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DO CLOSE-IN GIANT PLANETS ORBITING EVOLVED STARS PREFER ECCENTRIC ORBITS?

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ABSTRACT

The NASA Kepler and K2 Missions have recently revealed a population of transiting giant planets orbiting moderately evolved, low-luminosity red giant branch stars. Here, we present radial velocity measurements of three of these systems, revealing significantly non-zero orbital eccentricities in each case. Comparing these systems with the known planet population suggests that close-in giant planets around evolved stars tend to have more eccentric orbits than those around main-sequence stars. We interpret this as tentative evidence that the orbits of these planets pass through a transient, moderately eccentric phase where they shrink faster than they circularize due to tides raised on evolved host stars. Additional radial velocity measurements of currently known systems, along with new systems discovered by the recently launched NASA TESS mission, may constrain the timescale and mass dependence of this process.

1. INTRODUCTION

The NASA Kepler mission has discovered thousands of extrasolar planets, allowing populations of planets orbiting different types of stars to be compared (Howard et al. 2012; Petigura et al. 2013; Dressing & Charbonneau 2015; Santerne et al. 2016; Fulton et al. 2017; van Sluijs & Van Eylen 2018). However, the population of planets around evolved stars remained poorly described because so few have been discovered to date, particularly at orbital distances of 0.5 AU or less (Sato et al. 2005; Johnson et al. 2010; Lillo-Box et al. 2014; Barclay et al. 2015; Jones et al. 2016).

It has been suggested that the planet population of evolved stars should look quite different from their main sequence counterparts due to dynamical interactions driven by stellar evolution (Veras 2016). Accelerated angular momentum exchange should cause the planet to spiral in to the host star (Zahn 1977; Hut 1981; MacLeod et al. 2018). This results in a scenario where orbital decay happens faster than circularization, producing a population of transient, moderately eccentric close-in planets around evolved stars that are not seen around main sequence stars (Villaver & Livio 2009; Villaver et al. 2014). The increase in planetary heating from both elevated

stellar irradiation and tides raised on the planet will likely also cause inflation of these planets at late times (Bodenheimer et al. 2001; Lopez & Fortney 2016).

Two well-characterized, close-in inflated giant planets orbiting moderately evolved, or low-luminosity red giant branch stars, K2-97b and K2-132b, were recently discovered by the K2 extension to the Kepler mission (Grunblatt et al. 2016, 2017). Here, we report new radial velocity (RV) measurements of these planets, as well as RV measurements of a previously validated planet orbiting an evolved star observed by the original Kepler mission, Kepler-643 (Huber et al. 2013; Morton et al. 2016). These measurements allow us to constrain the orbital eccentricities of these planets, which motivate an investigation of the orbital eccentricities of the population of planets around giant stars compared to dwarf stars.

2. OBSERVATIONS

RV measurements of K2-97, K2-132, and Kepler-643 were obtained between 2016 January 27 and 2018 February 1 using the High Resolution Echelle Spectrometer (HIRES) on the Keck-I Telescope at the Maunakea Observatory in Hawaii. Individual measurements and orbit solutions are shown in Figure 1. All RV spectra were obtained through an iodine gas cell. In order to constrain orbital parameters, we fit the radial velocity data using the publicly available software package RadVel (Fulton et al. 2018). The orbital period of the planets were fixed to published values from transit measurements (Morton et al. 2016; Grunblatt et al. 2017), while we fit for the semi-amplitude, phase, and modified eccentricity parameters of the orbit (Eastman et al. 2013). We also fit for an RV jitter term for our measurements and obtained a value between 5-10 m s⁻¹ for all systems studied here. We adopted the same method for determining RVs as described in Butler et al. (1996).

