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# Structural Evolution of Gold-Doped Bismuth Clusters $AuBi_n^-$ (n = 4-8)

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#### Abstract

The structures of gold-doped bismuth clusters,  $AuBi_n^-$  (n = 4-8), are investigated through a joint photoelectron spectroscopy and density functional theory (DFT) study. Well-resolved photoelectron spectra are obtained at several photon energies. Global minimum searches coupled with DFT calculations yield low-lying structures, whose relative energies are further evaluated by single-point energy calculations at the CCSD(T) level of theory. Vertical detachment energies are calculated with the inclusion of spin–orbit effects to compare with the experimental data. Three-dimensional structures are found to be dominant in this size range, while a planar low-lying isomer is observed only for  $AuBi_4^-$ . The  $AuBi_6^-$  cluster possesses a

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"bow-tie-like" global minimum structure. Major isomers of the other clusters studied here can all be viewed to possess this structural motif. The gold dopant favors increasingly higher coordination with bismuth in AuBi<sub>n</sub><sup>-</sup> (n = 4-8). Chemical bonding analyses are performed to understand the geometric and electronic structure evolution of these bimetallic clusters. The gold atom interacts with neighboring bismuth atoms via localized  $\sigma$  bonds at low-coordination sites but via delocalized  $\sigma$ bonds at high-coordination sites. Greater charge transfer from Bi to Au is found for higher-coordinated Au. Molecular dynamics simulations indicate that the assigned global minimum of AuBi<sub>7</sub><sup>-</sup> is a highly stable structure, whereas the minor isomer of AuBi<sub>7</sub><sup>-</sup> displays a fluxional behavior.

#### Introduction

Clusters exhibit unique size-dependent physical and chemical properties that differ from their bulk counterparts. These size-dependent properties in bimetallic clusters depend on various factors such as additional degrees of freedom and composition, chemical interactions among different elemental atoms, or other alloying effects, which may result in increased stability or improved catalytic activity.<sup>1–5</sup> Hence, bimetallic clusters have attracted increasing attention because of their higher flexibility in attaining tunable properties. In this article, we present a joint experimental and theoretical study of bismuth anions doped with single gold atom, AuBi<sub>p</sub><sup>-</sup> (n = 4-8).

Bismuth nanoparticles have been shown to exhibit size-dependent superconductivity.<sup>6</sup> The electronic structures and bonding characters of Bi clusters (neutral, anionic, and cationic) have been investigated by photoelectron spectroscopy (PES)<sup>7–14</sup> and theoretical calculations.<sup>15–20</sup> There have been few combined experimental and theoretical studies on bismuth clusters. Gausa et al. performed both PES measurement and theoretical calculations for anionic bismuth clusters and reported a roof-like and a planar ring structure for bismuth tetramer and pentamer, respectively.<sup>21</sup> Kelting et al. used both gas-phase ion mobility spectrometry and trapped-ion diffraction measurements along with density functional theory (DFT) calculations to probe the structures of small-sized bismuth cluster cations.<sup>22</sup> Overall, small bismuth clusters are shown to exhibit more compact structures, whereas the larger clusters are more open and they are formed by the combination of four-, six-, or eight-atom clusters.

There have been numerous investigations on bismuth clusters doped with main group elements,<sup>5,23-32</sup> and a few theoretical studies of bimetallic clusters of bismuth with transition metals have been reported.<sup>33-36</sup> Specifically, recent articles of copper–bismuth binary systems provide an insight into the intermetallic dynamics.<sup>37,38</sup> Also, the combined experimental and theoretical study for tin–bismuth clusters was reported by Heiles et al.<sup>39,40</sup> Bimetallic cluster with gold<sup>41-45</sup> has attracted more attention as small gold clusters are known to possess unique catalytic properties.<sup>46</sup> We are aware of only two theoretical studies on neutral gold–bismuth clusters.<sup>35,36</sup> Our previous PES study of AuBi<sup>-</sup> and BiBO<sup>-</sup> revealed similarity in the electronic structure and bonding of gold and boronyl to bismuth.<sup>31</sup>

Here, we report the first combined PES and theoretical investigation of gold-doped bismuth anion clusters  $AuBi_n^-$  (n = 4-8). The structure evolution in these small bimetallic clusters has been elucidated. Knowledge obtained from this study will pave the way for future studies of larger and more complex bimetallic Au-Bi clusters, which may exhibit novel chemical and physical properties.

