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PPPL--2520

DE88 011874

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Relaxation Phenomena in the High Temperature S-1 Spheromak

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Operation of the S-1 device in a high current density ($j/n_e \geq 2 \times 10^{-14} \text{ A}\cdot\text{m}$) regime has created high electron temperature spheromaks ($50\text{eV} \leq T_e \leq 130\text{eV}$). The mechanisms and causes of the periodic relaxation events often observed in these hotter spheromak plasmas were made clear. Also, a relationship between the MHD relaxation cycle and confinement characteristics was revealed for the first time. Resistive loss at the outer edge of the plasma causes a departure from the initial force-free minimum-energy Taylor state to a MHD profile unstable to low- n ideal MHD modes; a relaxation event then returns the configuration to nearly a Taylor state.

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Plasma relaxation oscillations near the force-free, minimum-energy (Taylor) state, in both spheromaks and RFPs, have recently received markedly increased attention. The significant achievements of this paper are identification of the mechanism of relaxation cycle around the Taylor state in high temperature spheromak plasmas and demonstration that the confinement characteristics of the spheromak are responsible for deviations from the Taylor state, causing relaxation phenomena which in turn affect confinement.

The minimum energy state of the force-free spheromak configuration is the Taylor state,¹ in which $(\vec{j} \cdot \vec{B})/B^2 = \mu = \text{constant}$ throughout the plasma volume where j is current density and B is magnetic field strength. Actual spheromak plasmas are observed to be close to the Taylor state in the low temperature regime.²⁻⁴ In high temperature spheromak plasmas, deviations from a Taylor state ($\mu = \text{constant}$) are observed; in addition, a force-free configuration does not strictly permit a pressure gradient in the plasma since $\nabla p = \vec{j} \times \vec{B} = 0$, where $p = \text{pressure}$. The questions arise as to how much pressure (or pressure gradient) a spheromak in a near-Taylor state can maintain, and is the pressure limit due to MHD instabilities?

Relaxation oscillations were first observed⁵ in the S-1 Spheromak device on the global parameters. Spheromaks in CTX were observed⁶ to deviate from the Taylor state and become unstable to low n-mode ($n = \text{toroidal mode number}$) instabilities, in agreement with theory, but did not exhibit relaxations. By measuring the radial magnetic field profile of spheromaks in the CTCC device,⁷ sudden stepwise instabilities in the configuration could be explained by a periodic evolution from broad stable profiles to peaked unstable profiles which then triggered a readjustment.

The present paper reveals the mechanism of a relaxation event in S-1 spheromak plasmas. By measuring the detailed 2-D internal structure of the spheromak configuration, q is directly measured; the stability of the configuration is thus determined and the cause of the relaxation is clearly revealed for the first time. Also for the first time, the effects of the relaxation events in spheromaks on confinement are identified in high temperature plasmas in the S-1 spheromak device by use of a multi-point Thomson scattering system yielding radial profiles of temperature and density. It was found that resistivity profiles (higher near the edge of the plasma) cause the spheromak to deviate from the Taylor state to one unstable to low-n modes. Resistivity then allows this configuration to undergo magnetic reconnection, letting the

configuration relax back to the Taylor state. The relaxation is often accompanied by a degradation in confinement. Also, the relaxation involves a flux conversion process, important in both spheromaks and RFPs.⁸

In the S-1 experiment, spheromak plasmas are produced by inductive transfer of toroidal and poloidal magnetic flux from a flux core which contains poloidal and toroidal windings.^{9,3} The MHD stability against $n=1$ (tilt or shift) modes is maintained with the help of passive conductors consisting of a set of figure-eight coils⁹ and funnel-shaped conductors as shown in Fig.1.

Radial profiles of poloidal magnetic field B_p and toroidal magnetic field B_t are measured as a function of time with a magnetic probe array inserted into the plasma. By scanning the probe array discharge by discharge, 2-D magnetic field contours in the R-z plane were made to calculate poloidal flux Ψ , toroidal flux Φ , and $q(\Psi)$ in the plasma.^{10,6} Globally coherent modes in the toroidal direction are monitored by a set of 16 external magnetic pick-up coils equally spaced in the toroidal direction at a distance of 60cm from the midplane. The electron temperature T_e and density n_e profiles are measured by a seven channel Thomson scattering system. The measurement points are distributed every 7cm radially on a line which is tilted by 25 degrees from the midplane, as shown in Fig.1.

Under a given operating condition, the relaxation events are somewhat reproducible. Discharges most frequently exhibit only one relaxation event although discharges with two or three events occur occasionally. By adjusting plasma parameters, the first (and only) relaxation event in a discharge was made very reproducible over many discharges, and these are the discharges which are analyzed below.

