

ENERGY SYSTEMATICS OF THE GIANT GAMOW-TELLER RESONANCE
AND A CHARGE-EXCHANGE DIPOLE SPIN-FLIP RESONANCE

D.J. Horen

Oak Ridge National Laboratory, Oak Ridge, Tennessee 37830

D.E. Bainum

Emporia State University, Emporia, Kansas 66801

C.C. Foster and C.D. Goodman

Indiana University Cyclotron Facility, Bloomington, Indiana 47405

C. Gaarde

The Niels Bohr Institute, University of Copenhagen, Copenhagen, Denmark

C.A. Goulding and M.B. Greenfield

Florida A&M University, Tallahassee, Florida 32307

J.A. Rapaport and T.N. Taddeucci

Ohio University, Athens, Ohio 45701

E. Sugarbaker and T. Masterson

University of Colorado, Boulder, Colorado 80309

S.M. Austin, A. Galonsky and W. Sterrenburg

Michigan State University, East Lansing, Michigan 48824

In a series of papers¹⁻⁵⁾ in the early 1960's, Fujita, Ikeda and Fujii explored the description of isobaric analogue states (IAS) in terms of proton particle-neutron hole pairs ($\bar{p}n$) and subsequently hypothesized the existence of a collective giant Gamow-Teller (GT) resonance to explain the hindrance of GT transitions in beta decay. These workers²⁻⁴⁾ also pointed out the probable existence of additional collective resonances of the type $\Delta\ell > 0$ and $\Delta S = 1$. Bohr and Mottelson⁶⁾ have discussed the general features of collective modes of excitation involving spin degrees of freedom. The first experimental observation of a giant resonance for $N > Z$ nuclei was reported by Doering et al.⁷⁾ from a study of the (p,n) reaction using incident energies of 25 to 45 MeV. In this work we report energy systematics for the giant GT resonance as well as a new resonance excited via a $L=1, S=1$ interaction.

Calculations have shown^{8,9)} that the strength of the central spin-isospin component relative to the central isospin component increases by more than a

factor of two with increasing proton energy between $E_p=100$ and 200 MeV. From measurements of zero-degree cross sections at 120 MeV,¹⁰⁾ values have been deduced for the volume integrals of the central isospin and central spin-isospin potentials which agree within about 20% with the theoretical⁹⁾ calculations. $L=1$ resonances have been observed in $^{90}\text{Zr}(p,n)^{90}\text{Nb}$ at $E_p=120$ MeV¹¹⁾ and in $^{208}\text{Pb}(p,n)^{208}\text{Bi}$ at $E_p=120$ and 160 MeV. The cross section of the $L=1$ resonance at the first maximum was found to be comparable to that of the giant GT resonance at 0° and behaved similarly as a function of proton energy. Since the GT resonance is excited via the spin-isospin component of the effective interaction, it was argued¹¹⁾ that excitation of the $L=1$ resonance also involves $S=1$. This then implies that the $L=1$ resonance is of a charge-exchange dipole mode with spin flip and, hence, could have $J^\pi = 0^-, 1^-$ or 2^- .

We have used the beam-swinger facility¹³⁾ at IUCF, protons with incident energies of 120, 160, and 200 MeV, and neutron flight paths of 60-70m to study the

energetics of the GT and L=1 resonances for a number of targets with $A > 90$. For some targets, angular distributions were measured in 2.5° intervals out to about 15° , while for others 5° intervals were used. Targets studied included $^{90,92,94}\text{Zr}$, $^{112,116,124}\text{Sn}$, ^{169}Tm , and ^{208}Pb . The targets were in the form of self-supporting metallic foils with thicknesses between $40\text{--}180\text{ mg/cm}^2$. Neutron time-of-flight spectra for $\theta = 4.5^\circ$, i.e., near a maximum^{11,12}) in the differential cross section for $\Delta\lambda=1$, are shown in Fig. 1. The