Since RV measurements are not usually taken at regular time intervals, data sampling is often uneven and thus introduces orbital parameter biases, potentially inflating eccentricities beyond their true value (Eastman et al. 2013). To ensure that our measured eccentricities are

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TABLE 1									
Close-In	Giant	PLANETS	Orbiting	Giant	Stars				

Name	Mass	Radius	Semimajor Axis	Eccentricity	Stellar Mass	Stellar Radius	Reference
K2-132b K2-97b K2-39b Kepler-643b Kepler-91b	$\begin{array}{c} 0.49 \pm 0.06 \; \mathrm{M_{J}} \\ 0.48 \pm 0.07 \; \mathrm{M_{J}} \\ 0.125 \pm 0.014 \; \mathrm{M_{J}} \\ 1.01 \pm 0.20 \; \mathrm{M_{J}} \\ 0.81 \pm 0.18 \; \mathrm{M_{J}} \end{array}$	$\begin{array}{c} 1.30 \pm \! 0.07 \; R_{J} \\ 1.31 \pm \! 0.11 \; R_{J} \\ 0.51 \pm 0.06 \; R_{J} \\ 1.14 \pm 0.05 \; R_{J} \\ 1.37 \pm 0.07 \; R_{J} \end{array}$	0.086 AU 0.081 AU 0.057 AU 0.126 AU 0.0731 AU	0.36 ± 0.06 0.22 ± 0.08 0.15 ± 0.08 0.37 ± 0.06 $0.04^{+0.06}_{-0.02}$	$\begin{array}{c} 1.08 \pm 0.08 \; \mathrm{M}_{\odot} \\ 1.16 \pm 0.12 \; \mathrm{M}_{\odot} \\ 1.19 \pm 0.08 \; \mathrm{M}_{\odot} \\ 1.15 \pm 0.12 \; \mathrm{M}_{\odot} \\ 1.31 \pm 0.1 \; \mathrm{M}_{\odot} \end{array}$	$\begin{array}{c} 3.85 \pm 0.13 \; \mathrm{R}_{\odot} \\ 4.20 \pm 0.14 \; \mathrm{R}_{\odot} \\ 2.93 \pm 0.21 \; \mathrm{R}_{\odot} \\ 2.69 \pm 0.11 \; \mathrm{R}_{\odot} \\ 6.30 \pm 0.16 \; \mathrm{R}_{\odot} \end{array}$	1, this work 1, this work 2 3, 4, this work 5
HD 102956b TYC3667-1280-1b	$0.96 \pm 0.05 \; \mathrm{M_{J}}$ $5.4 \pm 0.4 \; \mathrm{M_{J}}$	non-transiting non-transiting	0.081 AU 0.21 AU	0.05 ± 0.03 $0.04^{+0.04}_{-0.02}$	$1.70 \pm 0.11 \ \mathrm{M_{\odot}}$ $1.87 \pm 0.17 \ \mathrm{M_{\odot}}$	$4.4 \pm 0.1 \; \mathrm{R}_{\odot}$ $6.26 \pm 0.86 \; \mathrm{R}_{\odot}$	6 7

NOTE. — Reference key: 1. Grunblatt et al. (2017), 2. Petigura et al. (2017a), 3. Huber et al. (2013), 4. Morton et al. (2016), 5. Barclay et al. (2015), 6. Johnson et al. (2010), 7. Niedzielski et al. (2016).

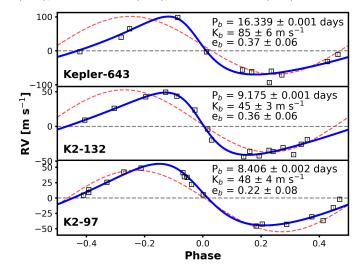


Fig. 1.— Keck/HIRES radial velocity observations of Kepler-643 (top), K2-132 (center) and K2-97 (bottom), three systems where close-in giant planets orbit evolved stars. All orbits display moderate eccentricities between 0.2 and 0.4. The planets appear to follow a trend, where those on longer orbits are more eccentric than those orbiting their host star more closely. Circular orbits are shown as red dotted lines for reference.

robust, we produced 100 artificial RV datasets of circular orbits for each system, with equivalent orbital periods, semi-amplitudes, and random scatter as measured in our real data, taken at the same times as our real measurements. We then recovered an orbit from each artificial dataset using the same techniques given for our real RV data. We find that the distribution of eccentricities recovered from fitting the artificial datasets is consistent with zero in all cases. For all best fit orbit solutions for the simulated, e=0 orbit generated data, we do not recover an eccentricity of greater than 0.1. We therefore conclude that the eccentricities found by our analysis are not due to sparse sampling of our RV measurements.

