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Multi-band remote sensing based retrieval model and 3D analysis of water depth in Hulun Lake, China

Changyou Li^a, Biao Sun^{a,*}, Keli Jia^a, Sheng Zhang^a, Weiping Li^b, Xiaohong Shi^a, Claudia M.d.S. Cordovil^c, Luis S. Pereira^c

^a College of Water Conservancy and Civil Engineering, Inner Mongolia Agricultural University, Hohhot, 010018, PR China
 ^b College of Environment & Energy Resources, Inner Mongolia Science & Technology University, Baotou, 014010, PR China
 ^c CEER - Biosystems Engineering, Institute of Agronomy, Technical University of Lisbon, Tapada da Ajuda, 1349-017 Lisbon, Portugal

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ABSTRACT

Hulun Lake, a large lake located on the cold and arid Hulunbeir grassland in the Inner Mongolia Autonomous Region, is the fifth largest in China and the largest in the north of the country. However, the information on the lake's characteristics (e.g., water depth versus surface area) is scarce in literature. Based on the lake's physiographic features, this study developed and used a model that merges the sunlight reflection band with the thermal infrared radiation band to simulate the lake's characteristics. The model verification and error analysis indicated an optimal model structure of logarithm. Thus, this logarithmic model was selected to analyze the spectral data. The results indicated that the model did a good job in reproducing observed water depths and accurately predicted the depths on 24 September 2007. This showed that this model can be reliably applied to the cold and arid region. Subsequently, the results were used to generate a triangular irregular network (TIN) model, which in turn was used to compute the functional relations between water level, surface area, and volume. The correlation between water level and volume is superior to that between water level and area. The regression equation developed in this study can be used to estimate the volume when water elevation is known.

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1. Introduction

Water depth, one of the basic parameters for the study of a lake environment, is conventionally measured using a positioning device mounted on a boat. The example devices are a surveying rod, plummet, ecosounding, and sonar. However, because the number of measuring points (i.e., nodes) cannot be too large and may limit conditions of field operations, the measured data have general limitations in representing the true terrain of the lake bottom. With the 3S (i.e., remote sensing, global positioning system, and geographic information system) technology advancement and maturing, its has been applied to many fields (e.g., [1–3]). One of applications is to use remote sensing to indirectly measure water depth. This indirect method uses space satellite sensors to receive the sunlight's reflection and the self-thermal radiation of a water body. Subsequently, the satellite data are processed to retrieve water depth.

The available retrieval models can be classified into theoretical, semi-theoretical–empirical, and statistical correlation [4]. The first two types of models have not been widely used in practice because the optical parameters relevant to water body and required by those models cannot be determined and because the timings of other measurable parameters may not be coincident with those of satellite data. As a result, the current literature is dominated by researches conducted using

* Corresponding author. Tel.: +86 13404843412.

E-mail addresses: sunbiao_label@yahoo.com.cn, label2003@163.com (B. Sun).





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Fig. 1. Map showing the location of Hulun Lake.

statistical correlation models (e.g., [5–8]). These researches were mainly conducted for shallow seas located in humid areas (e.g., [9,10]), using images taken in summer and with wavelengths of solar radiation. In contrast, there are few research literatures about lakes in cold and arid regions, and few literatures about retrieving the water depth using the thermal infrared band. Currently, the applications about thermal infrared remote sensing are mainly concentrated on soil moisture and drought monitoring, etc. [11].

Three-dimensional terrain analysis/visualization is the new development trend of the 3S technology [12] and can more intuitively and accurately present true terrains than the information of two-dimensional data. Nowadays, the visualization is mainly applied to the fields of virtual geographic environments, digital city construction and land management and utilization, among others [13,14].

