,00**0**-5,000 inten**s**itie**s **with a**ll**owan**ce **for** s**urfa**c**e** s**l**_**m**e**t**ry**.**

In fa**ct, the**s**e t**wo m**ethods** of s**unning**/int**egra**t**ing ov**e**r** i**nt**e**n**sities **ar**e **r**e**ally j**u**st the t**w**o li**m**it**s **of a continu**ou**s rang**e **of choic**e**s in** s**am**pl**ing a given volume of k s**p**ac**e**, a**s **i**ll**u**s**trated in Fig. 8 [38]. H**e**r**e **ar**e sh**own** th**e holographic** im**a**ges **for a** sim**p**le **pyramida**l clu**s**te**r of Cu**

pol**ar**i**zed** r**ad**iati**on can cause preferent**i**a**l **ex***c*i**tat**i**on of sp**i**n-up or** s**p**i**n-down electron**s, **even** if **there were equal** po**pulat**i**ons o**f **the two ty***p***e**s i**n** th**e init**i**a**l s**p**i**n-orb**i**t-spl**i**t core** s**tate**s**. I**n **e**i**ther case**, **the degree o**f **d**i**chro**i**c asymmetry can be** m**easured a**s **a** f**unct**i**on o**f k **v**i**a**

$$
\mathbf{A}^{\rm CD}(\underline{k}) = [\mathbf{I}^{\rm RCP}(\underline{k}) - \mathbf{I}^{\rm LCP}(\underline{k})]/[\mathbf{I}^{\rm RCP}(\underline{k}) + \mathbf{I}^{\rm LCP}(\underline{k})] \quad , \tag{14}
$$

where IRcP and ILCP a**r**e **th**e **int**e**n**s**itie**s m**ea**s**ured with r**ig**ht and left** p**olarize**d **light, r**es**p**ec**ti**ve**l**y**• V**ery few **mea**s**ur**e**ment**s **of** the **k** de**penden**ce **of &CD in** c**ore-**level **emi**ss**ion ha**ve **been** ma**de to dat**e**, but we i**llus**tra**te the **types of** e**ffect**s e**xpected wi**th **two** ex**a**m**p**l**e**s**.**

Bansm**ann and co-workers [39a] have studied norma**l **CD in C I**s **emission from CO ad**s**or**b**ed on Pd(**l**ll) in a** c**hira**l **experi**m**ental** g**eomet**ry**. Some of** th**eir experi**m**ent**al da**ta as a f**u**n**cti**on** o**f ele**c**tron emission an**gl**e** 0 **ar**e sh**own** in **Fi**g**. 9, toge**t**her with** th**eore**t**i**c**a**l c**a**lc**u**l**ation**s b**a**s**ed on sever**a**l model**s**. Th**e **effe**c**ts are quite** p**rono**u**nced, being as large a**s **+--75% variations** i**n &CD. The three theoreti**c**a**l c**urves a**l**l agree rea**s**onab**ly **we**l**l wit**h **the data:** t**wo are ba**s**ed upon treating an** is**o**l**ated C**O **mo**l**ecu**le **on**ly**, and** o**ne** incl**ud**es **the effe**ct **of the Pd** su**b**s**trata. Two of** thes**e** c**urve**s **(**...... a**nd** **) have be**en calc**ulated by We**s**tp**hal **et a**l**. [3**9**b] An a** m**ultip**l**e-**sc**atterin**g **diffra**c**t**i**on pi**c**ture of the out**g**oin**g w**av**e, **t**h**u**s **e**m**ph**asiz**in**g **t**h**e fa**c**t that it is only throuqh photoelectron scatterinq and diffra**c**tion fro**m **neiqhborinq ato**m**s that normal circular dichroism can** m**anifest itself in core-level emission• D**i**ffra:**t**ion** th**eo**ry **in**cl**ud**in**g the** e**ffe**c**t**s **of the** un**derly**in**g Pd at**om**s (**..... **) shows that th**e s**ub**s**tr**a**ta could produce noti**c**eable effe**c**t**s **on su**c**h data, es**p**ecially at** l**o**we**r** e**n**e**r**g**i**es **for whi**c**h ba**c**k** sc**attering i**s m**or**e **i**mp**ort**a**nt,** b**ut ther**e a**r**e as ye**t no** c**on**clus**i**ve ex**p**e**ri**me**n**tal **data indi**ca**t**i**n**g s**u**c**h** e**ffe**c**t**s**. Th**e **futur**e me**a**s**urement of** c**ir**c**u**l**ar** d**i**ch**ro**is**n** i**n core** e**mi**ss**ion with** sy**nchrotron** radiation from ins**ertion devi**c**e**s d**esigned to** p**roduce h**i**gh-brightn**ess ci**r**cu**l**a**rl**y**-**po**lariz**e**d rad**i**at**i**on,** c**oup**led **wi**t**.h ana**lys**i**s **in** terms **of** mo**r**e **a**cc**urate** c**lu**s**ter-ba**s**ed mu**l**t**i**p**lesc**attering cal**c**ulations** [8b-d], thus **re**pres**ent**s a very in**tere**s**tin**g **new dire**c**tion of** s**tudy** in **p**hot**oe**lec**tron diffra**c**tion.**

