#### SULFHYDRYL OXIDATION-REDUCTION POTENTIALS DERIVED FROM THERMAL DATA

BY HENRY BORSOOK, EMORY L. ELLIS, AND HUGH M. HUFFMAN

(From the William G. Kerckhoff Laboratories of the Biological Sciences, California Institute of Technology, Pasadena)

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The isolation of glutathione by Hopkins in 1921 and his experiments suggesting that this compound is probably an intermediary in biological oxidations and reductions awakened an active interest in the biological significance of sulfhydryl compounds in general (1, 2). Among the fundamental data pertaining to these compounds are their oxidation-reduction potentials. Soon after the discovery of glutathione a number of attempts were made to measure these potentials by electrometric and colorimetric methods. In all except the most recent investigations the potential observed in aqueous solutions with noble metal electrodes was independent of the concentration of the oxidized form (R—S—S—R) (3–5). The data fitted an empirical electrode equation of the form

$$E = E_0 - \frac{RT}{F}$$
 pH  $- \frac{RT}{nF}$  ln (R—SH)

instead of an equation of similar form in which the last term is

$$\frac{RT}{nF} \ln \frac{(\mathrm{R-SH})^2}{\mathrm{R-S-S-R}}$$

Accordingly these potentials are not referable to the reaction

$$R \rightarrow S \rightarrow R + 2H^+ + 2(e) \rightleftharpoons 2R \rightarrow SH$$

whose characteristic potential was sought; and their quantitative significance will be obscure until the actual electrode reaction in each case is established.

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Whatever be the explanation for this behavior of sulfhydryl compounds *in vitro*, knowledge of the value of the free energy change (potential) for the, at least hypothetically, reversible system  $R-S-S-R + 2H^+ + 2e \rightleftharpoons 2R-SH$  is important because glutathione and cysteine are oxidized and reduced *in vivo* (6-8), by enzymes in the presence of suitable substrates (9, 10), without enzymes by certain tissue extracts (11), and by ascorbic acid (12).

The solution of this problem was undertaken in this laboratory by application of thermal data in conjunction with the third law of thermodynamics. For this method the substances under investigation must be obtained in a high degree of purity; and a relatively large quantity of material, about 40 gm., is required. For these reasons the substances studied first were cysteine, cystine,  $\beta$ -thiolactic acid, and its disulfide oxidation product  $\beta,\beta'$ -dithiodilactic acid. The values obtained give some indication of the probable order of magnitude of the free energy change for the corresponding glutathione system. The preparation of oxidized and reduced glutathione in a sufficiently high degree of purity is in progress. When these preparations are completed, direct measurements on these substances will be made.

The great advantage offered by reliable thermal data in the computation of free energy changes, which may be expressed as equilibrium constants or oxidation-reduction potentials, is that the chemical reaction is precisely defined. In the case of equilibrium studies, especially where these involve electrode potential measurements, the actual reaction which occurs is often only guessed at. For these reasons the thermal data yield the final reference values.

Observations have been published recently from two different laboratories which leave little room for doubt that the potentials observed are those of thermodynamically reversible systems of which R—SH and R—S—S—R compounds are among the components. One group of workers, Ghosh *et al.* (13), employed an electrometric method; the other, Fruton and Clarke (14), a colorimetric method. The values obtained by these two methods for apparently the same system, *e.g.* cystine-cysteine, nevertheless are widely different and far beyond the probable experimental error. The thermal data presented below indicate that it is im-

		Standa	vrd state		In	aqueous solution	r
	Entropy of formation, $\Delta S^0$	Heat of com- bustion at constant pressure	Heat of formation, $\Delta H^0$	Free energy of formation, $\Delta F^0$	Solubility	$\frac{RT \ln}{N(\text{saturated})}$	$\Delta F$ (1 m)
			At 25°				
	entropy units per mole	calories per mole	calories per mole	calories per mole	mole per 1000 gm. water	calories per mole	calories per mole
<i>l</i> -Cysteine (solid)	-152.3	532,200	-127,880	-82,480	0.229	-870	-81,610
<i>l</i> -Cystine "	-286.1	997, 770	-251,920	-166,630	0.000456	-4550	-162,080
Thiolactic acid (liquid)	- 66 -	511,300	-112,140	-82,420	Miscible in	+2390	-84,810
					all pro- portions		
β,β'-Dithiodilactic acid (solid)	-212.0	946,520	-232,150	-168,950	0.00639	-3050	-65,900
			At 37°				
<i>l</i> -Cysteine				-80,650 -163,200	$0.404 \\ 0.000671$	-550 -4490	-80,110 -158,710

TABLE I

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probable that the chemical reaction whose potential was measured was in either case simply

Cystine + 
$$2H^+$$
 +  $2(e) \rightleftharpoons 2$  cysteine

Free Energy of Formation in Standard State—It is unnecessary here to present in detail the method of calculating equilibrium constants from thermal data. The general principles and the details of their application have been described in previous communications (15–17). The data necessary for calculating equilibria in aqueous solution are specific heats for the entropy values, heats of combustion for  $\Delta H$ , solubilities, ionization constants, and activity coefficients.

These data for the four compounds studied, except their ionization constants and activity coefficients, are given in Table I. The details of the preparation and purification of these compounds and of the thermal data are given elsewhere (18). The values for the heats and free energies of formation in the standard state given in Table I are slightly modified from the figures in our previous communication because of a change in the value of the heat of combustion of benzoic acid. The free energy values in the standard state at 37° for cysteine and cystine were calculated from the 25° values by means of the van't Hoff equation, which in its integrated form, on the assumption that  $\Delta H$  is constant over a short temperature interval, is

$$\frac{\Delta F_2}{T_2} - \frac{\Delta F_1}{T_1} = -\Delta H\left(\frac{T_2 - T_1}{T_1 T_2}\right) \tag{1}$$

Free Energies of Formation of Neutral Forms in Aqueous Solution—From this point on the calculation of the free energy changes in solutions at all hydrogen ion concentrations becomes complicated. In order to keep the direction clear we shall anticipate data on the ionization constants in Table III to obtain the values for the free energies of formation of the neutral forms in solution.

The free energy of formation in aqueous solution is given by the equation

$$\Delta F(1 \text{ M}) = \Delta F^{0} - RT \ln \frac{N(\text{saturated solution})}{N(m=1)}$$
(2)

where N (saturated solution) is the mole fraction in the saturated solution, and N (m = 1) is the mole fraction when 1 mole of the substance is dissolved in 1000 gm. of water. Mole fraction is defined by the equation  $m_1/(m_1 + m_2)$  where  $m_1$  and  $m_2$  are the numbers of moles of solute and solvent respectively. In the cases of the two this acids the complication is encountered that a fraction of the material in the saturated solution is in the ionized form. The treatment of this complication is discussed below.

The values for the solubility of *l*-cystine in Table I are taken from the data of Dalton and Schmidt (19). The solubilities of the two remaining compounds were determined by means of a technique similar to that employed by these authors. Solubility tubes were shaken in an air bath at the temperature indicated for 48 to 72 hours, after which the solution was filtered at the temperature of the bath. The quantity of solid in a weighed quantity of solution was determined by evaporating the solution to dryness at 85–90°. Preliminary experiments showed that the two substances studied could be recovered quantitatively from their solutions by this method. In the case of *l*-cysteine the tubes containing the amino acid were half filled with freshly boiled water and the air was displaced by hydrogen to prevent oxidation during the period of shaking. The figures given in Table I are averages of a number of separate experiments in which the extremes differed by less than 6 per cent. This uncertainty is negligible in the calculation of the free energy of formation of the substance in solution.

