Complex lasso: new entangled motifs in proteins

Supplementary Material

Wanda Niemyska, Pawel Dabrowski-Tumanski, Michal Kadlof, Ellinor Haglund, Piotr Sułkowski and Joanna I. Sulkowska

Contents

1	Construction of minimal surfaces	1
	1.1 Area Minimizing	3
	1.2 Laplacian Fairing	3
	1.3 Edge Swapping	4
	1.4 Initialization	5
	1.5 Identification of lasso types	5
2	Details of protein reconstruction	7
3	Full list of proteins	10
4	Posttranslational modifications	23
5	List of multimeric proteins	25
6	Complex lasso classification based on CATH database	26
7	Examples of proteins with various lasso structures	27
8	Analysis of proteins with small covalent loops	31
9	Mini-proteins	33
10	Structural alignment of proteins with L_6 lasso type	35

1 Construction of minimal surfaces

As described in the main manuscript, we define complex lassos as configurations in which backbone tails pierce through a surface spanned on loop formed by a part of the backbone chain. We note, that our procedure could be as well applied to any other well defined loop, possibly in other (bio)polymers. We classify lassos with respect to the number of crossings (piercings) through this surface. Note that on a fixed boundary (the covalent loop) in \mathbb{R}^3 one can span an infinite number of surfaces. Therefore an unambiguous definition and construction of such surface is crucial for our work.

In our analysis we have decided to work with minimal surfaces. Intuitively, mininmal surface is a surface that would be formed by a soap bubble spanned on a given boundary. There are several equivalent definitions of such surfaces (connecting various mathematical disciplines). One of them is the local minimization condition: a surface $M \subset \mathbb{R}^3$ is minimal if and only if every point $p \in M$ has a neighborhood with the smallest area relative to its boundary. Notice that this is a local property: for a fixed global boundary there might be many such surfaces, possibly with different (smaller) global area. In our applications however surfaces determined with the local condition were sufficient. It can be shown that with appropriate assumptions the minimal surfaces can be equally well defined as a critical point of the Dirichlet energy functional, or as a surface with vanishing mean curvature.

In practical applications we need to work with discrete, triangulated versions of minimal surfaces, approximating the smooth surface. We construct such triangulated surfaces using discrete analogs of local area minimization and minimal Dirichlet energy conditions. The boundary of a triangulated surface is also discretized, being the polygonal chain in \mathbb{R}^3 with vertices in positions of $C\alpha$ atoms of the loop.

There are several algorithms, used in particular in computer graphics, that determine such triangulations. In our work we implemented a slightly modified version of an algorithm discussed in [1]. The initial data for this algorithm consists of coordinates of n vertices in the covalent loop, and the number of triangles in the triangulation that we are going to construct. This number allows to adjust the level of details of the resulting mesh – the larger the number, the surface is approximated more accurately. Once some initial mesh has been specified (as described in section 1.4 below), we iteratively adjust it by performing three operations that minimize the (local) area and the Dirichlet energy: Area Minimizing, Laplacian Fairing and Edge Swapping.

The scheme of applied algorithm is as follows [1]:

- 1. Initialization
- 2. Edge Swapping
- 3. DO {
- 4. DO Laplacian Fairing WHILE (area change $> \epsilon_1$)
- 5. Edge Swapping
- 6. DO Area Minimizing WHILE (area change $> \epsilon_2$)
- 7. Edge Swapping
- 8. } WHILE (area change > ϵ_0)

Positive constants ϵ_0 , ϵ_1 and ϵ_2 above are three fixed tolerance parameters – we quit the iteration if the modification of a triangulation in a given step does not change the surface area sufficiently (more than the relevant ϵ parameter).

In what follows we discuss each step of the algorithm in more detail. We use the similar notation as in [1]. A triangular mesh M is represented as a triple $\langle I, P, T \rangle$, where $I = \{1, 2, \ldots, N\}$ is the set of its vertices, $P: I \to \mathbb{R}^3$ is a mapping assigning each vertex

index its position in 3-dimensional space, and T is a set of triangles. Each triangle $t \in T$ is represented as an ordered triple $t = \langle i, j, k \rangle$ for $i, j, k \in I$ (with the vertices positions at P(i), P(j) and P(k)). For simplicity we write $P_i \equiv P(i)$. Furthermore we assume that first n indices in I correspond to the fixed vertices of the boundary polygon (the covalent loop in a protein); to adjust the triangulation we can change locations of last N - n vertices.

1.1 Area Minimizing

The area A of the mesh $M = \langle I, P, T \rangle$ is the sum of the areas of all triangles from the set T

$$A(M) = \sum_{t = \langle i, j, k \rangle \in T} \frac{1}{2} |P_j P_k \times P_j P_i|.$$
(1)

In the process of Area Minimizing (step 6 in our algorithm) we adjust coordinates P_{n+1}, \ldots, P_N in order to minimize the value area functional A(M). To this end we need to find a solution of the system of equations $\frac{\partial A(M)}{\partial P_h} = 0$, for all $h \in \{n+1, \ldots, N\}$. This set is equivalent to [1]:

$$P_{h} = -\left(\sum_{\langle h,j,k\rangle \in NT(h)} \frac{(P_{j}P_{k})^{2}I_{3} - (P_{j}P_{k})(P_{j}P_{k})^{T}}{|P_{j}P_{k} \times P_{j}P_{h}|}\right)^{-1} \times \sum_{\langle h,j,k\rangle \in NT(h)} \frac{(P_{j}P_{k} \cdot P_{j})P_{j}P_{k} - (P_{j}P_{k})^{2}P_{j}}{|P_{j}P_{k} \times P_{j}P_{h}|},$$
(2)

where $NT(i) \subseteq T$ is the set of all triangles containing vertex P_i , and I_3 is the 3×3 identity matrix. As the right-hand side of the above equation contains P_h , this is the iterative procedure of approximating the P_h position. This process can be repeated until the given tolerance ϵ_2 is reached.

1.2 Laplacian Fairing

With Laplacian Fairing we change the coordinates of mesh vertices in a way that minimizes the discrete version of Dirichlet energy functional. The continuous form of Dirichlet energy functional is

$$\frac{1}{2} \int_{\Omega} ||\nabla r(x)||^2 dV = \frac{1}{2} \int_{\Omega} \left(r_u^2(u,v) + r_v^2(u,v) \right) du dv, \tag{3}$$

where $r_u = \partial_u r$ and $r_v = \partial_v r$, Ω is a closed subset of \mathbb{R}^2 and $r: \Omega \to \mathbb{R}^3$ is a parametrization of the surface with boundary $\partial[r(\Omega)]$. It is known that critical points of the Dirichlet functional are harmonic functions, i.e. parametrizations r whose Laplacian vanishes, $\Delta r(u, v) = r_{uu} + r_{vv} = 0$. In discrete mesh we use a discrete version of the Laplacian, which at each vertex can be expressed by the so-called umbrella operator

$$\Delta(P_i) = \sum_{j \in N(i)} w_{ij}(P_j - P_i), \tag{4}$$

where $N(i) \subseteq I$ is the set of indices of vertices neighboring the vertex *i*, and w_{ij} are weights normalized so that $\sum_{j \in N(i)} w_{ij} = 1$ for each $i \in I$. As in the smooth case, the discrete Laplacian measures the difference between the value of a function at a particular point and the average of that function in its neighbors.

The weights w_{ij} in the formula (4) may be chosen in many different ways. In our implementation we define these weights by

$$w_{ij} = \frac{1}{2} (\operatorname{ctg}(\alpha_{1ij}) + \operatorname{ctg}(\alpha_{2ij})),$$

where α_{1ij} and α_{2ij} are angles in two triangles that share the edge $P_i P_j$, opposite to this edge. Our definition of weights differs slightly from the one given in [1]

In Laplacian Fairing we impose the condition that the discrete Laplacian vanishes, $\Delta(P_i) = 0$, for all interior vertices P_i , $i \in \{n + 1, ..., N\}$. This leads to a system of (N - n) (usually nonlinear) equations with (N - n) variables, which cannot be solved explicitly, but enables to approximate each P_i iteratively with:

$$\overline{P_i} = \sum_{j \in N(i)} w_{ij} P_j, \tag{5}$$

where weights w_{ij} are computed from the old locations P_i and P_j and $\overline{P_i}$ is the new location.

1.3 Edge Swapping

In the process of Edge Swapping we change the connectivity of the mesh in the way that it minimizes the local area. We consider all pairs of triangles which share one edge (e.g. $t_1 = \langle i, j, h \rangle$ and $t_2 = \langle i, j, k \rangle$) and replace the common edge $P_i P_j$ by the edge $P_h P_k$, if only it results in a triangulation of smaller area (see Fig. 1). Note that locations of the four vertices P_i, P_j, P_h, P_k remain unchanged – the only modification is in the connectivity of these vertices.

In a single Edge Swapping iteration we consider consecutively all edges in the mesh. If at least one swapping takes place (based on the above criteria) we continue this process. This operation is very fast and simple, however it returns just a local optimum (it is possible to find a global minimum, however with much higher computational cost).



Figure 1: Edge Swapping.

1.4 Initialization

The initial mesh may be somehow arbitrary; we construct it as follows. First we specify the number of triangles m in the triangulation we are after. Second, we specify the polygonal boundary P_1, \ldots, P_n consisting of (fixed) n points; to obtain more accurate triangulation, we can also divide boundary segments into shorter ones. Third, we compute the center of mass P_c of this boundary polygon and add s interior vertices along each line segment P_iP_c , $i \in \{1, 2, \ldots, n\}$. The number s is determined in order to obtain ca. m triangles in the mesh; some of these triangles are subsequently split into three smaller ones to get precisely m triangles in the mesh. Finally, we connect the vertices as shown in Fig. 2 (left panel). Our implementation differs slightly from original [1] shown in the right panel in Fig. 2. We reduce the number of edges sharing the center of mass P_c – this makes the central region of the triangulation less dense, and results in a smoother triangulated minimal surface.



Figure 2: Left panel: an example of the initial mesh used in our algorithm, with three additional vertices P_3 , P_7 and P_{11} in the boundary. Right panel: the initial mesh for the same input used in the implementation of the algorithm in [1].

1.5 Identification of lasso types

Once the triangulation of the minimal surface is determined we can verify which segments of the protein tail (or two tails) cross the surface. To identify a lasso type we also need to determine the direction of crossing (if only the surface is orientable which in our work always was the case). We denote the direction by drawing pierced triangles in different colors (e.g. in Fig. 3 blue and green triangles are pierced from opposite directions), and label the segments of a tail that pierce the surface with plus or minus signs respectively (e.g. tail segments denoted -10 and +289 in Fig. 3 pierce the surface from opposite directions).

Note that some proteins have complicated backbone configuration, giving rise to complicated, self-intersecting surfaces. In such cases it is convenient to present the triangulated surface as a planar barycentric embedding, in which each vertex of a triangulation is an average of vertices it is connected to. By a theorem by Tutte, such representation can be uniquely determined purely from the connectivity structure of a triangular surface. We use a well known algorithm by Tutte [3] to determine such baricentric representation (with hyperbolic modification of the positions of the vertices in order to present it in a more pleasing way). As an example, such planar barycentric embedding for triangulated minimal surface spanned on a covalent loop in the protein with PDB code 30m0, is shown in Fig. 3.



