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STATISTICAL TECHNIQUES FOR AUTOMATING THE DETECTION OF ANOMALOUS PERFORMANCE IN ROTATING MACHINERY *

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K. R. Piety Oak Ridge National Laboratory Oak Ridge, Tennessee 37830

T. E. Magette
Department of Nuclear Engineering
University of Tennessee
Knoxville, Tennessee 37916

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OAK RIDGE NATIONAL LABORATORY
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K. R. Piety
Oak Ridge National Laboratory
Oak Ridge, Tennessee 37830

T. E. Magette
Nuclear Engineering Department
University of Tennessee
Knoxville, Tennessee 37919

Introduction

Scope of the work: The purpose of our research is the demonstration of surveillance techniques which extend the sophistication existing in automated systems monitoring industrial rotating equipment. This task involves assessing the effectiveness of ongoing monitoring programs and the potential of alternative approaches. Our evaluations of deficiencies in existing or proposed surveillance systems have strongly influenced the system developed at ORNL and are therefore presented in some length.

We have formulated techniques to automate the recognition of anomalous conditions in rotating equipment and have implemented these on a minicomputer. Time and frequency domain descriptors are selected to compose an overall signature characterizing the monitored equipment. The anomaly detection techniques apply an approximate statistical test to each signature descriptor. The effectiveness of this monitoring system was evaluated in laboratory tests on a small rotor assembly, using vibration signals from both displacement probes and accelerometers. As demonstrated over several months of testing, this monitoring system is capable of detecting anomalous performance while exhibiting a false alarm rate below 0.5%.

Background: The practice of monitoring gross vibrational levels as an indication of machinery health began more than 150 years ago. However, it was not until 1939 that vibration sensors and rudimentary signal analysis techniques enabled the compilation of empirical vibrational severity criteria (1-3). Only in the past twenty five years have advancements in data processing techniques and computer hardware allowed machinery health to be evaluated using signatures derived from the detailed structure of vibrational signals (4,5).

Although the advantages of signature analysis techniques are widely acknowledged, the demand such analysis methods place on plant personnel

limit their use for general surveillance tasks (5,6). Computer automation of these monitoring requirements alleviates this drawback and allows maintenance personnel to direct their efforts towards equipment most in need of attention. Additionally, a computerized surveillance system should provide sufficient sensitivity to provide an early warning of incipient failures, thus enhancing diagnostic capabilities and allowing better scheduling of maintenance. However, while monitoring machinery to detect excessive vibration is a well established practice, a best approach for automating such monitoring activities has not gained general acceptance.

Limitations of monitoring systems: There are certain drawbacks associated with all systems presently used for on-line surveillance of rotating equipment. The most basic of such systems are those which derive a set of parameters characterizing the vibration signal (such as its peak-to-peak amplitude, RMS power, or power at the rotational frequency) for comparison with absolute limits (7-9). To set such limits one must resort to a vibration severity chart, perform analytical calculations for the equipment to be monitored, or accumulate the necessary information from testing. Since fixed limits must encompass the "worse-case" conditions over the entire range of normal operations, sensitivity to anomalous performance at any given operational state is reduced (9,10). Another disadvantage frequently associated with this approach is a lack of information on which to base diagnostic decisions (9,11).

In an effort to compensate for this deficiency some monitoring systems add trending capabilities or utilize the detail available with complete spectral analysis (12-16). Unfortunately, due to the storage limitations which exist in systems monitoring several hundred data channels. trending the entire power spectrum is typically not practical. storage problems associated with maintaining full spectral detail is further compounded if baseline signatures and limiting criteria are to be saved as a function of operational conditions. A common compromise is to trend only gross vibrational levels and to alarm if these parameters exceed acceptable limits. The complete power spectra of the vibrational signals are saved only at baseload conditions at the outset . of monitoring, with further spectral analysis performed only upon operator request, at widely spaced intervals, or under alarm conditions. A decision to monitor only gross vibrational level sacrifices sensitivity (6,11,19). However, the decision to monitor a larger set of detailed descriptors makes it difficult to establish meaningful detection criteria (particularly as a function of operational conditions) and has, in some cases, completely exhausted the patience of operations personnel (7).

Another approach taken by some researchers is the implementation of statistical algorithms as a basis for anomaly detection (17-19). Both the experience and success in applying these techniques have been

limited. Our own previous efforts with a strictly statistical approach revealed that the rotating equipment being monitored was nonstationary. Even at fixed conditions, the equipment would operate for indefinite periods described by one set of statistical parameters and then randomly change to other equally normal conditions with different statistics. Data taken under such conditions results in biased samples of the statistical populations, thereby destroying the rigor of statistical tests (18). Statistical techniques can also be data intensive and thus become unmanageable with the added complication of varying operational conditions.

The most mathematically complex, techniques envisioned for automated surveillance systems may be generally referred to as pattern recognition methods (19-22). Implementation of these methods typically requires accumulation of signatures from any abnormal conditions to be detected, in addition to those for normal conditions. Such comprehensive data requirements cannot normally be satisfied, particularly at the onset of surveillance activities. In addition, since pattern recognition methods have characteristically been developed for other applications, they rarely incorporate — and then only indirectly — engineering knowledge pertinent to specific surveillance tasks. It nonetheless would appear that some of these methods do show promise as diagnostic algorithms once the required data is obtained.

The ORNL surveillance system overview: This monitoring system is the result of applying engineering judgment to the specific task of automating machinery surveillance. To maintain high sensitivity to anomalies, vibrational signatures are catalogued as a function of operational conditions, and detection decisions are based on simple statistical tests. The determination of alarm criteria is accomplished automatically based upon normal data obtained during a learning period. Judicious feature selection is incorporated to reduce storage requirements; however, data logging adequate for diagnostic investigations is provided. False alarms are reduced by implementing processing logic that compensates for normal data variations.

