

Electroweak baryogenesis

This article has been downloaded from IOPscience. Please scroll down to see the full text article.

2012 New J. Phys. 14 125003

(<http://iopscience.iop.org/1367-2630/14/12/125003>)

View [the table of contents for this issue](#), or go to the [journal homepage](#) for more

Download details:

IP Address: 131.215.71.79

The article was downloaded on 02/01/2013 at 16:14

Please note that [terms and conditions apply](#).

Electroweak baryogenesis

David E Morrissey¹ and Michael J Ramsey-Musolf^{2,3}

¹ TRIUMF, 4004 Wesbrook Mall, Vancouver, BC V6T 2A3, Canada

² Department of Physics, University of Wisconsin, Madison, WI 53705, USA

³ Kellogg Radiation Laboratory, California Institute of Technology, Pasadena, CA 91125, USA

E-mail: dmorri@triumf and mjrm@physics.wisc.edu

New Journal of Physics **14** (2012) 125003 (39pp)

Received 19 May 2012

Published 4 December 2012

Online at <http://www.njp.org/>

doi:10.1088/1367-2630/14/12/125003

Abstract. Electroweak baryogenesis (EWBG) remains a theoretically attractive and experimentally testable scenario for explaining the cosmic baryon asymmetry. We review recent progress in computations of the baryon asymmetry within this framework and discuss their phenomenological consequences. We pay particular attention to methods for analyzing the electroweak phase transition and calculating CP-violating asymmetries, the development of Standard Model extensions that may provide the necessary ingredients for EWBG, and searches for corresponding signatures at the high energy, intensity and cosmological frontiers.



Content from this work may be used under the terms of the [Creative Commons Attribution-NonCommercial-ShareAlike 3.0 licence](https://creativecommons.org/licenses/by-nc-sa/3.0/). Any further distribution of this work must maintain attribution to the author(s) and the title of the work, journal citation and DOI.

Contents

| | |
|--|-----------|
| 1. Introduction | 2 |
| 2. The electroweak phase transition | 4 |
| 2.1. Perturbative analyses | 5 |
| 2.2. Non-perturbative studies | 11 |
| 2.3. Extending the Standard Model scalar sector | 13 |
| 3. Creating CP asymmetries and baryons | 15 |
| 3.1. Particle number changing reactions | 17 |
| 3.2. CP-violating sources | 18 |
| 4. Testing electroweak baryogenesis | 26 |
| 4.1. The intensity frontier: CP-violation and electroweak baryogenesis | 26 |
| 4.2. The high energy frontier: CP-violation and phase transitions | 30 |
| 4.3. The cosmological frontier: gravity waves and more | 33 |
| 5. Summary | 34 |
| Acknowledgments | 35 |
| References | 35 |

1. Introduction

Electroweak baryogenesis (EWBG) is one of the most attractive and promising ways to account for the observed baryon asymmetry of the Universe [1–3]. As its name suggests, EWBG refers to any mechanism that produces an asymmetry in the density of baryons during the electroweak phase transition (EWPT). While many specific realizations of EWBG have been proposed, they all have many features in common, and in this review we attempt to describe them in a unified way⁴.

The typical initial condition assumed for EWBG is a hot, radiation-dominated early Universe containing zero net baryon charge in which the full $SU(2)_L \times U(1)_Y$ electroweak symmetry is manifest [11–14]. As the Universe cools to temperatures below the electroweak scale, $T \lesssim 100$ GeV, the Higgs field settles into a vacuum state that spontaneously breaks the electroweak symmetry down to its $U(1)_{em}$ subgroup. It is during this phase transition that EWBG takes place.

Successful EWBG requires a first-order EWPT. Such a transition proceeds when bubbles of the broken phase nucleate within the surrounding plasma in the symmetric phase. We illustrate this process in figure 1. These bubbles expand, collide and coalesce until only the broken phase remains.

Baryon creation in EWBG takes place in the vicinity of the expanding bubble walls. The process can be divided into three steps [4]:

1. Particles in the plasma scatter with the bubble walls. If the underlying theory contains CP violation, this scattering can generate CP (and C) asymmetries in particle number densities in front of the bubble wall.

⁴ See [4–10] for previous reviews of EWBG.

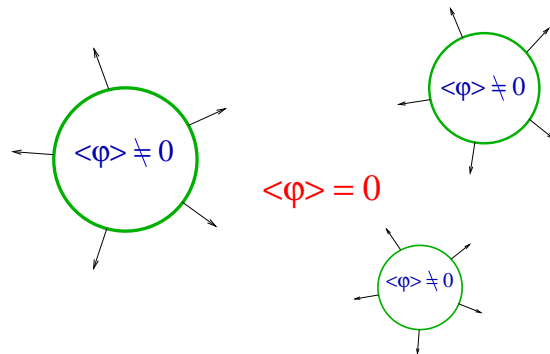


Figure 1. Expanding bubbles of the electroweak-broken phase within the surrounding plasma in the electroweak-symmetric phase.

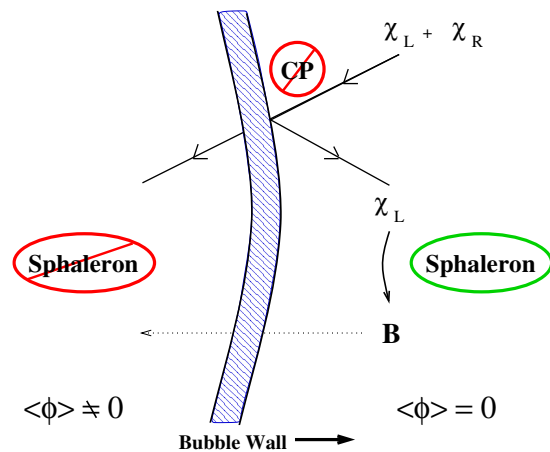


Figure 2. Baryon production in front of the bubble walls.

2. These asymmetries diffuse into the symmetric phase ahead of the bubble wall, where they bias electroweak sphaleron transitions [15, 16] to produce more baryons than antibaryons.
3. Some of the net baryon charge created outside the bubble wall is swept up by the expanding wall into the broken phase. In this phase, the rate of sphaleron transitions is strongly suppressed, and can be small enough to avoid washing out the baryons created in the first two steps.

We illustrate these three steps in figure 2.

These EWBG steps satisfy explicitly the three Sakharov conditions for baryon creation [17]. Firstly, departure from thermodynamic equilibrium is induced by the passage of the rapidly expanding bubble walls through the cosmological plasma. Secondly, violation of baryon number comes from the rapid sphaleron transitions in the symmetric phase. And thirdly, both C- and CP-violating (CPV) scattering processes are needed at the phase boundaries to create the particle number asymmetries that bias the sphalerons to create more baryons than antibaryons.

All the ingredients required for EWBG are contained in the Standard Model (SM). Unfortunately, EWBG is unable to explain the observed baryon asymmetry within the SM alone. The first impediment is that the SM EWPT is first-order only if the mass of the Higgs boson

lies below $m_h \lesssim 70$ GeV [18, 19]. This is much less than the experimental LEP II lower bound of $m_h > 114.4$ GeV [20] and the more recent LHC discovery of a Higgs-like boson with mass near 125 GeV [21, 22]. Even if the phase transition were first-order, the CP violation induced by the Cabibbo–Kobayashi–Maskawa (CKM) phase does not appear to be sufficient to generate large enough chiral asymmetries [23–25].

Therefore an essential feature of all viable realizations of EWBG is new physics beyond the SM. This beyond the Standard Model (BSM) physics must couple to the SM with at least a moderate strength, and it must be abundant in the thermal plasma at the time of the EWPT. Together, these two conditions imply the existence of new particles with masses not too far above the electroweak scale and direct couplings to the SM. Thus, a generic prediction of EWBG is that new phenomena should be discovered in upcoming collider and precision experiments. It is this property that sets EWBG apart from many other mechanisms of baryon creation.

Because of the prospects for experimental probes of EWBG, it is particularly important to achieve robust theoretical predictions for the baryon asymmetry within this framework as well as for the associated phenomenological implications within specific BSM scenarios. Consequently, we review both progress in developing the theoretical machinery used for computations of the baryon asymmetry as well as developments on the phenomenological front. The former entail a mix of non-perturbative Monte Carlo studies and various perturbative approximations. Work on the phenomenological side includes applications to specific BSM scenarios, such as the Minimal Supersymmetric Standard Model (MSSM), and the delineation of consequences for collider studies, low-energy probes of CP-violation and astrophysical observations.

The plan for this review is as follows. In section 2 we discuss the EWPT in greater depth, concentrating on its strength and other characteristics. Next, in section 3 we describe in more detail the creation of asymmetries in the CP and baryon charges during the phase transition. Some of the ways the new ingredients required for EWBG can be studied in the laboratory are discussed in section 4. Finally, section 5 is reserved for our conclusions.

2. The electroweak phase transition

Baryon creation in EWBG is closely tied to the dynamics of the EWPT. In this transition, the thermal plasma goes from a *symmetric* state in which the full $SU(2)_L \times U(1)_Y$ gauge invariance is manifest to a *broken* one where only the $U(1)_{\text{em}}$ electroweak subgroup remains [11, 13, 14]. As discussed above, the transition must be first-order and proceed through the nucleation of bubbles of the broken phase. In this section we will discuss the dynamics of this phase transition and describe the role it plays in EWBG.

The transition from symmetric to broken phase in the SM can be characterized by the vacuum expectation value (VEV) of the Higgs field $H \equiv (H^+, H^0)^T$ that transforms as $(\mathbf{1}, \mathbf{2}, 1/2)$ under $SU(3)_c \times SU(2)_L \times U(1)_Y$. A field basis can always be chosen such that only the real component of H^0 develops a non-zero expectation value. Thus, we will write

$$\phi/\sqrt{2} \equiv \langle H^0 \rangle. \quad (1)$$

The symmetric phase corresponds to $\phi = 0$ and the broken phase to $\phi \neq 0$. Note that (in unitary gauge) the masses of the W^\pm and Z^0 weak vector bosons and the fermions are proportional to ϕ .

The features of this transition that are most relevant for EWBG are (a) its character (first-order, second-order, cross over); (b) the critical temperature T_c and the bubble nucleation temperature T_n that describe when it occurs; (c) the sphaleron transition rate Γ_{sph} that governs the rate of baryon number generation and washout; and (d) the bubble nucleation rate. These features have been studied using a broad range of theoretic tools.

The most robust computations of many of these quantities are performed using non-perturbative, Monte Carlo methods. However, given the level of effort required to perform such studies, they have only been applied to a few specific theories of electroweak symmetry breaking. Instead, perturbative methods have been used much more frequently to study the dynamics of the EWPT in a broad range of BSM scenarios. Perturbative analyses can also provide helpful insight into some aspects of phase transition dynamics that may be less accessible with Monte Carlo methods. It should be emphasized, however, that the application of perturbation theory to EWPT physics is fraught with uncertainties as well as the potential for ambiguities. In the SM, for example, one often finds the transition temperature computed perturbatively to be significantly lower than the value obtained from Monte Carlo studies for a given value of the Higgs boson mass. Nevertheless, given the widespread use of perturbation theory, we begin by reviewing this approach, first laying out the conventional treatment and then commenting on various difficulties. We subsequently review salient features of the non-perturbative analyses.

2.1. Perturbative analyses

In a perturbative analysis of the EWPT, the central object is the (renormalized) finite-temperature effective potential. This quantity coincides with the free energy of the cosmological plasma [8, 26–28], provided it is reasonably close to thermodynamic equilibrium. The key feature of the effective potential is that the expectation value ϕ of the Higgs field is that which minimizes its value.

To one-loop order, the effective potential is given by [8]

$$V_{\text{eff}}(\phi, T) = V_0(\phi) + V_1(\phi) + \Delta V_1^{(T)}(\phi, T), \quad (2)$$

where $V_0 = -m^2\phi^2/2 + \lambda\phi^4/4$ is the tree-level potential, $V_1(\phi)^{(0)}$ is the one-loop effective potential at $T = 0$, and $V_1^{(T)}(\phi, T)$ contains the leading thermal corrections.

The expression for $V_1(\phi)$ is well-known [29]:

$$V_1(\phi) = \sum_i \frac{n_i(-1)^{2s_i}}{4(4\pi)^2} m_i^4(\phi) \left[\ln \left(\frac{m_i^2(\phi)}{\mu^2} \right) - \mathcal{C}_i \right], \quad (3)$$

where the sum i runs over all particles in the theory, each with n_i degrees of freedom, field-dependent mass $m_i(\phi)$ and spin. Furthermore, we have assumed a mass-independent renormalization with μ as the renormalization scale and the \mathcal{C}_i are scheme-dependent constants. Choosing $\mu \sim \max\{m_i(\phi)\}$ optimizes the perturbative expansion. Let us also mention that Fadeev–Popov ghosts are massless and decouple if we work in the Landau gauge ($\xi = 0$), in which case $n_i = 3$ should be used for each vector boson and contributions from Goldstone bosons included as well.

The thermal corrections are given at one-loop order by [8]

$$\Delta V_1^{(T)}(\phi, T) = \sum_{i=\text{boson}} n_i \frac{T^4}{2\pi^2} J_b \left(\frac{m_i^2}{T^2} \right) - \sum_{j=\text{fermion}} n_j \frac{T^4}{2\pi^2} J_f \left(\frac{m_j^2}{T^2} \right), \quad (4)$$

where J_b and J_f are loop functions. For small arguments, $x \ll 1$, they have the expansions [30]

$$J_b(x^2) = -\frac{\pi^4}{45} + \frac{\pi^2}{12}x^2 - \frac{\pi}{6}x^3 - \frac{1}{32}x^4 \ln(x^2/a_b) + \mathcal{O}(x^3), \quad (5)$$

$$J_f(x^2) = -\frac{7\pi^4}{360} - \frac{\pi^2}{24}x^2 - \frac{1}{32}x^4 \ln(x^2/a_f) + \mathcal{O}(x^3), \quad (6)$$

with $\ln(a_b) \simeq 5.4076$ and $\ln(a_f) \simeq 2.6351$. At large arguments, $x \gg 1$, both loop functions reduce to [30]

$$J_b(x^2) \simeq J_f(x^2) = \left(\frac{x}{2\pi}\right)^{3/2} e^{-x} \left(1 + \frac{15}{8x} + \mathcal{O}(x^{-2})\right). \quad (7)$$

This form shows the familiar Boltzmann suppression of particles much heavier than the temperature.

To illustrate the effect of thermal corrections on the Higgs potential, it is helpful to write the potential in a simplified approximate form using the high-temperature expansions of equations (5), (6), noting that heavy particles ($m \gg T$) decouple quickly. This yields [30]

$$V_{\text{eff}}(\phi, T) \simeq D(T^2 - T_0^2)\phi^2 - ET\phi^3 + \frac{\bar{\lambda}}{4}\phi^4, \quad (8)$$

where D and $\bar{\lambda}$ are slowly varying functions of T (but not ϕ).

In the limit of $E = 0$ in equation (8) the phase transition is second-order, with a transition temperature of $T = T_0$ and a Higgs expectation value for $T < T_0$ of

$$\phi = T_0 \sqrt{\frac{2D}{\bar{\lambda}}(1 - T^2/T_0^2)}. \quad (9)$$

For non-zero E in equation (8), the phase transition becomes first-order. Starting from $T \gg T_0$, a second minimum away from the origin develops when $T = T_1$ with

$$T_1 = T_0 \sqrt{\frac{8\bar{\lambda}D}{8\bar{\lambda}DT_0^2 - 9E^2}}, \quad (10)$$

where the temperature-dependent coefficients D and $\bar{\lambda}$ are to be evaluated at $T = T_1$. This second symmetry-breaking minimum becomes degenerate with the origin at the *critical temperature* T_c , and becomes deeper at lower temperature, as illustrated in figure 3. The degree to which the phase transition is first-order is typically characterized by ϕ_c/T_c , where ϕ_c is the location of the minimum at T_c . In terms of the parameters in the potential, it is

$$\frac{\phi_c}{T_c} = \frac{2E}{\bar{\lambda}}. \quad (11)$$

Sometime after the temperature falls below T_c , regions of the cosmological plasma tunnel to the deeper broken minimum and the phase transition proceeds by the nucleation of bubbles.