Figure 2 shows the time evolution of the T_e profile. The radial position in Fig.2 is defined as the distance along the laser beam path from the point where the beam crosses the midplane ($z=0$ cm, $R=47$ cm). After formation of the spheromak ($t=300\mu\text{sec}$), the T_e profile gradually peaks until $360\mu\text{sec}$. Peaking is caused by an increase in the temperature near the center of the plasma where the ohmic heating power is highest. A maximum T_e of $\sim 75\text{eV}$ is reached at $t=360\mu\text{sec}$, when the peaking is most pronounced. This T_e profile is consistent with a resistivity profile higher near the edge of the plasma. Since this data (Fig.2,3) was obtained with magnetic probes inserted into the plasma to measure field profiles at the same time, the maximum T_e was lower ($\sim 30\%$ in this case) than was otherwise obtainable.

Figure 3(a), (b) show the radial profiles of B_p and B_t on the midplane as a function of time. The B_p profile near the magnetic axis ($B_p=0$ or $R \approx 40\text{cm}$) gradually becomes steeper as time increases to $360\mu\text{sec}$. Based on $\nabla \times \vec{B} = \mu_0 \vec{j}$, this steepening implies that j_t is also peaking. The B_t profile also shows a peaking during the same period; this is expected because the B_t profile can be interpreted as representing the j_t profile assuming an approximately constant $\lambda (\equiv j_t/B_t)$ profile. Within the resolution of the T_e measurement, the peaking of j_t and T_e show a very similar time evolution.

Hence, the resistivity profile produced by the strong heating in the core region causes the outer (poloidal) currents to decay faster than the inner (toroidal) currents. This, in turn, produces further preferential heating of the center region (positive feedback), while also causing a further departure from a Taylor state.

The Ψ , Φ , and q_0 are shown in Fig.4(a) - (c). Immediately after spheromak formation ($t \approx 300\mu\text{sec}$), Ψ/Φ is about 2.7 and q on axis, q_0 , is 0.55, which are expected values for the Taylor state. From $300\mu\text{sec}$ to $360\mu\text{sec}$, however, Ψ/Φ increases, indicating the development of a poloidal-flux-rich configuration deviating from the Taylor state. The increase in Ψ/Φ is due to a preferential decay of Φ over Ψ which is emphasized in the plot of $\dot{\Psi}/\Psi - \dot{\Phi}/\Phi$, the difference in decay rates. Only during this peaking period is the preferential decay of Φ over Ψ so dramatic. Also during this peaking period, q_0 is decreasing. When q_0 falls below $1/2$, toroidal mode analysis indicates¹⁰ an $n=2, m=1$ mode suddenly develops and increases in amplitude. The amplitude of the $n=2$ (and all toroidal modes) is much lower early in the peaking phase.

The "peaking phase" is followed by a "broadening phase". From $360\mu\text{sec}$ to $390\mu\text{sec}$, the profiles of B_t (and j_t) are clearly observed to broaden while the slope of B_p near the magnetic axis decreases, again indicating a broadening of the j_t profile. The polarity of $\dot{\Psi}/\Psi - \dot{\Phi}/\Phi$ reverses, indicating a conversion of poloidal flux to toroidal flux ($\dot{\Psi} < 0, \dot{\Phi} > 0$). As this is the only time during decay that $\dot{\Psi}/\Psi - \dot{\Phi}/\Phi$ switches polarity, it is a decisive indicator of flux conversion. The magnetic flux conversion brings the spheromak from the non-Taylor like state with excessive Ψ to a Taylor-like state with the proper balance of Ψ and Φ for a given size and shape configuration. Ψ/Φ decreases to 3.0. Also q_0 returns to 0.55. This relaxation event results in a 20% loss in total magnetic flux.

The T_e profile [Fig.2] broadens as a result of a sudden drop in central temperature. Density profile and density itself change very little during the relaxation. Possible causes of the drop in T_e are a loss of high T_e particles which are replaced by low T_e particles of the edge region and/or a loss of the central ohmic heating power, both of which are caused by the magnetic reconnection process. The former is consistent with the simulation of Sgro et al.¹¹ which suggests that during the relaxation, the hot plasma near the original magnetic axis is expelled while a new axis, which is formed near the edge, brings in cold plasma. In the experiment, roughly 40% of the total thermal energy is lost. On a finer scale, high frequency ($> 50kHz$) magnetic fluctuations are observed to increase by a factor of ~ 3 to 5 during the relaxation, offering another loss channel.