Feature selection: A vibration signature is obtained by selecting only a subset of the various signal descriptors that can be derived from data processing techniques. This seelction process introduces available engineering knowledge related to individual equipment, critical fault events, or the signal character into the monitoring system. For example, the power in the fifth order (five times the rotational speed) would logically be included as a feature describing a fan with five blades. Obviously, the specific set of parameters comprising a signature will vary for dissimilar applications. Discarding or combining redundant descriptors should result in a reduced set of descriptors which enhance the information contained in the measured data. For our test purposes we chose 48 parameters per signal which define the phase, size and shape of the time-averaged waveform, the total power of the

signal, the harmonic and nonharmonic power, the power and phase of the first three orders of rotation, the spectrum-weighted order, and the average harmonic and nonharmonic order. A detailed explanation of these descriptors is given in the appendix. Although these features are not proposed as an optimum set for other monitoring applications, many of the frequently chosen descriptors are included, and the ability to compare the performance of descriptors with different levels of detail is provided.

Reference catalogue of baseline data: Baseline signatures are catalogued as a function of operational conditions. This procedure necessitates access to variables defining the operational state, for example, speed, load, or flow. Discrete intervals are chosen to span the full range available to controlling variables; once specified, the interval structure determines the maximum number of entries required in the reference catalogue. Since it has been demonstrated that variations in speed and load can introduce changes in vibration exceeding those associated with anomalies (10), compensation for such changes stimulated by control variables is necessary for maintaining sensitivity for anomaly detection and for reducing false alarms. Although most investigations acknowledge these facts (7-10), few monitoring systems implement capabilities for handling this complication. We chose the direct cataloguing approach after reviewing various mathematical alternatives and experimenting with techniques, based on principal components analysis and regression analysis.

Establishing limiting criteria: Baseline signatures and their normal interval of variation are established automatically by observing equipment operation during an initial learning period. During this period. the equipment must be operated at or near all conditions for which monitoring capability will be needed. The learning period should be of sufficient duration to include a representative sample of normal variations. This period was 2-4 days in our investigations. quacy of learning appears to be more closely related to elapsed clock time than to the number of signatures measured because of the biased sampling previously cited (18). Several checks are available to ascertain if the learning period has been adequate. These include counters which conservatively estimate the proportion of the learning signatures considered normal and the number of learning signatures since the last abnormal classification, as well as the ability to switch to the monitoring mode for a defined period during which a detailed monitoring summary is automatically obtained. If necessary, additional learning can be initiated at any time. Since the system detects deviations from whatever baselines are established, sensitivity to further degradation is maintained whether or not equipment was operating normally during the learning period.

Detection logic: During monitoring, each vibration signature is measured under steady operating conditions and tested to determine if

its deviations from the baseline signatures are statistically significant. While the application of classical statistics is invalidated by biased sampling and by lumping differing operations into coarse intervals, the deviations calculated in approximate standard deviation units do provide a quantitative measure of problem severity. Approximate methods of calculating signature deviations, although lacking in mathematical elegance, are incorporated because they have proven to reduce the incidence of false alarms.

During learning, the maximum and minimum values encountered for every feature are stored for each operational interval. When a signature at a given operational state is tested, the extreme values normal to that operational interval and those values from its nearest neighbors are combined to obtain a smeared interval that encloses all extremes. From this interval, a pseudo mean, m, and standard deviation, c, are calculated as follows:

$$m = \frac{Max + Min}{2}$$

$$\sigma = \frac{\text{Max} - \text{Min}}{6}.$$

The absolute deviations calculated using these quantities are compared against a confidence limit which decreases from C+3 to C (an input parameter) as the number of measurements, M, upon which m and σ are based, increases from 0 to 500.

$$\left|\frac{x-m}{\sigma}\right| \leq c+3 \cdot \frac{500-M}{500}$$

Statistical intuition and experience indicate that values of C around 7 are most appropriate. For industrial surveillance applications, testing the gross vibration levels against established severity criteria (1-4) is recommended. This additional detection capability would provide limited protection during learning when no other performance monitoring is in force and would inherently set an upper limit on the statistically-derived criteria.

Comprehensive data logging for diagnosis: No automatic diagnostic logic is implemented in this system. However, the detection of anomalous events does automatically initiate procedures that log data to assist in diagnosis. If a signature is encountered that exceeds normal bounds, an anomaly signature catalogue is begun for all signals from the suspect machine. The anomaly catalogue allows detailed comparisons between data

accumulated following the suspect event with that in the baseline reference catalog obtained during learning. Additionally, a detection summary which tallies suspect events for each signature component and computes the average deviation is collected and available upon request. Also upon demand a variety of visual displays from standard signal processing algorithm (orbits and detailed power spectra) can be obtained, although data from these analysis capabilities is not automatically retained. It is expected that the data collected for diagnostic purposes will allow the development of algorithms to diagnose the most probable faults.

Results

Software implementation: The surveillance software has been implemented on a Digital Equipment Corp. PDP 11/34 minicomputer with 28K words of memory. Mass storage capability is provided by two disks, each with a 1.5M word capacity. All programs are written in FORTRAN except for the peripheral handler routines that require assembly language.

A small portion of the disk storage is required for the software system; the remaining portion, $^{\sim}2M$ words, is available for data storage. The burden of the data storage is associated with cataloguing baseline data. The total storage requirement, R, for this reference catalogue is given by

$$R = 4 \sum_{i=1}^{M} o_i \sum_{j=1}^{S_i} D_{ij},$$

where M is the number of machines to be monitored; 0_i , the number of lumped operational states allowed for the *i*th machine; S_i , the number of sensors on the *i*th machine; and D_{ij} , the number of descriptors used to describe the information from the *j*th sensor on the *i*th machine.

The mass storage requirements for the monitoring system are within reason for even large scale industrial applications. Assume, for example, that one desired to monitor 100 machines, each equipped with eight sensors. An analysis that assigns 20 lumped operational states to each machine and characterizes each signal with 25 descriptors would require 1.6M words of storage. This allows one to describe each piece of equipment with 200 descriptors and still reserve some storage area for logging diagnostic data.

Evaluation of monitoring system: A laboratory evaluation of the monitoring software has been accomplished using a small rotor assembly

driven by a fractional horsepower motor (1). Three displacement probes are installed on the rotor as shown in Fig. 1.

One probe ("keyphasor") provides a tach signal and, through supplementary electronics, generates a rotationally synchronized sampling pulse to trigger the analog-to-digital converter. Two other probes, placed at 90° to each other, measure the radial vibration of the shaft. In addition, two accelerometers, not shown in Fig. 1, have been installed on the inboard bearing housing to measure the orthogonal components of radial vibration.

