

1 **Title: “Genome-scale methods converge on key mitochondrial genes**  
2 **for the survival of human cardiomyocytes in hypoxia.”**

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29 Running head: Constraint-based modelling, hypoxia and human genetics

30

31

32 **Abstract**

33 Background: Any reduction in myocardial oxygen delivery relative to its demands can  
34 impair cardiac contractile performance. Understanding the mitochondrial metabolic  
35 response to hypoxia is key to understanding ischemia tolerance in the myocardium.  
36 We employed a novel combination of two genome-scale methods to study key  
37 processes underlying human myocardial hypoxia tolerance. In particular, we  
38 hypothesised that computational modelling and evolution would identify similar  
39 genes as critical to human myocardial hypoxia tolerance. Methods & Results: We  
40 analysed a reconstruction of the cardiac mitochondrial metabolic network using  
41 constraint-based methods, under conditions of simulated hypoxia. We used flux  
42 balance analysis, random sampling and principle components analysis to explore  
43 feasible steady-state solutions. Hypoxia blunted maximal ATP (-17%) and haeme (-  
44 75%) synthesis and shrank the feasible solution space. TCA and urea cycle fluxes  
45 were also reduced in hypoxia, but phospholipid synthesis was increased. Using  
46 mathematical optimization methods, we identified reactions that would be critical to  
47 hypoxia tolerance in the human heart. We used data regarding SNP frequency and  
48 distribution in the genomes of Tibetans (whose ancestors have resided in persistent  
49 high-altitude hypoxia for several millennia). Six reactions were identified by both  
50 methods as being critical to mitochondrial ATP production in hypoxia:  
51 phosphofructokinase, phosphoglucokinase, Complex II, Complex IV, aconitase and  
52 fumarase. Conclusions: Mathematical optimization and evolution converged on  
53 similar genes as critical to human myocardial hypoxia tolerance. Our approach is  
54 unique and completely novel and demonstrates that genome-scale modelling and  
55 genomics can be used in tandem to provide new insights into cardiovascular genetics.

## 56 **Introduction**

57 Systems biology uses mathematical and computational methods to describe and  
58 explore complex biological networks. An important recent trend in systems biology  
59 has been the development and application of ‘constraint-based modelling’<sup>1</sup>.  
60 Constraint-based modelling provides three very significant advantages over traditional  
61 mathematical approaches for the study of large and complex biochemical systems.  
62 First, very large models (up to thousands of reactions) can be accommodated. Thus  
63 the entire metabolic network of a mitochondrion (for example) can be modelled.  
64 Second, precise descriptions of the behaviour of each enzyme in the system (i.e. rate  
65 laws) are not required. Finally, detailed information regarding the activity of a single  
66 protein (for example, whether an enzyme is allosterically modified or not) is not  
67 necessary. Thus *unlike traditional ‘kinetic’ models, constraint-based models do not*  
68 *rely on, nor do they require, detailed knowledge of an enzyme’s phosphorylation*  
69 *status (for example), nor the abundance of substrates and products.*

70

71 Constraint-based modelling is able to confer these advantages because the underlying  
72 models and assumptions are simple. The basic unit for constraint-based modelling is a  
73 *network model*, similar to the London Underground map. In the case of a biochemical  
74 network, this is constructed using 1) the known presence or absence of reactions  
75 based on genomic, proteomic or biochemical data; and 2) the known (species-  
76 specific) stoichiometry of all the chemical reactions included in the network. To this  
77 basic model are added a series of ‘constraints’ (from which the method derives its  
78 name), including reaction directionality, mass and charge balancing and absolute  
79 limits to metabolite uptake and excretion. Unlike traditional enzyme kinetic  
80 parameters (e.g. Michaelis-Menten midpoints), many of the underlying assumptions

81 in constraint-based models are robust to variations in physical environment (such as  
82 temperature). However, constraint-based models are not able to simulate the exact  
83 behaviour of a biochemical system. Instead, by keeping the underlying assumptions as  
84 simple and robust as possible, they attempt to mirror the constraints which the true  
85 network faces *in vivo*. Nevertheless, one can predict the most likely behaviour of the  
86 system (using Monte Carlo methods) or predict the behaviour of the network at an  
87 optimum value of some assumed 'physiological objective'. A more detailed  
88 description of the approach can be found in the Methods and Supplemental Materials  
89 of the present manuscript, and in many excellent reviews<sup>1-4</sup>. Regarding its utility:  
90 constraint-based modelling, using genome-scale metabolic networks, has been used to  
91 successfully predict the metabolic signatures of human inherited diseases<sup>5-8</sup>, and to  
92 permit the *in silico* design of tumour-specific toxins<sup>9</sup> and aid in the design of  
93 microbial strains for the purposes of metabolic engineering<sup>10</sup>.

94

95 Myocardial ischemia and hypoxia, whether cause or consequence, are common  
96 features of the failing heart; understanding the mitochondrial response to hypoxia is  
97 key to understanding ischemia tolerance. Myocardial hypoxia can be due to any  
98 number of factors, but is most commonly caused by coronary artery or microvascular  
99 heart disease, exacerbated by increased oxygen demand from ventricular remodelling.  
100 Ischaemic heart disease remains the leading cause of death in the developed world;  
101 therefore gaining new insights into the mechanisms whereby heart cells can survive  
102 hypoxia of any duration is a matter of considerable importance.

103

104 Hypoxia, consequent upon a reduction in barometric pressure, is also a consistent  
105 environmental challenge for human populations at high altitude, where it has led to a

106 robustly detectable degree of genetic and phenotypic divergence over evolutionary  
107 timescales<sup>11,12</sup>. Thus human populations at high altitude offer a unique opportunity to  
108 study the genetic response to hypoxia. We used a novel combination of genome-scale  
109 modelling, mathematical optimization and genome-wide analysis of single nucleotide  
110 polymorphisms (SNPs) in humans to study the response of cardiac mitochondria to  
111 hypoxia. In particular, we sought to test our hypothesis that if evolution is an  
112 optimization process, then mathematical optimization methods, when applied to a  
113 metabolic model, would converge on the same set of reactions, critical to  
114 environmental (in this case hypoxic) performance. By comparing information from  
115 natural (evolution) and mathematical optimization methods we sought to identify key  
116 genes and reactions that underlie cardiac tolerance to hypoxia.  
117

## 118 **Methods**

119 The reconstruction of the human cardiac mitochondrial metabolic network from  
120 proteomic and biochemical data was described previously<sup>13</sup>. Briefly, proteomic and  
121 transcriptomic data were used to derive an organelle ‘metabolic parts list’ (i.e. a list of  
122 all metabolic proteins known to be associated with a cardiac mitochondrion). These  
123 parts were ‘connected’ by their species-specific stoichiometric chemical equations.  
124 The draft reconstruction was extensively tested and manually curated. The final model  
125 used herein comprised 195 reactions, 235 metabolites and 25 exchange reactions (for  
126 a full description see<sup>13, 14</sup> and the Supplementary Materials). The exchange reactions  
127 did not represent genuine biochemical reactions, but instead described the exchanges  
128 that were necessary between the network and its environment so that a steady-state  
129 could be achieved. Having reconstructed the network, a series of limits or ‘constraints’  
130 were added, all of which constrained the upper and lower limits of metabolite  
131 exchange of the model with its environment (e.g. oxygen, glucose). These constraints  
132 are in Supplementary Table 1 and represent maximum and minimum flux rates in  
133 human heart mitochondria *in vivo*. To simulate hypoxia, we reduced the upper  
134 constraint on oxygen uptake in the model to 25% of baseline values (normoxia), from  
135  $39.1 \mu\text{M min}^{-1} (\text{g mitochondrial protein})^{-1}$  (henceforth shortened to U) to 9.775 U. Our  
136 choice of simulating severe hypoxia was motivated by an intention to highlight any  
137 effects; however, it is worth noting that complete anoxia can occur in regions of  
138 ischemic myocardium (e.g. during acute myocardial infarction).

