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Eccentricity Compensator for Log-Polar Sensor

Sota Shimizu, Member, IEEE, Joel W. Burdick, Member, IEEE,

Abstract—This paper aims at acquiring robust rotation, scale, and translation-invariant feature from a space-variant image by a fovea sensor. A proposed model of eccentricity compensator corrects deformation that occurs in a log-polar image when the fovea sensor is not centered at a target, that is, when eccentricity exists. An image simulator in discrete space remaps a compensated log-polar image using this model. This paper proposes Unreliable Feature Omission (UFO) that reduces local high frequency noise in the space-variant image using Discrete Wavelet Transform. It discards coefficients when they are regarded as unreliable based on digitized errors of the input image. The first simulation mainly tests geometric performance of the compensator, in case without noise. This result shows the compensator performs well and its root mean square error (RMSE) changes only by up to 2.54[%] in condition of eccentricity within 34.08[°]. The second simulation applies UFO to the log-polar image remapped by the compensator, taking its space-variant resolution into account. The result draws a conclusion that UFO performs better in case with more white Gaussian noise (WGN), even if the resolution of the compensated log-polar image is not isotropic.

I. INTRODUCTION

THE log-polar mapping, inspired by analytic formulation of biological study of the primate visual system [1], is a method of space-variant imaging that can reduce image data size drastically. Some computational models mapping the log-polar image from a uniform-resolution image have been reported [2][3]. In order to obtain the log-polar image, 2 types of actual fovea sensors have been proposed and developed. One is by a special CCD or CMOS log-polar chip, where united size of each photosensitive element increases as going to periphery [5]-[7]. The other is by a special fovea lens, such as a Wide-Angle Foveated (WAF) lens, where a projected image is distorted geometrically [8]-[10].

One of the most remarkable advantages of the log-polar image is to give us rotation and scale-invariant (RS-invariant) property [5][10], because its image resolution distributes isotropically and changes logarithmically from the image center towards the periphery. Assume a situation where a view direction (that is, the optical axis) of the fovea sensor is perpendicular to a planar target image (that is, without shear). If the fovea sensor is directed towards the image center of the target image accurately, we can obtain the RS-invariant feature from the image that is located at different distances and rotated about the optical axis. But if the fovea sensor is not centered at the image center correctly, a positional error between the optical axis and the image center (that is, so called, positional eccentricity) causes geometric deformation in the log-polar image and reduces the RS-invariant property (see Fig. 1(d) and (f), and also refer to [5]). We need to differentiate the deformation and image distortion. It should be noted that the latter occurs inherently due to space-variant sampling by the fovea sensor.

This paper discusses a method for acquiring rotation, scale, and translation-invariant (RST-invariant) feature, robust to the eccentricity and noise, from the log-polar image by the fovea sensor. The following 2 points are focused mainly.

- Remapping a new log-polar image from the original log-polar image by compensating the eccentricity in order to increase robustness of geometric RS-invariant property.
- Removing unreliable Wavelet Transform coefficients of the remapped image by taking space-variant resolution into account in order to improve image quality.

In terms of the first issue, we can see relevant ideas in some active visual tracking researches using the log-polar image (e.g. image warping technique [11] and a concept of virtual retina [12]). They are characterized as follows:

- (a) Cartesian coordinates have been used for computing image motion (that occurs due to active camera motion).
- (b) A remapped log-polar image (or displacement in the image) has been computed from the original image using the image motion.

In Cartesian space, translation caused by the positional eccentricity can be compensated easily. This property seems to have led to applying the affine model to compute the image motion [11][13]. In addition, the log-polar space is compatible with representing rotation and scaling [13]. Each of these ideas has performed its following correlation process well to increase stabilization of visual tracking in the central field of view (so-called, the fovea). However, it seems that the above researches have not discussed deeply enough with respect to quality of the remapped image (or the computed displacement), although it is space-variant. This problem motivates the second issue that pays attention to resolution of the log-polar image remapped from the original one, in order to estimate reliability of image components. The resolution of the log-polar image is space-variant inherently. In addition

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Sota Shimizu is with Division of Biology, California Institute of Technology, Pasadena, CA, 91125, USA (phone: +1-626-395-2359; e-mail: sato@caltech.edu).