The rotor can attain spends from 0 to 200 revolutions per second (rps); this was the only contract variable altered during tests. For our purpose, lumped operational states were chosen to correspond to 1-rps intervals. This speed resolution was a convenient choice which offered reasonable detail.

In our previous work (18), the monitoring system was unable to maintain a low false alarm rate over extended periods of testing using the limiting criteria which were automatically established. This difficulty was overcome by modifying the detection logic and by extending the learning period. We have, in fact, demonstrated that a learning file composed in a few days can be used to monitor normal operation for periods of several months without false alarms becoming a difficulty.

In our tests, two signatures describing rotor operation are actually calculated, one for the displacement probes and the other for the accelerometer. Signature descriptors for both the horizontal and vertical directions combine to formulate this signature.

The detection capability of the monitoring system was investigated by introducing fault conditions into the test setup. The four fault types chosen for testing include shaft rub, imbalance, mechanical looseness, and misalignments. Each anomaly type can be introduced in varying degrees of severity. Some faults introduced no discernible perturbation to the vibration signals; however, detection was always possible as the severity level was increased. After the anomalous conditions associated with fault testing are removed, the return to normal operation is verified by the monitoring system. Examples of the type diagnostic data available from the system are presented as the individual tests are described.

Imbalance test: The balance of the rotor was altered by the addition of a 1.52-g mass 3.32 cm from the shaft centerline (translating to 0.238 Nt m) (ref. Fig. 1). The change in the vibration was readily detected by

^{1.} Bently Nevada Corp., Minden, Nevada, Model RK-3.

both horizontal and vertical displacement probes, as illustrated by the detection summary shown in Table 1. Any signature for which some descriptor was out of bounds is considered suspect. This was the case for all 1000 comparison signatures of each type comprising this summary. An interesting detail in this test is that the weight added actually improved the balance of the rotor. This is apparent from Fig. 2 which plots the time-averaged orbit for both baseline and imbalance condi-This can also be seen from the detection summary which shows a reduction (negative deviations) in the signal descriptors associated with the amplitude of the vibration. A change in vibrational amplitude at the first order is well established as the primary indication of changes in balance. However, as noted in Table 1, this descriptors was affected less dramatically than others. This results from the asymmetric domain (always positive) of power spectrum measurements which reduces their statistical sensitivity to reductions in their magnitude. This can be corrected by using instead the log of their magnitudes. phase of the first order does show significant variations throughout the entire speed range as demonstrated in Fig. 3. A similar plot is shown in Fig. 4 which contrasts normal and anomalous variations for the peak displacement descriptor as a function of speed.

Misalignment test: The alignment of the rotor can be altered by placing shims under the bearing pedestals. The data shown resulted from raising one side of the inboard bearing pedestal by 1.32 mm, offsetting the centerlines of the motor and rotor shafts. The misalignment was readily detected as indicated by most of the descriptors shown in Table 2. Unexpectedly, all descriptors except nonharmonic power showed a decrease in their magnitudes. Figure 5 shows this effect in detail for the power at the second order and is in contrast to Fig. 6 which shows the increase in the nonharmonic power.

The decrease in overall and harmonic vibration levels is not, however, an indication that the damage potential has been reduced since the coupling to the motor destructively failed within 12 hours. The prominent peak in the plot of nonharmonic power, Fig. 6, resulted from data taken just prior to the destruction of the coupling. The reduction in vibration levels was not common to all misalignment tests; nonetheless, it does serve as a base in point to caution system designers that would ignore the importance of such effects.

Mechanical looseness test: This test is accomplished by loosening the screws that fasten the inboard bearing pedestal to the base plate. In this case, the accelerometers had a greater sensitivity to the abnormality than did the proximity probes. This rather pronounced effect in the accelerometer signatures, tabulated in the detection summary given in Table 3, most likely results from altering the mechanical impedance at the bearing pedestal (23). All descriptors influenced by the harmonic content of the signal were strongly affected. A plot of the extreme values experienced under both normal and loose conditions for the power at the second order as a function of speed is shown in Fig. 7.

Partial shaft rub test: The shaft rubs which were introduced in our tests were detected most strongly by the accelerometer signals. The data given here is from the least severe case, a partial shaft rub, where the rub screw (see Fig. 1) is allowed to lightly bounce against the shaft. This anomaly emphasizes again the importance of choosing descriptors which measure nonharmonic signal power (11). As seen from the detection summary in Table 4, the nonharmonic power is the only parameter which dependably indicates the presence of the rub. Detailed power spectra for the accelerometer under normal and rub conditions are shown in Figs. 8 and 9, respectively. The noise floor of the rub spectrum is raised over a rather broad order interval; this train has been characteristic of rub anomalies we tested.

Summary and recommendations: The monitoring system automatically established limiting criteria during an initial learning period of a few days; and subsequently, while monitoring the test rotor during an extended period of normal operation, experienced a false alarm rate of 0.5%. At the same time, the monitoring system successfully detected all fault types that introduced into the test setup. Tests on real world equipment are needed to provide final verification of the monitoring techniques. The incremental expense required to implement hardware for this purpose would be small in an industrial plant where sensors, electronics, and cabling already exist for vibration monitoring. Furthermore, the data required to make this monitoring approach effective would not hinder normal industrial operations.

There are areas that would profit from additional investigation in the laboratory environment. A comparison of the relative value of alternate descriptors under given fault conditions would be worthwhile. This should be pursued in conjunction with extending the set of fault types available, e.g., lecaring problems. Other tests should examine the effects of using fewer (more coarse) intervals to define the lumped operational states. Finally, techniques to diagnose the most probable fault should be developed by drawing upon the extensive data automatically logged by the monitoring system.

Appendix:

In Table A-1 is a list of the descriptors which we chose to include in our vibration signatures. Many of these descriptors are commonly used and require no additional explanation. However, I will provide some discussion for those where confusion may exist.