#### Methods

**Experimental Method.** The experiments were performed using a magnetic-bottle PES apparatus equipped with a laser vaporization supersonic cluster source, details of which have been published else-where.<sup>47,48</sup> Briefly, bimetallic gold–bismuth cluster anions were produced by laser vaporization of an Au/Bi mixed target. A high-pressure helium carrier gas seeded with 5% argon was used to quench the plasma, initiate nucleation, and cool the clusters via supersonic expansion. The gold–bismuth cluster anions were extracted perpendicularly from the cluster beam and analyzed by a time-of-flight mass spectrometer. Clusters of interest were mass-selected, decelerated, and photodetached by the 193 nm (6.424 eV) radiation from an ArF excimer laser and the fourth harmonic (266 nm, 4.661 eV) and third

harmonic (355 nm, 3.496 eV) from a Nd:YAG laser. Photoelectrons were collected at nearly 100% efficiency by a magnetic bottle and analyzed in a 3.5 m long electron flight tube. Photoelectron spectra were calibrated using the known spectra of Au\_ and Bi\_. The energy resolution of the apparatus was  $\Delta E_k/E_k \approx 2.5\%$ , that is, approximately 25 meV for 1 eV electrons, where  $E_k$  is the kinetic energy and  $\Delta E_k$  is the change in kinetic energy of the electron.

**Theoretical Methods.** Global optimization with the basin-hopping (BH) method<sup>49,50</sup> combined with DFT is used to search the low-lying and global minimum structures of each cluster. For the BH-DFT search, we used generalized gradient approximation (GGA) with the Perdew–Burke–Ernzerhof (PBE)<sup>51</sup> exchange correlation functional and double numerical polarized basis set as implemented in DMOL 4.0 program.<sup>52</sup> We used several initial geometries and employed  $1.0 \times 10^{-6}$  Hartree energy convergence,  $2 \times 10^{-3}$  Å gradient convergence, and  $5.0 \times 10^{-3}$  Å displacement convergence for geometry optimization.

Top 10–15 low-lying isomers obtained from the BH search were considered as the candidates for the global minimum. These candidates were reoptimized using meta-GGA M06 functional<sup>53</sup> and the aug-cc-pVTZ (effective core potential, ECP)54-56 basis set, as implemented in Gaussian 09 package.<sup>57</sup> We optimized these isomers at the lowest spin multiplicity as well as two higher multiplicities. Frequency calculations were done to verify that the isomers were true minima on the potential energy surface. The inclusion of spin-orbit (SO) effects is essential for both gold and bismuth,<sup>30,58</sup> and previous studies on gold or gold-doped clusters have shown that inclusion of SO effects provided quantitatively better theoretical data for comparison with experimental PES spectra.<sup>59-61</sup> Next, single-point energies of these candidate isomers were calculated at the SODFT level using the PBE0 functional<sup>62</sup> and the CRENBL (ECP)<sup>63</sup> basis set, as implemented in the NWCHEM 6.3 package.<sup>64</sup> The SO effects were included for both gold and bismuth in these calculations.<sup>63</sup>

The first vertical detachment energy (VDE) of a cluster was calculated as the energy difference between the neutral and anionic clusters at the optimized structure of the anion. The higher VDEs were calculated by adding vertical excitation energies to the first VDE. Each VDE was then fitted with a unit-area Gaussian of 0.05 eV width to yield the simulated PES spectrum. The global minimum structure was identified by comparing the experimental PES spectrum with the simulated spectra of the low-lying isomers. We also performed coupledcluster calculations [CCSD(T)] with the aug-cc-pVDZ (ECP) basis set to support the credibility of the assigned isomers. Further, for a quantitative support, we calculated the root-mean-square deviation (rmsd) for the assigned major isomers. We aligned the first peak of the simulated spectra with experimental first VDE and calculated the rmsd of next three peaks of the simulated spectra with respect to the corresponding experimental peaks. The overall theoretical approaches appear to be quite reliable in identifying the global minimum clusters even in the cases where the simulated spectra of more than one candidate isomer exhibit resemblance to the experimental spectrum, as also shown previously.<sup>59–61</sup> Additionally, for two AuBi<sub>7</sub><sup>-</sup> isomers, we performed Born- Oppenheimer molecular dynamic (BOMD) simulations at 300 and 260 K for 5 ps with a time step of 1 fs, using the CP2K software.65 We also performed chemical bonding analyses using the AdNDP<sup>69</sup> method at the PBE0/Def2-TZVP (ECP) level of theory.

