

Linear magnetoresistance in the low-field limit in density-wave materials

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The magnetoresistance (MR) of a material is typically insensitive to reversing the applied field direction and varies quadratically with magnetic field in the low-field limit. Quantum effects, unusual topological band structures, and inhomogeneities that lead to wandering current paths can induce a cross-over from quadratic to linear MR with increasing magnetic field. Here we explore a series of metallic charge- and spin-density-wave systems that exhibit extremely large positive linear MR. By contrast to other linear MR mechanisms, this effect remains robust down to minuscule magnetic fields of tens of Oersted at low temperature. We frame an explanation of this phenomenon in a semiclassical narrative for a broad category of materials with partially gapped Fermi surfaces due to density waves.

linear magnetoresistance | density-wave materials | Fermi surface

The evolution of the electronic transport under the influence of a magnetic field can be deeply revealing of the fundamental properties of a material. Classically, the transverse magnetoresistance $\rho_{xx}(H_z)$ evolves quadratically with magnetic field H , saturating at high fields if the hole and electron densities are not compensated (1–3). The asymptotic behavior in the low-field limit of $\omega_c\tau \ll 2\pi$, where ω_c is the cyclotron frequency and τ is the relaxation time, arises from the Onsager reciprocity relation, which requires $\sigma_{ij}(\mathbf{H}) = \sigma_{ji}(-\mathbf{H})$. The leading term in the magnetoresistance (MR) at low field is thus $\Delta\rho = \rho(H) - \rho(H = 0) \sim H^2$ (1, 2).

Other functional forms have been observed, most notably the symmetric linear form of $\Delta\rho \sim |H|$, which is nonanalytic at $H = 0$ but is allowed in the high-field limit, $\omega_c\tau \gg 2\pi$. There are several well-established electronic and geometric mechanisms for generating this behavior in the high-field limit (1–10), which can be separated into two classes. The first is due to special features at the Fermi surface, such as sufficiently low electron density to permit condensation of the electrons into the lowest spin-split Landau level (4), linear dispersion from a Dirac cone with infinitesimally small carrier mass (5), Umklapp scattering (6), and magnetic breakdown (7). The second class is predominantly geometric in nature, such as an average over a combination of open and closed electron trajectories in polycrystals (2), guiding center diffusion in weak disorder (8), or strong mobility fluctuations due to irregular current paths from a strongly inhomogeneous medium or conductive grain boundaries (9, 10). Neither class addresses linear MR in the low-field regime where $\omega_c\tau \ll 2\pi$, the focus of our experiments.

While MR in metallic paramagnets and ferromagnets is typically small and negative, as the magnetic field quenches spin fluctuations and reduces spin scattering of itinerant carriers, large positive linear MR has been reported over the years in systems with charge-density-wave (CDW) order. This includes $2H$ -NbSe₂ (7), Nb₃Te₄ (11), (PO₂)₄(WO₃)₈ (12), and RTe₃ ($R = \text{Tb}$ and Ho) (13). The linear MR in the low-field limit has been attributed to a wide range of mechanisms, from magnetic breakdown (7) to scattering of

CDW fluctuations at Fermi surface hot spots (13). Here we argue that there exists a universal mechanism to create linear MR in the low-field/low-temperature limit. The salient features are a consequence of itinerant carriers turning sharp corners of the Fermi surface. This mechanism is greatly enhanced in both charge- and spin-density-wave (SDW) systems, as the formation of correlated electronic states opens a gap at the Fermi surface, removing sheets of open electron paths while keeping only small electron/hole pockets/ellipsoids with small orbits of sharp curvature. The change in the Fermi surface topology provides a generic approach to creating linear MR in the low-field limit in correlated electron systems.