The waveform from a vibration sensor attached to a rotating machine has a repetitive component. Regardless of magnitude of this component, its presence can be enhanced by time-averaging the waveform. This process requires that the raw signal be sampled at some integer multiple of the frequency of rotation, f_0 . These sampled values, $\mathbb{X}(i\Delta t)$, are then averaged using the following formula

$$\bar{X}_{i} = \frac{1}{NREV} \sum_{n=1}^{NREV} X(i\Delta t + nT) \quad (i = 0, 1, 2, ... NPTS-1)$$
 (1)

where T is the period of rotation

$$T = NPTS \cdot \Delta t = \frac{1}{f_0}$$
 (2)

This time-averaging technique is equivalent to applying a comb filter to the original signal which passes only the fundamental frequency and its harmonics. The time averaged waveforms from two sensors at 90° to each other can be used to obtain average orbital plots which describe the motion of the shaft centerline at the monitored position. The "NPTS" values (usually 30) that describe the averaged waveform, \bar{X}_{i} , are correlated with the averaged waveform obtained initially as a baseline, \bar{X}_{i} , to derive three additional quantities. The shape factor is the maximum value obtained for the normalized correlation function, H(J), which is defined by

$$|e|(J) = \frac{\prod_{i=1}^{NPTS} \overline{X}_{i+J} \cdot \overline{XB}_{i}}{||e|(J)||}$$
 (J = 0, 1, 2, ... NPTS-1) (3)

Values for \bar{X}_{i+j} beyond X_{NPTS} are obtained by repeating the original waveform. The point J=L where H(J) is a maximum also defines the lag value, LAG, and the size factor, SZF, according to the following expressions,

$$LAG = \hat{J} * \frac{360}{NPTS}$$
 (4)

$$SZF = \frac{\sum_{i=1}^{NPTS} \overline{X}_{i+L} \cdot \overline{XB}_{i}}{\sum_{i=1}^{NPTS} \overline{XB}_{i}^{2}}$$
(5)

When analyzing the vibrational signals from rotating machinery, order domain analysis (instead of the more familiar frequency domain) simplifies interpretation of results, especially when variable speed operation exists. The basic relationship that allows conversion between the two domains is

$$Q = \frac{f}{f_0} \tag{6}$$

where f_o is the fundamental rotational frequency.

Integral orders (Q = 1, 2, 3, etc.) occur at harmonics of the running speed. If the vibrational signal is analyzed for NREV revolutions, the minimum order resolution achievable is

$$\Delta Q = \frac{1}{NREV} \tag{7}$$

The power at any order, Q_i , will be denoted by $G(Q_i)$ where $Q_i = i\Delta Q$, i = 1, NOC.

Thus the total power in the vibrational signal up to some desired order, $\boldsymbol{Q}_{\mathrm{D}}\text{,}$ is obtained by summing

$$TPOW = \sum_{i=1}^{k} G(Q_i)$$
 (8)

where

$$K = \frac{Q_D}{\Delta Q} \tag{9}$$

The harmonic power in the signal can be obtained by summing the power spectrum estimates at integral orders

$$HPOW = G(m)$$

$$m=1$$
(10)

The nonharmonic power is the difference of these two quantities

$$NHPOW = TPOW - HPOW \qquad (11)$$

When combining power estimates over an order interval, another parameter of interest is the power-weighted average order. This parameter provides an indication of the order at which the power in the interval is concentrated. This is given by

ATO =
$$\begin{bmatrix} k & Q_{i}^{2} & G(Q_{i}) \\ \frac{i=1}{k} & G(Q_{i}) \\ i=1 \end{bmatrix}^{1/2}$$
 (12)

Similarly the average harmonic order is given by

AHO =
$$\begin{bmatrix} N & & & & & \\ & N & & & & & \\ & m=1 & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & \\ & & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\$$

and the average nonharmonic order is given by

ANHO =
$$\begin{vmatrix} k & Q_{i}^{2} & G(Q_{i}) & -N & m^{2} & G(m) \\ \frac{i=1}{k} & \frac{N}{m=1} & G(m) \\ i=1 & \frac{1}{2} & G(M) & \frac{1}{2} & G(M) \end{vmatrix}$$
 (14)

All of the parameters defined above can be calculated from the time domain signal directly without the need for order domain transformations. The total power can be obtained by integrating the squared time signal,

TPOW =
$$\frac{1}{T} \int_0^T \chi^2(t) dt$$
 (15)

TPOW
$$\approx \frac{1}{\text{NDAT}} \stackrel{\text{NDAT}}{\rightleftharpoons} \chi_{\mathbf{i}}^2 \approx \stackrel{k}{\rightleftharpoons} G(Q_{\mathbf{i}})$$
 (16)

The total harmonic power can be obtained by integrating the time averaged waveform

$$HPOW \approx \frac{1}{NPTS} \sum_{i=1}^{NPTS} \tilde{\chi}_{i}^{2} \approx \sum_{i=1}^{N} G(m)$$
 (17)

The sums of the squared orders weighted by their power in Eqs. (12)-(14) are equal to integrating the square of the derivative of the time signal and the time averaged signals, respectively,

$$\sum_{i} Q_{i}^{2} G(Q_{i}) = \frac{1}{T} \int [\chi^{2}(t)]^{2} dt$$
 (18)

$$\approx \frac{1}{\text{NDAT}} \left(\frac{\chi_{i} - \chi_{i-1}}{\Delta t} \right)^{2} (\Delta t)$$
 (19)

$$\sum_{m} m^{2} G(m) \approx \frac{1}{NPTS} \sum_{i=1}^{NPTS} \left(\frac{\chi_{i} - \chi_{i+1}}{\Delta t} \right)^{2} (\Delta t)$$
 (20)

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- 22. H. E. Hunter, "Demonstration of the Use of ADAPT to Derive Predictive Maintenance Algorithms for KSC Central Heat Plant," Report No. AVSD-0084-73-RR, AVCO Systems Division for NASA, Wilmington, Mass., 01887, November 1972.
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Table 1. Detection summary (1000 signatures tested) for imbalance test over the speed range of 60 to 85 rps.