J.W.Burdick is with Division of Engineering and Applied Science, California Institute of Technology, Pasadena, 91125, USA (e-mail: jwb@robotics.caltech.edu).

to that, that of the remapped one is anisotropic from the image center (see Fig. 1(c) and note the eccentricity gives space-variant resolution that is not isotropic, even if the deformation is corrected). Discrete Wavelet Transform (DWT) is well known as multi-resolution analysis [15] and it has been applied to foveation of the image [16]. The authors think this structure is suitable for representing the anisotropic log-polar image as mentioned above.

This paper is organized in the following way. Chapter II proposes a model of eccentricity compensator that corrects the deformation in the original log-polar image. An image simulator in discrete space remaps a compensated log-polar image by this model. Chapter III proposes Unreliable Feature Omission (UFO), that is, a method for reducing local high frequency noise from the space-variant image using Discrete Wavelet Transform. UFO is simulated and discussed by adding different 3 kinds of white Gaussian noise to the original log-polar image.

II. ECCENTRICITY COMPENSATOR

A. Acquisition of Wide-Angle Distorted Foveated Image

A distorted foveated image DF is computed from a Cartesian target image I. The image DF simulates an input image by the fovea sensor. In the following definitions, it is assumed that the image I is on the object plane and is shifted with eccentricity θ_{ε} in the ϕ_{ε} -direction. The θ_{ε} denotes angle between the optical axis of the fovea sensor and the straight line from the optical center O_c to the image center O of the image I, as in Fig. 2. The image center O is the origin of continuous coordinates (x, y). Discrete coordinates, (x_d, y_d) , of the image I are computed using an element size (δ_x, δ_y) .

$$\begin{cases} x_d = \left[x / \delta_x + 0.5 \right] \\ y_d = \left[y / \delta_y + 0.5 \right] \end{cases}$$
(1)

A direction (θ, ϕ) , from a point P(x, y) to the optical center O_c of the fovea sensor, is expresses as

$$\begin{cases} \theta = \tan^{-1} \{ \sqrt{(x + \varepsilon \cos \phi_{\varepsilon})^2 + (y + \varepsilon \sin \phi_{\varepsilon})^2} / L \} \\ \phi = \tan^{-1} \{ (y + \varepsilon \sin \phi_{\varepsilon}) / (x + \varepsilon \cos \phi_{\varepsilon}) \} \end{cases},$$
(2)

where L is a length from the optical center O_c to the object plane, and ε is positional eccentricity on the object plane.

$$\varepsilon = L \tan \theta_{\varepsilon} \quad , \tag{3}$$

Continuous coordinates (x', y') of the distorted foveated image *DF* are expressed as

$$\begin{cases} x' = \alpha_1(r(\theta)\cos\phi - r(\theta_\varepsilon)\cos(\phi_\varepsilon)) \\ y' = \alpha_1(r(\theta)\sin\phi - r(\theta_\varepsilon)\sin(\phi_\varepsilon)) \end{cases}, \tag{4}$$

where $r(\theta)$ shows the image height of the fovea sensor versus incident angle θ , α_1 is magnification of the image, θ_{ε} and ϕ_{ε} denote the direction from the image center *O* to the optical center O_c . The origin *O'* of the coordinates (x', y')corresponds to the direction $(\theta_{\varepsilon}, \phi_{\varepsilon})$ (that is, the image center *O*). Discrete coordinates, (x'_d, y'_d) , of the image *DF* are computed using an element size (δ'_x, δ'_y) .

$$\begin{cases} x'_d = \begin{bmatrix} x'/\delta'_x + 0.5 \end{bmatrix} \\ y'_d = \begin{bmatrix} y'/\delta'_y + 0.5 \end{bmatrix}$$
(5)



(a) Target image *I* (of 512x512)









(f) P₂ (of 128x64)

Fig. 1 (a) Target image *I*, (b) distorted foveated image *DF*, (c) undistorted foveated image *UDF*, (d) compensated log-polar image *CLP*, and (e) a polar image P_1 and (f)the original log-polar image P_2 in each eccentricity $\theta_e = 0[^\circ]$, 18.69[$^\circ$], and 34.08[$^\circ$] from the left



Fig. 2 Coordinate systems (2 points Q are identical with each other)