139

140 Computational analysis of network models rarely leads to a single set of predicted  
141 fluxes. Instead, methods are used to analyze the possible combinations of fluxes that  
142 allow a steady-state, given the applied constraints. The solutions together are termed

143 the feasible steady-state solution space. Alternatively, one can use linear optimization  
144 to compute a set of fluxes that optimize the value of a given objective function, an  
145 approach typically referred to as flux balance analysis (FBA). For example, this  
146 method would return a set of fluxes that correspond to the highest possible rate of  
147 ATP production by the network, if ATP production was the objective function. When  
148 conducting FBA, we optimized the mitochondrial network for three objective  
149 functions (phospholipid, haeme and ATP synthesis)<sup>13</sup>. Alternate optimal solutions  
150 (i.e. other sets of fluxes that also gave an optimal objective) were accounted for via  
151 flux variability analysis (see below). We also studied the optimization of all three  
152 objectives simultaneously (see Supplementary Materials for details). This method  
153 comprises placing the objective functions under study into hierarchical order (for  
154 example, haeme biosynthesis then phospholipid biosynthesis then ATP synthesis).  
155 The network is optimized for the first objective, then optimized for the second with  
156 the first held at optimal value and so forth.

157

158 We used two computational methods to identify reactions that are critical to hypoxia  
159 tolerance in the mitochondria metabolic network – shadow prices<sup>15</sup> and flux spans<sup>16</sup>.  
160 Shadow prices have been used in metabolic network analysis before<sup>15, 17</sup>. Shadow  
161 prices (also known as Lagrange multipliers) are measures of the degree to which the  
162 value of the objective function is affected by the availability of a particular resource.  
163 For example, if ATP synthesis were the objective function, a shadow price of 1.0 for  
164 glucose (for example) would indicate that a 1 unit increase in glucose availability  
165 would lead to an equivalent increase in ATP synthesis. A shadow price of 2.0 would  
166 indicate that a unit increase in the availability of glucose would result in a two unit  
167 increase in ATP synthesis, and so forth. We reasoned therefore that reactions for

168 which metabolites with large, positive shadow prices were either substrates or  
169 products, would be crucial to hypoxic performance (at least, for the objective function  
170 under investigation). To assess the likelihood that our method had outperformed  
171 chance, we used simple permutation testing.

172

173 Our second approach was to use flux spans. Using flux variability analysis<sup>18</sup> we  
174 computed the range of values that flux through each reaction could take at an  
175 optimum (computed using FBA). Taken together, these ranges delineate the set of  
176 alternate optimal solutions (i.e. different sets of fluxes that result in the same optimal  
177 value of the objective)<sup>18</sup>. By calculating the difference between the upper and lower  
178 feasible fluxes we derived a flux span for each reaction. Here we express these as a  
179 relative ratio. Hence a reaction with flux = 10 U and with the lower and upper feasible  
180 fluxes being 8 and 12 U respectively would have a relative flux span of 0.4 (or 40%).  
181 We reasoned that reactions with the smallest relative flux spans would be critical to  
182 hypoxia tolerance and hypoxic performance. Again, we used permutations to estimate  
183 the probability that our method had outperformed chance alone.

184

185 We used data from a genome-wide allelic differentiation scan (GWADS) comparing  
186 SNP frequencies of Tibetans ( $n = 35$ ) residing at 3200-5000 m, with 84 individuals  
187 from the founder population. Subjects were recruited from three distinct regions of  
188 China: the North Western region of Yunnan province, Mag Xiang and Zhaxizong  
189 Xiang (both in the Tibet Autonomous Region). Genotypic data from the HapMap  
190 Phase III Han population were also included. These data have been analyzed  
191 previously<sup>11</sup> and full details can be found in this earlier publication. Each gene was  
192 assigned a genome-wide  $p$ -value that serves as an estimate of the degree of selective



193 pressure applied to that gene (through differences in SNP frequency). Details  
194 regarding the calculation of these  $p$ -values can also be found elsewhere <sup>11</sup>. We  
195 extracted the  $p$ -values corresponding to the genes in our model and ranked genes by  
196 smallest GWADS  $p$ -value first, producing a list of nuclear-encoded mitochondrial  
197 genes with an accompanying measure of selective pressure in humans living in  
198 persistent hypoxia.

199

200 Where appropriate, means and standard deviations are given. However, modelling  
201 results are often a single datum point (e.g. differences in optimal ATP synthesis rate,  
202 determined using flux balance analysis, under hypoxia and normoxia) and are  
203 therefore given as such.

204

205

## 206 **Results**

207 We optimized the network for three physiological ‘targets’ (objective functions) -  
208 ATP, haeme and phospholipid biosynthesis<sup>13</sup> – using flux balance analysis (FBA)<sup>1</sup>.  
209 Hypoxia reduced the optimal ATP synthesis rate by 13%, from 45.8 to 36.6 U. Figure  
210 1 shows a quantized heatmap of the accompanying differences in flux. There were  
211 reductions in flux through many reactions comprising the TCA cycle and oxidative  
212 phosphorylation. There were also reductions in flux through most reactions  
213 comprising fatty acid uptake, transport, activation and oxidation, although some were  
214 maintained due to the imposition of a minimum uptake rate (this is a physiological  
215 constraint imposed by the ability of fatty acids to diffuse freely across membranes).  
216 Glycolytic rates were similar, which was expected as maximal ATP synthesis was the  
217 objective. The flux through multiple reactions required for phospholipid biosynthesis  
218 were increased and the demand reaction was activated in hypoxia. To ensure that the  
219 degree of simulated hypoxia affected our results quantitatively but not qualitatively,  
220 we performed additional flux balance analysis experiments at various intermediate  
221 oxygen uptake rates. The results are in Supplementary Figure 1. Briefly, maximal  
222 ATP synthesis was progressively reduced by increasing hypoxia. Consistent with our  
223 interpretation, phospholipid biosynthesis was not activated until O<sub>2</sub> uptake dropped  
224 below a critical level, at which point a ‘sink’ for fatty acid carbons was required.  
225 There was no evidence of qualitative shifts in carbon flux as maximal O<sub>2</sub> uptake rate  
226 was progressively reduced.  
227  
228 Haeme synthesis was blunted by 75% in hypoxia (hypoxia: 0.650 vs. normoxia: 2.44  
229 U). The pattern of flux differences between the optimized network in normoxia and  
230 hypoxia was similar to that with ATP synthesis as the objective. Flux through

231 reactions comprising the TCA cycle, oxidative phosphorylation, the urea cycle and  
232 haeme synthesis itself were suppressed. There were increases in long-chain (C20:4  
233 and C22:6) activation and an increase in phospholipid biosynthesis. A heatmap of  
234 differences in flux across the network under these conditions (haeme biosynthesis as  
235 the objective function in hypoxia vs. normoxia) is given in Supplementary Figure 2.  
236 However, when phospholipid biosynthesis was the objective it was unchanged by  
237 oxygen restriction, at 22.8 U.

238

239 We then performed multiple objective analyses with three different hierarchies of  
240 objective functions. 1. ATP > haeme > phospholipid: In normoxia, and with ATP  
241 synthesis fixed at its optimal value of 45.8 U, haeme and phospholipid synthesis were  
242 eliminated. In hypoxia, with ATP synthesis fixed at its optimal value of 36.6 U,  
243 haeme synthesis was still eliminated; however, optimized phospholipid biosynthesis  
244 was now non-zero, although reduced ~100-fold at 0.265 U. 2. Haeme > phospholipid  
245 > ATP: In normoxia, with haeme biosynthesis at its optimal rate of 2.44 U, both  
246 phospholipid and ATP synthesis were abolished. In hypoxia, with haeme biosynthesis  
247 at 0.650, phospholipid biosynthesis was possible and optimized to 0.867 U; ATP  
248 synthesis was abolished. 3. Phospholipid > haeme > ATP: As maximal phospholipid  
249 biosynthesis was unaffected by hypoxia it was fixed at 0.867 U for both conditions  
250 (normoxia/hypoxia). In both normoxia and hypoxia, haeme biosynthesis gained  
251 optimal values the same as those where it was the only objective function considered  
252 (normoxia: 2.44 U vs. hypoxia: 0.650 U). In normoxia, ATP biosynthesis was  
253 subsequently limited to 8.85 U; in hypoxia it was reduced far less, to 19.3 U. A  
254 summary of all the optima is in Supplementary Table 2.