	Displacement Signature				Acceleration Signature			
Signature Descriptor	X Sensor No. Out (Dev. ^a)		Y Sensor No. Out (Dev.a)		X Sensor No. Out (Dev. ^a)		Y Sensor No. Out (Dev. ^a)	
Lag values Shape factor Size factor	997 0 416	(-12.2)	802 8 1	(-18.9)	994 0 0	(0.0)	0 0 0	(0.0)
Peak values	416	(-10.4)	1	(-26.3)	0	(0.0)	0	(0.0)
Total power	81	(-10.6)	1	(-18.6)	0	(0.0)	0	(0.0)
Harmonic power	81	(10.6)	1	(-18.6)	0	(0.0)	0	(G.O)
Nonharmonic power	0	(0.0)	0	(0.0)	0	(0.0)	0	(0.0)
Average order	350	(8.7)	18	(12.5)	95	(8.0)	0	(0.0)
Average harmonic order	38	(8.9)	12	(11.8)	1	(7.5)	0	(0.0)
Average nonharmonic order	0	(0.0)	0	(0.0)	0	(0.0)	0	(0.0)
PSD order 1 PSD order 2 PSD order 3	71 0 0	(-10.9) (0.0) (0.0)	1 1 0	(-18.6) (-8.5) (0.0)	0	(0.0) (0.0) (0.0)	0	(0.0) (0.0) (0.0)
Phase order 1 Phase order 2 Phase order 3	1000 726 11		416 914 10		1000 445 409		0 0 0	
	No. of	suspect s	ignatur	es = 1000	No. of	suspect s	ignature	s = 1000

aDeviations from baseline data in approximate standard deviation units.

Table 2. Detection summary (500 signatures tested) for misalignment test over the speed range of 55 to 100 rps.

	Displacemen	t Signature	Acceleration Signature			
Signature Descriptor	X Sensor No. Out (Dev.a)	Y Sensor No. Out (Dev.a)	X Sensor No. Out (Dev.a)	Y Sensor No. Out (Dev.a) 0 0 0 0 (0.0)		
Lag values Shape factor Size factor	426 0 463 (-18.1)	336 13 51 (-18.4)	487 0 2 (-8.8)			
Peak values	310 (-13.7)	47 (-11.0)	0 (0.0)	0 (0.0)		
Total power	313 (-13.1)	47 (-16.4)	0 (0.0)	0 (0.0)		
Harmonic power	315 (-13.7)	47 (-18.7)	0 (0.0)	0 (0.0)		
Nonharmonic power	459 (333.9)	461 (514.3)	38 (10.0)	0 (0.0)		
Average order	23 (3.5)	6 (-10.7)	179 (10.4)	0 (0.0)		
Average harmonic order	11 (9.6)	7 (18.7)	101 (14.4)	0 (0.0)		
Average nonharmonic order	0 (0.0)	0 (0.0)	408 (-14.2)	14 (-8.3)		
PSD order 1 PSD order 2 PSD order 3	315 (-13.7) 101 (-9.1) 10 (27.0)	47 (-18.7) 47 (-8.3) 11 (18.0)	5 (20.5) 0 (0.0) 14 (35.0)	0 (0.0) 0 (0.0) 0 (0.0)		
Phase order 1 Phase order 2 Phase order 3	493 1 28	327 189 305	496 22 336	3 0 1		
e.	No. of suspect	signatures = 500	No. of suspect signatures = 500			

 $^{^{}lpha}$ Deviations from baseline data in approximate standard deviation units.

Table 3. Detection summary (1000 signatures tested) for mechanical looseness test over the speed range of 75 to 95 rps.

	Displacemen	t Signature	Acceleration Signature			
Signature Descriptor	X Sensor No. Out (Dev. ^a)	Y Sensor No. Out (Dev. ^a)	X Sensor No. Out (Dev. a)	Y Sensor No. Out (Dev. a) 0 0 0 26 (9.9)		
Lag values Shape factor Size factor	0 0 7 (-8.6)	5 0 0 (0.0)	194 0 0 (0.0)			
Peak values	8 (-9.0)	0 (0.0)	151 (9.8)	309 (17.1)		
Total power	7 (-8.4)	0 (0.0)	137 (9.7)	210 (17.3)		
Harmonic power	7 (-8.5)	0 (0.0)	114 (10.1)	313 (17.0)		
Nonharmonic power	47 (24.9)	6 (9.9)	121 (15.8)	96 (16.1)		
Average order	0 (0.0)	0 (0.0)	13 (9.1)	0 (0.0)		
Average harmonic order	0 (0.0)	0 (0.0)	7 (9.1)	0 (0.0)		
Average nonharmonic order	0 (0.0)	0 (0.0)	341 (-11.3)	15 (7.9)		
PSD order 1 PSD order 2 PSD order 3	7 (-8.5) 0 (0.0) 0 (0.0)	0 (0.0) 0 (0.0) 0 (0.0)	0 (0.0) 957 (154.0) 901 (126.8)	112 (13.2) 216 (21.5) 131 (16.3)		
Phase order 1 Phase order 2 Phase order 3	0 0 0	29 32 0	353 419 266	0 0 0		

aDeviations from baseline data in approximate standard deviation units.

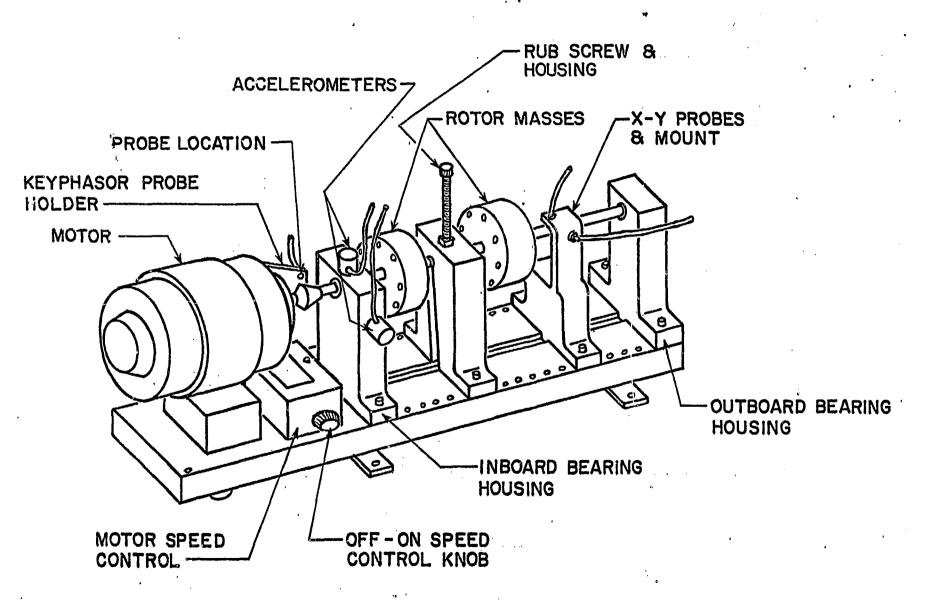
Table 4. Detection summary (20 signatures tested) for partial shaft rub test over the speed range of 60 to 65 rps.