Advanced Wide Angle Foveated (AdWAF) model [10] is used as a model of the image *DF* in this paper. This model uses both Cartesian coordinates and logarithmic coordinates in both planar projection and spherical projection. The field of view (FOV) is divided into 4 areas, that is, fovea ($0 \le \theta \le \theta_0$), para-fovea ($\theta_0 \le \theta \le \theta_1$), near-periphery ($\theta_1 \le \theta \le \theta_2$), and periphery ($\theta_2 \le \theta \le \theta_{max}$). Figure 3 compares a simulated AdWAF image and a Cartesian image by pinhole camera (PHC) lens model. In this figure, the boundaries of FOV, that is, θ_0 , θ_1 and θ_2 , are 9.826 [°], 19.107 [°], and 34.715 [°], respectively. Intensity is changed in order to see each boundary intuitively. The image height $r(\theta)$ of the AdWAF model is defined in the following.



(a)AdWAF image (b)Cartesian image Fig. 3 Comparison of AdWAF image and Cartesian image

AdWAF model:

w

 $r = r_{\max} c_0 f_1 \tan \theta \qquad (0 \le \theta \le \theta_0),$

here
$$f_1$$
 is a focal length for planar projection.

$$r = r_{\max} \{ c_1 \log_a f_1 \tan \theta + d_1 \} \quad (\theta_0 \le \theta \le \theta_1), \tag{6}$$

where a basis *a* is defined as $a = \exp(1/f_1 \tan \theta_0)$. This corresponds to the brightest area in Fig. 3.

 $r = r_{\max} \{ c_2 \log_b(f_2\theta) + d_2 \} \qquad (\theta_1 \le \theta \le \theta_2),$

where f_2 is a focal length for spherical projection, and a basis *b* is defined as $b = \exp(1/f_2\theta_2)$.

$$r = r_{\max} \{ c_3 f_2 \theta + d_3 \} \qquad (\theta_2 \le \theta \le \theta_{\max}),$$

where r_{max} is the maximum image height when $\theta = \theta_{\text{max}}$, c_i (*i*=0, 1, 2, 3) is a scale modification factor for adjusting the image height, and d_i (*i*=1,2,3) is calculated by continuity of the image height and its magnification.

PHC lens:

$$r = \frac{r_{\max}c_0}{\tan \theta_{\max}} \tan \theta \qquad (0 \le \theta \le \theta_{\max}).$$

$$L = \frac{r_{\max}}{\tan \theta_{\max}}.$$

B. Geometric Modeling of Compensated Log-polar Image

As shown in Fig. 1(b), the image DF is distorted highly. Continuous coordinates, (x'', y''), of the undistorted foveated image UDF are expressed as

$$\begin{cases} x'' = \alpha_2 (L \tan \theta \cos \phi - \varepsilon \cos \phi_{\varepsilon}) \\ y'' = \alpha_2 (L \tan \theta \sin \phi - \varepsilon \sin \phi_{\varepsilon}) \end{cases}$$

where α_2 is magnification. The origin O'' of the coordinates (x'', y'') corresponds to the image center O. Discrete coordinates, (x''_d, y''_d) , of the image UDF are computed using an element size (δ''_x, δ''_y) .

$$\begin{cases} x_d'' = \left\lfloor x'' / \delta_x'' + 0.5 \right\rfloor \\ y_d'' = \left\lfloor y'' / \delta_y'' + 0.5 \right\rfloor \end{cases}.$$

Continuous coordinates, (η, ξ) , of the compensated log-polar image *CLP* (that is, a remapped log-polar image after correcting the deformation caused by the eccentricity) are computed from the coordinates (x'', y'').

$$\begin{cases} \eta = \tan^{-1}(y'' / x'') \\ \xi = \alpha_3(r(\Theta) - r_0) \end{cases} \qquad (\theta_0 \le \Theta \le \theta_1),$$

where r_0 is a radius from which the log-polar image starts, α_3 is magnification, and Θ is defined as

$$\Theta = \tan^{-1}(\frac{\sqrt{x''^2 + {y''}^2}}{L''})$$
 ,

where $L''=\alpha_2 L$. Discrete coordinates, (η_d, ξ_d) , of the image *CLP* are computed using an element size $(\delta_{\eta}, \delta_{\xi})$.

$$\begin{cases} \eta_d = \left[\eta / \delta_\eta + 0.5 \right] \\ \xi_d = \left[\xi / \delta_\xi + 0.5 \right] \end{cases} \qquad (\theta_0 \le \Theta \le \theta_1),$$

where the maximum integer of η_d is replaced with 0 (that is, the discrete value η_d corresponds to $0 \le \eta < 2\pi$).