Results

We present in Fig. 1 detailed $\rho(T, H)$ data on the density-wave systems GdSi, SrAl₄, and Cr, in addition to comparisons to NbSe₃ and (PO₂)₄(WO₃)₈ derived from the literature. GdSi and Cr have SDWs driven by Fermi surface nesting with Néel transitions at $T_N = 54.5$ and 311.5 K, respectively (14–18). SrAl₄ develops a CDW state below $T_{\text{CDW}} = 245$ K (19), with no confounding contributions from spin order. All of the SDW and CDW ordering wave vectors are incommensurate: $\mathbf{Q} \sim (0, 0.483, 0.092)$ in GdSi (14–16), $\mathbf{Q} \sim (0.952, 0, 0)$ in Cr (18), and $\mathbf{Q} \sim (0, 0, 0.11)$ in SrAl₄ (19). GdSi turns into a field-induced ferromagnet at $H_c = 20.7$ T (15), while the SDW in Cr extends to

Significance

Magnetoresistance has a history of revealing key electronic characteristics of materials. From early measurements on noble metals to definitive characterization of localization effects in semiconductors to recent studies of topological materials, the magnetoresistive response provides an experimental technique to explore the Fermi surface in detail, and to predict and craft physical properties through its sign, functional form, and potential quantum character. Linear magnetoresistance in density-wave systems has eluded clear explanation for over half a century. Here, we present measurements that lead to a general explanation based on unusual current paths tied to the formation of long-range charge or spin order. This mechanism potentially extends to the large magnetoresistance observed in semimetals like Bi, graphite, and WTe₂.

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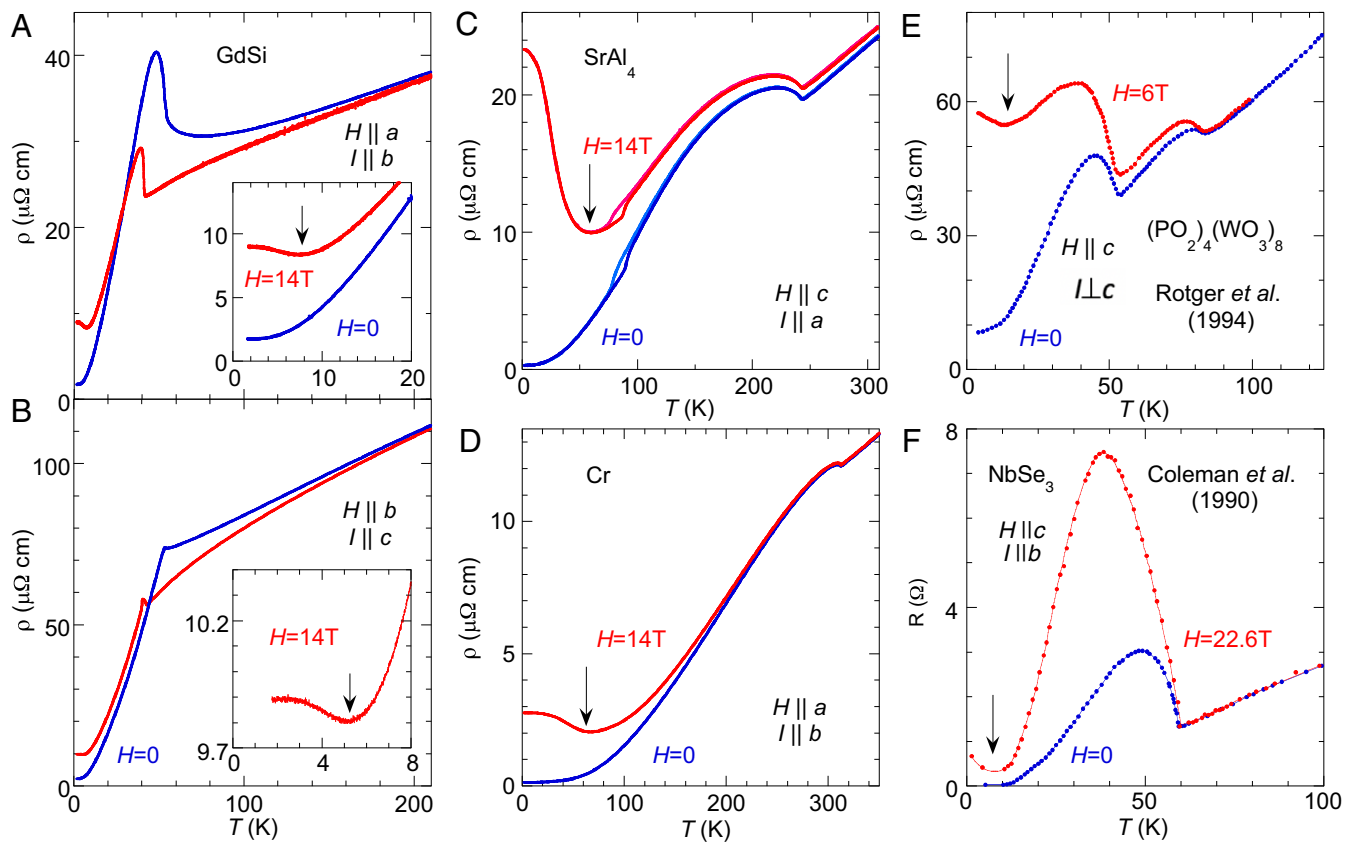