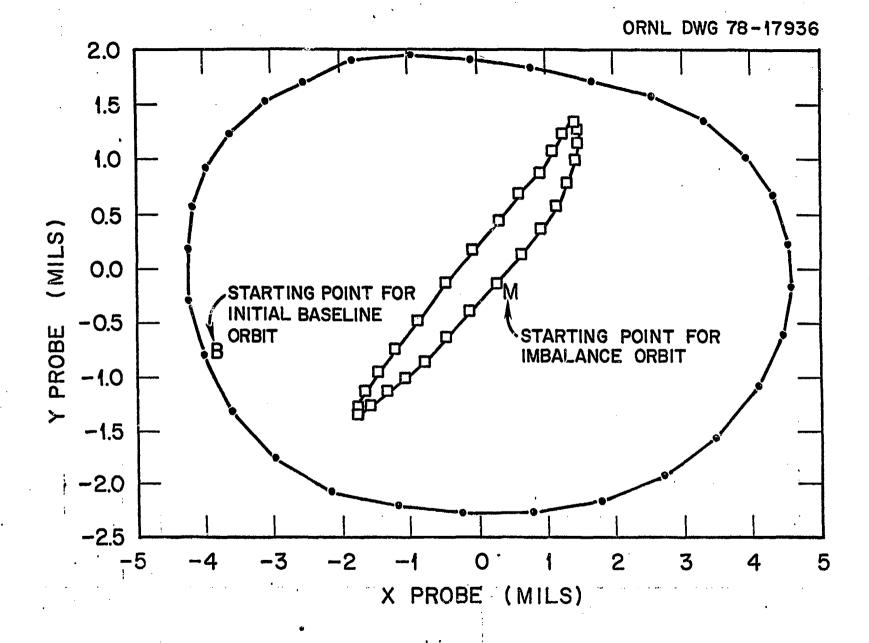
	Displacemen	t Signature	Acceleration Signature			
Signature Descriptor	X Sensor No. Out (Dev. a)	Y Sensor No. Out (Dev. ^a)	X Sensor No. Out (Dev. ^a)	Y Sensor No. Out (Dev.a)		
Lag values Shape factor Size factor	0 0 0 (0.0)	0 0 0 (0.0)	0 0 0 (0.0)	0 0 0 (0.0)		
Peak values	0 (0.0)	0 (0.0)	0 (0.0)	20 (27.1)		
Total power	0 (0.0)	0 (0.0)	0 (0.0)	15 (17.9)		
Harmonic power	0 (0.0)	0 (0.0)	0 (0.0)	0 (0.0)		
Nonharmonic power	4 (26.4)	17 (85.7)	19 (19.4)	20 (30.8)		
Average order	0 (0.0)	0 (0.0)	0 (0.0)	0 (0.0)		
Average harmonic order	0 (0.0)	0 (0.0)	0 (0.0)	0 (0.0)		
Average nonharmonic order	0 (0.0)	0 (0.0)	0 (0.0)	0 (0.0)		
PSC Stuer 1 PSD order 2 PSD order 3	0 (0.0) 0 (0.0) 0 (0.0)	0 (0.0) 0 (0.0) 0 (0.0)	0 (0.0) 0 (0.0) 0 (0.0)	0 (0.0) 0 (0.0) 0 (0.0)		
Phase order 1 Phase order 2 Phase order 3	0 0 0	0 0 1	0 0 0	0 0 0		
	No. of suspect	signatures = 17	No. of suspect	signatures = 20		

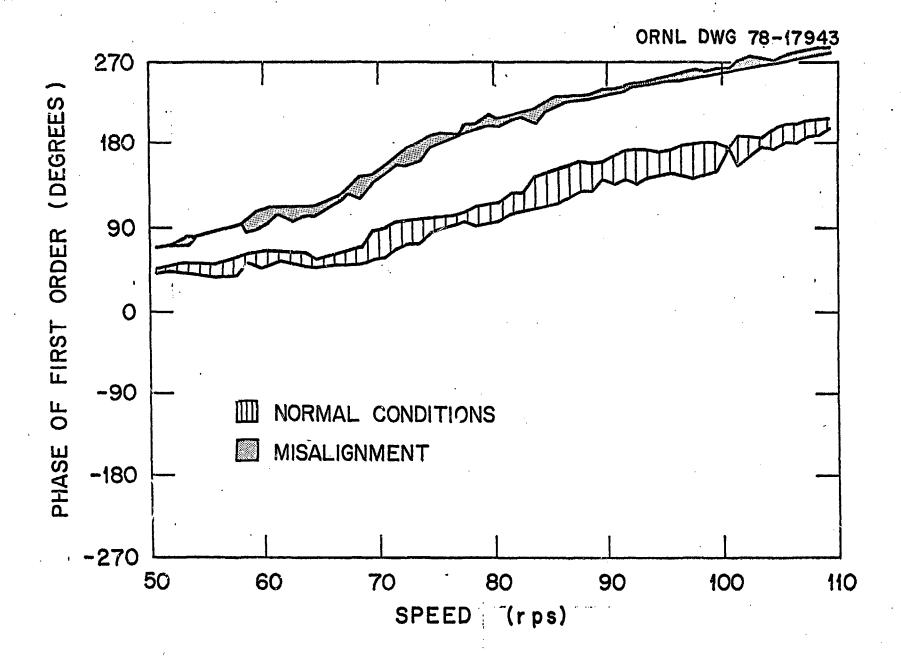
lphaDeviations from baseline data in approximate standard deviation units.