In the saturated solutions all the substances undergo some ionization. In order to compute the free energy of formation in solution of any particular form this must be taken into account. The details of this calculation for cysteine are presented to illustrate the general method applicable to weak acids, amino acids, and weak bases, whether mono- or polyvalent. Proceeding from highly acid to highly alkaline solutions the ionic forms of cysteine will be designated as  $R^+$ ,  $R^\pm$ ,  $R^-$ , and  $R^-$ . In the saturated solution

$$(R^+) + (H^+) = (OH^-) + (R^-) + 2(R^-)$$
 (3)

le equilibrium expressions for the various forms are

$$\frac{(\mathbf{R}^{\pm}) \ (\mathbf{H}^{+})}{(\mathbf{R}^{+})} = K_{1}; \quad \frac{(\mathbf{R}^{-}) \ (\mathbf{H}^{+})}{(\mathbf{R}^{\pm})} = K_{2}; \quad \frac{(\mathbf{R}^{-}) \ (\mathbf{H}^{+})}{(\mathbf{R}^{-})} = K_{3}$$

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If the total concentration of cysteine in all forms is designated as C, from the above relations,

$$C = (\mathbf{R}^{\pm}) \left( \frac{(\mathbf{H}^{+})^{3} + K_{1}(\mathbf{H}^{+})^{2} + K_{1}K_{2}(\mathbf{H}^{+}) + K_{1}K_{2}K_{3}}{K_{1}(\mathbf{H}^{+})^{2}} \right)$$
(4)

From Equation 3 and the equilibrium relations

$$(\mathrm{H}^{+}) = \frac{K_{w}}{(\mathrm{H}^{+})} + (\mathrm{R}^{\pm}) \left( \frac{-(\mathrm{H}^{+})^{3} + K_{1}K_{2}(\mathrm{H}^{+}) + 2K_{1}K_{2}K_{3}}{K_{1}(\mathrm{H}^{+})^{2}} \right)$$
$$= \frac{K_{w}}{(\mathrm{H}^{+})} + C \left( \frac{-(\mathrm{H}^{+})^{3} + K_{1}K_{2}(\mathrm{H}^{+}) + 2K_{1}K_{2}K_{3}}{(\mathrm{H}^{+})^{2} + K_{1}K_{2}(\mathrm{H}^{+}) + K_{1}K_{2}K_{3}} \right)$$
(5)

At 25°, C is 2.29  $\times$  10<sup>-1</sup>; and from Table III the values of  $K_1$ ,  $K_2$ , and  $K_3$  are 1.95  $\times$  10<sup>-2</sup>, 4.57  $\times$  10<sup>-9</sup>, and 1.66  $\times$  10<sup>-11</sup> respectively.

Equation 5 is simplified by substituting the limits of the possible values of  $(H^+)$  and eliminating the negligible terms. Through the range from pH 4 to 8, Equation 3 becomes

$$(\mathrm{H}^{+}) = \frac{K_{w}}{(\mathrm{H}^{+})} + C\left(\frac{K_{1}K_{2} - (\mathrm{H}^{+})^{2}}{K_{1}K_{2} + K_{1}(\mathrm{H}^{+})}\right)$$
(6)

From Equation 6 it is seen that  $(H^+)^2$  must be less than  $K_1K_2$ . With  $10^{-5.5}$  and  $10^{-6.0}$  for  $(H^+)$  the drift of the disagreement between the left- and right-hand sides of Equation 4 shows that the value of  $(H^+)$  which will satisfy this equation lies between  $10^{-5.0}$  and  $10^{-5.5}$ . In this case  $K_1K_2$  in the denominator is negligible compared with  $K_1(H^+)$ . With this elimination the value of  $(H^+)$  becomes  $10^{-5.04}$ . On substituting this value into Equation 4 it is found that practically all of the amino acid in the saturated aqueous solution is in the zwitter ionic form. The same is true for cystine.

 $\beta$ -Thiolactic acid is miscible with water in all proportions. The hydrogen ion concentration and the degree of ionization will depend upon the concentration of the acid. However, at 1 M less than 1 per cent is ionized. For the calculation of the free energy of solution we may assume that all the acid, both when the concentration of water is 0 and when the acid is at 1 M concentration in water, is in the neutral form. The calculated pH of the saturated aqueous solution of  $\beta$ , $\beta'$ -dithiodilactic acid is approximately 3.16, corresponding to ionization of 11 per cent of the acid. In computing the free energy of solution the mole fraction of the saturated solution  $N_s$  was multiplied by the fraction of the material which is present in the neutral form  $\alpha$ , here 0.89. The term for the free energy of the solution becomes

$$RT \ln \frac{N(\text{saturated solution})}{N(m=1)} \alpha$$

In the cases of the three other substances the value of  $\alpha$  is 1. In computing the free energy of solution of substances miscible with water in all proportions, as in the case here of  $\beta$ -thiolactic acid, the term for N(saturated solution) = 1.

Table I gives the values of  $\Delta F(1 \text{ m})$  at 25° for the four substances, and at 37° for cysteine and cystine.

Ionization Constants and Activity Coefficients-In order to express the free energy changes at all hydrogen ion concentrations in a useful form, *i.e.* in terms of the total concentrations of oxidant and reductant, the ionization constants of these substances must be known. Where they may take the form of polyvalent ions, it is better to attempt an approximate determination of the thermodynamic ionization constants rather than to leave them in the form of titration constants. Otherwise systematic differences may appear between the observed and theoretical oxidationreduction potentials at different hydrogen ion concentrations (15, 16), because in the usual experimental solutions, e.g. where buffers are used, the ionic strength may be quite high, and will be different at different hydrogen ion concentrations. As a result the corrections for activity coefficients are large, they may be different for oxidant and reductant, and will vary at different pH values of the experimental solutions.

Accordingly we have attempted estimation of the thermodynamic ionization constants of the four substances studied here. These estimations are based on electrometric titrations, except in the case of cystine. For this substance solubility data were used. In the electrometric titrations the hydrogen electrode against a saturated calomel cell was employed for cysteine and  $\beta$ -thiolactic acid, the glass electrode for  $\beta,\beta'$ -dithiodilactic acid. With cysteine one titration was made with platinized asbestos suspended in the solution, and with  $\beta$ -thiolactic acid colloidal platinum, to minimize oxidation of the sulfhydryl group during the titration. The values obtained were the same as when this precautionary measure was omitted.

In every case complications arising from overlapping ionization of these polyvalent compounds are encountered. The procedure with cysteine will again be chosen to illustrate the general method employed in deriving the individual titration and thermodynamic ionization constants. The calculations are long and laborious, particularly for the ionization in alkaline solutions. In order to facilitate following the development a few examples of actual data are given in Table II.

JaOH ,dded	Volume of solution	Con- centra- tion of added NaOH	pH	$A_{\mathbf{H}^+}$	Total concen- tration of cysteine in all	Appro tratio of est str	ximate cons for put timating ength, $\mu$	oncen- irpose ionic , of	nic strength, u	$w \times \gamma_{\mathrm{H}^+}^{*}$ $v \times 10^{-14}$	$I^{+} = \gamma_{-}$
				{	forms	(R±)	(R-)	(R=)	0	× ×	~
(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)	(10)	(11)	(12)
cc.	cc.	mole per l.		mole per l.	mole per l.	mole per l.	mole per l.	mole per l.			
2.00	27.00	0.005739	7.35	$4.467 \times 10^{-8}$	0.0500	0.0435	0.00650	0	0.0057	1.106	0.92
5.00	30,00	0.01292	7.895	$1.274 \times 10^{-8}$	0.0450	0.02925	0.01575	0	0.0129	1.127	0.895
15.04	40.04	0.02913	9.03	$9.376 \times 10^{-10}$	0.03375	0.004388	0.02835	0.00101	0.0298	1.180	0.85
19.04	44.04	0.03353	9.70	$1.977 \times 10^{-10}$	0.03068	0.000920	0.0255	0.00491	0.0367	1.199	0.84
25.06	50.06	0.03876	10.41	$3.882 \times 10^{-11}$	0.02696	0.000135	0.0140	0.0129	0.0480	1.224	0.83
31.10	56.1	0.04295	10.95	$1.117 \times 10^{-11}$	0.02406		0.00529	0.0188	0.0556	1.238	0.83
	•				,	1					

Calculation of Ionization Constants of l-Cyste

TA:

0.1635 gm. of cysteine dissolved in 25 cc. of water; NaOH = 0.07748 N, 25°. pK<sub>2</sub> =  $-\log \gamma_{=} = (0.5 \times 3.3 \sqrt{\mu})/(1 + 0.33 \sqrt{\mu})$ .

