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CHARACTERIZATION OF COMPOSITE HIGH TEMPERATURE SUPERCONDUCTORS FOR MAGNETIC BEARING APPLICATIONS

by

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Characterization of Composite High Temperature Superconductors for Magnetic Bearing Applications

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Abstract

A study of high temperature superconductor composites for use in magnetic bearings applications is presented. Fabrication and characterization techniques are described. Magnetometry and mechanical force measurements are correlated with a particular emphasis on the role of superconductor particle size. Results are discussed in terms of fundamental limits of Meissner effect levitation.

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Introduction

The phenomen**o**n o**f** Me**i**ssner e**ff**ect i**nd**u**c**e**d** levitation of a permanent m**a**gnet above a high temperature super**c**ondu**c**tor (HTS) at 77 K has evolved from a scientific curiosity **w**ith great pedagogical appeal to having real potenti**a**l fo**r** applications in practical rotating machinery. Simple pr**o**totype bearings have been fabricate**d** whose **r**oto**r**s are capable of spinning in a stable configuration with minimal friction at high rates of speed $\frac{1}{2}$. Detailed mechanical me**a**surements of the forces between permanent magnets and H**T**S mater**i**als have been per**f**ormed **3**,4. Levitation pressures and stiffnesses using "conven**t**ional**"** material such as sintered **¥**- Ba-**C**u-O a**r**e too sm**a**ll to **ha**v**e p**ractical utility. **H**owev**er**, these studies indicate that there is no physical reason that, through the improvement of both the intragranular an**d** intergranular critical current densities (J_c), the pressure and **s**tiffnes**s** cannot achiev**e p**ractical values with Y-Sa-CU-O **2** Recent measurements usin_ melt quen**c**hed Y-Ba-Cu**-**O seem to bear this prediction out o.

Materials requirements **f**or H**T**S materials to be use**d** in bearing applications are somewhat diffe**r**ent from those for other applications su**c**h as **wi**res. **I**t_has been shown using **Y**-Ba-Cu-O **p**ow**d**e**r** suspended **i**n par**aff**in 2, that **l**ev**i**t**a**ti**o**n o**f** a ma**g**net can be achieved without a continuous zero resist**a**nce path across the supercon**d**uctor an**d** that the per**f**ormance o**f** such an insulating matrix HTS composite is **e**qual to that **o**f a cold p**r** ssse**d** ceramic **HT**S m**a**teri**a**l. **T**h**e** m**e**chan**i**cal **pr**ope**r**ties of such composites, how**e**ver, coul**d** fa**r** excee**d** tho**s**e of the brittle **c**erami**c**s**.** Mechanical st**r**ength of the **H**TS material could be crucial i**f** the super**c**onductor is to be us**e**d as th**e** high spee**d** rotor in a bearing assembly **w**here **i**t m**a**y be subject to appre**c**iable centri**f**ugal **s**tress**e**s. Fu_Ithermo**r**e, the fabri**c**ation of the superconducto**r** into l**a**rge an**d c**omp**l**icated slhapes could be facilitated by a machinable **c**omposite matrix **o**r one that c**o**u**l**d be injection molded. Metal **m**atrix composi**t**es **c**ou**l**d be employed in **a**pplications where high the**r**mal conductivity is important. **H**igh th**e**rmal conducti**v**ity could be valuable if the particular application required the super**co**nductor not to be immerse**d** in a cr**y**ogenic liquid but cooled by con**d**uction th**r**ough a cold stage.

This paper **d**escribes a study o**f** Y-Ba-Cu-O composites for magnetic bea**r**ing applications. **P**ro**c**edures for the fabricat**i**on of epoxy matrix and metal matrix composites are described. Me**a**surements o**f** the magnetization versus **f**iel**d** and temperature of these composites are presented and cor**r**elated **w**ith two di**ff**e**r**ent mechanical measurements: st**a**t**i**c force measurements an**d** viDrating beam sti**ff**ne**s**s mea**s**urements. The dependence of levitation p**r**ope**r**ties on the s**i**ze of the HTS grains in the composite **is** a**dd**ressed and **d**i**sc**usse**d** in terms of vortex dynamics of a t**y**pe **II** supercon**d**uctor in the mixed state. Finally, the physical limits of Meissner

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levitation with HTS materials are explored and possible routes to achieve those limits are suggested.

Experimental Details

Samples

All the HTS composites used in this study were based on YBa2Cu3O7-x. Despite the higher critical temperatures of the TI and Bi based superconductors, Y-Ba-Cu-O remains the best
levitator at 77 K due its superior J_C⁴. The magnitude of the induced magnetization in a type II superconductor in the mixed state is directly related to the size of the supercurrents it can support.

Composites were fabricated using powders processed in different ways to produce differing grain sizes. Calcining under reduced oxygen pressure at 800 C of solid state mixed precursors was used to produce fine powder $(x1 \mu)$ single phase YBa2Cu3O7-x 6. Re-annealing this vacuum calcined material under l'atm of flowing O₂ at 920 C promoted some grain growth $(3-5 \mu)$. YBa₂Cu_{307-x} was also synthesized
using precursors co-precipitated out of HNO₃ solution which were sintered, cold pressed and O₂ annealed at 1 atm 920 C. The annealed pellets were reground and yielded material with a broad distribution of grain sizes (\leq 20 μ). YBa₂Cu₃O₇ $x/Ag_{1,0}$ synthesized using a similar HNO₃ and co-precipitation Foute produced material with a more uniform grain size (=20

Paraffin composites were fabricated by mixing superconducting powder into melted wax on a hot plate. resulting mixture was easily moldable into a variety of large shaped objects. This technique produced a composite with approximately a 50% volume fill factor of superconductor which tended to be somewhat non-uniform due to the settling of the powder during solidification.