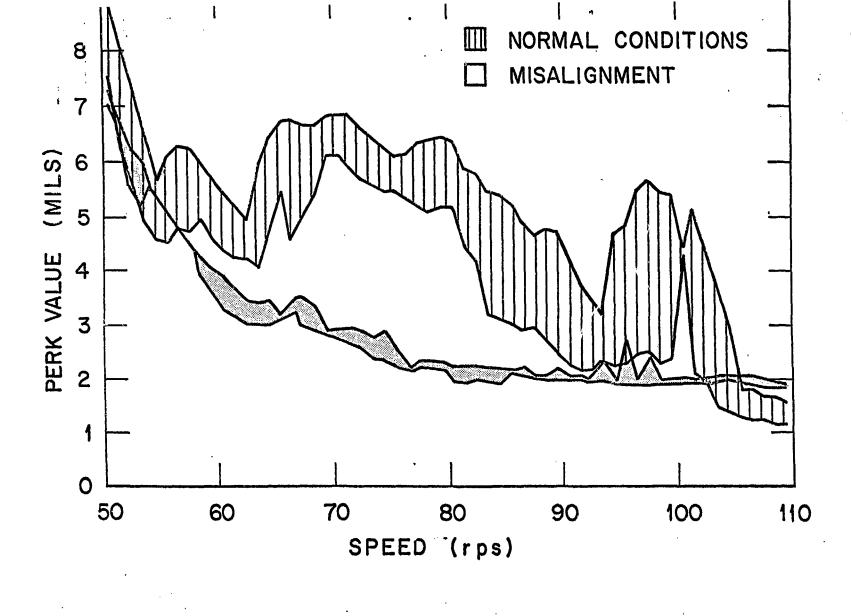
Table A-1. Descriptors in vibration signature

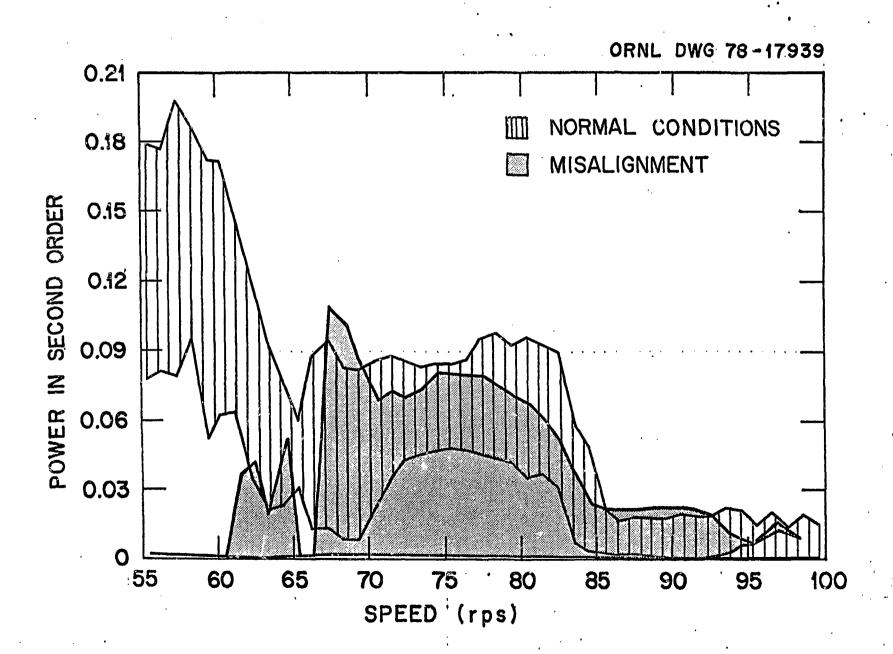
- 1. Time-averaged waveform ("NPTS" values)
- 2. Lag value of time-average waveform
- 3. Shape factor for time-average waveform
- 4. Size factor for time-average waveform
- 5. Peak signal value
- 6. Total signal power
- 7. Harmonic power in signal
- 8. Nonharmonic power in signal
- 9. Average order of signal
- 1.0. Average harmonic order of signal
- 11. Average nonharmonic order of signal
- 12. Power at first order of signal
- 13. Power at second order of signal
- 14. Power at third order of signal
- 15. Phase of first order of signal
- 16. Phase of second order of signal
- 17. Phase of third order of signal