Fig. 1. Finite-field magnetoresistance anomaly in the zero-temperature limit in CDW/SDWs. Transverse MR $\rho_{xx}(T, H_z)$ at zero (blue) and high (red) fields are contrasted for (A and B) GdSi ($H \parallel a$ and b , respectively), (C) SrAl₄, (D) Cr, (E) (PO₂)₄(WO₃)₈ (data from ref. 12), and (F) NbSe₃ (data from ref. 22). The CDW and SDW transitions manifest as the resistance anomalies at higher temperature. Arrows point to where the in-field low-temperature resistance anomaly starts to grow with decreasing temperature. SrAl₄ has an extra structural transition at $T \sim 80$ K as indicated by the temperature hysteresis (19). For our samples, the ratio of $\rho(300 \text{ K})/\rho(2 \text{ K}) = 25$ for GdSi with $\parallel b$, 58 for GdSi with $\parallel c$, 77 for SrAl₄, and $\rho(350 \text{ K})/\rho(2 \text{ K}) = 92.4$ for Cr. This resistance anomaly at finite fields and zero temperature was also observed in semimetals Bi, graphite (20), and WTe₂ (21).

beyond 16 T (17). We measure $\rho_{xx}(H_z, T)$ over a wide magnetic-field range and temperatures from 0.35 to 350 K (Figs. 1 and 2).

All of the listed materials exhibit a resistivity anomaly at the density-wave (DW) ordering temperature for both zero and high fields (Fig. 1). In addition to the DW anomaly, these systems also show a finite-field resistivity anomaly $\rho_{xx}(T, H_z = \text{constant})$ in the zero-temperature limit, which grows with decreasing T and extrapolates to its greatest value at $T = 0$. The onset temperature for the resistivity anomalies are marked by arrows in Fig. 1. Similar high-field, low-temperature $\rho(T, H = \text{constant})$ anomalies have been reported in semimetallic Bi, graphite, and WTe₂ (20, 21), and were attributed to metal-insulator transitions (20). The finite-field, low-temperature anomalies we consider here exist in highly conductive CDW and SDW systems with only partially gapped Fermi surfaces. Our proposed mechanism based on carriers turning sharp Fermi surface corners provides a different explanation for the zero-temperature resistance anomaly of Fig. 1. We argue that its relationship to linear or quadratic MR depends on the structure of the Fermi surface and the degree of disorder, and can be applied to both DW systems and semimetals.

We feature in Fig. 2 two of the most prominent linear MR cases available to us, the pure SDW system GdSi and the pure CDW system SrAl₄, as well as linear MR from three different CDW systems in the literature: (PO₂)₄(WO₃)₈, Nb₃Te₄, and 2H-NbSe₂ (7, 11, 12). In all cases, a strong MR with a positive, linear field dependence was observed in the low-temperature limit. The magnitude of the effect is large: e.g., an MR ratio $\Delta\rho_{ii}(H)/\rho_{ii}(0) =$

3.5–8 ($i = a, b, c$) at $H = 20$ T for GdSi and ~ 75 at $H = 14$ T for SrAl₄, with $\Delta\rho(H)/\rho(0)$ still $\sim 1\text{--}2\%$ at a few hundreds of Oersted. The nearly linear behavior spans more than three decades of field range, and is clearly present even for $\omega_c\tau \ll 2\pi$.

For both GdSi and SrAl₄, the linear MR in the low-temperature limit evolves into a parabolic field dependence at more elevated temperatures (Fig. 3), similar to RTe₃ in the literature (13). Although MR is often fit to a power law with a temperature-dependent exponent (7, 13), our attempts to perform a scaling analysis such as the Kohler plot to collapse all $\rho(T, H)$ data onto a universal curve were not successful. Instead, there likely exist contributions from multiple electron- and hole-like conduction bands at the gapped Fermi surface, with potentially different functional forms under field.

