UNIVERSITÉ DE MONTRÉAL

A PROBABILISTICALLY ANALYZABLE CACHE TO ESTIMATE TIMING BOUNDS

HASSAN ANWAR DÉPARTEMENT DE GÉNIE INFORMATIQUE ET GÉNIE LOGICIEL ÉCOLE POLYTECHNIQUE DE MONTRÉAL

MÉMOIRE PRÉSENTÉ EN VUE DE L'OBTENTION DU DIPLÔME DE MAÎTRISE ÈS SCIENCES APPLIQUÉES (GÉNIE INFORMATIQUE) JUIN 2016

© Hassan Anwar, 2016.

UNIVERSITÉ DE MONTRÉAL

ÉCOLE POLYTECHNIQUE DE MONTRÉAL

Ce mémoire intitulé :

A PROBABILISTICALLY ANALYZABLE CACHE TO ESTIMATE TIMING BOUNDS

présenté par : <u>ANWAR Hassan</u> en vue de l'obtention du diplôme de : <u>Maîtrise ès sciences appliquées</u> a été dûment accepté par le jury d'examen constitué de :

M. <u>GUÉHÉNEUC Yann-Gaël</u>, Doctorat, président
M. <u>BELTRAME Giovanni</u>, Ph. D., membre et directeur de recherche Mme NICOLESCU Gabriela, Doctorat, membre

DEDICATION

This work is dedicated to my beloved Wife and Son Praise worthy Mother and Father, My Brother and Sister and Dr. Giovanni Beltrame for guiding me with love and patience...

ACKNOWLEDGEMENT

I humbly praise ALLAH ALMIGHTY and am grateful to Him, Who helped me live and accomplish the tasks including the research work presents in this thesis; Dr. Giovanni Beltrame my supervisor at École Polytechnique de Montréal, who is always there to help me during my entire thesis. I would have been nowhere without him and am very proud to have worked under his supervision. I offer my sincerest thanks to him for his patience, guidance, illustrious advice, useful suggestions, kind and dynamic supervision throughout the research work. His personal interest, valuable suggestions, most co-operative, constructive and thoughtful behavior, resulted in the completion of this thesis.

I must also thank the administration of École Polytechnique de Montréal for providing me an excellent environment, perfect for conducting research and provide scholarship for Master Thesis. I would like to pay my heartiest gratitude to my fellows in MistLab for their cooperation, help, and valuable suggestions.

I also wish to express my feelings of gratitude to my wife, son, father, mother, brothers, sister and other relatives, who prayed for my health and brilliant future. I would not have achieved my goals without their sincere co-operation and love. I am also using this opportunity to thank all my friends who prayed for me and encouraged me through their love and sincerity.

May God bless all these wonderful people.

Hassan Anwar June, 2016.

RÉSUMÉ

Les architectures informatiques modernes cherchent à accélérer la performance moyenne des logiciels en cours d'exécution. Les caractéristiques architecturales comme : deep pipelines, prédiction de branchement, exécution hors ordre, et hiérarchie des mémoire à multiple niveaux ont un impact négatif sur le logiciel de prédiction temporelle. En particulier, il est difficile, voire impossible, de faire une estimation précise du pire cas de temps d'exécution (WCET) d'un programme ou d'un logiciel en cours d'exécution sur une plateforme informatique particulière. Les systèmes embarqués critiques temps réel (CRTESs), par exemple les systèmes informatiques dans le domaine aérospatiale, exigent des contraintes de temps strictes pour garantir leur fonctionnement opérationnel. L'analyse du WCET est l'idée centrale du développement des systèmes temps réel puisque les systèmes temps réel ont toujours besoin de respecter leurs échéances. Afin de répondre aux exigences du délai, le WCET des tâches des systèmes temps réel doivent être déterminées, et cela est seulement possible si l'architecture informatique est temporellement prévisible. En raison de la nature imprévisible des systems informatiques modernes, il est peu pratique d'utiliser des systèmes informatiques avancés dans les CRTESs. En temps réel, les systèmes ne doivent pas répondre aux exigences de haute performance. Les processeurs conçus pour améliorer la performance des systèmes informatiques en général peuvent ne pas être compatibles avec les exigences pour les systèmes temps réel en raison de problèmes de prédictabilité. Les techniques d'analyse temporelle actuelles sont bien établies, mais nécessitent une connaissance détaillée des opérations internes et de l'état du système pour le matériel et le logiciel. Le manque de connaissances approfondies des opérations architecturales devient un obstacle à l'adoption de techniques déterministes de l'analyse temporelle (DTA) pour mesurer le WCET. Les techniques probabilistes de l'analyse temporelle (PTA) ont, quant à elles, émergé comme les techniques d'analyse temporelle pour la prochaine génération de systèmes temps réel. Les techniques PTA réduisent l'étendue des connaissances nécessaires pour l'exécution d'un logiciel informatique afin d'effectuer des estimations précises du WCET. Dans cette thèse, nous proposons le développement d'une nouvelle technique pour un cache probabilistiquement analysable, tout en appliquant les techniques PTA pour prédire le temps d'exécution d'un logiciel. Dans ce travail, nous avons mis en place une cache aléatoire pour les processeurs MIPS-32 et Leon-3. Nous avons conçu et mis en œuvre les politiques de placement et remplacement aléatoire et appliquer des techniques temporelles probabilistiques pour mesurer le WCET probabiliste (pWCET). Nous avons également mesuré le niveau de pessimisme encouru par les techniques probabilistes et comparé cela avec la configuration du cache déterministe. La prédiction du WCET fournie par les techniques PTA est plus proche de la durée d'exécution réelle du programme. Nous avons comparé les estimations avec les mesures effectuées sur le processeur pour aider le concepteur à évaluer le niveau de pessimisme introduit par l'architecture du cache pour chaque technique d'analyse temporelle probabiliste. Ce travail fait une première tentative de comparaison des analyses temporelles déterministes, statiques et de l'analyse temporelle probabiliste basée sur des mesures pour l'estimation du temps d'execution sous différentes configurations de cache. Nous avons identifié les points forts et les limites de chaque technique pour la prévision du temps d'execution, puis nous avons fourni des directives pour la conception du processeur qui minimisent le pessimisme associé au WCET. Nos expériences montrent que le cache répond à toutes les conditions pour PTA et la prévision du programme peut être déterminée avec une précision arbitraire. Une telle architecture probabiliste offre un potentiel inégalé et prometteur pour les prochaines générations du CRTESs.

ABSTRACT

Modern computer architectures are targeted towards speeding up the average performance of software running on it. Architectural features like: deep pipelines, branch prediction, outof-order execution, and multi-level memory hierarchies have an adverse impact on software timing prediction. Particularly, it is hard or even impossible to make an accurate estimation of the worst case execution-time (WCET) of a program or software running on a particular hardware platform.

Critical real-time embedded systems (CRTESs), e.g. computing systems in aerospace require strict timing constraints to guarantee their proper operational behavior. WCET analysis is the central idea of the real-time systems development because real-time systems always need to meet their deadlines. In order to meet the deadline requirements, WCET of the real-time systems tasks must be determined, and this is only possible if the hardware architecture is time-predictable. Due to the unpredictable nature of the modern computing hardware, it is not practical to use advanced computing systems in CRTESs. The real-time systems do not need to meet high-performance requirements. The processor designed to improve average cases performance may not fit the requirements for the real-time systems due to predictability issues.

Current timing analysis techniques are well established, but require detailed knowledge of the internal operations and the state of the system for both hardware and software. Lack of in-depth knowledge of the architectural operations become an obstacle for adopting the deterministic timing analysis (DTA) techniques for WCET measurement. Probabilistic timing analysis (PTA) is a technique that emerged for the timing analysis of the next-generation real-time systems. The PTA techniques reduce the extent of knowledge of a software execution platform that is needed to perform the accurate WCET estimations. In this thesis, we propose the development of a new probabilistically analyzable cache and applied PTA techniques for time-prediction. In this work, we implemented a randomized cache for MIPS-32 and Leon-3 processors. We designed and implemented random placement and replacement policies, and applied probabilistic timing techniques to measure probabilistic WCET (pWCET). We also measured the level of pessimism incurred by the probabilistic techniques and compared it with the deterministic cache configuration. The WCET prediction provided by the PTA techniques is closer to the real execution-time of the program. We compared the estimates with the measurements done on the processor to help the designer to evaluate the level of pessimism introduced by the cache architecture for each probabilistic timing analysis

technique. This work makes a first attempt towards the comparison of deterministic, static, and measurement-based probabilistic timing analysis for time-prediction under varying cache configurations. We identify strengths and limitations of each technique for time- prediction, and provide guidelines for the design of the processor that minimize the pessimism associated with WCET. Our experiments show that the cache fulfills all the requirements for PTA and program prediction can be determined with arbitrary accuracy. Such probabilistic computer architecture carries unmatched potential and great promise for next generation CRTESs.