In order to investigate the transport under the highest T_e conditions, the magnetic probe was removed from the plasma. Under these conditions, a maximum peak temperature of over 100eV is obtained [Fig.4(d)] at about $350\mu\text{sec}$, just before the onset of relaxation. The energy confinement time, τ_E , is calculated by comparing the energy input at the central core and the time evolution of the plasma kinetic energy assuming $T_e = T_i$. If $Z_{\text{anomalous}}$ is set between 3 - 5, the maximum value of τ_E is between $50\mu\text{sec}$ and $100\mu\text{sec}$ in the middle of the peaking phase[Fig.4(e)].

The whole process of a relaxation cycle can be schematically represented as in Fig.5. In principle, the cycle described above can be repeated. In fact, multiple relaxation events are sometimes observed in S-1, giving the appearance of "sawtooth"-like phenomena. The behaviour of the decaying spheromak, and the number of relaxation events, depend on the magnetic Reynolds number S and the resistivity profile, based on the simulation by Sgro et al.¹¹ If S is smaller than 500, there is little resistivity gradient between the plasma's center and its edge so that the configuration decays self-similarly and no instability is encountered. For higher $S > 2000$, the time between relaxations is predicted to become comparable to or greater than the configuration lifetime, so one expects to be able to observe only one or two relaxations, if any. For intermediate S , one predicts multiple relaxations; in practice, however, a relaxation reduces S so that, again, only one or two relaxations at most may be expected. In S-1, S becomes as high as 3000.

In summary, a "sawtooth" type relaxation cycle was observed both in the

magnetic configuration and the pressure profile of S-1 spheromak discharges during the decay phase. It was found that the confinement characteristics of the spheromak were significantly affected by the relaxation phenomena, particularly in the broadening phase. In order to make the spheromak more viable to fusion reactor, it is essential to avoid these catastrophic relaxation phenomena by controlling current profile.

We acknowledge useful discussions with T. K. Chu on temperature and MHD properties. This work was supported by the U.S. Department of Energy under Contract No.DE-AC02-76-CH0-3073.

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Figures

FIG. 1. S-1 device

The dotted points on the laser beam path indicate the measuring points of Thomson scattering.

FIG. 2. Time evolution of radial T_e profile, showing peaking prior to a relaxation event.

The radial position is defined by the distance along the laser beam path from the point where the beam crosses the midplane ($z=0\text{cm}, R=47\text{cm}$).

FIG. 3. Radial profiles of (a) poloidal and (b) toroidal magnetic field on the midplane as a function of time

FIG. 4. Time evolution through a relaxation cycle during the decay phase of:

- (a) Ψ/Φ (poloidal flux/toroidal flux)
- (b) $\dot{\Psi}/\Psi - \dot{\Phi}/\Phi =$ Difference in decay rate of Ψ and Φ .
- (c) q value at the magnetic axis
- (d) peak electron temperature T_e
- (e) energy confinement time τ_E

The thermal energies of the electrons and ions are assumed to be equal and $Z_{\text{anomalous}}$ is set to 3. Therefore, if $Z_{\text{anomalous}}$ increases by a factor of n , τ_e roughly decreases by a factor of n .