The ionization relations of cysteine may be written as follows:

$$\frac{(\mathbf{R}^{\pm})(\mathbf{H}^{+})}{(\mathbf{R}^{+})\gamma_{+}} = K_{1}; \quad \frac{(\mathbf{R}^{-})(\gamma_{-})(\mathbf{H}^{+})}{\mathbf{R}^{\pm}} = K_{2}; \quad \frac{(\mathbf{R}^{-})(\gamma_{-})(\mathbf{H}^{+})}{(\mathbf{R}^{-})(\gamma_{-})} = K_{3}$$

 $R^+$  is the form in acid solution in which the ionization of the carboxyl group is suppressed,  $R^\pm$  the zwitter ion,  $R^-$  the form in which presumably the ionization of the amino group is suppressed, and  $R^=$  the form in which the sulfhydryl group is ionized.  $\gamma_+$ ,  $\gamma_-$ , and  $\gamma_-$  are the corresponding activity coefficients.

In all these computations the activity coefficient of the zwitter ion or neutral molecule in the case of the thio acids was taken as unity. The observations of Harned and Owen (20) on acetic acid and glycine (21) and of Pfeiffer and Würgler (22) and of Cohn (23) on the solubility of amino acids in salt solutions indicate that at the concentration of amino acids and salts in our solutions little error was incurred by this assumption.

The first dissociation constant  $pK_1$  is given by the expression

$$pK_1 = pH + \log (R^+) + \log \gamma_+ - \log (R^\pm)$$

 $(\mathbf{R}^+)$  was taken as the difference between the concentration of hydrochloric acid added and the concentration of hydrogen ions in the solution. The latter quantity is the antilog of the nega-

BLE II ine on Alkaline Side of Neutrality;  $pK_2$  and  $pK_3$ 

$M_{OH} = \frac{(11)}{(5)}$	Bound $(Na) = (3) - (13)$	$ (\mathbf{R}^{\pm}) = (6) - (17) - (21) $	$-\log{(R^{\pm})}$	(R-)	$-\log (R^{-})$	$-\log \gamma_{-} = -\log (12)$	$ \begin{array}{c} \mathbf{p}\mathbf{K}_2 = (4) + \\ \mathbf{n}_1 \\ \mathbf{n}_2 \\ - (16) \end{array} $	$(\mathbf{R}^{=}) = (6) - (17) - (17)$	$-\log(R^{=}) = -\log(21)$	-log γ=	$p \mathbf{K}_3 = \begin{pmatrix} 4 \\ (22) + (23) - \\ (18) - (19) \end{pmatrix}$
(13)	(14)	(15)	(16)	(17)	(18)	(19)	(20)	(21)	(22)	(23)	(24)
mole per l.	mole per l.	mole per l.		mole per l.				mole per l.			
$2.476  imes 10^{-7} \\ 8.948  imes 10^{-7} \\ 1.258  imes 10^{-5}$	0.005738 0.01291 0.02912	0.04426 0.03209 0.00545	$1.354 \\ 1.494 \\ 2.264$	0.005738 0.01291 0.02747	2.241 1.889 1.561	0.036 0.048 0.069	8.27 8.34 8.39				
$6.065 \times 10^{-5}$ $3.153 \times 10^{-4}$ $1.198 \times 10^{-3}$	0.03347 0.03844 0.04175			$\begin{array}{c} 0.02654 \\ 0.01541 \\ 0.00628 \end{array}$	1.576 1.812 2.202	0.074 0.079 0.083		0.00371 0.01149 0.01778	2.431 1.940 1.750	0.298 0.337 0.361	10.78 10.80 10.78

 $\mathrm{pH} - \log(\mathrm{R}^-) - \log \gamma_- + \log(\mathrm{R}^\pm), \quad \mathrm{pK}_3 = \mathrm{pH} - \log(\mathrm{R}^=) - \log \gamma_- - \log(\mathrm{R}^-) - \log \gamma_-$ 

tive of the pH observed,  $A_{\rm H}$ , divided by the activity coefficient of the hydrogen ion in the given solution.

The hydrogen ion activity coefficients at different ionic strengths were calculated from the data of Harned and Hamer (24) on the activity of HCl in KCl solutions, and of Spencer (25) of KCl in aqueous solutions at  $25^{\circ}$  by means of the following equations.

$$\begin{split} \gamma_{\mathrm{HCl}^{2}} &= \gamma_{\mathrm{H}^{+}} \times \gamma_{\mathrm{Cl}^{-}} \\ \gamma_{\mathrm{KCl}^{2}} &= \gamma_{\mathrm{K}^{+}} \times \gamma_{\mathrm{Cl}^{-}} \end{split}$$

The assumption was made that in these dilute solutions  $\gamma_{\mathrm{K}^+} = \gamma_{\mathrm{Cl}^-}$ . Then  $\gamma_{\mathrm{KCl}} = \gamma_{\mathrm{Cl}^-}$  and  $\gamma_{\mathrm{HCl}^2} = \gamma_{\mathrm{H}^+} \times \gamma_{\mathrm{KCl}}$ ;  $\gamma_{\mathrm{H}^+} = \gamma_{\mathrm{HCl}^2}/\gamma_{\mathrm{KCl}}$ . The values so obtained were preferred to those given by the empirical equations of Larsson and Adell (26) and of Bjerrum and Unmack (27).

The difference between the total concentration of amino acid present and the concentration of bound acid is  $(\mathbf{R}^{\pm})$ , the concentration of the zwitter ion.

The activity coefficients of the monovalent cation and anion of the amino acids or thio acids were taken to be the same as those of the hydrogen ion.

In the calculation of the basic dissociation constants it was assumed that the salts of the amino acids and thio acids were completely dissociated. The amount of salt present was calculated from the bound base which was obtained by subtracting the concentration of hydroxyl ions,  $M_{\rm OH^-}$ , from the concentration of NaOH added.  $M_{\rm OH^-}$  was computed from the observed pH as follows:

$$K_{w} = \frac{\gamma_{\mathrm{H}^{+}} \times \gamma_{\mathrm{OH}^{-}}}{A_{\mathrm{H}_{2}\mathrm{O}}} \times M_{\mathrm{H}^{+}} \times M_{\mathrm{OH}^{-}} = \gamma_{w} \times M_{\mathrm{H}^{+}} \times M_{\mathrm{OH}^{-}}$$
$$M_{\mathrm{H}} = \frac{A_{\mathrm{H}^{+}}}{\gamma_{\mathrm{H}^{+}}}; \quad M_{\mathrm{OH}^{-}} = \frac{K_{w}}{\gamma_{w}} \times \frac{\gamma_{\mathrm{H}^{+}}}{A_{\mathrm{H}^{+}}}$$
(7)

 $K_w$  and  $\gamma_w$  at different ionic strengths were determined by Harned and Hamer (24);  $A_{\rm H^+}$  is the antilog of the negative of the pH observed; and  $\gamma_{\rm H^+}$  was calculated as described above. (B) –  $M_{\rm OH^-}$ , where (B) is the concentration of added base, is the bound base.