255

256 We next used uniform random sampling <sup>19</sup>, a method that characterizes the steady-  
257 state solution space without requiring an objective function. Figure 1b shows a  
258 quantized heatmap of differences in median flux. Consistent with the FBA results,  
259 fluxes through reactions comprising oxidative phosphorylation, the TCA cycle and  
260 fatty acid metabolism were reduced in hypoxia. Without the requirement to maximize  
261 ATP synthesis in normoxia that was elsewhere imposed by FBA, glycolytic flux  
262 increased in hypoxia. The heatmap shows a reduction in flux through lactate  
263 dehydrogenase and the lactate transporter; however, this represents a *reversal* in flux,  
264 from uptake to efflux. Also noteworthy is a reduction in urea cycle flux in hypoxia.

265

266 We analysed the sampled data using principal components analysis (PCA), allowing  
267 us to visualize patterns of change. We modelled the sampled data together and found  
268 that five components captured 65% of the total variance. When plotted, the scores on  
269 these components revealed that hypoxia substantially reduced the dimensions of the  
270 solution space, reducing the flexibility of the metabolic network even though the  
271 dimensions of the space were the same. This was especially apparent in principal  
272 components 1 and 2 (Figure 2), with principal component 1 being dominated by  
273 reactions related to gas exchange, the TCA cycle and oxidative phosphorylation and  
274 principal component 2 being dominated by reactions related to iron transport and  
275 haeme biosynthesis.

276

277 Given that optimal phospholipid biosynthesis was unaffected by oxygen restriction,  
278 we continued by studying those metabolites and reactions that limited optimal ATP  
279 and haeme biosynthesis in the mitochondrial metabolic network under hypoxia. We  
280 first computed shadow prices for all metabolites in the model when optimising the

281 network for either ATP or haeme synthesis. Table 2 gives metabolites with the largest  
282 positive shadow prices and the corresponding twenty discrete reactions for each  
283 objective function. Three classes of metabolite (and reaction) dominated: long-chain  
284 (>20C) fatty acid transport, glycolysis and haeme biosynthesis. When optimising for  
285 ATP synthesis, the largest shadow prices were several-fold larger than when  
286 optimising for haeme synthesis (e.g. 4.0 for cytosolic fructose diphosphate, fdp(c), vs.  
287 1.2 for cytosolic arachidonic acid, c206(c)). When optimizing the network with ATP  
288 synthesis as the objective function, the metabolites with large positive shadow prices  
289 were mainly related to glycolysis, oxidative phosphorylation and the TCA cycle.  
290

291 We next computed flux spans, using flux variability analysis. The reactions with the  
292 smallest relative flux spans when optimizing the network for either haeme or ATP  
293 synthesis are given in Table 3. As with shadow prices, the magnitude of the parameter  
294 (in this case, relative flux span) was several fold different when optimizing ATP vs.  
295 haeme synthesis; in both cases the difference (larger shadow prices and smaller flux  
296 spans) was consistent with ATP synthesis being more tightly restricted by hypoxia.  
297 Interestingly, reactions related to oxidative phosphorylation both had narrow flux  
298 spans regardless of whether ATP or haeme synthesis were the objectives. In particular,  
299 complex IV of the respiratory chain was ranked in the top two (Table 3). Perhaps  
300 unsurprisingly, reactions related to proto-haeme synthesis and iron transport also had  
301 small relative flux spans when optimizing for haeme synthesis. When optimizing the  
302 network for ATP synthesis, reactions from the TCA cycle and glycolysis were highly  
303 represented.  
304

305 We generated a complete list of nuclear-encoded mitochondrial genes with a

306 corresponding measure of selective pressure at high altitude. The twenty ‘most  
307 selected’ genes (i.e. smallest  $p$ -value) are in Table 1. Using permutations, we assessed  
308 the likelihood that mathematical optimization had outperformed chance when  
309 predicting genes under pressure. When conducting shadow price analysis with ATP  
310 synthesis as the objective, we selected the 16 metabolites with the largest positive  
311 shadow price corresponding to 20 discrete reactions shown in Table 2. Of these 20  
312 reactions, two (phosphofructokinase (PFK) and phosphoglycerate kinase (PGK))  
313 carried flux and corresponded to genes in Table 1. However, permutation testing  
314 suggested that random selections of 16 metabolites would equal or outperform our  
315 modelling approach most of the time ( $p = \sim 0.860$ ). We observed that two of the only  
316 three metabolites with shadow prices of 3 or greater when optimizing the network for  
317 either objective (cytosolic fructose 6-phosphate and fructose diphosphate, f6p(c) and  
318 fdp(c) respectively in Table 2) are both substrate and product for PFK, the most  
319 ‘heavily selected’ gene in Table 1. We next compared the reactions highlighted by  
320 shadow price analysis whilst optimizing the network for haeme synthesis. Three  
321 reactions were common with those in Table 1: hydroxymethylbilane synthase  
322 (HMBS), porphobilinogen synthase (PPBNGS) and phosphoglycerate kinase (PGK).  
323 Once again, permutations suggested that shadow pricing had not outperformed chance  
324 when identifying genes under pressure.

325

326 We used a similar approach to assess the performance of flux span analysis. Table 3  
327 shows that flux span analysis identified three (haeme synthesis) and six (ATP  
328 synthesis) reactions that were common with those that were the most heavily selected  
329 genes in Table 1. With ATP synthesis as the objective, we used permutation testing to  
330 assess whether modelling had outperformed chance when predicting genes under

331 pressure. Random selections only matched flux span analysis 1675 out of 100000  
332 times, offering evidence that this approach had outperformed chance at  $p < .05$ .  
333  
334 We repeated this process with haeme synthesis as the objective function. Using  
335 100000 permutations, random selection matched the model performance  
336 approximately half the time ( $p = \sim 0.525$ ). Hence using flux span analysis with haeme  
337 as the objective had not outperformed chance.

338 **Discussion**

339 Myocardial hypoxia can be either acute or chronic and occurs whenever oxygen  
340 delivery is insufficient to meet the needs of the contracting myocardium. This can be  
341 due to any combination of reduced O<sub>2</sub>-carrying capacity due to anaemia, reduced  
342 haemoglobin saturation (whether environmental or pathological), poor cardiac output  
343 or compromised blood flow due to coronary artery or microvascular heart disease, and  
344 increased oxygen demand associated with stress or structural remodelling (e.g.  
345 ventricular hypertrophy). Ischaemic heart disease remains the leading cause of death  
346 in the developed world. A notable feature of heart failure is that, once left ventricular  
347 dysfunction has been established, patients suffer a relentless apoptotic loss of viable  
348 cardiomyocytes that some investigators believe to be due to repeated, transient  
349 ischaemic and hypoxic events <sup>20</sup>. Therefore understanding the mechanisms whereby  
350 heart cells can survive either transient or sustained hypoxia and ischaemia is a matter  
351 of considerable importance. Here we present an entirely new approach to this question  
352 using systems biology methods that encompass genomics, metabolic modelling and  
353 mathematical optimization.

354

355 We first studied the effect that hypoxia had on the solution space (the set of all  
356 feasible fluxes) of the reconstructed cardiac mitochondrial metabolic network using  
357 two complementary methods – optimization (FBA) and Monte Carlo sampling.  
358 Optimization requires an objective function; in keeping with previous work we  
359 studied three objectives that are central to mitochondrial function: the synthesis of  
360 ATP, haeme and mixed phospholipids <sup>13</sup>. Although maximal phospholipid synthesis  
361 was unaffected by hypoxia, both haeme and ATP synthesis were reduced (by 75% and  
362 13% respectively). The reduction in maximal ATP synthesis was accompanied by



363 reductions in TCA cycle flux, oxidative phosphorylation and fatty acid uptake and  
364 processing but a seemingly paradoxical increase in phospholipid biosynthesis.