FIG. 5. Schematic diagram of relaxation cycle

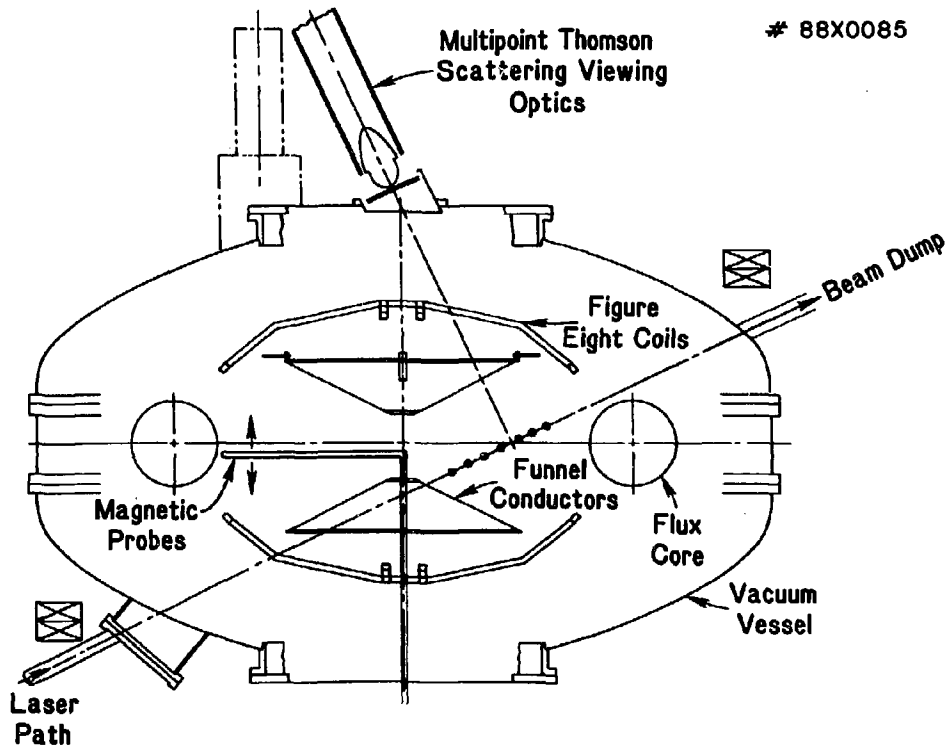


FIG. 1

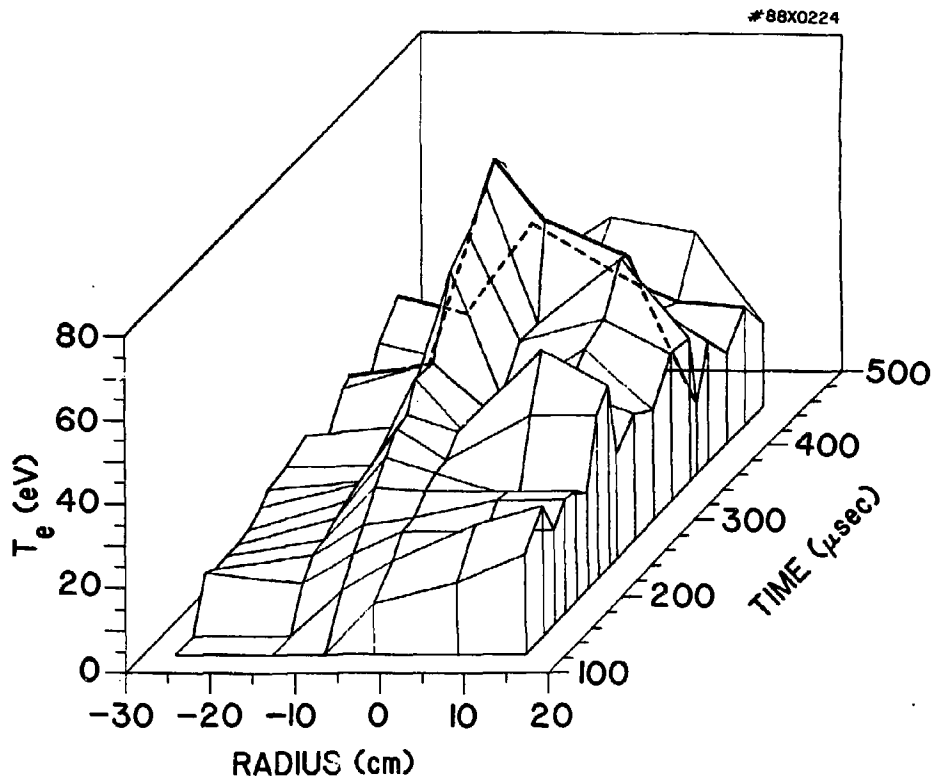


FIG. 2

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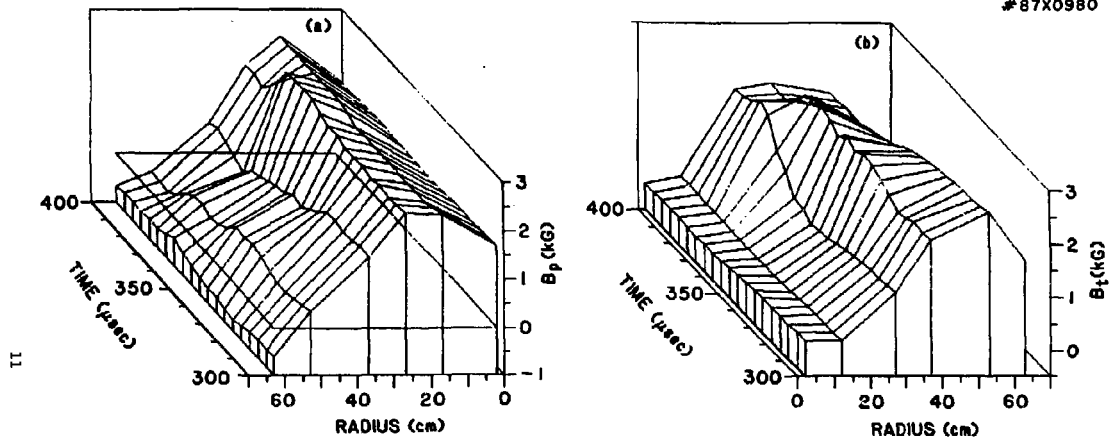