The bound base is divided between  $\mathbb{R}^-$  and  $\mathbb{R}^=$ . To determine the partition the approximate concentration of  $\mathbb{R}^=$  was computed from the titration constants,  $K'_2$  and  $K'_3$ , taken by inspection from the titration curve, for the first part of the alkaline titration where ( $\mathbb{R}^=$ ) is very low. The bound base minus  $2(\mathbb{R}^-)$  gives ( $\mathbb{R}^-$ ), the concentration of  $\mathbb{R}^-$ . The total concentration of amino acid minus ( $\mathbb{R}^-$ ) and ( $\mathbb{R}^=$ ) gives ( $\mathbb{R}^{\pm}$ ), the concentration of zwitter ion. At the highly alkaline end of the titration curve ( $\mathbb{R}^{\pm}$ ) was calculated by means of  $K'_2$  and  $K'_3$ . The calculated quantity at each pH was subtracted from the total concentration of amino acid present. The difference between the total bound base and this quantity divided by 2 gives  $(R^{=})$ . The total bound base minus  $(R^{\pm})$  minus  $2(R^{=})$  gives  $(R^{-})$ .

The following are the equations for computing  $(R^{\pm})$  and  $(R^{=})$ 

$$\mathbf{R}^{\pm} = C \left( \frac{(\mathbf{H}^{+})^{2}}{(\mathbf{H}^{+})^{2} + K_{2}(\mathbf{H}^{+}) + K_{2}K_{3}} \right)$$

and

$$\mathbf{R}^{-} = C \left( \frac{K_2 K_3}{(\mathbf{H}^+)^2 + K_2 (\mathbf{H}^+) + K_2 K_3} \right)$$

where C is the total concentration of amino acid.

The titration constants were also used to compute the approximate ionic strength at each stage in the titration in order to obtain the activity coefficients of the different ions. For the activity coefficients of the divalent ions the following modified Debye-Hückel equation was employed.

$$-\log \gamma_{-} = \frac{(0.5) (3.3) \sqrt{\mu}}{1 + 0.33 \sqrt{\mu}}$$
(8)

3.3 instead of 4 was used in the numerator to allow for the distance between the charges in the divalent ion (28). Similarly, in assessing the contribution of the divalent ion to the ionic strength  $3.3(R^{=})$  instead of  $4(R^{=})$  was taken.

With these values for  $(\mathbb{R}^{\pm})$ ,  $(\mathbb{R}^{-})$ , and  $(\mathbb{R}^{=})$ , and their corresponding activity coefficients tentative values for  $K_2$  and  $K_3$  were obtained from the beginning and end of the titration curve. These values and correspondingly adjusted activity coefficients were used for recalculation of  $(\mathbb{R}^{=})$  and  $(\mathbb{R}^{\pm})$  at the initial and terminal stages of the titration. By this process of successive approximation values of  $(\mathbb{R}^{\pm})$ ,  $(\mathbb{R}^{-})$ , and  $(\mathbb{R}^{-})$  were obtained for final values of  $K_2$  and  $K_3$ .

The above treatment of the titration data did not give a constant value for  $pK_2$ . The value obtained increased with increasing pH. At pH 7.0  $pK_2$  found was 8.22, at pH 8.0, 8.33, and at pH 9.0, 8.37. This drift was independent of the ionic strength, identical values being obtained at the same pH over 10-fold variation in ionic strength. The excellent agreement of the  $pK_3$ values over a wide range of ionic strengths (Table III) also shows TABLE III

Ionization Constants at 25° of l-Cysteine, l-Cystine,  $\beta$ -Thiolactic Acid, and  $\beta$ , $\beta'$ -Dithiodilactic Acid

Concen-	Ionic	Ac	tivity coef	ficients us	ed	I	onization	n constan	ts
substance	$\mu$	γ++	$\begin{vmatrix} \gamma_{\pm+} \text{ or} \\ \gamma_{+} \end{vmatrix}$	$\begin{vmatrix} \gamma_{\pm-} \text{ or} \\ \gamma_{-} \end{vmatrix}$	γ=	pK1	pK2	pK3	pK4
				l-Cyster	ine				
mole per l.									
0.015	0.034		0.85			1.70			
0.028	0.175		0.77			1.71		1	
0.042	0.017			0.88			8.34		
0.031	0.182			0.77			8.33		
0.028	0.045			0.835	0.47			10.78	
0.019	0.158			0.77	0.26			10.78	
Averag Titrati centr Knig	ce value on cons cation ht (29).	taken stants, 0.02 M	pK', s	at 30°, Cannan	con- and	1.71	8.33 8.18	10.78 10.28	
·			BURLIN.	l-Cystic	re				,
0.00000	0.01	0.60	10.01	1		0.06.	2 00		
0.0019	0.02	0.60	0.88			1.08	2.03		
0.014	0.11	0.32	0.80			1.00	2.05		
0.0022	0.005	0.0-	0.00	0.92		1.00		8 00	
0.00099	0.10			0.80				8.01	
0.0036	0.01			0.91	0.69			7.99	10.26
0.0069	0.02			0.88	0.60			7.96	10.23
Averag Titrati Sano	e value on con (30)	taken stants,	рК',	at 25	°, of	1.04 1.60	2.05 2.21	8.00 7.86	10.25 9.85
tratio	on cons on 0.02 M	ants, p 4, of Ca	nnan ar	d Knig	ncen- ht	<1.0	1.7	7.48	9.02
• · · · · ·			<i>β</i> -T	hiolacti	e acid				
0.047	0.028		0.86	0.825		4.32	10.45		
0.029	0.059						10.47		
			$\beta, \beta'$ -Di	thiodila	ctic ac	id			
0.0030	0.0046	0.78					4.99		
0.0031	0.0056	0.91				4.08			

that the drift cannot be ascribed to the use of incorrect activity coefficients. Further, at these low hydroxyl ion concentrations assumptions regarding the activity coefficient of the hydroxyl ion, or of the divalent anion, are negligible. The only reasonable explanation which suggests itself to us is association of the zwitter ion, increasing with increasing pH. If this explanation be correct the curve of pK<sub>2</sub> against pH indicates that the true value is in the neighborhood of 8.1. The pK<sub>2</sub> value chosen, 8.33, is that obtained in the mid-region of the titration curve of this group, between pH 8.0 and 8.4. The only titration data in the literature reported in sufficient detail to permit recalculation of the dissociation constants with suitable activity coefficients, those of Tague (31) for glycine and phenylalanine, show no evidence of such a drift in the ionization of the amino group as we have observed with cysteine. The data reported by Cannan and Knight (29) for cysteine at 0.1 M concentration at 30° are insufficient for the estimation of whether this drift was present in their titrations or not.

In the case of  $\beta$ -thiolactic acid the calculations are simpler because there are only two ionizable groups with widely separated constants.

In  $\beta$ , $\beta'$ -dithiodilactic acid there are two overlapping dissociation constants in the acid region. The same procedure as in the case of the overlapping basic dissociation constants of cysteine was employed, the concentration of bound acid being used instead of bound base.

