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Films of Fe<sub>0.79</sub>Ge<sub>0.21</sub> with thicknesses of 300 nm were synthesized by ion beam sputtering, and were annealed at temperatures from 200 to 550 °C. The materials were characterized by x-ray diffractometry, Mössbauer spectrometry, vibrating sample magnetometry, ferromagnetic resonance spectrometry, and electrical resistivity measurements. The as-prepared materials comprised chemically disordered bcc crystallites of sizes less than 20 nm, and were found to have a distribution of internal strains. Upon annealing at temperatures of 250 °C and below, there occurred strain relaxation, some evolution of short range chemical order, and an improvement in soft magnetic properties. The coercive field was a minimum for the sample annealed at 250 °C. Crystallite growth occurred at higher annealing temperatures, accompanied by a transition in several measured parameters from those of ultrafine grained materials to those typical of polycrystalline materials. This trend can be explained with the random anisotropy model. Mössbauer and magnetization measurements indicated that the Ge atoms behave as magnetic holes. The <sup>57</sup>Fe hyperfine magnetic field distribution, and its change during chemical ordering, can be calculated approximately with a model of magnetic response. The large local isomer shifts at <sup>57</sup>Fe atoms near Ge atoms suggest that a local depletion of 4s conduction electron density should be incorporated into the model.

### **I. INTRODUCTION**

In the field of magnetic materials, a subtopic of recent interest is the magnetic properties of materials with nanoscale microstructures. The magnetic properties of nanophase materials can be tuned from soft to hard, depending on the magnetic coupling between their small crystallites. In particular, there is widespread interest in an extremely soft magnetic material, "Finemet," which is produced commercially by the dense precipitation of nanocrystalline bcc Fe–Si within an amorphous matrix.<sup>1,2</sup> Soft magnetic properties of large-grained polycrystals were studied previously for alloys of Fe–Ge and Fe–(Al,Si)–Ge,<sup>3–5</sup> and with metalloid substitutions the magnetic properties were studied in the amorphous state.<sup>6,7</sup> Noteworthy is the slightly negative magnetostriction of Fe–Ge alloys with compositions of 20–25 at. % Ge.<sup>4,5</sup>

Here we report results of a study on the microstructure and the magnetic properties of nanocrystalline Fe-Ge alloys; specifically the change in magnetic properties upon annealing, and their correlation to changes in the structure of the materials. Our thin films of Fe-Ge were made by sputtering. Their composition of 79.5 at. % Fe-21.5 at. % Ge lies near the low-temperature phase field of the bcc-based  $DO_3$  ordered structure,<sup>8</sup> and short- or long-range  $DO_3$  order (SRO or LRO) appeared after the as-prepared alloys were annealed at low temperatures. The strain relaxation, growth of crystallites, and the growth of chemical order were measured by x-ray diffractometry and Mössbauer spectrometry. The latter technique also provided information on local magnetism. Macroscopic magnetic parameters were obtained from vibrating sample magnetometry, and ferromagnetic resonance was used for obtaining magnetic parameters and for testing the sample homogeneity. Electrical resistivity was also measured.

We found that samples annealed at higher temperatures first underwent a relaxation of strains and the growth of chemical SRO. For annealings at progressively higher temperatures but below 300 °C, there was a corresponding decrease in coercive field and an improvement in the quality of ferromagnetic resonance (FMR) spectra. In addition, both magnetization and Mössbauer spectrometry measurements indicated that the easy axis of film magnetization tended away from its initially normal orientation. and toward the plane of the film. For samples annealed at temperatures above 300 °C, however, there was an increase in coercive field and a degradation in the ferromagnetic resonance spectra toward values typical of polycrystalline materials. A change was also observed in the orientation of magnetization, as the earlier trend was reversed and the sample plane became harder magnetically due to textured crystallite growth. This transition coincided with the ongoing increase in average crystallite size, suggesting that the soft magnetic properties after the 250 °C annealing may be partially understood with the model of random anisotropy<sup>9</sup> that has been used to interpret the soft magnetic properties of Finemet.<sup>2</sup>

