

HEAVY ION FUSION SYSTEM ASSESSMENT:
FINAL FOCUS AND TRANSPORT MODEL *

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4.1. HEAVY ION FUSION SYSTEM ASSESSMENT: FINAL FOCUS AND TRANSPORT MODEL*

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1. Overview

At the end of the induction linac the beamlets are laterally separated for transport to final focus and, if necessary, split to provide an increased final number of beamlets on target (N_0). Splitting may be required for symmetric illumination, to stay within space charge limits, or to provide a sufficient number of beamlets to build up a desired intensity waveform through the use of path length differences. The N_0 transport channels from the linac to final focus are composed of cold bore superconducting quadrupoles and bends, and possibly higher order magnetic elements which may be needed to control the effects of momentum dispersion and aberrations. The beamlets have a head-to-tail velocity difference on the order of 5% imposed during the final stages of acceleration, which produces an order of magnitude or more compression during transport, so the final pulse length is in the desired range (5-20 ns) at the pellet. As the beamlets compress, space charge limits in transport are increasingly stressed, with large apertures and close packing of quadrupoles especially pronounced immediately before the final focus magnet set.

The major features of the final focus system are determined largely by the requirements of spot size on the pellet, reactor chamber radius, and the shielding required to reduce the neutron, x-ray and gas fluxes from the reactor to an acceptable level. The final focus quadrupole triplets described by R. Martin⁽¹⁾ are well suited to serve as the basic final focus components. HIBALL II⁽²⁾ adopts for this purpose a pair of triplets separated by a pair of weak bends which aid in the removal of line-of-sight neutrons. This general arrangement is also adopted in the present study.

Transport within the reactor vessel has, in most studies, been assumed to take place in near vacuum ($P < 10^{-4}$ Torr Li) to avoid disruption by the two-stream instability.⁽³⁾ Alternatively, a "high pressure window" ($P = 1 - 10$ Torr Li) may also be available for stable propagation;⁽³⁾ its suitability, however, in a reactor/beam line environment is very unclear because of the large gas load that may stream back into the final focus lenses. HIBALL II specifies $P < 3 \times 10^{-6}$ Torr Pb vapor to avoid the stripping of electrons from the beam ions (which might cause spot size blow up through the interaction with the beam's electric field). Unfortunately, several attractive reactor concepts considered in the present study (HYLIFE⁽⁴⁾, CASCADE⁽⁵⁾, WET WALL⁽⁶⁾) have residual gas pressures in the range $10^{-2} - 10^{-3}$ Torr Li at reasonable repetition rates (2 - 10 Hz); this pressure must be taken into account with regard to both transport in the reactor and the leaking of gas into the final focus beam lines. Recent calculations⁽⁷⁾ indicate that, contrary to earlier conclusions, the two-stream instability is benign at these pressures due to the detuning effect of beam convergence.

To produce the small spot radius (r_s) on target, the final beamlet unnormalized emittance (ϵ) must satisfy the condition $\epsilon < r_s\theta$, where θ is the beamlet convergence cone half-angle. For the typical parameters $r_s = 3$ mm, $\theta = 10$ mr, we require $\epsilon < 3 \times 10^{-5}$ m-r. This value appears to be achievable using high brightness ion sources⁽⁸⁾ and is well matched to the desired range of normalized emittance for a cost-optimized accelerator. Allowance must also be made for the effects on spot size of momentum spread ($\pm\Delta p$), various forms of beam jitter, and space charge induced blow-up. A final focus system composed of a pair of triplets has dispersion at the pellet which leads to an increased spot radius $\Delta r_s \approx 8L\theta (\Delta p/p)$, where L is the distance from the center of the final magnet to the pellet. Unless this is corrected by special beamline elements, it is desirable to limit the momentum spread to the range $\Delta p/p \leq \pm 10^{-3}$. This is a severe requirement on the accelerator system (which must produce a value less than $\sim \pm 10^{-4}$ prior to compression).