TABLE OF CONTENTS

DEDIC	ATION	[iii
ACKNO	OWLEI	DGEMENT	iv
RÉSUN	1É		v
ABSTR	ACT		vii
TABLE	OF C	ONTENTS	ix
LIST O	F TAB	LES	xii
LIST O	F FIGU	URES	xiii
LIST O	F ABB	REVIATIONS	xiv
LIST O	F APP	ENDIX	XV
CHAPT	FER 1	INTRODUCTION	1
1.1	Conte	xt and Motivation	2
1.2		tives/Purpose of Study	3
1.3		em Statement	4
1.4	Novel	ty and Impact	5
1.5		rch Contributions	5
1.6		s Layout	6
CHAPT	FER 2	TIMING ANALYSIS	7
2.1	Deteri	ministic Timing Analysis Techniques	7
	2.1.1	Static Techniques	8
	2.1.2	Measurement Techniques	8
	2.1.3	Comparison Between Static and Measurement Techniques	9
2.2	Proba	bilistic Timing Analysis Techniques	10
	2.2.1	Measurement-Based Probabilistic Timing Analysis	11
	2.2.2	Extreme Value Theory for MBPTA	12
	2.2.3	Achieving Time Randomization	14
	2.2.4	Static Probabilistic Timing Analysis Technique	15

	2.2.5	Comparison Between Measurement and Static Probabilistic Timing
		Techniques
СНАРТ	TER 3	TIME-PREDICTABLE ARCHITECTURES
3.1	Time-	Predictable Architecture
	3.1.1	Architectural Modifications
3.2	Proba	bilistically Analyzable Single-core Architecture
3.3	Proba	bilistic Multi-core Architecture
3.4	Proba	bilistically Analyzable Real-time Systems
	3.4.1	Probabilistically Analyzable Cache
	3.4.2	Probabilistic Analyzable Bus
3.5	Time-	Predictable Real-time systems
СНАРТ	TER 4	PROBABILISTICALLY ANALYZABLE CACHE ON FPGA 2
4.1	Introd	uction $\ldots \ldots 2$
4.2	Inspira	ation $\ldots \ldots 2$
	4.2.1	Cache Organization
	4.2.2	Cache Mapping Scheme
	4.2.3	Direct Mapped Cache
	4.2.4	Fully Associative Cache
	4.2.5	Set Associative Cache
	4.2.6	Comparison
4.3	Rando	mized Cache
4.4	Cache	Model
	4.4.1	Instruction Cache Model
	4.4.2	Data Cache Model
4.5	Hardw	vare Implementation
	4.5.1	Cache RTL Model
	4.5.2	Random Number Generation
	4.5.3	Parametric Hash Function
4.6	Exper	imental Results
	4.6.1	Achieving i.i.d Property
СНАРТ	TER 5	CACHE DESIGN CONSIDERATIONS TO IMPROVE TIMING ANAL-
YSIS	S BOUI	NDS
5.1	Introd	uction $\ldots \ldots 4$
5.2	WCE	Γ Estimation Techniques

	5.2.1	Cache Overview	44
5.3	Timing	g Techniques	44
	5.3.1	Deterministic Timing Analysis	44
	5.3.2	Measurement-Based Probabilistic Timing Analysis	45
	5.3.3	Modelling EVT for WCET	45
	5.3.4	Steps in MBPTA	46
	5.3.5	Static Probabilistic Timing Analysis	46
5.4	Predic	tion Evaluation Under Timing Techniques	48
	5.4.1	Cache Hardware Configuration	48
5.5	Experi	imental Setup	49
	5.5.1	Cache Setup	49
5.6	Experi	imental Evaluation	50
	5.6.1	Prediction Analysis under Associativity	50
	5.6.2	Prediction Analysis under Cache Size	52
	5.6.3	Prediction Analysis under Line Size	53
СНАРТ	TER 6	DISCUSSION	58
СНАРТ	TER 7	CONCLUSION	61
REFER	ENCES	5	63
APPEN	DIX .		69

LIST OF TABLES

Table 4.1	VHDL Basic Signals Descriptions	34
Table 4.2	Resource Utilization and Overhead (Virtex-5)	39
Table 4.3	Independence Tests.	39
Table 4.4	Identical Distribution Tests.	40
Table 4.5	Predicted pWCET (T_p) at 10^{-3} Exceedance Probability versus Mea-	
	sured WCET (T_m) for the RND Cache. Times are shown in milliseconds.	40
Table 4.6	Deterministic/Probabilistic WCETs and respective Bounds. $\ . \ . \ .$	41
Table 4.7	Pessimism between Predicted pWCETs at 10^{-3} Exceedance Probability	
	versus Deterministic Cache.	42
Table 5.1	Independence and Identical Distribution Tests	46
Table 5.2	Level of Pessimism Introduced by varying Cache Parameters	55
Table 5.3	Deterministic/Probabilistic WCETs and respective Execution Bounds.	56
Table 5.4	Pessimism between Predicted pWCETs at 10^{-3} Exceedance Probability	
	versus Deterministic Cache.	56

LIST OF FIGURES

Figure 2.1	Exceedance Probability.	12
Figure 2.2	Gumbel Distribution.	13
Figure 2.3	EVT-Computing System	14
Figure 3.1	Timing Distribution of different Architectures	19
Figure 3.2	Probability Density Probabilistic Architectures: avoiding corner cases	
	will improve WCET Estimation and Bound the Execution-Time t with	
	Probability P $(t > t_x)$	20
Figure 3.3	Probability Density for Deterministic Architectures	21
Figure 4.1	Address Bit Partitioning - Direct Mapped Cache.	30
Figure 4.2	Address Bit Partitioning - Set-Associative Cache.	30
Figure 4.3	Instruction Cache State Machine.	33
Figure 4.4	Data Cache State Machine.	34
Figure 4.5	Structure of the Proposed Cache.	35
Figure 4.6	The Hash Function uses a Random Number, the Address Bits, and	
	Four XOR Stages to Produce a Random Placement	37
Figure 4.7	Execution-Time Measurement	38
Figure 4.8	Pessimism between Predicted pWCETs at 10^{-3} Exceedance Probability	
	versus Deterministic Cache.	42
Figure 5.1	Impact on Time-Prediction by varying Associativity-MBPTA	50
Figure 5.2	Impact on Time-Prediction by varying Associativity-SPTA	51
Figure 5.3	Impact on Time-Prediction by varying Cache Size-MBPTA	52
Figure 5.4	Impact on Time-Prediction by varying Cache Size-SPTA	53
Figure 5.5	Impact on Time-Prediction by varying Cacheline-MBPTA	54
Figure 5.6	Impact on Time-Prediction by varying Cacheline-MBPTA	54
Figure 5.7	Comparison between Time-Prediction via Timing Techniques and Max-	
	imum Execution-Time	55
Figure 5.8	Pessimism between Predicted pWCETs at 10^{-3} Exceedance Probability	
	versus Deterministic Cache.	56

LIST OF ABBREVIATIONS

AHB	Advanced Hierarchical Bus
AMBA	Advanced Microprocessor Bus Architecture
CRTESs	Critical Real-Time Embedded Systems
COTS	Commercial Off-The-shelf
DTA	Deterministic Timing Analysis
DWC	Duplication with Compare
EVT	Extreme Value Theory
FPGA	Field-Programmable Gate Array
GPD	Generalized Pareto Distribution
I.I.D	Independent and Identical Distributed
LLC	Last Level Cache
LRU	Least Recently Used
MBDTA	Measurement Based Deterministic Timing Analysis
MBPTA	Measurement Based Probabilistic Timing Analysis
PHF	Parametric Hash Function
PTA	Probabilistic Timing Analysis
RT	Real-Time System
SDTA	Static Deterministic Timing Analysis
SPTA	Static Probabilistic Timing Analysis
ТА	Timing Analysis
TDM	Time Division Multiplexing
TPA	Time-Predictable Architecture
TR	Time Randomized
	Time Randomized

CHAPTER 1 INTRODUCTION

Time-prediction is the key requirement of a critical real-time embedded system (CRTESs) [21]. The next generation of real-time systems will heavily depend on the accurate prediction of worst-case execution-time (WCET) of software running on a particular processor. Current processor architectures are based on the following paradigm: Make the common case fast and the uncommon case correct [58]. This design approach leads towards architectures in which the average-case execution-time is optimized at the cost of worst-case execution-time. Modelling the performance enhancement features of current processors, e.g. pipelining, multi-level cache, dynamic branch prediction, out-of-order execution, chip-multi-threading, and speculative execution for WCET analysis often results in computationally infeasible problems. Real-time systems need an architecture in which the most primary design parameters are a fast and predictable worst case. The work accomplished in this project is focused on the design and usage of probabilistically analyzable cache for time-prediction. The measurements of probabilistic worst-case execution-time bounds (pWCET) under varying randomized cache configurations are the central idea. The time-prediction analysis is performed by using probabilistic timing analysis (PTA) techniques. Drawing our inspiration from [21], we implement the probabilistically analyzable time-predictable cache which can be used to apply PTA techniques. The idea stems from the research on real-time systems and the fact that these systems have to be used in a real-time environment, e.g. air-bag system in a car, auto-braking system on a plane, etc. All these systems should be timeliness; this means missing a deadline could have serious repercussions. Knowing the upper bound of the system execution-time allows the experts to design their systems in a way that keeps the worst execution-time in content.