Before discussing the dynamics of such a first-order phase transition, it is worth examining the validity of the perturbative expansion outlined above. This expansion is known to break down at very high temperatures when the thermal loop expansion parameter $g^2 T^2/m^2(\phi)$ becomes large [14, 31] (where g^2 is the coupling entering in the loop). Indeed, we saw above that the leading thermal corrections, which are only generated by loops in this formalism, completely change the vacuum structure of the theory and induce a restoration of symmetry

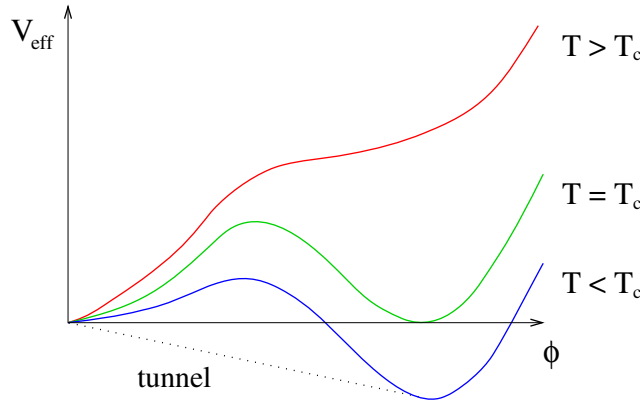


Figure 3. Schematic temperature dependence of the effective potential.

at very high temperatures. The breakdown of the perturbative expansion can be postponed by resumming the most dangerous thermal corrections by incorporating thermal mass corrections in the propagators. The net result of such a *daisy resummation* is to generate an additional term in the effective potential [32]:

$$V_1^{(\text{daisy})} = -\frac{T}{12\pi} \sum_{\{b\}'} n_b [\bar{m}_b^2(\phi, T) - m_b^2(\phi)]^{3/2}, \quad (12)$$

where the sum runs only over scalars and longitudinal vectors, and \bar{m}^2 is the field-dependent thermal squared mass:

$$\bar{m}^2(\phi) = m^2(\phi) + \Pi(T), \quad (13)$$

with $\Pi(T) \propto T^2$ the thermal contribution to the mass.

The daisy correction is particularly important for a first-order transition because it affects primarily the crucial cubic term. For example, suppose the contribution to the cubic term comes from a scalar with a zero-temperature mass of $m^2(\phi) = g\phi^2$ with a thermal correction of $\Pi(T) = \kappa T^2$. The would-be cubic term becomes

$$\Delta E \phi^3 = \frac{1}{12\pi} g^{3/2} \phi^3 \rightarrow \frac{1}{12\pi} [g\phi^2 + \kappa T^2]^{3/2}. \quad (14)$$

When $\Pi(T)$ is large relative to $m^2(\phi)$, this corrected expression ceases to behave as a cubic in ϕ and the phase transition might no longer be first-order.

When the EWPT is first-order, it proceeds by the nucleation of bubbles of the broken phase within the surrounding plasma of the symmetric phase. Bubble nucleation is governed by thermal tunneling [33] from the local minimum at $\phi = 0$ to a deeper minimum at $\phi \neq 0$. In nucleating a bubble there is a competition between the decrease in free energy, proportional to bubble volume, with the increase due to the tension of the wall, proportional to bubble area. As such, there is a minimum radius for which a bubble can grow after it is formed, and this limits the tunnelling rate. Bubble formation and growth only begins in earnest when this rate exceeds the Hubble rate, which occurs at some temperature $T_n < T_c$, called the *nucleation temperature*. Once a sufficiently large bubble is formed, it expands until it collides with other bubbles and the Universe is filled with the broken phase. The typical profile and expansion rate of a bubble wall can be computed from the effective potential [30, 34, 35], taking into account frictional

effects from scattering with surrounding particles in the plasma [36–38]. As we will see in the next section, baryon creation processes are very sensitive to the speed and profile of the walls.

A first-order EWPT is not sufficient for successful EWBG. The transition must also be *strongly first-order*. Within the context of perturbation theory calculations, the quantitative condition for a strongly first-order phase transition has typically been taken to be

$$\frac{\phi_c}{T_c} \gtrsim 1. \quad (15)$$

This ratio approximates a factor that appears in the rate for sphaleron transitions in the broken phase within the bubble walls, to be discussed in more detail below (see equation (22) and following)⁵. When this condition is not met, these transitions will wash out the baryons created by EWBG. As we will describe below, the necessity of a very strong phase transition is one of the reasons why EWBG does not work in the SM, and is therefore a strong motivator of new physics beyond the SM.

While the condition of equation (15) is a frequently applied approximation, obtaining a robust calculation of the baryon abundance from EWBG requires addressing several issues. Perhaps the most significant is the reliability of perturbation theory. As alluded to above and as recently discussed in [50], a comparison of perturbative computations with those obtained using non-perturbative methods (see section 2.2) often reveals significant quantitative differences on quantities such as T_c . On the other hand, perturbation theory generally reproduces trends associated with the variation of underlying model parameters, such as the mass of the Higgs boson. For the purpose of determining the precise numerical values of underlying parameters that yield a first-order *versus* second-order or cross-over transition, one should rely on the results of non-perturbative computations. At the same time, perturbation theory is the only feasible approach for surveying a broad range of BSM scenarios and identifying the general regions of model parameter space that are likely to yield viable EWBG. One can then perform Monte Carlo computations that focus on a more limited range of parameters within a given model.

Within the context of perturbative studies, several additional considerations arise. Here, we survey a few of these issues including gauge invariance as well as a variety of sources of theoretical uncertainties. Beginning with the former, the lack of gauge invariance in conventional perturbative analyses has been a topic of recent interest [50–52]. In particular, it is well-known that the VEV of the one-loop effective potential ϕ at any temperature is gauge-dependent [41–51], so that the ratio on the left-hand side of equation (15) is not a well-defined physical quantity. Moreover, the procedure outlined above to determine T_c perturbatively also introduces a spurious gauge-dependence, as one may observe by expressing the right side of equation (11) in an arbitrary gauge [50]:

$$\frac{\phi_c}{T_c} = \frac{2E}{\bar{\lambda}} = \frac{3 - \xi^{3/2}}{48\pi\lambda} [2g_2^3 + (g_1^2 + g_2^2)^{3/2}] + \dots, \quad (16)$$

where the additional terms are ξ -dependent contributions associated with the one-loop corrections to the Higgs quartic self-coupling. As indicated above, the conventional analyses have been performed in the Landau gauge, even though a small change in the choice of gauge parameter can significantly alter the ratio ϕ_c/T_c .

Obtaining a gauge-invariant *baryon number preservation criterion* (BNPC) requires several modifications of the naïve perturbative treatment described above:

⁵ One should keep in mind that the relevant temperature for the dynamics is the slightly lower bubble nucleation temperature rather than the critical temperature, although it is often the case that $T_n \simeq T_c$ [39, 40].

1. Determine T_c (or T_n) in a gauge-invariant manner by following the evolution of $V_{\text{eff}}(\phi, T)$ and consistently implementing the so-called Nielsen identities [42, 43]. One procedure for doing so entails carrying out an \hbar -expansion of $V_{\text{eff}}(\phi, T)$, as outlined in [43, 47, 50]. A generalization of this procedure also allows one to approximate the full daisy resummation in a gauge-invariant way and to reproduce the trends for T_c found in nonperturbative calculations [50]. This approach entails evaluating the one-loop $V_{\text{eff}}(\phi, T)$ with the value of the field ϕ_0 that minimizes the tree-level potential, while in equation (12) one makes the replacement

$$[\bar{m}_b^2(\phi, T) - m_b^2(\phi)]^{3/2} \rightarrow [\bar{m}_b^2(\phi_0(T), T) - m_b^2(\phi_0)]^{3/2}, \quad (17)$$

where $\phi_0(T)$ minimizes the one-loop potential in the high- T limit (obtained by retaining only the thermal mass corrections in equation (13)). The result is a set of manifestly gauge-invariant functions of T (one for each extremum) whose evolution with T can be used to obtain a gauge-invariant T_c . Within the SM, this value is generally in better agreement with the results of lattice computations than the value obtained using the conventional approach in the Landau gauge.

This approach as well as alternatives have been applied to the Abelian Higgs model [49, 51, 52]. Using a Hamiltonian approach [49], it is possible to obtain a gauge-invariant effective potential, though an extension including the daisy resummation has yet to be developed. When $V_1^{(\text{daisy})}$ is not included, computations of T_c and the latent heat obtained with the conventional approach in the Landau gauge agree to a high degree with those obtained using the Hamiltonian formulation [51]. More recently, the authors of [52] argued that by adopting a power counting in which the Higgs self-coupling $\lambda \sim g^3$ (g is the Abelian gauge coupling) and including terms linear in T in the would-be Goldstone boson mass in $V_1^{(\text{daisy})}$, the gauge dependence is of higher-order in g , rendering the gauge-dependence more gentle when the coupling is sufficiently small. The feasibility of extending the latter approach as well as the Hamiltonian formulation to a non-Abelian theory remains to be demonstrated.

As discussed below, there exists considerable interest in BSM scenarios that introduce new scalars that carry no SM gauge charges. The presence of these singlets may allow for the appearance of a tree-level barrier between the broken and unbroken phases, suggesting that the character of the transition at finite- T may depend less decisively on the gauge-degrees of freedom than in the SM or Abelian Higgs model. In a recent study of the latter model augmented by a gauge singlet scalar S [53], the authors find that the presence of a tree-level cubic term $H^\dagger HS$ does not by itself render the gauge dependence less severe, though it becomes less pronounced when the strength of the first-order phase transition (as measured by the magnitude of the latent heat) grows.

2. Perform a gauge-invariant computation of the energy of the sphaleron configuration, E_{sph} . In perturbation theory, it is possible to do so in the broken phase by working with the high-temperature effective theory in which zero-temperature masses are replaced by their (gauge-invariant) Debye masses. The energy E_{sph} then depends on a gauge-invariant scale $\bar{v}(T)$ that is not the same as $\phi(T)$, and the fluctuation determinant κ that characterizes the leading quadratic corrections to the sphaleron action [54–56].
3. Compute the baryon density n_B at the end of the EWPT, corresponding to a time delay of Δt_{EW} after its onset, and compare with the initial density resulting from the CPV transport

dynamics described in section 3 below. The resulting ratio is called the ‘washout factor’

$$S = \frac{n_B(\Delta t_{EW})}{n_B(0)}. \quad (18)$$

For the baryon asymmetry created by EWBG to be preserved, the washout factor S must not be too small.

Rewriting the washout factor in terms of X , defined according to

$$S > e^{-X}, \quad (19)$$

the quantitative BNPC is [50]:

$$\frac{4\pi B}{g} \frac{\bar{v}(T_c)}{T_c} - 7 \ln \frac{\bar{v}(T_c)}{T_c} > -\ln X - \ln \left(\frac{\Delta t_{EW}}{t_H} \right) + \ln \mathcal{Q} \mathcal{F} + \hbar \ln \kappa. \quad (20)$$

Here B parameterizes the relationship between the scale $\bar{v}(T)$ and the sphaleron energy [15, 57]

$$E_{\text{sph}}(T) \simeq B \frac{2m_W}{\alpha_w} \left(\frac{\bar{v}(T)}{v(0)} \right), \quad (21)$$

where B is a constant of order unity that depends on the mass of the Higgs boson, $v(0) = 174 \text{ GeV}$ is the value of the Higgs VEV at $T = 0$, and α_w is the weak coupling. The other quantities in equation (20) include: the Hubble time t_H ; a quantity \mathcal{Q} characterizing the contribution of sphaleron zero modes; a function \mathcal{F} that characterizes the dependence of the unstable mode of the sphaleron on $\bar{v}(T)$; and a factor κ accounting for fluctuations that are not zero modes. The appearance of the logarithms in equation (20) and the dependence on Δt_{EW} result from integrating the baryon number evolution equation [18, 58]

$$\frac{dn_B}{dt} \simeq -\frac{13N_f}{2} \frac{\Gamma_{\text{ws}}}{VT^3} n_B, \quad (22)$$

where N_f is the number of fermion families and $\Gamma_{\text{ws}}/VT^3 \propto \exp(-E_{\text{sph}}/T)$ is the sphaleron rate per unit volume inside the bubble. Qualitatively, the BNPC in equation (20) corresponds to the requirement that the sphaleron rate in the broken phase during the phase transition be much slower than the Hubble expansion rate.

The quantities in equation (20) point to the various sources of theoretical uncertainty that arise, including but not limited to the issue of gauge invariance. For example, the conventionally employed condition of equation (15) results from replacing the gauge-invariant ratio $\bar{v}(T_c)/T_c$ by the gauge-dependent one ϕ_c/T_c and making specific choices for the parameters appearing in equation (20). In particular, it has been assumed that one may take $X = 10$ [3, 18], corresponding to allowing the initial baryon asymmetry to be five orders of magnitude larger than what is presently observed—an assumption that is questionable in light of recent studies of the CPV transport dynamics discussed in section 3. Additional significant uncertainties are associated with the value of the fluctuation determinant κ and the duration of the transition Δt_{EW} . In short, even if one employs an appropriately gauge-invariant procedure to determine the degree of baryon number preservation, considerable uncertainty remains as to the precise requirement.

Nearly all phenomenological studies carried out over the past decade or so have neglected one or more of these issues. Even if one places some trust in the use of perturbation theory to analyze EWPT dynamics relevant to EWBG, it should be clear that considerable work

Table 1. Maximum values of the Higgs boson mass, M_h^C , for a first-order EWPT in the SM as obtained from lattice studies.

| Lattice | Authors | M_h^C (GeV) |
|----------------|---------|----------------|
| 4D Isotropic | [76] | 80 ± 7 |
| 4D Anisotropic | [74] | 72.4 ± 1.7 |
| 3D Isotropic | [72] | 72.3 ± 0.7 |
| 3D Isotropic | [70] | 72.4 ± 0.9 |

remains to obtain precision statements about the presence or absence of a sufficiently strong first-order transition in a given BSM scenario. It may be, for example, that a given BSM scenario significantly modifies the dependence of E_{sph} on the gauge-invariant scale $\bar{v}(T_c)$, the dependence of \bar{v} on T_c itself, the duration of the transition, or the fluctuation determinant. While existing perturbative analyses have proven extremely useful in identifying theories whose EWPT dynamics can allow for viable EWBG, in light of the open theoretical issues we encourage a revisitation of these calculations, especially if they are to be compared with direct experimental tests.

2.2. Non-perturbative studies

Dedicated non-perturbative numerical analyses of the EWPT have been carried out for the SM, the MSSM and the two-Higgs-doublet model (2HDM) [19, 59–78]. Among the properties studied that are particularly relevant to EWBG are the critical temperature T_c , the weak sphaleron rate Γ_{sph} (the focus of [61, 62, 75]), and the character of the transition (first- or second-order, cross over, etc). As we discuss in section 4.3, the latent heat L is also critical for the amplitude of gravity wave production, and it has been studied in, for example, [19].

The process of bubble nucleation that is the starting point for EWBG requires a first-order phase transition. In the SM, the presence of a first-order transition is found to require a sufficiently light Higgs boson. Consequently, considerable attention has been paid to the value of the maximum value of the Higgs mass for which a first-order transition exists. Representative results from lattice studies are given in table 1. The results obtained with the three-dimensional (3D) lattices require first carrying out the procedure of dimensional reduction to a the 3D effective theory (see, e.g., [65]) before studying the phase transition properties of the latter using Monte Carlo methods. For either 3D or 4D studies, a criterion must be identified for determining the character of the phase transition. Among those employed are the susceptibility associated with the scalar field $\chi \propto \langle (\phi^\dagger \phi - \langle \phi^\dagger \phi \rangle)^2 \rangle$ and correlation lengths. The scaling behavior of χ with lattice volume can be used to determine whether the transition is first-order, second-order or cross over. For $M_h \gg M_h^C \simeq 75$ GeV, as implied by collider searches for the Higgs, the transition appears to be a cross-over transition.

A first-order transition can be accomplished by introducing additional scalar fields that couple to the Higgs sector. As discussed below, a particularly important example is the MSSM where the scalar top quarks couple strongly to the Higgs fields. Lattice studies imply that for sufficiently light right-handed (RH) stops, \tilde{t}_R , the transition can be not only first-order but strongly so, and that T_c decreases with the RH stop mass. The lowering of T_c is important for

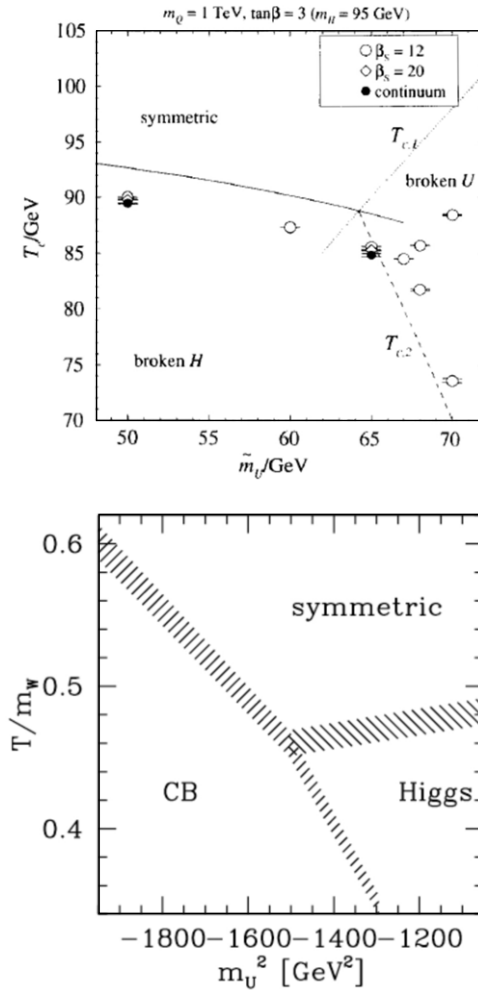


Figure 4. Dependence of the critical temperature T_c in the MSSM on the SUSY-breaking RH stop mass parameter m_U taken from [71] (top panel) and [77] (bottom panel). Note that the contribution to the \tilde{t}_R mass-squared from this parameter goes as $-\tilde{m}_U^2 = m_U^2$. The phase labeled ‘CB’ or ‘broken U’ denotes a phase in which the stop field acquires a non-zero VEV, corresponding to a color and charge-breaking vacuum. Top panel reprinted from Laine and Rummukainen [71], copyright 1998 with permission from Elsevier. Bottom panel reprinted with permission from Csikor *et al* [77], copyright 2000 by the American Physical Society.

the protection of the baryon asymmetry from washout by EW sphalerons inside the expanding bubbles, since at the onset of the transition $\Gamma_{\text{sph}} \sim \exp(-E_{\text{sph}}/T_c)$. Lowering T_c reduces Γ_{sph} by both reducing the magnitude of the denominator in the exponential and increasing the sphaleron energy E_{sph} . Results for the dependence of T_c on the supersymmetry (SUSY)-breaking RH stop mass parameter obtained from [71, 77] are shown in figure 4. Note that the stop mass-squared parameter must be negative to lower T_c . Increasing its magnitude in this parameter space region thus lowers the overall mass of the \tilde{t}_R .