Cartesian coordinates, (x''', y'''), of a compensated foveated image *CF* are expressed as

$$\begin{cases} x''' = \alpha_4 r(\Theta) \cos \eta \\ y''' = \alpha_4 r(\Theta) \sin \eta \end{cases}$$

where α_4 is magnification. Discrete coordinates, $(x_d^{''}, y_d^{''})$, of the image *CF* are computed using an element size $(\delta^{''}_x, \delta^{''}_y)$.

$$\begin{cases} x_d''' = \left[x''' / \delta_x''' + 0.5 \right] \\ y_d''' = \left[y''' / \delta_y''' + 0.5 \right] \end{cases}$$

C. Image Simulator in Discrete Space

In discrete space, image simulator of the proposed compensator outputs the image *CLP* using the following 2 mappings f and f_{CLP} .

$$f : I \to DF,$$

$$DF(x'_{d}, y'_{d}) = \begin{cases} 0 & , if \ N = 0\\ \frac{1}{N} \sum_{i \in S} I(x_{d \ i}, y_{d \ i}) & , if \ N \ge 1 \end{cases},$$
 (7)

where *N* is the number of points (x_{di}, y_{di}) $\{i \in S \mid x'_d \le x'_{di} \le x'_d + 1 \cap y'_d \le y'_{di} \le y'_d + 1\}$ corresponding to each point (x'_d, y'_d) . Note that the *N* is not constant with respect to each point (x'_d, y'_d) .

$$f_{CLP}: DF \to CLP,$$

$$CLP(\eta_d, \xi_d) = \begin{cases} 0 , if N = 0 \\ \frac{1}{N} \sum_{i \in S_{CLP}} DF(x'_{d\,i}, y'_{d\,i}), if N \ge 1 \end{cases}, \quad (8)$$

where *N* is the number of the points (x'_{di}, y'_{di}) { $i \in S_{CLP} | \eta_d \le \eta_{di} \le \eta_d + 1 \cap \xi_d \le \xi_{di} \le \xi_d + 1$ } corresponding to each point (η_d, ξ_d) .

Some methods for foveation and cortical mapping are known [2]-[4]. The mappings f and f_{CLP} denote foveation and a kind of cortical mapping, respectively. The latter can be called log-polar remapping. These mappings formulize how the *N*-multiple points correspond to each point in the remapped image in addition to geometric modeling. It is noted that the proposed image simulator computes intensity of each point in a different way from the above methods [2]-[4], taking the fovea lens into consideration. This mapping way is discussed again in next chapter, with respect to digitized errors of the remapped image.

D. Performance Test of Geometry

In the following simulation, a boundary between fovea and para-fovea is defined as $r_0 = r_{\text{max}} c_1 f_1 \tan \theta_0$ in the AdWAF model. Figure 1(a) shows a target image *I* of 512x512 [pixels], and Fig. 1(b) shows the distorted foveated image *DF* of 128x128 [pixels], simulated from the image *I* using the mapping *f* by eq.(7) where the r_{max} of the AdWAF model is 36 [pixels], in 3 cases of eccentricity $\theta_c = 0$ [°], 18.69 [°] and 34.08 [°] (in condition of $\delta = \delta_x = \delta_y$ and $\phi_c = 0$). Figure 1(d) shows the compensated log-polar image *CLP* of 128x64 [pixels] that corresponds to the para-fovea by eq. (6) where $\theta_0 = 9.826$ [°] and $\theta_1 = 19.107$ [°]. In order to test the compensator, a polar image P_1 (Fig. 1(e)) and the original log-polar image P_2 (Fig. 1(f)) of 128x64 [pixels] are computed from the image *DF* and compared with the image *CLP*. The image P_1 has polar coordinates (r', ϕ') around the origin O'. The image P_2 has polar coordinates $(r(\theta), \phi)$ around the optical axis. Their discrete images are represented by $P_1(r'_d, \phi'_d)$ and $P_2(r_d, \phi_d)$, respectively. The compensator corrects the deformation of the log-polar image well in each eccentricity, although the resolution of the image *CLP* distributes anisotropically. It should be noted that this comparison takes practical use of the fovea sensor by the fovea lens and log-polar chip into account. In order to understand effect of the compensator more intuitively, the undistorted foveated image (*UDF*) is also shown in Fig. 1(c). Note the right eye of the woman is always located nearly at the origin O'' (center) in each image *UDF*.