WCET estimation of a probabilistically analyzable system can be determined through static probabilistic timing analysis (SPTA) [33] and measurement-based timing analysis (MBPTA) [24] techniques. Both techniques provide cumulative distribution function or pWCET function that upper bounds the execution-time of a program. The analysis guarantees that the execution-time of a program only exceeds the corresponding execution-time bound with the probability lower than a targeted probability. In this project, we will explore both static and measurement-based probabilistic timing techniques.

Static probabilistic timing analysis is based on an extension of a real-time calculus [57] while measurement-based probabilistic timing analysis is based on measurements of the executiontime at a higher level of abstraction. The methodology uses in this work will leverage the probabilistic approach to solve the dependability problem of the program on the execution history. The dependability problem can be solved by introducing the randomization in the hardware components, e.g. randomized placement and replacement cache policies. Due to randomization, we implement a probabilistic system which follows a particular mathematical property that is essential to be able to apply PTA techniques — the execution-time behavior of the system is independent and identically distributed [34]. The SPTA and MBPTA have been commonly used for pWCET estimations for real-time systems. These timing techniques are used for real-time systems since probabilistic techniques do not dependent on any history [45].

Probabilistic analysis of a cache has been an active research field in the last couple of year [45, 41]. Most of the work presented so far is based on simulation or development of the timing techniques. The application of PTA techniques on timing measurements extracted from the probabilistically analyzable hardware has not been extensively explored. Furthermore, the probabilistic analysis of the hardware processor such as processors implemented on FPGA [56, 2] is not studied so far. Therefore, the probabilistic analysis of the computing system is of great interest for the real-time systems community. In this work, we used open source VHDL cores of MIPS-32 and Leon-3 and integrated randomized cache in it.

1.1 Context and Motivation

In general, determining the WCET bound on a hardware platform is a challenging task due to the complexity of the processor architectural design. The unavailability of the proprietary processor designs makes it more complicated. Accurate modelling of the design for a worstcase execution-time calculation is a tedious job. Moreover, as discussed earlier, features that enhance average performance heavily depend on the execution history, e.g. memory traces of the instructions. The history is hard to model for WCET analysis since a long history leads towards the state explosion problem for the final WCET. The probabilistic timing analysis is an emerging technique which helps eliminate the need for the detailed design knowledge and execution history required to model the timing behavior of all the architectural components.

To enable the probabilistic timing analysis of the applications running on a processor, we need to introduce randomization in the timing behavior. The randomization in timing is achieved by employing randomized placement and replacement policies for L1-cache. The randomization helps to make the system more predictable, i.e. if the probabilistic response of the system is known, meaningful predictions can be made using the arbitrarily specified confidence interval. The prediction comes with pessimism due to the overestimation generated by the timing analysis techniques [21]. Therefore, we need a new constructive approach for designing processor architectures to minimize this pessimism. For this purpose, processors need to consider time predictability as a major and important factor in their design. In other

words, an architecture design with a new paradigm based on Make the worst case fast and the whole system easy to analyze [58]. General-purpose processors are designed to maximize throughput [21]. Real-time systems require a processor in which WCET is reasonable and known at design time. Classical performance enhancement techniques in computer architectures are extremely hard to model for the WCET analysis. For example, execution history is considered as key for performance improvements, but also the main issue for WCET analysis. Therefore, we need different techniques to manage execution history. The processors designed for low WCET will never be as fast as the processors designed for performance improvement. There are two different design methodologies; either to design for an accurate WCET analysis or for fast computations. Therefore, deterministic computer architecture provides WCET bound that is higher than the real WCET in which the level of pessimism is very high. The difference between the real WCET and the bound is caused by the pessimism of the analysis due to certain factors such as infeasible execution path, lack of certain information, complex architectural design, lack of information provided by the vendors, and state explosion problem due to long execution history. Here, we would like to present our idea of the probabilistically analyzable cache.

Timing analysis for probabilistic architecture can be performed by using probabilistic timing analysis techniques which provide probabilistic WCET bounds (pWCET) [21]. WCET bounds derived from probabilistically analyzable computer architecture is almost equal to the real WCET. To design a probabilistic analyzable system, we used randomized cache [9]. We will use two variants of PTA, i.e. SPTA [3] and MBPTA [24]. In this context, we design and implement the probabilistically analyzable time predictable cache to improve timing analysis bounds.

1.2 Objectives/Purpose of Study

The objective of this research is the definition and implementation of a fully probabilistically analyzable cache for time-prediction. In this research project, we design and implement the probabilistic cache to perform probabilistic timing analysis on the timing values derived by running the benchmark (C-codes) on the processor. The PTA techniques are developed as a solution to reduce the amount of information needed to determine tight WCET estimates. Probabilistic analysis estimates the chance of forthcoming actions based on an a priori model of the probability. It is a novel approach to timing analysis of next-generation real-time embedded systems. The observed execution-times of programs having the distinct probability of occurrence can be modelled with independent and identically distributed random variables. Current processors do not fulfil these properties due to their deterministic nature. To guarantee a particular probabilistic timing behavior of a system, we have to remove determinism from computer architecture because determinism introduces dependencies between instructions and it is not possible to make any assumptions of a normal distribution of events. Our approach is to guarantee the randomness and normal distribution of events inside all hardware components using a real random number generator [49]. The purpose of this project is to make possible the probabilistic timing behavior at the hardware level. The project includes the development of a hardware infrastructure aimed at design space exploration for future power-efficient and high-performance computer architectures for real-time embedded systems which include randomized caches. The hardware implementation of the probabilistic cache will be the main goal. We used benchmarks with high industrial relevance. The pessimism observed under different cache configurations with PTA techniques on the probabilistic architecture is also studied.

1.3 Problem Statement

This thesis aims at defining a novel approach for probabilistically analyzable cache for the real-time systems. In particular, our work intends to provide solutions able to mitigate multiple problems, including, but not limited to:

- Randomization in the timing behavior of the hardware components (e.g. randomized cache) to make the system more predictable. If the probabilistic response of the system is known, meaningful predictions can be made using arbitrarily specified confidence intervals.
- Cache plays an important role for performance enhancement. Therefore, we design a randomized cache that is organized to speed-up execution-time and provide tight WCET bounds.
- Utilization of both variants of PTA techniques to understand and study how PTA techniques affect the prediction bound.
- To implement the effective probabilistic analyzable cache, one has to consider (a) timeprediction as the first order design parameter (b) the design should be probabilistically analyzable and can be used to define the bound for pWCET, and (c) feasible for real-time systems. The purpose is the definition of a probabilistically analyzable system that can work under real-time constraints and it is sufficiently fast to meet performance requirements.

The main challenges we foresee are:

- Finding the architectural issues and their solutions.
- Designing novel timing analysis techniques and their validation and evaluation.
- Implementing a randomized cache and integration with the processors.

These challenges are addressed by using probabilistic techniques, such as SPTA and MBPTA, and by improving existing timing analysis techniques (e.g. the work done in [3] used random replacement cache for timing improvement) or by introducing a novel technique. We implement the architecture, i.e. processor with probabilistic cache as a prototype system is implemented on an field-programmable gate array (FPGA). Its effectiveness is evaluated by making use of benchmark suites such as the Mälardalen benchmark [35]. For the system implementation, we use existing tools, i.e. Gaisler LEON3 [2] processor, and [56] and modify it accordingly to meet our needs. We studied pessimism and time- prediction under varying cache parameters, such as cache-line, cache-size, and associativity.