2.3. Extending the Standard Model scalar sector

The need for a strongly first-order EWPT is one of the two reasons why EWBG does not work in the SM. Indeed, the failure of EWBG in the SM (or baryogenesis of any form) is a motivation for new physics near the electroweak scale. Such new physics is also needed to stabilize the electroweak scale itself, and can also account for the dark matter (DM). While a broad range of extensions of the SM have been proposed to strengthen the EWPT to allow for EWBG, most of them fall into two groups. In the first group—exemplified by the MSSM—new scalars couple to the Higgs field and enhance the cubic term in the effective potential by running in loops. The second group consists of scalar fields coupling to the Higgs that develop non-trivial dynamics in the early Universe that influences the effective Higgs potential directly. A third and more radical direction is to modify the cosmological evolution during the EWPT away from radiation-domination. In all cases, new light scalars with significant couplings to the Higgs are typically needed, and these may lead to observable effects at colliders.

In the first class of new physics, in which a new scalar X modifies the Higgs potential through its loop effects, the relevant interactions can usually be written in the form [39, 79]

$$-\mathcal{L} \supset M_X^2 |X|^2 + \frac{K}{6} |X|^4 + Q |X|^2 |H|^2. \quad (23)$$

The third term is a *Higgs portal* coupling that cannot be forbidden by symmetries. Assuming that X does not develop an expectation value, the mass of the physical complex scalar is

$$m_X^2 = M_X^2 + \frac{Q}{2} \phi^2. \quad (24)$$

Applying this to the effective potential yields

$$\Delta V_{\text{eff}}(\phi, T) \supset -\frac{n_X T}{12\pi} [\Pi_X(T) + M_X^2 + Q \phi^2/2]^{3/2}, \quad (25)$$

where $\Pi_X(T)$ is the thermal mass of X and n_X is the number of degrees of freedom. If $Q \phi^2/2$ is much larger than the other terms for $\phi \simeq \phi_c$, this correction gives a strong enhancement of the cubic operator that drives a first-order phase transition. If X is charged under $SU(3)_c$, the contribution to the cubic is further enhanced at two-loop order by corrections involving virtual gluons [80, 81]. The net result is that a strongly first-order EWPT can be obtained for $Q \gtrsim 1$ and $M_X^2 \lesssim 0$, if X is a $SU(3)_c$ triplet, but much larger Q values are needed if X is a gauge singlet [81, 82].

New scalars coupling in this way to the Higgs field have been studied extensively in the context of SUSY and especially within the MSSM. For early perturbative studies, see [83, 85, 86]. In this case the X scalar corresponds to the lightest scalar top quark (stop). It is a $SU(3)_c$ triplet with electric charge $q = 2/3$, and it must be mostly RH to be both light and consistent with precision electroweak data [39]. The other (mostly left-handed (LH)) stop must be considerably heavier to push up the mass of the Higgs boson [39]. The couplings in equation (23) are fixed by SUSY to be $Q \simeq y_t^2$ and $K \simeq 4\pi\alpha_s$ (up to small corrections from electroweak effects and left–right stop mixing), while the M_X^2 mass term corresponds to the RH stop soft mass-squared.

A first-order phase transition strong enough for EWBG is found to be marginally consistent with the MSSM [39, 71, 87]. As discussed above, in order to quench the sphaleron rate by lowering T_c , a negatively valued M_X^2 mass term is needed to cancel against the thermal mass appearing in equation (12) [39]. This has the effect of destabilizing the origin of the scalar

field space in the X direction, making possible an expectation value for the X field. Such a VEV would be disastrous since it would imply the spontaneous breakdown of electric charge and color. However, a detailed computation of the thermal evolution of the effective potential for ϕ and X finds that slightly negative values of M_X^2 , but still large enough for EWBG, are phenomenologically acceptable. In this scenario, thermal effects can stabilize the X direction more strongly than the ϕ direction, and the system can evolve first to a local minimum with $\phi \neq 0$ and $X = 0$. This local minimum might not be as deep as the charge-breaking minimum with $X \neq 0$, but it can be sufficiently long-lived to describe the Universe we observe. A negative M_X^2 also implies a very light stop mass, which forces the other heavier stop to be extremely heavy to drive up the mass of the lightest Higgs boson.

A second way to make the EWPT more strongly first-order is to couple the Higgs to a new scalar that develops a VEV near the electroweak scale [88–94]. A simple example of this is

$$-\mathcal{L} \supset m_N^2 N^2 + A_N N^3 + \lambda_N N^4 + (A_H N + \zeta_H N^2) |H|^2 + \dots \quad (26)$$

These interactions can allow both H and N to develop expectation values, resulting in a mixing between the physical singlet and $SU(2)_L$ scalars in the theory. When the singlet and $SU(2)_L$ mass parameters are similar, it is convenient to track the evolution of the VEVs in polar coordinates [88, 92]:

$$\langle H^0 \rangle = \varphi \cos \alpha, \quad \langle N \rangle = \varphi \sin \alpha. \quad (27)$$

Applying this parametrization to equation (26), one obtains cubic terms in the tree-level potential for φ that can lead to a strongly first-order EWPT. The singlet can also strengthen the phase transition by contributing to the loop-induced cubic term in the effective potential or by reducing the effective Higgs quartic coupling near the critical temperature [92]. Similar effects have been found in gauge extensions of the SM [95] as well as in theories with two or more $SU(2)_L$ doublets [78, 96–99].

When the characteristic mass scale of the singlet sector is significantly larger than the $SU(2)_L$ part, the singlet can be integrated out of the theory. This produces effective Higgs interactions of the form

$$-\mathcal{L} \supset -\mu^2 |H|^2 + \lambda |H|^4 + \frac{1}{\Lambda_N^2} |H|^6 + \dots, \quad (28)$$

where Λ_N characterizes the mass scale of the singlet sector. For values not too large, $\Lambda_N \lesssim 1000$ GeV, the new sextic term can also drive a strongly first-order EWPT [100–102].

In addition to these two classes of mechanisms to strengthen the EWPT during a radiation-dominated universe, there are proposals that rely on alternative cosmological histories [103–105]. These scenarios frequently also contain new scalar fields that couple to the Higgs or other new physics that could be observed at low energies. A prime example is *cold EWBG* [104–109], where the evolution of the Universe is assumed to be dominated for a period by the dynamics of a new scalar field Φ that interacts with the Higgs, such as an inflaton [106] or a dilaton controlling the size of an extra spatial dimension [109]. For appropriate Φ -Higgs couplings, this dynamics can trap the Higgs field at its symmetry-preserving origin down to temperatures much lower than the electroweak scale. Eventually, Φ is assumed to evolve such that the origin of the Higgs potential becomes unstable, and the energy of Φ is transferred to non-trivial Higgs configurations. Some of these configurations are expected to carry non-zero winding numbers, which can translate into the production of baryons when they decay [110]. This also has the effect of reheating the Universe to a temperature that is small relative to the

electroweak. A net baryon number can be created with new CPV Higgs couplings [107], or possibly even from the CP violation present in the SM [111].

3. Creating CP asymmetries and baryons

Baryons are created in EWBG through a combination of scattering, diffusion and transfer reactions in the vicinity of the expanding bubble walls during the EWPT. Sphaleron transitions are rapid in the symmetric phase outside the bubbles, and they provide the requisite source of baryon number violation. However, sphalerons alone are not enough; a net CP asymmetry is also needed to bias the sphalerons to produce more baryons than antibaryons.

The CP asymmetry relevant for EWBG is n_L , the excess number density of LH fermions over their antiparticles. Such an asymmetry can be created during the EWPT together with an equal opposite asymmetry in n_R by CPV interactions in the bubble wall. However, since sphalerons correspond to transitions between distinct $SU(2)_L$ vacua, only n_L directly affects baryon creation. The corresponding equation for the baryon density n_B is

$$\partial_\mu j_B^\mu = -\frac{N_f}{2} [k_{ws}^{(1)}(T, x)n_B(x) + k_{ws}^{(2)}(T, x)n_L(x)], \quad (29)$$

where $j_B^\mu = (n_B, \vec{j}_B)$ is the baryon number current density, x is the coordinate orthogonal to the bubble wall, and $k_{ws}^{(j)}(T, x)$ are the weak sphaleron rate constants that account for the change in rate outside and inside the bubbles. Outside one has [58]

$$\begin{aligned} k_{ws}^{(1)}(T, x) \Big|_{\text{out}} &= \mathcal{R} \times \frac{\Gamma_{ws}}{VT^3}, \\ k_{ws}^{(2)}(T, x) \Big|_{\text{out}} &= \frac{\Gamma_{ws}}{VT^3}, \end{aligned} \quad (30)$$

with Γ_{ws}/V giving the weak sphaleron rate per unit volume for N_f fermion families

$$\begin{aligned} \frac{\Gamma_{ws}}{VT^3} \Big|_{\text{out}} &= 6\kappa\alpha_W^5 T, \\ \mathcal{R} &\simeq \frac{15}{4} \end{aligned} \quad (31)$$

and $\kappa \simeq 20$ [58]. Deep inside the bubble these expressions become

$$k_{ws}^{(1)}(T, x) \Big|_{\text{in}} = \frac{13N_f}{2} \frac{\Gamma_{ws}}{VT^3}, \quad (32)$$

$$k_{ws}^{(2)}(T, x) \Big|_{\text{in}} \approx 0. \quad (33)$$

The computation of Γ_{ws}/V inside the bubble has been discussed in section 2. Note that equation (22) used in determining the washout factor is an approximation to equation (29) that neglects \vec{j}_B inside the bubble. It is clear from equation (29) that without the chiral asymmetry n_L , no net baryon charge will be created.

The production of n_L arises from interactions of particles with the bubble wall. The corresponding interaction rates are typically much faster than $k_{ws}(T, x)$ so that in practice one may decouple equation (29) from the system of equations that govern n_L production. The latter

encode a competition between several distinct dynamics:

- (a) C- and CPV interactions with the bubble wall that lead to the generation of particle number asymmetries for one or more species;
- (b) particle number-changing reactions that tend to drive the plasma toward chemical equilibrium;
- (c) flavor oscillations that result from off-diagonal mass-matrix elements;
- (d) scattering and creation-annihilation reactions that cause diffusion of the particle asymmetries ahead of the bubble wall and that push the system toward kinetic equilibrium in this asymptotic region.

In the earliest work on this problem, these equations were reasonably assumed to have the form motivated by kinetic theory [112]

$$\partial_\mu j_k^\mu = - \sum_{a,\ell} \Gamma_a^{k\ell} \mu_\ell + S_k^{\text{CPV}}, \quad (34)$$

where $j_k^\mu = (n_k, \vec{j}_k)$ denotes the current density for a given species of particle ‘ k ’, $\Gamma_a^{k\ell}$ is the rate for a given reaction ‘ a ’ that affects the chemical potentials of particle species ‘ ℓ ’, and S_k^{CPV} is a CPV source term. Diffusion arises in this formalism by making the diffusion *ansatz*, which relates the three-current to the gradient of the number density:

$$\vec{j}_k = D_k \vec{\nabla} n_k, \quad (35)$$

where $D_k(x, T)$ is the *diffusion constant* for the particle species.

The reaction rate $\Gamma_a^{k\ell}$ terms in equation (34) couple different particle currents to one another. For example, the top Yukawa interaction involving the third-generation SM quark doublet Q , the RH top quark T , and the Higgs doublet H leads to a term of the form

$$-\Gamma_Y (\mu_Q - \mu_T - \mu_H) \quad (36)$$

in the transport equation for j_Q^μ that couples to j_T^μ and j_H^μ . CP-violation in this example is embodied by the source S_Q^{CPV} , that tends to generate a non-zero number density n_Q . This number density would subsequently be diluted by the reaction term of equation (36) that transfers some of it to the T and H densities.

Under the assumptions leading to equation (34), a robust determination of n_L entails identifying all of the relevant particle species involved in the plasma dynamics, computing the relevant CPV sources and particle number changing reaction rates, and solving the resulting set of coupled equations. Significant progress has been achieved over the years on all aspects of the problem. We first review studies of the particle number changing reactions. Next, we discuss recent advances in deriving reliable CPV sources. Throughout the discussion, we will use the MSSM as our primary example since this is the theory in which these issues have been studied in the greatest detail.

Before proceeding, we make a few preliminary comments regarding time scales. An important consideration in determining the relative importance of a given process in the production of n_L is the associated time scale compared to the time scale for diffusion ahead of the bubble wall. As outlined in [113–115], in order for a given particle density to affect the dynamics of n_L generation in the unbroken phase, that density must diffuse ahead of the advancing wall. The time it resides in the unbroken phase is the time it takes for the advancing wall to ‘catch up’ with the diffusing density. For a given time t , the diffusion length is

$d_{\text{diff}} = \sqrt{\bar{D}t}$, where \bar{D} is an effective diffusion constant formed from an appropriate combination of individual diffusion constants D_k . The distance traversed by the wall is $d_{\text{wall}} = v_w t$. Equating the two leads to the diffusion time scale: $\tau_{\text{diff}} = \bar{D}/v_w^2$. Taking representative estimates for the effective diffusion constant $\bar{D} \simeq 50/T$ and wall velocity $v_w \simeq 0.05$ leads to $\tau_{\text{diff}} \sim 10^4/T$. Any process X having $\tau_X \ll \tau_{\text{diff}}$ must be included in the analysis of dynamics leading to n_L production, whereas for $\tau_X \gg \tau_{\text{diff}}$ the process X effectively decouples. In particular, the rate for electroweak sphaleron transitions implies $\tau_{\text{EW}} \gg \tau_{\text{diff}}$ so that one may first solve the dynamics leading to n_L and then use the latter as an input for the generation of n_B via equation (29).

Note that the wall velocity plays a significant role through its impact on τ_{diff} . As v_w increases, other processes have less time to equilibrate before the relevant particle species are captured by the bubble. This effect is particularly important when n_L is sourced by CPV interactions involving BSM degrees of freedom. In order for any charge asymmetry involving the latter to be transferred into a non-vanishing n_L , the particle number-changing reactions that facilitate this transfer must take place more quickly than the time it takes for the wall to overtake the diffusion process.

3.1. Particle number changing reactions

Tracking the full set of coupled particle number densities can be very complicated. For instance, in the MSSM with CP-violation in the Higgsino–gaugino sector, the resulting set of coupled equations can involve up to 30 or more components. Fortunately, in many cases the scope of the problem can be significantly reduced.

The most important simplification to the coupled equations is to relate algebraically the number densities of different particle species linked by reactions that are very fast compared to the other time scales of the problem (such as the diffusion time or the passage time of the bubble wall). In our top Yukawa example in equation (36), the corresponding reaction is typically very fast with $\tau_{Y_t} \ll \tau_{\text{diff}}$, implying that this process achieves chemical (as opposed to kinetic) equilibrium well before the Q , H and T densities are captured by the advancing wall. Consequently, it is an excellent approximation to set

$$\mu_Q - \mu_T - \mu_H = 0. \quad (37)$$

This reduces the number of coupled equations by one.

A frequent simplification arises in supersymmetric theories such as the MSSM as a result of ‘superequilibration’, wherein $\mu_P = \mu_{\tilde{P}}$ with P and \tilde{P} denoting an SM particle and its superpartner, respectively. Superequilibrium may arise either when a given supergauge interaction is fast compared to the time scale for diffusion ahead of the advancing bubble wall, or a chain of Yukawa reactions effectively yields $\mu_P = \mu_{\tilde{P}}$. Exceptions may occur, however, when either the gauginos become heavy, thereby suppressing the corresponding supergauge reaction rates, or a chain of Yukawa reactions is kinematically blocked.