We adopt a phenomenological approach to disentangle linear and quadratic components, fitting the measured MR as $\rho(H, T) = \rho(T, H = 0) + A(T)|H| + B(T)H^2$ as a function of field at various temperatures. We note that this form is distinct from a simple cross-over between linear and quadratic dependencies, and that this procedure is only valid to a magnitude of $\Delta\rho$ that is comparable to $\rho(H = 0)$. As plotted in Fig. 3 B and D for GdSi and SrAl₄, respectively, contributions from $A(T)$ and $B(T)$ to the MR are very different, although they are both insensitive to the range of fitting for $0.5 \text{ T} < H < 4 \text{ T}$ in GdSi, and for $0.1 \text{ T} < H < 0.7 \text{ T}$ in SrAl₄. In both systems, the linear component $A(T)H$ dominates over the quadratic term $B(T)H^2$ at low temperature, but $A(T)H$ drops dramatically with increasing values of the zero-field resistivity, $\rho(T, H = 0)$. We plot $A(T)H$ and $B(T)H^2$ against

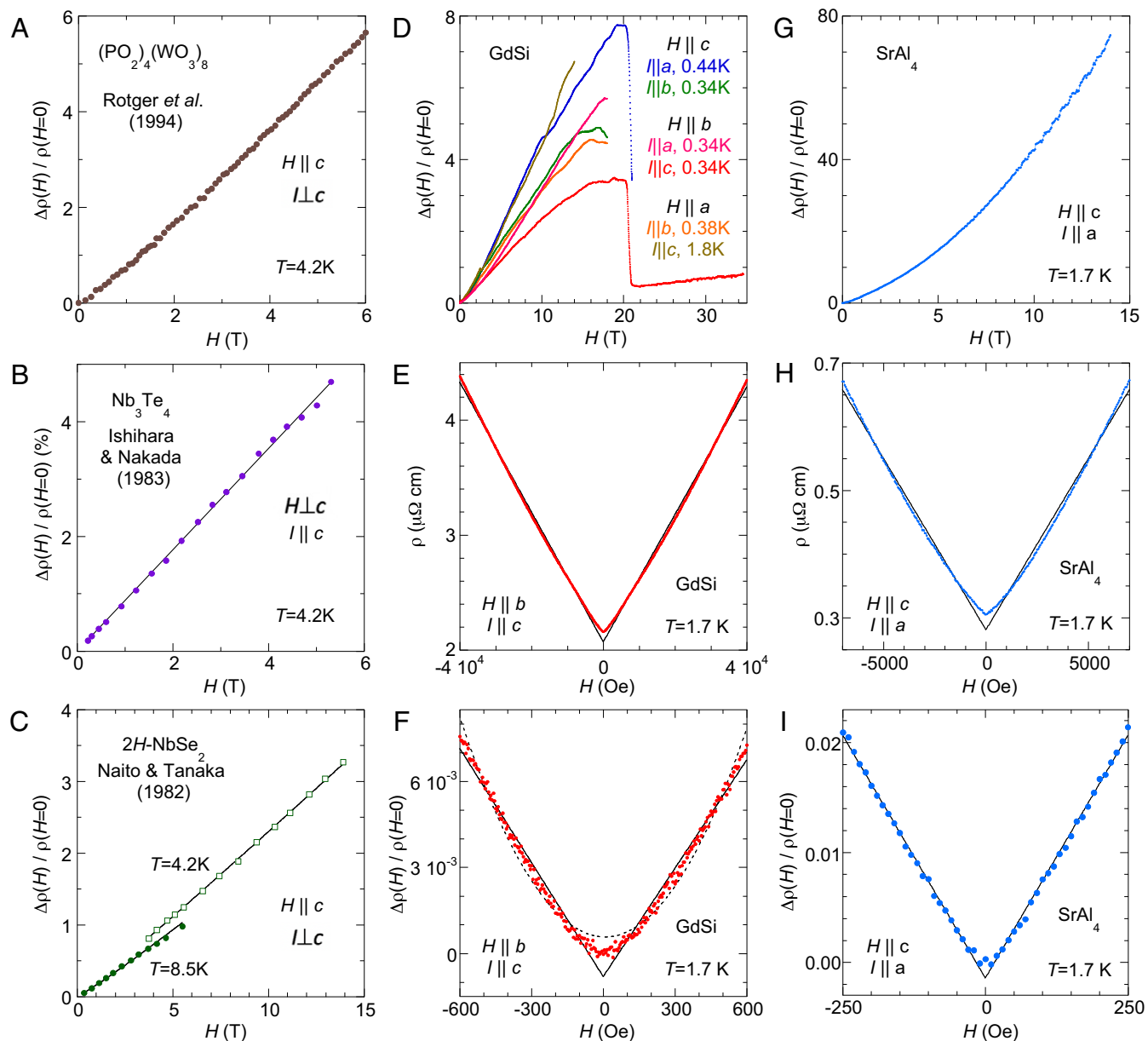


Fig. 2. Linear transverse MR at low field. Positive linear MR as exemplified by five different CDW and SDW systems: (A) $(\text{PO}_2)_4(\text{WO}_3)_8$ (data from ref. 12), (B) Nb_3Te_4 (data from ref. 11), and (C) 2H-NbSe_2 (data from ref. 7), in addition to (D–F) GdSi, and (G–I) SrAl_4 . Linear MR varies over a field range spanning more than three decades, with (D and G) $\Delta\rho/\rho \sim 800\%$ in GdSi and $\sim 7,500\%$ in SrAl_4 ; (E and H) $\Delta\rho/\rho \sim 100\%$; and (F and I) $\Delta\rho/\rho \sim 1\%$. Black solid and dashed lines are even-parity linear ($\sim |H|$) and quadratic fits to the data, respectively. GdSi undergoes a first-order spin-flip transition at ~ 3 T for both $H\parallel a$ and $H\parallel c$ (15). Hence we focus on its MR behavior under the $H\parallel b$ geometry where the spin canting under field is continuous.