1.4 Novelty and Impact

The main contributions of this research project can be summarized as follows:

- Development of the probabilistic component randomized cache. The randomization is based on a parametric hash function and can be extended to implement other probabilistic components, e.g. probabilistic bus.
- Development of a methodology of timing analysis for the probabilistic systems. The probabilistic properties can be realized by using caches with random placement and replacement policies.
- Investigation of prediction effects for probabilistic systems under varying cache configurations. The techniques to predict timing analysis bound for estimation ensure the reliability of realtime systems. Moreover, with successful probabilistic cache implementation and its analysis, it can bring enormous benefits for software production, verification, and certification cost. The aerospace industry of Quebec and Canada, as well as other technology areas, will benefit from knowledge transfer and commercialization of probabilistic real-time system software development.

1.5 Research Contributions

The results presented in this thesis were summarized in two papers:

- H. Anwar, C. Chen, and G. Beltrame (2015). A Probabilistically Analyzable Cache Implementation on FPGA, 13th IEEE International New Circuits And Systems Conference (NEW-CAS), Grenoble. [10].
- H. Anwar, C. Chen, and G. Beltrame (2016). Cache Design Considerations to Improve Timing Analysis Bounds, (to be submitted).

The first paper presents the implementation of a probabilistically analyzable randomized cache for the MIPS-32 processor on FPGA. The details are presented in Chapter 4. The second paper presents the comparison of deterministic and probabilistic timing analysis techniques for time-prediction under varying cache configurations. The paper presents the strengths and limitations of timing techniques on time-prediction to help architects design processors for real-time systems to minimize the pessimism associated with the WCET bounds. The details are mentioned in Chapter 5.

For the sake of completeness, we would like to mention that during the course of this work two additional unrelated papers were published:

- H. Anwar, S. Jafri, S. Dytckov, M. Daneshtalab, M. Ebrahimi, A. Hemani, J. Posila, G. Beltrame, and H. Tenhunen (2014). Exploring spiking neural network on coarse-grain re-configurable architectures. Proceedings of International Workshop on Manycore Embedded Systems. ACM, New York, NY, USA, MES '14, 64–67 [12].
- H. Anwar, M. Daneshtalab, M. Ebrahimi, J. Plosila, H. Tenhunen, S. Dytckov, and G. Beltrame (2014). Parameterized AES-based crypto processor for FPGAs. Digital System Design (DSD), 2014 17th Euromicro Conference, 465–472 [11].

These papers are not considered part of this thesis.

1.6 Thesis Layout

The rest of the thesis is organized as follows:

- Chapter 2 reviews the basic concepts in the field of timing analysis, as well as relevant work in the context of probabilistic timing analysis.
- Chapter 3 presents the time predictable architectures and the difference between the general purpose processors and time predictable processors.
- Chapter 4 presents our idea and approach to design probabilistically analyzable cache.
- Chapter 5 discusses the different cache design approaches under deterministic and probabilistic timing techniques. This Chapter also discusses the prediction analysis under different cache design parameters.
- Chapter 6 lists our findings, how valuable they are and why.
- Chapter 7 summarizes the contributions of this dissertation and suggests some potential ideas that warrant further investigation.

CHAPTER 2 TIMING ANALYSIS

This chapter discusses the related work in Timing Analysis (TA) techniques, which have two variants — deterministic and probabilistic. We discuss how these two techniques have been used in the past to estimate WCET bound. TA techniques have significant value in real-time systems to determine the WCET bound and henceforth ensure the accurate behavior of the system. The good knowledge of a timing analysis is the key to designing CRTESs.

The family of timing analysis techniques can be classified into two sub-categories: deterministic timing analysis (DTA), and probabilistic timing analysis (PTA) [51]. Furthermore, the TA techniques can be classified into four distinct approaches: static and measurement-based deterministic timing analysis (SDTA and MBDTA) and static and measurement-based probabilistic timing analysis (SPTA and MBPTA) [51]. The main purpose of timing analysis is to calculate the tight bounds of WCET.

2.1 Deterministic Timing Analysis Techniques

Finding the WCET of a program consists of three possibilities (a) computing the execution-times of all possible execution paths (b) computing the execution-times of a set of possible paths that can be guaranteed to include the longest path and (c) computing the execution-time of the longest possible path. To perform any of these three methods, two approaches can be considered (a) deterministic timing analysis based on the model of the hardware and software code representation (b) execution of the program code on the real hardware (measurement-based approach).

Firstly, deterministic timing analysis techniques are discussed. These are considered as the classical techniques used to find WCET bound [68]. These techniques consider time taken by the task or program depending on the time spent in instructions, a particular path, and specific hardware [69]. This technique requires modelling of the architecture and building a representation of the program, e.g. syntax tree that represents the structure of the code. Control flow graph is also used to express the structure of the executable code. To calculate the execution-time bounds for timing analysis problems, this technique splits the task into a sequence of sub-tasks. These sub-tasks deal with the properties of the control flow and others with the execution-time of instructions/series of instructions on a particular hardware. The timing methods provide the execution-time bound with the guarantee that the execution-time of the program will not exceed the derived bounds. The attempts to find the execution-time bounds analyze the possible control-flow paths and the execution-times for this set of paths. There are two approaches for deterministic timing analysis techniques named static techniques and measurement-based techniques.

Static techniques are used to estimate WCET by examining the source code without executing it on the hardware. Researchers started developing static techniques for industry in the late 1980s. However, the most popular industrial standards are end-to-end timing measurements techniques. A lot of work has been done for static timing techniques. Static techniques work at a higher-level of abstraction to determine the structure of a program's task and subtask. It works on either a piece of the source code or disassembled binary executable. This technique also works at a lowlevel using timing information about the real hardware on which the code will eventually run, considering this information as a representation of the hardware. The model needs to consider all aspects of the hardware such as pipeline, branch prediction, and cache. However, obtaining execution-times from a model instead of measuring it on a hardware platform is only possible if a realistic model of the architecture is available. After combining high and low level techniques, the tool attempts to give an upper bound on the execution-time required to execute a particular code on a hardware platform [69]. At the low-level, static techniques use the behavior of architectural features that improve the average-case performance of the processor, e.g. instruction/data caches, branch prediction and instruction pipelines. It is likely, but increasingly complex, to determine tight WCET bounds if the advanced architectural features are taken into account in the timing model. For example, cache locking techniques can be used for analyzing WCET estimation but provide predictability far away from the actual execution [17]. This is one of the reasons the research community is shifting towards probabilistic techniques which we discuss in section 2.2. Static techniques give good results for simple hardware. Hence, a possible limitation of the static technique is the hardware (the processor architecture itself) because the processor hardware has reached a level complexity that it is very hard to model. The modelling process can introduce errors from several sources like chip design errors, lack of documentation (companies do not provide the detail of the architecture), errors in model creation, etc. As a result, the developed model predicts a different behavior to that observed on real hardware with more pessimistic bounds than the actual ones. Typically, when it is impossible to have accurate predictions, a pessimistic result is used. Modelling a multi-core processor for WCET estimations is even harder than single-core processor. There are many popular and academic tools that implement various forms of static techniques such as aiT, Rapitime, and Bount-T [69].

2.1.2 Measurement Techniques

The measurements techniques get the timing information by executing the task on the hardware with a given set of inputs. No modelling and assumptions are required for this technique [69]. This technique measures the maximum/minimum observed execution-time, or execution-time distribution. Measurement-based timing techniques usually measure the execution-times of the tasks on the real hardware to produce an estimate of the WCET bound. This technique is used to find the execution-times either on all execution paths, or on a subset of execution paths. Finding executiontimes of all possible paths does not guarantee the WCET since the longest path may be missed

times of all possible paths does not guarantee the WCET since the longest path may be missed. One approach is to divide the task into sub-tasks and find the WCET for each sub-tasks. Then, it is easy to combine it with the high-level analysis to get the WCET estimates. The small sub-tasks of the primary task can be measured automatically using techniques such as instrumentation (adding markers to the sub-tasks) or with hardware support such as debuggers and processor hardware tracing modules. These markers help to find the traces of the execution-times which involve both the path taken by the task and the time at which different points are executed. The trace is then analyzed to find the maximum time that each part of the sub-tasks used. Measurement-based timing analysis provides less pessimistic results for complex hardware [44]. This technique is different from the static analysis which suffers from extreme pessimism. Therefore, measurement-based techniques are the industrial standard with some limitations, i.e. it relies on observing the worst-case measured execution-time during the testing, and it is hard to execute it for all the test cases that might affect the worst-case. There are few tools available in the market to measure the execution-time bound by using measurement timing techniques. Among those, the most famous are Chalmers, SWEET and Heptane [69].

2.1.3 Comparison Between Static and Measurement Techniques

In this section, we compare the static and measurement-based techniques to highlight the differences and similarities in their execution-time methodologies, abilities, and technical problems. Static methods are based on control-flow analysis and bound calculation to cover all possible execution paths and estimate the WCET. The overestimation is due to the processor-specific modelling. The main advantage of static methods is the fact that the analysis can be done without running the program on an actual hardware. This analysis method often needs high-tech equipment to simulate the hardware and peripherals of the targeted system.