#### **Results and Discussion**

The experimental photoelectron spectra of  $AuBi_n^-$  (n = 4-8) are shown in **Figures 1 and 2** at three detachment photon energies: 355 nm (3.496 eV), 266 nm (4.661 eV), and 193 nm (6.424 eV). Many detachment transitions were observed for each cluster and were labeled by letters.

The X band in each spectrum represents the transition from the ground state of the anion to that of the neutral, whereas bands A, B, ... stand for the transitions to the excited states of the neutral species. Weaker features labeled with X', A', B', ... indicate they are from minor isomers. The experimental first VDEs and the energy gap (energy difference between X and A peaks) are given in **Table 1**, along with the theoretical first VDEs and relative energies calculated at the CCSD(T) level of theory for the top candidates. The considerable shift to the lower binding energy side is normally observed in the theoretical VDEs with respect to the experiment and is attributed to the SO coupling used for the theoretical calculations.



**Figure 1.** Photoelectron spectra of  $AuBi_4^-$  at (a) 355 nm, (b) 266 nm, and (c) 193 nm;  $AuBi_5^-$  at (d) 355 nm, (e) 266 nm, and (f) 193 nm; and  $AuBi_6^-$  at (g) 355 nm, (h) 266 nm, and (i) 193 nm detachment photon energies.



**Figure 2.** Photoelectron spectra of  $AuBi_7^-$  at (a) 355 nm, (b) 266 nm, and (c) 193 nm and  $AuBi_8^-$  at (d) 355 nm and (e) 266 nm detachment photon energies.

**Table 1.** Experimental First VDE (eV) labeled X and X' in Figure 1 and 2, the Energy Gap (eV) between Bands Labeled X and A or Bands Labeled X' and A' in Figure 1 and 2 for  $AuBi_n^-$  (n = 4–8), Theoretical First VDE, Point Group, and Relative Energies eV at CCSD(T)/aug-cc-pVDZ (ECP) Level for Top Isomers of  $AuBi_n^-$  (n = 4–8)

	Experimental		Theoretical			
	VDE	gap	isomer	VDE	point group	$\Delta E$
AuBi <sub>4</sub> -	2.29 (X')	0.56	I	1.83	C <sub>2v</sub>	0.00
	2.45 (X)	0.68	II	1.98	$D_{2h}$	0.16
			III	2.35	$C_{s}$	0.17
AuBi₅⁻	2.28 (X)	0.70	I	1.96	$C_{s}$	0.00
	□2.0 (X′)	□0.6	П	1.93	$C_{s}$	0.11
AuBi <sub>6</sub> ⁻	2.73 (X)	0.28	I	2.26	$C_{s}$	0.00
			II	2.47	$C_{2v}$	0.30
AuBi <sub>7</sub> -	1.91 (X)	0.90	I	1.54	C <sub>1</sub>	0.00
	2.16 (X')	0.39	II	1.74	$C_{s}$	0.08
AuBi <sub>8</sub> ⁻	2.78 (X)	0.19	I	2.36	$C_{s}$	0.00
			II	2.19	$C_1$	0.18
			III	1.98	C <sub>1</sub>	0.20

In **Figures 3 and 4**, the simulated spectra of the top two or three lowest-lying isomers are compared with the experimental spectrum of each anionic cluster. The structures and simulated spectra of other low-lying isomers are presented in the Supporting Information.



**Figure 3.** Comparison of the experimental photoelectron spectra (red) of (a)  $AuBi_4^-$ , (b)  $AuBi_5^-$ , and (c)  $AuBi_6^-$  with simulated spectra (black) of the top candidate isomers (insets display the corresponding isomer structures).