The solubility data of Sano (30) were used for the calculation of the four constants of cystine, each pair overlapping. It was assumed that over the whole range from pH 0.83 to 9.58 the concentration of the zwitter ion was the same and equal to the minimum solubility, 0.000457 mole per liter observed by Sano. It is implied in this assumption that the activity coefficient of the zwitter ion is unity throughout. If this minimum solubility, *i.e.* ( $\mathbb{R}^{\pm\pm}$ ), is represented by  $\lambda$ , the four equilibrium expressions are

$$\frac{\gamma_{\pm-}(\mathbf{R}^{\pm-})(\mathbf{H}^{+})}{\gamma_{++}(\mathbf{R}^{++})} = K_{1}; \quad \frac{\lambda(\mathbf{H}^{+})}{\gamma_{\pm+}(\mathbf{R}^{\pm+})} = K_{2}; \quad \frac{\gamma_{\pm-}(\mathbf{R}^{\pm-})}{\lambda} = K_{3};$$
$$\frac{\gamma_{\pm}(\mathbf{R}^{\pm})(\mathbf{H}^{+})}{\gamma_{\pm-}(\mathbf{R}^{\pm-})} = K_{4}$$

where (H<sup>+</sup>) represents the hydrogen ion activity. In acid solutions the concentration of the divalent cation, (R<sup>++</sup>), is given by the expression  $\lambda(H^+)^2/K_1K_2 \gamma_{++}$  and in alkaline solutions the concentration of the divalent anion R<sup>=</sup> by  $\lambda K_3 K_4/(H^+)^2 \gamma_{-}$ .

Sano used a series of buffers for his solubility measurements at different hydrogen ion concentrations, with the result that the ionic strengths ranged, in the acid series, from 0.01 to 0.35, and, in the alkaline series, from 0.005 to 0.115. The calculated activity coefficients of the divalent ions varied accordingly from 0.69 to 0.15 in the acid range and from 0.92 to 0.28 in the alkaline range. For this reason the equilibrium constants involving the divalent

			$T_{A1}$	BLE	11				
Calculated	and	Observed	Solubility	of	Cystine	at	Different	Hydrogen	Ion
		Concentr	rations, in	Bu	ffer Solu	tion	ıs at 25°		

			Calculated from	ionization constants
pH	Ionic strength, $\mu$	Observed by Sano (30)	Of Sano	In Table III and activity coefficients
		mole per l.	mole per l.	mole per l.
7.52	0.10	0.000689	0.000664	0.000645
7.98	0.10	0.000985	0.00107	0.000994
8.55	0.005	0.00222	0.00280	0.00226
8.78	0.01	0.00363	0.00457	0.00363
9.05	0.02	0.00687	0.00864	0.00684
9.85	0.115	0.0521	0.0898	0.00473

cation and anion,  $K_1$  and  $K_4$ , are less trustworthy than  $K_2$  and  $K_3$ .

The four ionization constants were estimated by successive approximation, as in the case of the overlapping ionizing groups of cysteine. The same assumptions were made regarding activity coefficients. The differences between the pK values in Table III for cystine and those deduced by Sano from the same data are mostly to be ascribed to our introduction of activity coefficients, and to some extent to different weighting of the individual values. Table IV shows that a closer agreement is thus obtained between observed and calculated solubility at different hydrogen ion concentrations than with the constants given by Sano. These figures are presented because the interpretation given certain experimentally observed potentials for the cystine  $\rightleftharpoons$  cysteine

system, discussed below, depends on the accuracy of the calculated solubility of cystine in the experimental solutions.

In Table III are collected the values for the ionization constants obtained at the extremes of ionic strengths. The averages given are of a considerably larger number of determinations than those shown. The titration constants of Cannan and Knight and of Sano are given for comparison. The agreement in the calculated ionization constants even where there were large differences in activity coefficients shows that the values used for these are nearly correct or that the errors are compensatory.

Oxidation-Reduction Potentials of Cystine  $\Rightarrow$  Cysteine—With these data we can now proceed to the calculation of the oxidationreduction potentials at different hydrogen ion concentrations of cystine  $\Rightarrow$  cysteine and of the  $\beta$ , $\beta'$ -dithiodilactic acid  $\Rightarrow$  thiolactic acid systems. In both systems the reaction mechanisms postulated are between the neutral molecules. The calculated potential at any given hydrogen ion concentration is independent of the mechanism postulated. Our method of developing electrode potential equations to be used in conjunction with thermal data has been described in detail in previous communications (15, 17). We shall present here only the final equations.

For the postulated reaction

Cystine<sup>±±</sup> + 2(H<sup>+</sup>) + 2(e) 
$$\rightleftharpoons$$
 2 cysteine<sup>±</sup>

the electrode potential equation is

$$E_{\rm obs.} = \tilde{E} - \frac{RT}{2f} \ln \frac{({
m R}-{
m SH})^2}{({
m R}-{
m S}-{
m R}-{
m R})} - \frac{RT}{2f} \ln \frac{(K_1^{
m SH})^2}{K_1^{
m SS}K_2^{
m SS}}$$

 $-\frac{RT}{2f}\ln\frac{(\mathrm{H}^+)^4+K_1^{\mathrm{SS}}(\mathrm{H}^+)^3+K_1^{\mathrm{SS}}K_2^{\mathrm{SS}}(\mathrm{H}^+)^2+K_1^{\mathrm{SS}}K_2^{\mathrm{SS}}K_3^{\mathrm{SS}}(\mathrm{H}^+)+K_1^{\mathrm{SS}}K_2^{\mathrm{SS}}K_3^{\mathrm{SS}}K_4^{\mathrm{SS}}}{((\mathrm{H}^+)^3+K_1^{\mathrm{SH}}(\mathrm{H}^+)^2+K_1^{\mathrm{SH}}K_2^{\mathrm{SH}}(\mathrm{H}^+)+K_1^{\mathrm{SH}}K_2^{\mathrm{SH}}K_3^{\mathrm{SH}})^2}$ 

 $\tilde{E}$  is the molal electrode potential; R, T, and f have their usual significance. (R—SH) and (R—S—R) are the concentrations of total cysteine and cystine respectively, *i.e.* the sum in all forms.  $K_1^{ss}, K_2^{ss}, K_3^{ss}, K_4^{ss}$  are the ionization constants of cystine,  $K_1^{s\pi}, K_2^{s\pi}, K_3^{s\pi}$  the ionization constants of cysteine.

A more rigorous form of Equation 9 would include activity coefficients. We have computed potentials between pH 3 and

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pH 9, with ionic strengths varying from 0 to 0.2, and have found that the difference, when activity coefficients are taken into account, is negligible. The activity coefficients used were those given in Tables II and IV.

The usual term,  $RT/f \times 2.303$  pH, cancels out in Equation 9. The dependence of the potential on the pH is implicit in the last term. The equation takes this form because cystine contains one more ionizable group than cysteine.

It is customary to tabulate electrode potentials of organic oxidants and reductants as  $E'_0$  values; *i.e.*, the potentials at stipulated pH values when the concentrations of total oxidant and reductant are equal so that the corresponding log term in the electrode equation becomes 0. This mathematical convenience is not obtained here when the final concentrations of cystine and cysteine are equal. Accordingly, in Table V a series of potentials is given, in which the concentrations of cystine and cysteine are such that log (R—SH)<sup>2</sup>/(R—S—S—R) is 0. This reference potential is designated as  $E''_0$  to distinguish it from the commonly used  $E'_0$ .

In discussion of the reversibility of the cystine-cysteine system it has not been generally realized that even in those conditions where the system is reversible the potential will vary for the same ratio of cysteine to cystine with their actual concentrations. This is a result of the squaring of the cysteine concentration, while the cystine concentration is taken only to the first power. On theoretical grounds, therefore, we may expect more negative potentials, or the reduction of progressively more negative dyes, with increasing concentrations of cysteine. This, in itself, is not evidence of the irreversibility of the system under observation.