Epoxy matrix composites were produced by infiltrating pressed pellets of the superconducting powders under vacuum. The pressed pellets made from fully annealed single phase $YBa₂Cu₃O_{7-x}$ powder were immersed in epoxy at 100 C. Inflitration of the epoxy into the pellet was achieved by evacuating the mold containing the pellet and the epoxy. pumping was maintained until all bubbling due to outgassing The ceased. The composite was then cured at 100 C for 10 hours. Void free composites with superconductor volume fraction as high as 70% resulted. An optical micrograph of such a composite made from nitrate co-precipitated YBa₂Cu₃O_{7-X} is shown in Fig. 1. Unlike the wax matrix composites in which the superconducting grains were electrically isolated from each other being completely surrounded by the insulating paraffin, using the vacuum infiltration technique, the macroscopic electrical conduction paths in the pressed

 $\sim 10^{11}$ MeV and $\sim 10^{11}$

pellets were preserved in the epoxy matrix composites.

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Metal matrix composites were formed using finely divided particles of soft metals such as tin and indium. The metal powder was mixed thoroughly with the superconductor powder with a mortar and pestle. The mixture was cold-pressed at 25 ksi . For soft matale. The mixture was cold-pressed at 25 produce some flow at the minimum pressure was sufficient to produce some flow of £he meta**]** around the Y-Ba-Cu-O particles even at **r**oom temperatu**r**e, and at such lo**w** the matals comunical reaction between the $Y=BA-CU-O$ and $(70/30 \text{ by volume})$ composite is choice mich in $\frac{1}{2}$ a $\frac{1}{2}$ -Ba-Cu-O/Sn (70/30 by volume) composite is shown in Fig. 2. A **3** mm thick pellet of such a metal mat**r**ix **co**m**p**osite w**a**s capable of l**e**vitating **a** permanent magnet without bein**g** imme**rs**ed in liquid nitrogen, thermall**y** sunk to a **c**opper **c**ol**d** stage maintained at 77 K. A **p**araffin composite of simil**ar** dimensions did not have the thermal conductiv**i**ty to cool sufficiently to **l**evitate the magnet without **d**i**r**ect immersion in liqui**d** nitrogen.

Detailed magnetometry and force measurements were
performed on the four samples described in Table 1. T per**f**ormed on th**e** fou**r** samples desc**r**ibed in **T**able **i. T**hree increasing HTS grain size, and one cold-pressed Y-Ba-Cu-O/Ag ceramic (123/Ag) were studied. The active volume represented the volume of the sample occupied by HTS material. Magnetometry samples were cut as long thin parallelepipeds $(0.1 \times 0.1 \times 1$ cm) to minimize dependent in parallelepip (0.i x 0.**i** x I cm) to minimize **d**emagnetiz**a**tion effects. **Fo**rce **m**e**a**su**r**eme**n**ts were pe**rfo**rmed on **t**hin squa**r**e plates all approx**i**mately the same size (**I** x **1** x 0.**1**7 cm).

$Measurement$ **Techniques**

Magnetometry was carried out with a Quantum Design SQUID
magnetometer. Magnetization as a function of temperature and magnetometer. Magnetiz**a**tion **a**s a **f**unction o**f** temperatur**e** and field was measure**d**. Minor hysteresis loops with smal**l** field excursions (as small as \approx 1 gauss) were obtained for comparison to analogous force hysteresis loops. The hysteresis in the field setting of the SQUID superconducting solenoid was checked with a non-hysteretic calibration standard so that the measured hysteresis of the HTS samples was confirmed to originate entirely from the **HTS sample** was confirmed to one complete

Static fo**r**ces between **t**he H**T**S materials and permanent repulsive force between the magnet affixed to a pyrex spacer resting on the balance pan and an approaching superconductor indicated by the apparent increase in weight of the magnet. Precise control of the magnet/superconductor separation was achieved using a motorized translation stage. The magnetic a**c**hieve**d** using a moto**r**ized t**r**ans**l**ati**o**n **s**tage**.** The magneti**c** field of the permanent magnet as a function of **d**istance was calibrate**d** with a Hall p**r**obe gaussmeter.

Dynamic stiffness measurements were obtained Using a

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permanent magnet suspended over the superconductor on a
cantilevered beam ... The motion of the beam was monitored with an Optron optical tracking camera. The dynamic stiffness as a function of oscillation amplitude of the magnet/superconductor system was determined by following the motion of the beam after being plucked, correcting for the dynamic response of the beam itself. By altering the positioning of the beam both horizontal and vertical stiffness could be determined. Static force and dynamic stiffness measurements were performed only at 77 K with the HTS material immersed in liquid nitrogen. However, correlations with magnetometry results permitted the prediction of mechanical performance at low temperatures by using low temperature magnetization data.

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Results

Shown in Fig. 3 are representative magnetometry and force results for comp 3, taken at 77 K. Both sets of data were measured while increasing the magnetic field (decreasing the magnet/superconductor separation for the force measurements) following an initial cooldown in zero field. The force data was taken as a function of separation between the HTS composite and a 1.9 cm diameter rare earth permanent magnet which produced a field of 3.4 kgauss at the center of its pole face. Note that in this configuration, for small magnet / superconductor separation, the superconductor experiences a nearly uniform field across its surface pointing perpendicular to the surface. The separation was converted to field strength, so that the data shown is force versus the component of the magnetic field in the levitation

Shown in both the magnetization and force data are minor hysteresis loops at applied fields of 300 and 1000 Gauss obtained by pausing and decreasing the applied field slightly and then returning to the original field. Decreasing the field in the magnetization measurements means lowering the current in the superconducting solenoid, in the force measurement it means increasing the magnet/superconductor separation. The irreversibility associated with vortex pinning is clearly evident in both the force and magnetization results. Previous studies 2,3 have demonstrated that it is the stiffness defired by the slope of the minor force loops $(K = dF/dz)$ which determines the mechanical resonant frequency of the coupled magnet /
superconductor system, $w = (K/m)^{\frac{1}{2}}$.