Figure 3: Left panel: cartoon representation of glutamate receptor, ionotropic kainate 5 protein (PDB code 30m0). Middle panel: triangulation of a minimal surface for 30m0 protein. The minimal surface, spanned on the covalent loop, is pierced twice by a tail (from opposite directions), through triangles in blue and green. Two cysteins and a cystein bond are shown in orange. Right panel: baricentric representation of a minimal triangulated surface for 30m0 protein. Two cysteins and a cystein bond comprise a part of the boundary and are shown in orange. Green and blue triangles are pierced from opposite sides by 10th and 289th tail segment respectively.

In our analysis we try not to include proteins whose lasso structure could be changed by thermal fluctuations. First, we impose a condition that there must be at least 10 amino acids separation between consecutive crossings (from opposite directions), i.e. a piece of a tail piercing a surface must be sufficiently "deep". There is one exception from this rule. Observe in Fig. 4 (right panel) that one may find a complex protein structure where a minimal surface spanned on a covalent loop, which has two distinct pieces located close to each other. In such case a tail may pierce both pieces of the surface and have less than 10 amino acids between these two crossings, but nonetheless we include such structures in our analysis. To detect such configurations automatically we compute (using Dijkstra algorithm) the shortest distance (along segments of the triangulation of the minimal surface) between two triangles that are pierced by a tail. If this distance is long enough (larger than 10 segments of the mesh) we include such a structure in our classification.

We also demand that the segment between the cysteine bridge and the first piercing includes at least 4 amino acids, see Fig. 4 (left panel).



Figure 4: Left: in 3utk protein there are less than 4 amino acids between the cysteine bridge and the first piercing, therefore we don't include this protein in our analysis. Right: in 4p1e protein a short (less than 10 amino acids) tail segment pierces two separated triangles in a surface than is bent – included in our analysis.

2 Details of protein reconstruction

Homologue structures were identified with psi-blast algorithm (implemented in MOD-ELLER software) run against all PDB sequences database provided by MODELLER team (http://salilab.org/modeller/downloads/pdball.pir.gz) with default parameters. Targets and template candidates were superimposed, and 3D alignment was calculated with Chimera [2] software. With these alignments, gaps coverage of found homologues was calculated. The first factor in the selection of a template was the overall percentage of the gap coverage in the alignment and the second the sequence similarity. All structures that had gaps longer than 8 amino acids without coverage were rejected. All structures left have been individually inspected with support of KnotProt database [4]. Doubtful structures were rejected.



Figure 5: Example of a gapped structure (PDB code 1a7s chain A), with missing coordinates of 4 amino acids from the loop region, that were reconstructed with Modeller to determine a complex lasso type. Thick lines denote the original PDB structures (a backbone CA chain trace), thin lines mark modeled loops that were used to identify a lasso type.

Type	PDB Codes
A	1auk_A 1evs_A 1fsu_A 1g3p_A 1jvq_A 1lsh_A 1me8_A 1p49_A 1uhg_A 1z70_A 2bb3_A 2j04_B 2qqh_A 2wsd_A 2z04_A 2zf8_A 3a77_A 3c64_A 3ep1_A 3g89_A 3hi7_A 3kt7_A 3m03_A 3m8n_A 3nir_A 3nt1_A 3pgb_A 3sxx_A 3tw5_A 3vuo_A 3wky_A 4cvu_A 4d9i_A 4db5_A 4gqz_A 4kc3_B 4l0k_A 4l1d_A 4m7g_A 4mai_A 4ncd_A 4nn5_A 4o4y_L 4o5j_A 4o5p_B 4o65_A 4o6k_A 4oh3_A 4osn_A 4p79_A 4pmk_A 4r7q_A 4tmd_A 4uvq_A 4uvu_A 4wat_A
В	 Iařs.A Iagq.A Ialu.A 1ax8.A 1b12.A 1b5k.A 1bcp.A 1bgc.A 1bqu.A 1bu8.A 1cru.A 1d2t.A 1dof.A 1dx4.A 1egi.A 1f01.A 12q.A 1f82.A 1f97.A 1fcq.A 1fo8.A 1g5g.A 1gcy.A 1gku.B 1gml.A 1gv9.A 1h30.A 1hc1.A 1huw.A 1jqA 1jdp.A 1jnd.A 1jn8.A 1jv5.A 1kl9.A 1kxo.A 1lntL A 1h7A 1hml.A 1m48.A 1ms9.A 1nff.A 1n8y.A 1ne2.A 1neu.A 1njr.A 1nko.A 1now.A 1nst.A 1o3u.A 1oi0.A 1olz.A 1omz.A 1p53.A 1p91.A 1pb7.A 1pgA.A 1qbw.A 1jpz.A 1jpu.A 1jzvA. 1ja5.A 1g5.A 1g5.A 1g91.A 1pb7.A 1pgu.A 1jzw.A 1kxo.A 1ix5j.A 1scf.A 1so7.A 1sgj.A 1t6c.X 1tfz.A 1tgz.A 1agx.A 1qbt.A 1r3e.A 1rxd.A 1s4n.A 1s5j.A 1scf.A 1so7.A 1sgj.A 1t6e X 1tfz.A 1tgz.A 1u5X.A 1uct.A 1ups.A 1ux6.A 1uzk.A 1v0w.A 1v0m.A 1va6.A 1w07.A 1w8a.A 1w8k.A 1x9d.A 1zecz.A 1zju.A 1yj.A 1yis.A 1z4v.A 1zk5.A 1zro.A 2acw.A 2arr.A 2b7n.A 2b91.A 2bec.A 2bgh.A 2bog.X 2bou.A 2bsy.A 2c2a.A 2c9k.A 2cdc.A 2d1g.A 2d1h.A 2ddf.A 2ddu.A 2de0.A 2di4 A 2dre A 2dvk.A 2e1v.A 2ecf.A 2eng.A 2fiy.A 2fi0.A 2ing.A 2ji9.A 2ji9.A 2ji0.A 2jid.A 2ji0.A 2jij.A 2ji0.A 2jiks.A 2mpr.A 2nsm.A 2mv2.A 2mxf.A 2myk.A 2co5n.A 2oay.A 2our.A 2yzs.A 2h2t.A 2beh.A 2bft.A 2bu1.A 2dv4.A 2uy2.A 2veq.A 2vl7.A 2yzm.A 2xv1.A 2wu2.A 2wdz.A 2wz59.A 2wc59.A 2w63.A 2w93.A 2w85.A 2wnf.A 2wnk.A 2wnv.A 2wy3.A 2x1q.A 2x2u.A 2x2u.A 2x2u.A 2x2i.A 2x3q.A 2x4i.A 2x4i.A 2xdv4.A 2yg2.A 2ykt.A 2ydv4.A 2yg2.A 2ykt.A 2ymo.A 2z2r.A 2z3q.A 2z4i.A 2zdb.A 23bu.D 3c3v.A 3g0.A 3g1.A 3g1.A 3g1.A 3b1b.A 3b1b.A 3b1k.A 3b1k.A 3b0k.A 3bwu.D 3c3v.A 3g0.A 3c10.A 3c1.A 3cqn.A 3cwx.A 32b.A 3422.A 3d5b.B 3d1q.J 3dx1.A 3c0g.A 3g2m.A 3gn.A 3gn.A 3gn.A 3gn.A 3gn.A 3gn.A 3g6.A 3g6.A 3g6.A 3g6.A 3g6.A 3g6.A 3g6.A 3g6.A 3g6.A 3g7.A 3ga.A 3gn.A 3gn.A 3gn.A 3gn.A 3gn.A 3gn.A 3gn.A 3gn.A 3g6.A 3g7.A 3ga.A 3gh.A 3gn.A 3gn.A 3gn.A 3gn.A 3gn.A 3gn.A 3gn.A 3g6.A 3g6.A

Table 1: A. PDB codes of proteins with chain annotation (the last letter), with positions of some atoms along the chain not determined experimentally, and for which it was impossible to determine whether the repaired model has correct complex lasso type. B. PDB codes of proteins with chain annotation (the last letter), with positions of some atoms along the chain not determined experimentally, whose chains and complex lasso type were successfully modeled.

3 Full list of proteins

PDB	Loop	Function	Organism	Organism
code	range	(classification)	Species	Genus
1AC5_A	79-345	Carboxypeptidase	Saccharomyces cerevisiae	Saccharomyces
1AHL_A	6-36	Neurotoxin	Anthopleura xanthogrammica	Anthopleura
1AHO_A	12-63	Neurotoxin	Androctonus australis	Androctonus
1AK0_A	72-217	Endonuclease	Penicillium citrinum	Penicillium
1AOC_A	60-161	Coagulation factor	Tachypleus tridentatus	Tachypleus
1AOZ_A	81-538	Oxidoreductase	Cucurbita pepo var. melopepo	Cucurbita
1ATA_A	22-60	Proteinase	Ascaris suum	Ascaris
1AX8_A	96-146	Cytokine	Homo sapiens	Homo
$1B8W_A$	16-32	Toxin	Ornithorhynchus anatinus	Ornithorhynchus
1BCP_A	41-201	Toxin	Bordetella pertussis	Bordetella
1BDS_A	6-32	Anti-hypertensive protein	Anemonia sulcata	Anemonia
1BEA_A	29-86	Serine protease inhibitor	Zea mays	Zea
$1BF0_A$	32-53	Calcium channel blocker	Dendroaspis angusticeps	Dendroaspis
1C01_A	11-64	Antimicrobial	Macadamia integrifolia	Macadamia
1C01_A	23-49	Antimicrobial	Macadamia integrifolia	Macadamia
1CCV_A	20-56	Hydrolase 3	Apis mellifera	Apis
1CFE_A	44-112	Pathogenesis-related	Solanum lycopersicum	Solanum
1CPY_A	56-298	Hydrolase	Saccharomyces cerevisiae	Saccharomyces
1CQ3_A	8-185	Cytokine	Cowpox virus	Orthopoxvirus
1D2S_A	164-188	Transport	Homo sapiens	Homo
$1D6B_A$	16-32	Toxin	Ornithorhynchus anatinus	Ornithorhynchus
1DOF_A	167-403	Lyase	Pyrobaculum aerophilum	Pyrobaculum
1DP4_A	164-213	Hormone/growth factor	Rattus norvegicus	Rattus
1DTV_A	18-62	Hydrolase	Hirudo medicinalis	Hirudo
1DTV_A	19-43	Hydrolase	Hirudo medicinalis	Hirudo
1DTV_A	22-58	Hydrolase	Hirudo medicinalis	Hirudo
1DYS_A	93-152	Cellulase	Humicola insolens	Humicola
1E4M_A	14-434	Hydrolase	Sinapis alba	Sinapis
1E4M_A	6-438	Hydrolase	Sinapis alba	Sinapis
1ESC_A	197-255	Hydrolase	Streptomyces scabiei	Streptomyces
1ETE_A	44-127	Cytokine	Homo sapiens	Homo
1FD3_A	15-30	Antimicrobial	Homo sapiens	Homo
1FJR_A	70-164	Signaling protein	Drosophila melanogaster	Drosophila
1FLC_A	126-174	Hydrolase	Influenza c virus	Influenzavirus C
1FLC_A	196-238	Hydrolase	Influenza c virus	Influenzavirus C
1FOB_A	253-311	Hydrolase	Aspergillus aculeatus	Aspergillus
1G66_A	147-179	Hydrolase	Penicillium purpurogenum	Talaromyces
$1G6X_A$	30-51	Hydrolase	Bos taurus	Bos
1GAK_A	60-134	Cell adhesion	Haliotis fulgens	Haliotis
1GP0_A	1598-1634	Receptor	Homo sapiens	Homo
1GXY_A	21-223	Transferase	Rattus norvegicus	Rattus
1H30_A	444-470	Growth arrest spec.	Homo sapiens	Homo
1H30_A	643-670	Growth arrest spec.	Homo sapiens	Homo
1HCN_B	23-72	Hormone	Homo sapiens	Homo
1HCN_B	26-110	Hormone	Homo sapiens	Homo
1HX2_A	21-60	Hydrolase	Bombina bombina	Bombina
1I1J_A	35-106	Hormone/growth factor	Homo sapiens	Homo
		• -	Ċ	ontinued on the next page