In summary, the required small spot size on the pellet is met by low specified emittance, small momentum spread, and a set of other focal and reactor constraints which are only partially understood at present. The convergence cone half-angle, θ , is set at a value which is determined by tradeoffs among economic and physical factors. Factors driving a low value of θ are dispersion, aberrations, magnet costs, reactor economics, shielding and beamline vacuum. Factors driving a large value of θ are the emittance limit, space charge limits, and jitter control. The typical range of reactor values ($\theta = 5-20$ mr) is the result of compromise among these factors. Aside from the spot size condition, it is desired to make the normalized emittance relatively large ($\epsilon_n = \beta\gamma\epsilon > 10^{-5}$ m-r) since transportable current is found to vary as $\epsilon_n^{2/3}$, and too small a value of ϵ_n could result in an unreasonably large number of beamlets in the high energy portion of the linac (N increasing above ~ 24).

2. Pulse Compression

At the end of acceleration the ion pulse is typically 100-400 ns in length, which is well matched to the bandwidth of the accelerator pulse forming system. Subsequent reduction to the desired 5-20 ns length desired for the fusion pellet implosion is achieved by the mechanism of drift compression in the transport lines leading to the final focus system. If the initial pulse length (in m) is ℓ_0 and the drift lines have length Z_0 , then a head to tail velocity tilt of approximately

$$\frac{\Delta v}{v} = \frac{\ell_0}{Z_0} \quad (1)$$

must be applied in the final stages of acceleration. If, for example, $\ell_0 = 20$ m and $Z_0 = 400$ m then the pulse tail must move 5% faster than the head in the transport lines. There are several important considerations in this approach:

- (a) The bends in the transport system must handle the velocity tilt and space charge with a minimum of dispersive effects. There have been only rudimentary (but encouraging) calculations of a design to accomplish this.

- (b) Longitudinal space charge forces reduce the velocity tilt as the pulse compresses; the initial tilt must be large enough that it is not entirely removed before the desired final pulse length is reached.
- (c) Any residual tilt remaining in the pulse at the time of final focus will result in a potentially severe second order chromatic aberration at the pellet. It is assumed that this can be compensated by the use of rapidly pulsed quadrupoles in an upstream location. These pulsed quadrupoles would impose a time dependent envelope oscillation which would cancel the time dependent aberration resulting from the remaining tilt.
- (d) The generation of longitudinal momentum spread by the inhomogeneous fields acting during compression is minimal (ideally $\Delta p/p \leq 10^{-3}$ in final focus). A recent, and preliminary particle-in-cell simulation of compression dynamics indicates that final momentum spread can be on the order of 10% of the initial tilt⁽⁹⁾. This is larger than desired by a factor of several.

The System Assessment model assumes the favorable resolution of these concerns. However, the role of space charge in removing tilt appears to be sufficiently fundamental that a scale law has been devised for the System Model. We adopt the approximate representation of longitudinal electric field

$$E_z = - \frac{g}{\gamma^2} \frac{\partial \lambda}{\partial z}, \quad (2)$$

where $\lambda(z,t)$ is the line charge density of the beamlet and

$$g = \frac{1}{2} + \log_e \left(\frac{b^2}{a^2} \right) \approx 1.3 \quad (3)$$

is a geometric factor involving the ratio of channel radius b and beam radius a . Then a pulse with parabolic longitudinal profile must have initial tilt

$$\left(\frac{\Delta v}{v} \right)_0^2 \geq 12 g K \left(1 - \frac{\ell_f}{\ell_0} \right). \quad (4)$$

Here ℓ_0 and ℓ_f are initial and final pulse lengths and K is beamlet perveance in final focus

$$K = \frac{2 q e I}{(\beta \gamma)^3 M c^3} (4 \pi \epsilon_0)^{-1}. \quad (5)$$

The system code generally uses the limiting value $K = \theta^2$ (see discussion of perveance limit given below) where θ is the convergence half angle in final focus. Inserting the typical values $\theta = .01$ rad and $l_f/l_o = .05$ we find the tilt condition

$$\left(\frac{\Delta v}{v}\right)_o > \left[(12)(1.3)(10^{-4})(.95) \right]^{1/2} = .038. \quad (6)$$

This is an appreciable, but probably not unacceptable, value. A residual momentum spread of $\pm 5\%$ of this tilt would be double the value of $\pm .001$ assumed in the model. Thus we are somewhat optimistic on this point.