The image CLP is estimated using root mean square error (RMSE) from a model log-polar image LP, acquired from the image I (Fig.4). The RMSE E is defined as

$$E = \sqrt{\frac{\left\|CLP - LP\right\|^2}{N_\eta \cdot N_\xi}}$$

where N_{η} and N_{ξ} shows the size of the log-polar image.







Figure 5 compares RMSE of the image P_1 (broken line), the image P_2 (dashed line) and the image CLP (solid line) versus the eccentricity θ_{ε} (when $\phi_{\varepsilon} = 0$). The RMSE of the image CLP is smaller in all incident angles than those of the images P_1 and P_2 . This means that the compensator corrects the deformation in the images P_1 and P_2 well. However, the RMSE of the image CLP increases gradually as the eccentricity gets larger, because the intensity of more points in the image CLP is computed from lower-resolution part (like the periphery) of the image DF (the intensity from the lower-resolution part has larger error than higher-resolution one). The RMSE of the image CLP changes by up to 2.54[%], in condition of the eccentricity within $\theta_{\varepsilon} = 34.08$ [°].

The log-polar image acquired from a uniform-resolution image such as the image I is space-variant inherently, however, its resolution changes isotropically. When a low-pass filter is used for such space-variant image in order to reduce noise, not only noise but also fine information is lost from the original image. In addition, if the eccentricity exists, the resolution of the image *CLP* is not only space-variant but also anisotropic. In order to estimate the resolution, this paper uses digitized errors, $\Delta \eta$ and $\Delta \xi$, in the η and ξ -directions of the image *CLP*. They are computed from digitized errors, $\Delta \theta$ and $\Delta \phi$, in the radial and tangential directions of the image *DF* (as an input image by the fovea sensor), respectively.

$$\begin{cases} \Delta \eta = \left| \frac{\partial \eta}{\partial \theta} \right| \cdot \Delta \theta + \left| \frac{\partial \eta}{\partial \phi} \right| \cdot \Delta \phi \\ \Delta \xi = \left| \frac{\partial \xi}{\partial \theta} \right| \cdot \Delta \theta + \left| \frac{\partial \xi}{\partial \phi} \right| \cdot \Delta \phi \end{cases}$$
(9)

Fourier-Mellin Transform (FMT) is well known as a method for registering RST-invariant feature [18]-[20]. FMT reduces the influence of the eccentricity by extracting translation-invariant property based on Fourier Transform, while its feature is influenced by the anisotropic space-variant resolution because the feature is computed from Cartesian image (see the image UDF). On the other hand, the proposed compensator computes feature using log-polar geometry as in the image *CLP*. A method for acquiring feature, more robust to the eccentricity and noise, from the anisotropic space-variant image is proposed in the next chapter.

III. UNRELIABLE FEATURE OMISSION

A. Definition for Space-variant Image

If the image *CLP* is up-sampled from the low-resolution part of the image *DF* not fulfilling the sampling theorem, alias occurs as noise. This noise appears in components more than some frequency. Unreliable Feature Omission (UFO) discards such components using Discrete Wavelet Transform (DWT), because it is suitable for local noise reduction from the space-variant image. UFO is applicable also for the anisotropic space-variant resolution caused by the eccentricity, mentioned in the previous chapter. UFO is defined as follows:

1) Define DWT of the image *CLP* as ω . Its coefficient is expressed as $\omega_{j,k,i}^c$, where *j* is resolution level and *c* denotes diagonal, horizontal and vertical components as *d*, *h*, and *v*, respectively

2) If points in the image, corresponding to each coefficient $\omega_{j\,k,i}^c$, fulfill conditions $H \wedge \Xi$, H and Ξ in each case of c=d, h and v, respectively, discard the coefficient (set it as zero) as to determine a matrix v of wavelet coefficients.