PDB	Loop	Function	Organism	Organism
\mathbf{code}	range	(classification)	Species	Genus
1I4U_A	51-173	Transport protein	Homarus gammarus	Homarus
1IJV_A	12-27	Defensin	Homo sapiens	Homo
1IYB_A	25-81	Hydrolase	Nicotiana glutinosa	Nicotiana
1JDP_A	168-216	Signaling protein	Homo sapiens homo sapiens	Homo
1JER_A	60-95	Electron transport	Cucumis sativus	Cucumis
1JFU_B	10-155	Membrane	Bradyrhizobium japonicum	Bradyrhizobium
1JLI_A	16-84	Cytokine	Homo sapiens	Homo
$1JY5_A$	26-84	Hydrolase	Calystegia sepium	Calystegia
$1JY5_A$	57-90	Hydrolase	Calystegia sepium	Calystegia
1KJ6_A	18-33	Antibiotic	Homo sapiens	Homo
1KTH_A	30-51	Structural protein	Homo sapiens	Homo
1KXO_A	42-170	Ligand binding	Pieris brassicae	Pieris
$1LE6_A$	48-122	Hydrolase	Homo sapiens	Homo
1LKI_A	12-134	Cytokine	Mus musculus	Mus
1LKI_A	18-131	Cytokine	Mus musculus	Mus
$1M4L_A$	138-161	Hydrolase	Bos taurus	Bos
1MC2_A	1050-1134	Toxin	Deinagkistrodon acutus	Deinagkistrodon
1MEG_A	153-204	Hydrolase	Carica papaya	Carica
1MJN_A	161-299	Immune system	Homo sapiens	Homo
1N1F_A	10-103	Immune system	Homo sapiens	Homo
1N2Z_A	183-259	Transport protein	Escherichia coli	Escherichia
1NF2_A	35-265	Structural protein	Thermotoga maritima	Thermotoga
1NSC_A	86-419	Hydrolase(o-glycosyl)	Influenza B virus	Influenzavirus B
1NYO_A	8-142	Immune system	Mycobacterium tuberculosis	Mycobacterium
10H1_A	16-55	Cysteine proteinase inh.	Staphylococcus aureus	Staphylococcus
10K0_A	45-73	Inhibitor	Streptomyces tendae	Streptomyces
1PB7_A	236-290	Ligand binding	Rattus norvegicus	Rattus
$1PZ7_A$	175-201	Structural protein	Gallus gallus	Gallus
1PZS_A	54-165	Oxidoreductase	Mycobacterium tuberculosis	Mycobacterium
$1Q25_A$	385-419	Protein binding	Bos taurus	Bos
1Q25_A	81-111	Protein binding	Bos taurus	Bos
1Q77_A	14-114	Structural protein	Aquifex aeolicus	Aquifex
1QCX_A	72-206	Lyase	Aspergillus niger	Aspergillus
$1QFT_A$	48-169	Ligand binding	Rhipicephalus appendiculatus	Rhipicephalus
$1QG8_A$	155-243	Transferase	Bacillus subtilis	Bacillus
$1 QGV_A$	38-79	Transcription	Homo sapiens	Homo
$1R8N_A$	44-89	Hydrolase	Delonix regia	Delonix
$1SCF_A$	43-138	Hormone/growth factor	Homo sapiens	Homo
1 SGL_A	26-84	Hydrolase	Trichosanthes lepiniana	Trichosanthes
1 SGL_A	57-90	Hydrolase	Trichosanthes lepiniana	Trichosanthes
$1 SHI_A$	5-33	Neurotoxin	Stichodactyla helianthus	Stichodactyla
$1SVB_A$	74-105	Viral	Tick-borne encephalitis virus	Flavivirus
$1T61_A$	164-222	Structural protein	Bos taurus	Bos
$1T61_A$	53-108	Structural protein	Bos taurus	Bos
1TAP_A	33-55	Proteinase	Ornithodoros moubata	Ornithodoros
$1TZP_A$	44-265	Hydrolase	Escherichia coli	Escherichia
$1U53_A$	65-148	Antibiotic	Necator americanus	Necator
1UDK_A	20-41	Unknown	Naja nigricollis	Naja
1UDK_A	7-37	Unknown	Naja nigricollis	Naja
			Co	ontinued on the next page

		Table 2 – contin	ued from the previous page	
PDB	Loop	Function	Organism	Organism
code	range	(classification)	Species	Genus
1UWC_A	29-258	Hydrolase	Aspergillus niger	Aspergillus
1UZK_A	1549-1574	Glycoprotein	Homo sapiens	Homo
1VF8_A	28-373	Immune system	Mus musculus	Mus
1W8K_A	265-363	Antigen	Plasmodium vivax	Plasmodium
1W8K_A	388-444	Antigen	Plasmodium vivax	Plasmodium
1WC2_A	30-69	Hydrolase	Mytilus edulis	Mytilus
1WC2_A	65-178	Hydrolase	Mytilus edulis	Mytilus
1WC2_A	72-157	Hydrolase	Mytilus edulis	Mytilus
1WKT_A	11-72	Toxin	Williopsis saturnus var. mrakii	Cyberlindnera
1WKT_A	27-58	Toxin	Williopsis saturnus var. mrakii	Cyberlindnera
1WQK_A	6-30	Toxin	Anthopleura elegantissima	Anthopleura
1WS8_A	58-92	Electron transport	Cucurbita pepo	Cucurbita
1X8Q_A	41-171	Ligand binding	Rhodnius prolixus	Rhodnius
1XTA_A	56-134	Toxin	Naja atra	Naja
1XTM_B	93-186	Structural protein	Bacillus subtilis	Bacillus
1YG9_A	51A-113	Hydrolase	Blattella germanica	Blattella
1YI9_A	81-126	Oxidoreductase	Rattus norvegicus	Rattus
1YS1_A	190-270	Hydrolase	Burkholderia cepacia	Burkholderia
1ZMI_A	3-18	Antimicrobial	Homo sapiens	Homo
1ZMM_A	4-19	Antimicrobial	Homo sapiens	Homo
$2B7U_A$	217-254	Hydrolase	Charybdis maritima	Drimia
$2B9L_A$	69-105	Immune system	Holotrichia diomphalia	Holotrichia
2BB6_A	3-252	Transport protein	Bos taurus	Bos
2BGH_A	25-89	Transferase	Rauvolfia serpentina	Rauvolfia
2C1C_A	138-161	Hydrolase	Helicoverpa zea	Helicoverpa
2CKS_A	166-406	Hydrolase	Thermobifida fusca	Thermobifida
2CMZ_A	68-114	Membrane	Vesicular stomatitis indiana virus	Vesiculovirus
2D5W_A	314-458	Peptide binding	Thermus thermophilus	Thermus
2DDU_A	1475-1522	Signaling	Mus musculus	Mus
2DRE_A	45-92	Plant protein	Lepidium virginicum	Lepidium
$2E1V_A$	125-433	Transferase	Chrysanthemum x morifolium	Chrysanthemum
2ENG_A	16-86	Hydrolase	Humicola insolens	Humicola
2ENG_A	87-199	Hydrolase	Humicola insolens	Humicola
2ENG_A	89-189	Hydrolase	Humicola insolens	Humicola
2ERF_A	153-214	Sugar	Homo sapiens	Homo
2F5X_A	142-178	Transport protein	Bordetella pertussis tohama I	Bordetella
2FMA_A	144-174	Metal binding	Homo sapiens	Homo
$2G5X_A$	32-214	Hydrolase	Lychnis chalcedonica	Silene
2GHV_E	366-419	Viral	Sars coronavirus	Betacoronavirus
2GUM_A	364-412	Viral protein	Human herpesvirus 1	Simplexvirus
2HCZ_X	42-70	Allergen 2	Zea mays	Zea
2HCZ_X	73-140	Allergen 2	Zea mays	Zea
2IKD_A	23-54	Hydrolase	Manduca sexta	Manduca
2IKE_A	83-113	Hydrolase	Manduca sexta	Manduca
$2J6D_A$	35-56	Toxin	Conus striatus	Conus
2JD4_A	2845-2870	Metal binding	Mus musculus	Mus
2JD4_A	3024-3055	Metal binding	Mus musculus	Mus
2JIG_A	195-230	Hydrolase	Chlamydomonas reinhardtii	Chlamydomonas
2JKS_A	66-77	Immune system	Toxoplasma gondii	Ioxoplasma
			Co	ontinued on the next page

PDB	Loop	Function	Organism	Organism
code	range	(classification)	Species	Genus
2JON_A	48-94	Allergen	Olea europaea	Olea
2JOP_A	60-125	Immune system	Homo sapiens	Homo
2JR3_A	16-32	Antimicrobial	Pelodiscus sinensis	Pelodiscus
2JTO_A	10-27	Hydrolase	Rhipicephalus bursa	Rhipicephalus
2JTO_A	47-64	Hydrolase	Rhipicephalus bursa	Rhipicephalus
2JX9_A	41-71	Cell adhesion	Mus musculus	Mus
2K8P_A	70-124	Signaling	Homo sapiens	Homo
2KER_A	43-70	Hydrolase	Streptomyces parvulus	Streptomyces
2KQA_A	20-57	Toxin	Ceratocystis platani	Ceratocystis
2KQA_A	60-115	Toxin	Ceratocystis platani	Ceratocystis
2KXI_A	67-128	Transferase	Neisseria meningitidis serogroup b	Neisseria
2L3O_A	43-106	Cytokine	Mus musculus	Mus
2LVX_A	408-437	Hydrolase	Schizosaccharomyces pombe	Schizosaccharomyces
2MJK_A	12-28	Antimicrobial	Gallus gallus	Gallus
2MM2_A	18-65	Plant protein	Pyrenophora tritici-repentis	Pyrenophora
2MN3_A	16-30	Antimicrobial	Ornithorhynchus anatinus	Ornithorhynchus
20IZ_D	130-161	Oxidoreductase	Alcaligenes faecalis	Alcaligenes
2OR7_A	38-90	Immune system	Mus musculus	Mus
20YA_A	446-507	Ligand	Mus musculus	Mus
2PE4_A	43-333	Hydrolase	Homo sapiens	Homo
2PMV_A	8-228	Transport protein	Homo sapiens	Homo
2PSP_A	58-84	Signaling	Sus scrofa	Sus
2PSP_A	8-35	Signaling	Sus scrofa	Sus
2PT5_A	10-110	Transferase	Aquifex aeolicus	Aquifex
2Q90_A	298-332	Oxidoreductase	Melanocarpus albomyces	Melanocarpus
2QN4_A	41-90	Hydrolase	Oryza sativa subsp. japonica	Oryza
2QRL_A	205-249	Oxidoreductase	Saccharomyces cerevisiae	Saccharomyces
2RL8_A	106-141	Protein transport	Bos taurus	Bos
2RNG_A	52 - 70	Antimicrobial	Tachypleus tridentatus	Tachypleus
2UUR_A	175-229	Structural protein	Homo sapiens	Homo
2UUX_A	24-51	Inhibitor	Rhipicephalus appendiculatus	Rhipicephalus
2UUX_A	52-69	Inhibitor	Rhipicephalus appendiculatus	Rhipicephalus
2VEC_A	10-204	Cytosolic	Escherichia coli	Escherichia
2VGA_A	33-199	Viral	Vaccinia virus	Orthopoxvirus
2W2G_A	492-623	Rna-binding	Sars coronavirus	Betacoronavirus
2W61_A	390-442	Glycoprotein	Saccharomyces cerevisiae	Saccharomyces
2W8X_A	51-69	Membrane	Rhipicephalus appendiculatus	Rhipicephalus
2W9X_A	165-333	Hydrolase	Cellvibrio japonicus	Cellvibrio
2WB9_A	26-196	Transferase	Fasciola hepatica	Fasciola
2WBF_X	755-809	Hydrolase	Plasmodium falciparum	Plasmodium
2WNK_A	179-218	Membrane protein	Toxoplasma gondii	Toxoplasma
2X46_A	50 - 155	Allergen	Argas reflexus	Argas
2XFD_A	90-101	Sugar	Escherichia coli	Escherichia
2XRC_A	123-163	Immune system	Homo sapiens	Homo
2XU3_A	156-209	Hydrolase	Homo sapiens	Homo
2Y1B_A	74-118	Membrane	Escherichia coli	Escherichia
2Y8T_A	304-393	Membrane	Toxoplasma gondii	Toxoplasma
2YDV_A	71-159	Receptor	Homo sapiens	Homo
2Z4I_A	145-211	Signaling	Escherichia coli	Escherichia
			Co	ntinued on the next page