3. Perveance Limit

The minimum number of final beamlines (N_o) required to transport the beam ions to the fusion pellet with radius r_s can be estimated from a consideration of space charge effects in the reactor chamber. First consider the situation in which the beamlets transverse the chamber in vacuum and that space charge is the dominant defocussing effect. Then the beam envelope equation is

$$\frac{d^2 a}{ds^2} = \frac{K}{a} \quad , \quad (7)$$

where K is the beamlet perveance:

$$K = \frac{2Iqe}{(B\gamma)^3 m_o c^3 A 4\pi\epsilon_o} = \frac{2Iq}{(B\gamma)^3 A (31 \times 10^6 \text{ amp})} \quad . \quad (8)$$

The perveance is a dimensionless measure of beamlet current. The minimum beamlet radius resulting from this equation is

$$r = a_{\text{lens}} \exp(-\theta^2/2K) \quad , \quad (9)$$

where θ is the convergence cone half angle and

$$a_{\text{lens}} = L\theta \quad (10)$$

is the beam radius at the final lens. For a power reactor, we expect $L = 5-10$ m, $\theta = 10-20$ mr, and $r = 2-4$ mm. To make space charge negligible,

we therefore require, in the absence of neutralization

$$K \lesssim (.1) \theta^2 . \quad (11)$$

This condition leads to unacceptably large numbers of beamlets when the charge state exceeds $q = 2-3$, so some degree of neutralization must be invoked in general. The figure adopted in the HIFSA study is 90% neutralization, either from the ionization of residual gas or co-injection of electrons. Recent calculations by Olson⁽¹⁰⁾ indicate that the ion pulse is able to trap an electron cloud of sufficient density and low enough temperature to accomplish this. Thus assuming neutralization we adopt the condition

$$K \leq \theta^2 . \quad (12)$$

The final number of beamlets N_0 can be related to the total energy delivered to the pellet (W), beamlet current (I), and pulse-length (τ_p) by

$$N_0 = \frac{W}{I \tau_p / qe} \approx \frac{4We^2 q^2}{K(\beta\gamma)^5 A^2 m_0^2 c^5 4\pi\epsilon_0 \tau_p} . \quad (13)$$

A convenient formula for N_0 is

$$N_0 = (.138) \left(\frac{q}{A} \right)^2 \frac{W \text{ MJ}}{K(\beta\gamma)^5 \tau_{ns}} , \quad (14)$$

where final pulse length is given in nanoseconds (τ_{ns}) and we used the non-relativistic formula $T_0 = (\beta\gamma)^2 m_0 c^2 / 2$. For the typical case ($q = 3$, $A = 200$, $W_{MJ} = 4$, $\tau_{ns} = 10$, $K = 2.25 \times 10^{-4}$, $\beta\gamma = .33$), we get $N_0 = 14.1$, which rounds up to $N_0 = 16$ for symmetric two-sided illumination.

4. Transport Lines

Transport lines from the Linac to the final focus train serve a variety of purposes:

- a. drift compression,
- b. bends matched to final focus configuration,
- c. delay lines for multiple pulse linac,
- d. correction and compensation of aberrations and dispersion,
- e. pulse splitting.

It has not been feasible to make detailed estimates of cost, length and configuration which accommodate all of these features. A crude estimate of cost, which is proportional to the length and total number of the transport

lines is used in the system code:

$$\text{cost/m} = (5000\$) \left[1 + \left(\frac{[B\rho]}{200 \text{ T-m}} \right)^2 \left(\frac{K}{2 \times 10^{-4}} \right)^2 \right]. \quad (15)$$

The actual perveance, of course, is much lower than the final value (K) during most transport; but the dependence of radius on current is approximately correct. The quantity $[B\rho]$ is the magnetic rigidity of the ions ($[B\rho] = \beta\gamma Mc/qe$). Tunnel costs are a separate item in the system code.

Any splitting zones required to convert the N accelerated beamlets into N_0 final beamlets are costed at 20 k\$/m for a total bend of $\pi/8$ radius:

$$\frac{\text{cost}}{\text{split}} = \frac{20,000\$}{\text{m}} \left(\frac{[B\rho]}{2T} \right) \left(\frac{\pi}{8} \right). \quad (16)$$

The length of beam lines is highly dependent on both the focal geometry and the final focus train length ($8L$), where L is the focal length of lenses close to the reactor (see sect. 6). A rough matchup of geometry has motivated the following formulas (length per transport line)

Single sided Illumination:

$$\text{line length} = 18L$$

Double sided Illumination:

$$\text{line length} = 9L + \left(\frac{3\pi}{2} - 1 \right) \rho,$$

where

$$\rho = [B\rho]/2T$$

is the average radius of curvature in the bend system. The total length is not allowed to be shorter than $18L$.