Recently, the authors of [115] carried out an analysis of the particle number changing reactions for the MSSM under the assumptions leading to the general form of the transport equations in equation (34), obtaining numerical solutions to the full set of coupled transport equations. Superequilibrium is found to occur in significant regions of the parameter space. Typical results for various particle number density profiles obtained in this work are given in figure 5. Baryon number generation is governed by the size of the diffusion tail for n_L (red curve) ahead of the advancing wall ($z < 0$).

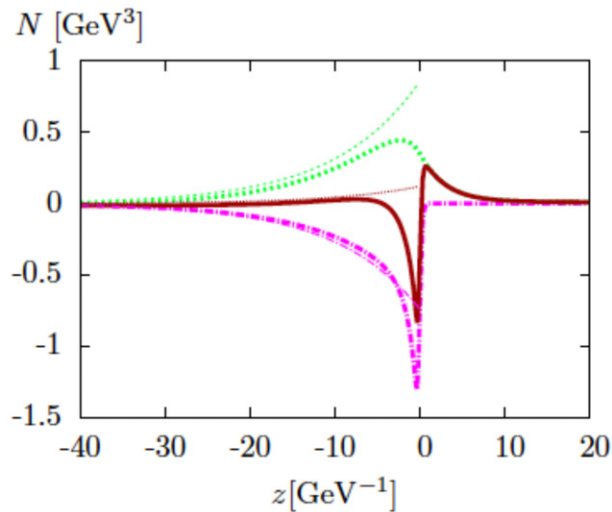


Figure 5. Particle number profiles with respect to the bubble wall ($z = 0$) obtained in the MSSM [115]. Pink, green and red curves give, respectively, number densities of third generation LH quarks, third generation LH leptons, and total n_L . Bubble wall interior corresponds to $z > 0$. Thin curves represent results of an analytic approximation valid sufficiently far in front of the wall. Reprinted from Chung *et al* [115], copyright 2009 with permission from JHEP.

For scenarios involving more than a single Higgs doublet H , such as the MSSM, an additional situation involving Yukawa interactions may arise that can substantially alter the generation of n_L . In the SM, the hierarchy of fermion Yukawa couplings implies that only τ_Y is much shorter than τ_{diff} and that one need consider only the $Q-T-H$ interactions indicated above. In a 2HDM scenario, however, the bottom quark (squark) and tau (stau) Yukawa couplings may be enhanced with respect to their SM values by $\tan\beta$, implying that the Γ_Y involving these particles grows as $\tan^2\beta$. For $\tan\beta \gtrsim 5$ (20), the bottom (tau) Yukawa reactions effectively equilibrate on a time scale shorter than the diffusion time scale, implying that one cannot neglect their effect on the coupled set of transport equations [113].

In the MSSM case, the net effect of the enhanced bottom Yukawa coupling can be to significantly suppress the final baryon asymmetry n_B/s when the masses of the RH top and bottom squarks are nearly degenerate, or even lead to a sign change in the baryon asymmetry for $m_{\tilde{b}_R} < m_{\tilde{t}_R}$. For sufficiently large Y_τ and light tau sleptons, a significant n_L (and, thus, n_B/s) asymmetry can nevertheless be generated, as an initial Higgs–Higgsino asymmetry is transferred into the LH tau lepton sector through the tau Yukawa reactions [113, 114]. These dynamics are illustrated in figure 6, where one sees the vanishing of the baryon asymmetry for degenerate RH tops (\tilde{t}_1) and sbottoms (\tilde{b}_1).

3.2. CP-violating sources

As the foregoing discussion makes clear, analyzing the detailed nature of the particle number changing interactions and their parameter dependence is essential for predicting the baryon asymmetry, even if the CPV sources have maximal strength. At the same time, deriving reliable

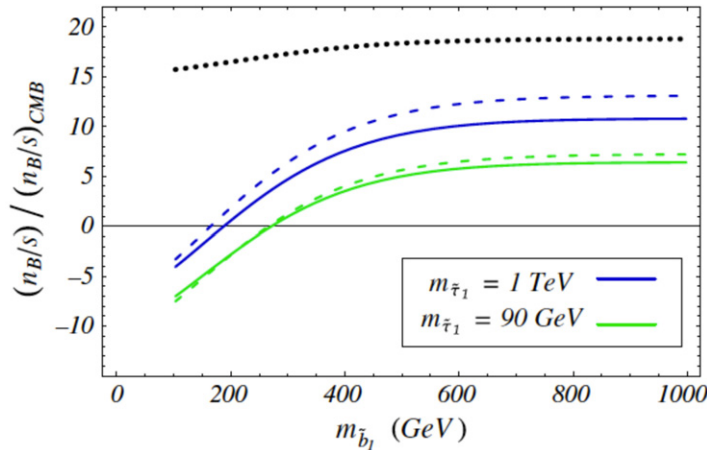


Figure 6. Baryon asymmetry as a function of RH bottom squark mass in the MSSM, scaled to the value obtained from the cosmic microwave background [113]. The blue (green) curves correspond to the RH stau mass of 1 TeV (90 GeV), while the black dotted line is obtained neglecting the bottom and tau Yukawa couplings. Solid curves give results of full numerical solution to transport equations, while the dashed line corresponds to an analytic approximation. A RH stop mass of 200 GeV has been assumed. Reprinted with permission from Chung *et al* [113], copyright 2009 by the American Physical Society.

CPV sources remains an on-going theoretical challenge that is part of a broader quest for a systematic treatment of the EWBG transport dynamics.

The earliest papers derived S^{CPV} using computations of quantum mechanical reflection and transmission from a barrier (the bubble wall). The idea was originally applied to the generation of a lepton number asymmetry during the EWPT by Cohen *et al* [116, 117] and subsequently applied directly to the baryon sector [118–124]. The resulting baryon asymmetry within the SM, computed using this approach, was generally considered to be too small to account for the observed value [23, 24], so attention turned to scenarios involving physics beyond the Standard Model (BSM). A significant advance appeared in the incorporation of diffusion [112], with the resulting framework remaining the state-of-the-art for the better part of a decade when applied to BSM models (see, e.g. [83–85, 125–129]).

It was subsequently realized that the essentially Markovian nature of this framework omitted potentially important ‘memory effects’ that could lead to further enhancements of n_L [130–132]. Using the VEV insertion approximation depicted in figure 7, where the Higgs VEV-dependent off-diagonal entries of the mass matrix are treated as perturbative interactions, [132] computed S^{CPV} in the MSSM for Higgsino and top squark transport near the bubble wall. As shown in the figure, the inputs for these sources involve two distinct particle species, either the Higgsinos and electroweak gauginos in the fermionic source case or the LH- and RH top squarks in the scalar case. When the masses of the two species become nearly degenerate, the source S^{CPV} becomes resonantly enhanced. The presence of this feature is phenomenologically important, as an enhanced source will generate a particle asymmetry more effectively for a given CPV phase. Given the stringent limits on CPV phases implied by the non-observation of the electric dipole moments (EDMs) (see below), the resonant source

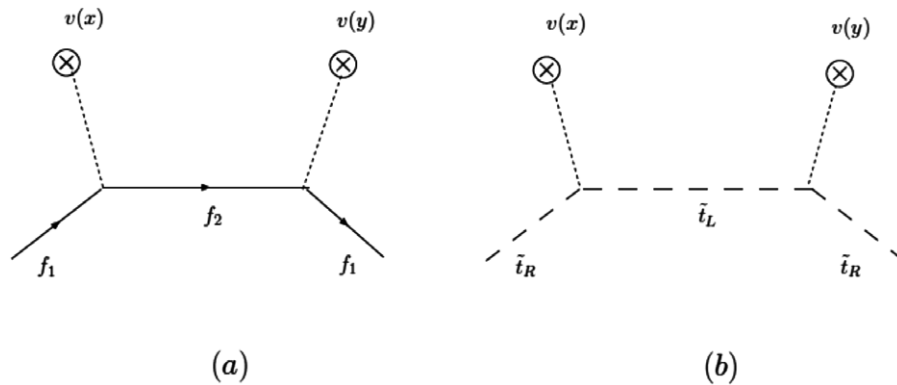


Figure 7. Contributions to CPV sources in the VEV-insertion approximation [133]. Here, $v(x)$ denotes appropriate combination of scalar background fields (VEVs) at spacetime position x^μ interacting with (a) fermions $f_{1,2}$ (b) scalar to quarks $\tilde{t}_{L,R}$. Reprinted with permission from Lee *et al* [133], copyright 2005 by the American Physical Society.

enhancement is essential for viable EWBG in many instances. The same resonant enhancement was also found to apply to the CP-conserving parts of figure 7, which increases the relaxation rate of the non-vanishing densities sourced by the CPV parts, reducing the strength of the resonant enhancement of the baryon asymmetry but not completely mitigating it [133].

A rigorous treatment of the spacetime evolution of particle densities that incorporates the memory effects is properly made using the Schwinger–Keldysh closed time path (CTP) formulation of non-equilibrium quantum field theory [134–137] (for a pedagogical discussion in the context of EWBG, see [133]). In contrast to the ‘in–out’ matrix elements relevant to scattering processes, analysis of the spacetime evolution of densities in the plasma requires study of the ‘in–in’ matrix elements, appropriately averaged over a thermal ensemble. The corresponding evolution involves four Green functions

$$\tilde{G}(x, y) = \begin{pmatrix} G^t(x, y) & -G^<(x, y) \\ G^>(x, y) & -G^{\bar{t}}(x, y) \end{pmatrix}, \quad (38)$$

where for a complex scalar field $\phi(x)$

$$G^>(x, y) = \langle \phi(x)\phi^\dagger(y) \rangle_T, \quad (39)$$

$$G^<(x, y) = \langle \phi^\dagger(y)\phi(x) \rangle_T, \quad (40)$$

while $G^t(x, y) = \theta(x_0 - y_0)G^>(x, y) + \theta(y_0 - x_0)G^<(x, y)$ and $G^{\bar{t}}(x, y) = \theta(x_0 - y_0)G^<(x, y) + \theta(y_0 - x_0)G^>(x, y)$. Here, the subscript T indicates an appropriate ensemble average. The fully interacting Green functions $\tilde{G}(x, y)$ satisfy a pair of Schwinger–Dyson equations

$$\tilde{G}(x, y) = \tilde{G}(x, y)_0 + \int d^4z \tilde{G}(x, z)_0 \tilde{\Pi}(z, y) \tilde{G}(y, z), \quad (41)$$

$$\tilde{G}(x, y) = \tilde{G}(x, y)_0 + \int d^4z \tilde{G}(x, z) \tilde{\Pi}(z, y) \tilde{G}(y, z)_0, \quad (42)$$

where the ‘0’ subscript indicates the free Green function and $\tilde{\Pi}$ is a matrix of self-energy functions corresponding to equation (38). Acting with the free equation of motion operator (e.g., $\partial_x^2 + m^2$ for a scalar field) on equations (41), (42), taking the difference of the two resulting equations, and considering the ‘<’ component in the limit $x \rightarrow y$ yields the transport equation

$$\partial_\mu j^\mu(X) = \int d^3z \int_{-\infty}^{X_0} [\Pi^>(X, z)G^<(z, X) - G^>(X, z)\Pi^<(z, X) + G^<(X, z)\Pi^>(z, X) - \Pi^<(X, z)G^>(z, X)], \quad (43)$$

where the effect of all interactions are contained in the convolution of the Green functions and self-energies on the right-hand side. In the VEV insertion approximation, CPV and CP-conserving interactions of the scalar field ϕ with spacetime-varying Higgs background field (the bubble wall) are contained the self-energies. Particle number changing interactions, as well as those associated with scattering and creation/annihilation, also live in the $\tilde{\Pi}$. Note that the source for the divergence of the particle number current contains an integral over the history of the system, leading to the presence of memory effects as emphasized in [132].

Subsequent work has attempted to refine this formulation, particularly within the MSSM. The authors of [138, 139] endeavored to go beyond the VEV insertion approximation by noting that, when resummed to all orders in the VEVs, the interactions of figure 7 lead to spacetime-dependent mass matrices for the supersymmetric particles. In the case of stops, for example, the corresponding term in the Lagrangian is

$$\mathcal{L}_i^{\text{mass}} = (\tilde{t}_L^* \quad \tilde{t}_R^*) \begin{pmatrix} M_{LL}^2(x) & M_{LR}^2(x) \\ M_{LR}^2(x)^* & M_{RR}^2(x) \end{pmatrix} \begin{pmatrix} \tilde{t}_L \\ \tilde{t}_R \end{pmatrix}, \quad (44)$$

where

$$M_{LL}(x) = M_Q^2 + m_t^2(x) + \Delta_t(x), \quad (45)$$

$$M_{RR}(x) = M_T^2 + m_t^2(x) + \Delta_t(x), \quad (46)$$

$$M_{LR}^2(x) = y_t v(x) [A_t \sin \beta(x) - \mu \cos \beta(x)]. \quad (47)$$

Here, M_Q and M_T are, respectively, the spacetime-independent third generation LH- and RH stop mass parameters; $m_t(x) = y_t v(x)/\sqrt{2}$ is the spacetime dependent top mass, with top Yukawa coupling y_t and spacetime-dependent VEV $v(x) = \sqrt{v_u^2(x) + v_d^2(x)}$; $\Delta_t(x)$ a function of $\beta(x) = \tan^{-1}[v_u(x)/v_d(x)]$, $v(x)$, and the weak mixing angle; and where μ and $y_t A_t$ are supersymmetric Higgs mass and stop triscalar couplings, respectively. Note that in general $\text{Arg}(\mu A_t) \neq 0$, so that the off-diagonal entry $M_{LR}^2(x)$ effectively contains a spacetime-dependent CPV phase. At each point in spacetime, then, the propagating degrees of freedom—the mass eigenstates \tilde{t}_j ($j = 1, 2$)—are related to the weak interaction eigenstates \tilde{t}_a ($a = L, R$) by a unitary transformation $U(x)$

$$\tilde{t}_j = U(x)_{ja}^\dagger \tilde{t}_a. \quad (48)$$

The authors of [138, 139] computed the current densities for the \tilde{t}_a ($a = L, R$) by expanding the mass-squared matrix $M_{ab}^2(x)$ in equation (44) about a given point z^μ by a radius r , diagonalizing $M_{ab}^2(z)$ using equation (48), solving for the locally free Green functions

$\tilde{G}^0(z - r/2, z + r/2)$, and treating the first-order term in the expansion of the mass-squared matrix,

$$r^\lambda \frac{\partial M^2}{\partial x^\lambda}, \quad (49)$$

as an interaction in the CTP Schwinger–Dyson equations, equations (41) and (42). The resulting solution for the LH stop current $j_{\tilde{t}_L}^\lambda$ then drives the creation of non-vanishing baryon number via the EW sphalerons, as per equations (34), (29). Similar methods were applied to determine the chargino current $j_{\tilde{\chi}^\pm}^\lambda$.

The effect of including the fully re-summed VEVs and the first-order interaction of equation (49) is to reduce the strength of the resonance. As an illustration for the chargino sources with $M_2 = 200$ GeV, $M_A = 150$ GeV, and $\text{Arg}(\mu A_t) = \pi/2$, one finds that for $|\mu| \approx M_2$ the baryon asymmetry Y_B is enhanced by about a factor of seven relative to its off-resonance magnitude at $|\mu| = 100$ GeV. This result represents about a factor of two reduction in Y_B compared to the result obtained using the VEV insertion approximation in [83], and is considerably smaller still than obtained in [132, 133]. Nonetheless, it suggests that obtaining the observed value of Y_B in the MSSM *via* chargino and neutralino sources would be viable even when a VEV resummation is performed. Two estimates of the baryon asymmetry generated by this mechanism in the MSSM are shown in figure 8.

Parallel efforts on the resummation problem were carried out in [141–143], adopting the framework of the Kadanoff–Baym equations [144] that are deduced from the Schwinger–Dyson equations. (For a related effort using the Bogoliubov approach, see [145]). Applying this analysis to the MSSM and performing a two-flavor analysis with approximate treatment of the off-diagonal densities the authors of [146, 147] concluded that a proper treatment of flavor oscillations as well as a VEV resummation vastly suppresses Y_B in the MSSM, rendering it unviable in light of current EDM limits on the CPV phases.

To explain the arguments behind these conclusions, the subsequent response by the authors of [148, 149], and the parallel work by the authors of [150–154], we present here a specific example involving scalar particles, which avoids the complications associated with spin. Our example consists of a two-flavor scalar field theory. In the presence of a spacetime-dependent mass-squared matrix, performing the flavor rotation of equation (48) leads to the Lagrangian in terms of local mass eigenstates $\Phi = (\phi_1, \phi_2)$

$$\mathcal{L}_{\text{scalar}} = \partial_\mu \Phi^\dagger \partial^\mu \Phi - \Phi^\dagger \hat{M}^2(x) \Phi - \Phi^\dagger \Sigma^\mu \partial_\mu \Phi + (\partial_\mu \Phi^\dagger) \Sigma^\mu \Phi + \Phi^\dagger \Sigma^\mu \Sigma_\mu \Phi + \mathcal{L}_{\text{int}}, \quad (50)$$

where $\hat{M}^2(x) = \text{diag}[m_1^2(x), m_2^2(x)]$,

$$\Sigma^\mu = U^\dagger(x) \partial^\mu U(x), \quad (51)$$

and \mathcal{L}_{int} contains interactions of Φ with other particles in the plasma that lead to chemical and kinetic equilibrium as well as diffusion ahead of the bubble wall.