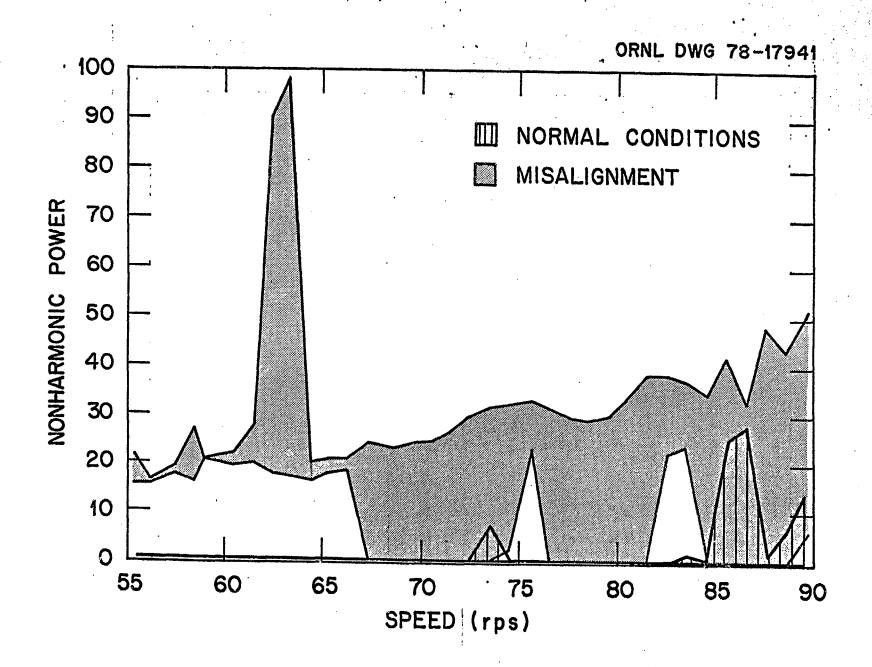


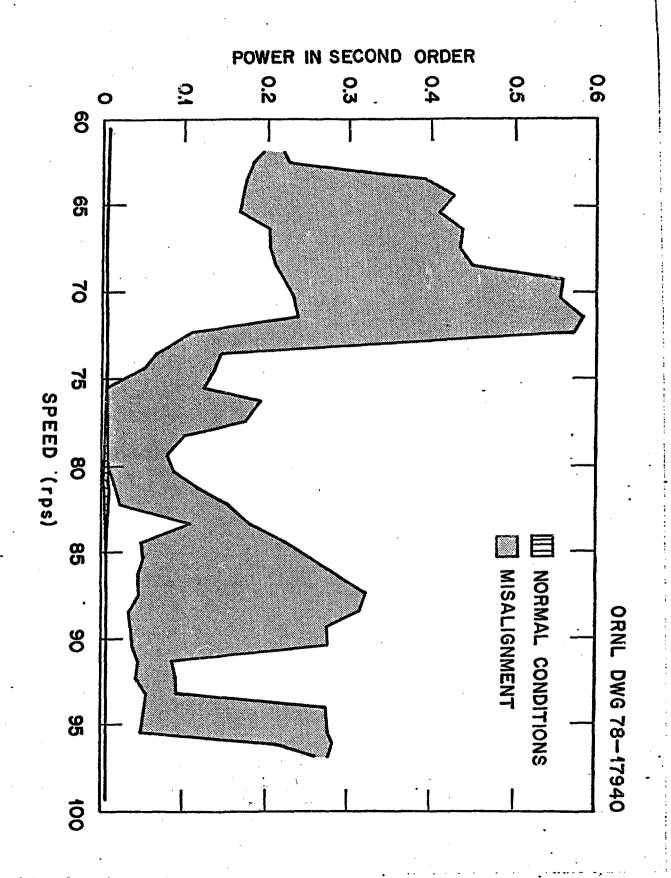


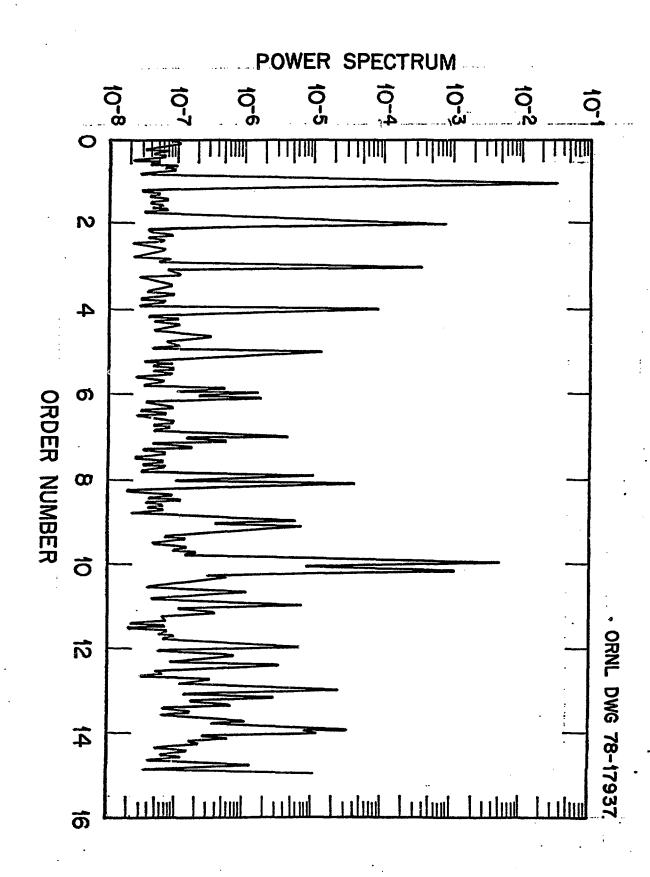


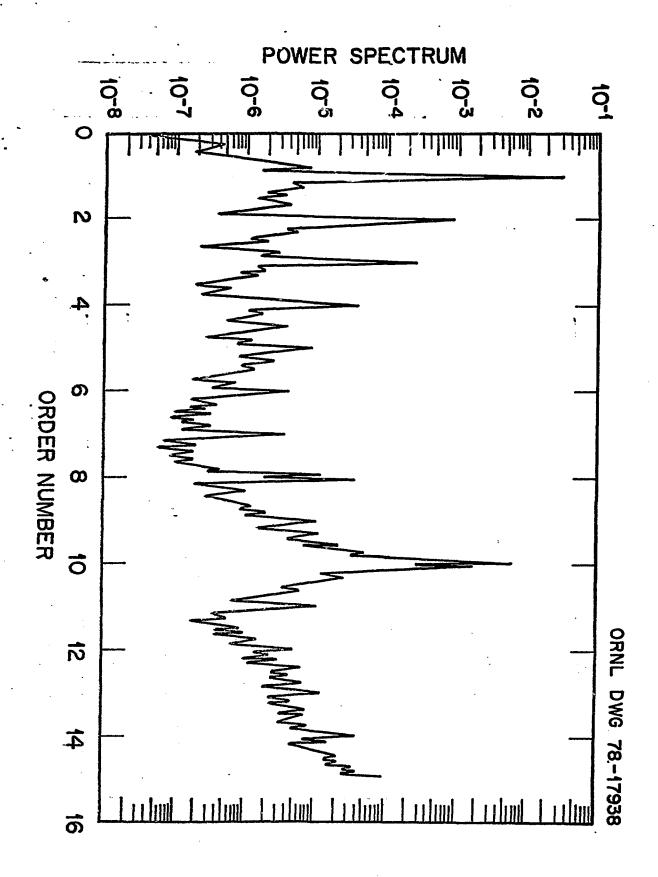












F. 1 The note assembly used in testing the monitoring software. The time overeged orbits for normal and imbalance conditions. - Fig. 2 Range for phase values of the first order under normal and imbalances conditions v. speed. The range of peak values_experienced_ under mormal and imbalance conditions V. speed. Amplitude extremes experienced by
the power in the second order
under normal and misslighed
conditions v. speed. Amplitude ettems efperienced by the monkermonic porver under mormal and misaligned conditions of speed. Amplitude extremes experienced by

the power in the second order under

normal and musiligned conditions V.

Jij 8. Power spectrum for horizontal accelerometer during partial sheft rub test et speed 59 rps.