Uniform Illumination:

$$\text{line length} = 20L + 2\pi\rho.$$

This is necessary to carry beamlets to the back side of the reactor.

Double Pulse delay lines:

$$\text{line length} = 18L + Bc \tau_d$$

where delay time $\tau_d = 10^{-5}$ s is assumed. The second pulse lines have length $18L$.

5. Transportable Current

Immediately prior to final focus the beamlet current (as computed from the perveance limit) can potentially exceed the Maschke transport

limit.(11) To insure against this possibility, the final beamlet current (I) is tested against this limit, allowing a factor of two for compression during final focus; that is, $I \leq 2 I_{\text{limit}}$ is allowed.

The specific formula for limiting current used here(12) is the general form

$$I_{\text{limit}} = (2.89 \times 10^6 \text{ Amp}) \left(1 - \frac{\sigma_0^2}{\sigma^2} \right) \left[\sigma_0^4 (\beta\gamma)^5 \eta^2 \left(\frac{A}{q} \right) \left(\frac{\epsilon_n}{\sigma} \right)^2 B^2 \right]^{1/3} \quad , 17)$$

where σ_0 and σ are the normal and depressed tunes of the transport lattice, η is the quadrupole occupancy factor and B is the quadrupole field at the beam edge. We adopt the maximum reasonable values for these quantities as understood at present:

$$\begin{aligned} \sigma_0 &= 85^\circ = 1.48 \text{ rad} \quad , \\ \sigma_0/\sigma &= 10 \quad , \\ \eta &= .5 \quad , \\ B &= 3T \quad , \end{aligned}$$

to obtain

$$I < 2 I_{\text{limit}} = (45.2 \times 10^6 \text{ Amp}) (\beta\gamma)^{5/3} \left(\frac{A}{q} \right)^{1/3} \epsilon_n^{2/3} \quad . \quad (18)$$

For the typical values $A/q = 67$, $\beta\gamma = .33$, $\epsilon_n = 10^{-5}$ rad-m, we get $I < 13.4$ kA, (which is generally satisfied).

6. Final Focus Components and Their Arrangement

The final focus system described in the HIBALL II report(2) serves as a model for HIFSA. The essential layout consists of two quadrupole triplets separated by a pair of weak bends ($\sim 3^\circ$ each). The first triplet expands the beamlet to a radius of ~ 20 -40 cm and the second triplet focusses it onto the pellet. The bends allow line-of-sight neutrons to be removed from the beamline. If neutrons were absent then a single quadrupole quadruplet would be adequate. The magnets are assumed to be superconducting with a warm bore (for system efficiency), with the possible exception of the final quadrupole, which may be an iron dominated electromagnet in order to withstand the neutron flux. A rough model of the system optics is obtained by taking the focal length of all six quadrupoles equal to the distance (L) from the middle of the final magnet to the fusion pellet. The beam radius in the final magnet is $L\theta$, and the maximum radius in the train is $3L\theta$, which is reached in the second and fifth quadrupoles. Space charge effects are incorporated in this design only in the crude sense that magnet gradients are increased by a factor of $\sqrt{2}$ over the values required in the absence of space charge. Magnet lengths are set equal $L/2$ except for the

final quadrupole, which is generally shorter ($\sim L/4$) in order to reduce the final focal length. Total length for the train is set at $8L$ (generally in the range 50-100 m), which is 50% occupied by magnets. The superconducting wire is set back to a radius of twice that of the beam to allow room for shielding, cooling and thermal insulation.