The <sup>57</sup>Fe hyperfine magnetic field distribution was obtained from Mössbauer spectra by assuming a strong correlation between local hyperfine magnetic field and local isomer shift. The large local isomer shifts suggest that a local depletion in 4s conduction electron density should be considered when calculating the hyperfine magnetic fields within the magnetic response model.<sup>10-12</sup>

### **II. EXPERIMENT**

### A. Sample preparation

The Fe-Ge thin films were deposited onto a 5.1 cm square optically polished fused quartz substrate by standard ion beam sputtering. A mosaic sputtering target was used, consisting of a 10 cm diam polycrystalline 99.999 at. % Ge plate overlapped by a pair of 99.998 at. % Fe foils. The area of the surface impacted by the beam was approximately 25% Ge and 75% Fe. The substrate was positioned slightly off axis, and rotated at 3 rpm in order to minimize film columnar growth and self-shadowing effects. The system base pressure before sputtering was  $8 \times 10^{-8}$ Torr while the pressure of gettered argon gas during sputtering was  $1.1 \times 10^{-4}$  Torr. The maximum temperature of the film during deposition was 50 °C. A film thickness of  $280\pm8$  nm was measured by thickness profilometer measurements on a step-masked portion of the film. The film composition was measured by a Kevex energy dispersive x-ray spectrometer mounted on a JEOL 6800 scanning electron microscope, and by an EDAX 9900 energy dispersive x-ray spectrometer mounted on a Philips EM430 transmission electron microscope. Samples were cored from the deposited film, and 1 cm diam samples were used for Mössbauer spectrometry, x-ray diffractometry, and electrical resistivity measurements, and 0.5 cm diam samples were used for vibrating sample magnetometry and ferromagnetic resonance spectrometry measurements. Samples were annealed in a flowing-gas tube furnace using gettered ultrapure argon gas and a quartz lamp heat source. The typical annealing procedure was as follows: the sample was allowed to warm in the convective flow away from the center for 5-10 min to avoid thermal shock, then placed in the center of the furnace for a 15 min soak period. Upon removal from the center of the furnace, the sample was placed in the original position for a 10 min period to cool in the flowing gas.

# **B. Measurements**

X-ray diffractometry was performed with an Inel CPS-120 diffractometer system using monochromatized Co  $K\alpha$ radiation and a curved position sensitive detector (PSD) spanning 120° in  $2\theta$  angle. For this diffractometer system the angle of incidence was fixed (typically at 14°), so the direction of  $\Delta k$  was different for each diffraction peak. Mössbauer spectra were obtained at room temperature using a conventional constant acceleration spectrometer. A radiation source of 30 mCi <sup>57</sup>Co in a Rh matrix was used, and conversion electron spectra were obtained with a He–CH<sub>4</sub> flow-gas detector.

Magnetization measurements were performed on a Digital Measurement Systems vibrating sample magnetometer. Hysteresis loops were taken along the film normal at magnetic fields to 17.5 kOe, providing values for sample saturation magnetization,  $4\pi M_s$ . The effective magnetiza-



FIG. 1. X-ray diffraction pattern of the as-prepared and two annealed samples of sputtered- $Fe_{0.79}Ge_{0.21}$  thin films.

tion  $(4\pi M_{\rm eff})$ , which measures the total demagnetizing field normal to the sample plane, was evaluated from the hysteresis loop using the projected point of intersection between the linear low field magnetization behavior and the saturation magnetization. In-plane hysteresis loops provided values for  $4\pi M_s$ , the remanent magnetization  $(4\pi M_r)$ , the in-plane anisotropy field, and the coercive field,  $H_c$ .