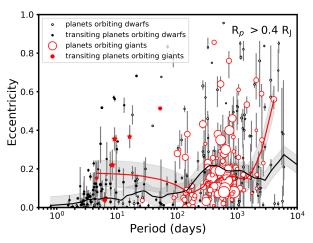
3. ECCENTRICITY DISTRIBUTIONS AROUND EVOLVED STARS

Figure 2 illustrates the population of known giant planets with published eccentricities orbiting giant stars as well as the equivalent planet population orbiting dwarfs in the orbital period and eccentricity plane (left) and the a/R_* and eccentricity plane (right). Planets are designated as giants if $R_p > 0.4~R_{\rm J}$. 419 dwarf star systems and 136 giant star systems with constrained eccentricities listed in the NASA Exoplanet Archive are included in our figure (Akeson et al. 2013). Transiting systems are shown as filled circles, while non-transiting systems

are shown as empty circles. For non-transiting systems, planet radii were estimated using the mass-radius relations of Chen & Kipping (2017). Distinctions as giant or dwarf star systems were made using the physically motivated boundaries in effective temperature and surface gravity described in Huber et al. (2016). Stellar parameters have been taken from the NASA Exoplanet Archive, and individual sources for all known close-in giant planets with published eccentricities orbiting giant stars are listed in Table 1. Our new RV measurements give tentative evidence that the dwarf and giant system eccentricity distributions are inconsistent at periods $\lesssim 50$ days and $a/R_* \lesssim 10$.

Figure 3 illustrates the cumulative distributions of eccentricities for various different planetary system samples analyzed here. When considering planets of all sizes, close-in planets show a tendency for low eccentricities. However, this preference is not as strong when considering only giant planets, likely due to trends related to planet multiplicity (Van Eylen & Albrecht 2015; Xie et al. 2016). Remarkably, comparing the population of giant planets orbiting at $\lesssim 50$ day orbital periods as well as all known planets around giant stars (red lines) to the equivalent planet population orbiting dwarf stars (black lines) illustrates a stronger preference for moderate eccentricities in giant star systems than is seen in dwarf star systems.

To evaluate the significance of the difference between the dwarf and giant star planet populations, we compared the median eccentricities for both populations (see Figures 2 and 3). We restrict our analysis to giant (> $0.4 R_{\rm J}$) planets with orbital periods between 4.5 and 30 days and published eccentricity constraints. This ensures that all planets compared here could have been detected around both dwarf and low-luminosity red giant branch stars observed by K2. Furthermore, this sample includes the closest-in known transiting planets orbiting evolved stars while rejecting the shortest period dwarf system planets, which likely would be engulfed by evolved stars due to their large sizes. It also minimizes biases due to planets found in surveys which were particularly wellsuited to discovering short-period giant planets on circular orbits around dwarf stars (e.g., WASP, Pollacco et al. 2006). Planets with published upper limits on eccentricity are treated as having circular orbits with error distributions that reach the listed upper limit at a $1-\sigma$ confidence interval. We find a median eccentricity of $0.152^{+0.077}_{-0.042}$ for close-in giant planets orbiting evolved stars, and a median eccentricity of $0.056^{+0.022}_{-0.006}$ for close-in



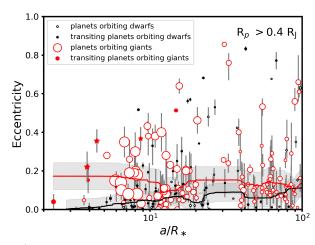


Fig. 2.— Left: Orbital period versus eccentricity for all giant ($>0.4~\rm{R_{J}}$) planets with published eccentricities orbiting giant and dwarf stars. Stellar radius scales with the size of the points; planets orbiting giant stars are shown in red, while planets orbiting dwarfs are shown in black. The systems with eccentricities measured in this study are highlighted as red stars. A locally weighted regression of the eccentricities of are shown by the solid black and red lines for the dwarf and giant star populations, respectively. Right: Same as left, except with $a/\rm{R_{*}}$ on the x-axis.

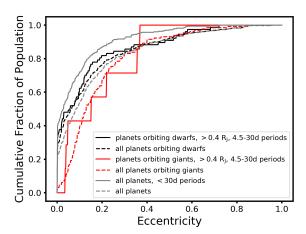


Fig. 3.— Cumulative eccentricity distributions of different populations of planets. Planets orbiting giant stars (red lines), particularly at periods of 30 days or less, display a preference for moderate eccentricities not seen in dwarf star systems (black lines).

giant planets orbiting dwarfs.