FIG. 3

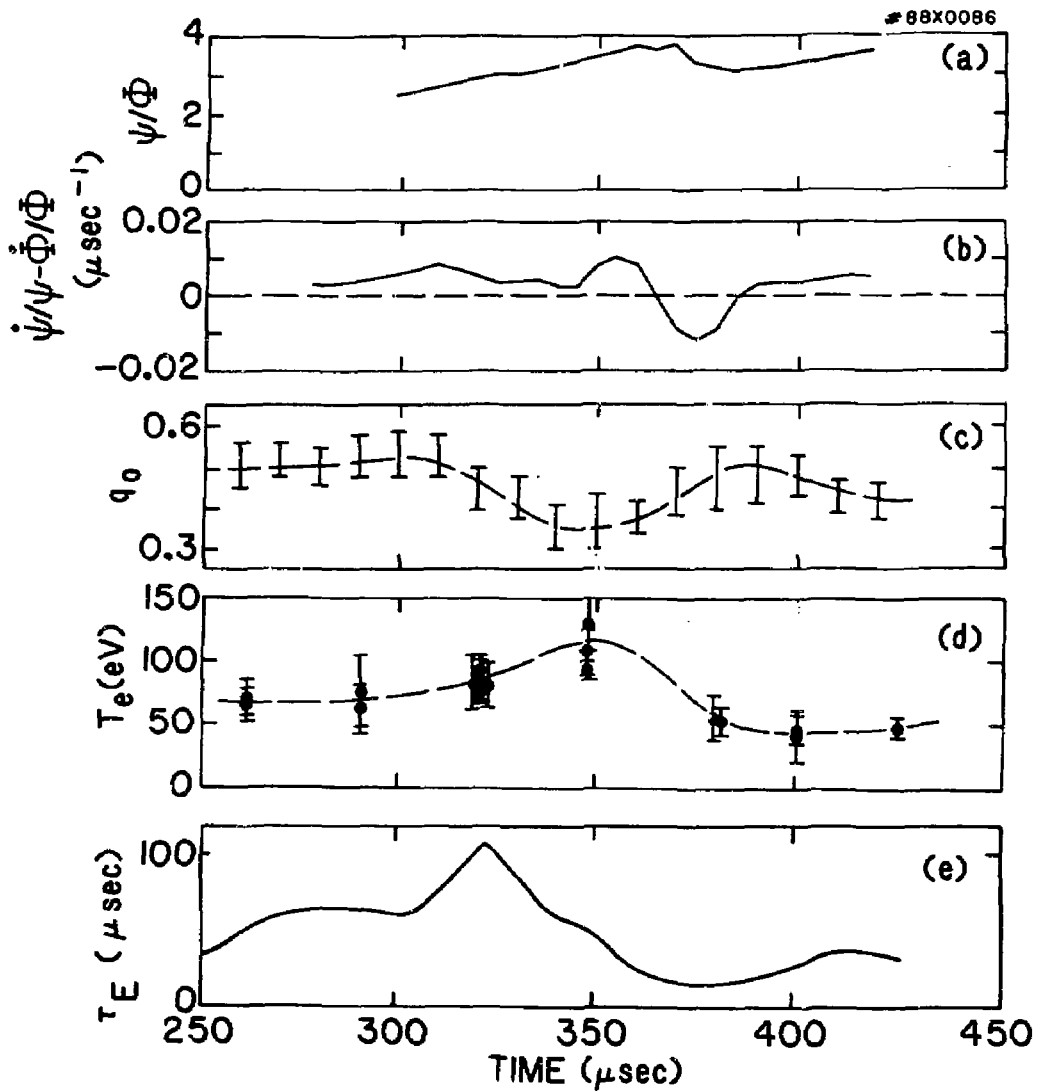


FIG. 4

Relaxation
• $m=1$ $n=2$ Kink Mode

• Flux Conversion from Ψ to Φ
• $T_e \downarrow$ ($\tau_{pf} < \tau_{tf}$)

Taylor State
 $\psi/\Phi=C$ $q > 0.5$

Peaked j Profile
 $\psi/\Phi > C$ $q \lesssim 0.4$

Peaked T_e Profile

Heating

Toroidal Current Peaking

$T_e \uparrow$

$\tau_{pf} > \tau_{tf}$

FIG. 5

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