Measurement-based methods use real measurements (execution runs). Except for the case in which all potential execution paths are measured or the processor is simple enough to let each measurement be started in a worst-case initial state, there is still a chance that some context-dependent executiontimes may be missed. For this reason, this method is unsafe to some extent. To calculate estimations, the measurement methods may use control-flow analysis to include all possible execution paths or they may only use the observed execution paths. The benefit of using measurement-based technique is that it is simpler to apply because it requires no need to model processor behavior and it produces WCET and best case execution-time estimates. The results are more precise, closer to the exact WCET bounds and also incurs less pessimism as compared to the static techniques especially for complex processors. Both techniques share some technical problems and solutions. The front-ends are similar as both use: a) executable code as input b) control-flow analysis c) bound/estimate prediction can be similar. For example, the implicit path enumeration technique (IPET) [1] used for prediction is employed by some static tools and by some measurement-based tools [43]. The main technical problem for static techniques is the modelling of processor behavior which is not an issue for most measurement-based technique, for which the main issue is to measure the executiontimes accurately with fine granularity. The handling of the timing anomalies gives an interesting comparison of both the techniques. Timing anomalies are hard to access for the measurement-based technique that makes it very hard to find a worst-case initial state. To remain on the safe side, the measurement should be done for all possible initial states, which is unrealistic. Measurementbased techniques use only a subset of initial states. Static techniques are based on an abstract interpretation. Therefore, static techniques have ways to express the absence of information and analyze large state sets including all possible states for a safe analysis.

2.2 Probabilistic Timing Analysis Techniques

As discussed in section 1, advancement in the architectural features, adoption of more complex systems lead towards the timing analysis wall [58], that limits the usage of static timing analysis techniques [48]. In this context, probabilistic timing analysis approach is proposed by [21]. Authors showed in their work how probabilistic timing approach attacks the timing analysis wall. They also provide an experimental evidence of the ways probabilistic timing analysis approach reduces the execution platform knowledge that is required to produce a probabilistically accurate WCET estimation.

WCET estimation is a complex process for real-time systems [17]. Cache memories are employed to meet the performance requirements which makes it harder to accurately predict WCET. Different timing methods are used for the WCET estimations including deterministic timing techniques, e.g. SDTA [71] and probabilistic technique, e.g. MBPTA [44]. The deterministic approaches require a detailed platform knowledge which are not addressed in this research project. For example, deterministic timing analysis techniques [70] operate on a deterministic processor architecture which requires a detail knowledge of all the factors that influence execution history, that affects the timing behavior. For example, STA can be applied at cache level, enabled with least recently used (LRU) replacement policy. For timing analysis, this technique needs knowledge of all previous memory accesses made by the program. This requires an accurate abstract cache model. Any flaw in that model (i.e. the address of some memory accesses is unknown) leads towards degradation of the WCET estimation [1]. However, if hardware and software detailed knowledge is available, STA provides the tightest WCET estimation as compared to PTA techniques [44]. PTA techniques on the other hand are useful for industrial users because they require less information for computing tight-enough WCET estimates. The processor architectures used in the industry encounter ever increasing complexity. The task of acquiring and modelling detailed knowledge about the hardware and software is a tedious job and sometimes not even possible [51]. For such, we will mainly focus on probabilistic timing analysis approaches. The main objective of PTA is to provide a

11

probability distribution that bounds the probability of the execution-time of a program exceeding a given value, i.e. the mechanical parts in the aircraft are designed to keep a probability of failure in mind (e.g. 10^{-09} per hour of operation in aircraft applications [38]). This bound is called a probabilistic worst-case execution-time (pWCET) as shown in Figure 2.1. Probabilistic techniques reduce the cost of acquiring the required knowledge to perform trustworthy and less pessimistic WCET analysis [24] which makes them attractive for WCET estimation. However, a lot of work is being done on the deterministic version of timing analysis. The static timing analysis techniques rely on the exhaustive knowledge of both the hardware and software. Static techniques require a mathematical representation of the code and a cycle accurate model of the platform. Linear programming techniques are employed with a mathematical representation of the code to determine the timing behavior of the model. This timing behavior of the model is used to determine the upper bound on the WCET. The bounds provided by the static techniques are stronger than the measurement-based techniques. But the cost of acquiring the detailed knowledge of hardware and software make this technique less useful. This is due to the fact that the hardware platform, i.e. processor's internal architecture, is not well documented or some parts are hidden. This will cause the under estimation or over estimation of the WCET. There are some other possibilities like intellectual property restrictions. Measurement-based timing analysis techniques rely on the thorough testing of the system with the variety of input data, observing the longest execution-time and adding engineering margins to find upper bound for the WCET.

2.2.1 Measurement-Based Probabilistic Timing Analysis

Measurement-based probabilistic timing analysis is a technique used to reduce the cost of acquiring the knowledge needed to compute trustworthy WCET bounds [36, 24, 43]. MBPTA approach determines the WCET estimates for an arbitrarily low probability of exceedance — named probabilistic WCET or pWCET. This technique is based on the Extreme Value Theory (EVT) and provides an estimation of the WCET of a task or application running on a hardware platform. In order to defeat the dependence on the execution history, this technique employs randomization in hardware structure. For this, MBPTA technique uses the theory of rare events [21]. There are two rare event theories which fits the WCET estimation: theory of extreme values [34] and theory of large deviations [34]. To the best of our knowledge, EVT is the only theory implemented so far for WCET estimation. The EVT provides an estimation for the maximum of a sequence that consists of independent and identically distributed random variables [39]. The EVT can be used to provide the average execution-time and worst case execution-time of the program or software [20, 9]. The EVT is mainly used for the statistical purpose [34] along with Block Maxima [34] which is used to select highest execution-time and peak over threshold [34] which is also used to measure highest execution-time. Mainly, the EVT is used on time deterministic architectures for WCET computations. In this work, we used EVT on time randomized hardware for WCET bound.

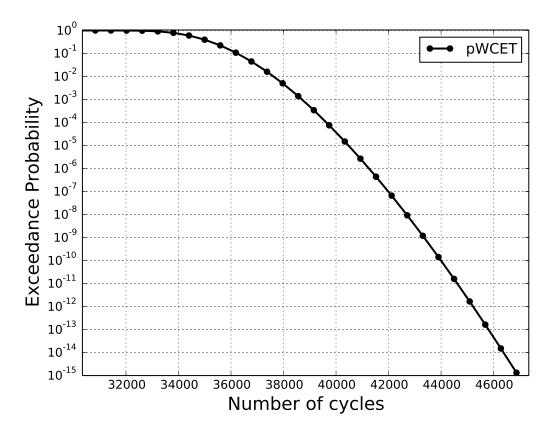


Figure 2.1 Exceedance Probability.

2.2.2 Extreme Value Theory for MBPTA

Extreme value theory is used to find the probability of rare events. The EVT has been used in the past to find the average and the worst case execution-time of software programs [4]. The EVT has used to find the pWCET that upper bounds the execution-time of the program. It also computes cumulative distribution function with the guarantee that the execution-time of the program only exceeds the given bound with a probability lower than a threshold, e.g. 10^{-15} .

In order to use EVT for MBPTA, we need to give special treatment to the timing values that would be observed by running the application/software program on a processor. The timing values should be regarded as random variables that must have i.i.d property. We used EVT to predict the maximum execution-time in a set of observations. There are two ways to perform EVT on timing values. The first approach is Peak over Threshold method [20] which models the distribution of timing values over a certain threshold. In this case, limiting the distribution of exceedance probability can be shown by using generalized pareto distribution (GPD). The second approach for EVT considers the largest (maximum) observation among the successive periods. The maximum distribution is modelled to follow one of the Gumbel, Frechet or Weibull distributions [34]. We used

Gumbel distribution to model our timing values as shown in Figure 2.2.