We also tested the sensitivity of these values to increasing the planet radius cut to $> 0.8~R_{\rm J}$, as well as adjusting the inner period bound between 3-8 days, and the outer period bound between 25-80 days. We find that our statistics are only significantly affected by changing the inner period bound, driven by the small number of close-in planets known orbiting evolved stars. Thus, we choose bounds to include all known close-in planets orbiting evolved stars while minimizing the number of close-in planets around dwarf stars without an evolved counterpart population.

To further quantify the significance of the eccentricity dichotomy between the populations of giant planets orbiting dwarf and giant stars, we calculate the AndersonDarling statistic, which is more robust to different-sized and small number distributions than similar tests such as the Kolmogorov-Smirnov statistic (Simpson 1951; Stephens 1974). We find that both samples are drawn from the same parent population in 6.3% or fewer of cases. Adjusting our planet radius and period cuts, we find that both samples are drawn from the same parent population in 3.8%–15.4% or fewer of cases for all tested samples. This range is dominated by stochastic variation due to the small sample of evolved systems.

As an additional test, we performed a Monte Carlo simulation in which we drew an equal number of eccentricity values from the eccentricity distributions of our biasresistant sample of close-in giant planets orbiting dwarf stars and giant stars in 4.5-30 days. We find that after repeating this process one million times, the random sample of planets drawn from the dwarf star sample has a similar or higher median eccentricity than the planets orbiting giant stars in 5.7% of cases, with a range of 4.1% to 16.7% for all period and radius ranges tested. We also performed the same test for the population of all close-in planets known around dwarf and giant stars, as well as all planets known around dwarf and giant stars, and find that the dwarf star sample has a similar or higher median eccentricity in 0.34% and 10.6% of cases, respectively.

Thus, based on our statistical tests, we conclude that close-in, evolved star system planets display different eccentricity characteristics than close-in dwarf star system planets at a 1- to 2- σ level. We note that this is a conservative estimate, as many early literature estimates of eccentricities for both types of systems may be biased toward higher eccentricities due to mischaracterization of systematic and astrophysical uncertainties (Eastman et al. 2013). More recent RV studies, using newer analysis packages such as RadVel, account for this artificial bias. Reanalysis of RV measurements used to constrain the population of planetary eccentricities could remove this bias, but is beyond the scope of this Letter.

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4. DISCUSSION

The formation of close-in giant planets is commonly explained by three different hypotheses: in situ formation, disk migration, and tidal migration (see Dawson & Johnson (2018) for a recent review). Populations of eccentric giant planets are generally viewed as evidence for tidal migration, as they cannot be explained by the other two prevailing mechanisms. Although these planets support tidal migration theory for close-in giant planet formation, we assert that unlike those around dwarf stars, these close-in giant planets are actively undergoing tidal migration induced by the late stage evolution of their host stars.

Models of the dynamical evolution of close-in giant planets can be strongly affected by the evolution of the host star (Villaver & Livio 2009; Villaver et al. 2014). The timescale of this dynamical evolution is defined by the tidal interactions between the planet and its host star. Following Villaver et al. (2014), the eccentricity evolution of a planetary orbit will be dominated by planetary tides driving orbit circularization on the main sequence, and stellar tides driving tidal inspiral on the red giant branch. For example, assuming equilibrium tides for our star and a standard Q formalism for planetary tides (Goldreich & Soter 1966; Hut 1981; Patra et al. 2017), the timescale for orbit circularization for K2-97b is ~ 4 Gyr, while the tidal inspiral timescale is $\lesssim 2$ Gyr. Orbital decay is driven more rapidly than eccentricity evolution as the stellar radius increases, producing a population of transient planets displaying moderate eccentricities at close-in orbits around evolved stars. This is consistent with our observations.

Villaver et al. (2014) also predict that more massive systems evolve more quickly toward lower eccentricities and semimajor axes. This is also tentatively supported by observations, as the most massive hosts in our sample also have the lowest eccentricity orbits (see Table 1). However, a larger sample of systems is needed to confirm this. Correlations between planet and star mass and composition and planetary orbital evolution have not yet been fully explored.