The study area was Hulun Lake located in the cold and arid region of northern China. Using the Landsat TM/ETM+ satellite images taken in periods between late autumn and early winter and the corresponding measured data on water depth, this study developed a water depth retrieval model that merges the solar reflection band and infrared thermal radiation band. After the simulation for verification and error analysis, the bottom topography data of Hulun Lake was further calculated. The modeling results and the measured point data on the terrain were conjunctively used to generate a 3D TIN model, which to the visual operation and spatial analysis, obtain the relationships between the bottom topography of the lake and the hydrologic characteristics.

2. Materials and methods

2.1. Study area

Hulun Lake, the fifth largest lake in size in China, has geographical coordinates between 116°58′E and 117°48′E and between 48°33′N and 49°20′N (Fig. 1). Towards the east are the Xing'anling Mountains and the west and south is the Mongolian Plateau. The lake has a geometric shape of an irregular oblique rectangle, with a northeast–southwest axis. The lake has a maximum length of 93 km and a maximum width of 41 km, an annual average surface area of 2054 km², and an average water depth of about 5 m. The area is located in the semi-arid continental temperate monsoon zone, which has an annual average precipitation of 233 mm and an annual average evaporation of 1446 mm [15]. Hulun Lake is part of the Argun River water system and the majority of water is supplied by precipitation as well as by several rivers including the Kelulun River with headwaters in the Kente Mountains of the Mongolian People's Republic, the Wuerxun River shared by Beier Lake and Hulun Lake, and the Xinkai River (nicknamed Dalaneluomu River). The Xinkai River, located in the northeast of Hulun Lake, can have dual flow directions: towards Hulun Lake when the Hailar River has a higher water level but towards the Argun River when Hulun Lake has a higher level [16].

Hulun Lake, with a large water surface area and nicknamed the "Prairie Pearl", is located on the Hulunbeir grassland of the Inner Mongolia Autonomous Region. The Hulunbeier grassland had plenty of water and lush grass, and is one

of the Chinese high-quality natural pastures and an important animal husbandry production base. Hulun Lake and the surrounding grasslands, totally about 7400 km² in size, were designated a Provincial Nature Reserve in 1990, approved as a National Nature Reserve in 1992, listed by the United Nations as an International Importance Wetland in January 2002, and were nominated as a World Biosphere Reserve member by the United Nations Educational Scientific and Cultural Organization (UNESCO) Man and the Biosphere Program in November 2002 [17,18]. Along with the Hulunbeier grassland and Daxinganling forest, Hulun Lake functions as an important ecological protection barrier in northern China and plays important roles in maintaining the regional biological diversity, protecting the ecological security of northern China and even Huabei District, and promoting sustainable economic and social development [19,20]. Since 2000, because of the interactive impacts of various natural and human factors, the water supplement to Hulun Lake has become much less than the water consumption. As a result, the lake level has been dropping from year to year, which has seriously impacted the lake's fisheries and its surrounding ecological health. This also resulted in the continuous deterioration of the Hulunbeier grassland environment. The objective of this study was to determine the water depths and the bottom terrains of Hulun Lake, providing the scientific information that can be used to develop lake protection measures.

2.2. Model principles

2.2.1. Sunlight reflection

The light radiation to a water body is either absorbed or reflected by water. As a result, the radiation tends to fade away with the increase of water depth. The radiation that reaches the lake bottom and is reflected back is subject to further losses to water absorption and reflection, and the remaining radiation will pass through the atmosphere to reach the space sensor. These processes can be mathematically described as [21]:

$$L_i = L_{i\infty} + C_i R_B(\lambda) e^{-k_i J Z} \tag{1}$$

where L_i is the *i* band radiation received by the sensor; C_i is a constant dependent on solar irradiance, atmospheric and water transmittance, and water surface refraction; $L_{i\infty}$ is the radiation into the deep water zone; R_B is the reflectance at the bottom of the water body; λ is the solar radiation; k_i is the attenuation coefficient of the water body; *f* is the path length of the water body (usually taken as 2); *Z* is the water depth.