Table 2 – continued from the previous page

		Table 2 – contin	ued from the previous page	
PDB	Loop	Function	Organism	Organism
code	range	(classification)	Species	Genus
2ZK9_A	76-172	Hydrolase	Chryseobacterium proteolyticum	Chryseobacterium
2ZK9_A	77-126	Hydrolase	Chryseobacterium proteolyticum	Chryseobacterium
2ZWS_A	322-370	Hydrolase	Pseudomonas aeruginosa	Pseudomonas
2ZX2_A	106-135	Immune system	Oncorhynchus keta	Oncorhynchus
2ZX2_A	6-35	Immune system	Oncorhynchus keta	Oncorhynchus
3A2E_A	10-86	Plant protein	Ginkgo biloba	Ginkgo
3AIH_A	181-216	Sugar binding	Homo sapiens	Homo
3BRN_A	40-153	Ligand binding	Argas monolakensis	Argas
3BWK_A	177-238	Hydrolase	Plasmodium falciparum	Plasmodium
3CQN_A	118-249	Oxidoreductase	Arabidopsis thaliana	Arabidopsis
3CTK_A	32-212	Hydrolase	Bougainvillea spectabilis	Bougainvillea
3D22_A	4-58	Oxidoreductase	Populus trichocarpa	Populus
3DB5_B	49-124	Transferase	Homo sapiens	Homo
3DJL_A	28-540	Oxidoreductase	Escherichia coli	Escherichia
3DUZ_A	128-158	Viral protein	Autographa cal. nuc. pol. virus	Alphabaculovirus
3EBW_A	41-162	Allergen	Periplaneta americana	Periplaneta
3EDH_A	42-198	Hydrolase	Homo sapiens	Homo
3EDY_A	365-526	Hydrolase	Homo sapiens	Homo
3EQN_A	5-424	Hydrolase	Phanerochaete chrysosporium	Phanerochaete
3F5V_A	4-117	Hydrolase	Dermatophagoides pteronyssinus	Dermatophagoides
3FLP_A	184-215	Sugar binding	Limulus polyphemus	Limulus
3G7N_A	25-254	Hydrolase	Penicillium expansum	Penicillium
3HELB	80-140	Transferase	Homo sapiens	Homo
3I26_A	108-156	Hydrolase	Breda virus serotype 1	Torovirus
3I5W_A	5-20	Antimicrobial	Homo sapiens	Homo
3JXG_A	78-261	Cell adhesion	Mus musculus	Mus
3L49_A	166-224	Transport protein	Rhodobacter sphaeroides	Rhodobacter
3L91_A	67-148	Hydrolase	Pseudomonas aeruginosa	Pseudomonas
3LQB_A	50-199	Hydrolase	Danio rerio	Danio
3M31_A	90-349	Oxidoreductase	Saccharomyces cerevisiae	Saccharomyces
3MB5_A	196-233	Transferase	Pyrococcus abyssi	Pyrococcus
3MTW_A	172-213	Hydrolase	Caulobacter vibrioides	Caulobacter
3NGG_A	10-35	Antibiotic	Oxyuranus microlepidotus	Oxyuranus
3NGW_A	24-192	Biosynthetic protein	Archaeoglobus fulgidus	Archaeoglobus
3NK4_A	251-335	Cell adhesion	Gallus gallus	Gallus
3NKQ_A	148-194	Hydrolase	Mus musculus	Mus
30EN_A	229-284	Transport protein	Rattus norvegicus	Rattus
3ON9_A	180-317	Viral	Ectromelia virus	Orthopoxvirus
30P8_A	288-326	Protein	Homo sapiens	Homo
30ZP_A	36-55	Hydrolase	Ostrinia furnacalis	Ostrinia
3PIV_A	4-99	Cytokine	Danio rerio	Danio
3PIW_A	6-101	Cytokine	Danio rerio	Danio
3Q2U_A	75-156	Membrane	Homo sapiens	Homo
3Q31_A	58-219	Lyase	Aspergillus oryzae	Aspergillus
3QDH_A	394-445	Cell adhesion	Actinomyces naeslundii	Actinomyces
3QSD_A	133-199	Hydrolase	Schistosoma mansoni	Schistosoma
3QTE_A	6-20	Antimicrobial	Homo sapiens	Homo
3QVP_A	164-206	Oxidoreductase	Aspergillus niger	Aspergillus
$3QW9_A$	84-153	Cytokine	Rattus norvegicus	Rattus
			Co	ntinued on the next page

		Table 2 – continu	ued from the previous page	
PDB	Loop	Function	Organism	Organism
code	range	(classification)	Species	Genus
3RLG_A	53-201	Hydrolase	Loxosceles intermedia	Loxosceles
3S8K_A	45-89	Hydrolase	Carica papaya	Carica
3SH4_A	159 - 193	Metal binding	Homo sapiens	Homo
3SUK_A	39-76	Unknown	Moniliophthora perniciosa	Moniliophthora
3SUK_A	79-138	Unknown	Moniliophthora perniciosa	Moniliophthora
3SUM_A	43-80	Unknown	Moniliophthora perniciosa	Moniliophthora
3SUM_A	83-145	Unknown	Moniliophthora perniciosa	Moniliophthora
3T0O_A	202-213	Hydrolase	Homo sapiens	Homo
3T94_A	138-205	Transferase	Sulfolobus solfataricus	Sulfolobus
3TC2_A	48-97	Hydrolase	Solanum tuberosum	Solanum
3U4Y_A	48-319	Structural protein	Desulfotomaculum acetoxidans	Desulfotomaculum
3U74_A	115-147	Hydrolase receptor	Homo sapiens	Homo
3U74_A	95-122	Hydrolase receptor	Homo sapiens	Homo
3UTK_N	61-115	Protein	Dickeya dadantii	Dickeya
3UYX_N	96-142	Viral	Influenza A virus	Influenza A
3V5A_N	425-647	Metal binding protein	Bos taurus	Bos
3V83_C	402-674	Metal binding protein	Homo sapiens	Homo
3V83_C	418-637	Metal binding protein	Homo sapiens	Homo
3VUP_A	177-244	Hydrolase	Aplysia kurodai	Aplysia
3VX0_A	440-475	Hydrolase	Aspergillus oryzae	Aspergillus
3WMT_A	76-129	Hydrolase	Aspergillus oryzae	Aspergillus
3WP4_A	4-172	Hydrolase	Neocallimastix patriciarum	Neocallimastix
3ZC9_A	41-85	Hydrolase	Murraya koenigii	Murraya
3ZPX_A	101-273	Hydrolase	Ustilago maydis	Ustilago
3ZUI_A	56-168	Immune system	Ornithodoros moubata	Ornithodoros
3ZXC_A	3-26	Signaling	Cupiennius salei	Cupiennius
3ZY2_A	266 - 353	Transferase	Caenorhabditis elegans	Caenorhabditis
4A56_A	53 - 107	Protein binding	Klebsiella oxytoca	Klebsiella
4A7U_A	57-146	Oxidoreductase	Homo sapiens	Homo
4ADI_A	49-287	Viral	Rubella virus	Rubivirus
4ADI_A	51-130	Viral	Rubella virus	Rubivirus
4B7Q_C	92-417	Hydrolase	Influenza a virus	Influenza A
4BOE_A	28 - 150	Cholesterol binding	Rhipicephalus appendiculatus	Rhipicephalus
4BQD_A	51-72	Blood clotting	Homo sapiens	Homo
4CMR_A	193-303	Hydrolase	Pyrococcus sp. st04	Pyrococcus
4CXP_A	66-218	Hydrolase	Arabidopsis thaliana	Arabidopsis
4CYL_A	111-309	Cell adhesion	Caenorhabditis elegans	Caenorhabditis
4CYL_A	113 - 155	Cell adhesion	Caenorhabditis elegans	Caenorhabditis
4D8M_A	414-489	Lipid	Bacillus thuringiensis	Bacillus
4ETR_A	30-101	Unknown	Pseudomonas aeruginosa	Pseudomonas
4F23_A	95-138	Viral	Influenza A virus	Influenza A
4FDI_A	308-419	Hydrolase	Homo sapiens	Homo
4FNK_C	97-139	Viral	Influenza A virus	Influenza A
4G2U_A	74-152	Immune system	Ostertagia ostertagi	Ostertagia
4GDI_A	92-417	Viral	Influenza A virus	Influenza A
4GE1_A	42-176	Amine-binding	Rhodnius prolixus	Rhodnius
4GQR_A	70-115	Hydrolase	Homo sapiens	Homo
4GV5_A	11-30	Toxin	Crotalus durissus terrificus	Crotalus
4GWN_N	103 - 255	Hydrolase	Homo sapiens	Homo
			Co	ntinued on the next page