A clear correlation between the observed field dependences of the levitation forces and magnetization can be demonstrated. Consider a point magnetic dipole arising from a superconductor, μ , oriented along the z axis in a magnetic field H. The potential energy of such a dipole is -#'H. It should be kept in mind that $\mu = \mu(H)$. The levitation force

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> felt b**y** the dipole is **i**n **t**h**e** z d**i**rection and fs given by th**e** negative g**r**adient of the energy,

$$
Y = (\mu + \text{Hd}\mu/\text{dH}) \text{dH}/\text{d}z \qquad (1)
$$

volume of the superconductor $F = \frac{1}{2}V/(4\pi)$, where V is the volume of the supercondu**c**tor, so that the force is given by,

$$
F = \frac{HV}{2\pi} (dH/dz) = 2\mu (dH/dz)
$$
 (2)

For type II superconductors equation (2) is valid for fields
less than Hc1 or even somewhat larger if there is strong flux less than H**cl** or even somewhat larger if **t**he**r**e is st**ro**n**g** flux pinning. **H**o**w**ever, at hi**g**h fi**e**lds**,** with the sup**e**rcon**d**uctor in the mixe**d** state equ**a**tion (**i) a**pplies.

Compa**r**e**d** in Fig. 4 a**r**e lev**i**tation for**c**e data measu**r**e**d** magnetometry data using equation (1). μ (H) and d μ /dH were obtained from SOUID magnetometry (μ). μ (μ) and $d\mu/dH$ were obtained **f**rom SQU**I**D m**a**gnetomet**ry r**esu**l**ts **a**n**d** d**H**/**d**z **fr**om measured m**a**gneti**c f**ie**ld v**ersus **d**istance **d**a**t**a for th**e** was assumed to produce a field in the **field in the formation**. The magnetic was assumed to produce a fie**ld** in the z **d**i**r**e**c**tion, uni**f**or**m** in the xy plane and **de**ma**g**neti**z**ation effe**c**ts on both the Considering these assumptions the agreement between the **C**onsidering these assumptions the agre**e**ment between the measured for**c**e data and the data derive**d** from the magn**e**tometry resu**l**ts is s**tr**ikin**g**.

Levitation Pressure

Fig. 5 displays the 77 K zero field cooled levitation
force data for the four samples listed in Table 1. Fig. 6
shows the consequenting \overline{z} shows the corresponding 77 \bar{k} magnetization data. The magnetization data in Fig. 6 is normalized to the actual volume of superconductor in each sample (see Table 1). clearly, as predicted by equations (1) and (2), for a given applied field the magnitude of the levitation force increase of the field induced magnetically future increase with the size of the fiel**d** in**d**u**c**e**d** magnetization.

A**l**so notewo**r**th**y** in **F**igs. 5 an**d** 6 is that at **l**ow fields, b**ot**h the m**a**gn**e**t**i**zation and levitat**i**on force scale with the **HTS** c**r**ystallite size. T**h**is dep**e**ndence is **a**tt**r**ibutabl**e** t**o** penetration d**e**pt**h** effects. Sma**l**l par**t**i**cl**e composit**es (**uuch as c**o**mp 2), with grain si**zes** o**f** the o**r**der a **f**e**w** times th**e** London penetration depth \approx 2000 Å at 77 K for $YBa_2Cu_3O_X$ ⁹,10 will experience field penetration into an appreciable
fraction of each superconducting grain and consequently yield a drastically smaller Meissner moment than larger grain composites, even at fields less than I mail larger grain **c**omp**o**site**s**, even at fie**lds l**es**s** tha**n** H**cl**" **T**his g**r**ain size the observed magnetization and lowithing which produc intragranular even though intergranular conduction r exist in the epoxy matrix composition when the paths existence in the epoxy matrix **c**omposites. The existence of large

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size **s**creening cu**rr**ent loop**s** is **u**n**d**ou**b**te**d**ly li**m**ite**d** b**y** low critical **c**u**r**rent **w**eak link**s a**cro**s**s **g**r**a**in boundaries. The **l**arg**e**st gra**i**n sample (**1**2**3**/**A**g) had large enough grains that **t**h**e** penetration repre**s**ented a negligibly small fraction o**f** the volume **o**f each gr**a**in so that at low **f**iel**d**s the magnetization approa**c**hed i00 % flux exclusi**o**n, M = [-1/4_] H.

Interestingly, the m**a**gnetiza**t**ion of **a**nd the le**v**itati**o**n forces from the small grain samples are comparable to that of
the large grain (123/Ag) sample at higher fields. In fact, the largest levitation force at fields in excess 300 gauss **th**e l**ar**ge**s**t le**vitation f**o**rce a**t **fie**l**d**s **in** e**xce**ss **3**00 g**au**ss **w**e**r**e **gen**e**ra**te**d** b**y com**p **2, wh**i**ch h**a**d s**ig**ni**f**i**ca**n**tl**y** smal**l**er **g**ra**ins** t**han** e**ith**e**r c**omp **3** o**r** 1**23**/**A**g**. lt** t**h**e**r**e**f**o**r**e **can b**e which they levitate magnets. At large heights, the magnetic **which** t**h**ey l**ev**it**at**e **m**a**gn**et**s. At** l**a**rge **heigh**ts**,** t**h**e ma**gn**e**tic** f**i**el**d**s a**re** qu**it**e l**o**w an**d th**e **lar**ger **gra**i**n** sa**m**p**les** of **t**_e gro**u**p **st**u**di**e**d woul**d o**ut-**pe**r**fo**r**m **the s**m**a**ller gr**ain**e**d s**ample**.** Ho**w**e**v**er**,** a**t lar**ger mor**e t**e**chn**olo**gi**c**a**ll**y** r**e**l**evant fi**e**ld**s o**f** a few **kgauss,** su**ch** as is eas**i**l**y** p**roduc**ed **clo**se **t**o **a p**e**rman**e**n**t mag**ne**t**,** t**h**e a**dvan**t**ag**e o**f** t**he** l**ar**ge g**ra**i**n**e**d** ma**teria**l **in** t**e**z_**n**s o**f** le**vita**t**i**o**n pr**essure **di**sa**pp**e**ar**s**.**