The value of  $\tilde{E}$  in Equation 9 from the data in Table I is

$$\frac{-162,080 - 2(-81,610)}{2 \times 23,074} = +0.025 \text{ volt}$$

The value of the other constant term

$$-\frac{RT}{2f}\ln\frac{(K_1^{\rm SH})^2}{K_1^{\rm SS}K_2^{\rm SS}}$$

will depend on the ionization constants chosen. We have recalculated Cannan and Knight's data on the dissociation of cystine and cysteine with the same assumptions regarding activity coefficients

#### TABLE V

Oxidation-Reduction Potentials for Cystine  $\rightleftharpoons$  Cysteine, and  $\beta,\beta'$ -Dithiodilactic Acid  $\rightleftharpoons \beta$ -Thiolactic Acid Systems, at 25° and 37° Relation between  $E''_0 \left( Potential When \frac{(R - SH)^2}{R - S - S - R} = 1 \right)$  and pH The values are measured in volts.

		Cystin	e-cysteine		Ditte I'le d'
$_{\rm pH}$	2	5°	3	7°	acid-thiolactic acid, 25°
	Series 1	Series 2	Series 1	Series 2	
0	+0.034	+0.059	+0.041	+0.068	+0.081
1	-0.028	-0.007	-0.024	-0.001	+0.022
<b>2</b>	-0.093	-0.083	-0.092	-0.080	-0.037
3	-0.152	-0.156	-0.154	-0.157	-0.096
4	-0.212	-0.212	-0.215	-0.215	-0.154
5	-0.271	-0.272	-0.277	-0.277	-0.207
6	-0.330	-0.331	-0.339	-0.339	-0.262
7	-0.389	-0.391	-0.401	-0.404	-0.321
8	-0.447	-0.453	-0.462	-0.469	-0.380
9	-0.494	-0.510	-0.511	-0.523	-0.438
10	-0.525	-0.554	-0.542	-0.571	-0.491
11	-0.556	-0.576	-0.575	-0.594	-0.519
12	-0.565	-0.579	-0.584	-0.598	-0.525

Series 1 for the cystine-cysteine system at  $25^{\circ}$  is computed on the basis of the thermodynamic ionization constants, *i.e.* allowance made for activity coefficients, derived from the data of Sano (for cystine) of the authors' for cysteine; Series 1 at  $37^{\circ}$ , on the basis that the changes in the ionization constants of the two amino acids with temperature are such that the term in which they occur in the electrode equation has the same value at  $25^{\circ}$ and  $37^{\circ}$ , apart from the change in value of RT/2f. Series 2 is computed on the basis of Cannan and Knight's titration constants (29), *i.e.* no allowance made for activity coefficients, but corrected for temperature at  $25^{\circ}$ and  $37^{\circ}$  as suggested by Cohn. The values of the constants used, expressed as pK', are:

Series	Tempera-		Cys	tine		Cysteine			
No.	ture	pK'1	pK'2	pK's	pK'4	pK'1	pK'2	pK'3	
	°C.								
1	25	1.04	2.05	8.00	10.25	1.71	8.33	10.78	
1	37	1.04	2.05	8.00	10.25	1.71	8.33	10.78	
<b>2</b>	25	1.0	1.72	7.65	9.19	1.96	8.35	10.28	
<b>2</b>	37	1.0	1.72	7.23	8.77	1.96	7.93	10.28	

pK values from Cannan and Knight's data corrected for activity coefficients

		30	1.0	1.64	7.57	9.42	1.76	8.26	11.00
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as described above. The values so obtained for cysteine are in good agreement, after allowance is made for the temperature difference, with those found in our electrometric titrations. In the case of cystine there are large differences between the values obtained by Cannan and Knight and those deducible from the solubility data of Sano. These differences are quite large for  $pK_1$ ,  $pK_{2}$ , and  $pK_{4}$ . Accordingly we have computed the potentials at different hydrogen ion concentrations for the cystine-cysteine system, employing on the one hand the thermodynamic dissociation constants based upon our titration data for cysteine and the solubility data of Sano, and on the other the titration constants, *i.e.* not corrected for activity coefficients, of Cannan and Knight modified for the difference in temperature as suggested by Cohn The figures in Table V show that the calculated values of (32).the potentials in the range of hydrogen ion concentrations from pH 4 nearly to 8 are practically unaffected by differences in the values chosen for the ionization constants. In this range the term

$$\frac{RT}{nF} \ln \frac{(K_1^{\text{SH}})^2}{K_1^{\text{SS}} K_2^{\text{SS}}}$$

and the ionization term nearly cancel out, so that the equation as a close approximation becomes in this pH range

$$E_{\rm obs.} = \tilde{E} - 2.303 \, \frac{RT}{f} \, \mathrm{pH} \tag{10}$$

This numerical coincidence occurs in the range of hydrogen ion concentrations where both amino acids are predominantly in the zwitter ionic form.

At 37°  $\tilde{E}$  is from Table I

$$\frac{-158,710 - 2(-80,110)}{2 \times 23,074} = +0.032$$
 volt

The large differences in the dissociation constants of cystine calculated from Sano's solubility data at  $25^{\circ}$  and the titration data of Cannan and Knight at  $30^{\circ}$  forbid their employment for the computation of the dissociation constants of cystine at  $37^{\circ}$ . So employed they lead to the extremely improbable values for the

heats of neutralization, computed by means of the equation  $\Delta pK = -\frac{\Delta H}{R \times 2.303} \left(\frac{T_2 - T_1}{T_1 T_2}\right)$ , of the second and fourth ionizable groups of 34,000 and 69,000 calories respectively. Accordingly the potentials at 37° for the cystine-cysteine system given in Table V are calculated on the basis that the changes in the ionization constants of the two amino acids with temperature are such that the term in which they occur in the electrode equation has the same value at 25° and 37°, apart from the change in value of RT/2f. The other series of values at 37° is computed on the basis of Cannan and Knight's titration constants corrected for temperature. The values of the constants used are given in the foot-note to Table VI. As at 25°, the values of the potentials from pH 4 to 8 are independent of these constants.

Oxidation-Reduction Potentials of Dithiodilactic Acid  $\rightleftharpoons$  Thiolactic Acid System—The electrode equation for the reaction  $\beta,\beta'$ -dithiodilactic acid +  $2H^+ + 2(e) \rightleftharpoons \beta$ -thiolactic acid is

$$E_{\text{obs.}} = \tilde{E} - \frac{RT}{2f} \ln \frac{(\text{R}-\text{SH})^2}{(\text{R}-\text{S}-\text{S}-\text{R})} - \frac{RT}{2f} \ln \frac{(\text{H}^+)^2 + K_1^{\text{SS}}(\text{H}^+) + K_1^{\text{SS}}K_2^{\text{SS}}}{((\text{H}^+)^2 + K_1^{\text{SH}}(\text{H}^+) + K_1^{\text{SH}}K_2^{\text{SH}})^2}$$
(11)

The significance of the symbols is similar to those in Equation 9.  $\tilde{E}$  at 25° from Table I is

$$\frac{-165,900 - 2(-84,810)}{2 \times 23,074} = +0.081 \text{ volt}$$

By inserting this value of  $\tilde{E}$  and the ionization constants of Table V into Equation 12 we have computed the  $E'_0$  values given in Table V.

The data in Table V show that the amino group strengthens considerably the reducing potential of the adjacent sulfhydryl group. Increasing the temperature from 25° to 37° slightly increases the reducing potential.

Direct Experimental Measurements of Cystine  $\rightleftharpoons$  Cysteine Oxidation-Reduction Potential—In Table VI are collected the potentials observed experimentally for the cystine-cysteine system from three different laboratories. In every case it was concluded that the system under observation was cystine  $+ 2H^+ + 2(e) \rightleftharpoons 2$  cysteine. These values are all markedly different from that calculated from the thermal data.