This model assumes that the light radiation received by the sensor is inversely proportional to water depth. The premises of the model are that the bottom reflectance is large and that the water is clear and shallow. These premises can impose application limitations of the model. To relax these limitations, Wei et al. [22] proposed a new remote sensing based retrieval method expressed as:

$$Z = -\frac{1}{k} \ln\left(1 - \frac{L_i - B}{A}\right) \tag{2}$$

where A and B are two coefficients, which can be determined based on observed Z and L_i .

Based on the *e* exponential an optical exponential attenuation model was proposed. This model requires two or more different bands and assumes a constant reflectance at the bottom. This multi-band retrieval model is independent of the bottom geometry and expressed as:

$$Z = A_0 + A_1 B_1 + A_2 B_2 + \dots + A_n B_n \tag{3}$$

where $B_i = \ln(L_i - L_{\infty})/k_i$; A_i are coefficients and can be defined by regressing measured water depths and radiation pixel values.

2.2.2. Lake thermal radiation

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In terms of the principle of thermal convection and because the atmosphere temperature in autumn is lower than the lake surface water temperature, the heat in the water will be transferred into the atmosphere through the water–air interface. The lowered temperature of lake surface water will increase the density and then sink, at the same time, causing the warmer and lighter water in the deep lake to rise. This will result in the vertical convection and mixing between the upper and lower lake water layers. This convection process can make the surface water temperature of a deep water area higher than that of shallow water area. The variation of lake surface water temperature with water depth can be described using the following mathematic equations [23].

Assume the heat is transferred from lake water to the ambient atmosphere and that the transferring rate per unit area is proportional to the water–air temperature difference, i.e.,

$$\frac{dQ}{dt} = -\gamma (T - T_a) \tag{4}$$

where γ is a heat exchange coefficient related to air temperature and wind speed; *T* and *T_a* are the temperatures of the lake water and the ambient atmosphere, respectively.



Fig. 2. The map showing the measurement points.

The temperature of lake water will fall due to the heat loss. The water cooling rate is proportional to the heat exchange rate and the relationship can be expressed as:

$$\frac{dT}{dt} = \frac{1}{cZ \cdot \left(\frac{dQ}{dt}\right)} \tag{5}$$

where *c* is the specific heat of water; *Z* is the water depth.

Solving Eqs. (4) and (5) simultaneously gives:

$$T = T_a + (T_0 - T_{a0}) \cdot \exp\left(\frac{-\gamma t}{cZ}\right)$$
(6)

where T_0 and T_{a0} are the initial temperatures of the water and atmosphere, respectively.

To more clearly comprehend the physical significance of Eq. (6), take the increment of surface lake water temperature distribution rewritten to the increment of water depth, expressed as:

$$\Delta T(Z) = A(Z)\Delta Z; A(Z) = (T_0 - T_{a0}) \cdot \frac{\gamma t}{cZ^2} \cdot \exp\left(-\frac{\gamma t}{cZ}\right)$$
(7)

where A(Z) is the temperature–water depth resolution coefficient, defined as the water surface temperature change as a result of per unit change of water depth. It is an indicator of the ability to use thermal infrared images to determine water depth.

2.3. Data and preprocessing

In terms of the physiographic features of Hulun Lake, this study used a multi-band statistical model to retrieve water depth. The number of samplings (i.e., the number of measurement nodes) determines whether the measured data can represent the true terrains of the lake bed. However, the data on water depth were scarce for Hulun Lake: 8 measurements in 1988; 9 in 1991; 13 in September 2008; and 11 in December 2008. These 41 measurements have no replicate in the position (Fig. 2). The 1988 and 1991 data were measured in the winter by the Hulun Lake Fishery; while the 2008 data were measured in September and December using a surveying plummet by an Inner Mongolia Agricultural University research team.

Table 1

The water level differences of the adjustment years relative to the year of 2008.