The or**i**g**in** of **the l**ar**g**e**r** mag**n**et**i**z**ati**o**n** o**f** the small g**r**a**in c**omposites at **hig**h fiel**d**s ma**y** l**l**e **in** s**u**rf**ac**e **barri**e**r**s to **th**e ent**ry** o**f** vo**rtice**s**. V**o**rtice**s w**il**l **b**e **rep**elle**d by** ot**h**e**r v**or**tic**e**s a**s we**ll** as t**h**e m**a**g**n**e**tic** fiel**d in** the **L**on**d**o**n** penetr**at**io**n** la**yer** 11**. In** small gra**ins** w**h**ere i**ndiv**idu**a**l v**o**rtices c**an**not iso**late** th**e**mse**l**ves **fr**um ei**ther** of these **i**n**f**luences, i**t** may be ene**r**geti**c**ally f**a**vorab**l**e for **f**lux to be inh**i**bited f**r**om pene**tra**tion **i**nto **th**e gr**ains** at fie**l**ds well p**a**st **H**cl. Without **fl**ux penetration the Meissner moment and hence the levitation fo**rc**e continues to incr**e**ase wi**t**h fiel**d.**

In a**dd**ition to the e**ff**e**c**ts o**f t**he Lond**o**n penetration volume and surfa**c**e barr**i**ers to flux ent**r**y, ther**e** is a t**h**i**r**d way in w**h**i**ch** _**r**ain size **c**o**u**l**d e**ffe**c**t magnet**i**zation **i**n a composite H**TS** m**a**terial v**ia b**u**l**k **p**inning o**f** vorti**c**es. The bulk p**i**nnin**g** o**f** vorti**c**es **c**ontrol**s** t_e intragra/_ular **J**c, and its effe**c**t upon magnetization can tr**e**at**ed** in terms of a **cr**itlcal state m**od**e**l**. Consi**d**e**r a c**ompo**s**ite f**o**rmed fi_ an array of cylindrical particles, radius R, height L, with intergranular J_C of zero and an external field applied intergranula**r J**c o**f** zero an**d** an ext**er**nal _iel**d** a**pp**lied paral**l**el to the axis 9_ the **c**y**l**in**d**e**rs**. Fo**l**lo**w**ing t**h**e Bean critical state m**o**d**e**l xz, assu**m**ing a field independent Je, the maxlmum magnetization o**f** such a sample **w**lll be Dro**duc**e**d**-when t**h**e _pplled fleld **r**eaches **a v**alue **H'**.(For a **s**l b of thickn D , $H'' = \pi J_c D/5$ with H^* in gauss and J_c in A/cm^2 . Further increases in field will produce no increases in magnetization. The superconductor is said to be in the magnetization. The supe**rc**on**d**uctor i**s** sa**id** to be in the "critical **s**tate" in **w**hic**h** sc**r**eening supe**r**current**s c**ir**c**ulate a**r**oun**d** the gra**i**ns, **e**veryw**h**ere **wi**th a densit**y** J**c**" Th**e** magnetic moment of each cy**l**ind**r**i**c**al grain in the **c**r**i**ti**c**al state is there**f**ore,

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$$
\mu_{\text{max}} = \int_0^R \pi r^2 J_C \text{ Ldr} = \pi J_C \text{LR}^3 / 3 \qquad (3)
$$

To get the magnetization of such a composite, equation [3] is divided by the volume of the cylindrical grains, πR^2L .

$$
Mmax = JCR/3
$$
 (4)

Therefore, to maximize the induced magnetization and thereby the levitation pressure in a composite superconductor, it is necessary to maximize the product J_CR. This effect of the dependence of magnetization on the size of the supercurrent loops has been demonstrated by scribing high quality thin films 13. Among the four samples studied, there was clearly a trade-off among penetration volume, current loop size, and surface barrier effects best met by grains of intermediate $size (comp 1).$

The 77 K magnetization data in Fig. 6 is instructive in that the deficiencies of the sintered Y-Ba-Cu-O used in this study are apparent and the achievable limits clearly delineated. The maximum possible diamagnetic response of a superconductor is 100 % flux exclusion shown in Fig. 6 by the line labelled $-M = (1/4\pi)H$. At 77 K and practical fields of 3000 gauss, these materials produced a Meissner moment of only a few percent of complete flux exclusion. With stronger flux pinning or surface barriers, vortices could be inhibited from entering the superconductor until much higher fields, increasing the magnetization and the levitation pressures produced. The sintered Y-Ba-Cu-O used in this work produce levitation pressures of \approx 0.2 psi on 3 kgauss permanent magnets at 77 K. Clearly, there is no fundamental physical reason why pressures of 10 psi are not achievable and with higher magnetic fields with enhanced field gradients perhaps significantly higher pressures may be reached.

While the operation of a HTS superconducting bearing at 77 K or higher presents clear engineering and cost advantages through the use of liquid nitrogen as the cryogen, there may be performance advantages to be gained at lower temperatures. In certain potential applications, such as turbomachinery for liquid hydrogen fueled rocket engines, working environments with temperatures of 20 K already exist. The correlation between the magnetometry and force data shown in Figs. 4-6 leads to confidence that low temperature magnetometry measurements may be used to predict mechanical force behavior at low temperatures where force measurements are not straightforward.