$$\begin{split} H &: \Delta \eta (\frac{k \cdot N_{\eta}}{2^{j-1}} + m, \frac{2l \cdot N_{\xi}}{2^{j-1}} + n) > \frac{4\pi M_{f}}{2^{j-1}} \\ &\Xi &: \Delta \xi (\frac{k \cdot N_{\eta}}{2^{j-1}} + m, \frac{2l \cdot N_{\xi}}{2^{j-1}} + n) > \frac{4N_{\xi} \cdot M_{f}}{2^{j-1}} \end{split}$$

where M_f is a parameter regulating accuracy of the digitized error in sub-pixel order. The *m* and *n* are integer determined by the resolution level *j*.

3) Define an image U by Invert Discrete Wavelet Transform (IWDT) of the v.

B. Performance Test of Compensated Log-polar Image

The image *CLP* is expressed as $DF + e \mapsto^{f_{CLP}} CLP$ when white Gaussian noise (WGN) *e* is added to the image *DF*. Figure 6 shows the RMSE of the image before UFO (by a broken line), the image *U* after UFO (by a solid line) versus the eccentricity θ_{ε} (when $\phi_{\varepsilon}=0$). The RMSE is computed from the model log-polar image *LP*. This simulation uses Haar wavelet for UFO in conditions of $N_{\eta}=2N_{\xi}=128$, and M_f =1.0. Circle, triangle and square show cases when the WGN is 0, 5 and 10[%], respectively. The RMSE is computed as an average of 100 times repetition.

In each case of the WGN, the RMSE increases gradually as the eccentricity gets larger. It is noted that the RMSE after UFO increases more gently than that before UFO. This means UFO performs better for removing unreliable DWT coefficients as the image CLP is remapped from the lower-resolution part of the image DF. When the WGN is 5 and 10[%], UFO increases quality of the image CLP by reducing local noise (UFO works better in case with more noise), even if the space-variant resolution is not isotropic. However, when the WGN is 0[%], the RMSE after UFO is slightly larger than that before UFO. The high level coefficients, removed by UFO, seem to include not only noise but also a part of the original signal. The following 2 reasons are guessed. One is that the distribution of the errors $\Delta \eta$ and $\Delta \xi$ is not approximated sufficiently to a dyadic pyramid. The other is that actual errors of $\Delta \eta$ and $\Delta \xi$ are smaller than estimated errors by eq. (9), because the image CLP uses a sort of moving average when it is remapped from the image DF as by eq. (8). Figure 7 compares with the RMSE when the regulating parameter $M_f = 1.5$. The RMSE by $M_f = 1.5$ is much closer to that before UFO than that by $M_f = 1.0$. This result is consistent with the above guess.



Fig. 7 RMSE when the regulating parameter M_F is changed



Fig. 9 *CF* when $\theta_{\varepsilon} = 0[^{\circ}]$, 18.69[$^{\circ}$], and 34.08[$^{\circ}$] from the left

IV. CONCLUSION

In the first simulation, it has been demonstrated that the eccentricity compensator performs well for correcting the deformation using log-polar geometry. The RMSE of the image *CLP* changes by up to 2.54[%], in condition of the eccentricity within θ_{ε} =34.08[°]. In the second simulation, it has been demonstrated that UFO performs better in case with more white Gaussian noise (WGN), even if the resolution of the image *CLP* is not isotropic. As future works, each of these methods will be extended to the affine model and different type of wavelet, respectively. Such improvements lead to more practical use and better performance.

Lastly, a mapping f'_{CF} from the image DF to the compensated foveated image CF is defined as eq. (10).

$$f'_{CF} : DF \to CF,$$

$$CF(x''_{d}, y''_{d}) = \begin{cases} 0, & \text{if } N = 0 \\ \frac{1}{N} \sum_{i \in S'_{CF}} DF(x'_{d\,i}, y'_{d\,i}), & \text{if } N \ge 1 \end{cases}, \quad (10)$$

where *N* is the number of the points $(x'_{di}, y'_{di}) \{i \in S'_{CF} | (x'_d \le x'_{di} \le x'_d + 1) \cap (y'_d \le y'_{di} \le y'_d + 1)\}$ corresponding to each point (x''_d, y''_d) .