Usage of EVT for WCET estimation

The EVT is used to predict the worst case execution-time of the applications running on the processor. The inputs of EVT are the numbers of observations which are derived from the real execution of the code. Then EVT gives us the probabilistic prediction of the worst execution-time as shown in Figure2.3. However, there is a requirement associated with the observed values that the observed timing values should have, i.i.d property. The i.i.d property is associated with random variables. The independent property states *"Two random variables are said to be independent if they describe two events such that the occurrence of one event does not have any impact on the occurrence of the other"*. In addition, identical property states *two random variables are said to be identically distributed if they have the same probability distribution function*. In our case, the timing values are considered as random variables which the occurrence runs (execution-times) are independent of each other. EVT does not depend on how timing values are derived as it considers it as a black box as shown in Figure2.3. Timing values should follow i.i.d property to apply EVT to get pWCET. But the requirement for i.i.d puts some requirements and restrictions on the hardware

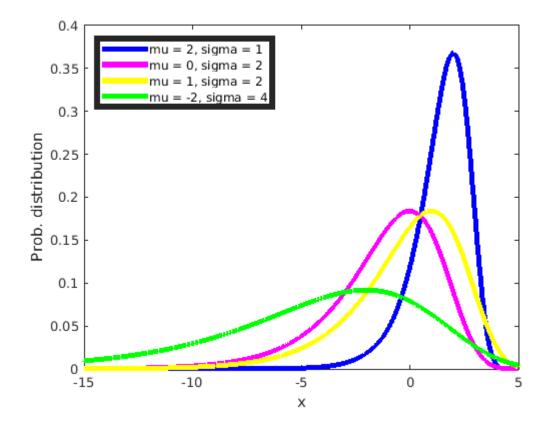


Figure 2.2 Gumbel Distribution.

platform, i.e. the hardware components are randomized which would facilitate the i.i.d property to timing values. We discuss this issue in detail in the next section.

2.2.3 Achieving Time Randomization

MBPTA considers events resulting from the observation of end-to-end measurements of the program. As discussed above, MBPTA uses a statistical method EVT to compute a probabilistic WCET estimate. Therefore, it requires that the observed execution-times are probabilistically independent events. The requirement for EVT is that: the execution-times of a program run (on the same path) have a distinct probability of occurrence and can be modelled with an independent random variable. This technique is being used for the analysis of cache and processor architectures [44, 51]. We also use this technique for the WCET prediction which we discuss in Chapter 4. One way to achieve the time randomization is to vary memory layout of the program and data that affects the program execution-time. This is a software-level technique to create randomization. But this approach is not very common in practice to achieve randomization since it puts extra burden on the user. The MBPTA technique can facilitate randomization by randomizing the placement and replacement policies which helps to make the overall system probabilistically analyzable. This approach achieves randomization at hardware level by changing the design of the cache. The random placement and replacement policies breaks the dependencies in which the index-set of the data is changed at every run. In this manner, designers do not need to control the location of the data in memory. The observed execution-times can be regarded as i.i.d random variables so that EVT can be applied.

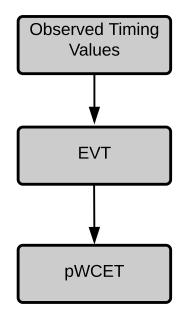


Figure 2.3 EVT-Computing System.

2.2.4 Static Probabilistic Timing Analysis Technique

The static version of PTA is SPTA that uses a model of a processor to derive a priori probabilities for the latency of the program instructions running on a processor [17]. This technique has been the recent subject of many studies [21, 27, 5, 17]. In SPTA, the execution-time of a probability distribution for an individual instruction is determined statically from a processor model [45]. It means that the probabilities for the execution-time of each instruction are independent. Whether an executed instruction is a cache hit, or a cache miss, it does not affect the probabilities of later instructions on a queue. Each instruction derives its own probabilistic timing behavior represented with the help of an execution-time profile (ETP). The ETP of an instruction is expressed as $ETP(I_i) = \langle \vec{t_i}, \vec{p_i} \rangle$ where $\vec{t}_i = (t_i^1, t_i^2, ..., t_i^n)$ and $\vec{p}_i = (p_i^1, p_i^2, ..., p_i^N)$, with $\sum_{j=1}^{N_i} p_i^{N_j} = 1$. The convolution function is used to combine all the ETPs of the instructions to obtain the new ETP, which is used to represent the time distribution of all convolved instructions. The probabilistic cache with evict-on-miss random replacement policy is introduced to reduced WCET of the system and it works in this way: when a cache miss happens, a cache block is selected randomly for the new entry from the main memory. Different from Least Recently Used (LRU) replacement policy, this random behavior avoids cases with low pathological occurrence probabilities which are hard to test and predict such as [21]. Therefore the WCET can be improved. Several formulae have been proposed for SPTA analysis of probabilistic caches. [72] uses reuse window to calculate a probability of each memory address access but this has been proved unsound by [21]. This is because, during the probability calculation, memory accesses are not independent of one another. Due to lack of this independence, the result of his formula cannot be used in some cases. [21] proposed another formula for SPTA, as shown in equation (2.1). In this formula, N is cache associativity and K are reused distance. Reuse distance represents the number of memory addresses between two continuous accesses to the same memory address.

$$P(hit) = \begin{cases} \left(\frac{N - (K-1) - 1}{N - (K-1)}\right)^K & ifK < N\\ 0 & ifK \ge N \end{cases}$$
(2.1)

Equation (2.1) represents the hit probability of each memory address in the cache. This equation takes the number of cache entries into account and when *reuse distance* is beyond its scope, the hit probability is 0. By using equation (2.1), the pessimistic probabilities of all memory addresses are obtained and are independent of each other. Therefore, the overall probability distribution can be calculated by convolution of all probabilities. Execution Time Profile (ETP), as shown is equation (2.2), is used to represent timing information (numbers of cycles) and its associated probability.

$$ETP = \{(c_1, c_2, ...), (p_1, p_2, ...)\}$$
(2.2)

Where c_i is the numbers of cycles, and p_i is its corresponding occurrence probability.

Consider an example; suppose there are two ETPs:

$$ETP_1 = \{(1, 2, 3), (0.1, 0.3, 0.6)\}$$
$$ETP_2 = \{(1, 3), (0.2, 0.8)\}$$

From SPTA, we can compute their convolution:

$$ETP_1 \otimes ETP_2 = \{(1, 2, 3), (0.1, 0.3, 0.6)\} \otimes \{(1, 3), (0.2, 0.8)\}$$
$$ETP = \{(2, 3, 4, 5, 6), (0.02, 0.06, 0.2, 0.24, 0.48)\}$$

Drawbacks

- To determine the execution history, SPTA requires a detailed knowledge of hardware and software. This knowledge is hard to model due to intellectual property restrictions or hindered documentation. Any reduction in available knowledge leads to a rapid degradation of the tightness of the WCET estimation.
- MBPTA works for complex processor architecture. Whereas, SPTA works only for simple processor architectures [1].

The relevance of a PTA to our research is represented by the proposition of a taxonomy and a general framework for accurate WCET prediction for the aerospace computing systems. The primary motivation of this technique is to cope with the history dependency which is highly desired due to the steadily growing complexity of modern computers.

2.2.5 Comparison Between Measurement and Static Probabilistic Timing Techniques

Probabilistic timing analysis pursues the goal of achieving pWCET estimation through static and measurement-based techniques:

- The execution-time of the application can be accurately modelled at some level of execution granularity by a probability distribution.
- Probabilistic timing analysis attacks the timing wall.
- Probabilistic timing analysis reduces the extent of knowledge about the execution platform required to produce probabilistically accurate WCET estimations.
- Probabilistic timing analysis aims to obtain pWCET estimates for an arbitrarily low probability so that even if pWCET estimates are exceeded, it would be exceeded with low probabilities.

Starting with the efforts on timing analysis using the probabilistic cache, several different cache models are proposed. [53] proposed a randomized replacement policy for standard and skewed associative caches which improves WCET at the cost of degrading performance for the best cases. For a different approach, [44] proposed a software method for conventional caches. It modifies memory objects offline using compilers and linkers or online using program loader and runtime libraries. There are two techniques for probabilistic cache timing analysis. The first technique is SPTA. Reuse distance, cache associativity, and entry cache numbers are usually used for calculation. [72] proposed a cache hit formula using reuse distance which simplifies computational complexity. The probabilities for each cache access are made independent and the final result is the convolution of all cache accesses.

However, his methodology has been found faulty [21, 4] Another formula is given by [45], which may overestimate the cache hit ratio [28]. Thus, the result of probabilities for timing may be too optimistic and incorrect. [27] developed a formula to estimate WCET, assuming the reuse distance is known, which is proved to be optimal by [4] with limited information. Besides, an exhaustive analysis approach as opposed to a simplified formula is proposed in [4]. To reduce the computational complexity, the comprehensive approach can be combined with simplified equations. As computational complexity increases, the result is more accurate, but its calculation time grows as well. Apart from SPTA, the MBPTA methodology based on EVT assuming independent and identically distributed random property is tested and Gumbel distribution function is proved to fit the distribution. With these assumptions, result from EVT shows that this technique is close to SPTA. Besides, with mathematical techniques, only a few hundred simulations are required for calculation.