**Figure 4.** Comparison of the experimental photoelectron spectra (red) of (a)  $AuBi_7^-$  and (b)  $AuBi_8^-$  with simulated spectra (black) of top candidate isomers (insets display the corresponding isomer structures).

**AuBi**<sub>4</sub><sup>-</sup>. The 355 nm spectrum of AuBi<sub>4</sub><sup>-</sup> (Figure 1a) displays two relatively weak bands (X' and A') and three intense bands (X, A, and B). The 266 nm spectrum (Figure 1b) is quite congested at the higher binding energy side. The 193 nm spectrum (Figure 1c) reveals three prominent bands (H–J) and two weak bands (K and L). The spectra of AuBi<sub>4</sub><sup>-</sup> indicate that they are from two potential isomers populated in the cluster beam.

Figure 3a presents the theoretical spectra of the three lowest-lying isomers I, II, and III (energy ranking is based on the CCSD(T)/augcc-pVDZ (ECP) level of theory). Isomer I is the lowest-energy isomer among the selected top candidates at both PBE0/CRENBL (ECP) level and CCSD(T)/aug-ccpVDZ (ECP) level of theory (Table S1). The other two isomers are slightly higher (~0.16 eV) in energy at the CCSD(T)/ aug-cc-pVDZ (ECP) level than isomer I while almost degenerate with one another. Despite a systematic shift of around 0.45 eV, isomers I and II can reproduce the X'-A' and X-A gaps, as well as almost all the main bands. Isomer III can be responsible for the weak features (such as C and D) in the experimental spectrum. Consequently, all three isomers should be present in the cluster beam. Other candidates were easily ruled out because of their relatively high energy at the CCSD(T)/ aug-cc-pVDZ (ECP) level of theory or because of notable differences in the theoretical and experimental spectra (Figure S1). Thus, the global minimum of AuBi<sub>4</sub><sup>-</sup> probably includes two major isomers, the  $C_{2v}$  isomer I and  $D_{2h}$  isomer II, along with a minor  $C_s$  isomer III. Interestingly, the gold atom of isomer II is coordinated with four Bi atoms, while that of isomers I and III is coordinated with two and one Bi atoms, respectively. Previously reported structures for neutral AuBi<sub>4</sub> are completely different from the anions reported here.<sup>32</sup>

**AuBi**<sub>5</sub><sup>-</sup>. The 355 nm spectrum of AuBi<sub>5</sub><sup>-</sup> (Figure 1d) exhibits three prominent bands (X, A, and B). Two discernible shoulders (X' and A') are also observed at around band X. The 266 nm spectrum (Figure 1e) reveals more and congested bands at the higher binding energy side; some are better seen in the 193 nm spectrum (Figure 1f). The weak bands (X', A'-D') suggest the existence of a minor isomer.

We examined 10 low-lying structures carefully and found that isomer I was the lowest-energy candidate at all levels of theory (Table S2). Simulated spectra of all the top candidates are presented in Figure S2. On close examination of the theoretical spectra, we observe that the X band and the two overlapping peaks (A and B) along with the peaks at higher binding energy are all well-reproduced by the simulated spectrum of isomer I (Figure 3b). This good agreement between the experiment and the theory is further supported by the 0.096 eV rmsd value of first four peaks (Table S6) and gives credence to the predicted global minimum. Isomer II is about 0.11 eV higher at the CCSD(T) level than isomer I. The theoretical spectrum based on isomer II contains closely spaced features which resemble the minor features labeled X', A',... of the experimental spectrum. Both isomers I and II are low-symmetry ( $C_s$ ) structures, which are related to the isomers of AuBi<sub>4</sub><sup>-</sup> with one added Bi atom.

**AuBi**<sub>6</sub><sup>-</sup>. The 355 nm spectrum of AuBi<sub>6</sub><sup>-</sup> (Figure 1g) shows three wellresolved and sharp bands (X, A, and B). Two more sharp bands are observed in the 266 nm spectrum (Figure 1h). The 193 nm spectrum of AuBi<sub>6</sub><sup>-</sup> (Figure 1i) reveals four more bands (E–H). Overall, the spectra of AuBi<sub>6</sub><sup>-</sup> are well-resolved without minor features observed in other spectra, suggesting that there is only one major isomer present in the cluster beam of AuBi<sub>6</sub><sup>-</sup>.