$\rho(T, H = 0)$ instead of T itself in Fig. 3 B and D to highlight the monotonic behavior of $A(\rho(T, H = 0))$. By comparison, $A(T)$ would saturate at low temperature, as demonstrated by all of the systems in Fig. 1. $B(T)$ does not change appreciably over a wide range of temperatures. The strong linear behavior approaching the zero-temperature limit is consistent with observations regarding Nb_3Te_4 and $(\text{PO}_2)_4(\text{WO}_3)_8$ (11, 12).

The rapid diminution of $A(T)$ at elevated temperature argues against phonon- (6) or excitation-based (13) scattering mechanisms as sources for the linear MR. It is also important to note that the low-temperature resistivity anomaly in $\rho(T, H = \text{constant})$ becomes more prominent in clean systems with higher residual resistivity ratio (RRR) values. In NbSe_3 , for example, the resistivity anomaly was only observed in samples with RRR

values of 284 and 87, but not of 31 (22). Previous experiments (23) on a Cr sample with an RRR of 1,760 found an MR ratio $\sim 3,000$ at 15 T and 4.2 K, which would nearly double the room-temperature resistance at zero field. This MR anomaly significantly surpasses the anomaly in our Cr sample with an RRR ~ 85 (Fig. 1D). $\rho(H)$ in Cr in general has a power exponent between 1 and 2 (23) depending on the degree of disorder and the relative field and crystalline directions.

The similarity in behavior between CDW and SDW systems (Figs. 1–3) suggests that both the low-temperature MR anomaly and its subset of low-field linear MR, $\Delta\rho \sim |H|$, may arise from a generic mechanism that is intrinsic to general features of the Fermi surface. We have performed density-functional theory (DFT) calculations for GdSi in the gapped SDW phase and, as