Ferromagnetic resonance (FMR) measurements were performed on an X-band electron spin resonance spectrometer using a TE<sub>102</sub> cavity at magnetic fields to 21 kOe. FMR spectra were obtained with the applied magnetic field, lying both in the sample plane and along the sample normal. Extracted parameters include values for  $4\pi M_{\rm eff}$ and an estimate of the in-plane anisotropy field. Measurements with the applied magnetic field along the sample normal, provided the spin wave resonances (SWR) spectra of the samples. Electrical resistivities of the samples were measured with a linear four point probe method, with corrections for the finite sample size and probe spacing.<sup>13</sup>

## III. RESULTS AND DISCUSSION

## A. X-ray diffractometry

Representative x-ray diffraction patterns are presented in Fig. 1. These data and all others showed only fundamental diffractions of the bcc lattice, and none from the hexagonal  $B8_1$  structure, even though some  $B8_1$  phase could be expected in equilibrium.<sup>8</sup> Superlattice diffractions of the bcc-based  $D0_3$  ordered structure were observed from samples annealed at the higher temperatures. The  $(\frac{1}{2}\frac{1}{2}\frac{1}{2})$ superlattice diffraction peak of the  $D0_3$  ordered structure was first seen in the diffraction pattern from the sample annealed at 400 °C, and its intensity grew with annealing temperature, approximately doubling in intensity for the specimen annealed at 550 °C. [For samples annealed at 350 °C, however, the  $(\frac{1}{2}\frac{1}{2}\frac{1}{2})$  peak was observed after annealing for several hours.] The fundamental diffraction peaks became sharper with increased annealing temperature, ow-



FIG. 2. (a) Crystallite size and (b) mean-square strain obtained from widths of the x-ray diffraction peaks vs annealing temperature.

ing to strain relaxation and grain growth. The breadths of the fundamental peaks were used to estimate the meansquared strain and the grain size by plotting the k-space width of a Lorentzian fit to each diffraction peak, versus the magnitude of k for the diffraction. The slopes of these graphs were used to obtain a mean-squared strain, and the y-axis intercepts were used to obtain an average value for grain size.<sup>14</sup> These data are presented in Figs. 2(a) and 2(b). To determine the crystallographic texture, x-ray diffraction was also performed with various angles of the incident beam. At an incidence angle of 14°, the observed  $(\frac{1}{2}\frac{1}{2}\frac{1}{2})$  peak was strongest. Since the  $(\frac{1}{2}\frac{1}{2}\frac{1}{2})$  peak is at a 2 $\theta$ diffraction angle of about 30°, we find that there is a crystallographic preference for the [111] direction to lie normal to the plane of the sample.

# B. Magnetometry, resistivity, and ferromagnetic resonance measurements

The results of magnetometry, resistivity, and ferromagnetic resonance measurements are presented in Table I. Data are presented for the average saturation magnetization, effective magnetization, and the in-plane coercive field for the as-prepared and annealed samples. The saturation magnetization shows no significant variation for the annealed samples, having a value near 14 kG. This agrees with previous results for Fe–Ge alloys,<sup>4</sup> is comparable to results found for evaporated Fe–Si and Fe–B alloys having similar compositions,<sup>15</sup> and matches the value of 14.0 kG obtained for polycrystalline Fe<sub>3</sub>Ge.<sup>16</sup>

TABLE I. Magnetic and electrical properties.

T <sub>anneal</sub> (°C)	〈 <i>H</i> 〉 (kG)	4πM <sub>S</sub> (kG) (±0.4)	$4\pi M_{\rm eff}$ (VSM) (kG) (±0.4)	$4\pi M_{\rm eff}$ (FMR) (kG) (±0.01)	H <sub>c</sub> (Oe) (±1)	μΩ cm (±0.01)
A-P	267	13.9	13.9	14.05	66	112
150	274	14.4	14.6	14.03	61	113
200	267	14.4	14.4	14.64	45	110
250	262	14.4	14.2	14.44	14	109
300	258	13.8	14.5	14.47	19	100
350	257	14.1	14.5	14.07	38	79
400	257	•••	•••	• • •	•••	76
450 	257	•••	•••	•••	•••	75