The effects of CP-violation are encoded in Σ^μ that contains, in particular, a spacetime derivative of the effective CPV phase associated with the off-diagonal elements of the undiagonalized matrix $M^2(x)_{ab}$. Applying the equation of motion associated with all terms in equation (50) except \mathcal{L}_{int} to the Schwinger–Dyson equations for the \tilde{G} leads to

$$[\partial_x^2 + \hat{M}^2(x) + 2\Sigma_\mu \partial_x^\mu + \Sigma^2 + (\partial \cdot \Sigma)] G^<(x, y) = -i \int d^4 z [\tilde{\Pi}(x, z) \tilde{G}(z, y)]^<, \quad (52)$$

with a similar equation holding for the operators acting on the y -coordinate. Taking the sum and difference of these two equations yields the constraint and kinetic equations, respectively.

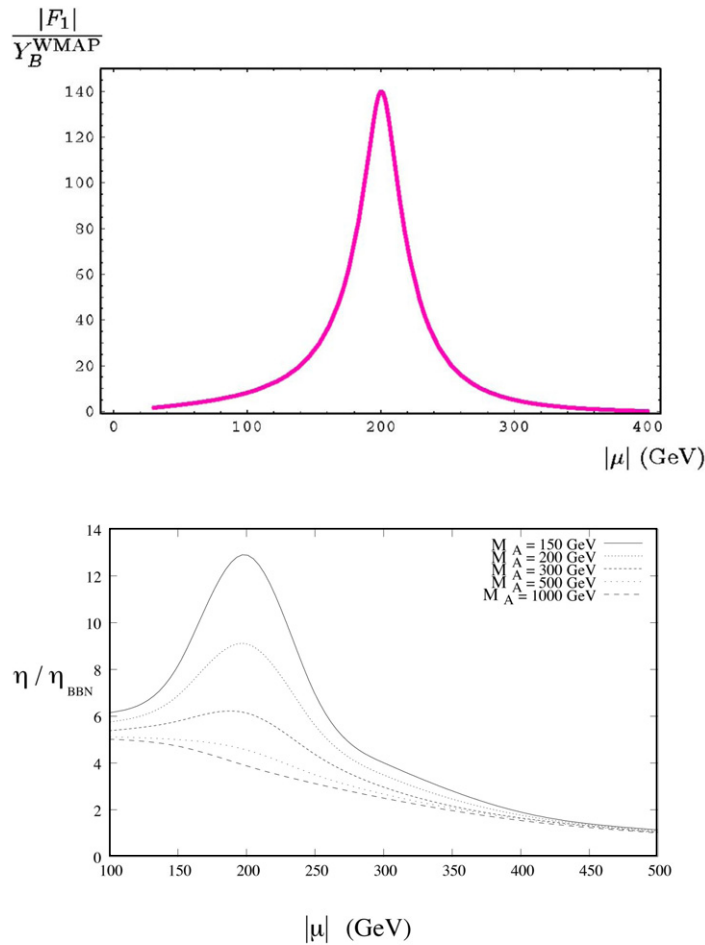


Figure 8. Baryon asymmetry in the MSSM. Top panel: computed using VEV-insertion approximation and relaxation terms while including contributions from both charged and neutral Higgsinos and electroweak gauginos [133]. Bottom panel: including only charged Higgsino and wino contributions but following the VEV resummation approach of [138, 139], from [140]. Top panel reprinted with permission from Lee *et al* [133], copyright 2005 by the American Physical Society. Bottom panel reprinted with permission from Balazs *et al* [140], copyright 2005 by the American Physical Society.

The former determines the dispersion relations for the propagating degrees of freedom, while the latter governs their dynamics. Extensive reviews of the related formalism can be found in [155, 156].

For the sake of the present discussion, we concentrate only on the kinetic equation. In doing so, it is convenient to consider the kinetic equation for the Wigner transform of the $G^<(x, y)$:

$$G^<(k, X) = \int d^4r e^{ik \cdot r} G^<(x, y) \quad (53)$$

with $r = x - y$ and $X = (x + y)/2$. The kinetic equation is

$$2k \cdot \partial_X G^<(k, X) = e^{-i\phi} \{-i[\hat{M}^2(X) - 2ik \cdot \Sigma(X) + \Sigma^2(X), G^<(k, X)] + \mathcal{C}(k, X)\}, \quad (54)$$

where $\mathcal{C}(k, X)$ denotes the so-called ‘collision term’ involving products of the G and Π Wigner transforms and the ‘diamond operator’ is defined by

$$\diamond(AB) = \frac{1}{2} \left(\frac{\partial A}{\partial X^\mu} \frac{\partial B}{\partial k_\mu} - \frac{\partial B}{\partial X^\mu} \frac{\partial A}{\partial k_\mu} \right). \quad (55)$$

Note that equation (54) and its partner constraint equation represent a set of coupled integral-differential equations in the space of Green functions for the local mass eigenstates. For simplicity we have suppressed the corresponding indices that would appear, for example, in the term

$$[-2ik \cdot \Sigma(X), G^<(k, X)]_{ij} = -2ik_\mu [\Sigma^\mu(X)_{i\ell} G^<(k, X)_{\ell j} - G^<(k, X)_{i\ell} \Sigma^\mu(X)_{\ell j}]. \quad (56)$$

The different terms in equation (54) embody various key physical dynamics that govern the creation of a net particle density ahead of the bubble wall: (a) the $[\hat{M}^2, G^<]$ term gives rise to flavor oscillations, much in analogy with those observed or neutrino oscillations; (b) the commutators involving the field Σ^μ contain the effects of the spacetime-dependent CPV phases that are essential for the generation of a non-vanishing number density; (c) the collision term \mathcal{C} includes the effects of scattering and particle creation/annihilation that gives rise to diffusion ahead of the bubble wall and thermalization within the plasma, thermal corrections to the masses and widths of the propagating degrees of freedom, and the particle number changing reactions discussed above. Note that equation (54) is exact to all orders in the spacetime-varying Higgs VEVs, is implied by the X^μ -dependence of the mass-squared matrix, the field Σ^μ , and \mathcal{C} . The X^μ -dependence of $\hat{M}^2(X)$ also gives rise to the ‘semi-classical force’ term that was first derived in this context for fermionic systems in [141] and that generates a CPV source term even for a single flavor situation.

Obtaining exact solutions of the kinetic and constraint equations is a daunting task. Recent progress has been achieved in obtaining approximate solutions by expanding the various terms in powers of different scale ratios ϵ_j appropriate to the plasma dynamics (see [133, 148, 149] for a discussion). The scales include (a) the typical quasiparticle frequency ω_{int} or deBroglie wavelength L_{int} that is intrinsic to its free propagation. Both scales are set by the plasma temperature (assuming local thermalization): $\omega_{\text{int}} \sim L_{\text{int}}^{-1} \sim T$. (b) The wall thickness L_w or the time scale τ_w over which the particle masses vary appreciably at a local point in space as the bubble expands; (c) the typical frequency of flavor oscillations, ω_{osc} given by the difference of the local eigenfrequencies $|\omega_1 - \omega_2|$ or the associated time and length scales, $\tau_{\text{osc}} \sim L_{\text{osc}}/c \sim \omega_{\text{osc}}^{-1}$; the length or time scales associated with the collisional interactions, $\tau_{\text{col}} \sim L_{\text{col}}/c$. The latter set the rates for diffusion, kinetic and chemical equilibration, and thermal damping (widths) of the quasiparticles; and (d) the chemical potentials associated with various particle species μ_j . Typically one finds the following ratios of scales to be significantly less than one:

$$\epsilon_w = \frac{L_{\text{int}}}{L_w}, \quad \epsilon_{\text{col}} = \frac{L_{\text{int}}}{L_{\text{col}}}, \quad \epsilon_\mu = \frac{\mu}{T}. \quad (57)$$

The parameter ϵ_w is particularly important for electroweak baryogenesis, as it must be non-zero in order for the coupled set of kinetic equations to generate a non-vanishing particle density. Since typically one finds $L_w \sim \mathcal{O}(20/T)$, implying that $\epsilon_w \lesssim 0.5$.

In this regime, an expansion in powers of ϵ_w —sometimes referred to as the ‘gradient expansion’—is justified, and most recent work has focused on solutions obtained to first-order in this small parameter⁶. In general, one also finds that $\epsilon_{\text{col}} \ll 1$ and $\epsilon_\mu \ll 1$, leading to well-defined approximations by expanding in these quantities. In contrast, the ratio of ‘intrinsic’ and oscillation length scales, $\epsilon_{\text{osc}} = L_{\text{int}}/L_{\text{osc}}$ depends strongly on the input parameters of the underlying Lagrangian. In the case of resonant baryogenesis, ω_{osc} is relatively small, and one finds that the resonant enhancement occurs when the corresponding length scale $L_{\text{osc}} \sim L_w \gg L_{\text{int}}$. In this case, one may also expand in ϵ_{osc} (though some terms must be resummed to all orders in ω_{osc} in order to maintain consistency with the continuity equation).

The work of [146, 147] yielded the first solutions of the kinetic equations for the MSSM under these approximations that take into account the interplay of both the fully resummed spacetime-varying VEVs with the off-diagonal densities. Applying the power counting in ϵ_w indicated above, they argued that the off-diagonal contributions to the RHS of equation (56) for the diagonal densities $G^<(k, X)_{ii}$ arise beyond leading non-trivial order, allowing one to neglect their effect as CPV sources for the diagonal terms. The corresponding numerical results then indicated that the value of Y_B in the resonant regime is substantially smaller than obtained in earlier work. Given the limits on CPV phases from EDM searches (see below), one would then conclude that EWB in the MSSM cannot yield the observed baryon asymmetry, contrary to the implications of earlier work.

Recently, however, the authors of [149] pointed out, using a simpler schematic two-flavor scalar field theory, that the approximations used in [146, 147] do not consistently implement the power counting in the ϵ_w . In particular, the solution to equation (54) involves an integral of the terms in equation (56) over a distance scale of order L_w . Although the fields Σ^μ are nominally $\mathcal{O}(\epsilon_w)$, this integral compensates for this nominal $1/L_w$ suppression. Thus, all contributions from the commutator in equation (56), including those involving off-diagonal terms $k \cdot \Sigma_{12} G_{21}^< - G_{12}^< k \cdot \Sigma_{21}$ that contribute to the evolution of the diagonal Green functions $G_{11}^<$ must be kept to leading non-trivial order in the ϵ_j . Dropping these off-diagonal contributions, as in [146, 147], removes the dominant CPV source for the diagonal Green functions that characterize the diffusion of particle number ahead of the advancing wall and leads to the suppressed asymmetry as obtained in that work. On the other hand, the consistent solution that retains these terms displays the substantial resonant enhancement that was noted in earlier works obtained with the VEV-insertion approximation.

It is important to emphasize that the most recent work on this problem has been completed using schematic two-flavor scalar field models, and not the MSSM for which CPV dynamics involving fermion fields (Higgsinos and gauginos) is the most viable mechanism for successful baryogenesis in this scenario. In addition, the authors of [153]—building on earlier work [150–152] and concentrating on the time-dependent, spatially homogeneous background field problem—have argued that contributions from so-called ‘fast modes’ or ‘coherence shells’ may have a significant impact on the magnitude of the particle asymmetries. In contrast to solutions of the constraint equations that satisfy particle-like dispersion relations (quasiparticle modes), the coherence shells correspond to regions of vanishing space or time components of the momentum and generate singular contributions to the spectral densities. A consistent treatment of these modes, which can mix with the quasiparticle modes, appears to require a resummation to all orders in ϵ_w . The implications for the full spacetime-dependent problem

⁶ This validity of the gradient or ϵ_w expansion corresponds to the ‘thick wall’ regime in earlier work.

remain to be analyzed. On the other hand, the progress achieved in [148, 149] represents a significant advance, not only for the implementation of a consistent power counting, but also for the full inclusion of the collision term $\mathcal{C}(k, X)$ that governs the evolution of kinetic equilibrium ahead of the advancing wall. Previous work had largely implemented equilibrium as an *ansatz*, rather than obtaining it as a direct solution of the dynamics.

Significant formal and phenomenological work remains to be completed. A full application to the dynamics of fermions—including resolution of questions involving the ‘semi-classical force’ term, the coherence shells, and off-diagonal densities—as well as a more realistic set of thermalizing interactions in the collision term are among the open theoretical problems. Phenomenological application to realistic scenarios like the MSSM that involve a more extensive set of coupled integral-differential equations, including both the network of particle number changing reactions as in [113, 115, 157] as well as the consistent treatment of flavor oscillations and spacetime-varying background fields in the presence of the thermalizing interactions in the plasma, will entail significant effort. Nonetheless, given the recent theoretical progress and indications that resonant EWB remains a viable mechanism, this investment of effort is likely to have a significant impact on the field.

4. Testing electroweak baryogenesis

EWBG requires new particles and interactions to obtain a strongly first-order EWPT and to provide sufficient CP-violation. These new particles cannot be much heavier than the electroweak scale, and they must couple significantly to the Higgs field. Together, these properties imply that such new particles will lead to observable effects in upcoming high-energy and high-precision experiments.

The prospect for observing new particles directly at the LHC and indirectly through high-sensitivity, low-energy studies of CPV observables imply that EWBG is a generally testable and, therefore, falsifiable, baryogenesis scenario. In this respect, it contrasts with other scenarios that typically involve higher scales, such as standard thermal leptogenesis or Affleck–Dine baryogenesis. In what follows, we summarize some of the primary experimental tests of EWBG, focusing largely but not exclusively on the MSSM as an illustration. We consider tests that may be performed for each of the three frontiers in particle physics: the high-energy frontier, the intensity frontier and the cosmological frontier.

4.1. The intensity frontier: CP-violation and electroweak baryogenesis

In general, the most powerful probes of BSM CP-violation that are relevant for EWBG are searches for the permanent EDMs of the electron, neutron and neutral atoms. In all cases, only null results have been attained to date, implying stringent constraints on new sources of CP-violation. Limits also exist on the muon EDM, though it is considerably less constraining than the electron EDM limit, even after accounting for the m_e/m_μ suppression of the former with respect to the latter. At the most basic level, one expects the one-loop EDM of an elementary fermion f generated by new field(s) of mass M to go as

$$d_f \sim e \left(\frac{m_f}{M^2} \right) \frac{\alpha_k}{4\pi} \sin \phi, \quad (58)$$

where α_k is either the fine structure constant or strong coupling (evaluated at the scale M) and ϕ is a CPV phase associated with the new interactions. For $\alpha_k = \alpha_{\text{em}}$ equation (58) gives

$$d_f \sim \sin \phi \left(\frac{m_f}{\text{MeV}} \right) \left(\frac{1 \text{ TeV}}{M} \right)^2 \times 10^{-26} e \text{ cm}. \quad (59)$$

The present limit on the EDM of the electron, $|d_e| < 10.5 \times 10^{-28} e \text{ cm}$ [158] obtained from an experiment on the Yb-F molecule, then implies that

$$|\sin \phi| \lesssim (M/2 \text{ TeV})^2. \quad (60)$$

Similar constraints follow from the limits on the neutron [159] and ^{199}Hg atomic [160] EDMs:

$$|d_n| < 2.9 \times 10^{-26} e \text{ cm}, \quad (61)$$

$$|d_A(^{199}\text{Hg})| < 3.1 \times 10^{-29} e \text{ cm}, \quad (62)$$

assuming that any contributions from the QCD θ -term interaction are sufficiently small that no cancellations between this source of SM CP-violation and that arising from new interactions occurs. Contributions from CP-violation associated with the SM CKM matrix first arise at three (four) loop order for d_n and d_A (d_e), implying effects at well-below the $10^{-30} e \text{ cm}$ level. The next generation of lepton, neutron and neutral atom EDM searches aim to improve the level of sensitivity by up to two orders of magnitude in the short term, while efforts to reach even greater sensitivity with storage ring hadronic EDM searches are underway (for a recent summary of present plans, see e.g., [161]).

The constraints implied in equation (60) generically render EWBG unviable. For the new particles to be sufficiently abundant in the electroweak plasma at $T \sim 100 \text{ GeV}$, their masses should be lighter than $\sim 500 \text{ GeV}$, implying $|\sin \phi| \lesssim 0.01$. In this case, the CPV sources in the transport equations discussed in section 3 are suppressed and EWBG becomes untenable as a result (cf figures 6, 8). There exist, however, several paths to evading the one-loop EDM constraints. In the MSSM, the one-loop EDMs contain one scalar (e.g. squark or slepton) and one fermionic superpartner (gaugino or Higgsino). By making one or the other species sufficiently heavy, the one-loop EDMs can be evaded, thereby relaxing the constraints of equation (60) on the CPV phase. At the same time, the other superpartner species may remain relatively light, enabling its interactions to generate the CPV sources for electroweak transport dynamics. Large differences in the scalar and fermion mass spectra have been motivated on other grounds recently, as in the case of ‘split SUSY’ models [162, 163] that contain heavy first and second generation sfermions but relatively light Higgsinos and electroweak gauginos. The present generic LHC lower bounds on the masses of the gluinos and first and second generation squarks is at least consistent with this scenario.