365

366 The degree to which maximal haeme synthesis was blunted in hypoxia was striking.  
367 This 75% loss of proto-haeme synthesis capacity was accompanied by many of the  
368 metabolic features observed when optimizing ATP production in hypoxia. Haeme is a  
369 major component of haemoglobin, itself substantially increased in response to  
370 hypoxia to enhance systemic oxygen transport <sup>21</sup>. Thus network stoichiometry forms a  
371 constraint to haeme biosynthesis that may partly define the speed with which haeme  
372 can be synthesized in hypoxia. Non iron-deficient anaemia is a common feature in  
373 heart failure patients, yet its aetiology is unknown <sup>22</sup>. Furthermore, many studies have  
374 shown that reduced haemoglobin is an independent predictor of risk in heart failure  
375 patients <sup>23, 24</sup>, although again the mechanism remains poorly understood. Our  
376 simulations suggest that hypoxia itself can cause significant reductions in proto-  
377 haeme synthesis, both in the heart and elsewhere, and that hypoxia of any kind could  
378 lead to a vicious cycle of blunted haeme synthesis, reduced O<sub>2</sub>-carrying capacity in  
379 blood and subsequently worsened hypoxaemia. Furthermore, in cultured human  
380 neurons, haeme deficiency causes a decrease in (haeme-containing) complex IV  
381 (cytochrome c oxidase) and activation of nitric oxide synthase <sup>25</sup>. Given that  
382 complex IV release is a key component of the p53 apoptotic cascade <sup>26</sup>, this suggests  
383 an intriguing new avenue for investigations into hypoxia-induced myocyte apoptosis.

384

385 We studied the effect on mitochondria of forcing them to balance competing  
386 objectives in hypoxia. When ATP production was given hierarchical ‘superiority’ (as  
387 is almost certainly the case *in vivo*), haeme synthesis was completely abolished in

388 normoxia and hypoxia. Thus haeme and ATP synthesis compete for the same  
389 resources; quite moderate reductions in O<sub>2</sub> supply, coupled with increases in ATP  
390 demand, might lead to profound reductions in haeme synthesis capacity due to  
391 stoichiometric constraints in the metabolic network. Interestingly, phospholipid  
392 biosynthesis was abolished in normoxia under this hierarchy but was active in  
393 hypoxia. This was likely due to competition with ATP synthesis for lipids; in hypoxia,  
394 ATP synthesis was diminished freeing up lipids for phospholipid synthesis.

395

396 We next studied the set of feasible solutions using random sampling. Multiple random  
397 samples of the solution space allow the generation of probability density functions for  
398 flux through every reaction; the most probable value can often predict the measured *in*  
399 *vivo* rate <sup>14</sup>. As with linear optimization (FBA) we observed reductions in TCA cycle  
400 and oxidative phosphorylation reactions, in addition to a reduction in urea cycle flux.  
401 This last is intriguing because flux through arginosuccinate synthetase (ASS) was  
402 decreased in simulated hypoxia. ASS been elsewhere been reported as a target of the  
403 von Hippel-Lindau tumour suppressor gene (*VHL*) <sup>27</sup>, an inverse regulator of HIF-1 $\alpha$ .  
404 Manipulation of *VHL* expression led to corresponding changes in ASS levels in  
405 RCC10 renal cell carcinoma cells.

406

407 Once again we observed that many of the reactions required for phospholipid  
408 biosynthesis were increased and the biosynthesis reaction itself was activated in  
409 hypoxia. Without this redirection of fatty acid flux, the imposition of hypoxia,  
410 combined with minimum uptake rates for fatty acids, would have led to an  
411 accumulation of unoxidized fatty acids in the model and a loss of homeostasis.  
412 Cardiac mitochondria face an identical challenge *in vivo* and redirect fatty acids to

413 storage (away from oxidation) when ischaemic <sup>28</sup>. Similarly, Langendorff-perfused  
414 hearts exposed to acute hypoxia increase phospholipid biosynthesis to maintain lipid  
415 homeostasis <sup>29</sup>. We also observed an increase in glycolytic flux (Figure 1B).

416

417 Overall, the pattern of change in metabolic flux in our simulations was strikingly  
418 consistent with experimental observations of cellular responses to hypoxia, including  
419 the reduction in flux through pyruvate dehydrogenase (PDHm) *in vivo* that is brought  
420 about by modulation of pyruvate dehydrogenase kinase <sup>30</sup>. It is interesting to note that  
421 the reduction in flux through PDHm in our simulations directly resulted from network  
422 stoichiometry, without any additional explanation or control. While the notion that  
423 glycolytic flux is increased in hypoxia is certainly not new, altered (particularly  
424 increased) lipid biosynthesis in response to hypoxia is a less often considered  
425 component of hypoxia tolerance. Previous investigators have reported both increased  
426 <sup>29,31</sup> and decreased <sup>32</sup> lipid synthesis in hypoxia in model systems. These  
427 discrepancies may be due to differences in isotope labelling strategy (e.g. acetate vs.  
428 glycerol vs. palmitate) or outcome measure. However, there is no question that lipids  
429 accumulate in the heart in response to hypoxia and ischaemia <sup>28</sup>. It should be noted  
430 that the details of whole heart lipid-handling in hypoxia and/or ischemia may be  
431 different to the mitochondrial response considered in isolation. It is interesting also  
432 that lipotoxicity – defined as a chronic mismatch between oversupply of acetyl-CoA  
433 from lipid breakdown and its subsequent mitochondrial oxidation – is a stoichiometric  
434 disorder and can be as readily caused by impaired oxidative phosphorylation (for  
435 example, by hypoxia) as lipid oversupply. The consistency of our simulations with  
436 experimental observations reinforced to us the notion that our methods were both  
437 robust and relevant.

438

439 We sought to test whether mathematical optimization had converged on the same  
440 reactions that human evolution had identified as being critical to optimal hypoxic  
441 function. We used data from a GWADS scan comparing SNP frequencies of Tibetans  
442 residing at 3500 m (and whose ancestors have ‘lived high’ for over 10,000 years <sup>33</sup>)  
443 with individuals from the HapMap Phase III Chinese Han sample, who are closely  
444 related but have resided at sea level throughout <sup>11</sup>. Tibetans were ideal for this study  
445 because, despite systemic adjustments (for example, increased breathing rates), they  
446 continue to have lower arterial oxygen content than sea-level dwellers <sup>34</sup>.

447

448 It is interesting that the largest shadow prices were recorded when optimizing the  
449 mitochondrial metabolic network for ATP synthesis in hypoxia. This suggests that,  
450 even in the case of competing objectives, increasing the supply of these metabolites  
451 would be especially advantageous when oxygen supply is limited (either by  
452 environment or pathology). The metabolite with the largest shadow price in any  
453 analysis we conducted was fructose diphosphate, a product of phosphofructokinase  
454 (PFK). However, permutation testing failed to support the notion that shadow prices  
455 and evolution had converged on similar reactions.