MCD in cor**e-**l**ev**el **emi**ss**ion** has s**o far been** s**tudied onl**y **for a few** c**a**s**e**s**, and then onl**y **with** a **fi**x**ed e**m**i**ssi**on dire**c**tion. In F**ig**.** 1**0, we show the first** d**ata of this** ty**pe du**e t**o Baungar**te**n** e**t al. [40a] f**o**r F**e **2**PI/**2,3,**1 **emi**ss**ion fro**m **F**e**(ll0). In th**e l**ow**e**r part of (**a**) ar**e s**hown two** part**i**al s**pectra ob**t**ained wi**th **t**he **sa**m**ple magn**etiz**a**t**ion** pa**ra**llel **to-** an**d anti** p**ar**a**l**l**el** t**o- t**he **dir**ec**tion o**f **h**e**l**i**cit**y **of c**i**r**c**u**la**rl**y**-polar**i**sed radiation; this i**s **equival**e**nt** t**o changing from right t**o l**eft** p**o**l**arisa**t**ion in the frame of the sam**p**le• The full spe**c**tru**m **in (a) r**ep**r**esen**t**s **an av**e**rag**e ove**r th**e **t**w**o** m**agn**et**i**z**a**t**ion**s • **In (b),** ACD is p**lott**ed**, an**d **it** is c**lear that** signi**fic**an**t** eff**ect**s **o**f **the order o**f **a** few **per**c**en**t a**r**e s**een, even if the**y **are** muc**h** sm**al**le**r than those found for n**o**r**m**al CD in Fig. 9 S**im**ilar re**s**ults** h**a**v**e** b**een o**b**tain**ed by **Waddi**ll **et a**l**. [40**b**] for Fe 2p e**m**i**ss**ion fro**m **thin o**v**er**lay**er**s **of Fe on Cu(001), again f**o**r** a **fixed direction of** em**i**ss**ion. Both** se**t**s **of** da**t**a **have** be**en q**ua**li**ta**ti**v**ely** e**x**p**la**i**ned in terms of prefe**r**ential excitation of** p**ho**t**oele**ctr**on**s **of** o**n**e **s**p**in o**r **another** i**n the 2P**l/**2** a**nd 2P3**/**2 peak**s**,**

which is simply a difference of two normal images, and

$$
\Delta^{(x,y,z,t-1,t)} = \left| F_{\sigma}(x,y,z,t,t) - F_{\sigma}(x,y,z,t,t) \right|, \qquad (16)
$$

in which F_{\perp} is the (complex) Fourier transform integral within U and the absolute value is taken after calculating the difference. The second spin argument here is the orientation of the scatterer, here chosen to be up. Through its sign, Δ can be shown to be sensitive to the $orientation$ of the scatterer, whereas the always-positive Δ' can be shown to measure more directly the strength of the spin-dependent exchange scattering.