CHAPTER 3 TIME-PREDICTABLE ARCHITECTURES

This chapter discusses a design methodology for time-predictable architectures. In this chapter, we discuss how time-predictable designs are different from general purpose processor architectures. We also discuss different probabilistic systems such as a probabilistically analyzable cache and bus. We propose the method of achieving the objectives of our research, i.e. the implementation of probabilistically analyzable, time-predictable computing systems.

3.1 Time-Predictable Architecture

As we know, computing systems that are subject to respond to strict operational deadlines from events, (i.e. alarms, commands, etc.) are called real-time systems. These are employed in many applications where the response time of a control system can have a critical impact on the safety of people or infrastructure, (e.g. airplanes, automobiles, and satellites). As critical applications become more and more complex, the performance of real-time systems has to increase to guarantee appropriate safety standards. The main obstacle to high-performance real-time systems is the unpredictable timing behaviour of the modern computer architectures. Currently, software designed for real-time systems needs to be guaranteed to be executed within the required time frame. Depending on the complexity of the underlying hardware architecture, this level of certainty might be difficult or impossible to reach. Within this context, this project will introduce a probabilistic approach: by enabling true randomized behaviour in processors and memory architectures, one can define probabilistic metrics for the timing behaviour of a system. This would bring real-time software engineering in line with other engineering domains that perform risk analysis using component failure probabilities.

However, there are few time-predictable architecture available based on the deterministic timing analysis, e.g. the multithreaded processor *Komodo* [46]. The *Komodo* processor core is used to execute Java applications natively. This processor assesses the memory at higher clock frequency than for the pipeline. This technique facilitates the pipeline to access the memory in a single pipeline cycle leading to a precisely predictable access time. There is one more processor for Java applications named Java optimized processor [58]. This processor takes advantages regarding predictability over the conventional processors. This processor introduced stack cache and method cache that prevents additional runtime stack, save/store procedures of the register file, prevents memory conflicts. These two above mentioned processors are based on single core architecture. There is a multicore processor architecture named *MERASA* [66] used to parallel execution of multithreaded with hard real-time requirements. Static and measurement-based WCET analysis techniques are supported by *MERASA*. The *MERASA* is based on a central cache configuration that can be used to assign with required number of cores used to execute a multithreaded application. These processors used deterministic timing techniques for WCET estimation, and their architectures are also deterministic.

Realization of a time-predictable computer architecture — it's definition, modification of a current processor architecture, and implementation is a domain of real-time systems research. Real-time processor architecture needs a reasonable and known WCET that makes it different from the general purpose processors. Classical enhancement are harder to model a system which gives an accurate prediction for WCET measurement. The key factors for performance enhancements such that knowledge of an execution history, mainly an issue for the WCET analysis. Therefore, we need to develop new techniques to design a processor for WCET estimation. We do not want to restrict the features but also want to actively add features that enhance performance and time predictability. PTA techniques are newly invented methods which are less dependent on having an execution history. In this work, our main focus will be on circulating around the improvement and inventing of new architectural features, i.e. a randomized cache for better WCET estimations.

Figure 3.1 shows the purpose of a time-predictable architecture. Figure 3.1 shows the best case execution-time (BCET), average case execution-time (ACET), and WCET bounds for tasks executing on different architectures [59]. The difference between the actual WCET and the bound is caused by the pessimism of the timing analysis already discussed in section 1. In figure 3.1 the first time line shows the execution-times for a commercial off-the-shelf (COTS) processor. The other two time lines show the timing for two different time-predictable processors. The Time-predictable processor has a higher BCET, ACET, and WCET than a COTS processor. However, the WCET is higher than the WCET of the COTS processor, the pessimism of the analysis is lower and the resulting WCET bound is lower as well. Even this type of processor is a better fit for critical real-time systems than today's standard processors. The Time-predictable processor, but the WCET and the WCET bound are decreased with the probability of exceedance that is defined as: the probability

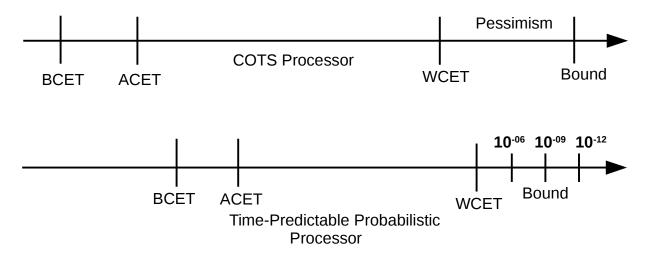


Figure 3.1 Timing Distribution of different Architectures.

of exceeding a given pWCET. Our goal is to design an architecture with a low WCET bound whose predictability is closer to the real execution-time. For critical real-time systems, the likely increase in the ACET and BCET is acceptable, because the complete system needs to be designed to reduce the WCET bound and improve predictability. It should be noted that a processor designed for low WCET will never be as fast as a processor designed for performance improvement of ACET [59]. In this research project, the randomized cache component is designed to facilitate the standard processor for WCET analysis. However, there are some other architectural modifications, e.g. randomized branch prediction also helps prediction. We did not implement them but provide this as a suggestion to help future researcher to take this project to the next level.

Figure 3.2 shows how the idea of the probabilistic system that might affects the verification of realtime systems. Consider a satellite on-board computer: the Y-axis shows the probability density (P (t)) of a given execution-time t on the X-axis for a particular task (e.g. sending telemetry data) running on the on-board computer. Normally the execution-time of an application on a deterministic architecture follows a distribution that might have some corner cases as shown in Figure 3.3. A conservative estimation will place the WCET far away from the actual maximum time used by the application, especially when considering possible interactions with other tasks. This would lead to a large overestimation of the computing resources needed for the task. Instead, a fully probabilistic architecture will have a lower performance on average since current computer architectures are optimized for the average case, but a much smoother distribution, with a single

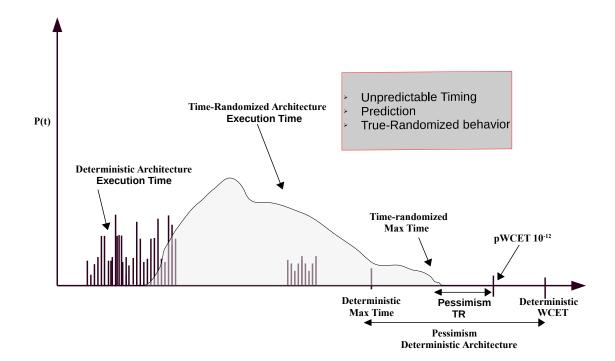


Figure 3.2 Probability Density Probabilistic Architectures: avoiding corner cases will improve WCET Estimation and Bound the Execution-Time t with Probability P $(t > t_x)$.

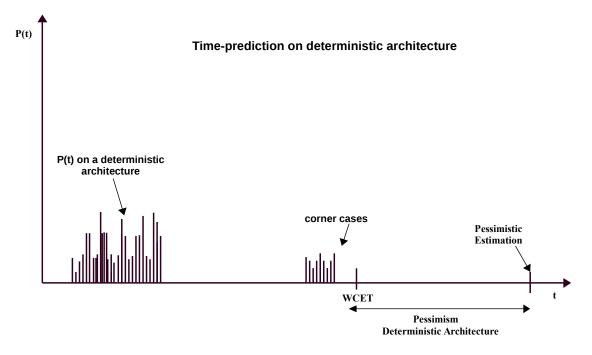


Figure 3.3 Probability Density for Deterministic Architectures.

bell curve. Using our methodology, the maximum execution-time t can be smoothly estimated as a probability function, e.g. P (t > t max) = 10^{-12} . The overestimation of the needed computing resources will be greatly reduced, as well as the cost of determining the WCET for every task. In addition, the combined effect of multiple tasks (e.g. housekeeping, attitude control, etc.) will be predictable without re-analyzing the complete system. In practice, this can reduce cost for the timing analysis of a critical system by several orders of magnitude. Bringing real-time systems development at the same level as any other domain of engineering will have a tremendous impact on the cost of production, verification and certification. As a whole, this research program will enhance the competitiveness of the Canadian aerospace industry: companies like MDA and Bombardier Aerospace could take advantage of the new probabilistic real-time systems for the development and reduced certification cost of spacecraft, high-altitude planes, and unmanned air vehicles.

3.1.1 Architectural Modifications

In order to develop a time-predictable computer architecture, we will need to modify the following architectural components/features of a current processor architecture. For the purpose of this work, few key arguments for a time-predictable computer architecture development are presented below.

- Pipelines will be simple, with minimum dependencies between instructions.
- Avoid processor's out-of-order execution and speculation as it increases WCET complexity.
- In-order to avoid an unbounded timing effect, time-predictable processors use prefetch queue

and double buffer.