It has been shown (17) in the case of three enzymatic reactions that, when the experimental reaction under observation is the same as that postulated, the observed potentials are in close agreement with those based on thermal data in which the intervention of the enzyme is ignored. In the cystine-cysteine system there is the more reason for expecting close agreement between the observed potentials and those calculated from thermal data because the complication of the requirement of an enzyme for the

TABLE VI E''<sub>0</sub> (in Volt) at 25° and pH 7.0 for l-Cystine +  $2H^+$  +  $2(e) \rightleftharpoons l$ -Cysteine

Method	E″₀	Investigator
Potentiometric oxidation of cys- teine with		
KIO3	+0.06	Williams and Drissen (33)
$K_2Cr_2O_7$	+0.13	
I <sub>2</sub>	+0.13	
Potentiometric; electrolytic for-		
mation of cysteine	-0.329	Ghosh, Raychaudhuri, and Ganguli (13)
Colorimetric; oxidation of cys-		
teine, reduction of cystine by		
dyes	-0.222	Fruton and Clarke (14)
From thermal data	-0.390	Authors

attainment of equilibrium in the experimental reaction was absent in all three of the above cases.

We have estimated that the extreme possible error in the thermal data for the free energy change in this reaction is 2000 calories. The probable error is much less. In terms of potential this extreme possible error is 43 millivolts. At pH 7.0 the potential calculated from the thermal data is practically independent of the dissociation constants assigned to the amino acids or of their activity coefficients. At hydrogen ion concentrations where these significantly affect the value of the calculated potential all other assumptions than those we have preferred (for independent reasons) augment the discrepancy between the calculated and observed potentials. It is certain that the calculated potential corresponds to the reaction which has been formulated only in the case of the thermal value. The reason for the large discrepancies in Table VI must therefore be sought in the experimental conditions in which the different values were obtained. In two of the three studies under consideration here the data given show conclusively that the potentials observed were significantly dependent on other reactions which were not taken into account.

In the experiments of Williams and Drissen (33) the shape of the titration curves, and the variation of the  $E'_0$  values with the nature of the oxidizing agent indicate that what was actually measured, for example in the case of the iodine titration of cysteine, was the reduction potential of the system  $I_2 \rightleftharpoons 2I^-$ . This conclusion is corroborated by the behavior of cysteine toward dyes (14, 34). 0.01 N cysteine for example at 30° and pH 7.0 completely reduces indigomonosulfonate whose  $E'_0$  is -0.16 volt. This would be impossible if the values of Williams and Drissen were even approximately correct.

There can be little doubt that the potentials observed by Ghosh, Raychaudhuri, and Ganguli (13) refer to a system in which cystine and cysteine are participants. These authors varied the concentrations of cystine and cysteine by electrolytic reduction of the cystine at the same mercury electrodes which were used to measure the potentials. The electrolysis also achieves, according to Ghosh and Ganguli, the necessary removal of the film of oxygen on the electrode. The potentials which they observed have been confirmed quantitatively by Green (34). He also confirmed their finding that the potential is 60 millivolts more negative after electrolysis than before.

The experiments of Ghosh and Ganguli support their view that the failure of previous workers to obtain thermodynamically reversible electrode potentials with the cystine-cysteine system is to be ascribed to a film of oxygen so firmly bound on the mercury electrodes used that it can be removed only by electrolysis. But their experimental data indicate that complexes of mercury and cystine probably existed in their solutions. In Table VII are given the concentrations of cystine which they reported, and the solubility of cystine at the same hydrogen ion concentrations and temperatures calculated from dissociation and titration constants

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and also interpolated from the directly observed solubilities of Sano. Ghosh *et al.* gave no details regarding the buffer solutions used and hence no allowance can be made for activity coefficients. In the pH range in which they worked, this correction is probably small, since very little of the cystine was in the divalent form, and their buffers were dilute (a large change in pH (0.6) occurred when the acid cystine solution was mixed with the buffer). The solubility of cystine in the solutions used by Ghosh *et al.* was probably therefore between those calculated from ionization

TABLE VII

Comparison of Concentrations of Cystine Found by Ghosh et al., and Solubility of Cystine at Different Hydrogen Ion Concentrations and Temperatures

				Calculat	ed from
Temperature	рН	Found by Ghosh et al.	Interpolated from Sano's observed solubilities	Ionization constants, without introduction of activity coefficients	Titration constants of Cannan and Knight, corrected for temperature
° <i>C</i> .		mole per l.	mole per l.	mole per l.	mole per l.
25	8.60	0.0024	0.0025	0.0023	0.0056
	8.50	0.0024	0.0021	0.0019	0.0043
	8.50	0.0018	0.0021	0.0019	0.0043
	8.40	0.0024	0.0018	0.0016	0.0034
	8.40	0.0015	0.0018	0.0016	0.0034
	8.05	0.0018	0.00076	0.00097	0.0017
	8.05	0.00087	0.00076	0.00097	0.0017
	7.5	0.0034	0.00069	0.00060	0.00079
	7.5	0.0028	0.00069	0.00060	0.00079
20	7.0	0.00171		0.00043	0.00044

constants alone (*i.e.* without taking activity coefficients into account) and the values obtained by Sano in various buffer solutions. Table VII shows that the concentrations of cystine found by Ghosh *et al.* in some of their solutions exceeded the calculated and experimentally observed solubilities. They also exceed from pH 7.0 to 8.05 the solubilities computed from the titration constants of Cannan and Knight, which were obtained in solutions whose ionic strengths varied from 0.02 to 0.1. At pH 7.0 the discrepancy between the concentration of cystine found by Ghosh *et al.* and the expected solubility is greatest. At this pH uncer-

tainties regarding dissociation constants and activity coefficients affect the value of the calculated solubility only to a slight extent. If the pH values of the solutions of Ghosh *et al.* were those reported, it follows that a large fraction of the cystine (supersaturation being excluded) was not free in solution. The obvious suggestion is that it existed in the form of a mercury-cystine complex.

An alternative hypothesis to complex formation, to account for the discrepancy between the solubility data and the concentration of cystine found by Ghosh *et al.*, is that in the course of the electrolysis, not only was cysteine formed, but the solutions also became much more alkaline. This possibility is excluded by the concordance of the  $E_0$  values obtained by Ghosh, Raychaudhuri, and Ganguli, by Green, and by Ghosh and Ganguli, calculated on the basis of initial pH (before electrolysis) in buffer solutions ranging from pH 7.0 to 9.2, and secondly by the observation of Green, that an electrolyzed solution gave the usual more positive potential against fresh mercury.

In spite of the fact, therefore, that Ghosh *et al.* observed no precipitate when they passed  $H_2S$  through their solutions, their data indicate that a mercury complex of cystine, and probably also therefore of cysteine, existed in their solutions. As a result their standard electrode potential,  $E_0$ , is composed not only of the molal electrode potential of the cystine-cysteine reaction, and the log of the ratio of their ionization constants, but also of a term for the ratio of the equilibrium constants of the two amino acids with mercury. It is improbable that the equilibria between cystine and cysteine and mercury are such that they exactly cancel each other.

We must call attention here to the combustion values for cystine and cysteine reported by Becker and Roth (35). These are lower than those given in Table I obtained in this laboratory. They yield standard free energy values,  $\Delta F^0$ , of -82,480 and -166,630 for cysteine and cystine respectively, which lead to a value of +0.096 volt for  $\tilde{E}$  instead of +0.025 volt calculated from the thermal data in Table I. The higher figure for  $\tilde{E}$  gives  $E''_0$ values in reasonably close agreement with those given of Ghosh *et al.* Thus at pH 7.0,  $E''_0$  from our thermal data is -0.390volt, according to Ghosh *et al.* it is -0.329 volt, and from the combustion data of Becker and Roth it is -0.319 volt.