Neither magnetometry nor FMR measurements indicated the presence of in-plane uniaxial anisotropy for any sample. However, the shapes of the in-plane hysteresis loops for all samples are consistent with the existence of positive perpendicular anisotropy, which indicates that the easy axis of magnetization lies normal to the plane of the sample. Such anisotropy is commonly observed for relatively thick films of permalloy<sup>17</sup> and cobalt-rich amorphous films<sup>18</sup> having negative magnetostriction constants. It is caused by the magnetoelastic coupling to the strains in the samples. The magnitude of the perpendicular anisotropy field  $(H_u)$  for thin films can be obtained from  $H_u = 4\pi M_s - 4\pi M_{\text{eff}}$ , as the presence of the easy axis normal to the film plane will reduce the effective magnetizing field given by  $4\pi M_{\rm eff}$ . Here the experimental uncertainties in  $4\pi M_s$  obscure determination of a value for the perpendicular anisotropy. However, a trend in the magnitude of  $H_u$  can be observed in the ratio of remanent to saturation magnetization  $(M_r/M_s)$ , shown in Fig. 3. For the samples annealed at lower temperatures this ratio remains near 0.5, indicative of positive perpendicular anisotropy. However, as the strain in the sample decreases [see Fig. 2(a)], the



FIG. 3. Intensity ratio of the second and fifth lines of the Mössbauer spectra (left-hand scale) and ratio of the remanent magnetization to saturation magnetization (right-hand scale) of  $Fe_{0.79}Ge_{0.21}$  thin films vs annealing temperature.

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corresponding drop in  $H_u^1$  will make the film plane "easier," seen as an increase in the ratio  $M_r/M_s$  toward the ideal easy plane value of 1. Figure 3 indicates that  $M_r/M_s$ has a maximum value occurring for the samples annealed at 250 °C. The evolution of  $M_r/M_s$  for the samples annealed at still higher temperatures is driven by a different mechanism, namely the growth of textured grains having an in-plane easy axis, as discussed in Sec. III C.

The spin wave resonance spectra obtained from FMR taken normal to the plane of the sample were used as an indicator of the sample uniformity, as the mode spectra are sensitive to spatial variations in the magnetization or anisotropy field. The quality of a SWR spectrum was evaluated by the number of resolvable absorption modes, and also by the mode spacing relative to the expected spacing, which is quadratic in the mode number for standing SWR modes. The SWR spectra were found to improve for samples annealed at higher temperatures, with the best SWR spectra being obtained for the sample annealed at 300 °C. For this sample the mode behavior was approximately quadratic, and provided a deduced exchange stiffness (A) of  $1.5(3) \times 10^{-6}$  erg/cm. This behavior tracks the observed decrease in strain in the samples. However, the sample annealed at 350 °C showed only a single broad absorption mode. This mode had a very large FMR absorption linewidth  $(\Delta H_0)$  of 160 Oe, in contrast to values of 30–50 Oe measured for the highest field mode for all other samples. It should be noted that while the FMR linewidths of samples annealed at low temperatures are comparable to those found for amorphous iron-rich films,<sup>18</sup> the large linewidths found for the 350 °C samples are more typical of a polycrystalline alloy.

The trend found from FMR of improved soft magnetic properties with higher annealing temperature, followed by a degradation, was also found in the data on coercive field (see Table I). The coercive field decreases as samples were annealed at temperatures up to 350 °C, but then  $H_c$  begins to increase for higher temperatures. The decrease in  $H_c$  can be attributed to stress relaxation in the samples. The increase observed in  $H_c$  and  $\Delta H_0$ , and the disruption of the SWR spectra observed for the specimen annealed at 350 °C, may be explained by the random anisotropy model<sup>9</sup> that was used recently to explain the variation in  $H_c$  with grain size in nanocrystalline Fe-Si-B-Cu-Nb alloys.<sup>2</sup> This model predicts that the exchange interaction (A) will dominate the magnetocrystalline anisotropy  $(K_1)$  for materials having grain sizes smaller than the ferromagnetic exchange length,  $L_{\rm ex} = \sqrt{(A/K_1)}$ . This condition leads to soft magnetic behavior. Once the grain size exceeds  $L_{ex}$ , however, the material properties will become typical of polycrystals. For our Fe-Ge samples the transition occurs for an average grain size of 24 nm, from which we calculate a magnetocrystalline anisotropy of  $K_1 = 3 \times 10^6$  erg/cm<sup>3</sup>. This value of  $K_1$  is quite large and can be attributed to our use of an average grain size, whereas  $L_{ex}$  should be determined from the largest grain diameters in the sample.