From the standpoint of CPV for EWBG, one must still consider EDMs generated at two-loop level, as in the ‘Barr–Zee’ graphs of figure 9. Recently, the full set of such diagrams were computed by the authors of [164] and the corresponding implications for MSSM baryogenesis delineated in [165, 166]. Even with the two-loop suppression and the most optimistic CPV sources computed using the VEV-insertion approximation, only one CPV phase in the gaugino–Higgsino sector remains sufficiently unconstrained as to remain a potentially viable driver of MSSM EWBG: the relative phase of the bino soft mass parameter M_1 , the soft parameter b and the supersymmetric Higgs mass parameter μ : $\phi_1 = \text{Arg}(M_1 \mu b^*)$. Since ϕ_1 is associated with the presence of the bino degrees of freedom, it only enters the two-loop graphs

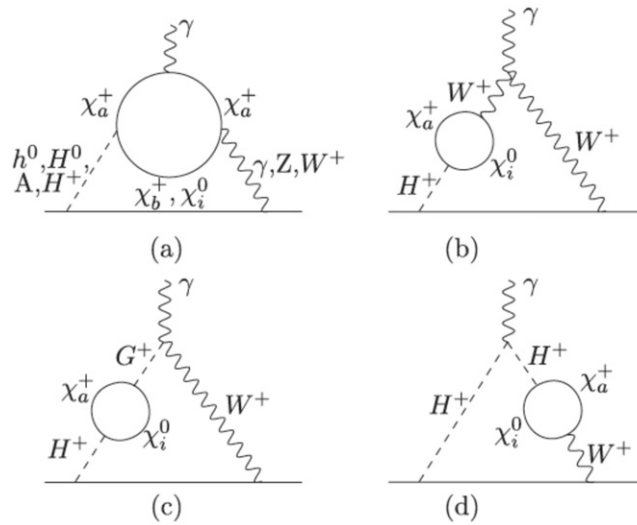


Figure 9. Two loop EDMs in the MSSM (see [164] and references therein). Reprinted with permission from Li *et al* [164], copyright 2008 by the American Physical Society.

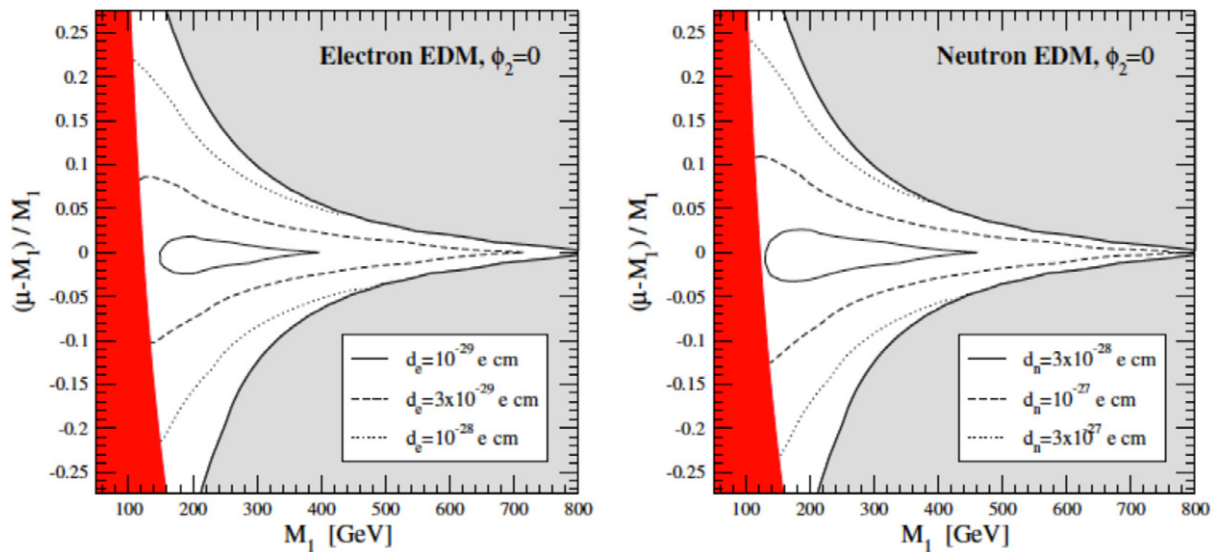


Figure 10. Curves of constant d_e and d_n for MSSM EWBG in the limit of heavy sfermions [166]. For each curve, ϕ_1 is set to the value giving the correct baryon asymmetry. Reprinted from Cirigliano *et al* [166], copyright 2010 with permission from JHEP.

involving the χ_k^0 and the exchange of a (W^\pm, H^\mp) pair, representing a small sub-class of the full two-loop diagrams. During the EWPT, the relevant CPV sources would be those involving the Higgsino–bino processes in figure 7, corresponding to ‘neutralino-driven’ EWBG. A summary of the relation between baryon asymmetry and EDMs of the electron and neutron are given in figure 10 in the region of resonant electroweak gaugino–Higgsino EWBG. As indicated by the

innermost contours, to conclusively test or rule out MSSM EWBG would require improvements in the sensitivity of EDM searches by roughly two orders of magnitude, roughly consistent with the goals of the next generation of experiments.

Recently, the authors of [167] carried out an analysis of the viability of stop, sbottom and stau sources, whose effects depend on the CPV phase in the corresponding soft trilinear couplings. The corresponding contributions to the EDM also arise at two-loop order and are in principle suppressed. However, present constraints from the ^{199}Hg EDMs rule out the viability of stop- or sbottom-driven EWBG. Future improvements in neutron and/or electron EDM searches could conclusively test the viability of stau-driven EWBG in the MSSM.

Going beyond the MSSM, it is possible to introduce new CPV interactions in the scalar sector that could evade present EDM constraints but still generate the CPV sources as needed for EWBG [168–170]. The authors of [168] studied the CPV sources in the NMSSM and found that the presence of the additional gauge singlet superfield gives rise to a new CPV source that is second-order in the ϵ_w expansion—associated with a ‘semi-classical force’ term in kinetic theory—and that may contribute strongly away from the resonant regime. This source depends on the same CPV phases as in the MSSM, so one must contend with constraints from EDM searches. At the time this work was completed, a minimum first and second generation sfermion mass of 1 TeV was sufficient to evade the existing $d_{e,n}$ bounds. More recently, the authors of [170] observed that a new phase associated with the gauge-singlet extension of the MSSM could successfully drive EWBG through both top and stop sources as well as Higgsino–bino interactions (for a related study, see [171]). The dominant constraints on this phase are associated with two-loop contributions to the down quark ‘chromo-electric dipole moment’ as it might generate a ^{199}Hg atomic EDM. Nonetheless, NMSSM EWB remains viable even with these stringent constraints. An earlier and more extensive $U(1)'$ extension was studied by the authors of [95], who found a sufficiently large baryon asymmetry could be generated from CPV sources associated with spontaneous CPV during the EWPT and whose CPV effects relaxed to sufficiently small values in the broken phase so as to evade the EDM bounds.

In all of the foregoing scenarios, the CPV interactions are flavor diagonal. Recently, some attention has focused on the possibility that flavor non-diagonal CPV might provide the source for EWBG while evading the one-loop EDM bounds [97, 172, 173]. As with SM CKM CPV, flavor non-diagonal CPV interactions that involve the second and third generation quarks would not contribute to EDMs until at least two-loop order. On the other hand, the associated CPV effects could appear in the B - and/or D -meson system, allowing for a potential probe of this possibility. To illustrate, we consider the schematic 2DHM of [173], applied to the second and third generation fermions as needed for CPV in the $b \rightarrow s$ transitions. The corresponding interaction is

$$\mathcal{L} = \lambda_{ij}^u \bar{Q}^i (\epsilon H_d^\dagger) u_R^j - \lambda_{ij}^d \bar{Q}^i H_d d_R^j - y_{ij}^u \bar{Q}^i H_u u_R^j + y_{ij}^d \bar{Q}^i (\epsilon H_u^\dagger) d_R^j + \text{h.c.}, \quad (63)$$

where (i, j) run over the second and third generations. For purposes of illustration, one may make several simplifying assumptions, including taking $\tan \beta = 1$ at $T = 0$ and setting $y_{sb} = \lambda_{sb} = 0$ and retaining the one CPV phase that remains in the limit of vanishing y_{ss} and λ_{ss} (after field redefinitions): $\theta_{\lambda_{bs}} = \text{Arg}(\lambda_{bs})$. In the VEV-insertion approximation the CPV sources are proportional to $|\lambda_{bs}|^2 \sin \theta_{\lambda_{bs}}$. On the other hand, CPV in the B_s system arises from tree-level

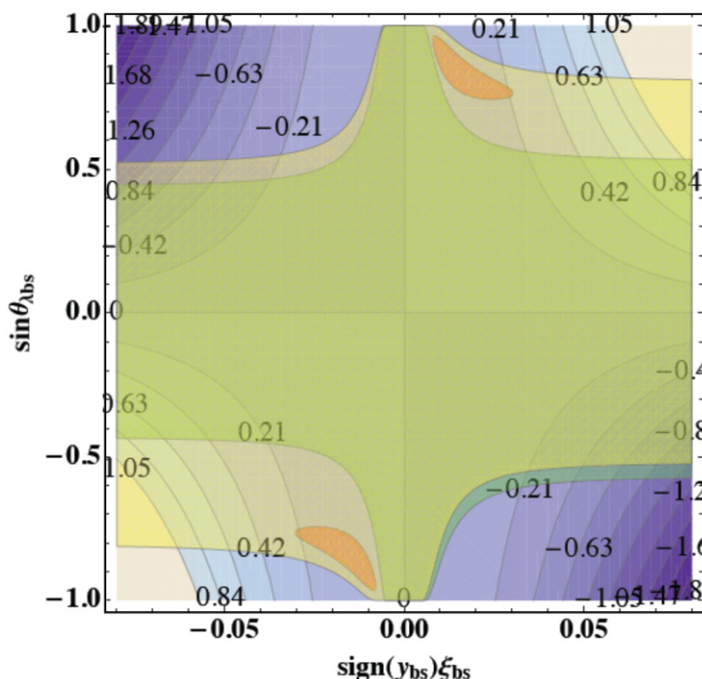


Figure 11. Contours of constant baryon asymmetry in the ‘electroweak beautygenesis’ scenario of [173]. Reprinted with permission from Liu *et al* [173], copyright 2012 by the American Physical Society.

exchange of the Higgs field $H_{bs} = -\cos \beta H_u + \sin \beta H_d^\dagger$, leading to the mixing operator

$$\frac{\zeta_{bs}^2}{\Lambda_{bs}^2} (\bar{b}_L s_R) (\bar{b}_L s_R), \quad \text{with } \Lambda_{bs} \sim m_{H_{bs}}^2 / v$$

with $\Lambda_{bs} \sim m_{H_{bs}}^2 / v$ and $\zeta_{bs} \propto |\lambda_{bs}| (1 \pm \exp(i\theta_{\lambda_{bs}}))$ depending on the signs of the y_{ij} .

The resulting curves of constant baryon asymmetry, shown in the $(\sin \theta_{\lambda_{bs}}, \lambda_{bs} / \sqrt{2})$ plane are given in figure 11, along with constraints from the Tevatron and LHCb experiments. Note that in this restricted, schematic model, non-negligible contributions to the baryon asymmetry can occur. Future improvements in the sensitivity of LHCb studies could either uncover CPV in a region consistent with a significant contribution to the asymmetry or place stringent constraints on this possibility. On the other hand, EDM searches are relatively insensitive to the CPV phase $\theta_{\lambda_{bs}}$, as the operator in equation (64) contains no first generation quarks and involves only flavor non-diagonal combinations of the opposite chirality quarks. Clearly there exists considerable room for additional studies of flavor non-diagonal EWBG, including a more extensive study of the framework discussed here as well as those analyzed in [97, 172]. The extent to which this possibility could provide a viable EWBG alternative to flavor diagonal CPV in EWBG in light of increasingly stringent EDM limits remains to be seen.

4.2. The high energy frontier: CP-violation and phase transitions

New particles related to EWBG can potentially be created at observable rates at high-energy colliders such as the LHC. This is especially true of new colored states that help to strengthen

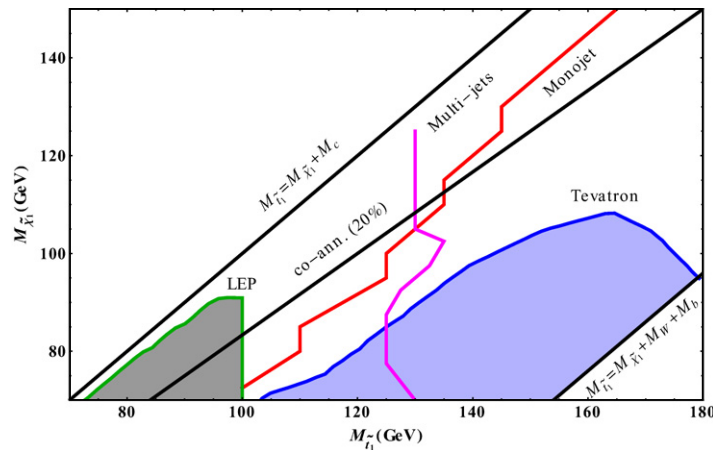


Figure 12. Tevatron and LHC limits on a light stop that decays to a charm quark and a neutralino LSP, $\tilde{t}_1 \rightarrow c \chi_1^0$. Reprinted from He *et al* [184], copyright 2012 with permission from JHEP.

the EWPT, such as a light stop in the MSSM or more generally a new X scalar as discussed in section 2. To have an adequate effect, these particles must be lighter than about $m_X \lesssim 200$ GeV implying very large LHC (and Tevatron) production cross sections. Even so, such states should be consistent with existing collider limits.

One way to hide a light colored scalar is to have it decay to dijets. This can arise from a $\tilde{X} q_i q_j$ coupling. Even though the dijets in this case would form an invariant-mass peak at the X mass, the backgrounds at the LHC (and the Tevatron) are so large that they swamp the signal in the low-mass region. Moreover, the cuts used in existing searches for single or paired dijet resonances at both the LHC and the Tevatron do not extend or have limited sensitivity to lighter masses $m_X \lesssim 200$ GeV [174–176]. Some sensitivity could be recovered with more generous cuts [177], or if the X decays involve heavy flavor [178].

A second way for a light colored state X to have escaped detection is for it to decay to a light quark and a long-lived neutral N fermion (that could be the DM). This is natural in the MSSM, where the light stop ($X = \tilde{t}_1$) can decay to a charm quark and the lightest neutralino ($N = \chi_1^0$). For small $X - N$ mass splittings, the decay products are very soft and difficult to detect using the standard searches for multiple jets and missing energy, and dedicated Tevatron searches only limit splittings above about 35 GeV [179, 180]. In figure 12 we illustrate the current limits on a light stop that decays via $\tilde{t}_1 \rightarrow c \chi_1^0$ based on data from the Tevatron and the LHC. Instead, some sensitivity can be recovered through monojet searches, requiring a single hard jet and missing energy [181–184], as can also be seen in figure 12, although a full test of the parameter space will be challenging [185]. A potential further probe may be provided by the decays of stoponium, a bound state consisting of a stop and its anti-particle [186–189].