Adjustment period	Winter 1988	Winter 1991	18 Oct. 1990	15 Sep. 1998	17 Oct. 2001	7 Oct. 2006	24 Sep. 2007
Water level variation (m)	2.8	3.7	3.68	3.68	2.9	0.82	0.4

Table 2

The pooled data on the adjusted water depths.

Year	Point	Original measurement (m)	Adjusted water depth (m)	Adjusted water depth for the other years (m)				
				18 Oct. 1990	15 Sep. 1998	17 Oct. 2001	7 Oct. 2006	24 Sep. 2007
	1	5.1	2.3	5.98	5.98	5.2	3.12	2.7
	2	6.55	3.75	7.43	7.43	6.65	4.57	4.15
	3	5.4	2.6	6.28	6.28	5.5	3.42	3
Winter 1000	4	6.3	3.5	7.18	7.18	6.4	4.32	3.9
Winter 1988	5	6.55	3.75	7.43	7.43	6.65	4.57	4.15
	6	5.8	3	6.68	6.68	5.9	3.82	3.4
	7	4.1	1.3	4.98	4.98	4.2	2.12	1.7
	8	6.05	3.25	6.93	6.93	6.15	4.07	3.65
	1	6	2.3	5.98	5.98	5.2	3.12	2.7
	2	4.6	0.9	4.58	4.58	3.8	1.72	1.3
	3	5.4	1.7	5.38	5.38	4.6	2.52	2.1
	4	7.5	3.8	7.48	7.48	6.7	4.62	4.2
Winter 1991	5	7.2	3.5	7.18	7.18	6.4	4.32	3.9
	6	7.2	3.5	7.18	7.18	6.4	4.32	3.9
	7	7.18	3.48	7.16	7.16	6.38	4.3	3.88
	8	5.9	2.2	5.88	5.88	5.1	3.02	2.6
	9	6.4	2.7	6.38	6.38	5.6	3.52	3.1
	D71	3.38	3.38	7.06	7.06	6.28	4.2	3.78
	D72	3.26	3.26	6.94	6.94	6.16	4.08	3.66
	D73	3.28	3.28	6.96	6.96	6.18	4.1	3.68
	F51	3.42	3.42	7.1	7.1	6.32	4.24	3.82
	F52	3.24	3.24	6.92	6.92	6.14	4.06	3.64
	F53	3.3	3.3	6.98	6.98	6.2	4.12	3.7
Sep. 2008	G22	2.64	2.64	6.32	6.32	5.54	3.46	3.04
	G23	3.16	3.16	6.84	6.84	6.06	3.98	3.56
	H41	3.22	3.22	6.9	6.9	6.12	4.04	3.62
	G81	3.1	3.1	6.78	6.78	6	3.92	3.5
	F7	2.92	2.92	6.6	6.6	5.82	3.74	3.32
	C8	3.52	3.52	7.2	7.2	6.42	4.34	3.92
	D9	3.31	3.31	6.99	6.99	6.21	4.13	3.71
	A10	1.88	1.88	5.56	5.56	4.78	2.7	2.28
	D11	3.1	3.1	6.78	6.78	6	3.92	3.5
	D7	3.36	3.36	7.04	7.04	6.26	4.18	3.76
	E8	3.7	3.7	7.38	7.38	6.6	4.52	4.1
	F5	3.67	3.67	7.35	7.35	6.57	4.49	4.07
Dec. 2008	F9	2.9	2.9	6.58	6.58	5.8	3.72	3.3
	G8	3.08	3.08	6.76	6.76	5.98	3.9	3.48
	H3	3.12	3.12	6.8	6.8	6.02	3.94	3.52
	I2	0.85	0.85	4.53	4.53	3.75	1.67	1.25
	15	1.96	1.96	5.64	5.64	4.86	2.78	2.36
	H5	3.47	3.47	7.15	7.15	6.37	4.29	3.87

As mentioned above, Hulun Lake is located on the Inner Mongolia Plateau. The strong wind in summer can induce large waves, whereas, the lake temperature rapidly drops by the end of September and in early October because the weather starts to cool down. Based on the aforementioned retrieval principle (Eqs. (4) and (5)), the thermal infrared remote sensing images taken between late autumn and early winter are preferred because of the large water–air temperature difference as well as the rapid drop of the lake water temperature. Hence, this study used the high-quality Landsat TM images taken on 18 October 1990, 15 September 1998, 7 October 2006 and 24 September, 2007, and the ETM+ image taken on 17 October 2001.