Finally, the electrical resistivity data presented in Table I show a decrease that begins after annealing at 300 °C. This decrease correlates with the onset of long range ordering and grain growth in the material.

# C. Mössbauer spectrometry—Hyperfine magnetic fields

To obtain the hyperfine magnetic field (HMF) distribution, the experimental spectra were processed using the method of Le Caër and Dubois.<sup>19</sup> In this method a linear relationship between the isomer shift, I (with respect to pure Fe), and HMF, H, is assumed:

$$I = AH + B. \tag{1}$$

The constants A = -0.0015 mm s<sup>-1</sup> kG<sup>-1</sup> and B = +0.637 mm s<sup>-1</sup> were determined from the best fit of the calculated spectrum to the experimental one. The areas of the individual overlapping subpeaks in the HMF distributions were obtained by fitting the distribution to a set of Gaussian functions. Using an independent second method, the HMF distribution was assumed to be a sum of normalized Gaussian functions:

$$P(H) = \sum_{i=0}^{z} \frac{p_i}{\sqrt{\pi\sigma_i}} \exp\left[-\left(\frac{H-H_{0i}}{\sigma_i}\right)^2\right],$$
 (2)

where  $p_i$  is a normalized probability for a specific nearneighbor environment,  $(\sum_{i=0}^{z} p_i = 1)$ , and  $\sigma_i$  is a measure of the width of the *i*th Gaussian function. We used z=8 so that a Gaussian peak was associated with each possible number of Ge atoms in the 1nn shell of a <sup>57</sup>Fe atom. The HMF distribution was then convolved with a sextet of Lorentzian lines, with width and relative separations characteristic of a pure Fe spectrum. The isomer shift for each sextet,  $I_i$ , and the parameters  $p_i$ ,  $H_{0p}$  and  $\sigma_i$  were freely adjusted in the fitting routine. The values of  $p_i$  obtained with this second method were in good agreement with our results from the method of LeCaër and Dubois. With the HMF distribution, P(H), we calculated the mean HMF,  $\langle H \rangle$ , as

$$\langle H \rangle = \int_0^\infty H P(H) dH,$$
 (3)

and these data are presented in Table I. During annealing, the local environments around the <sup>57</sup>Fe atoms undergo a modest change as the alloy develops chemical order. In an alloy of Fe<sub>3</sub>Ge, the average number of Ge atom neighbors about a <sup>57</sup>Fe atom can increase from 2 to 8/3 upon ordering. Upon annealing, the average HMF was reduced by about 10 kG, as expected, since the extra Ge atoms should cause a reduction in HMF, but the saturation magnetization was essentially unchanged. These small changes in  $M_S$ and  $\langle H \rangle$  upon ordering suggest that Ge atoms act as magnetic holes in the bcc Fe lattice, and cause little disturbance to the magnetic moments at the Fe atoms themselves.

The relative intensities of the second and fifth peaks of the sextets were obtained in the course of obtaining the HMF distribution. Figure 3 shows the relative intensity of the second and fifth Mössbauer peaks with respect to the first and sixth peaks as a function of annealing temperature. It is well known that this intensity ratio depends on



FIG. 4. Mössbauer spectra of the sputtered  $Fe_{0.79}Ge_{0.21}$  thin films as prepared, and after annealing. The solid line was recalculated from the P(H) curves of Fig. 5.