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Nevertheless this agreement in the last two values is only fortuitous. In a private communication Professor Roth agreed that their combustion values are less reliable than ours. Only a small amount of material was supplied them, and they burned it without either testing its purity or purifying it further. That it contained considerable impurity is indicated by the lower percentages of sulfur which they found, by their lower values for the heats of combustion, and by the large variations in the individual determinations.

Fruton and Clarke (14) measured the potential of the cystinecysteine system colorimetrically. They measured the equilibrium degree of reduction of dyes with known oxidation-reduction potentials by different concentrations of cysteine at different hydrogen ion concentrations. The following evidence attested to the thermodynamic reversibility and the accuracy of the observed potentials. The same  $E'_0$  values (corresponding to  $E''_0$  in Tables VI and VII) were obtained with different dyes and with different concentrations of cysteine. The dyes in their reduced form were reoxidized by cystine, and the final degree of reoxidation attained was in accord with the  $E'_0$  values given by the reduction experiments with cysteine.

From these observations the  $E''_0$  value of the cystine-cysteine system at pH 7.0 and 25° is -0.22 volt, which is 100 millivolts more positive than the value given by Ghosh *et al.* and 170 millivolts more positive than our thermal value.

These discrepancies are far beyond the possible experimental errors. We accordingly undertook a repetition of the experiments of Fruton and Clarke, and have confirmed them in principle, though we have been unable to confirm them in detail. We have found that an equilibrium is attained *in vacuo*, of which at least some, if not all, of the components are cysteine, cystine, and the oxidized and reduced forms of the dye. The  $E''_0$  values we obtained were approximately 50 millivolts more negative than those reported by Fruton and Clarke.

We shall describe only the general features of our experimental procedure which was not essentially different in the reduction experiments from that of Fruton and Clarke. The cysteine was measured into the overhang of a Thunberg tube and the other solutions—dye, buffer, and cystine—into the lower compartment.

The vessel was evacuated and then the contents of the upper and lower compartments were mixed. The vessels containing different mixtures were then kept in a vacuum desiccator which was continuously evacuated by an oil pump. The dyes and amino acids used were recrystallized specimens. The dyes finally chosen, indigodisulfonate and brilliant alizarin blue, were used in concentrations of 0.00005 M and 0.0001 M. The final concentration of cystcine was varied from 0.0001 to 0.001 m, and of cystine up to 0.002 м. The experiments were carried out at room temperature and in buffer solutions at pH 7.5 (phosphate), 8.0, and 8.5 (borate). After equilibrium was attained, in 2 to 3 days, the vacuum in the desiccator was broken by admitting purified hydrogen or nitrogen, and the colors in the Thunberg tubes compared with previously prepared dilutions of the dye. The desiccator technique with continuous evacuation was used because we were unable otherwise to maintain a sufficiently high vacuum for the length of time required for the attainment of equilibrium. With these low concentrations of reactants an air leak giving a pressure of 1 mm. of Hg radically distorted the results.

We observed that in solutions containing the same concentration of cysteine and different concentrations of added cystine that the degree of reduction finally attained was always less the higher the initial concentration of cystine. This was the case with brilliant alizarin blue and with indigodisulfonate. On the assumption that the reaction here was simply 2 cysteine + oxidized dye  $\rightleftharpoons$  cystine + reduced dye the calculated  $E''_0$  value at pH 8.0 was between -0.29 and -0.30. The corresponding value of Fruton and Clarke at 25° is approximately -0.27 volt. At pH 8.5, with brilliant alizarin blue, the  $E''_0$  value we have found was between -0.32 and -0.34; that of Fruton and Clarke is -0.29 volt.

In most of the experiments the effect of the added cystine on the equilibrium degree of reduction was less than the theoretical amount calculated on the basis of the reaction 2 cysteine + reduced dye  $\rightleftharpoons$  cystine + oxidized dye. We do not at present attach more than semiquantitative significance to these observations and the above  $E''_0$  values. The range of concentrations of cysteine, which gave degrees of reduction which were neither too low nor too high to be measured, was small, between 0.0004 M and 0.0007 M, with 0.0001 M indigodisulfonate; the maximum possible concentration of cystine at pH 8.5 is only approximately 0.002 m; and the method for measuring the color is crude.

In every instance, with and without added cystine, and with indigodisulfonate, brilliant alizarin blue, and cresyl violet, we observed a greater degree of reduction than the  $E''_0$  values of Fruton and Clarke call for. In further disagreement with their observations we have been unable to observe any reoxidation of reduced dyes by cystine with concentrations of reactants and hydrogen ion concentration identical with theirs.

Nevertheless, in confirmation of Fruton and Clarke's observations, the dye-reducing potency of cysteine, which we have observed, fell far short of that called for by the  $E''_0$  values of Ghosh et al., let alone the thermal values. The present situation of this problem may be summarized therefore as follows: Two experimental systems have been found, those of Ghosh et al. and of Fruton and Clarke, in which cysteine and cystine participate in an oxidation-reduction equilibrium. The potentials obtained in these two systems differ by 100 millivolts, much too large a quantity to be ascribed to experimental error. Both these directly obtained experimental values are more positive than the potential calculated from thermal data. The potential of Ghosh et al. is nearer to the thermal value, but even it differs by 70 millivolts. This difference is within the possible error of the thermal data. Yet the experimental data presented by Ghosh et al. show conclusively that important reactions were not taken into account in their calculation of the potential. In view of the even greater difference, 170 millivolts, between the colorimetric and thermal values, it is highly probable that in these colorimetric measurements also there are important side reactions. The only possible doubt of the thermal value is regarding the accuracy of the actual experimental measurements. It is improbable that any corrections here would bring it into accord with one of the experimental values. While, as stated above, the final reference value for the stated reaction is the thermal value, its usefulness is limited. In any set of experimental conditions the experimental oxidationreduction potential may be more pertinent. But the difference between it and the thermal value is an indication that the reaction is not simply the reduction of cystine to cysteine or vice versa.

Catalytic Action of Selenium Dioxide on Oxidation of Cysteine-

In the course of our colorimetric experiments we observed that small amounts of selenium dioxide catalyze the reduction of indigodisulfonate by cysteine. Thus with 0.00005 M dye, 0.001 M cysteine, and  $0.00001 \text{ M SeO}_2$ , the dye is completely reduced in 1 hour at room temperature, whereas without the selenium dioxide nearly a week is required. Salts of iron, copper, cobalt, nickel, or magnesium do not possess this catalytic property. With high concentrations of cysteine (0.1 M) and SeO<sub>2</sub> (0.01 M) a white crystalline complex precipitates out of solution. Dissolved in strong HCl, red selenium and cystine precipitate out. The same degree of reduction of dyes was attained with selenium dioxide as without, both with and without added cystine. The only dyes we could use with this catalyst in the range of hydrogen ion concentrations from pH 7.0 to 8.5 were indigodisulfonate and phenosafranine. Brilliant alizarin blue, gallophenine, and cresyl violet appeared to be destroyed by it.

#### SUMMARY

1. Data are presented from which the oxidation-reduction potentials of the systems, cystine  $\rightleftharpoons$  cysteine, and dithiodilactic acid  $\rightleftharpoons$  thiolactic acid, have been calculated.

2. These values and other evidence show that the potentials previously obtained for the cystine  $\rightleftharpoons$  cysteine system by direct measurement are not referable exclusively to this system.

3. Some experiments are described in which addition of cystine has been observed to affect the degree of reduction of dyes by cysteine.

4. Selenium dioxide is a catalyst for the reduction of indigodisulfonate (and probably other dyes not attacked by the selenium dioxide) by cysteine. A cysteine-selenium dioxide complex has been isolated.

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