Shown in Fig. 7 are magnetization versus field data (zero field cooled) at 20 K for the four test samples characterized in Figs. 4-6. It is notable that for each material, the peak in the magnetization has moved to higher

field, and at **3000** gauss, **ea**ch is t**e**n times l**a**rg**e**r than its levitation pressures also a f are \sim $\frac{1}{2}$ $\frac{1}{2}$ levitation preserved at 27 Y 1900 ten larger than what was measured at 77 K, levitation pressures at 20 K of 2-**3** temperature increased be influencing this low temperature improvement. There is an decreas**e** in the London low field magnetization of the small mattives even the large low field magnetization of the small particle sample (co**m**p 2). Depinning of vortices and the overcoming of surface
barriers can be a thermally activated process so that increased magnetization would be expected for each sample. Nevertheless, at 3000 gauss and 20 K, there is still room for another factor of five innected by there is still room for **^a**not**h**e**^r ^f**a**c**t**or** of **^f**ive improvement **^b**e**fo**r^e ^t**he I00** % Me**i**ssner effect limit is rea**c**hed**.**

Vertical Ma_get_ Stif**fness**

The stiffness is an important design parameter in any bearing system. It may be defined for a given direction r , by $K_T = dF_T/dr$ which quantifies the restoring force experienced by a levitated magnet when disturbed from its equilibrium by a levltated magnet w**h**en **d**istu**r**b**e**d **fr**om its equi**l**ib**ri**um position. **K a**lso **d**etermines the natural frequ**e**nc**i**es of the vibrationa**l** modes of levitated **c**ompon**e**nts. **I**n **d**esigns of high speed **ro**tating m**a**chine**r**y prec**i**sely def**i**ne**d** equilibr**i**um positions, **cr**i**t**ical fr**eq**uencies, and contr**o**l of the n**o**rmal modes a**r**e c**r**ucial as is th**e** ability to withstand tra**n**sient per**t**urbations.

Of primary imp**or**tanc**e** is the v **r**tz**c**.al sti**f**fness, K z **=** dF/**d**z, the stif**f**ness in the levitation **d**i**r**e**c**tion. Of primary importance is the vertical stiffness, $K_z =$ Differentiation of equation (1) predicts that K_z will depend both on the magnitude of the induced magnetic moment, μ , and its first two derivatives with respect to field moment, μ , and _s **f**irst t**w**o derivatives with _espect to **f**ield d_/dH a**n**d $d^2\mu/dH^2$.

$$
K = \mu d^{2}H/dz^{2} + d\mu/dH [H d^{2}H/dz^{2} + 2 (dH/dz)^{2}]
$$

+ $d^{2}\mu/dH^{2} [H (dH/dz)^{2}]$ [5]

With the hysteretic behavior of type II superconductors in the mixed state, it is not immediately obvious which magnetization slope, $d\mu/dH$, is involved, that of the major magnetization curve or the minor loop in Fig. 3. Previous static force and vibration studies of permanent magnet / HTS static **fo**r**c**e a**nd** vibra**t**i**o**n s**t**u**die**s **of** p**e**rmanent magnet / HTS system as well as the single slope of the minor the dynamic response of the count in Fig. 3) which determin the dynamic **r**_pon_e of the coupled mechanical system.

Shown in Pig. 8 are 77 K vertical stiffness data for three of the test samples as a function of vibration
amplitude using the plucked beam technique. The magnet/superconductor separation was chosen so that the field at the surface of the superconductor was approximately 1000 gauss. The smallest crain composite was approximately 1000 gauss. The smallest grain composite (comp 2) yielded a

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stiffness too small to separate **f**rom that of the bare beam. In Fig. 9 are plotted the slopes (dM/dH) of the magnetization loops (like those of Fig. 3) as a function of the amplitude of the excursion from H O **=** I000 gauss. Analogous behavior to the mechani**c**al stiffness data in Fig. 8 is evident. Therefore, **f**o**r** the experimental configuration used to obtain the data of Fig. 8 , the second te**r**m **i**n equation (6), that proportional to $d\mu/dH$ is apparently quite important. For H_o = I00**0** gauss an**d** low v**i**b**r**a**t**i**on a**mp**l**itudes (fie**ld e**x**c**u**r**sions)- u the stiffes**t** sa**m**ple was ¥**123**/Ag whi**c**h was not the sam**p**le yielding the la**r**gest ma**g**netizat**i**on an**d** levit**a**tion pressure (**c**omp **I**). The previously observe**d** empi**r**i**c**al rule t**h**at sti**f**fness sc**a**les with levitation p**r**essu**r**e is not universally vali**d**.

The slop**e**s of the minor magnetiza**t**ion hyste**r**esis loo**p**s (Fig. 9), whi**c**h strongly influenc**e** the mechani**c**al stiffness, are also clearly correlated with the low field Meissner
fractions (Fig. 6) for the samples studied. The samples with fracti**o**ns (Fig. 6) for **t**he samples stu**d**ie**d**. **T**he **s**amples with th**e** largest low **f**ie**l**d flux ex**c**lusi**o**n als**o** pro**d**uce minor **l**oops with **t**he largest slopes, at l**e**as**t f**or small ex**c**ursions 6**H**. **T**his paralle**l** a**r**gues that the vib**r**atio**n**al **be**havi**or** in the ver**ti**cal **d**i**r**e**c**t**i**on is l**arg**ely **d**ue to the **dy**nam**ic r**esponse of t!lat part of the supercondu**c**to**r**,s m**a**gnetiza**t**ion arising **f**rom the su**r**fa**c**e screening cu**rr**en**t**s. Due to Lon**d**on pene**t**r**a**tion depth effe**c**ts, samples with the lar**ge**st grains have the largest total screening currents flowing and consequently are mechanzc**a**lly _az_es**n**. As their amplitudes in**c**rea**s**e, however, the m**i**no**r** loops become mo**r**e hyste**r**et**i**c indicating the onset of vortex motion. Such a model also ex**p**lains the more drastic decrease in both the mech**an**ical (F**i**g. 8) **a**nd magneti**c** s**t**iffness (Yig. 9) with amplitu**d**e for the largest grain sample (**!**23/Ag). A**s** a**l**ready suggested, su**c**h l**a**rge p**a**rtic**l**es can accommodate la**r**ger vo**r**tex **d**ensities **d**ue to minimized inter-vortex an**d** sur**f**ace barrie**r** repulsive effec**t**s an**d** so a**r**e most sus**c**eptible to flux motion. However, vortex **d**ynami**c**s must play some role **i**n the vertical s**t**i**f**fness even at low vib**r**ation amplitudes. Fo**r** the l**a**rgest grain samples at low amplitudes, at 77 K and $H_0 = 1000$ gauss, dM/dH does not achieve the pure Meissne**r** S**c**re**e**ning cu**r**rent value o**f i**/4_**.**