the angle between the direction of the  $\gamma$ -ray beam and the direction of magnetization, and can vary between 0 (when the two directions are parallel) to 4/3 (when the two directions are perpendicular). For our experimental geometry, where the  $\gamma$ -ray beam is normal to the plane of the thin film, the Mössbauer results suggest that the directions of magnetization were oriented randomly in the as-prepared sample. After annealing, the average magnetization rotated toward the plane of the film, achieving a maximum inplane component for the sample annealed at 250 °C. A large in-plane component is consistent with the reduction in external field energy that is possible with a soft magnetic material. At higher annealing temperatures the average magnetization tended to rotate back out of the plane of the film. Grain growth at these higher annealing temperatures would tend to emphasize the magnetic anisotropy of the individual crystallites. An easy axis of magnetization along the [100] direction (which is the easy axis of magnetization of both bcc  $\alpha$ -Fe and the cubic phase of Fe<sub>3</sub>Ge)<sup>20</sup> should force some component of the magnetization out of the plane of the film if the films were isotropic, or if they had some [111] crystallographic texture, as determined by x-ray diffractometry.

Typical Mössbauer spectra are shown in Fig. 4, with their HMF distributions in Fig. 5. Distinct peaks in the HMF distribution correspond to the different numbers of first nearest neighbor (1nn)Ge atoms about <sup>57</sup>Fe atoms. Previous work with bcc Fe-Ge alloys<sup>21,22</sup> showed that each Ge atom in the 1nn or 2nn shell of a <sup>57</sup>Fe atom perturbed the <sup>57</sup>Fe HMF by  $\Delta H_1 = +23.2$  kG and  $\Delta H_2 = +8.1$  kG. The large perturbation from the 1nn Ge atoms can be used to calculate approximately the positions of the peaks of the HMF distribution, assuming that Ge atoms in the 2nn and 3nn shells of Fe are expected to slightly modify the HMF peak positions and widths. Further knowledge from x-ray diffractometry that there is strong  $D0_3$  order after annealing at temperatures above 400 °C allows us to identify the strongly growing peaks in the HMF distribution with the two <sup>57</sup>Fe sites in the  $D0_3$  structure, one of population 1/3 (minority site) having (0) 1nn Ge atoms, and the second with population 2/3 (majority site) having (4) 1nn Ge



FIG. 5. HMF distributions obtained from the Mössbaur spectra of Fig. 4 by the method of Le Caër and Dubois. The peaks are identified by the number of Ge atoms in the 1nn shell of  $^{57}$ Fe as labeled at the top of the figure.

atoms. Using these two pieces of information from the dilute alloy Mössbauer spectra and from our x-ray diffractometry study, the HMF's associated with the different numbers of 1nn Ge atoms are labeled at the top of Fig. 5. Since the peaks of the two  $^{57}$ Fe environments with (0) and (1) 1nn Ge atoms are not resolved, we refer to their combination as the (0,1) 1nn Ge atom peak.

The populations of the <sup>57</sup>Fe sites having different numbers of Ge neighbors [the  $p_i$  in Eq. (2)] are parameters that describe the short-range order (SRO) in the alloy. The evolution of these SRO parameters with annealing temperature is presented in Fig. 6. We know that the populations of the different <sup>57</sup>Fe neighborhoods in a fully disordered alloy are binomial probabilities:

$$p_i = \frac{8!}{i!(8-i)!} c^i (1-c)^{8-i}, \tag{4}$$

where c=0.21 for our alloy. These values of  $p_i$  are included on the left side of Fig. 6, where the closed circle is for a



FIG. 6. Populations of the  ${}^{57}$ Fe sites vs annealing temperature, determined from the areas under the peaks of the HMF distribution. The disconnected leftmost points were obtained from the binomial distribution from an alloy of Fe-21% Ge. The points at the right were obtained for a perfectly  $D0_3$ -ordered structure of Fe-21.75% Ge, assuming the extra Fe atoms occupied randomly the Ge sites.

TABLE II. Local isomer shifts.