For the described final focus layout the spot radius is given by

$$r_s^2 \approx \frac{\epsilon^2}{\theta^2} + (8L\theta\Delta P/P)^2, \quad (19)$$

assuming aberrations and space charge in final transport can be neglected. The minimum spot radius is obtained with

$$\theta = \left(\frac{\epsilon}{8L\Delta P/P} \right)^{1/2}. \quad (20)$$

For the system cost algorithm we use the formula

$$\frac{\text{M\$}}{\text{Train}} = \frac{\text{enclosure}}{\text{cost}} + (1.2) \left(.5\text{M\$} + 8 \frac{\text{M\$}}{\text{magnet}} \right). \quad (21)$$

The enclosure cost is \$2830/m for a cut and cover tunnel. The factor of (1.2) includes all shielding, utilities, power supplies, etc. A .5M\$ price is included to cover the transition zone in which the gas load is reduced, and the factor of 8 reflects the number of magnets per line. The cost per magnet estimate is based on the third quadrupole, which is of medium size compared with the others. Its wire radius is $4\theta L$, with field at the wire $B_c = 8 \sqrt{2} [B\rho] \theta/L$, where $[B\rho]$ is the magnetic rigidity of the beam. Generally, values of B_c obtained range from $\sim (1.0 - 5.0)\text{T}$, but an upper limit of 8T at the wire is imposed.

The cost per magnet is a modification of the formula used in the induction linac design code LIACEP, (described elsewhere in the HIFSA report), which in turn was based on a 1979 survey of existing design estimates. It is

$$\frac{\text{M\$}}{\text{magnet}} = (77 \times 10^{-4}) (.285 \frac{l_m}{m} + .43) (8 + 76.8 r_c + 81.1 r_c B_c), \quad (22)$$

where $r_c = (4\theta L - .04 \text{ m})$. A point check of this formula with a current SSC magnet cost code gave agreement within 10% for a large bore quadrupole.

7. Geometric Aberrations

During final focus significant deviations from paraxial ray optics may appear if the beam is focussed too abruptly. These deviations appear as a third-order effect in the formulation of beam transport, and their

consequence is to distort the beam spot shape such that intensity is reduced. D. Neuffer has given the condition⁽¹³⁾ for this distortion to be tolerable, assuming the spot radius is determined by emittance ($r_s = \epsilon/\theta$):

$$\epsilon < (0.15) r_s^{5/4} \rho^{-1/4}, \quad (23)$$

where ρ is radius of curvature of a particle at the beam edge in the final focus quadrupole fields. In the present study, momentum spread and possibly space charge also play a role in determining spot radius, so Neuffer's formula is modified by substituting $\epsilon = \theta r_s$ to obtain the equivalent form

$$\theta < .15 (r_s/\rho)^{1/4}, \quad (24)$$

which should apply in the more general situation. This formula is used in the system code to place an upper limit on θ . The typical maximum values are in the range 15-30 mr and may be slightly conservative since some measures such as the insertion of octupoles can be taken to reduce such aberrations.

Aberrations in final focus associated with closeness of the beam envelope to the magnet pole tips are generally not expected to be a problem since in most cases the final focus coils are moved well back from the aperture (by a factor of two) in order to allow space for shielding and insulation. In addition, the magnets are operated at a fixed strength, thus permitting flexibility in design that could minimize aberrations due to field errors, fringe fields etc.

8. Gas Load in Final Focus Lenses

It is essential that the residual pressure in the reactor chamber ($P \sim 10^{-2} - 10^{-3}$ Torr Li) be attenuated by a large factor between the reactor and the final focus train. Otherwise the bulk of the beam ions are stripped before the focal process is completed and are thereby misdirected. It is assumed in the study that this can be achieved with a combination of fast shutters and pumping in a transition region of about 1.0 m in length located between the final quadrupole and the reactor shield. Some estimates of the requirements follow.

The stripping length $\ell_s = (n_g \sigma_s)^{-1}$ should be at least 300 m in the final magnet if beam loss is to be kept below $\sim 1\%$. There is further pumping upstream so ℓ_s gets longer rapidly as one moves away from the reactor. The stripping length is approximately (see subsection 9.2)

$$\ell_s \approx \frac{1.0 \text{ cm}}{P_{\text{Torr}}} \left(\frac{92}{Z_i} \right), \quad (25)$$

we require (for U^{238} on Li)

$$P \lesssim 3 \times 10^{-5} \text{ Torr,}$$

which is a factor of 30 to 300 below the pressure in the chamber. High speed shutters (for example spinning disks with holes) could open a 10 cm diameter hole for a period as short as 2 ms, so the beam line would only be open for 1% of the time if the system rep rate was 5 Hz. It is only open for the low pressure residual gas, i.e., the high pressures following the explosion are blocked.