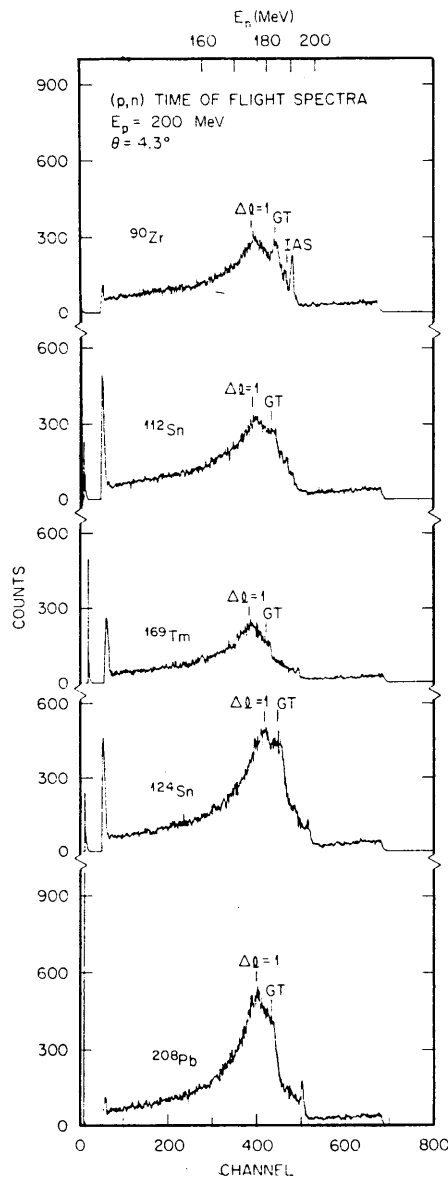


Figure 1. Time-of-flight spectra at 4.3° for the (p,n) reaction at $E_p = 200\text{ MeV}$ for targets of ^{90}Zr , ^{112}Sn , ^{169}Tm , ^{124}Sn , and ^{208}Pb .

results of detailed analyses of these data will be given elsewhere. Here, we focus attention on the energy systematics of the GT and L=1 resonances.

In Fig. 2 we have plotted versus $(N-Z)/A$ the energy differences between the giant GT and L=1 resonances, respectively, and the IAS. The energies of the IAS and GT resonances have been determined from 0° spectra, and those for the L=1 resonance from preliminary analyses of the 4.5° spectra. The uncertainties for $E_{\text{GT}} - E_{\text{IAS}}$ are less than 0.4 MeV , and those for $E_{\Delta\lambda=1} - E_{\text{IAS}}$ are estimated to be $<1\text{ MeV}$. As can be seen from the figure, to first order both energy differences can be represented by linear functions of $(N-Z)/A$ which have about the same slope. From Fig. 2, we find the energy differences in MeV