456

457 The results gained by examining flux spans were more compelling. Flux spans are the  
458 range of values within which a reaction rate can lie at a computed optimum. We  
459 reasoned that reactions with narrow flux spans would be under greater selective  
460 pressure. We generated a list of reactions with the smallest flux spans (yet which  
461 carried flux) and compared these with the SNP data. When we optimized for ATP  
462 synthesis, the results supported the notion that mathematical optimization and

463 evolution had converged on similar reactions (where 6/20 reactions were common  
464 between the two selections). The common reactions selected by flux span analysis and  
465 evolution were related to haeme synthesis (although only when optimizing for haeme  
466 synthesis), glycolysis (PFK, PGK), the TCA cycle (aconitase and fumarase) and  
467 oxidative phosphorylation (Complexes II and IV). We propose that our combined  
468 method has identified reactions that are especially important in maintaining or  
469 increasing mitochondrial ATP synthesis in the hypoxic heart. This view is supported  
470 by the existing literature. For example, it was recently reported that mice exposed to  
471 three weeks of normobaric hypoxia had reduced Complex II, IV and aconitase activity  
472 in cardiac mitochondria <sup>35</sup> while fumarate accumulation leads to ‘pseudo-hypoxic’  
473 activation of HIF-1 $\alpha$  <sup>36</sup>, suggesting that many of the same reactions highlighted here  
474 indeed have important roles in hypoxic adaptation and, hence, survival. Our combined  
475 approach also yielded an unexpected benefit: Computational analysis was able to  
476 provide suggestions as to whether genes were under positive or negative selective  
477 pressure (an important distinction to which traditional genome-wide analytical  
478 techniques are blind).

479

480 A final note regarding PFK: basic biochemistry textbooks all highlight the importance  
481 of PFK as a key regulatory step in glycolysis (e.g. page 444 in <sup>37</sup>). Yet there is a  
482 tautology here: PFK is heavily regulated biologically (for example, by ATP/AMP,  
483 fructose 2,6-bisphosphate <sup>37</sup> etc.). However its heavy regulation is evidence for, not an  
484 explanation of, its importance. We note that in our simulations, using multiple  
485 objectives and alternative analytical strategies, PFK was repeatedly highlighted as  
486 being an important determinant of the objective. Our model contained no information  
487 whatsoever regarding biological regulation (for example, allosteric modulation by

488 other small molecules). In other words, our simulations suggest that PFK is important  
489 because it occupies a critical point in the metabolic network due to network topology  
490 and nothing more. By extension, this protein is likely to be under strong evolutionary  
491 selective pressure in many environments, leading to complex phenotypic properties.  
492 Once again this was supported in the genetic data, at least in hypoxia.

493

#### 494 *Limitations*

495 Our main hypothesis - that evolution and mathematical optimization would converge  
496 on similar targets – was supported. In so doing we generated a list of genes that the  
497 two methods independently highlighted as potentially important for hypoxic survival.  
498 Although we believe that the nature of our combined approach adds additional  
499 support to the significance of these genes, we wish to stress that genes identified by  
500 any genome-wide method should be treated as ‘candidates’ only. Direct experimental  
501 evidence will always be required to clarify the function of each. Of course, for some  
502 of the genes identified by our approach, overwhelming evidence already exists  
503 confirming their importance (for example, pyruvate dehydrogenase<sup>30, 38, 39</sup>).

504

505 A second limitation relates to possible differences in the Han vs. Tibetan environment  
506 beyond simply altitude (e.g. diet and temperature). Several points are pertinent:

- 507 1. Although temperatures may differ between the two locations, most very high  
508 altitude populations descend lower in winter;
- 509 2. Diet may differ; however many essential elements (reliance on vegetables and use  
510 of rice) are similar;

511 3. Multiple studies have utilized the Han vs Tibetan genome comparison. All have  
512 found the same primary hit (EPAS1), which is a gene regulating expression of a  
513 hypoxia-responsive transcription factor;

514 4. The candidates in the present study were chosen because computational analysis of  
515 a separate network model suggested their role in hypoxia. This makes it more likely  
516 that this was indeed the cause and is, potentially, another benefit of our approach.

517 **Disclosure**

518 HM was, from 2011-13, contracted as a consultant to GSK relating to development of  
519 a drug in the field of hypoxia. However, no involvement was needed and he received  
520 no payment. IT was supported in part by an ATTRACT programme grant  
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522

523



524 **References**

- 525 1. Lewis NE, Nagarajan H, Palsson BO. Constraining the metabolic genotype-  
526 phenotype relationship using a phylogeny of in silico methods. *Nat Rev*  
527 *Microbiol.* 2012;10:291-305
- 528 2. Bordbar A, Palsson BO. Using the reconstructed genome-scale human  
529 metabolic network to study physiology and pathology. *J Intern Med.*  
530 2012;271:131-141
- 531 3. Oberhardt MA, Palsson BO, Papin JA. Applications of genome-scale  
532 metabolic reconstructions. *Mol Syst Biol.* 2009;5:320
- 533 4. Edwards LM, Thiele I. Applying systems biology methods to the study of  
534 human physiology in extreme environments. *Extreme Phys Med.* 2013;2
- 535 5. Sigurdsson MI, Jamshidi N, Jonsson JJ, Palsson BO. Genome-scale network  
536 analysis of imprinted human metabolic genes. *Epigenetics.* 2009;4:43-46
- 537 6. Smith AC, Robinson AJ. A metabolic model of the mitochondrion and its use  
538 in modelling diseases of the tricarboxylic acid cycle. *BMC Syst Biol.*  
539 2011;5:102
- 540 7. Shlomi T, Cabili MN, Ruppin E. Predicting metabolic biomarkers of human  
541 inborn errors of metabolism. *Mol Syst Biol.* 2009;5:263
- 542 8. Thiele I, Swainston N, Fleming RMT, Hoppe A, Sahoo S, Aurich MK,  
543 Haraldsdottir H, Mo ML, Rolfsson O, Stobbe MD, Thorleifsson SG, Agren R,  
544 Bolling C, Bordel S, Chavali AK, Dobson P, Dunn WB, Endler L, Hala D,  
545 Hucka M, Hull D, Jameson D, Jamshidi N, Jonsson JJ, Juty N, Keating S,  
546 Nookaew I, Le Novere N, Malys N, Mazein A, Papin JA, Price ND, Selkov E,  
547 Sigurdsson MI, Simeonidis E, Sonnenschein N, Smallbone K, Sorokin A, van  
548 Beek JHGM, Weichart D, Goryanin I, Nielsen J, Westerhoff HV, Kell DB,

- 549 Mendes P, Palsson BO. A community-driven global reconstruction of human  
550 metabolism. *Nat Biotech.* 2013;advance online publication
- 551 9. Frezza C, Zheng L, Folger O, Rajagopalan KN, MacKenzie ED, Jerby L,  
552 Micaroni M, Chaneton B, Adam J, Hedley A, Kalna G, Tomlinson IP, Pollard  
553 PJ, Watson DG, Deberardinis RJ, Shlomi T, Ruppin E, Gottlieb E. Haem  
554 oxygenase is synthetically lethal with the tumour suppressor fumarate  
555 hydratase. *Nature.* 2011;477:225-228
- 556 10. Hua Q, Joyce AR, Fong SS, Palsson BO. Metabolic analysis of adaptive  
557 evolution for in silico-designed lactate-producing strains. *Biotechnol Bioeng.*  
558 2006;95:992-1002
- 559 11. Beall CM, Cavalleri GL, Deng L, Elston RC, Gao Y, Knight J, Li C, Li JC,  
560 Liang Y, McCormack M, Montgomery HE, Pan H, Robbins PA, Shianna KV,  
561 Tam SC, Tsering N, Veeramah KR, Wang W, Wangdui P, Weale ME, Xu Y,  
562 Xu Z, Yang L, Zaman MJ, Zeng C, Zhang L, Zhang X, Zhaxi P, Zheng YT.  
563 Natural selection on *epas1* (*hif2alpha*) associated with low hemoglobin  
564 concentration in tibetan highlanders. *Proc Natl Acad Sci U S A.*  
565 2010;107:11459-11464
- 566 12. Yi X, Liang Y, Huerta-Sanchez E, Jin X, Cuo ZX, Pool JE, Xu X, Jiang H,  
567 Vinckenbosch N, Korneliussen TS, Zheng H, Liu T, He W, Li K, Luo R, Nie  
568 X, Wu H, Zhao M, Cao H, Zou J, Shan Y, Li S, Yang Q, Asan, Ni P, Tian G,  
569 Xu J, Liu X, Jiang T, Wu R, Zhou G, Tang M, Qin J, Wang T, Feng S, Li G,  
570 Huasang, Luosang J, Wang W, Chen F, Wang Y, Zheng X, Li Z, Bianba Z,  
571 Yang G, Wang X, Tang S, Gao G, Chen Y, Luo Z, Gusang L, Cao Z, Zhang Q,  
572 Ouyang W, Ren X, Liang H, Huang Y, Li J, Bolund L, Kristiansen K, Li Y,