Once measured data of water depth was less and not enough to constitute a modeling point, and its timings of measurement were hardly coincident with the generated time of satellite images. In order to increase the number of modeling points and using all water depth data to generate a time of satellite images, in the case of neglecting the sedimentation velocity of the lake's bottom, the water level variation for different times in 2008 (Table 1) was calculated. Then water level variation for a year (e.g., 1988) was subtracted from the original measurements on the dates of that year (the third column in Table 2) to get the adjusted water depths (columns 4–9 in Table 2), while the original measurements for 2008 were not adjusted. The adjusted 30 data points in the years of 1988, 1991, and September 2008 were used to build the model, while the 11

Table 3	
Correlation coefficients of the water depths with bands. ^a	

Image time	Band 1	Band 2	Band 3	Band 4	Band 5	Band 6	Band 7
1990-10-18	0.618	0.634	0.617	0.311	0.046	0.320	0.116
1998-09-15	0.673	0.646	0.707	0.459	0.079	0.518	-0.466
2001-10-17	0.610	0.559	0.661	0.510	-0.012	0.530	-0.163
2006-10-07	0.369	0.518	0.452	0.564	0.094	0.671	0.080
2007-09-24	0.898	0.889	0.865	0.799	-0.215	0.748	0.107

^a Bands 1–5 and 7 are the sunlight reflection; bands 1, 2, and 3 are the blue–green, green, and red, respectively; band 4 is the near-infrared; bands 5 and 7 are the short-infrared; band 6 is the thermal infrared.

adjusted data points in December 2008 were used to verify the model. The water level data were measured by the Hulun Lake experiment station.

3. Results and discussion

The five-year water depths were found to be well correlated with bands 1, 2, 3, 4, and 6 (Table 3). These correlations were stronger than those between the water depths and the ratios of any one band to another (e.g., bands 1–2, bands 3–4, etc.). The final model was selected by examining the combinations of logarithmic (or arithmetic) values of the reflection bands (i.e., bands 1, 2, 3, and 4) with logarithmic (or arithmetic) values of the thermal infrared band (i.e., band 6). That is, the final model was selected by evaluating four initial models, designated Model I, Model II, Model III, and Model IV, respectively.

Model I: Arithmetic Values of the Reflection Bands + Arithmetic Values of the Thermal infrared band:

$$Z = A_0 + A_1 B_1 + A_2 B_2 + A_3 B_3 + A_4 B_4 + A_6 B_6.$$
(8)

Model II: Arithmetic Values of the Reflection Bands + Logarithmic Values of the Thermal Infrared Band:

$$Z = A_0 + A_1 B_1 + A_2 B_2 + A_3 B_3 + A_4 B_4 + A_6 \ln B_6.$$
⁽⁹⁾

Model III: Logarithmic Values of the Reflection Band + Arithmetic Values of the Thermal Infrared Band:

$$Z = A_0 + A_1 \ln B_1 + A_2 \ln B_2 + A_3 \ln B_3 + A_4 \ln B_4 + A_6 B_6.$$
 (10)

Model IV: Logarithmic Values of the Reflection Bands + Logarithmic Values of the Thermal Infrared Band:

$$Z = A_0 + A_1 \ln B_1 + A_2 \ln B_2 + A_3 \ln B_3 + A_4 \ln B_4 + A_6 \ln B_6.$$
⁽¹¹⁾