As with the levita**t**ion p**r**essure results, comparison between the magnetic an**d** mechani**c**al stiffness **r**esults can provide **i**nsight as to the physical limits to w**h**ic**h** the slope dM/dH at which the screening currents can respond is the complete Meissner effect limit $1/(4\pi) = 0.080$. As may be $\begin{bmatrix} 1 & 0 & 0 \\ 0 & 0 & 0 \end{bmatrix}$ **complex** $\begin{bmatrix} 1 & 0 & 0 \\ 0 & 0 & 0 \end{bmatrix}$ **i** $\begin{bmatrix} 1 & 0 & 0 \\ 0 & 0 & 0 \end{bmatrix}$ **complex** $\begin{bmatrix} 1 & 0 & 0 \\ 0 & 0 & 0 \end{bmatrix}$ **complex** $\begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \end{bmatrix}$ **complex** $\begin{bmatrix} 0 & 0 & 0 \\$ s_{max} and s_{max} $\text{max}_{i=1}$ $\text{max$ the maximum magnetic stiffness measure**d** was 0.025 **f**or the **1**2**3**/Ag sample. As with the levitation pressure **t**hese values improve a**t** 20 K, again presumably due to improve**d** vortex pi**n**ning. **T**hese results a**r**e shown in Fig**.** i0. At low temperatures the theoretical limit of 0.08 is being approa**c**hed by the 123/Ag sample.

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 \Rightarrow

 $\alpha = 0$ and
 $\beta = 0$

 $\lim_{\Delta t \to 0} \frac{1}{\| \Delta t \|_{\infty} + \|\Delta t \|_{\infty}} = \lim_{\Delta t \to 0} \frac{1}{\| \Delta t \|_{\infty}} = \lim_{\Delta t \to 0} \lim_{\Delta t \to 0$

Horizontal Magnetic Stiffness

If the forces between a magnet and a type I superconductor with a horizontal flat surface are modelled in terms of those between a magnet and an image magnet in the superconductor, clearly there will be only forces in the vertical direction. Neglecting edge effects, there will be no horizontal restoring forces or stiffness. The lack of a horizontal restoring force prompted early experimenters to employ a bowl shaped superconductor to achieve stable levitation¹⁴. For a type II superconductor in the mixed state, however, horizontal motion of the suspended magnet implies the movement of vortices within the superconductor, out of some regions, into others. Therefore, if internal vort ax pinning is appreciable, there will be barriers
opposing horizontal deflection ¹⁵. The image of the suspended magnet in the superconductor may be distorted in the direction of the horizontal motion resulting in magnetic forces on the suspended magnet opposing such motion. The dissipation associated with the irreversibility of vortex motion will manifest itself as a viscous drag 16. Such vortex drag effects may be easily demonstrated by spinning a levitated magnet above a superconductor. If the magnet's field is cylindrically symmetric about its axis of rotation, it will spin freely. If it is even slightly asymmetric magnetically about its axis of rotation, its rotational energy will rapidly dissipate.

Horizontal stiffness measurements were performed for each of the samples in Table 1 using the plucked beam technique with the displacement of the beam, and the magnet attached to it, parallel to the superconductor surface. The pole face of the magnet employed was comparable in dimension to the HTS samples. Therefore edge effects may not have been negligible. Nevertheless, the results are qualitatively
similar to those obtained with a maynet substantially smaller
in area than the superconductor 8, The dependence of the horizontal stiffness on amplitude is shown in Fig. 11. A comparison of Figs. 8 and 11 reveals that for each sample, for the same magnet/superconductor separation and vibration amplitude, the vertical stiffness was a factor of three The lack of a Meissner screening larger than the horizontal. current contribution to the horizontal stiffness, present in the vertical case, accounts for the smaller horizontal mechanical stiffness.

The sample dependence of the horizontal stiffness behavior shown in Fig. 11 is similar to that of the vertical The vertical stiffness in Fig. 8, but for different reasons. stiffness dependence on grain size was explicable by a London penetration depth argument, the larger grains containing more integrated screening current and consequently producing more of a vertical spring constant. The greater horizontal

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stiffness of the large grain samples may be attributable to the greater density of pinned vortices in the large grains. t**he** g**r**eat**er d**e**n**s**it**y **o**f **p**i**n • voru**l**c**e**s** i**n** t**h**e **lar**g**e grains. Du**e **t**o t**heir** s**urface ba**rr**ier**s, **f**e**w v**o**rtices** c**an en**t**er t**he _ **s**mall **grain** s**am**pl**e**s **which c**o**n**sequ**e**ntl**y m**o**re c**lo**s**ely **appr**o**ximate t**h**e rever**s**ib**l**e behavi**o**r** o**f** a **type I** s**u**p**er**co**nduc**tor **which pr**o**d**u**c**es **no h**o**rizontal su**if**fnes**s**.**

The horizo**ntal** s**tiffne**ss resul**ts provide fur**the**r** i**nsi**g**ht** in**t**o **t**he **m**ag**n**e**t**ic be**h**av**i**o**r o**f **H**TS **ma**terials whi**c**h !_a**d**s to the observe**d** me**c**hanical **b**ehavior of the coupl**ed** magn**e**t/HTS system. Thoug**h**, from a p**r**act**i**cal desi**g**n point o**f** view, the horizontal sti**ff**ness is of second**a**r**y** imp**o**rtan**c**e. Any practic**al s**uper**c**on**d**u**c**to**r** bearing design wou**ld** not **e**mploy flat **p**lana**r** be**a**ri**ng** s**u**rfaces but **r**a**t**he**r** suit**a**bl**y** shape**d** super**c**onducting components so that t**h**e h**o**rizonta**l s**tif**f**ness a**c**tually r**e**sults **f**rom a _¢ertical,, stiffness turne_ sideways. An example of su**c**h a shape w**o**ul**d** be **a U** or a bow**l sh**ape.