The gas volume which is passed by the open shutters is characterized by molecular flow (long mean free path) and can be readily removed by pumping except for the line of sight fraction. This fraction can be reduced to a few percent of the passed volume if the transition zone is long enough; we assume for the study that a length equal to ten times the beam radius is adequate. Hence the transition length formula: $\ell_t = 10 \theta \cdot [\text{Reactor Radius } (R_c + X)]$. The cost of this section is set at 500 k\$ per line.

The development of a transition zone design is a critical item for HIF.

9. Beam Transport within The Reactor

9.1 Reactor Environment

The system model defines a reactor chamber of radius $R_c = 5 - 10$ m surrounded by a Li blanket and shielding of total thickness $X = 2$ m. The beamlets must pass through whatever residual gas remains in this zone as they converge towards the pellet. An additional beam line length of ~ 1 m between the final magnet and the shielding is occupied by pumping ports and shutters required to prevent a significant amount of gas from reaching upstream into the final focus lenses. No restrictions based only on gas fill are specifically incorporated into the system model. However, it is assumed that a gas density no greater than $\sim 3 \times 10^{14} \text{ cm}^{-3}$ Li (equals 10^{-2} Torr Li or equivalent other vapor at 300° K) is present at the moment of beamlet transit. Since pressures in the range 1 - 10 Torr appear immediately following an explosion this implies the presence of a very powerful self pump-down of the chamber to match the repetition rate of $\sim 1-10$ Hz. The difficulties associated with densities higher than $3 \times 10^{14} \text{ cm}^{-3}$ Li are: (a) gas flux into final focus lenses, (b) filamentation instability and possibly the two-stream instability, which are treated below, and (c) possible beam spot spreading from stripping. Limitations due to beam scattering and energy loss set in at $n_g \geq 3 \times 10^{16} \text{ cm}^{-3}$ and are not relevant here. Fortunately the reactor types considered here [Granular Wall, Wetted Wall, HYLIFE (Li jets), and Magnetically Protected Dry Wall] all appear to be potentially capable of meeting this requirement. An interesting contrast is provided by the HIBALL chamber (not considered here), which employs a Li-Pb layer. This special surface pumps down the chamber to $\sim 10^{11} \text{ cm}^{-3}$ Pb vapor at a 5 Hz shot rate. A brief discussion of stability and stripping follows.

9.2 Stripping

The cross section for gas stripping of the beam ions is approximately given by

$$\sigma_s \approx \frac{2.45 \times 10^{-18} \text{ cm}^2}{\beta^2} \left(\frac{Z_i}{92} \right) \exp(-.063Z^*) \quad , \quad (26)$$

Z_i = atomic no. of ion ,

Z^* = stripped state of ion .

Here we have used the numerical fit by Stroud⁽⁷⁾ for U²³⁸ on Li, generalized to apply to other heavy ions by incorporating the factor $(Z_i/92)$. For low Z^* , a typical value is (10 GeV, U²³⁸).

$$\sigma_s \approx 2.7 \times 10^{-17} \text{ cm} \quad .$$

A stripping length is defined:

$$l_s = \frac{1}{n_g \sigma_s} = (370 \text{ cm}) \frac{10^{14}}{n_g} \quad (27)$$

An average stripped state of approximately

$$\overline{Z^*} = Z_{\text{initial}}^* + \frac{R_c + X}{l_s} \quad (28)$$

results as the ions approach the pellet. If n_g is taken as $3 \times 10^{14} \text{ cm}^{-3}$ then, since $R_c + X$ is expected to be on the order of 10m, it is clear that as many as ten electrons are removed in addition to the initial state q .

The consequences of stripping in the chamber are unclear at present. The beam current increases as Z^* , and the rigidity decreases as $1/Z^*$. Hence we expect the stripped ion beam to be more easily disrupted by beam-plasma instabilities. These are discussed below. A second concern is that the beam will not focus to the desired small spot radius due to increased space charge forces. The few estimates made to date of this effect suggest that the problem is reduced or eliminated by the fact that electrons stripped from the ions travel with the beam and neutralize the increased space charge and current. The dangerous possibility is that, since there will be a spread in charge states, the ions will be deflected by varying amounts in the residual self electric field of the beam and the spot size will be spread. Research on this topic--dynamics of the beam envelope in the gas

environment including the statistical effects of stripping and neutralization--has been inadequate and has been identified by HIFSA as one of the most important areas for future simulation and experiment. If stripping is found to be unacceptable in the considered reactor designs then either some other propagation mode which is insensitive to stripping must be considered or a reactor chamber of the HIBALL type ($n_g \ll 10^{14}$) must be considered.