		Table $2 - \text{continu}$	ued from the previous page	
PDB	Loop	Function	Organism	Organism
code	range	(classification $)$	Species	Genus
4H14_A	21-165	Viral	Bovine coronavirus	Betacoronavirus
4HJ1_A	756-852	Viral	Rift valley fever virus	Phlebovirus
4HJ1_A	777-825	Viral	Rift valley fever virus	Phlebovirus
4HLN_A	126-506	Transferase	Hordeum vulgare	Hordeum
4HS9_A	181-238	Hydrolase	Proteus mirabilis	Proteus
4HYQ_A	152-199	Hydrolase	Streptomyces albidoflavus	Streptomyces
4I71_A	199-304	Hydrolase	Trypanosoma brucei brucei	Trypanosoma
4IGT_A	739-794	Membrane protein	Rattus norvegicus	Rattus
4IHZ_A	33-80	Hydrolase	Crataeva tapia	Crateva
4IO2_A	193-247	Membrane	Adineta vaga	Adineta
4J37_A	142-196	Rna binding protein	Homo sapiens	Homo
4JD0_A	32-241	Transferase	Thermotoga maritima	Thermotoga
4JJO_A	23-48	Sugar binding	Clavibacter michiganensis	Clavibacter
4JP6_A	29-61	Unknown	Carica papaya	Carica
4JP6_A	64-120	Unknown	Carica papaya	Carica
4JPH_A	87-137	Cytokine	Mus musculus	Mus
4JWO_A	154-263	Phosphate binding	Planctomyces limnophilus	Planctopirus
4KK7_A	150-345	Protein binding	Mycobacterium tuberculosis	Mycobacterium
4KKI_A	3-242	Transport protein	Homo sapiens	Homo
4KNC_A	44-229	Sugar binding	Pseudomonas aeruginosa	Pseudomonas aeruginosa
4KP1_A	102-365	Isomerase	Methanocaldococcus jannaschii	Methanocaldococcus
4KYP_A	43-69	Toxin	Hottentotta judaicus	Hottentotta
4L05_A	55-150	Oxidoreductase	Brucella abortus	Brucella
4L3N_A	425-478	Viral	Human betacoronavirus 2c	Betacoronavirus
$4L7G_A$	217-382	Hydrolase	Homo sapiens	Homo
4LB1_A	4-19	Antimicrobial	Homo sapiens	Homo
4LBF_A	4-19	Antimicrobial protein	Homo sapiens	Homo
4LQ6_A	33-81	Hydrolase	Mycobacterium tuberculosis	Mycobacterium
4MYK_A	35-242	Hydrolase	Trypanosoma cruzi	Trypanosoma
4N03_A	89-347	Transport protein	Thermomonospora curvata	Thermomonospora
4N3T_A	87-162	Oxidoreductase	Candida albicans	Candida
4N7C_A	44-175	Protein binding	Blattella germanica	Blattella
4NT5_A	2739-2788	Protein binding	Homo sapiens	Homo
40IE_A	280-329	Viral	West nile virus	Flavivirus
40IE_A	291-312	Viral	West nile virus	Flavivirus
4P02_B	163-430	Transferase	Rhodobacter sphaeroides	
4P27_A	56-130	Allergen	Schistosoma mansoni	Schistosoma
4PLM_A	121-154	Protein binding	Gallus gallus	Gallus
$4R2B_A$	290-357	Transport	Ochrobactrum anthropi	Ochrobactrum
4TLP_A	44-88	Hydrolase	Psophocarpus tetragonolobus	Psophocarpus
	Tab	le 2. Protein chains with	a single lasso $(L_1 \text{ type})$ i.e. with	

Table 2: Protein chains with a single lasso $(L_1 \text{ type})$, i.e. with loops pierced once by a tail. In total 331 loops pierced once have been identified in 296 proteins.

=

PDB	Loop	Function	Organism	Organism
code	range	(classification)	Species	Genus
1AOC_A	10-95	Coagulation factor	Tachypleus tridentatus	Tachypleus
1BR9_A	1-72	Proteinase	Homo sapiens	Homo
1ETE_A	93-132	Cytokine	Homo sapiens	Homo
$1F2L_A$	8-34	Cytokine	Homo sapiens	Homo
$1 \text{G0Y}_{-} \text{R}$	104-147	Immune system	Homo sapiens	Homo
1GVZ_A	22-157	Hydrolase	Equus caballus	Equus
1HC1_A	562-609	Oxygen transport	Panulirus interruptus	Panulirus
1KKH_A	112-286	Transferase	Methanocaldococcus jannaschii	Methanocaldococcus
$1M8A_A$	6-32	Cytokine	Homo sapiens	Homo
1NR4_A	10-34	Cytokine	Homo sapiens	Homo
107Z_A	9-36	Chemokine	Homo sapiens	Homo
10MZ_A	244-296	Transferase	Mus musculus	Mus
$1 \mathrm{QFX}_A$	109-453	Hydrolase	Aspergillus niger	Aspergillus
$1RJT_A$	9-36	Cytokine	Homo sapiens	Homo
1TVX_A	25-51	Cytokine	Homo sapiens	Homo
1XWE_A	1514-1588	Signaling	Homo sapiens	Homo
1YPY_A	49-136	Viral protein	Vaccinia virus	Orthopoxvirus
1 ZPU_A	102-521	Oxidoreductase	Saccharomyces cerevisiae	Saccharomyces
1ZXT_A	12-36	Signaling	Human herpesvirus 8	Rhadinovirus
2FFU_A	345-423	Transferase	Homo sapiens	Homo
2GMF_A	88-121	Growth factor	Homo sapiens	Homo
$2HDL_A$	3-29	Cytokine	Homo sapiens	Homo
2LT5_C	3-78	Hydrolase	Rana pipiens	Rana
20IZ_D	81-113	Oxidoreductase	Alcaligenes faecalis	Alcaligenes
2P3X_A	25-88	Oxidoreductase	Vitis vinifera	Vitis
$2Q9O_A$	114-540	Oxidoreductase	Melanocarpus albomyces	Melanocarpus
2RA4_A	11-35	Cytokine	Homo sapiens	Homo
2VGA_A	6-166	Viral	Vaccinia virus	Orthopoxvirus
$2X97_C$	467-612	Hydrolase	Drosophila melanogaster	Drosophila
2YAU_A	89-213	Oxidoreductase	Leishmania infantum	Leishmania
$3F95_A$	768-811	Hydrolase	Pseudoalteromonas sp.	Pseudoalteromonas
3GV3_A	9-34	Cytokine	Homo sapiens	Homo
3HHS_A	586-630	Oxidoreductase	Manduca sexta	Manduca
3HHS_A	588-637	Oxidoreductase	Manduca sexta	Manduca
3NKQ_A	156-350	Hydrolase	Mus musculus	Mus
3NSW_C	3-62	Immune system	Ancylostoma ceylanicum	Ancylostoma
3PXL_A	85-488	Oxidoreductase	Trametes hirsuta	Trametes
3RT4_A	22-67	Immune system	Camelus dromedarius	Camelus
3SQR_A	108-524	Oxidoreductase	Botrytis aclada	Botrytis
3'TM0_A	19-156	Transferase/antibiotic	Enterococcus faecalis	Enterococcus
3TN2_A	11-35	Cytokine	Homo sapiens	Homo
3ZK4_A	203-367	Oxidoreductase	Lupinus luteus	Lupinus
4ADI_A	37-242	Viral protein	Rubella virus	Rubivirus
4HCS_A	15-40	Signaling	Danio rerio	Danio
4HWM_A	68-124	Unknown	Klebsiella pneumoniae	Klebsiella
4N11_A	10-278	Hydrolase	Ustilago maydis	Ustilago
4PSC_A	55-91	Hydrolase	Trichoderma reesei	Trichoderma

Table 3: Protein chains with a double lasso $(L_2 \text{ type})$, i.e. with loops pierced twice by a tail. In total 47 loops pierced twice have been identified in 46 proteins.

PDB	Loop	Function	Organism	Organism
code	range	(classification)	Species	Genus
1BJ7_A	63-154	Allergen	Bos taurus	Bos
1DZK_A	63-155	Transport	Sus scrofa	Sus
1EPA_A	60-154	Retinoic	Rattus norvegicus	Rattus
1KT6_A	70-174	Transport	Bos taurus	Bos
$1LF7_A$	76-168	Immune	Homo sapiens	Homo
$1U3D_A$	80-190	Signaling	Arabidopsis thaliana	Arabidopsis
2EHG_A	58-145	Hydrolase	Sulfolobus tokodaii	Sulfolobus
2L5P_A	98-203	Transport	Rattus norvegicus	Rattus
2RA6_A	73-166	Transport	Trichosurus vulpecula	Trichosurus
2VGA_A	112 - 152	Viral	Vaccinia virus	Orthopoxvirus
2YG2_A	95-183	Lipid transport	Homo sapiens	Homo
3AGN_A	1-54	Hydrolase	Ustilago sphaerogena	Ustilago
3EEQ_A	60-285	Structural	Sulfolobus solfataricus	Sulfolobus
3FIQ_A	63 - 155	Transport	Rattus norvegicus	Rattus
$3 \mathrm{KFF}_{-} \mathrm{A}$	64-157	Transport	Mus musculus	Mus
3KQ0_A	72-165	Signaling	Homo sapiens	Homo
3L4R_A	64-157	Allergen,	Canis familiaris	Canis
3NSJ_A	241 - 407	Immune	Mus musculus	Mus
3O22_A	89-186	Isomerase	Homo sapiens	Homo
$3QL6_A$	6-167	Oxidoreductase	Bos taurus	Bos
3S26_A	78-177	Transport	Mus musculus	Mus
3SAO_A	58 - 151	Transport	Gallus gallus	Gallus
$4CK4_{-}A$	66-160	Transport	Ovis aries	Ovis
$4H14_A$	172 - 252	Viral	Bovine coronavirus	Betacoronavirus
40DD_B	62-154	Allergen	Canis lupus familiaris	Canis

Table 4: Protein chains with a triple lasso (L_3 type), i.e. with loops pierced three times by a tail. In total 25 loops triply pierced have been identified in 25 proteins.

	~ .	
code range (classification)	Species	Genus
4QI7_A 167-211 Oxidoreductase	Neurospora crassa	Neurospora

Table 5: Protein chains with a sixfold lasso (L_6 type), i.e. with loops pierced six times by a tail. In total 1 loop pierced six times has been identified in 1 protein.

PDB	Loop	Function	Organism	Organism	Type
code	range	(classification)	Species	Genus	
2D1G_A	216-269	Hydrolase	Francisella tularensis subsp. novicida	Francisella	
2DVZ_A	93-152	Transport protein	Bordetella pertussis	Bordetella	
$2YHG_A$	564-779	Hydrolase	Saccharophagus degradans	Saccharophagus	
$3OM0_A$	17-273	Membrane	Rattus norvegicus	Rattus	T
3WA1_A	67-161	Toxin	Lysinibacillus sphaericus	Lysinibacillus	$L_{1,1}$
4A3X_C	78-119	Cell adhesion	Candida glabrata	Nakaseomyces	
$4ASL_A$	78-119	Cell adhesion	Candida glabrata	Nakaseomyces	
$2 CMZ_A$	177-224	Membrane protein	Vesicular stomatitis indiana virus	Vesiculovirus	
4JGL_A	57-142	Structural protein	Bacteroides eggerthii	Bacteroides	$L_{1,2}$
1CQ3_A	132-171	Cytokine	Cowpox virus	Orthopoxvirus	$L_{4,2}$

Table 6: Protein chains with a two-sided lasso $(L_{i,j}$ type), i.e. with loops pierced by both tails, respectively i and j times. In total 10 two-sided lassos have been identified in 10 proteins.