Conclusions

Several im**po**r**tant C**oncl**us**io**n**s **can** b**e** d**r**a**wn** f**r**o**m** t**h**e **ex**par**i**mental **re**s**ult**s p**r**es**ent**e**d in the** pr**ecedin**g s**ec**t**ion. Th**e p**r**i**nc**ipal **c**o**nclu**si**o**n to be **d**ra**wn** a**ddre**sse**s** the p**r**a**ct**ica**l** u**t**ility of **HT**S compo**s**ites **i**n ma**g**netic l**e**v**i**tat**i**on applicati**o**ns. **HT**S **c**om**p**osites, **b**oth insul**a**ting and metal matrix, rep**r**esent a **re**alisti**c** alte**r**native to **ce**ramic **HT**S materials fo**r** magneti**c l**evitation applications at tempe**r**atures as **h**i**g**h as **7**7 **K**. T**h**e**y c**an **s**a**t**is**fy** req%li**r**ements of mech**a**ni**c**al st**r**ength, mach**i**nabi**l**it**y**, an**d** thermal cond**u**ctiv**i**ty unique to rota**t**ing ma**c**hin**e**ry appli**c**ations with**o**ut sacri**f**icin**g** loa**d** bearin**g o**r stiffness capabiliti**e**s.

The results, ho**w**ever, sho**w** that the**r**e i**s** su**b**stantial room for improvement o**f** the **s**upercondu**c**ting properties of the HTS material, speci**f**ically in criti**c**al currents, if the **f**ull ;**o**tentia**l** of HT**S** Meissner e**ffec**t **l**evit**a**tion is **to** be **r**ealized. Magnetometry measu**r**ements **c**oup**l**e**d** with _echanical force and stiffness measurements clearly delineate these
limits. Levitation pressures in excess of 10 psi are limits. **L**evitation p**r**essures in excess of **1**0ps**l** are achievable using **3** kgauss permanent ma**g**nets if the crystallite size and flux pinning can be improved. Recent breakthroughs in HTS materials synthesis involving melt breakthroughs in HTS materials synthes**i**s involving melt properties 17-20 demonstrate that such impressive magnetization ^p**r**ope**r**ties ^uem**o**ns**t**rat**^e** that suc^h improvements are possible.

. The 77 **K** stif**f**nes**s d**a**t**a **i**n **F**ig. **8** le**v**e**l** ou**t** at about **1** lb/a**n**, for a **1 c**m _ bear**ing** su**rf**a**ce** a**r**ea, t**o** small **t**o b**e** o**f** any p**r**actical **v**alue. How**e**v**e**r, substan**t**ial imp**ro**vement**s** in complete Meissner effect: $\bar{\mu}$, $d\mu/dH$ $d\mu/dH$ in equation (5). Furthermore, the stiffness scales with the area of the bearing surface making possible much stiffer bearings if machinery designs could be adjusted to trient bearings if **m**achinery designs could be adjusted to tolerate la**r**ger

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be**arin**g s**urfa**ce **ar**e**a**s.

One import**a**nt fac**t**o**r** i**n** co**n**trol**lin**g t**h**e s**up**e**rc**o**n**d**u**c**tin**g **p**ro**per**t**i**es o**f** a**n HTS c**ompos**it**e **is th**e **HTS cry**s**t**all**i**t**e size. C**o**nflicting ef**f**ect**s o**f p**arti**cl**e **s**i**z**e **w**e**re identified by sc**rutiniz**i**ng **m**ag**n**e**to**m**e**t**ry r**es**u**lt**s. Sm**all **pa**r**tic**le **co**mp**osi**tes **h**a**d th**e**ir n**e**t** mag**ne**t**ization and r**es**u**lt**a**nt lev**i**t**a**t**i**o**n** p**r**ess**ure** l**i**m**it**ed b**y L**o**ndon p**ene**t**r**ation** o**f** e**xt**er**na**ll**y appli**e**d fi**e**ld**s**,** yet at **high f**iel**ds pr**Q**duc**e**d** m**a**g**n**e**tiza**t**ion**s as **g**rea**t** o**r** g**r**ea**t**e_ t**h**a**n t**he **la**rge**r** pa**r**t**icl**e **co**mp**o**s**ite**s **b**e**c**a**use o**f s **composites benefitted from the larger size of the screening** c**o**mpos**i**t**e**s **b**e**n**ef**it**t**ed fr**om t**h**e l**ar**ge**r** s**ize** o**f** t**h**e **screening cur**re**nt** l**oo**p**s** p**roducing larger** m**a**g**n**et**iza**t**ion** a**n**d **th**e la**r**ge**r net** scree**nin**_ **curr**e**nts pr**o**ducing a greater ve**rt**ica**l **s**t**if**f**n**ess**, bu**t s**uffered from** a **gr**e**ater** s**u**s**c**ep**t**i**bi**l**ity to** _J**u**x **p**e**n**e**tr**at**ion and** vo**r**t**e**x mo**ve**m**en**t **which** l**imited** t**h**e **high fi**e**ld** l**evita**t**ion pr**ess**ure**s **a**n**d** l**o**w**e**r_d t**h**e m**agn**e**tic stiffness** for **larg**e amp**l**itu**d**e **vi**br**at**io**ns. O**p**ti**mi**zed** compos**i**tes **will** t**h**ere**f**or**e** rep**r**ese**n**t **a co**mp**r**om**i**se amo**n**g **s**ever**al co**mp**e**t**ing fa**c**tor**s**. Alth**oug**h, un**a**mb**i**guously**, **im**p**r**o**v**e**d perf**o**rm**a**nc**_ **wi**l**l b**e pr**o**du**c**e**d by s**tr**o**ng**ly pinned, hig**h **Jc** m**a**ter**i**al**.**