- 573 Zhang Y, Zhang X, Li R, Yang H, Nielsen R, Wang J. Sequencing of 50  
574 human exomes reveals adaptation to high altitude. *Science*. 2010;329:75-78
- 575 13. Vo TD, Greenberg HJ, Palsson BO. Reconstruction and functional  
576 characterization of the human mitochondrial metabolic network based on  
577 proteomic and biochemical data. *J Biol Chem*. 2004;279:39532-39540
- 578 14. Thiele I, Price ND, Vo TD, Palsson BO. Candidate metabolic network states  
579 in human mitochondria. Impact of diabetes, ischemia, and diet. *J Biol Chem*.  
580 2005;280:11683-11695
- 581 15. Savinell JM, Palsson BO. Network analysis of intermediary metabolism using  
582 linear optimization. I. Development of mathematical formalism. *J Theor Biol*.  
583 1992;154:421-454
- 584 16. Ghosh A, Zhao H, Price ND. Genome-scale consequences of cofactor  
585 balancing in engineered pentose utilization pathways in *saccharomyces*  
586 *cerevisiae*. *PLoS ONE*. 2011;6:e27316
- 587 17. Varma A, Boesch BW, Palsson BO. Stoichiometric interpretation of  
588 *escherichia coli* glucose catabolism under various oxygenation rates. *Appl*  
589 *Environ Microbiol*. 1993;59:2465-2473
- 590 18. Mahadevan R, Schilling CH. The effects of alternate optimal solutions in  
591 constraint-based genome-scale metabolic models. *Metabolic engineering*.  
592 2003;5:264-276
- 593 19. Kaufman DE, Smith RL. Direction choice for accelerated convergence in hit-  
594 and-run sampling. *Operations Research*. 1998;46:84-95
- 595 20. Sabbah HN, Sharov VG, Goldstein S. Cell death, tissue hypoxia and the  
596 progression of heart failure. *Heart Fail Rev*. 2000;5:131-138

- 597 21. Martin D, Windsor J. From mountain to bedside: Understanding the clinical  
598 relevance of human acclimatisation to high-altitude hypoxia. *Postgrad Med J*.  
599 2008;84:622-627; quiz 626
- 600 22. Coats AJ. Anaemia and heart failure. *Heart*. 2004;90:977-979
- 601 23. Sharma R, Francis DP, Pitt B, Poole-Wilson PA, Coats AJS, Anker SD.  
602 Haemoglobin predicts survival in patients with chronic heart failure: A  
603 substudy of the elite ii trial. *European Heart Journal*. 2004;25:1021-1028
- 604 24. Go AS, Yang J, Ackerson LM, Lepper K, Robbins S, Massie BM, Shlipak  
605 MG. Hemoglobin level, chronic kidney disease, and the risks of death and  
606 hospitalization in adults with chronic heart failure: The anemia in chronic  
607 heart failure: Outcomes and resource utilization (anchor) study. *Circulation*.  
608 2006;113:2713-2723
- 609 25. Atamna H, Killilea DW, Killilea AN, Ames BN. Heme deficiency may be a  
610 factor in the mitochondrial and neuronal decay of aging. *Proc Natl Acad Sci U*  
611 *S A*. 2002;99:14807-14812
- 612 26. Schuler M, Bossy-Wetzel E, Goldstein JC, Fitzgerald P, Green DR. P53  
613 induces apoptosis by caspase activation through mitochondrial cytochrome c  
614 release. *Journal of Biological Chemistry*. 2000;275:7337-7342
- 615 27. Harten SK, Esteban MA, Maxwell PH. Identification of novel vhl regulated  
616 genes by transcriptomic analysis of rcc10 renal carcinoma cells. *Adv Enzyme*  
617 *Regul*. 2009;49:43-52
- 618 28. Scheuer J, Brachfeld N. Myocardial uptake and fractional distribution of  
619 palmitate-1 c14 by the ischemic dog heart. *Metabolism*. 1966;15:945-954

- 620 29. Chabowski A, Gorski J, Calles-Escandon J, Tandon NN, Bonen A. Hypoxia-  
621 induced fatty acid transporter translocation increases fatty acid transport and  
622 contributes to lipid accumulation in the heart. *FEBS Lett.* 2006;580:3617-3623
- 623 30. Kim JW, Tchernyshyov I, Semenza GL, Dang CV. Hif-1-mediated expression  
624 of pyruvate dehydrogenase kinase: A metabolic switch required for cellular  
625 adaptation to hypoxia. *Cell Metab.* 2006;3:177-185
- 626 31. Harris P, Gloster J. The effects of acute hypoxia on lipid synthesis in the rat  
627 heart. *Cardiology.* 1971;56:43-47
- 628 32. Cheng P, Hatch GM. Inhibition of cardiolipin biosynthesis in the hypoxic rat  
629 heart. *Lipids.* 1995;30:513-519
- 630 33. Aldenderfer M. Moving up in the world: Archaeologists seek to understand  
631 how and when people came to occupy the andean and tibetan plateaus. *Am Sci.*  
632 2003;91:542-529
- 633 34. Beall CM. Two routes to functional adaptation: Tibetan and andean high-  
634 altitude natives. *Proc Natl Acad Sci U S A.* 2007;104 Suppl 1:8655-8660
- 635 35. Heather LC, Cole MA, Tan JJ, Ambrose LJ, Pope S, Abd-Jamil AH, Carter  
636 EE, Dodd MS, Yeoh KK, Schofield CJ, Clarke K. Metabolic adaptation to  
637 chronic hypoxia in cardiac mitochondria. *Basic Res Cardiol.* 2012;107:268
- 638 36. Ashrafian H, O'Flaherty L, Adam J, Steeples V, Chung YL, East P,  
639 Vanharanta S, Lehtonen H, Nye E, Hatipoglu E, Miranda M, Howarth K,  
640 Shukla D, Troy H, Griffiths J, Spencer-Dene B, Yusuf M, Volpi E, Maxwell  
641 PH, Stamp G, Poulson R, Pugh CW, Costa B, Bardella C, Di Renzo MF,  
642 Kotlikoff MI, Launonen V, Aaltonen L, El-Bahrawy M, Tomlinson I, Pollard  
643 PJ. Expression profiling in progressive stages of fumarate-hydratase

- 644 deficiency: The contribution of metabolic changes to tumorigenesis. *Cancer*  
645 *Res.* 2010;70:9153-9165
- 646 37. Berg JM, Tymoczko JL, Stryer L. Glycolysis. *Biochemistry.* 2002.
- 647 38. Mora A, Davies AM, Bertrand L, Sharif I, Budas GR, Jovanovic S, Mouton V,  
648 Kahn CR, Lucocq JM, Gray GA, Jovanovic A, Alessi DR. Deficiency of pdk1  
649 in cardiac muscle results in heart failure and increased sensitivity to hypoxia.  
650 *EMBO J.* 2003;22:4666-4676
- 651 39. Papandreou I, Cairns RA, Fontana L, Lim AL, Denko NC. Hif-1 mediates  
652 adaptation to hypoxia by actively downregulating mitochondrial oxygen  
653 consumption. *Cell Metab.* 2006;3:187-197
- 654
- 655