Tidal interaction and migration has long been thought to cause radius inflation in gas-giant planets (Bodenheimer et al. 2001; Ogilvie & Lin 2004; Storch & Lai 2014). Increased irradiation due to stellar evolution is also thought to be a source of planetary heating (Lopez & Fortney 2016). Two of the close-in evolved planets with new RV measurements presented here, K2-97b and K2-132b, show signs of being significantly inflated relative to similar planets seen orbiting main sequence stars (Grunblatt et al. 2017).

To evaluate the dominant radius inflation mechanism for these planets, we follow the prescription for tidal heating given by Miller et al. (2009) and Dobbs-Dixon et al. (2004), and assume synchronous rotation of the planet and tidal quality factors $Q_p = 10^4$ and $Q_* = 10^6$, within an order of magnitude of observed and model constraints (Patra et al. 2017; Gallet et al. 2017). We find that if the planets are actively circularizing, tidal evolution driven by the star can dominate planetary heating by an order of magnitude over irradiative mechanisms. Furthermore, tidal resonance locking may also greatly enhance tidal heating rates (Fuller 2017). Thus, planet radius inflation

for these systems may be driven solely by tidal processes.

However, a precise constraint on Q_p for these systems is necessary to construct a model of the planet eccentricity evolution. The value of Q_p considered above suggests the orbit circularization timescale is significantly shorter than the orbital decay timescale. In contrast, the observed eccentricities of these planet orbits suggests that orbit circularization and orbital decay are happening on similar timescales, implying $Q_* \sim Q_p$. This disagrees with predictions of Q_* for evolved stars (Gallet et al. 2017). Determining the causes of late stage planet inflation will require more in-depth characterization of the combined effect of increased irradiation and stellar tides on a larger sample of planets.

5. SUMMARY AND OUTLOOK

The NASA Kepler and K2 Missions have recently revealed a population of giant planets at small orbital separations around evolved stars. Here, we report radial velocity observations which show that a majority of these planets display moderate eccentricities, indicating a different evolutionary state for planets around giant stars than those orbiting main sequence stars. This late stage evolution is likely driven by the increase in size of the stellar radius and convective envelope, strongly increasing the angular momentum exchange between the star and the planet, causing the planet to circularize its orbit and spiral into the host star. These two components of orbital evolution must happen on timescales similar enough such that these migrating giant planets with moderate eccentricities appear to be relatively common around evolved stars (Villaver et al. 2014). These planets will thus allow constraints on the determination of the tidal quality factors Q_p and Q_* . Continued follow-up of low-luminosity red giant branch stars will allow estimation of close-in planetary occurrence around evolved stars (Grunblatt et al. 2018, in prep.), which will further constrain our understanding of planetary evolution and dynamical interactions within planetary systems.

Additional eccentricity constraints and more systems are needed in order to confirm the tentative result presented here. The NASA TESS Mission, launched earlier this year, will observe two orders of magnitude as many evolved stars as Kepler and K2, likely resulting in over 100 planet detections around evolved stars (Sullivan et al. 2015; Campante et al. 2016; Barclay et al. 2018). This detection of additional planets orbiting evolved stars will outline the diversity of all such systems, and the likelihood and timescale of planetary system disruption via stellar tides. With this information, we can investigate how quickly planets undergo orbital evolution around low-luminosity red giant branch stars, and at what point planets can no longer survive around giant stars, significantly distinguishing these systems from planet populations of main sequence stars.

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REFERENCES

Akeson, R. L., Chen, X., Ciardi, D. et al. 2013, PASP, 125, 989 Barclay, T., Endl, M., Huber, D. et al. 2015, ApJ, 800, 46

Barclay, T., Pepper, J., & Quintana, E. V. 2018, ArXiv e-prints, arXiv:1804:05050

Bodenheimer, P., Lin, D. N. C., & Mardling, R. A. 2001, ApJ, 548, 466

Butler, R. P., Marcy, G. W., Williams, E. et al. 1996, PASP, 108, $500\,$

Campante, T. L., Schofield, M., Kuszlewicz, J. S. et al. 2016, ApJ, 830, 138

Chen, J., & Kipping, D. 2017, ApJ, 834, 17

Dawson, R. I. & Johnson, J. A., ArXiv e-prints, arXiv:1801.06117
Dobbs-Dixon, I., Lin, D. N. C., & Mardling, R. A. 2004, ApJ, 610, 464