The results from using a least-square method to fit each of these four models to the five-year data are presented in Table 4. Although the correlation coefficients for the model construction periods were generally lower than those for the model verification period, the root mean squared errors for the model construction periods were consistently smaller. The higher correlation coefficients for the model verification period are because of the fewer verification sample points. Overall, all four models had a comparable performance while Model IV (Fig. 3) was superior to the other three models and thus selected as the final optimal model. The sequential performance of the final optimal model (i.e., Model IV) was 24 September 2007, 15 September 1998, 7 October 2006, 18 October 1990, and 17 October 2001, consistent with correlation coefficient in Table 3.

For the five years, the final model has the following structures:

(1) 18 October 1990:

$$Z = 4.85 \ln B_1 + 7.01 \ln B_2 + 5.02 \ln B_3 + 0.85 \ln B_4 + 1.78 \ln B_6 - 63.05.$$
(12)

(2) 15 September 1998:

$$Z = 0.18 \ln B_1 - 0.84 \ln B_2 + 5.82 \ln B_3 - 2.32 \ln B_4 + 30.67 \ln B_6 - 150.23.$$
(13)

(3) 17 October 2001:

$$Z = 12.37 \ln B_1 + 9.06 \ln B_2 + 2.5 \ln B_3 + 0.32 \ln B_4 + 10.22 \ln B_6 - 139.44.$$
(14)

(4) 7 October 2006:

$$Z = -5.73 \ln B_1 + 3.56 \ln B_2 + 5.41 \ln B_3 + 1.17 \ln B_4 + 28.26 \ln B_6 - 137.92.$$
(15)

(5) 24 September 2007:

$$Z = 4.5 \ln B_1 + 2.28 \ln B_2 + 3.08 \ln B_3 - 1.39 \ln B_4 + 11.02 \ln B_6 - 81.76.$$
⁽¹⁶⁾

Date	Model	Model construction		Model verification		
		Correlation coefficient	Root mean squared error (m)	Correlation coefficient	Root mean squared error (m)	
	Ι	0.6946	0.4033	0.8549	0.4483	
19 October 1000	II	0.6945	0.4000	0.8548	0.4500	
18 October 1990	III	0.6996	0.4000	0.8648	0.4600	
	IV	0.6996	0.4000	0.8648	0.4600	
	Ι	0.7827	0.3225	0.8096	0.3300	
15 Contombor 1009	II	0.7833	0.3220	0.8096	0.3304	
15 September 1998	III	0.7824	0.3242	0.8106	0.3229	
	IV	0.7831	0.3237	0.8106	0.3233	
	Ι	0.8058	0.3463	0.6355	0.6017	
17 October 2001	II	0.8059	0.3461	0.6363	0.6011	
17 October 2001	III	0.8096	0.3429	0.6424	0.5939	
	IV	0.8097	0.3427	0.6433	0.5934	
	Ι	0.6936	0.3983	0.8087	0.4245	
7 October 2000	II	0.6840	0.3977	0.6009	0.4221	
7 October 2006	III	0.7029	0.3929	0.8070	0.4235	
	IV	0.7038	0.3924	0.8086	0.4212	
	Ι	0.9266	0.2168	0.9285	0.2838	
24 Sontombor 2007	II	0.9280	0.2167	0.9304	0.2800	
24 September 2007	III	0.9267	0.2167	0.9284	0.2835	
	IV	0.9281	0.2166	0.9303	0.2797	



Fig. 3.	Plots showing the	measured vs. p	predicted water	depths by the	e final model (i.	.e., Model IV)
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Separation of the land and water for satellite image data used masks in ENVI software, receiving image data of pure water area in Hulun Lake, then to do Band Math using Eqs. (12)-(16), acquiring the water depths distribution maps (Fig. 4(a)-(e)).

Table 4

Performance statistics of the final model.



Fig. 4. The modeled water depths and lake water surface boundary.