PDB	Loop	Function	Organism	Organism
code	range	(classification)	Species	Genus
1H30_A	283-570	Growth arrest spec.	Homo sapiens	Homo
1ZD0_A	48-131	Structural	Pyrococcus furiosus	Pyrococcus
2JH1_A	91-127	Cell adhesion	Toxoplasma gondii	Toxoplasma
2JH1_A	181-226	Cell adhesion	Toxoplasma gondii	Toxoplasma
2XJP_A	29-175	Cell adhesion	Saccharomyces cerevisiae	Saccharomyces
2XJP_A	176 - 263	Cell adhesion	Saccharomyces cerevisiae	Saccharomyces
2ZOU_A	44-128	Cell adhesion	Homo sapiens	Homo
3IAI_A	23-203	Lyase	Homo sapiens	Homo
3V5A_D	481-675	Metal binding protein	Bos taurus	Bos
3V83_C	474-665	Metal binding protein	Homo sapiens	Homo
3V83_C	137 - 331	Metal binding protein	Homo sapiens	Homo
4A3X_C	50-179	Cell adhesion	Candida glabrata	Nakaseomyces
4A3X_C	180-262	Cell adhesion	Candida glabrata	Nakaseomyces
4ASL_A	50-179	Cell adhesion	Candida glabrata	Nakaseomyces
4ASL_A	180-262	Cell adhesion	Candida glabrata	Nakaseomyces
4G7A_A	24-178	Lyase	Sulfurihydrogenibium sp. yo3aop1	Sulfurihydrogenibium
4HT2_A	22-202	Lyase	Homo sapiens	Homo
4KG7_A	54-123	Hydrolase	Mycobacterium smegmatis	Mycobacterium
4P1E_A	185-304	Transport	Escherichia fergusonii	Escherichia

Table 7: Protein chains with a supercoiling lasso (LS type), i.e. with loops pierced several times by one tail from the same direction. In total 19 supercoiled loops have been identified, in 14 proteins.

PDB code	Loop range	Lasso type	Function (classification)	Organism Species	Organism Genus	Chain type
1C01_A	11-64 23-49	$\begin{array}{c} L_1\\ L_1\end{array}$	Antimicrobial	Macadamia integrifolia	Macadamia	L_1L_1
$1E4M_M$	6-438 14-434	$\begin{array}{c} L_1\\ L_1\end{array}$	Hydrolase	Sinapis alba	Sinapis	L_1L_1
1FLC_A	126-174 196-238	$\begin{array}{c} L_1\\ L_1\end{array}$	Hydrolase	Influenza C virus	Influenzavirus C	L_1L_1
1HCN_B	23-72 26-110	L_1 L_1	Hormone	Homo sapiens	Homo	L_1L_1
1JY5_A	26-84 57-90	L_1 L_1	Hydrolase	Calystegia sepium	Calystegia	L_1L_1
1LKI_A	12-134 18-131	L_1 L_1	Cytokine	Mus musculus	Mus	L_1L_1
$1Q25_A$	81-111 385-419	L_1 L_1	Protein binding	Bos taurus	Bos	L_1L_1
1 SGL_A	26-84 57-90	L_1 L_1 L	Hydrolase	Trichosanthes lepiniana	Trichosanthes	L_1L_1
1T61_A	55-108 164-222 7 27	L_1 L_1 L_1	Structural protein	Bos taurus	Bos	L_1L_1
1UDK_A	20-41	$\begin{array}{c} L_1\\ L_1\end{array}$	Unknown	Naja nigricollis	Naja	L_1L_1
1WKT_A	$11-72 \\ 27-58$	$\begin{array}{c} L_1\\ L_1\end{array}$	Toxin	Williopsis saturnus var. mrakii	Cyberlindnera	L_1L_1
2HCZ_X	42-70 73-140	$\begin{array}{c} L_1\\ L_1\end{array}$	Allergen 2	Zea mays	Zea	L_1L_1
2JTO_A	10-27 47-64	L_1 L_1	Hydrolase	Rhipicephalus bursa	Rhipicephalus	L_1L_1
2KQA_A	20-57 60-115	$\begin{array}{c} L_1\\ L_1\\ r\end{array}$	Toxin	Ceratocystis platani	Ceratocystis	L_1L_1
2PSP_A	8-35 58-84	$\begin{array}{c} L_1\\ L_1\\ I \end{array}$	Signaling	Sus scrofa	Sus	L_1L_1
2UUX_A	24-51 52-69	L_1 L_1	Inhibitor	appendiculatus	Rhipicephalus	L_1L_1
2ZK9_X	76-172 77-126	L_1 L_1 L	Hydrolase	proteolyticum	Chryseobacterium	L_1L_1
2ZX2_A	0-55 106-135 20.76	$\begin{array}{c} L_1\\ L_1\\ I \end{array}$	Immune system	Oncorhynchus keta	Oncorhynchus	L_1L_1
3SUK_A	39-70 79-138	L_1 L_1	Unknown	Moniliophthora perniciosa	Moniliophthora	L_1L_1
3SUM_A	43-80 83-145	L_1 L_1	Unknown	Moniliophthora perniciosa	Moniliophthora	L_1L_1
3U74_A	95-122 115-147	L_1 L_1	Hydrolase receptor	Homo sapiens	Homo	L_1L_1
4CYL_A	111-309 113-155	$\begin{array}{c} L_1\\ L_1\end{array}$	Cell adhesion	Caenorhabditis elegans	Caenorhabditis	L_1L_1
4HJ1_A	771-965 777-825	$\begin{array}{c c} L_1 \\ L_1 \\ L_1 \end{array}$	Viral	Rift valley fever virus	Phlebovirus	L_1L_1
4JP6_A	29-61 64-120	$\begin{array}{c} L_1\\ L_1\\ \end{array}$	Unknown	Carica papaya	Carica	L_1L_1
40IE_A	280-329 291-312	$\begin{array}{c} L_1\\ L_1\end{array}$	Viral	West nile virus	Flavivirus	L_1L_1
					Continued on th	ie next page

PDB	Loops	Lasso	Function	Organism	Organism	Chain
code	range	type	(classification)	Species	Genus	type
1AOC_A	60-161 10-95	L_1 L_2	Coagulation factor	Tachypleus tridentatus	Tachypleus	L_1L_2
1ETE_A	44-127 93-132	L_1 L_2	Cytokine	Homo sapiens	Homo	L_1L_2
20IZ_D	81-113 130-161	L_2 L_1	Oxidoreductase	Alcaligenes faecalis	Alcaligenes	$L_{2}L_{1}$
$2Q9O_A$	114-540 298-332	L_2 L_1	Oxidoreductase	Melanocarpus albomyces	Melanocarpus	L_2L_1
4H14_A	21-165 172-252	L_1 L_3	Viral	Bovine coronavirus	Betacoronavirus	L_1L_3
2CMZ_A	68-114 177-224	$\begin{array}{c} LL_{1,1} \\ L_1 \end{array}$	Membrane	Vesicular stomatitis indiana virus	Vesiculovirus	$L_{1,1}L_1$
1CQ3_A	8-185 132-171	$\begin{array}{c} L_1\\ L_{4,2} \end{array}$	Antimicrobial	Macadamia integrifolia	Macadamia	$L_{1}L_{4,2}$
3V5A_N	425-647 481-675	L_1 LS	Metal binding	Bos taurus	Bos	L_1LS
3HHS_A	586-630 588-637	L_2 L_2	Oxidoreductase	Manduca sexta	Manduca	L_2L_2
2JH1_A	91-127 91-127	LS LS	Cell adhesion	Toxoplasma gondii	Toxoplasma	LSLS
2XJP_A	29-175 176-263	LS LS	Cell adhesion	Saccharomyces cerevisiae	Saccharomyces	LSLS
1DTV_A	18-62 19-43	L_1 L_1	Antimicrobial	Macadamia integrifolia	Macadamia	$L_1L_1L_1$
1WC2_A	$\begin{array}{c} 22-58 \\ 30-69 \\ 65-178 \\ 72-157 \end{array}$	L_1 L_1 L_1 L_1	Hydrolase	Mytilus edulis	Mytilus	$L_1L_1L_1$
2ENG_A	16-86 87-199 89-189	$ \begin{array}{c} L_1 \\ L_1 \\ L_1 \\ L_1 \end{array} $	Hydrolase	Humicola insolens	Humicola	$L_1L_1L_1$
4ADI_A	37-242 49-287 51-130	$ \begin{array}{c} L_2\\ L_1\\ L_1 \end{array} $	Viral	Rubella virus	Rubivirus	$L_{2}L_{1}L_{1}$
2VGA_A	6-166 33-199 112-152	$L_2 \\ L_1 \\ L_3$	Viral	Vaccinia virus	Orthopoxvirus	$L_2L_1L_3$
3NKQ_A	148-194 156-350 413-801	$ \begin{array}{c} L_1\\ L_2\\ L_{1,2} \end{array} $	Hydrolase	Mus musculus	Mus	$L_1 L_2 L_{1,2}$
1H30_A	283-570 444-470 562-609	$LS \\ L_1 \\ L_1$	Growth arrest spec.	Homo sapiens	Homo	LSL_1L_1
2JD4_A	2686-2958 2845-2870 3024-3055	$LS \\ L_1 \\ L_1$	Metal binding	Mus musculus	Mus	LSL_1L_1
4A3X_C	50-179 78-119 180-262	$LS \\ LS_{1,1} \\ LS$	Cell adhesion	Candida glabrata	Nakaseomyces	LSLL _{1,1} LS
			1		Continued on t	he next page

Table 8 – continued from the previous page

PDB	Loops	Lasso	Function	Organism	Organism	Chain
code	range	type	(classification)	$\mathbf{Species}$	Genus	type
	50-179	LS				
$4ASL_A$	78-119	$LS_{1,1}$	Cell adhesion	Candida glabrata	Nakaseomyces	$LSLL_{1,1}LS$
	180-262	LS				
	137-331	LS				
2V02 C	402-674	L_1	Motel hinding	Home capions	Homo	TGT.T.TG
3V83_C	418-637	L_1	Metal binding	Homo sapiens	пото	
	474-665	LS				

Table 8 – continued from the previous page

Table 8: Protein chains with more than one pierced lasso in structure. In total 16 different loop arrangements have been identified in 47 proteins.

4 Posttranslational modifications

In order to reveal the possible function of the lasso motif the posstranslationally modified amino acids were selected in the set of topologically nontrivial structures. The analysis showed, that in the case of 4 protein chains the modified residue was located inside the pierced covalent loop (Tab. 9).

PDB code	Loop range	Lasso loop type	Index of modified residue	Modified residue code	Modified residue name	Modified residue image
	4 117	Т	24	CCD		
3F 5 V_A	4-117	L_1	34	CSD	3-Sulfinoalanine	NH ₂ OH
2VEC_A	10-204	L_1	122	CSO	S-Hydroxycysteine	
4IHZ_A	33-80	L_1	74	CSX	S-Oxy Cysteine	
3MTW_A	172-213	L_1	211	KCX	Lysine N <i>e</i> -Carboxylic Acid	

Table 9: The protein chains with posttranslational modifications found inside the pierced covalent loop.

In other 10 chains the modified residue was external to the covalent loop. As such residue can still influence the sequential, or spatial proximity of the piercing, we calculated the sequential distance between the modified residue and the closes piercing (Tab. 10).

PDB code	Index of piercing residue	Index of modified residue	Distance	Modified residue code	Modified residue name
4FDI_A	73	79	6	DDZ	3,3-Dihydroxy
2Q9O_A	92	98	6	OHI	3-(2-Oxo-2H-Imidazol-4-yl)- -L-Alanine
3QSD_A	127	324	197	074	[Propylamino-3-Hydroxy- -Butan-1,4-Dionyl]- -Isoleucyl-Proline
2HCZ_X	58	9	49	HYP	4-Hydroxyproline
1YG9_A	40	289	249	CSX	S-Oxy Cysteins
3QL6_A	179	198	19	SEP	Phosphoserine
2PSP_A	47	1	46	PCA	Pyroglutamic Acid
3KQ0_A	29	1	28	PCA	Pyroglutamic Acid
4GQR_A	63	1	62	PCA	Pyroglutamic Acid
4JP6_A	48	1	47	PCA	Pyroglutamic Acid

Table 10: The protein chains with modified residues, external to the pierced covalent loop. In the table the distance between the modified residue and the sequentially nearest piercing is given.