Ge neighbors	0	1	2	3	4
I (mm/s)	0.142	0.176	0.210	0.262	0.343

combination of the (0) and (1) 1nn Ge environments:  $p_{1,0}=p_0+p_1$ . The initial state of the alloy is partially disordered, although there is some SRO in the alloy. This SRO is characteristic of the  $D0_3$  structure; the as-prepared material has a noticeable excess of the (4) Ge environment (the majority site of the  $D0_3$ -ordered structure), and probably a deficit of the (1) Ge environment (which is not expected in the  $D0_3$  ordered structure).

Although we know by inspection the populations of the two different sites in fully  $D0_3$ -ordered Fe<sub>3</sub>Ge, there is a substantial modification of these populations when the alloy is substoichiometric. In particular, those <sup>57</sup>Fe atoms that would have had (4) 1nn Ge atoms now have some of those Ge atoms replaced with Fe atoms. If we assume that these extra Fe atoms are distributed at random over the Ge sites, there is a probability,  $\delta c$ , for finding an Fe atom on any Ge site:

$$\delta c = 1 - 4c. \tag{5}$$

These extra Fe atoms do not affect the environments of the  ${}^{57}$ Fe atoms on the minority sites of the  $DO_3$  structure (nor of other antisited Fe atoms), which have (0) 1nn Ge neighbors. For those  ${}^{57}$ Fe atoms on the majority sites, however, a random substitution of Fe atoms into their four neighboring Ge sites gives a ratio for the number of  ${}^{57}$ Fe environments with (4) and (3) Ge neighbors:

$$\frac{p_4}{p_3} = \frac{(4!/4!0!)\delta c^0 (1-\delta c)^4}{(4!/3!1!)\delta c^1 (1-\delta c)^3} = \frac{1-\delta c}{4\delta c}.$$
(6)

Equation (6) is a particularly sensitive measure of  $\delta c$ , which can then be converted into the composition of the alloy. In our ordered alloy, the ratio  $p_4/p_3=1.76$ , so we obtain  $\delta c=0.124$  with Eq. (6) and c=0.219 from Eq. (5). This is in good agreement with our composition determination by x-ray fluorescence spectrometry, and may even be more accurate. All the  $p_i$  can be determined for an off-stoichiometric alloy by employing similar arguments, and for an alloy of c=0.219 these  $p_i$  are presented as isolated points on the right-hand side of Fig. 6. The experimental data show that the SRO in the alloy is highly developed for annealings at temperatures above 400 °C, consistent with the observation of strong x-ray superlattice diffractions.

## D. Mössbauer spectrometry—Isomer shifts

There are different isomer shifts for <sup>57</sup>Fe atoms having different numbers of 1nn Ge atoms. Using our two methods for extracting the HMF distribution, we found local isometer shifts I with respect to pure bcc Fe, as listed in Table II. If these local isomer shifts arise from the change in the density of 4s electrons at <sup>57</sup>Fe nuclei,  $N_{4s}$  the relationship between I and  $N_{4s}$  (Ref. 23) implies changes in  $N_{4s}$  of -0.071, -0.088, -0.105, -0.134, and -0.175 electrons for <sup>57</sup>Fe atoms with (0), (1), (2), (3), and (4) 1nn Ge atoms, respectively. These changes are large, and show that 1nn Ge atoms cause a significant electronic disturbance at <sup>57</sup>Fe atoms. Because the addition of Ge atoms reduces  $N_{4s}$  and makes the HMF more positive, the effect of a 1nn Ge atom is to deplete the spin down 4s electron density at the <sup>57</sup>Fe nucleus. This local effect may not correspond to the overall effect on the 4s band, however.