We examined a total of 13 low-lying structures and isomers I and II emerged as the top two candidates (Figure 3c). These are the lowestenergy isomers at both the M06/aug-cc-pVTZ (ECP) and PBE0/CRENBL (ECP) levels (Table S3). Other isomers were easily ruled out because of their high relative energies. The theoretical spectra of all the low-lying isomers are presented in Figure S3. The difference in relative energy among the top two isomers is less than 0.09 eV at the PBE0/CRENBL (ECP) level, but at the CCSD(T)/aug-cc-pVDZ (ECP) level isomer I is the lowest in energy and isomer II is 0.30 eV higher. Furthermore, on comparing the theoretical spectra with the experimental spectra, isomer II can be readily ruled out. The simulated spectral pattern of the "bow-tie-like" isomer I is almost in perfect agreement with that of the experiment (rmsd = 0.048 eV, Table S6), providing considerable confidence that the  $C_s$  isomer I is the plausible global minimum for AuBi<sub>6</sub><sup>-</sup>.

**AuBi**<sub>7</sub><sup>-</sup>. The 355 nm spectrum of AuBi<sub>7</sub><sup>-</sup> (Figure 2a) is quite complicated with both weak (X' and A') and intense (X, A–C) bands. The 266 nm spectrum (Figure 2b) exhibits two intense bands (E and G), as well as two shoulders (D and F) on band E. The 193 nm spectrum (Figure 2c) displays two more broad bands (H and I), beyond which the signal/noise ratio became quite poor. As will be shown below, there are at least two isomers contributing to the experimental spectra.

We selected a total of 12 low-lying isomers, many of which are very close in energies, even at the CCSD(T)/aug-cc-pVDZ (ECP) level of theory (Table S4). At the PBE0/CRENBL (ECP) level, the top 10 candidates are within ~0.2 eV of the lowest-energy isomer I. In such cases, a precise spectral match becomes the most important criterion to identify the possible global minimum structure. Upon careful examination of the theoretical spectra (Figure S4), we believe that isomers I and II are the two most promising candidates (Figure 4a). Isomer I is the lowest-energy candidate at all levels of theory, and the spectral features of isomer I agree reasonably well with the major experimental features. Also, the calculated rmsd of first four peaks is only 0.085 eV (Table S6). Isomer II is almost degenerate with isomer I at the CCSD(T) level and seems to produce features labeled X' and A'. Hence, isomer II is assigned as the minor isomer in the cluster beam. Although both isomers I ( $C_1$ ) and II ( $C_s$ ) are low-symmetry structures, they can be viewed as adding one additional Bi atom to the "bow-tie-like" isomer motif of AuBi<sub>6</sub><sup>-</sup>.

**AuBi**<sub>8</sub><sup>-</sup>. The 355 nm spectrum of  $AuBi_8^-$  (Figure 2d) displays two intense and closely spaced bands (X and A). Followed by a small energy gap after band A, a weak band B is cut off at the threshold. The 266 nm spectrum of  $AuBi_8^-$  (Figure 2e) reveals a well-resolved band B and four more intense bands (C–F). Because of the technical difficulty, we could not acquire 193 nm PES spectra, but we think that the 355 and 266 nm data contained sufficient features to compare with the theory. The well-resolved spectra for  $AuBi_8^-$  suggest that the cluster beam most likely contained a single major isomer.

Figure 4b presents the theoretical photoelectron spectra of the top three isomers out of the eight selected candidates (Figure S5). Isomer I is the lowest-energy candidate at both the M06/aug-cc-pVTZ (ECP) and PBE0/CRENBL (ECP) levels of theory (Table S5). At the CCSD(T)/ aug-cc-pVDZ (ECP) level, isomer I also exhibits the lowest energy, followed by isomer II. The theoretical spectrum of isomer I reproduces the major features of the experimental spectrum with well-matched relative spacing between the peaks, and rmsd is only 0.054 eV (Table S6). The simulated spectra of the slightly higher energy isomer II are not in good agreement with the experimental spectra. We conclude that isomer I with  $C_s$  symmetry is likely the global minimum for AuBi<sub>8</sub><sup>-</sup>, which can be viewed as adding an additional Bi dimer to the "bow-tie-like" isomer of AuBi<sub>6</sub><sup>-</sup>.