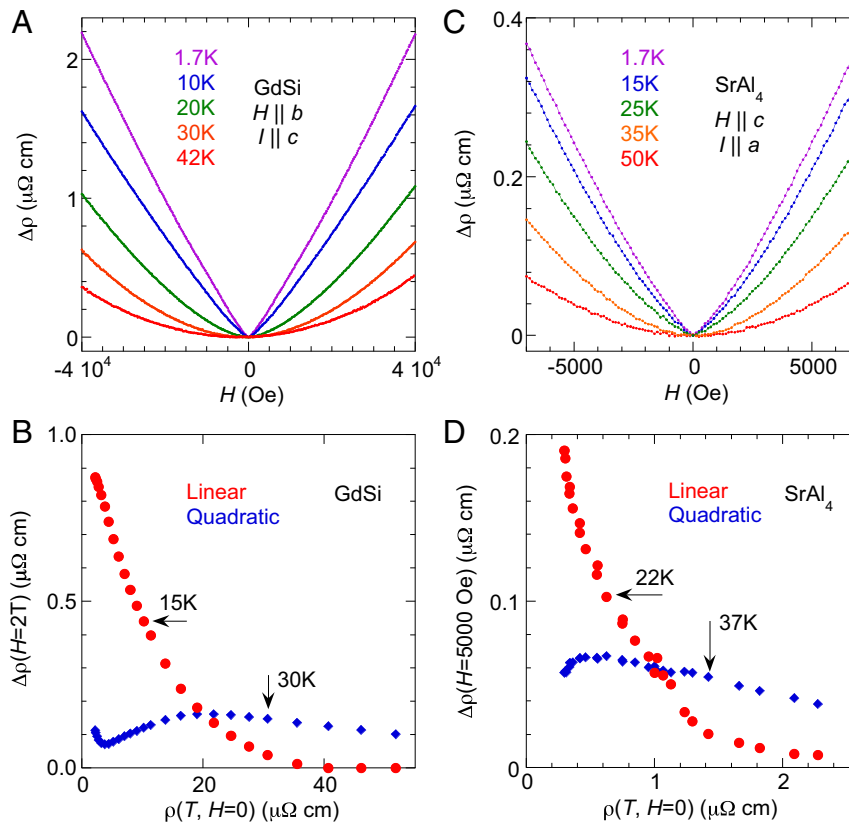


Fig. 3. Temperature evolution of linear and quadratic components in the prominent examples of the SDW system GdSi and the CDW system SrAl₄. (A and C) Representative curves of $\Delta\rho(H, T)$ are plotted together for varying temperatures. Fitting each curve with a sum of linear and quadratic terms, $\Delta\rho(H, T) = A(T)|H| + B(T)H^2$, gives the coefficients $A(T)$ and $B(T)$. (B and D) These coefficients are compared for their contributions [linear with $A(T)H$ and quadratic with $B(T)H^2$] to the MR under a field of 2 T for GdSi and 0.5 T for SrAl₄, respectively.

illustrated in Fig. 4, we find that its Fermi surface is marked by closed, bowtie or pinwheel-like volumes. These small volumes and their associated tight electron orbits contrast with the paramagnetic phase which has extended Fermi surfaces with nesting characteristics (14, 16). Similarly, the gapped Fermi surface of SrAl₄ is also closed in the form of several ellipsoids whose sizes are as small as 0.5% of the Brillouin zone volume (ref. 19 and schematically reproduced here in Fig. 4).

To validate our band structure calculations for GdSi, we probe the Fermi surface via cantilever torque magnetometry-based de Haas–van Alphen (dHvA) oscillations (Fig. 4) at the National High Magnetic Field Laboratory. Along the b axis, the three highest frequencies observed are 1,085, 508, and 432 T, which, respectively, enclose ~ 12 , 6, and 5% of the cross-sectional areas of the first Brillouin zone in the a – c plane. No frequency higher than 1,000 T was observed along either the c or a axes. The lowest frequency measured is 71.5 T for H along the c axis, which was also detected through a significant part of the b – c plane (Fig. 4F). The slowly varying form of $F(\theta)$ suggests an ellipsoidal Fermi surface that should present a small orbital for H along the b axis, although a corrugated cylinder cannot be ruled out without data over the full angular range. The 71.5-T frequency would represent an orbital of lateral size 0.05 – 0.1 Å⁻¹, enclosing 0.53% of the cross-sectional area of the first Brillouin zone in the a – b plane.