These local isomer shifts are consistent with Eq. (1) which was used successfully with the same values for the constants A and B for both ordered and disordered alloys. Interestingly, the constants A and B change by a factor of 2 during the process of  $D0_3$  ordering in Fe<sub>3</sub>Al.<sup>24,25</sup> On the other hand. Fig. 5 shows that the peaks in the HMF distribution increased slightly during ordering in Fe<sub>3</sub>Ge, whereas they remained unchanged during ordering in Fe<sub>3</sub>Al.<sup>24,25</sup> These peak shifts during ordering of Fe<sub>3</sub>Ge are small, however, and they suggest only small effects on the <sup>57</sup>Fe HMF distribution from 2nn and 3nn Ge atoms. Weak effects of 2nn or 3nn Ge atoms were found for those <sup>57</sup>Fe atoms with (0) 1nn Ge atoms, whose 2nn environment changes from about 1.5 2nn Ge atoms in the disordered state to nearly 6 Ge 2nn atoms in the ordered state. Measurements of 2nn HMF perturbations of dilute Fe-Ge allovs suggest that such a change would shift the (0) 1nn peak by +35 kG to a lower magnitude of HMF, but this is not observed. This trend could not be explained by changes in the 3nn shell-3nn Ge atoms tend to cause a positive HMF perturbation<sup>21,22</sup> but the number of 3nn Ge atoms around the minority Fe atoms decreases during ordering. A similarly weak effect of 2nn Al atoms was found previously for ordering in Fe<sub>3</sub>Al.<sup>25</sup>

The systematics of 1nn HMF perturbations in dilute Fe-Ge alloys<sup>21,22</sup> suggest that the main peaks in the <sup>57</sup>Fe HMF distribution should be separated by regular 23.2 kG intervals, as is common for many solutes in bcc Fe.<sup>26</sup> Figure 5 shows that this is not the case. Greater numbers of Ge atom neighbors cause progressively larger shifts. Stearns has attributed this trend to a saturation of the conduction electron polarization with increasing numbers of Fe neighbors.<sup>27</sup> We do not dispute this suggestion, but we can offer another possibility. The large local isomer shifts caused by 1nn Ge atoms imply large local changes in 4s electron density and polarization. Neighboring Ge atoms may alter the sensitivity of the <sup>57</sup>Fe HMF to neighboring magnetic moments. In the notation of the model of magnetic response in Refs. 10-12, this represents an effect of Ge atoms on the conduction electron response parameter,  $\alpha_{CEP}$ . It is possible to predict a nonlinearity in the positions of peaks in the HMF distribution through the indirect nonlocal contribution to the HMF,  $H_{INL}$  (Refs. 11, 12) but we do not yet know if this approach is realistic. We are now exploring this possibility and the further possibility that these nonlinear effects may be related to the weak effects of 2nn Ge atoms in partially ordered Fe-21 at. % Ge.

#### **IV. SUMMARY**

As-prepared sputtered films of Fe-21 at. % Ge (Fe-22 at. % Ge from Mössbaur spectrometry) were bcc polycrystals having a characteristic grain size of 17 nm and only some SRO characteristic of the  $DO_3$ -ordered structure. Upon annealing at progressively higher temprature, the first changes were a relaxation of stresses in the film, and some development of SRO. There was a simultaneous decrease in the magnetic coercive field, and a greater tendency of the magnetization to lie in the plane of the film. We believe this magnetic softening with low-temperature annealing is due primarily to stress relaxation in the sputtered films, since this change (and probably not the chemical ordering) is also consistent with observed changes in spin wave resonance modes. A minimum coercive field of 14 Oe was obtained after annealing at 250 °C.

After annealing at temperatures higher than 250 °C, the material underwent a significant grain growth and a strong development of  $D0_3$  order. There was a simultaneous increase in the magnetic coercive field, a decreased tendency of the magnetization to lie in the plane of the film, and a qualitative change in the spin wave resonance spectra. This correlation between grain growth and magnetic hardening is well explained by the random anisotropy model, assuming the ferromagnetic exchange length is 20–30 nm.

The qualitative features of Mössbauer spectra of Fe-21 at. % Ge could be well explained by the magnetic response model, in which the Ge atoms act as magnetic holes. The effects of 2nn Ge atoms on the HMF were much smaller than expected, however. We observed large local isomer shifts at  $^{57}$ Fe nuclei with 1nn Ge atoms, implying a strong loss of 4s down electrons at  $^{57}$ Fe nuclei.

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