#### **Structural Evolution**

The assigned global minima of the AuBi<sub>n</sub><sup>-</sup> (n = 4-8) clusters are all low-symmetry structures, as shown in **Figure 5**. The crystallized Bi<sub>4 2-</sub> anion is known to be square-planar,<sup>66</sup> and we can view AuBi<sub>4</sub><sup>-</sup> as an oxidized species of Bi<sub>4 2-</sub>. Although one of the AuBi<sub>4</sub><sup>-</sup> isomers (II) is a planar structure consisting of two congruent triangles connected by a central gold atom, both the gas-phase isomers I and II are clearly transformed structures and not related to Bi<sub>4 2-</sub>. The probable evolution of isomers I and II from AuBi<sub>4</sub><sup>-</sup> to AuBi<sub>8</sub><sup>-</sup> is depicted by arrows in Figure 5. The structures of the larger clusters are more compact as the



**Figure 5.** Identified global minimum structures of  $AuBi_4^-$  to  $AuBi_8^-$  and their structure evolution (black labels: major isomers and blue labels: minor isomers). The gold atom is represented in yellow color, and blue circles represent the additional atom that builds upon the previous cluster.

Au atom becomes more coordinated from  $AuBi_6^-$  to  $AuBi_8^-$ . In fact, in  $AuBi_7^-$  and  $AuBi_8^-$ , the gold atom is coordinated by five bismuth atoms. In Figure 5, we also depict the probable growth of the larger clusters, where the atom circled in blue represents the additional atom that seems to build upon the previous cluster.

It should also be pointed out that in the case of the AuBi<sub>7</sub><sup>-</sup> cluster, the two low-lying isomers competing for the global minimum are very close in energy. They are nearly degenerate even at the CCSD(T)/augcc-pVDZ (ECP) level of theory, differing in energy only by 0.076 eV, indicating a rather flat potential energy surface. This may be a manifestation of dynamic structural fluxionality, which has been a subject of interest in cluster science. To compare the relative stability of the two isomers of AuBi<sub>7</sub><sup>-</sup>, we performed BOMD simulations at two different temperatures, 300 and 260 K.

In **Figure 6**, we present the change in dihedral angle made by atoms (labeled 1–4) during a 5 ps simulation. Isomer I of  $AuBi_7^-$  is fairly stable at both temperatures, and its structure remains intact during the simulation (see **Movie S1** in the Supporting Information). On the other hand, isomer II is relatively unstable and undergoes structural transformations to isomers that appear like isomers III and IV (Table S4) at both temperatures, after ~1–2 ps in the simulation (see **Movie S2** in the Supporting Information). The snapshots where these isomers appear first in the simulation are presented in Figure 6.



**Figure 6.** Change in the dihedral angle of atoms (labeled 1–4) in  $AuBi_7^-$ . Isomer II (top curves) and isomer I (bottom curves) at temperatures 260 and 300 K.

#### **Charge Distribution and Chemical Bonding Analyses**

As gold is more electronegative than bismuth, we expected that there should be charge transfer from Bi to Au in the bimetallic clusters. Indeed, natural population analyses<sup>67</sup> confirmed that more negative charge is localized on the gold atom, but the magnitude of the charge varies with size (**Figure 7**). The degree of charge transfer depends on



**Figure 7.** Plot of negative charge on gold with the change in size of the  $AuBi_n^-$  clusters.

the position of the Au atom in the structure, that is, higher coordination results in a higher charge on gold. Specifically, isomer I of both  $AuBi_4^-$  and  $AuBi_5^-$ , which features a two-coordinated gold atom, exhibits a smaller negative charge compared to all other isomers and clusters which contain highly coordinated gold atoms.