$$E_{\text{GT}} - E_{\text{IAS}} = -30.00(N-Z)/A + 6.7 \quad (1a)$$

and

$$E_{\Delta\lambda=1} - E_{\text{IAS}} = -33.0(N-Z)/A + 13.6 \quad (1b)$$

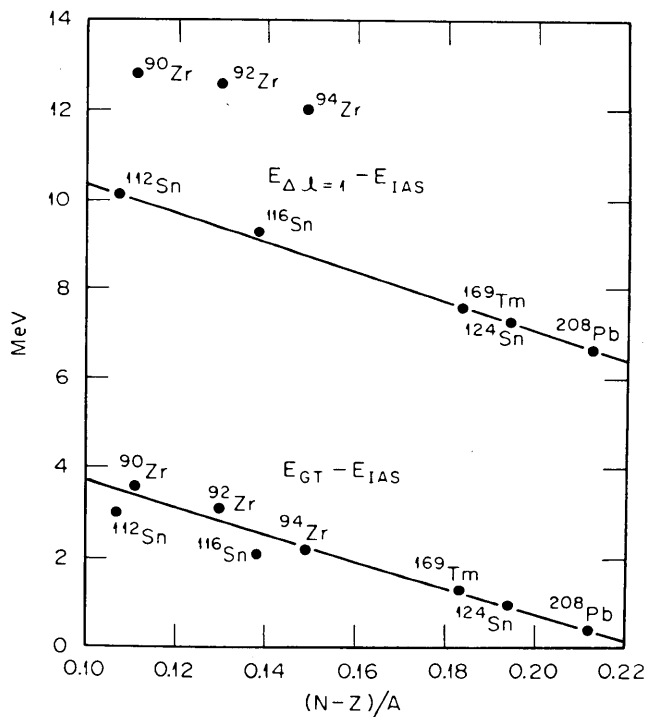


Figure 2. Plots of $(E_{\text{GT}} - E_{\text{IAS}})$ and $(E_{\Delta\lambda=1} - E_{\text{IAS}})$ versus $(N-Z)/A$.

The GT-type excitations with $L=0$, $S=1$ involve mainly $\bar{p}n$ excitations in which there is no change of radial wavefunctions, i.e., excitations within the same oscillator shell. The energies of these would lie close to those for the IAS except that an important contribution to the GT comes from transitions of the type $(j=l+1/2) \rightarrow (j=l-1/2)$. Consequently, the GT energy is shifted up relative to the IAS by an amount typical of this spin-orbit splitting. This accounts for the constant term in equation (1a). Now the residual p-n interactions introduce a further shift which Fujita et al.³⁾ estimated to be about $-30(N-Z)/A$, in good agreement with what is observed. Gapanov and Lyutostanskii¹⁴⁾ have made microscopic calculations of the excitation energies and strengths of the IAS and GT resonances for a number of nuclei from arsenic to lanthanum. Their predicted energy differences, $E_{GT}-E_{IAS}$, for ^{116}Sn and ^{124}Sn are in excellent agreement with our data (i.e., within 0.3 MeV); however, those for $^{90,92,94}\text{Zr}$ fall on a parallel line about 2 MeV higher than our measured values.¹⁴⁾ The calculated energies¹⁴⁾ for the IAS resonances for both the Zr and Sn isotopes agree within a few tenths of an MeV with observed values. Hence, the discrepancy between the calculated values of E_{GT} .

A striking feature in Fig. 2 is that the values of $E_{\Delta L=1}-E_{IAS}$ for the Zr isotopes lie about 3 MeV above the curve formed by the other elements. Since at present there are no detailed calculations of a $L=1$, $S=1$ resonance available for the Zr isotopes, one can only speculate as to the reasons for this. One might be that the distribution of strength among the J-components for the Zr isotopes differs from that for the other elements. Or, possibly, the effective energy for shell crossing in Zr is greater. (This might not be unreasonable from shell-model considerations).

In this work we have presented phenomenological systematics of the GT and a giant $L=1$ resonance (both of which involve spin flip) for the medium to heavy mass region. Some agreement with calculations using finite Fermi systems has been found. However, much additional investigation remains before detailed comparisons can be made.

We would like to thank Bill Lozowski and Tina Rife for fabricating many of the targets, and the staff of IUCF for providing the cyclotron operation and supporting functions. Theoretical discussions with Drs. W.G. Love, G.R. Satchler, and J. Speth are gratefully acknowledged. This work was supported in part by the Department of Energy, Division of Basic Energy Sciences under Contract No. W-7405-eng-26 with the Union Carbide Corporation, the National Science Foundation, and the Danish National Science Research Council.