Because the inflow into Hulun Lake has been decreasing since 1999, the lake level has been noticeably dropping from year to year and the cumulative decrease from 1999 to 2008 was 4 m. In accordance, the lake water surface boundary has been shrinking as well, as evidenced by the six lines in Fig. 4(f) that from the outside to the inside show the lake surface extension in 1999, 2002, 2004, 2005, 2007, and 2008, respectively. The modeled water depth distributions across the lake were similar except for 15 September 1998 (Fig. 4(a)–(e)). The noticeable discrepancies occurred in the lower-left half-closed lake bays, where the constrained flow convection and distinctly different water solutes might distort the spectral characteristics. As a result, the retrieved water depths were likely to have large errors. Nevertheless, the retrieved water depths for 24 September 2007 were close to the measured values and thus can be considered as the true water depths in Hulun Lake.

The retrieved water depths for 24 September 2007 (Fig. 4(e)) were vectorized using Arc GIS 9.2, with a 0.3 m water depth interval to achieve maximum accuracy. The lake bottom elevation beneath a given water depth contour was computed as the subtraction of the lake surface elevation to the contour value. The vectorized map was stored in a shape file format.

The water–land boundaries presented by the Landsat TM/ETM+ images taken from 1999 to 2009 were extracted using the method maximum likelihood provided by the ENVI software and stored as another shape file.

These two shape themes were overlaid in Arc GIS 9.2 to generate a TIN model of the lake (Fig. 5). The TIN model is displayed with a vertical exaggeration factor of 400 because the horizontal dimensions of 90 km long and 40 km wide are a magnitude larger than the maximum water depth of 8 m.

Analysis TIN model used 3d analysis tool in Arc GIS, to calculate area and volume in different water levels (Table 5), the relationships of water level, area, and volume shown in Fig. 6.

The quadratic regression equations presented in Fig. 6(b) can be used to more accurately determine the volume of Hulun Lake for a given water level. As an example application, the lake surfaces for the water levels of 545, 544, 543, 542, 541, 540, 539, and 538 m were derived and are shown in Fig. 7.



Fig. 5. The TIN model of the Hulun Lake bottom.

Table 5

The computed relationships of water level, area, and volume of Hulun Lake.

Water level (m)	$Area(km^2)$	Volume (10 ⁸ m ³)
545.0	2086.11	121.04
544.5	2072.65	110.64
544.0	2054.20	100.33
543.5	2031.30	90.10
543.0	1997.33	80.03
542.5	1954.74	70.15
542.0	1913.16	60.49
541.5	1844.46	51.09
541.0	1761.67	42.14
540.5	1724.21	33.43
540.0	1667.66	24.95
539.5	1546.92	16.89
539.0	1348.65	9.60
538.5	846.19	3.87
538.0	328.07	1.17



Fig. 6. Plots showing (a) water level vs. area and (b) water level vs. volume.

4. Conclusion

In terms of the physiographic characteristics of lakes in cold and arid regions, this study developed a multi-band water depth retrieval model that merges the sunlight reflection band with the thermal infrared radiation band. The thermal infrared band was selected because between late autumn and early winter the water–air temperature difference is large C. Li et al. / Mathematical and Computer Modelling 58 (2013) 771-781



Fig. 7. 3D maps showing the derived lake surfaces of Hulun Lake at various water levels.

and the lake temperature drops more dramatically. The model merges four reflection bands 1, 2, 3 and 4, and one thermal infrared band 6. The final model took the logarithmic of these five bands as independent variables. The simulation results indicated that the model performed best for 24 September 2007 and that the model is applicable for the cold and arid region of northern China. In addition, this study derived a TIN model of the Hulun Lake bottom and regression equations of elevation, area, and volume of Hulun Lake. Compared with the existing computational method, these equations can be used to more accurately compute the lake volume for a given level. Further, this study first mapped the lake bed terrain as well as boundaries of various water levels.

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