Dressing, C. D. & Charbonneau, D. 2015, ApJ, 807, 45 Eastman, J., Gaudi, B. S., & Agol, E. 2013, PASP, 125, 83 Fuller, J. 2017, MNRAS, 472, 1538

Fulton, B. J., Petigura, E. A., Blunt, S., & Sinukoff, E. 2018, ArXiv e-prints, arXiv:1801.01947

Fulton, B. J., Petigura, E. A., Howard, A. W., et al. 2017, ArXiv e-prints, arXiv:1703.10375

Gallet, F., Bolmont, E., Mathis, S., Charbonnel, C., & Amard, L. 2017, ArXiv e-prints, arXiv:1705.10164

Goldreich, P., & Soter, S. 1966, Icarus, 5, 375

Grunblatt, S. K., Huber, D., Gaidos, E., et al. 2016, AJ, 152, 185
Grunblatt, S. K., Huber, D., Gaidos, E., et al. 2017, AJ, 154, 254
Howard, A. W., Marcy, G. W., Bryson, S. T., et al. 2012, ApJS, 201, 15

Huber, D., Chaplin, W. J., Christensen-Dalsgaard, J., et al. 2013, ApJ, 767, 127

Huber, D., Bryson, S. T., Haas, M. R. et al. 2016, ApJS, 224, 2 Hut, P. 1981, A&A, 99, 126

Johnson, J. A., Aller, K. M., Howard, A. W., & Crepp, J. R. 2010, PASP, 122, 905

Jones, M. I., Jenkins, J. S., Brahm, R. et al. 2016, A&A, 590, A38 Kunitomo, M., Ikoma, M., Sato, B., Katsuta, Y., & Ida, S. 2011, ApJ, 737, 66

Lillo-Box, J., Barrado, D., Henning, T., et al. 2014, A&A, 568, L1 Lopez, E. D., & Fortney, J. J. 2016, ApJ, 818, 4

MacLeod, M., Cantiello, M., & Soares-Furtado, M. 2018, ApJ, 853, L1

Miller, N., Fortney, J. J., & Jackson, B. 2009, ApJ, 702, 1413Morton, T. D., Bryson, S. T., Coughlin, J. L., et al. 2016, ApJ, 822, 86

Niedzielski, A., Villaver, E., Nowak, G., et al. 2016, A&A, 589, L1 Ogilvie, G. I., & Lin, D. N. C. 2004, ApJ, 610, 477

Patra, K. C., Winn, J. N., Holman, M. J., et al. 2017, ArXiv e-prints, arXiv:1703.06582

Petigura, E. A., Howard, A. W., & Marcy, G. W. 2013, Proceedings of the National Academy of Science, 110, 19273

Petigura, E. A., Sinukoff, E., Lopez, E. D., et al. 2017a, AJ, 153, 142

Petigura, E. A., Howard, A. W., Marcy, G. W., et al. 2017b, ArXiv e-prints, arXiv:1703.10400

Pollacco, D. L., Skillen, I., Collier Cameron, A., et al. 2006, PASP, 118, 1407

Santerne, A., Moutou, C., Tsantaki, M., et al. 2016, A&A, 587, A64

Sato, B., Kambe, E., Takeda, Y., et al. 2005, PASJ, 57, 97 Simpson, P. B. 1951, The Annals of Mathematical Statistics, 22,

Stephens, M. A. 1974, Journal of the American Statistical Association, 69, 730

Storch, N. I., & Lai, D. 2014, MNRAS, 438, 1526

Sullivan, P. W., Winn, J. N., Berta-Thompson, Z. K. et al. 2015, ApJ, 809, 77

Van Eylen, V., & Albrecht, S. 2015, ApJ, 808, 126 Van Eylen, V., Albrecht, S., Gandolfi, D., et al. 2016, ArXiv

e-prints, arXiv:1605.09180 van Sluijs, L., & Van Eylen, V. 2018, MNRAS, 474, 4603

Veras, D. 2016, Royal Society Open Science, 3, 150571

Villaver, E., & Livio, M. 2009, ApJ, 705, L81 Villaver, E., Livio, M., Mustill, A. J., & Siess, L. 2014, ApJ, 794, 3

Xie, J.-W., Dong, S., Zhu, Z., et al. 2016, Proceedings of the National Academy of Science, 113, 11431

Zahn, J.-P. 1977, A&A, 57, 383