We also performed the chemical bonding analyses to better understand the structures and stability of the AuBi<sub>n</sub><sup>-</sup> (n = 4-8) clusters. Because of relativistic effects, the 6s orbital of the Bi atom is stabilized and tends not to bond with Au<sup>31,68</sup> Each bismuth atom only employs its 6p electrons to form localized  $\sigma$  or  $\pi$  bonds with neighboring atoms. While the gold atom can occupy both low-coordination and high-coordination sites, it interacts with neighboring bismuth atoms through both localized two-center two-electron (2c-2e)  $\sigma$  bonds and delocalized multicenter two-electron (nc-2e)  $\sigma$  bonds. The bonding analyses are shown in Figure S6 in the Supporting Information. The bonding analyses of AuBi<sub>4</sub><sup>-</sup> and AuBi<sub>5</sub><sup>-</sup> clearly present a correlation between high coordination of gold atom and delocalization of valence electrons. The low-coordinated AuBi<sub>4</sub><sup>-</sup> isomer I consists of seven localized 2c-2e  $\sigma$  bonds with occupation number (ON) of 1.96–1.99 |e|, whereas the high-coordinated isomer II has a delocalized 5c-2e bond with ON = 2 |e| and six 2c-2e  $\sigma$  bonds with ON = 1.76-2.00 |e|. Similarly, isomer I of AuBi<sub>s</sub>- has a low-coordinated gold and consists of eight localized 2c-2e  $\sigma$  bonds with ON = 1.76–1.98 |e|. On the other hand, isomer II has a high-coordinated gold atom and consists of one delocalized 5c-2e  $\sigma$  bond with ON = 1.98 |e| and seven localized 2c-2e  $\sigma$  bonds with ON = 1.72 – 1.99 |e|. Delocalized bonding is also revealed in AuBi<sub>n</sub><sup>-</sup> (n = 6 - 8) because of the high-coordinated Au. Specifically, the two isomers of AuBi<sub>7</sub><sup>-</sup> present considerable differences in their  $\sigma$  bonding framework. Isomer I has three 3c-2e  $\sigma$  bonds with ON = 1.78–1.94 |e|, whereas isomer II exhibits delocalization consisting of one 3c-1e ON = 1.00 |e|, one 3c-2e ON = 1.97 |e|, and 4c-2e ON = 1.89 |e|  $\sigma$  bonds.

#### Conclusions

We have performed a combined PES and DFT study on a series of Au-doped bismuth clusters  $AuBi_n^-$  (n = 4-8). Low-symmetry

three-dimensional (3D) structures are prevalent in this size range, although a planar isomer coexists with the 3D global minimum for AuBi<sub>4</sub><sup>-</sup>. The gold atom prefers low-coordination sites in 3D structures for n = 4 and 5, but increasingly high-coordination sites prevail from n = 6-8. AuBi<sub>6</sub><sup>-</sup> has a stable global minimum with a "bow-tie-like" structure, and the major isomers of other clusters also possess this motif. Chemical bonding analyses reveal that the gold atom interacts with neighboring bismuth atoms through localized  $\sigma$  bonds at lowcoordination sites but through delocalized  $\sigma$  bonds at high-coordination sites. This trend of local coordination in turn is directly correlated to the atomic charge localization on the gold atom, that is, the higher the coordination number of gold, the greater is the localized negative charge on gold. BOMD simulations suggest that the major isomer of AuBi<sub>7</sub>- is stable at 260 and 300 K, whereas the minor isomer shows a fluxional behavior and structural transformation at these temperatures.

**Supporting Information** — The Supporting Information is attached to this repository record; it is also available free at doi 10.1021/acs.jpcc.8b00166.

- Energy tables, simulated and experimental photoelectron spectra for all the top candidate isomers of  $AuBi_n^-$  (n = 4-8), and rmsd of simulated spectra of the major isomers (PDF)
- Fairly stable isomer I of AuBi<sub>7</sub><sup>-</sup> with its intact structure during the simulation (MPG)
- Relatively unstable isomer II of AuBi<sub>7</sub><sup>-</sup> undergoing structural transformations to isomers that appear like isomers III and IV (MPG)

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