Much re**m**a**ins to be ac**com**p**l**i**s**h**e**d in i**m**pr**o**ving HTS** magnetic **b**ea**r**ing pe**r**f**or**m**anc**e b**y impr**o**v**e**ment of HTS** s**u**per**co**n**duc**t**in**g p**ro**p**e**rt**i**es**. Even fur**the**r po**t**en**t**ia**l p**e**r**for**man**ce gain**s **may** be e**ffec**te**d by i**n**nov**at**iv**e **d**es**i**gn **a**ppr**o**a**che**s. **Eq**uat**i**o**ns (i)] a**n**d (5)** s**ugg**e**s**t **d**esign **c**onsi**d**e**ra**ti**o**ns _**hich a**s **yet hav**e **no**t **b**ee**n ser**i**ou**sly be produced by maximizing not only H, but dH/dz and d^2H/dz^2 as well. Thus improved performance will be brought about by **a**s **wel**l**. Thu**s i**mp**rove**d p**e**r**f**orm**an**c**e **will** be **br**o**ught ab**o**ut by** appr**o**pri**at**e**l**y shaping the supe**rco**n**d**u**c**tor and **t**h**e** mag**n**et**ic** field of the magnet.

All **p**ublishe**d** work to date ha**s** employ**ed** permanent magnets. Such magnets lim**i**t the ope**r**ational fi**eld**s to a few kgauss. Clearly highe**r** magn**e**tic **f**ields w**o**uld pro**d**u**c**e enhance**d** magnetization, **le**vitation pressure, magneti**c** s**t**i**ff**ness, pa**r**ti**c**ularly if the **s**upe**rc**onducting p**r**oper**t**i**e**s o**f** that attainable using permanent magnets can be created using superconducting solenoids. A potential novel approach for senerating high fields could be the use of trapped flux HTS magnetic "replicas". Actual trapped flux HTS magnets have already been produced with captured fields exceeding 1 kgauss²¹. Ultimately, the practicality of HTS magnetic kgauss 2**1**. Ultimately, the practicallty o**f H**TS magn**e**tic ^b**ear**ings **ce**rtainly wi**l**^l **^h**lng^e **on** su**ch** ⁿ**o**ve**^l** eng**i**nee**ri**ng approaches.

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TABLE \mathbf{r}

 \mathbf{A}

الشارات ستورده الأرسل وا

Test Samples

AS REC^ID
500X

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OPTICAL METALLOGRAPHY LABORATORY

MAGNETIZATION [GAUSS]

FIG. 3

ZSBZ ZZZ E0Z POTHE ..T. DAIN PS:PT 06. TE SNU

BS\SS.9

 $\hat{\omega}$

 $\frac{1}{2}$

HUG 31 .20 14:22 NIKC ..T. BFDG S03 1S1 182S

 $\frac{\omega}{\tilde{\mu}}$

EV 2

 $\mathcal{M}^{(1)}$ and \mathcal{M}

 $\ddot{}$

n , aoz do

Fig. 10

82/82.9

2887 7ST 68S PUS 14:56 UTRC "L" BLDG **IE SUA** سم
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 $\label{eq:2.1} \frac{1}{\sqrt{2}}\int_{\mathbb{R}^3}\frac{1}{\sqrt{2}}\left(\frac{1}{\sqrt{2}}\int_{\mathbb{R}^3}\frac{1}{\sqrt{2}}\left(\frac{1}{\sqrt{2}}\int_{\mathbb{R}^3}\frac{1}{\sqrt{2}}\left(\frac{1}{\sqrt{2}}\int_{\mathbb{R}^3}\frac{1}{\sqrt{2}}\right)\frac{1}{\sqrt{2}}\right)\frac{1}{\sqrt{2}}\right) \,d\mathcal{H}^3\left(\frac{1}{\sqrt{2}}\int_{\mathbb{R}^3}\frac{1}{\sqrt{2}}\int_{\mathbb{R}^$ $\label{eq:2.1} \mathcal{L}(\mathcal{A}) = \mathcal{L}(\mathcal{A}) \mathcal{L}(\mathcal{A})$ $\label{eq:2.1} \frac{1}{\sqrt{2}}\sum_{i=1}^n\frac{1}{\sqrt{2}}\sum_{i=1}^n\frac{1}{\sqrt{2}}\sum_{i=1}^n\frac{1}{\sqrt{2}}\sum_{i=1}^n\frac{1}{\sqrt{2}}\sum_{i=1}^n\frac{1}{\sqrt{2}}\sum_{i=1}^n\frac{1}{\sqrt{2}}\sum_{i=1}^n\frac{1}{\sqrt{2}}\sum_{i=1}^n\frac{1}{\sqrt{2}}\sum_{i=1}^n\frac{1}{\sqrt{2}}\sum_{i=1}^n\frac{1}{\sqrt{2}}\sum_{i=1}^n\frac$ $\label{eq:2.1} \frac{1}{\sqrt{2}}\sum_{i=1}^n\frac{1}{\sqrt{2}}\sum_{i=1}^n\frac{1}{\sqrt{2}}\sum_{i=1}^n\frac{1}{\sqrt{2}}\sum_{i=1}^n\frac{1}{\sqrt{2}}\sum_{i=1}^n\frac{1}{\sqrt{2}}\sum_{i=1}^n\frac{1}{\sqrt{2}}\sum_{i=1}^n\frac{1}{\sqrt{2}}\sum_{i=1}^n\frac{1}{\sqrt{2}}\sum_{i=1}^n\frac{1}{\sqrt{2}}\sum_{i=1}^n\frac{1}{\sqrt{2}}\sum_{i=1}^n\frac$