5 List of multimeric proteins

Multimeric proteins in study, for which at least one chain possess at least one pierced covalent loop (PDB codes with the chain names in parenthesis): 1AOC (A,B), 1AOZ (A,B), 1BCP (A,G), 1CQ3 (A,B), 1DEU (A,B), 1DOF (A,C,B,D), 1DP4 (A,C), 1DZK (A,B), 1EPA (A,B), 1ETE (A,C,B,D), 1F2L (A,C,B,D), 1FD3 (A,C,B,D), 1FJR (A,B), 1FLC (A,C,E), 1GXY (A,B), 1HC1 (A,C,B,E,D,F), 1I1J (A,B), 114U (A,B), 11JV (A,B), 11YB (A,B), 1JDP (A,B), 1JY5 (A,B), 1LE6 (A,C,B), 1M8A (A,B), 1N2Z (A,B), 1NF2 (A,C,B), 1NR4 (A,C,B,E,D,G,F,H), 1NSC (A,B), 1O7Z (A,B), 10MZ (A,B), 1PZ7 (A,B), 1Q77 (A,B), 1QFT (A,B), 1RXD (C,B), 1SCF (A,B), 1T61 (A,C,B,E,D,F), 1TVX (A,C,B,D), 1TZP (A,B), 1UWC (A,B), 1WS8 (A,C,B,D), 1XTA (A,B), 1XTM (A,B), 1YRB (A,B), 1ZMI (A,C,B,D), 1ZMM (A,C,B,D), 1ZPU (A,C,B,E,D,F), 1ZXT (A,C,B,D), 2BB3 (A,B), 2BB6 (A,C,B,D), 2BGH (A,B), 2C1C (A,B), 2CKS (A,B), 2CMZ (A,C,B), 2D1G (A,B), 2D5W (A,B), 2DRE (A,C,B,D), 2E1V (A,B), 2F5X (A,C,B), 2GHV (C,E), 2GMF (A,B), 2GUM (A,C,B), 2HYX (A,C,B,D), 2JD4 (A,B), 2JIG (A,B), 2OIZ (H,D), 2OR7 (A,B), 2OYA (A,B), 2PMV (A,C,B,D), 2PSP (A,B), 2PT5 (A,C,B,D), 2Q9O (A,B), 2QKI (C,F), 2QN4 (A,B), 2RA4 (A,B), 2RA6 (A,C,B,D), 2W8X (A,B), 2W9X (A,B), 2WB9 (A,B), 2WY3 (B,D), 2XRC (A,C,B,D), 2Y8T (A,D), 2YAU (A,B), 2YG2 (A,B), 2Z4I (A,B), 2ZOU (A,B), 2ZX2 (A,B), 3A2E (A,D), 3AIH (A,B), 3B1B (A,B), 3BRN (A,B), 3BWK (A,B,D), 3CGU (A,B), 3CQN (A,B), 3EBW (A,B), 3EEQ (A,B), 3EQN (A,B), 3ETO (A,B), 3F5V (A,B), 3F95 (A,B), 3FIQ (A,B), 3FLP (A,C,B,E,D,G,F,I,H,K,J,M,L,N), 3FW3 (A,B), 3G7N (A,B), 3HEI (B,D,F,H,J,L,N,P), 3HHS (A,B), 3I26 (A,C,B,D), 3I5W (A,B), 3IAI (A,C,B,D), 3JXG (A,C,B,D), 3KGL (A,C,B,E,D,F), 3L49 (A,C,B,D), 3NGG (A,B), 3NK4 (A,B), 3NSW (C,B,D,G,F), 3ON9 (A,B), 3OP8 (A,B), 3PIM (A,B), 3PIV (A,B), 3Q31 (A,B), 3QTE (A,C,B,D), 3QW9 (A,B), 3RT4 (A,C,B,D), 3S8K (A,B), 3SAO (A,B), 3SUK (A,B), 3SUM (A,C,B,D), 3T94 (A,C,B,E,D,F), 3TC2 (A,C,B), 3U4Y (A,B), 3UTK (A,B), 3UYX (A,B), 3V83 (A,C,B,E,D,F), 3VUP (A,B), 3WKY (A,B), 3ZK4 (A,C,B), 3ZPX (A,B), 3ZXC (A,B), 4A7U (A,F), 4ADI (A,C,B), 4B7Q (A,C,B,D), 4BQD (A,B), 4CK4 (A,B), 4CMR (A,B), 4COF (A,C,B,E,D), 4ETR (A,B), 4F23 (A,C,B), 4FDI (A,B), 4FNK (A,C,E), 4G2U (A,B), 4G7A (A,B), 4GDI (A,C,B,E,D,F), 4GE1 (A,C,B,D), 4GQZ (A,C,B,D), 4GV5 (A,C,B), 4HJ1 (A,C,B,D), 4HT2 (A,C,B,D), 4IHZ (A,B), 4IO2 (A,B), 4JPH (A,C,B,D), 4K3Y (A,C,B,D), 4KNC (A,B), 4KYP (A,C,B,D), 4L3N (A,B), 4LB1 (A,B,E,D), 4LB7 (A,B,E,D), 4LBF (A,C,B,E,D,G,F,H), 4ODD (A,C,B), 4PMK (A,B), 4R2B (A,B).

Lasso type	All	Mainly Alpha	Mainly Beta	Alpha Beta	Few secondary structures	Not classified
$\frac{\mathbf{Single},}{L_1}$	296*	17 1ak0, 1ax8, 1bea 1dof, 1ete, 1gak 1jli, 1le6, 1lki 1mc2, 1n1f,	74 1ahl, 1aoc, 1aoz 1ata, 1b8w, 1bds 1c01, 1ccv, 1cq3 1d2s, 1d6b,	89 1ac5, 1aho, 1bcp 1cfe, 1cpy, 1dp4 1dtv, 1dys, 1e4m 1esc, 1fd3,	9 1bf0, 1g6x, 1kth 1tap, 1udk, 2j6d 2psp, 3ctk, 3ngg	107 1ijv, 1xtm, 1zmi 1zmm, 2bb6, 2cmz 2f5x, 2ghv, 2gum 2ikd, 2ike,
$\begin{array}{c} \textbf{Double,} \\ L_2 \end{array}$	46*	3 1ete, 2gmf, 2p3x	23 1aoc, 1br9, 1f2l 1g0y, 1gvz, 1hc1 1m8a, 1nr4, 1o7z 1rjt, 1tvx,	7 1kkh, 10mz, 1qfx 2ch9, 2yau, 3rt4 3tm0		14 1ypy, 2lt5, 2vga 2x97, 3f95, 3nkq 3nsw, 3tn2, 3zk4 4adi, 4hcs,
$\begin{array}{c} \mathbf{Triple,} \\ L_3 \end{array}$	25*	1 3ql6	16 1bj7, 1dzk, 1epa 1kt6, 1lf7, 2l5p 2ra6, 2yg2, 3fiq 3kff, 3kq0,	4 1u3d, 2ehg, 3agn 3eeq		4 2vga, 4ck4, 4h14 4odd
$\mathbf{Sixfold,} \\ L_6$	1					$\frac{1}{4 \mathrm{qi}7}$
$\frac{\textbf{Two-sided},}{LL}$	10		1 1cq3	1 3 om 0		8 2cmz, 2d1g, 2dvz 2yhg, 3wa1, 4a3x 4asl, 4jgl
Supercoiling, LS	14		1 1h30	4 1zd0, 3iai, 3v5a 3v83		9 2jh1, 2xjp, 2zou 4a3x, 4asl, 4g7a 4ht2, 4kg7, 4p1e
Total	376**	20**	110**	103**	9**	134**

6 Complex lasso classification based on CATH database

Table 11: Classification of complex lasso structures based on CATH data base.

* Few proteins are multidomain proteins, with various CATH classification. For those proteins the CATH number corresponding to the domain in which the piercings occur was chosen.

 ** 47 proteins posses more than one pierced loop (see Tab. 8 and therefore can be categorized into two lasso classes.



7 Examples of proteins with various lasso structures

Figure 6: Proteins with L_1 topology consist of mainly beta strands (top row: protein with PDB code 3uyx) and mainly alpha helices (bottom row: protein with PDB code 3piw) based on CATH data base classification. Each row consists of the following panels: Left panel: cartoon representation of a given protein. Middle panel: triangulation of a minimal surface for this protein; the triangulated "soap bubble" surface, spanned on the covalent loop, is pierced once by a tail, through a triangle in blue; two cysteins and a cystein bond are shown in orange. Right panel: baricentric representation of a minimal triangulated surface for the same protein; two cysteins and a cystein bond comprise a part of the boundary and are shown in orange; blue triangle is pierced by a tail.



Figure 7: Protein with L_2 topology consist of mainly beta strands (top row: protein with PDB code 20iz) based on CATH data base classification. Left panel: cartoon representation of a given protein. Middle panel: triangulation of a minimal surface for this protein; the triangulated "soap bubble" surface, spanned on the covalent loop, is pierced twice by a tail, through a triangle in blue and green; two cysteins and a cystein bond are shown in orange. Right panel: baricentric representation of a minimal triangulated surface for the same protein; two cysteins and a cystein bond comprise a part of the boundary and are shown in orange; blue and green triangles are pierced by a tail.



Figure 8: Proteins with LS motif. Proteins with LS topology consist of mainly alpha helices (top row: protein with PDB code 1zd0), mainly beta strands (middle row: protein with PDB code 4asl) and mainly beta strands (bottom row: protein with PDB code 2xjp) based on CATH data base classification. Each row consists of the following panels: Left panel: cartoon representation of a given protein. Middle panel: triangulation of a minimal surface for this protein; the triangulated "soap bubble" surface, spanned on the covalent loop, is pierced once by a tail, through triangles in green(top panel) or blue(middle and bottom panels); two cysteins and a cystein bond are shown in orange. Right panel: baricentric representation of a minimal triangulated surface for the same protein; two cysteins and a cystein bond comprise a part of the boundary and are shown in orange; green triangles are pierced by a tail two times in the same direction.



Figure 9: Protein 1cq3 with LL motif. Example of protein with the most complicated LL topology which consist of mainly beta strands (PDB code 2oiz) based on CATH data base classification. Left panel: cartoon representation of a given protein. Middle panel: triangulation of a minimal surface for this protein; the triangulated "soap bubble" surface, spanned on the covalent loop, is pierced four times by the N-terminal tail and three times by the C-terminal through a triangles in blue and green; two cysteins and a cystein bond are shown in orange. Right panel: baricentric representation of a minimal triangulated surface for the same protein; two cysteins and a cystein bond comprise a part of the boundary and are shown in orange; blue and green triangles are pierced by the N-terminal and C-terminal tails.

8 Analysis of proteins with small covalent loops

In the case of mini-proteins (sec. 9) the piercing chain fragment is usually stabilized by bulky residues before and after piercing. Therefore we analyzed all lasso proteins with pierced loop comprising maximally 30 residues and checked if there is any bulky residue (TRP, TYR, PHE, MET, ARG, HIS, LYS, LEU) in the range of 5 residues from piercing. The results are contained in Tab. 12.