**Table 1:** Nuclear genes encoding mitochondrial proteins: the twenty ‘most selected’ (i.e. smallest GWADS *p*-values) in Tibetan high-altitude natives

| <b>Entrez ID</b> | <b>Gene name</b> | <b>GWADS min P</b> | <b>Reaction</b> |
|------------------|------------------|--------------------|-----------------|
| 5230             | 'PGK1'           | 0.000427922        | 'PGK'           |
| 5211             | 'PFKL'           | 0.000562071        | 'PFK'           |
| 4696             | 'NDUFA3'         | 0.001056733        | 'NADH2-u10m'    |
| 34               | 'ACADM'          | 0.002100322        | All 'FAOX'      |
| 435              | 'ASL'            | 0.003329005        | 'ARGSL'         |
| 539              | 'ATP5O'          | 0.003329005        | 'ATPS4m'        |
| 27068            | 'PPA2'           | 0.004127063        | 'PPAm'          |
| 2937             | 'GSS'            | 0.004425362        | 'GTHS'          |
| 8170             | 'SLC14A2'        | 0.004892165        | 'UREAt'         |
| 4715             | 'NDUFB9'         | 0.005012697        | 'NADH2-u10m'    |
| 7991             | 'TUSC3'          | 0.005679664        | 'NADH2-u10m'    |
| 3145             | 'HMBS'           | 0.006801907        | 'HMBS'          |
| 10476            | 'ATP5H'          | 0.008432045        | 'ATPS4m'        |
| 4709             | 'NDUFB3'         | 0.00856278         | 'NADH2-u10m'    |
| 50               | 'ACO2'           | 0.008803353        | 'ACONTm'        |
| 2271             | 'FH'             | 0.008830507        | 'FUMm'          |
| 1350             | 'COX7C'          | 0.01011429         | 'CompIVr1'      |
| 4697             | 'NDUFA4'         | 0.01011429         | 'NADH2-u10m'    |
| 210              | 'ALAD'           | 0.010792961        | 'PPBNGS'        |
| 23761            | 'PISD'           | 0.011201573        | 'PSDm'          |

**Table 2:** Metabolites with the largest positive shadow prices when optimising the mitochondrial metabolic network for either haeme or ATP synthesis (and corresponding reactions)

| Optimize haeme synthesis |                     |                                    | Optimize ATP synthesis |                     |                                      |
|--------------------------|---------------------|------------------------------------|------------------------|---------------------|--------------------------------------|
| <i>Metabolite</i>        | <i>Shadow price</i> | <i>Reaction(s)</i>                 | <i>Metabolite</i>      | <i>Shadow price</i> | <i>Reaction(s)</i>                   |
| c204(c)                  | 1.30                | C204 (1)§, C204t (1)               | fdp(c)                 | 4                   | <b>PFK*</b> (1), FBA (2)             |
| c204coa(c)               | 1.30                | C204, C204CRN1 (1), C204CRN3 (1)   | f6p(c)                 | 3                   | <b>PFK*</b> , PGI (3)                |
| c204crn(c)               | 1.30                | C204CRN1, C204CRN2 (1)             | g6p(c)                 | 3                   | HEX1 (4), PGI, G6PI#                 |
| c204coa(m)               | 1.30                | C204CRN3, <b>FAOXC204*#</b>        | 13dpg(c)               | 2.20                | <b>PGK*</b> (5), GAPD (6)            |
| c204crn(m)               | 1.30                | C204CRN2, C204CRN3                 | c204coa(c)             | 2                   | C204 (7), C204CRN1 (8), C204CRN3 (9) |
| pheme(m)                 | 1.00                | FCLTm (6)                          | c204crn(c)             | 2.00                | C204CRN1, C204CRN2 (10)              |
| ppp9(m)                  | 1.00                | PPPGOm (6), FCLTm,                 | dhap(c)                | 2.00                | TPI (11), FBA, G3PDm (12)            |
| pppg9(c)                 | 0.86                | CPPPGO (8), PPPG9tm (8)            | g3p(c)                 | 2.00                | FBA, G3PATm (13), G3PDm, GAPD, TPI   |
| pppg9(m)                 | 0.86                | PPPG9tm, PPPGOm,                   | glc-D(c)               | 2.00                | GLCt1 (14), HEX1                     |
| cpppg3(c)                | 0.76                | CPPPGO, UPPDC1 (9)                 | c204coa(m)             | 2.00                | C204CRN3, <b>FAOX204*#</b>           |
| hmbil(c)                 | 0.76                | <b>HMBS*</b> (10), UPP3S (11)      | c204crn(m)             | 2.00                | C204CRN2, C204CRN3                   |
| uppg3(c)                 | 0.76                | UPP3S, UPPDC1                      | 2pg(c)                 | 1.19                | ENO, PGM,                            |
| ppbng(c)                 | 0.19                | <b>HMBS*</b> , <b>PPBNGS*</b> (12) | 3pg(c)                 | 1.19                | <b>PGK*</b> , PGM                    |
| 5aop(c)                  | 0.10                | <b>PPBNGS*</b> , 5AOPtm (13)       | pep(c)                 | 1.19                | PYK, CITt#                           |
| 5aop(m)                  | 0.10                | 5AOPtm, ALASm (14)                 | succoa(m)              | 0.81                | AKGDm, ALASm#, OCOAT1m#              |
| succoa(m)                | 0.10                | AKGDm (15), ALASm, OCOAT1m#        | akg(c)                 | 0.62                | ICDHxm (20), ICDHym#, TYRTAm#, AKGDm |
| 13dpg(c)                 | 0.05                | <b>PGK*</b> (16), GAPD (17)        |                        |                     |                                      |



|          |                 |                    |  |  |  |
|----------|-----------------|--------------------|--|--|--|
| 2pg(c)   | 0.0476<br>19048 | ENO, PGM,          |  |  |  |
| 13dpg(c) | 0.0476<br>19048 | <b>PGK*</b> , GAPD |  |  |  |

§Bracketed numbers are reaction rank based on metabolite shadow price

#Flux through this reaction was zero

\*Corresponding gene is one of the 'twenty most selected' in Table 1

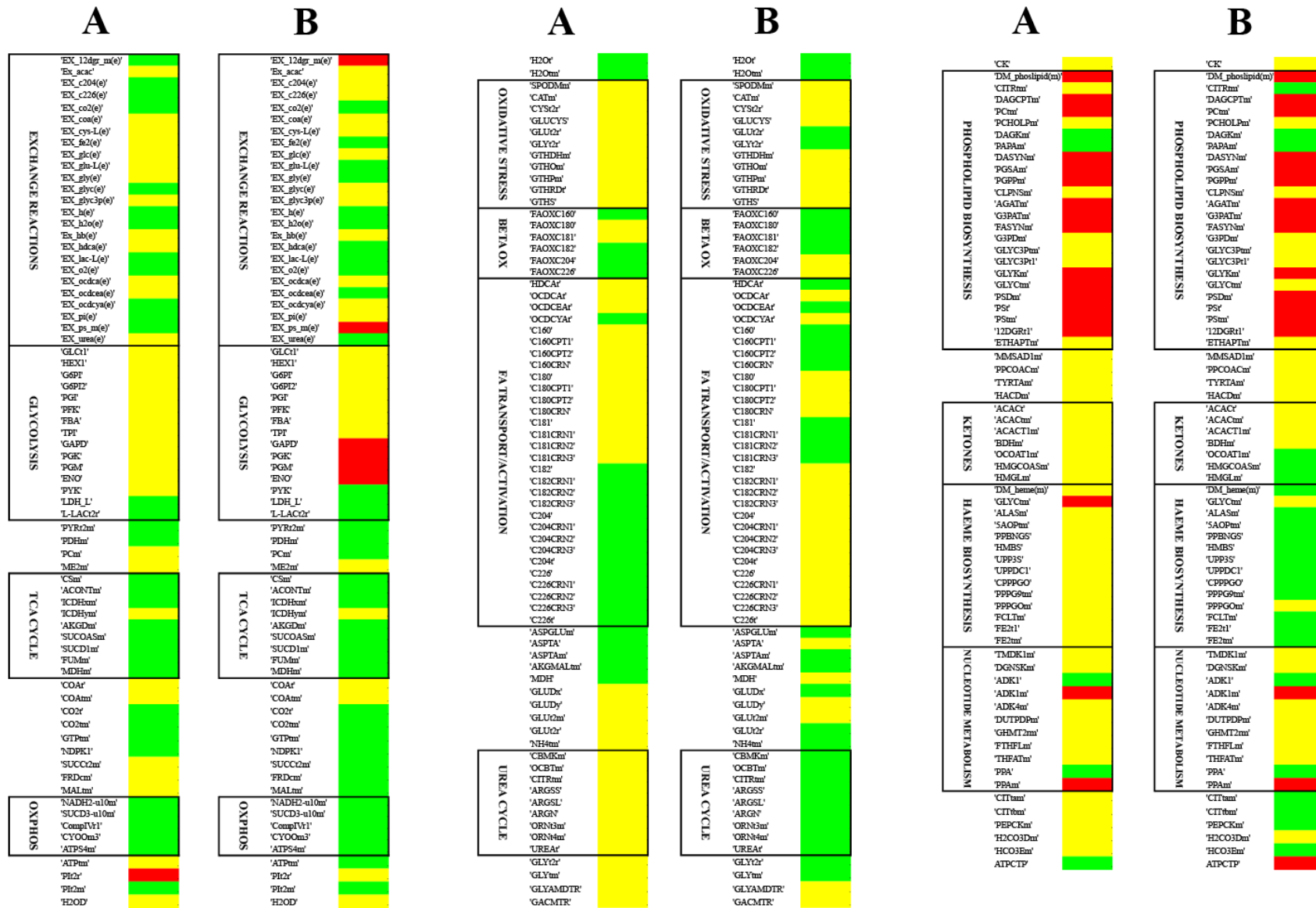
**Table 3:** Reactions with the smallest relative flux spans when optimising the mitochondrial metabolic network for either **a:** haeme synthesis or **b:** ATP synthesis