9.3 Filamentation Instability

The filamentation mode is a serious concern for high pressure reactors ($P \geq 10^{-2}$ Torr Li). If the beam ions strip to a sufficiently high average charge state and the beam is also neutralized by background electrons, then magnetic pinches can grow during propagation to the pellet and disrupt the convergence processes. A previous analysis of this phenomena⁽¹⁴⁾ gave the safety condition

$$\alpha = \frac{\omega_b R_c}{c} \leq 3, \quad (29)$$

where ω_b is the plasma frequency of the beamlet evaluated at the chamber wall, c is the speed of light, and R_c is the chamber radius. Because of convergence effects the total mode growth is only on the order of $\exp(\alpha) < 20$. The mean stripped charge state Z^* is used to evaluate ω_b .

$$\omega_b = \left(\frac{n_b Z^{*2} e^2}{\epsilon_0 m_0 A} \right)^{1/2}, \quad (30)$$

where n_b is the beamlet's number density. Using convenient system parameters we have the safety condition

$$W_{\text{beamlet}} \leq (33\text{MJ}) \left(\frac{A}{Z^*} \right)^2 \beta^3 \tau_{\text{ns}} \theta^2. \quad (31)$$

There is little problem provided $A/Z^* \geq 20$. We estimate for stripping by Li vapor

$$\frac{A}{Z^*} \gtrsim \frac{2.5\text{m}}{R_c P_{\text{Torr}}}, \quad (32)$$

so no problem is expected below $\sim 10^{-2}$ Torr, which is the case for the present study. If higher pressures are contemplated then this subject should be given renewed attention.

9.4 Two Stream Mode

Prior to 1985 it was generally believed that unstable two-stream modes eliminated the possibility of heavy ion beams propagating in a background pressure of 10^{-4} - 10^{-1} Torr Li. The analysis of converging beams by P. Stroud⁽⁷⁾ has reversed this opinion and for HIFSA we now (optimistically) assume that there is no restriction on pressure from this consideration.

The standard analysis for non-converging beams uses a Fourier decomposition in longitudinal variable (z) and time (t):

$$\text{Perturbed quantities} \sim \exp(ikz - \omega t), \quad (33)$$

where k is the wave vector and ω is the frequency. The resulting dispersion relation for the plasma electron-beam ion mode is

$$1 = \frac{\omega_b^2}{\omega^2} + \frac{\omega_p^2}{(\omega - kv)^2}, \quad (34)$$

where ω_b and ω_p are respectively the beam and electron plasma frequencies, and v is the beam velocity. Rapid growth occurs for $\omega \approx \omega_p$ and

$$k \approx \omega/v. \quad (35)$$

The maximum growth rate in this case is $(.6873) (\omega_p \omega_b^2)^{1/3}$, and only non-linear effects can result in saturation. When convergence of the beam envelope is taken into account this simple (and disastrous) picture is changed because the resonant condition does not persist with distance. The plasma frequencies (ω_b, ω_p) both increase as the beam converges and any particular unstable wave number k is quickly swept through resonance. The reader is referred to the article by Stroud for details; the relevant conclusion is that at typical HIF parameters, less than 1% of beam ions are deflected from the desired spot at pressures at least up to 3×10^{-3} Torr Li.

10. Sequence of Calculation

The HIFSA system code requires as input a set of parameters such as ion mass number and net electric power, and also the specification of major features such as pellet and reactor type. A conceptual power plant design is then computed, including cost breakdowns, cost of electricity, size of components, and dependent physical parameters such as spot radius. The

entire ensemble of designs computed from a broad range of input parameter sets is stored in a data base, which may be searched for a minimum COE subject to specified constraints. Final focus constraints play a large role in the system definition. In this section we give a brief outline of the way these constraints typically enter into the computational sequence (there are several alternatives.)