In Fig. 11, the image functions Δ and Δ' are plotted for the two different orientations of the scatterer: spin-up in parts $(a.2)-(a.4)$ and spin-down in parts $(b.2)-(b.4)$. The effects seen here are 10-15% of the magnitude of the peaks in the direct U images, and thus should be measurable, especially from higher-quality experimental data obtained with a next-generation synchrotron radiation source. As expected from their definitions, Δ and Δ' exhibit different behavior on flipping the scatterer spin: \triangle changes in sign, whereas \triangle' does not. Thus, it has been suggested that the locations of near-neighbor magnetic scatterers could be determined via Δ' , and actual spin flips (e.g., as temperature is changed) could be detected via Δ [42]. In parts (c.1)-(c.4) and $(d.1)-(d.4)$, the effect of adding a non-magnetic $0²$ scatterer midway between the two Mn²⁺ ions, with the scatterer spin being down, is considered. Although the normal image function U shows a strong additional peak due to the non-magnetic scatterer, this peak is strongly suppressed in Δ' , verifying that the latter should be useful for imaging only the magnetic scatterers in a system.

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Fig. 1- The basic process involved in photoelectron diffraction, with important physical variables indicated. Only single scattering is indicated for simplicity. In a holographic interpretation of such measurements, the direct or unscattered wave ϕ_{α} is identified with the reference wave, and the scattered waves $\phi_{\texttt{i}}$ are identified with object(subject) waves.

Ni(001): Ni 2p at 636 eV

Ru(0001): Ru 3d at 1206 eV

Graphite (0001) : C 1s at 946 eV

Fig. 4- The geometry of $c(2x2) S/Ni(001)$ is shown together with Fourier transform holographic images from Eq. 10, as based upon S 2p emission at 1327 eV. The hologram analyzed has cylindrical symmetry about the z axis, and extends from 10° to 50[°] above the surface. Images are shown in both the xy (=sulfur) and xz planes. No scattered-wave correction has been made, and results are shown for both experiment ((a) and (c)) and single-scattering theory ((b) and (d)). The positions of nearest-neighbor (N-N) and next-nearest-neighbor (N-N-N) S atoms are indicated. The vertical dashed line indicates the known positions of these atoms. [From Thevuthasan et al. ref. 27c]

XZ CROSS SECTION $(Y = 0.0 \text{ Å})$:

 $[001] = Z$

21

XY CROSS SECTION $(Z = 0.0$ Å):

N-N-N M.M

 $B.S2$ Al

Fig. 7- Theoretical Fourier transform images for $c(2x2)S/Ni(001)$ in the S plane obtained using only the right half of a hologram extending from 10° to 50° above the surface (as in Figs. 4 and 5). Data are shown for different numbers of energies in a phased sum according to Eq. 12b, but with no scattered-wave correction: (a) 1 energy, (b) = 3 energies, (c) = 5, (d) = 7, and (e) = 13 . The multiples of π/δ k at which artifacts can remain on spherical surfaces surrounding the origin are also indicated; the shaded peaks all occur at such positions. [From Thevuthasan et al., ref. 32b]

Fig. 9- Normal circular dichroism in C 1s emission from CO adsorbed on Pd(111). The experimental data and solid theoretical curve are from Bansmann et al. [ref. 39a]. The other two theoretical curves $(----- = CO only and -- \blacksquare$ CO in fcc sites on a 19-aton Pd(111) cluster, with the θ scan in the $[10,-1]$ azimuth) are from Westphal et al. [ref. 39b] and are based upon multiplescattering photoelectron diffraction calculations.

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