| <b>a. Optimize haeme synthesis<sup>#</sup></b> |   |      | <b>b. Optimize ATP synthesis</b> |   |      |
|--|---|------|----------------------------------|---|------|
| Reaction                                       | Relative flux span ( $\times 10^{-6}$ ) | Rank | Reaction                         | Relative flux span ( $\times 10^{-6}$ ) | Rank |
| <b>CompIVr1*</b>                               | 1.2                                     | 1    | ATPtm                            | 0.01                                    | 1    |
| CYOR-u10m                                      | 1.2                                     | 1    | <b>CompIVr1*</b>                 | 0.10                                    | 2    |
| <b>NADH2-u10m*</b>                             | 1.3                                     | 3    | CYOR-u10m                        | 0.10                                    | 3    |
| CPPPGO   | 1.4                                     | 3    | SUCOASm                          | 0.20                                    | 4    |
| FCLTm  | 1.4                                     | 3    | ENO                              | 0.21                                    | 5    |
| FE2t1  | 1.4                                     | 3    | GAPD                             | 0.21                                    | 6    |
| FE2tm  | 1.4                                     | 3    | <b>PGK*</b>                      | 0.21                                    | 7    |
| <b>HMBS*</b>                                   | 1.4                                     | 3    | PGM                              | 0.21                                    | 8    |
| PPPG9tm  | 1.4                                     | 3    | FBA                              | 0.21                                    | 9    |
| UPP3S  | 1.4                                     | 3    | GLCt1                            | 0.21                                    | 10   |
| UPPDC1   | 1.4                                     | 3    | HEX1                             | 0.21                                    | 11   |
| PPPGOm   | 1.4                                     | 3    | <b>PFK*</b>                      | 0.21                                    | 12   |
| 5AOPtm   | 1.4                                     | 3    | PGI                              | 0.21                                    | 13   |
| AKGDm  | 1.4                                     | 3    | TPI                              | 0.21                                    | 14   |
| ALASm  | 1.4                                     | 3    | <b>ACONTm*</b>                   | 0.22                                    | 15   |
| ASPGLUm  | 1.4                                     | 3    | AKGDm                            | 0.22                                    | 16   |
| ASPTAm   | 1.4                                     | 3    | CSm                              | 0.22                                    | 17   |
| GLYt2r   | 1.4                                     | 3    | ICDHxm                           | 0.22                                    | 18   |
| GLYtm  | 1.4                                     | 3    | <b>NADH2-u10m*</b>               | 0.27                                    | 19   |
| MDHm   | 1.4                                     | 3    | <b>FUMm*</b>                     | 0.29                                    | 20   |
| <b>PPBNGS*</b>                                 | 1.4                                     | 3    |                                  |   |      |

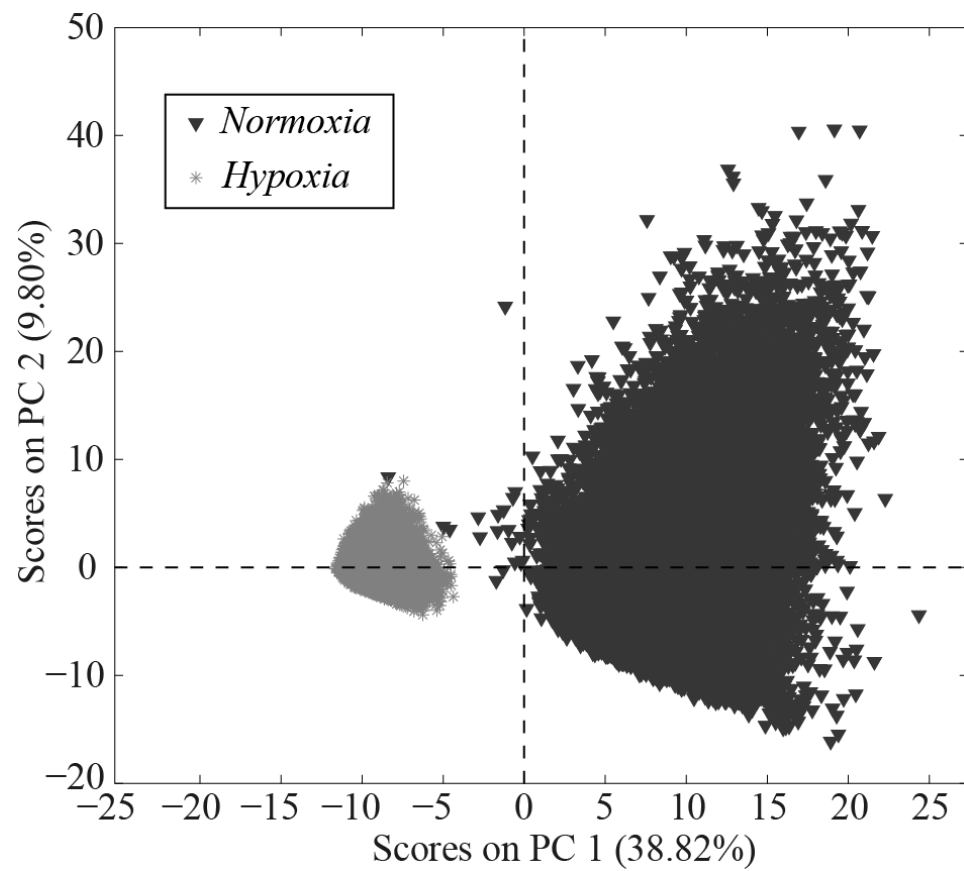
<sup>#</sup>21 reactions due to 'drawn ranking'

\*Corresponding gene is one of the 'twenty most selected' in Table 1

Constraint-based mitochondrial modelling, hypoxia and human genetics



**Figure 1:** Heatmap showing the effect of hypoxia on flux distribution in the mitochondrial metabolic network. Red = flux increased by  $> 0.1$  U; green = flux decreased by  $> 0.1$  U; yellow = flux changed by  $< 0.1$  U. **A:** Flux balance analysis, with ATP synthesis as the objective function. **B:** Uniform random sampling. ( $U = \mu\text{m min}^{-1} \text{g}^{-1}$ )



**Figure 2:** Biplot showing scores on principal component 1 vs. scores on principal component 2. Both components are from a five-component PCA model of data sampled in hypoxia and normoxia. Black triangles = normoxia; grey stars = hypoxia.