Figure 9 shows the image CF by eq. (10). The resolution distributes more anisotropically as the eccentricity gets larger. This mapping denotes a combination of the fovea sensor and the eccentricity compensator.

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REFERENCES

- E.L.Schwartz, "Spatial mapping in the primate sensory projection: Analytic structure and relevance to perception", Biological Cybernetics, Vol.29, pp.181-194, 1977.
- [2] G.Sandini and V.Tagliasco, "An anthropomorphic retina-like structure for scene analysis", Computer Graphics and Image Processing, 14, pp.365-372, 1980.
- [3] M. Bolduc and M. D. Levine, "A Review of Biologically-Motivated Space-Variant Data Reduction Models for Robotic Vision", Computer Vision and Image Understanding, vol.69, No.2, pp.170-184, 1998.
- [4] S. W. Wilson, "On the retino-cortical mapping", International Journal on Man-Machine Studies, vol. 18, pp.361-389, 1983.
- [5] F.Berton, G.Sandini and G.Metta, "Anthropomorphic Visual Sensors, Encyclopedia of Sensors", Edited by C.A. Grimes, E.C.Dickey and M.V.Pishko, Vol. 10, pp. 1-16, 2005.
- [6] J.Van der Spiegel, G.Kreider, C.Claeys, I.Debusschere, G.Sandini, P.Dario and et al., "A foveated retina-like sensor using CCD technology", Analog VLSI Implementations of Neural Networks. Kluwer, C.Mead and M.Ismail, Boston, 1989.
- [7] R.Wodnicki, G.W.Roberts and M.D.Levine, "A foveated image sensor in standard CMOS technology", In Custom Integrated Circuits Conference, Santa Clara, California, May 1995.
- [8] S.Shimizu, et.al., "Vision Sensor with Wide angle and High Distortion lens", Video proceedings of IEEE International Conference on Robotics and Automation, Visual Sensing 3, May 1995.
- [9] Y.Kuniyoshi, N.Kita, K.Sugimoto, et.al., "A Foveated Wide Angle Lens for Active Vision", Proc. of IEEE International Conference on Robotics and Automation, pp.2982-2988, May 1995.
- [10] S,Shimizu, "Wide-Angle Foveation for All-Purpose Use", IEEE transaction on robotics (in review)
- [11] A.Bernardino, J. Santos-Victor and G. Sandini, "Foveated active tracking with redundant 2D motion parameters", Robotics and Autonomous System 39, pp. 205-221, 2002.
- [12] F. Panerai, C. Capurro and G. Sandini, "Space Variant Vision for an Active Camera Mount", Proc. of SPIE Vol.2488, pp. 284-296, Visual Information Processing IV, June 1995.
- [13] C. Capurro, F. Panerai and G. Sandini, "Space Variant Vision for an Active Camera Mount", International Journal of Computer Vision, Vol.24, No.1, pp. 79-94, 1997.
- [14] A.Bernardino and J. Santos-Victor, "Binocular Tracking: Integration of Perception and Control", IEEE Transaction on Robotics and Autonomation, Vol. 15, No. 6, pp. 1080-1094, 1999.
- [15] S.Mallat, "A theory for muliresolution signal decomposition: the wavelet representation", IEEE Transaction on Pattern Analysis and Machine Intelligence, Vol.11 pp. 674-692, 1989
- [16] E.C.Chang and C.Yap, "A wavelet approach to foveating images", Proc. of ACM symposium on Computational Geometry, pp. 397-399, 1997
- [17] I. Daubechies, "Ten Lecture on Wavelets", SIAM Philadelphia, 1992
- [18] D.Casasent and D.Psaltis, "Position, Rotation and Scale-invariant Optical Correlation", Applied Optics, Vol. 15, pp.1795-1799, 1976.
- [19] B.S.Reddy and B.N. Chatterji, "An FFT-based Technique for Translation, Rotation and Scale-Invariant Image Registration", IEEE Transactions on Image Processing, Vol.5, No.8, pp.1266-1271, 1996.
- [20] G. Wolberg and S. Zokai, "Robust Image Registration using Log-polar Transform", Proc. of IEEE International Conference on Image Processing, Vol. 1, pp. 493-496, September 2000.