The new physics required for EWBG must also couple significantly to the $SU(2)_L$ -doublet Higgs field, and this can potentially induce observable changes in the production and decay properties of the Higgs boson. An important effect arises from colored X scalars that couple to the Higgs as in equation (23). Such scalars will contribute in loops to the amplitudes for Higgs boson production through gluon fusion and Higgs decay to diphotons. Large positive values of the coupling $Q > 0$ are needed to induce a strongly first-order phase transition. In this case their contribution to gluon fusion interferes constructively with the dominant top quark loop in

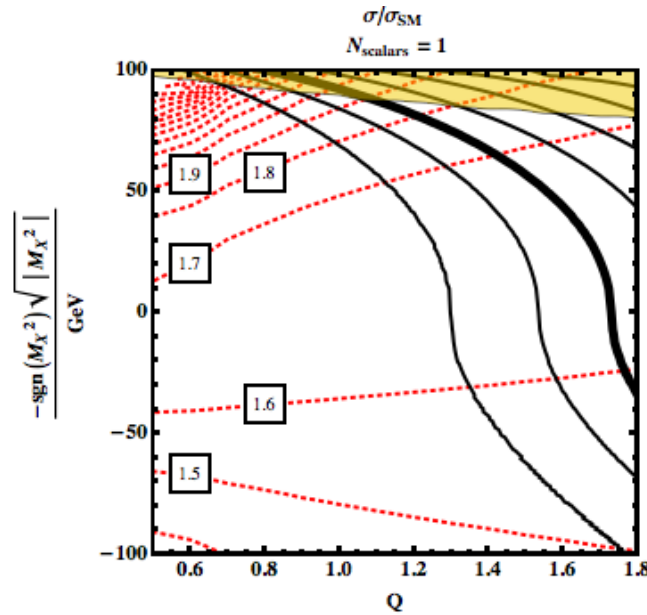


Figure 13. Rates of gluon fusion Higgs boson production relative to the SM (red dotted lines) and contours of ϕ_c/T_c (black solid lines) for one new color-triplet scalar for given values of the parameters $-\text{sgn}(M_X^2)\sqrt{|M_X^2|}$ and Q . The thick solid corresponds to $\phi_c/T_c = 0.9$ and the adjacent solid lines show steps of $\Delta(\phi_c/T_c) = 0.2$. Reprinted with permission from Cohen *et al* [79], copyright 2012 by the American Physical Society.

the SM, and destructively with the dominant W^\pm loop for diphoton decay. The net result is a significant enhancement in the rate of gluon fusion that is closely related to the strength of the EWPT, and a more modest decrease in the branching fraction to diphotons [79]. Similar results are found for the light stop of the MSSM [190].

In figure 13 we show the enhancement of the gluon fusion rate from X relative to the SM (red dotted lines) as a function of Q and the mass parameter M_X^2 , together with an estimate for where the phase transition is strong enough for EWBG (to the right of the thick black solid line). Gluon fusion is the dominant Higgs production mode at the LHC, and is the primary production channel for the $\gamma\gamma$, W^+W^- and Z^0Z^0 decay searches at the LHC. Indeed, the enhancement of the gluon fusion rate implied by this mechanism of strengthening the EWPT is already strongly constrained by (and in some tension with) current LHC and Tevatron Higgs searches [79, 191].

New uncolored X particles coupling to the Higgs boson as in equation (23) can also make the phase transition more strongly first-order, although their effect tends to be weaker than the colored case. If such a state has a non-trivial electric charge, it will modify the Higgs branching fraction to $h^0 \rightarrow \gamma\gamma$ [79, 99]. As in the coloured case, the interference with the W^\pm loop is destructive when the phase transition is made more strongly first-order. The net effect, therefore, is to decrease the Higgs branching to diphotons while leaving the gluon fusion rate largely unchanged. Uncolored X particles could also potentially be probed directly by their electroweak production channels, or their effects on the Higgs self-coupling [192].

The EWPT can also be made more strongly first-order if there are other fields that develop VEVs in the early Universe at about the same time as the Higgs. A simple example of this is the real singlet model presented in section 2 [92]. In this case, there will be an additional

fundamental scalar boson in the theory that will mix with the $SU(2)_L$ -doublet Higgs excitation. The resulting real scalar mass eigenstates will consist of a SM-like h_1 and a singlet-like h_2 . Decays of h_1 are frequently similar to the SM, but can be changed radically if $h_1 \rightarrow h_2 h_2$ is kinematically allowed. The decays of the h_2 state are typically inherited from h_1 , so the chain $h_1 \rightarrow h_2 h_2$ is likely to produce $4b$, $2b2\tau$ and 4τ final states, which can be distinctive but challenging to find at hadron colliders [193, 194]. On the other hand, the singlet-like h_2 state may have more exotic decay channels if there are other light states in the theory, such as a light singlet fermion [195, 196]. More generically, one could expect a significant signal reduction in conventional SM Higgs search channels due to the effects of mixing and $h_1 \rightarrow h_2 h_2$ decays if kinematically allowed [92], as well as the appearance of the second state h_2 [197].

New light particles are also needed to induce CP-violation in the expanding bubble walls. In many cases, they carry non-trivial electroweak charges and couple to the varying-Higgs background. This is true of the MSSM, where the main source comes from light neutralinos and charginos [198]. Direct searches for such particles created via their electroweak production modes are underway at the LHC, and some relevant exclusions have been obtained [199]. Even so, the detailed signals depend very sensitively on the decay channels of the new states.

4.3. The cosmological frontier: gravity waves and more

The strongly first-order phase transition needed for EWBG can produce a cosmological signal in the form of gravity waves [200, 201]. As discussed above, the phase transition proceeds by the formation of bubbles of the electroweak broken phase within the surrounding symmetric-phase plasma. Gravitational radiation is created by the turbulent expansion of the walls [202] and their subsequent collisions as they coalesce [200, 201]. The net effect of the many bubble collisions that occurred within the current Hubble radius is a uniform stochastic background of gravitational radiation with a characteristic spectrum.

The spectrum and intensity of gravity waves created by a strongly first-order phase transition depend on three parameters characterizing the transition [201, 202]: the latent heat α released by the phase transition at the nucleation temperature T_n relative to the background radiation energy, the characteristic rate of bubble nucleation β and the bubble wall velocity v_b . All three quantities can be computed from the finite-temperature effective potential discussed in section 2.

Estimates of the gravity wave signals produced by a strongly first-order EWPT suggest that it will be very difficult to detect in the foreseeable future [203–205]. The signal is typically too low in frequency to be picked up by the LIGO experiment, but it may be visible at LISA if the transition is extremely strong. The prospects of discovery are considerably better at BBO, but even in this case the signal from the phase transition could be obscured by larger gravity wave signals due to astrophysical processes or inflation [204].

New physics related to EWBG can also play an important role in other aspects of cosmology. A specific example of this is DM in the MSSM. Here, the lightest neutralino can play a key role in generating the baryon asymmetry as described in section 3, and can also make up the DM if it is the lightest superpartner (LSP). When the LSP is Bino-like, as motivated by the limits from EDM searches, the relic abundance tends to be too large. However, MSSM EWBG also requires a very light stop, and this state can reduce the Bino-like LSP abundance to an acceptable level by coannihilation [140, 206]. A similar interplay between the new states contributing to EWBG and those making up the DM is also found in a variety of other models.

5. Summary

EWBG remains a theoretically attractive and experimentally testable mechanism to generate the baryon asymmetry of the Universe. During the past decade, much of the theoretical attention has focused on leptogenesis—motivated in part by the discovery of neutrino oscillations and the relative simplicity of this scenario. More recently, however, there has been a resurgence of interest in EWBG due to its testability and the advent of new probes of physics at the terascale. Searches for new particles at the LHC could discover degrees of freedom that were thermally abundant during the EWPT and whose interactions could have engendered a strong first-order transition while giving rise to particle asymmetries needed to seed the production of baryons. At the same time, a generation of new searches for permanent EDMs will provide ever more powerful probes of possible flavor diagonal CP-violation in these new interactions that is an essential ingredient for successful EWBG. In parallel, new mechanisms involving flavor non-diagonal terascale CP-violation are under study, and these mechanisms may have signatures in experiments involving B-mesons at the LHC or super-B factories. In short, one may anticipate that either the ingredients for successful EWBG will be uncovered during the coming decade or that this scenario will be sufficiently constrained that more speculative, high-scale baryogenesis scenarios such as leptogenesis are left standing as the most viable alternatives.

Achieving this confrontation of experiment with EWBG requires having in hand the most robust theoretical tools for computing the baryon asymmetry and a sufficiently broad phenomenological framework. In both respects, the past decade has witnessed considerable advances. Substantial effort has been devoted to deriving and solving the relevant set of transport equations that underlie the production of LH particle number asymmetries, while new attention has focused on improving the computations of phase transition properties. Nonetheless, there exists ample room for further improvements. In the case of the EWPT, future work could include development of additional methods for carrying out gauge-invariant perturbative computations, calculations of the fluctuation determinant in BSM scenarios, and investigation of the other sources of uncertainty that enter the BNPC of equation (20). New Monte Carlo studies in representative BSM theories would also provide important benchmarks for gauging the validity of perturbative computations and their phenomenological implications. Continued refinements of the transport machinery would include application of the recent developments for scalar fields to fermionic systems, updated analyses of the ‘semiclassical force’ terms, and resolution of questions surrounding the coherence shells. From the standpoint of phenomenology, an interesting new direction entails the possible role of flavor non-diagonal CP-violation. Further study of signatures of BSM scalar sectors, including modified Higgs production cross sections, branching ratios, and exotic final states—as well as scenarios in which interesting scalar sector extensions could evade discovery at the LHC—is also an obvious priority.

More broadly speaking, explaining the origin of the visible matter of the Universe continues to be one of the primary motivations for seeking what lies BSM. While it is by no means certain that the explanation lies at the terascale, the time is ripe to address this possibility with vigor as part of the larger effort to determine what new symmetries and degrees of freedom—if any—are associated with the electroweak chapter of cosmic history. Whatever the outcome of the EWBG theory–experiment interface, one can expect this endeavor to yield important new insights into the fundamental laws of nature and their cosmological implications.

Acknowledgments

The authors thank V Cirigliano, S Profumo and Carlos Wagner for helpful discussions and critical reading of the manuscript. This work was supported in part by US Department of Energy Contract DE-FG02-08ER41531(MJRM) and the Wisconsin Alumni Research Foundation (MJRM), as well as by NSERC (DEM). DEM and MJRM would also like to thank the American Physical Society (<http://publish.aps.org>), Elsevier (www.journals.elsevier.com/nuclear-physics-b/) and *Journal of High Energy Physics* (JHEP) (<http://jhep.sissa.it/jhep>) and the corresponding authors for permission to reproduce figures.

References

- [1] Kuzmin V A, Rubakov V A and Shaposhnikov M E 1985 *Phys. Lett. B* **155** 36
- [2] Shaposhnikov M E 1986 *Pisma Zh. Eksp. Teor. Fiz.* **44** 364
Shaposhnikov M E 1986 *JETP Lett.* **44** 465 (Engl. transl.)
- [3] Shaposhnikov M E 1987 *Nucl. Phys. B* **287** 757
- [4] Cohen A G, Kaplan D B and Nelson A E 1993 *Ann. Rev. Nucl. Part. Sci.* **43** 27
- [5] Trodden M 1999 *Rev. Mod. Phys.* **71** 1463
- [6] Riotto A 1998 arXiv:[hep-ph/9807454](http://arxiv.org/abs/hep-ph/9807454)
- [7] Riotto A and Trodden M 1999 *Ann. Rev. Nucl. Part. Sci.* **49** 35
- [8] Quiros M 1999 arXiv:[hep-ph/9901312](http://arxiv.org/abs/hep-ph/9901312)
- [9] Dine M and Kusenko A 2003 *Rev. Mod. Phys.* **76** 1
- [10] Cline J M 2006 arXiv:[hep-ph/0609145](http://arxiv.org/abs/hep-ph/0609145)
- [11] Kirzhnits D A 1972 *Pisma Zh. Eksp. Teor. Fiz.* **15** 745
Kirzhnits D A 1972 *JETP Lett.* **15** 529 (Engl. transl.)
- [12] Kirzhnits D A and Linde A D 1972 *Phys. Lett. B* **42** 471
- [13] Dolan L and Jackiw R 1974 *Phys. Rev. D* **9** 3320
- [14] Weinberg S 1974 *Phys. Rev. D* **9** 3357
- [15] Manton N S 1983 *Phys. Rev. D* **28** 2019
- [16] Klinkhamer F R and Manton N S 1984 *Phys. Rev. D* **30** 2212
- [17] Sakharov A D 1967 *Pisma Zh. Eksp. Teor. Fiz.* **5** 32
Sakharov A D 1967 *JETP Lett.* **5** 24 (Engl. transl.)
Sakharov A D 1991 *Usp. Fiz. Nauk* **161** 61
Sakharov A D 1991 *Sov. Phys.—Usp.* **34** 392 (Engl. transl.)
- [18] Bochkarev A I and Shaposhnikov M E 1987 *Mod. Phys. Lett. A* **2** 417
- [19] Kajantie K, Laine M, Rummukainen K and Shaposhnikov M E 1996 *Nucl. Phys. B* **466** 189
- [20] Barate R *et al* (LEP Working Group for Higgs boson searches and ALEPH and DELPHI and L3 and OPAL Collaborations) 2003 *Phys. Lett. B* **565** 61
- [21] Aad G *et al* (ATLAS Collaboration) 2012 *Phys. Lett. B* **716** 1
- [22] Chatrchyan S *et al* (CMS Collaboration) 2012 *Phys. Lett. B* **716** 30
- [23] Gavela M B, Hernandez P, Orloff J and Pene O 1994 *Mod. Phys. Lett. A* **9** 795
- [24] Huet P and Sather E 1995 *Phys. Rev. D* **51** 379
- [25] Gavela M B, Hernandez P, Orloff J, Pene O and Quimbay C 1994 *Nucl. Phys. B* **430** 382
- [26] Kapusta J I and Gale C 2006 *Finite-Temperature Field Theory: Principles and Applications* (Cambridge: Cambridge University Press) p 428
- [27] Le Bellac M 2000 *Thermal Field Theory* (Cambridge: Cambridge University Press) p 256
- [28] Das A K 1997 *Finite Temperature Field Theory* (Singapore: World Scientific) p 404
- [29] Coleman S R and Weinberg E J 1973 *Phys. Rev. D* **7** 1888
- [30] Anderson G W and Hall L J 1992 *Phys. Rev. D* **45** 2685

- [31] Gross D J, Pisarski R D and Yaffe L G 1981 *Rev. Mod. Phys.* **53** 43
- [32] Parwani R R 1992 *Phys. Rev. D* **45** 4695
Parwani R R 1993 *Phys. Rev.* **48** 5965 (erratum)
Carrington M E 1992 *Phys. Rev. D* **45** 2933
Arnold P B and Espinosa O 1993 *Phys. Rev. D* **47** 3546
Arnold P B and Espinosa O 1994 *Phys. Rev. D* **50** 6662 (erratum)
- [33] Linde A D 1977 *Phys. Lett. B* **70** 306
Linde A D 1979 *Rep. Prog. Phys.* **42** 389
Linde A D 1983 *Nucl. Phys. B* **216** 421
Linde A D 1983 *Nucl. Phys. B* **223** 544 (erratum)
- [34] Dine M, Leigh R G, Huet P Y, Linde A D and Linde D A 1992 *Phys. Rev. D* **46** 550
- [35] Moore G D and Rummukainen K 2001 *Phys. Rev. D* **63** 045002
- [36] Moore G D 2000 *J. High Energy Phys.* **JHEP03(2000)006**
- [37] Megevand A and Sanchez A D 2010 *Nucl. Phys. B* **825** 151
- [38] Espinosa J R, Konstandin T, No J M and Servant G 2010 *J. Cosmol. Astropart. Phys.* **JCAP06(2010)028**
- [39] Carena M, Nardini G, Quiros M and Wagner C E M 2008 *J. High Energy Phys.* **JHEP10(2008)062**
- [40] Carena M, Nardini G, Quiros M and Wagner C E M 2009 *Nucl. Phys. B* **812** 243
- [41] Dolan L and Jackiw R 1974 *Phys. Rev. D* **9** 2904
- [42] Nielsen N K 1975 *Nucl. Phys. B* **101** 173
- [43] Fukuda R and Kugo T 1976 *Phys. Rev. D* **13** 3469
- [44] Fischler W and Brout R 1975 *Phys. Rev. D* **11** 905
- [45] Baacke J and Junker S 1994 *Phys. Rev. D* **49** 2055
- [46] Baacke J and Junker S 1994 *Phys. Rev. D* **50** 4227
- [47] Laine M 1995 *Phys. Rev. D* **51** 4525
- [48] Metaxas D and Weinberg E J 1996 *Phys. Rev. D* **53** 836
- [49] Boyanovsky D, Brahm D, Holman R and Lee D S 1996 *Phys. Rev. D* **54** 1763
- [50] Patel H H and Ramsey-Musolf M J 2011 *J. High Energy Phys.* **JHEP07(2011)029**
- [51] Wainwright C, Profumo S and Ramsey-Musolf M J 2011 *Phys. Rev. D* **84** 023521
- [52] Garny M and Konstandin T 2012 *J. High Energy Phys.* **JHEP07(2012)189**
- [53] Wainwright C L, Profumo S and Ramsey-Musolf M J 2012 *Phys. Rev. D* **86** 083537
- [54] Arnold P B and McLerran L D 1987 *Phys. Rev. D* **36** 581
- [55] Ringwald A 1988 *Phys. Lett. B* **201** 510
- [56] Carson L, Li X, McLerran L D and Wang R-T 1990 *Phys. Rev. D* **42** 2127
- [57] Brihaye Y and Kunz J 1993 *Phys. Rev. D* **48** 3884
- [58] Bodeker D, Moore G D and Rummukainen K 2000 *Phys. Rev. D* **61** 056003
- [59] Ambjorn J, Laursen M and Shaposhnikov M E 1987 *Phys. Lett. B* **197** 49
- [60] Ambjorn J, Laursen M L and Shaposhnikov M E 1989 *Nucl. Phys. B* **316** 483
- [61] Ambjorn J, Askgaard T, Porter H and Shaposhnikov M E 1990 *Phys. Lett. B* **244** 479
- [62] Ambjorn J, Askgaard T, Porter H and Shaposhnikov M E 1991 *Nucl. Phys. B* **353** 346
- [63] Kajantie K, Rummukainen K and Shaposhnikov M E 1993 *Nucl. Phys. B* **407** 356
- [64] Farakos K, Kajantie K, Rummukainen K and Shaposhnikov M E 1995 *Nucl. Phys. B* **442** 317
- [65] Kajantie K, Laine M, Rummukainen K and Shaposhnikov M E 1996 *Nucl. Phys. B* **458** 90
- [66] Jansen K 1996 *Nucl. Phys. Proc. Suppl.* **47** 196
- [67] Kajantie K, Laine M, Rummukainen K and Shaposhnikov M E 1996 *Phys. Rev. Lett.* **77** 2887
- [68] Kajantie K, Laine M, Rummukainen K and Shaposhnikov M E 1997 *Nucl. Phys. B* **493** 413
- [69] Csikor F, Fodor Z, Hein J, Jaster A and Montvay I 1996 *Nucl. Phys. B* **474** 421
- [70] Gurtler M, Ilgenfritz E-M and Schiller A 1997 *Phys. Rev. D* **56** 3888
- [71] Laine M and Rummukainen K 1998 *Nucl. Phys. B* **535** 423
- [72] Laine M and Rummukainen K 1999 *Nucl. Phys. Proc. Suppl.* **73** 180