- 1) K. Ikeda, S. Fujii and F.I. Fujita, Phys. Lett. 2, 169 (1962).
- 2) K. Ikeda, S. Fujii and J.I. Fujita, Phys. Lett. 3, 271 (1963).
- 3) J.I. Fujita, S. Fujii and K. Ikeda, Phys. Rev. 133, B549 (1964).
- 4) K. Ikeda, Prog. Theor. Phys. 31, 434 (1964).
- 5) J.I. Fujita and K. Ikeda, Nucl. Phys. 67, 145 (1965).
- 6) A. Bohr and B.R. Mottelson, Nuclear Structure, Vol. II (Benjamin, New York, 1969).
- 7) R.R. Doering, A. Galonsky, D.M. Patterson and G.F. Bertsch, Phys. Rev. Lett. 35, 1961 (1975).
- 8) F. Petrovich, "The (p,n) Reaction and the Nucleon-Nucleon Force," edited by C.D. Goodman, S.M. Austin, S.D. Bloom, J. Rapaport, and G.R. Satchler, (Plenum, New York, 1980) p. 115.
- 9) W.G. Love, op. cit., p. 23.
- 10) C.D. Goodman, C.A. Goulding, M.B. Greenfield, J. Rapaport, D.E. Bainum, C.C. Foster, W.G. Love and F. Petrovich, Phys. Rev. Lett. 44, 1755 (1980).
- 11) D.E. Bainum, J. Rapaport, C.D. Goodman, D.J. Horen, C.C. Foster, M.B. Greenfield, and C.A. Goulding, Phys. Rev. Lett. 44, 1951 (1980).

- 12) D.J. Horen, C.D. Goodman, C.C. Foster, C.A. Goulding, M.B. Greenfield, J. Rapaport, D.E. Bainum, E. Sugarbaker, T.G. Masterson, F. Petrovich and W.G. Love, Phys. Lett. 95B, 27 (1980).
- 13) C.D. Goodman, C.C. Foster, M.B. Greenfield, C.A. Goulding, D.A. Lind, and J. Rapaport, IEEE Trans. Nucl. Sci. NS-26, 2248 (1979).
- 14) Yu. V. Gaponov and Yu. S. Lyutostanskii, Yad. Fiz. 16, 484 (1972); transl. Sov. J. Nucl. Phys. 16, 270 (1973); Yad. Fiz. 19, 62 (1974); transl. Sov. J. Nucl. Phys. 19, 33 (1974).

GENERAL FEATURES OF THE GAMOW-TELLER RESONANCES

C.D. Goodman and C.C. Foster
Indiana University Cyclotron Facility, Bloomington, Indiana 47405

C. Gaarde and J. Larsen
Niels Bohr Institute, Copenhagen, Denmark

J. Rapaport and T.N. Taddeucci
Ohio University, Athens, Ohio 43701

E. Sugarbaker
Ohio State University, Columbus, Ohio 43212

D.J. Horen
Oak Ridge National Lab, Oak Ridge, Tennessee 37830

C.A. Goulding
University of Texas, Austin, Texas 78712

D. E. Bainum
Emporia State University, Emporia, Kansas 66801

M.B. Greenfield
Florida A&M University, Tallahassee, Florida 32307

A striking feature of the (p,n) reaction in the IUCF energy range is that the 0° neutron spectra are so strongly dominated by Gamow-Teller (GT) transitions that these spectra provide an instant snapshot of GT strength distributions. This feature of the (p,n) reaction is understood¹⁾ on the grounds that at 0°, where there is no transverse momentum transfer and the longitudinal momentum transfer is small, most terms in the projectile-nucleus interaction do not contribute, and the only important terms are $V_{\tau}(\tau_p \cdot \tau_i)$ and $V_{\sigma\tau}(\sigma_p \cdot \sigma_i)(\tau_p \cdot \tau_i)$, where σ and τ are spin and isospin operators, the subscript p refers to the projectile proton and the subscript i refers to the ith nucleon in the nucleus. A summation over nucleons is implied. The (p,n) results also show that V_{τ} is much smaller

than $V_{\sigma\tau}$ for $E_p \sim 200$ MeV.

In interpreting the data on GT strength distributions it is useful to think in terms of how a nucleus with a neutron excess responds to the transformation of a neutron to a proton. This is easily representable in an independent-particle model. Each nuclear state is represented as an occupancy pattern of a set of single-particle states appropriate to the specific model. The neutrons, of course, are indistinguishable from each other, so that the transformation of a neutron into a proton implies a summation over all neutrons. The relevant operator is $\tau_p^+ \tau_i^- (\sigma_p \cdot \sigma_i)$. The result of operating on the target ground state yields a fictitious state that we may call the collective Gamow-Teller (CGT) state. The Gamow-