Discussion

Both GdSi and SrAl₄ have similarly high electron densities n in the gapped phase, with Hall coefficients R_H on the order of several 10^{-10} m³/C (refs. 14 and 19). With $\rho(T = 1.7$ K, $H = 0$) of

GdSi and SrAl₄, of 2.2 and 0.31 $\mu\Omega$ cm, respectively, and carrier masses all around unity, the cyclotron frequency ω_c is typically small. For GdSi with seven conduction electrons per formula unit (three Gd $5d$ - $6s$ and four Si $3s$ - $3p$ electrons), we estimate on average for all carriers $\omega_c\tau = H/\rho n e c = 4 \times 10^{-3}$ at $H = 2$ T for our sample. The criteria for quantum linear MR (5) are thus not satisfied under our measurement conditions. Additionally, itinerant carriers would not have time to circle a full Fermi surface orbital. Instead they would only follow a small arc before being scattered away by either phonons or disorder to an incoherent state on the Fermi surface.

In general, a small arc would induce a very small directional change to the propagation of the carrier. However, the local curvature of the orbit could become large enough that within τ a carrier could round a sharp corner to change its direction by a significant fraction of 2π before being scattered away. The turning process at sharp corners would dominate the magnetoresistive contributions from all other carriers at flat parts of Fermi surface because the curvature of a sharp corner could define a large but local angular frequency ω . Despite the corner representing only a portion of a full revolution, the most significant contribution to the MR would come from the effectively large $\omega_c\tau$. Carrier movement on other, flatter regions of the Fermi surface only weakly contributes to the MR with a conventional quadratic dependence.

Although the importance of local curvature has been recognized in the literature, most often it still leads to predictions of quadratic MR because of assumptions of finite-sized rounding of the Fermi surface feature (24, 25), perfectly suited to explain the large quadratic MR in the semimetals Bi, graphite, and WTe₂

power-law exponent of the field dependence would be expected to change from 1 to 2.

This mechanism for large, positive, and linear MR is well suited for explaining the behavior of a broad family of DW materials, and potentially other metallic incommensurate antiferromagnets in which large patches of Fermi surface are gapped out by the formation of long-range order (26). By removing sheet-like Fermi surfaces for open electron paths upon ordering, closed electron or hole pockets represent a generic topology for the remaining density of states. Although only representing a small portion of the Fermi surface, they can manifestly dominate the response to an applied field. In fact, as seen for SrAl₄, its linear MR at $T = 1.7$ K is of order 7,500% by $H = 14$ T, effectively matching the total electrical resistivity at room temperature.

Methods

Aligned single crystals of GdSi, Cr, and SrAl₄ were prepared in bar shapes of 1–3-mm length for magnetotransport measurements. Electrical leads were attached by silver epoxy in a four-lead geometry. High-field MR was measured using LakeShore LS372 resistance bridges and a 3708 preamplifier in either an 18-T superconducting magnet or a 35-T dc magnet (Cell 12) at the National High Magnetic Field Laboratory (NHMFL), Tallahassee, FL, using Helium-3 cryostat inserts to reach 0.34 K. The lower-field data were taken with similar electronics in a 14-T Physical Property Measurement System (PPMS; Quantum Design, Inc.) for $1.7 \text{ K} \leq T \leq 350 \text{ K}$. All low-field data were taken following protocols to remove potential trapped flux in the superconducting magnet. Nevertheless, we estimate that the zero-field value is only precise to 20 Oe.

We also characterize germane Fermi surface features of GdSi via dHvA measurements at the NHMFL, using cantilever torque magnetometry with Andeen-Hagerling AH2700A capacitance bridges in an 18-T superconducting magnet down to $T = 0.34$ K. A monotonic polynomial background was first removed, and the oscillating spectra were Fourier transformed to detect major frequencies. The data were further fit to the Lifshitz–Kosevich formula, as the oscillating amplitude from torque magnetometry depends on temperature and field as $\sim TH^{-1/2} \exp(-\alpha T_D/H) / \sinh(-\alpha T/H)$, where T_D is the Dingle temperature, and coefficient $\alpha = 14.69(m/m_e)$ Tesla/K, with the carrier mass m normalized by the free-electron mass m_e . This provides the fitting functional form in Fig. 4 for both carrier mass and Dingle temperature.

Density-functional theory calculation employed a $1 \times 2 \times 1$ supercell with a halved first Brillouin zone of nonmagnetic GdSi. This procedure approximates the real $\mathbf{Q} \sim (0, 0.493, 0.092)$ with a commensurate $(0, 1/2, 0)$ antiferromagnetic order (14).