PDB	Loop	Loop	Loop	Piercing	Bulky
code	range	size	type	residue	residues
			-	index	
1B8W_A	16-32	17	L_1	38	Arg41
1BDS_A	6-32	27	L_1	39	Trp35, His43
1BF0_A	32-53	22	L_1	23	Phe20, Phe25
1C01_A	23-49	27	L_1	71	Trp69, Phe73
1D6B_A	16-32	17	L_1	38	Arg35, Tyr42
1DTV_A	19-43	25	L_1	9	Tyr12
1F2L A	8-34	27	La	39	Arg37, Leu41
				50	Phe49, Lys54
1FD3_A	15-30	16	L_1	36	Leu32, Lys39
$1G6X_A$	30-51	22	L_1	21	Arg20, Phe23
1IJV_A	12-27	16	L_1	33	Lys31, Lys36
1KJ6_A	18-33	16	L_1	39	Arg38, Arg42
1KTH_A	30-51	22	L_1	21	Lys20, Tyr22
$1M4L_A$	138-161	24	L_1	165	Lys168
1M8A A	6 32	27	La	37	Phe39, Leu45
IMOA_A	0-32	21	12	48	Phe49, Lys52
1ND4 A	10.24	95	T.	39	Arg36, Phr38
IIIn4_A	10-54	23	L_2	50	Phe47
1077 4	0.26	20	г	41	Arg38, Lys46
1072_A	9-30	20	L_2	53	Arg52, Lys54
10K0_A	45-73	29	L_1	33	Lys34
	0.26	20	T	41	Lys38, Leu45
INJ I _A	9-30	20	L_2	52	Lys49, Leu54
$1 SHI_A$	5-33	29	L_1	44	Lys46
1TAP_A	33-55	23	L_1	24	Arg23, Tyr25
	05 51	07	r	56	Leu60
$11VA_A$	20-01	21	L_2	67	Lys65, Leu68
1UDK_A	20-41	22	L_1	44	Phe43
1WQK_A	6-30	25	L_1	37	Leu34, Tyr39
1ZMI_A	3-18	16	L_1	26	Trp25, Phe27
1ZMM_A	4-19	16	L_1	27	Phe26, Tyr28
	10.00	05	<i>T</i>	41	Lys38, Leu43
IZXT_A	12-36	25	L_2	52	Arg49, Lys57
2HCZ_X	42-70	29	L_1	94	Tyr92, Tyr98
	0.00	~-	-	34	Lys32, Lys39
2HDL_A	3-29	27	L_2	50	His49, Leu51
2J6D_A	35-56	26	L_1	34	Arg33, Tvr35
2JD4_B	2845-2870	26	L_1	2699	Tvr2694, Phe2701
2JR3_A	16-32	$1\overline{7}$	L_1	37	Phe36, Arg40
	10-27	18	L_1	30	Leu34
2JTO_A	47-64	18	L_1	69	Lvs66, Lvs74
	01			Continue	d on the next page

PDB code	Loop range	Loop size	Loop type	Piercing residue index	Bulky residues
2KER_A	43-70	28	L_1	31	Tvr32
2LVX_A	408-437	30	L_1	444	Lvs442
2MJK_A	12-28	17	L_1	31	Lvs29, Leu34
2MN3_A	16-30	15	L_1	35	Arg32, Phe39
aDOD 4	8-35	28	L_1	47	Trp45, Lys48
2PSP_A	58-84	27	L_1	95	Tyr94, Phe96
	11.05	05	- -	40	Lys38, Phe42
2RA4_A	11-35	25	L_2	51	Lys48, Lys55
2RNG_A	52-70	19	L_1	74	Tyr73, Arg77
	24-51	28	L_1	58	Tyr55, Tyr59
200A_A	52-69	18	L_1	45	Arg44, Ty46
$2W8X_A$	51-69	19	L_1	42	Leu41, His43
2XFD_A	90-101	12	L_1	83	Trp 85
97 V 9 A	6-35	30	L_1	88	Trp87, Lys91
$LL\Lambda L_A$	106-135	30	L_1	188	Tyr187, Tyr192
2CV2 A	0.24	26	т	38	Leu36, Arg41
3GV3_A	9-34	20		50	Arg47, Lys54
$3I5W_A$	5-20	16	L_1	28	Tyr27, Leu29
3NGG_A	10-35	26	L_1	41	Lys40, Arg44
30ZP_A	36-55	20	L_1	28	Trp27, Trp29
3QTE_A	6-20	15	L_1	28	Trp27, Phe29
2TN2 A	11.25	25	La	40	Phe42
51N2_A	11-55	20	L2	51	Lys48
4BQD_A	51-72	22	L_1	42	Arg41, Phe43
$4GV5_A$	11-30	20	L_1	35	Trp34, Lys38
AHCS A	15-40	26	La	44	Lys42, Leu 45
4110.5-A	10-40	20		55	Lys54
4JJO_A	23-48	26	L_1	65	Arg62
4KYP_A	43-69	27	L_1	4	Lys2, Tyr5
$4LB1_A$	4-19	16	L_1	27	Trp26
$4LBF_A$	4-19	16	L_1	27	Trp26, Phe28
40IE_A	291-312	22	L_1	335	Tyr331, Arg336

Table 12 – continued from the previous page $\| \| = \| \mathbf{P}_{iarcing} \|$

Table 12: The protein chains with small covalent loops (comprasing maximally 30 residues) with potentially blocking bulky residues. For each piercing the closest bulky residue before and after piercing (if they exist) is given.

_

=

9 Mini-proteins

The column entitled "Lasso stabilization amino acids" contains the information, which amino acids occur before, and which after the plug. This information can be directly compared with the crossing position given in the column "Surface piercing bond". It is worth mentioning, that our method in several cases agrees with the experimental results. In case of Xanthomycin, BI-32169 and Sviceucin our method predicts exact position of the surface crossing, which is inside the region determined by experimental data between the closest bulky aminoacids. Only in case of Astexin 1(23) our calculated data differ from the experimental slightly. This implies, that our analysis can predict also the aminoacids stabilizing the topology.



Figure 10: Protein with L_1 topology or lasso topology identified in mini-protein (PDB code 1rpb). Left panel: cartoon representation of a given protein. Middle panel: triangulation of a minimal surface for this protein; the triangulated "soap bubble" surface, spanned on the covalent loop, is pierced once by a tail, through a triangle in green; Cys (number one, red boal) and Asp (number 9, pink) and amide bond between them is shown in black. Right panel: baricentric representation of a minimal triangulated surface for the same protein; an amide bond comprise a part of the boundary is shown in black; green triangle is pierced by a tail.

	Peptide	PDB id	Peptide	Id of atoms	Lasso stabilization	Surface piercing
			length (aa)	forming bond	amino $acids^a$	bond^a
Class I	Aborycin RP71955	1rpb	21	Cys1-Asp9	2 S-S bridges Cys1-Cys13 Cys7-Cys19	Tyr15-Ala16
Class II	Astexin 1(23) Astexin 1(19) ^c Astexin 3 Caulosegnin I Microcin J25 Microcin J25 ^d Streptomonomicin STM Caulonodin V Xanthomonin I Xanthomonin II	2lti 2m37 2m8f 2lx6 1pp5 1s7p 2mw3 2mlj 2mfy 4nag	23 19 24 19 21 21 21 18 14^{e} 16^{e}	Gly1-Asp9 Gly1-Asp9 Gly1-Asp9 Gly1-Glu8 Gly1-Glu8 Gly1-Glu8 Ser1-Asp9 Ser1-Glu9 Gly1-Glu7 Gly1-Glu7	Tyr14/Phe15 Tyr14/Phe15 Tyr15/Trp16 Arg15/Glu16 Phe19/Tyr20 — — Ile9/Phe12 Met9/Ile12	Glu17-Ser18 Tyr14-Phe15 Tyr15-Trp16 Arg15-Glu16 Phe19-Tyr20* Phe19-Tyr20* Pro14-Ala15 Tyr16-Trp17* Gly10-Gly11 Gly10-Gly11
Class III	BI-32169 The glucagon receptor antagonist	3njw	19	Gly1-Asp9	1 S-S bridge Cys6-Cys19/ <i>Trp13</i> / Trp17	Asn14-Thr15
Class IV	Sviceucin	2ls1	20	Cys1-Asp9	2 S-S bridges Cys1-Cys13 Cys7-Cys19/ Trp17	Thr15-Ala16

Table 13: Lasso peptides - all have L1 topology according to our notation.

^{*a*} According to [5]. Stabilization can occur by two bulky amino acids or by the presence of cysteine bonds. In case of bulky amino acids residue after pluging through the loop is in bold character whereas the residue before is not. Residues that have been hypothesized to stabilize the topology, but have not been identified by structural analysis or mutagenesis are in italics. For some proteins data of stabilizing residues are missing.

 b According to introduced method. Entries which differ with entries in "Lasso stabilization amino acids" column are in bold.

 c Astexin 1 was produced from the wild type strain and by heterologous expression under a 23-amino acid form accompanied by truncated forms, among which Astexin 1(19) was characterized.

 d Microcin J25 protein with PDB id 1s7p has exactly the same amino acid sequence as Microcin J25 with 1pp5 protein, but according to crystal structure the chain of 1pp5 is splited into two separate chains in 1s7p.

 e Xanthomonins I, II are of lenght 20 amino acids, but the structure deposited in PDB are truncated to the number of residues given in table.

* These intersections are shallow, i.e. they are close to the end of a tail or to the ring (in the distance less or equal 3 aa), so would not be counted as complex lasso in our analysis.

10 Structural alignment of proteins with L_6 lasso type

The L_6 lasso protein (cellobiose dehydrogenase) with PDB code 4qi7 is a two domain protein with only one homolog (PDB code 4qi6). One of the bridge forming cysteines is located in the linker joining two domains. This part is missing in the homolog, causing its trivial lasso type. Both structures (lasso containing domain with linker) are aligned in the Fig 11.



Figure 11: Structural alignment of cellobiose dehydrogenase with L_6 lasso type (blue structure, PDB code 4qi7) with its homolog (red structure, PDB code 4qi6). The covalent loop closing bridge is depicted as orange stripe. The missing fragment is denoted as a dashed line. To facilitate view, only one of two domains in each proteins is displayed.

References

- Chen W, Cai Y, Zheng J (2008) Constructing triangular meshes of minimal area. Computer-Aided Design and Applications 5 508-518.
- [2] Pettersen, E.F., Goddard, T.D., Huang, C.C., Couch, G.S., Greenblatt, D.M., Meng, E.C., and Ferrin, T.E. (2004) UCSF Chimera - A Visualization System for Exploratory Research and Analysis. J. Comput. Chem. 25(13):1605-1612
- [3] William T. Tutte, W.T. (1963) How to draw a graph. Proc. London Math. Society 13(52):743-768
- [4] Jamroz M, Niemyska W, Rawdon EJ, Stasiak A, Millett KC, Sulkowski P, Sulkowska JI (2014) KnotProt: a database of proteins with knots and slipknots. *Nucl. Acids Res.* D306-D314
- [5] Li Y, Zirah S, Rebuffat S (2015) Lasso Peptides. Bacterial Strategies to Make and Maintain Bioactive Entangled Scaffolds. SpringerBriefs in Microbiology