A net electric output of 1000 MW (for example) is desired, so a fusion power $P_f = 4000$ MW is tentatively selected. A repetition rate (r) is also specified, which fixes the fusion yield $Y = P_f/r$. A target type has also been specified; we assume here that the Lindl-Mark⁽¹⁵⁾ single shell gain curves are applicable. These curves relate gain (Q) to the net beam energy on target and the quantity $\gamma_p = r_s^{3/2}R$ where R is ion range in the pellet. The value of γ_p is specified, and $W = Y/Q$ is inferred from the gain curves. The required net beam power (P_b) is also determined from the Lindl-Mark formulation.

Some major beam parameters are now determined. Mass number (A) and charge state (q) have been specified at input but ion energy (T_0) must be selected from a band of permissible values such that the Lindel-Mark spot size condition

$$(.1) r_s < W_{MJ}^{1/3} < (.2) r_s \quad (36)$$

is satisfied. the range-energy relation then determines R , and spot radius is given by

$$r_s = (\gamma_p/R)^{2/3} . \quad (37)$$

The relativistic parameter $\beta\gamma$ is determined from T_0 and A :

$$\beta\gamma = \left[2 \left(\frac{T_0}{Am_0 c^2} \right) + \left(\frac{T_0}{Am_0 c^2} \right)^2 \right]^{1/2} , \quad (38)$$

and magnetic rigidity in final focus is

$$[B\rho] = \beta\gamma Am_0 c / qe . \quad (39)$$

Net beam current (electrical) is

$$I_{net} = \frac{P_b qe}{T_0} , \quad (40)$$

however the current per beamlet $I = I_{net}/N_0$ is not determined until the number of beamlets N_0 is fixed.

The beamlet cone half angle (θ) must be determined at this point. First a limit (θ_{\max}) is fixed by the aberration condition

$$\theta_{\max} = (.15) \left(\frac{r_s}{\rho} \right)^{1/4}, \quad (41)$$

where ρ is the radius of curvature in the final quadrupole in the final focus beamline. We use

$$\rho = \frac{[B\rho]}{B_p} \quad (42)$$

with specified B_p (typically $B_p = 1.0T$). The actual value of θ is the smaller of θ_{\max} and the optimum value

$$\theta = \frac{r_s}{\sqrt{2} 8L \Delta p/p} \quad (43)$$

The momentum spread is specified (typically $\Delta p/p = \pm 10^{-3}$) and the distance to the center of the final lens (L) is determined from the sum of the specified reactor cavity and blanket radii ($R_c + X$), and half the final lens length (ℓ):

$$L = (1 + 10 \theta) (R_c + X) + \ell/2 \quad (44)$$

with the factor $10 \theta \approx .1$ inserted to allow room for shutters and pumping.

The final lens aperture R_f and magnet length are determined simultaneously with L using the thin lens formulas

$$\ell = \frac{R_f [B\rho]}{LB} \quad (45)$$

$$R_f = (1.1) \theta (L + \ell) \quad (46)$$

At this point the final emittance (ϵ) is determined from θ and r_s :

$$\epsilon = r_s \theta / \sqrt{2} \quad (47)$$

where the factor of $\sqrt{2}$ reflects the fact that momentum spread and emittance are assumed to play an equal role in determining r_s . Normalized emittance is $\epsilon_n = \beta \gamma \epsilon$. This is the value used in the calculation of

accelerator parameters. In case this value of ϵ_n exceeds the tabulated values used in the LIACEP survey of the linac parameters we use its maximum tabulated value.

The beamlet current (I) and hence beamlet number (N_0) is now determined from the perveance condition

$$N_0 \geq (.138) \left(\frac{q}{A} \right)^2 \frac{W \text{ MJ}}{\Theta^2 (\beta\gamma)^5 \tau_{ns}} \quad (48)$$

If this inequality allows a smaller number of beamlets than is assumed for the Linac then the Linac number (N) is used, i.e. there may be splitting, but no merging is considered after acceleration.

Having determined N_0 , L, Θ and $[B\rho]$, the lengths, apertures and field strengths of the final focus elements are determined (total train length is 8L). These quantities are used to obtain a cost estimate which is entered into the system cost table. The lengths and costs of the transport lines are estimated in similar fashion. The remainder of the calculation determines the cost of the accelerator, balance of plant, reactor, etc. as well as the resultant net electrical output. If this output differs from the original input, the calculation is repeated with an increased or decreased value of fusion power.

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