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- Lifshitz IM, Azbel' Mla, Kaganov MI (1957) The theory of galvanomagnetic effects in metals. *Sov Phys JETP* 4:41–54.
- Ziman JM (1958) Galvanomagnetic properties of cylindrical Fermi surfaces. *Philos Mag* 3:1117–1127.
- Pippard AB (1989) *Magnetoresistance in Metals* (Cambridge Univ Press, Cambridge, UK), pp 35–39.
- Abrikosov AA (1998) Quantum magnetoresistance. *Phys Rev B* 58:2788–2794.
- Abrikosov AA (2000) Quantum linear magnetoresistance. *Europhys Lett* 49:789–793.
- Young RA (1968) Influence of localized Umklapp scattering on the galvanomagnetic properties of metals. *Phys Rev* 175:813–823.
- Naito M, Tanaka S (1982) Galvanomagnetic effects in the charge-density-wave state of 2H-NbSe₂ and 2H-TaSe₂. *J Phys Soc Jpn* 51:228–236.
- Song JCW, Rafael G, Lee PA (2015) Linear magnetoresistance in metals: Guiding center diffusion in a smooth random potential. *Phys Rev B* 92:180204.
- Xu R, et al. (1997) Large magnetoresistance in non-magnetic silver chalcogenides. *Nature* 390:57–61.
- Parish MM, Littlewood PB (2003) Non-saturating magnetoresistance in heavily disordered semiconductors. *Nature* 426:162–165.
- Ishihara Y, Nakada I (1983) Electrical transport properties of a quasi-one-dimensional Nb₃Te₄ single crystal. *Solid State Commun* 45:129–132.
- Rötger A, et al. (1994) Magnetotransport properties in the charge density wave state of the quasi-two-dimensional compounds (PO₂)₄(WO₃)_{2m}. *Europhys Lett* 25:23–29.
- Sinchenko AA, Grigoriev PD, Lejay P, Monceau P (2017) Linear magnetoresistance in the charge density wave state of quasi-two-dimensional rare-earth tritellurides. *Phys Rev B* 96:245129.
- Feng Y, et al. (2013) Incommensurate antiferromagnetism in a pure spin system via cooperative organization of local and itinerant moments. *Proc Natl Acad Sci USA* 110:3287–3292.
- Feng Y, et al. (2013) Evolution of incommensurate spin order with magnetic field and temperature in the itinerant antiferromagnet GdSi. *Phys Rev B* 88:134404.
- Feng Y, et al. (2014) Hidden one-dimensional spin modulation in a three-dimensional metal. *Nat Commun* 5:4218.
- Barak Z, Fawcett E, Feder D, Lorincz G, Walker MB (1981) Experimental and theoretical investigation of the magnetic phase diagram of chromium. *J Phys F Met Phys* 11:915–945.
- Feng Y, et al. (2005) Energy dispersive x-ray diffraction of charge density waves via chemical filtering. *Rev Sci Instrum* 76:063913.
- Nakamura A, et al. (2016) Characteristic Fermi surfaces and charge density wave in SrAl₄ and related compounds with the BaAl₄-type tetragonal structure. *J Alloys Compd* 654:290–299.
- Du X, Tsai S-W, Maslov DL, Hebard AF (2005) Metal-insulator-like behavior in semi-metallic bismuth and graphite. *Phys Rev Lett* 94:166601.
- Ali MN, et al. (2014) Large, non-saturating magnetoresistance in WTe₂. *Nature* 514:205–208.
- Coleman RV, Everson MP, Lu H-A, Johnson A, Falicov LM (1990) Effects of high magnetic fields on charge-density waves in NbSe₃. *Phys Rev B Condens Matter* 41:460–489.
- Arko AJ, Marcus JA, Reed WA (1968) High-field galvanomagnetic effects in antiferromagnetic chromium. *Phys Rev* 176:671–683.
- Allgaier RS, Perl R (1970) Weak-field galvanomagnetic properties of a new type of metallic model. *Phys Rev B* 2:877–883.
- Kesternich W (1976) Low-field magnetoresistance in metals. *Phys Rev B* 23:4227–4236.
- Elliott RJ, Wedgwood FA (1963) Theory of the resistance of the rare earth metals. *Proc Phys Soc* 81:846–855.