- [73] Csikor F, Fodor Z and Heitger J 1998 *Phys. Lett. B* **441** 354
- [74] Csikor F, Fodor Z and Heitger J 1999 *Phys. Rev. Lett.* **82** 21
- [75] Moore G D 1999 *Phys. Rev. D* **59** 014503
- [76] Aoki Y, Csikor F, Fodor Z and Ukawa A 1999 *Phys. Rev. D* **60** 013001
- [77] Csikor F, Fodor Z, Hegedus P, Jakovac A, Katz S D and Piroth A 2000 *Phys. Rev. Lett.* **85** 932
- [78] Laine M and Rummukainen K 2001 *Nucl. Phys. B* **597** 23
- [79] Cohen T, Morrissey D E and Pierce A 2012 *Phys. Rev. D* **86** 013009
- [80] Espinosa J R 1996 *Nucl. Phys. B* **475** 273
- [81] Cohen T and Pierce A 2012 *Phys. Rev. D* **85** 033006
- [82] Espinosa J R and Quiros M 1993 *Phys. Lett. B* **302** 51
- [83] Carena M S, Quiros M and Wagner C E M 1996 *Phys. Lett. B* **380** 81
- [84] Delepine D, Gerard J M, Felipe G R and Weyers J 1996 *Phys. Lett. B* **386** 183
- [85] Carena M S, Quiros M, Riotto A, Vilja I and Wagner C E M 1997 *Nucl. Phys. B* **503** 387
- [86] Carena M S, Quiros M and Wagner C E M 1998 *Nucl. Phys. B* **524** 3
- [87] Cline J M and Moore G D 1998 *Phys. Rev. Lett.* **81** 3315
- [88] Pietroni M 1993 *Nucl. Phys. B* **402** 27
- [89] Davies A T, Froggatt C D and Moorhouse R G 1996 *Phys. Lett. B* **372** 88
- [90] Huber S J and Schmidt M G 1999 *Eur. Phys. J. C* **10** 473
- [91] Huber S J and Schmidt M G 2001 *Nucl. Phys. B* **606** 183
- [92] Profumo S, Ramsey-Musolf M J and Shaughnessy G 2007 *J. High Energy Phys.* **JHEP08(2007)010**
- [93] Espinosa J R, Konstandin T and Riva F 2012 *Nucl. Phys. B* **854** 592
- [94] Espinosa J R, Gripaos B, Konstandin T and Riva F 2012 *J. Cosmol. Astropart. Phys.* **JCAP01(2012)012**
- [95] Kang J, Langacker P, Li T-j and Liu T 2005 *Phys. Rev. Lett.* **94** 061801
- [96] Turok N and Zadrozny J 1991 *Nucl. Phys. B* **358** 471
- [97] Cline J M, Kainulainen K and Trott M 2011 *J. High Energy Phys.* **JHEP11(2011)089**
- [98] Chowdhury T A, Nemevsek M, Senjanovic G and Zhang Y 2012 *J. Cosmol. Astropart. Phys.* **JCAP02(2012)029**
- [99] Borah D and Cline J M 2012 arXiv:1204.4722 [hep-ph]
- [100] Delaunay C, Grojean C and Wells J D 2008 *J. High Energy Phys.* **JHEP04(2008)029**
- [101] Grinstein B and Trott M 2008 *Phys. Rev. D* **78** 075022
- [102] Bernal N, Blum K, Nir Y and Losada M 2009 *J. High Energy Phys.* **JHEP08(2009)053**
- [103] Barenboim G and Rasero J 2012 *J. High Energy Phys.* **JHEP07(2012)028**
- [104] Krauss L M and Trodden M 1999 *Phys. Rev. Lett.* **83** 1502
- [105] Garcia-Bellido J, Grigoriev D Y, Kusenko A and Shaposhnikov M E 1999 *Phys. Rev. D* **60** 123504
- [106] Copeland E J, Lyth D, Rajantie A and Trodden M 2001 *Phys. Rev. D* **64** 043506
- [107] Smit J and Tranberg A 2002 arXiv:hep-ph/0210348
- [108] Tranberg A and Smit J 2003 *J. High Energy Phys.* **JHEP11(2003)016**
- [109] Konstandin T and Servant G 2011 *J. Cosmol. Astropart. Phys.* **JCAP07(2011)024**
- [110] Turok N and Zadrozny J 1990 *Phys. Rev. Lett.* **65** 2331
- [111] Tranberg A, Hernandez A, Konstandin T and Schmidt M G 2010 *Phys. Lett. B* **690** 207
- [112] Cohen A G, Kaplan D B and Nelson A E 1994 *Phys. Lett. B* **336** 41
- [113] Chung D J H, Garbrecht B, Ramsey-Musolf M J and Tulin S 2009 *Phys. Rev. Lett.* **102** 061301
- [114] Chung D J H, Garbrecht B, Ramsey-Musolf M J and Tulin S 2010 *Phys. Rev. D* **81** 063506
- [115] Chung D J H, Garbrecht B, Ramsey-Musolf M J and Tulin S 2009 *J. High Energy Phys.* **JHEP12(2009)067**
- [116] Cohen A G, Kaplan D B and Nelson A E 1990 *Phys. Lett. B* **245** 561
- [117] Cohen A G, Kaplan D B and Nelson A E 1991 *Nucl. Phys. B* **349** 727
- [118] Nelson A E, Kaplan D B and Cohen A G 1992 *Nucl. Phys. B* **373** 453
- [119] Cohen A G, Kaplan D B and Nelson A E 1992 *Phys. Lett. B* **294** 57

- [120] Farrar G R and Shaposhnikov M E 1993 *Phys. Rev. Lett.* **70** 2833
 Farrar G R and Shaposhnikov M E 1993 *Phys. Rev. Lett.* **71** 210 (erratum)
- [121] Farrar G R and Shaposhnikov M E 1994 *Phys. Rev. D* **50** 774
- [122] Farrar G R and Shaposhnikov M E 1994 arXiv:hep-ph/9406387
- [123] Joyce M, Prokopec T and Turok N 1994 *Phys. Lett. B* **338** 269
- [124] Joyce M, Prokopec T and Turok N 1996 *Phys. Rev. D* **53** 2930
- [125] Huet P and Nelson A E 1996 *Phys. Rev. D* **53** 4578
- [126] Cline J M, Kainulainen K and Vischer A P 1996 *Phys. Rev. D* **54** 2451
- [127] Funakubo K 1996 *Prog. Theor. Phys.* **96** 475
- [128] Davoudiasl H, Rajagopal K and Westphal E 1998 *Nucl. Phys. B* **515** 384
- [129] Cline J M, Joyce M and Kainulainen K 2000 *J. High Energy Phys.* JHEP07(2000)018
- [130] Riotto A 1996 *Phys. Rev. D* **53** 5834
- [131] Riotto A 1998 *Nucl. Phys. B* **518** 339
- [132] Riotto A 1998 *Phys. Rev. D* **58** 095009
- [133] Lee C, Cirigliano V and Ramsey-Musolf M J 2005 *Phys. Rev. D* **71** 075010
- [134] Schwinger J S 1961 *J. Math. Phys.* **2** 407
- [135] Keldysh L V 1964 *Zh. Eksp. Teor. Fiz.* **47** 1515
 Keldysh L V 1965 *Sov. Phys.—JETP* **20** 1018 (Engl. transl.)
- [136] Mahanthappa K T 1962 *Phys. Rev.* **126** 329
- [137] Bakshi P M and Mahanthappa K T 1963 *J. Math. Phys.* **4** 1
- [138] Carena M S, Moreno J M, Quiros M, Seco M and Wagner C E M 2001 *Nucl. Phys. B* **599** 158
- [139] Carena M S, Quiros M, Seco M and Wagner C E M 2003 *Nucl. Phys. B* **650** 24
- [140] Balazs C, Carena M S, Menon A, Morrissey D E and Wagner C E M 2005 *Phys. Rev. D* **71** 075002
- [141] Kainulainen K, Prokopec T, Schmidt M G and Weinstock S 2001 *J. High Energy Phys.* JHEP06(2001)031
- [142] Prokopec T, Schmidt M G and Weinstock S 2004 *Ann. Phys.* **314** 208
- [143] Prokopec T, Schmidt M G and Weinstock S 2004 *Ann. Phys.* **314** 267
- [144] Kadanoff L and Baym G 1962 *Quantum Statistical Mechanics* (New York: Benjamin)
- [145] Garbrecht B, Prokopec T and Schmidt M G 2004 *Eur. Phys. J. C* **38** 135
- [146] Konstandin T, Prokopec T and Schmidt M G 2005 *Nucl. Phys. B* **716** 373
- [147] Konstandin T, Prokopec T, Schmidt M G and Seco M 2006 *Nucl. Phys. B* **738** 1
- [148] Cirigliano V, Lee C, Ramsey-Musolf M J and Tulin S 2010 *Phys. Rev. D* **81** 103503
- [149] Cirigliano V, Lee C and Tulin S 2011 *Phys. Rev. D* **84** 056006
- [150] Herranen M, Kainulainen K and Rahkila P M 2009 *Nucl. Phys. B* **810** 389
- [151] Herranen M, Kainulainen K and Rahkila P M 2008 *J. High Energy Phys.* JHEP09(2008)032
- [152] Herranen M, Kainulainen K and Rahkila P M 2009 *J. High Energy Phys.* JHEP05(2009)119
- [153] Herranen M, Kainulainen K and Rahkila P M 2010 *J. High Energy Phys.* JHEP12(2010)072
- [154] Fidler C, Herranen M, Kainulainen K and Rahkila P M 2012 *J. High Energy Phys.* JHEP02(2012)065
- [155] Calzetta E and Hu B L 1988 *Phys. Rev. D* **37** 2878
- [156] Berges J 2005 *AIP Conf. Proc.* **739** 3
- [157] Cirigliano V, Ramsey-Musolf M J, Tulin S and Lee C 2006 *Phys. Rev. D* **73** 115009
- [158] Hudson J J, Kara D M, Smallman I J, Sauer B E, Tarbutt M R and Hinds E A 2011 *Nature* **473** 493
- [159] Baker C A *et al* 2006 *Phys. Rev. Lett.* **97** 131801
- [160] Griffith W C, Swallows M D, Loftus T H, Romalis M V, Heckel B R and Fortson E N 2009 *Phys. Rev. Lett.* **102** 101601
- [161] Hewett J L *et al* (RC Group Collaboration) 2012 arXiv:1205.2671 [hep-ex]
- [162] Giudice G F and Romanino A 2004 *Nucl. Phys. B* **699** 65
 Giudice G F and Romanino A 2005 *Nucl. Phys. B* **706** 65 (erratum)
- [163] Giudice G F and Romanino A 2006 *Phys. Lett. B* **634** 307
- [164] Li Y, Profumo S and Ramsey-Musolf M 2008 *Phys. Rev. D* **78** 075009

- [165] Li Y, Profumo S and Ramsey-Musolf M 2009 *Phys. Lett. B* **673** 95
- [166] Cirigliano V, Li Y, Profumo S and Ramsey-Musolf M J 2010 *J. High Energy Phys.* **JHEP01(2010)002**
- [167] Kozaczuk J, Profumo S, Ramsey-Musolf M J and Wainwright C L 2012 arXiv:1206.4100 [hep-ph]
- [168] Huber S J, Konstandin T, Prokopec T and Schmidt M G 2006 *Nucl. Phys. B* **757** 172
- [169] Huber S J, Konstandin T, Prokopec T and Schmidt M G 2007 *Nucl. Phys. A* **785** 206
- [170] Blum K, Delaunay C, Losada M, Nir Y and Tulin S 2010 *J. High Energy Phys.* **JHEP05(2010)101**
- [171] Cheung K, Hou T-J, Lee J S and Senaha E 2012 *Phys. Lett. B* **710** 188
- [172] Tulin S and Winslow P 2011 *Phys. Rev. D* **84** 034013
- [173] Liu T, Ramsey-Musolf M J and Shu J 2012 *Phys. Rev. Lett.* **108** 221301
- [174] Yu F 2011 *Phys. Rev. D* **83** 094028
- [175] Aad G *et al* (ATLAS Collaboration) 2011 *Eur. Phys. J. C* **71** 1828
- [176] CMS Collaboration *CMS EXO-11-016*
- [177] Kilic C, Okui T and Sundrum R 2008 *J. High Energy Phys.* **JHEP07(2008)038**
- [178] Choudhury D, Datta M and Maity M 2006 *Phys. Rev. D* **73** 055013
- [179] CDF Collaboration 2009, *Technical Report* CDFNote 9834, CDF, Tevatron, July, 2009
- [180] Abazov V M *et al* (D0 Collaboration) 2008 *Phys. Lett. B* **665** 1
- [181] Carena M, Freitas A and Wagner C E M 2008 *J. High Energy Phys.* **JHEP10(2008)109**
- [182] Bi X-J, Yan Q-S and Yin P-F 2012 *Phys. Rev. D* **85** 035005
- [183] Ajaib M A, Li T and Shafi Q 2012 *Phys. Rev. D* **85** 055021
- [184] He B, Li T and Shafi Q 2012 *J. High Energy Phys.* **JHEP05(2012)148**
- [185] Drees M, Hanussek M and Kim J S 2012 arXiv:1201.5714 [hep-ph]
- [186] Martin S P 2008 *Phys. Rev. D* **77** 075002
- [187] Martin S P and Younkin J E 2009 *Phys. Rev. D* **80** 035026
- [188] Younkin J E and Martin S P 2010 *Phys. Rev. D* **81** 055006
- [189] Barger V, Ishida M and Keung W-Y 2012 *Phys. Rev. Lett.* **108** 081804
- [190] Menon A and Morrissey D E 2009 *Phys. Rev. D* **79** 115020
- [191] Curtin D, Jaiswal P and Meade P 2012 *J. High Energy Phys.* **JHEP08(2012)005**
- [192] Noble A and Perelstein M 2008 *Phys. Rev. D* **78** 063518
- [193] Carena M, Han T, Huang G-Y and Wagner C E M 2008 *J. High Energy Phys.* **JHEP04(2008)092**
- [194] Chang S, Dermisek R, Gunion J F and Weiner N 2008 *Ann. Rev. Nucl. Part. Sci.* **58** 75
- [195] Menon A, Morrissey D E and Wagner C E M 2004 *Phys. Rev. D* **70** 035005
- [196] Barger V, Langacker P, Lee H-S and Shaughnessy G 2006 *Phys. Rev. D* **73** 115010
- [197] Barger V, Langacker P, McCaskey M, Ramsey-Musolf M and Shaughnessy G 2009 *Phys. Rev. D* **79** 015018
- [198] Cirigliano V, Profumo S and Ramsey-Musolf M J 2006 *J. High Energy Phys.* **JHEP07(2006)002**
- [199] ATLAS Collaboration *ATLAS-CONF-2012-023*
- [200] Kosowsky A, Turner M S and Watkins R 1992 *Phys. Rev. Lett.* **69** 2026
- [201] Kamionkowski M, Kosowsky A and Turner M S 1994 *Phys. Rev. D* **49** 2837
- [202] Kosowsky A, Mack A and Kahniashvili T 2002 *Phys. Rev. D* **66** 024030
- [203] Nicolis A 2004 *Class. Quantum Grav.* **21** L27
- [204] Grojean C and Servant G 2007 *Phys. Rev. D* **75** 043507
- [205] Huber S J and Konstandin T 2008 *J. Cosmol. Astropart. Phys.* **JCAP05(2008)017**
- [206] Balazs C, Carena M S and Wagner C E M 2004 *Phys. Rev. D* **70** 015007