- Use static branch prediction instead of dynamic predictors.
- To avoid inter-thread interference, need to develop a policy by using one thread per processor. This philosophy will remove the classic schedulability analysis and we need to do scheduling of a memory access.
- Inter-core interference via shared memory is also a problem for WCET analysis. To avoid this, develop a policy, e.g. randomized Time Division Multiplexing Access (TDMA) scheduled memory access.

3.2 Probabilistically Analyzable Single-core Architecture

Time-predictable computing systems fulfills the requirement of a real-time computing systems. We will need to perform a probabilistic analysis on each of the architectural components (processor, memory, and NoC) for accurate prediction of WCET. In this project we implemented the definition of a novel probabilistic architectures on an FPGA that will prove the applicability of the approach to space applications. One of the main obstacles to high-performance real-time systems is the unpredictable timing behaviour of the modern computer architectures; with multi-stage pipelines and three-level memory hierarchies, it is extremely difficult to accurately predict the execution-time of a given program. This is almost impossible with parallel (such as multi-core) architectures, due to the presence of the shared resources. Being conservative and over-estimating does not solve the problem because of the extremely large difference between the worst and the average cases. The design of powerful real-time systems needs a new approach for the architecture of instruction processors. In this context, we propose a probabilistic analysis approach: by enabling true randomized behaviour in all the components of a computer, one can define probabilistic metrics to the timing behaviour of a system. Successful implementation of such systems will have tremendous impact on the way critical systems are designed, and the potential benefits are enormous in terms of cost of integration, verification, and certification of real-time software. Probabilistic analysis of a computer architecture is introduced by the PROARTIS European Project [21]. PROARTIS focuses on worst case execution-time (WCET) and proposes targeted modifications to hardware modules to improve timing analysis.

This research project focused on the definition and implementation of a randomized computing system, e.g. randomized caches. We implemented the randomized cache and integrated it with MIPS-32 and Leon-3 processor as there source code are freely available [2, 56] and then implemented as a prototype on FPGA. A true random number generator will be implemented as well, based on an existing literature [52]. This generator will be used to guarantee a sufficient entropy pool for the complete randomization of the hardware architecture. The final result of this research will be a fully-functional prototype of a time-predictable probabilistic LEON3 on FPGA. We considered the timing estimation of a program running on the proposed architecture.

3.3Probabilistic Multi-core Architecture

This work is focused on the single-core architecture. Designing multi-core processor for WCET bound is an interesting idea. Here, we present a general approach and challenges associated to design a probabilistic multi-core architecture. Determination of WCET of applications executing on shared memory multi-core processors is hard to estimate. This hinders the adoption of multicore processors in CRTES [41]. We need to develop new timing analysis technique which empowers WCET measurements on multi-core architectures. Most existing multi-core processors contain one shared, usually last-level cache (LLC). This holds for processors used in critical and realtime systems, like the ARM Cortex A9 and A15, the Freescale P4080, and the Aeroex Gaisler

NGMP. While, an LLC offers a high potential for average performance improvement, it increases the complexity of a worst-case execution-time estimation, which has made LLC to be studied in the last years by the real-time community. This is due to the difficulty of determining which memory accesses will hit the cache and which will cause cache misses. This information is necessary to drive tight WCET estimates. Classifying cache accesses as a hit or a miss in non-shared caches has been already deemed as a complex process, subject to some degree of pessimism, therefore reducing the tightness of the estimated WCET bounds. This is even more complex with LLC, in which the main challenge for WCET estimation is an inter-task interference. The solution based on extending the WCET estimation process to the coordinated analysis of several tasks simultaneously sharing a LLC is a complex task. Alternatively, preventing inter-task interference by deploying cache partitioning techniques is the preferred solutions in real time systems to deploy LLC. This solution, however, introduces fragmentation in the use of the memory and may require significant changes in the memory management. Moreover, partitioning increases the complexity of the data sharing across tasks and task scheduling. These challenges highlight a need to explore a new type of cache, and how it can be used as LLC, in particular, need to consider time-randomised caches, which allow controlling inter-task interference without cache partitioning. This is the principle behind TR-LLC. A TR-LLC cache removes any dependency on the particular addresses accessed and its assigned cache set. Therefore, the LLC interference only depends on how often (frequency) its co-runner tasks cause a cache miss, and not the particular address generating the miss. As a result, controlling eviction frequency in a TR-LLC by delaying the time at which misses are served for each task is enough to dependably upper-bound the maximum effect in the LLC that a task may have on all other co-runners. Hence existing multi-core processor with an LLC can be use and need to design a hardware mechanism that limits the miss frequency of tasks in each core at analysis and deployment time. This will be done in such a way that the probabilistic upper-bounds can be obtained for inter-task effects in the LLC.

3.4 Probabilistically Analyzable Real-time Systems

Aiming at the development of a full probabilistic analyzable time-predictable computing system is a main focus for a research community. We cannot neglect the fact that such computing systems have stringent real-time requirements. Enforcing real-time requirements in a multi-processor systemon-chip (MPSoC) is a particularly challenging task. The probabilistically real-time systems are those system, where meeting the deadline is the first order priority [61]. Chances for missing the deadline is probabilistically arguable with target probabilities of 10^{-6} , 10^{-12} , etc. Real-time systems are becoming vital in applications such as flight control system, and modern cars where wires harnesses are replaced by bus, switches are replaced by smart switches engine and other functionalities of the car are controlled by the processors. Since, these system are designed to work in an extreme conditions, meeting the deadline for a particular operation, (e.g. opening of an air bag in the case of an accident should follow strict time deadlines that is very important for such life saving applications). The timing analysis poses the fundamental importance in realtime systems to accurately measure the WCET of a software/program running on it. The usage of a probabilistically analyzable real time system and especially worst case execution-time analysis allows to strongly reduce the over estimation produced by traditional timing analysis method. So far, the researchers have been focused on a probabilistically analyzable processor, cache, bus, and memory. But the whole system didn't probabilistically analysed. In the following sub-sections, a general overview of all each sub-system is presented.

3.4.1 Probabilistically Analyzable Cache

Previous works deal with the probabilistically analyzable cache, processor, and communication infrastructure [51, 24, 41]. In these papers, authors used the concept of time randomization to achieve the requirements for a probabilistically analyzable real-time systems. Because deterministic nature of placement and replacement policies makes it impossible to drive true probabilities for different execution-times. However, the usage of probabilistic cache increased complexity, energy, and performance of the system. But the benefit achieved regarding prediction by employing probabilistic cache is unparalleled. Authors enabled the usage of set-associative and direct mapped cache in the context of probabilistic timing analysis. They proved in their work how their design and methodology drastically reduce the information required by the analysis to drive WCET estimations. Authors encountered both approaches for measuring the WCET analysis: end-to-end measurements of instruction counts, or static techniques based on a source code analysis [70]. Both techniques are limited: static techniques work only on a simple hardware architectures and end-to-end measurements technique quickly loses its accuracy as software becomes more complex. In particular, the behaviour of a cache memory is a serious obstacle for the implementation of these techniques. Deterministic caches are hard to predict because they are geared towards improving the average cases [45, 64] used a random placement based on a parametric hash function to avoid conflict misses to improve the average cases. And, without considerin the real-time systems. [55] shows the impact of different cache policies on a WCET estimation, but without considering random replacement policies. [13] used randomized cache to make processing system more predictable. [26] introduces Static Probabilistic Timing Analysis (SPTA) for WCET estimation, but without any hardware support. [24] presents Measurement-Based Probabilistic Timing Analysis (MBTPA) assuming the existence of probabilistic hardware but without any actual implementation. [21] introduces the concept of probabilistically analyzable caches, but does not provide a cache implementation. These caches are based on random placement and replacement. Kosmidis presents a simulation of a probabilistic cache, and shows that it can be used for SPTA and MBPTA [45].

In [53], the usage of randomized cache over the deterministic one is demonstrated. They first used the standard cache replacement policy and observed a point comes in a simulation where cache miss rate is high enough that it effectively disable the cache usage. On the other side randomized cache successfully removed the pathological behaviors and achieved reasonable performance. This paper is first of its kind to use randomized cache which helps predictability for real-time systems.

[44] this paper extend the concept of applying MBPTA technique to the processor by applying it on cache and bus. In this paper, authors showed how to drive the probabilities and drive ETP for every program instruction.

Although there is argument provided in [54] that randomized cache are harmful in hard real-time systems, author claimed that traditional cache analysis method outperforms the SPTA analysis applied on cache with random replacement, but this argument is answered by the [51] that applicability of PTA depends on the particular hardware and software conditions, i.e. randomized cache with MBPTA technique provides tight and trustworthy WCET estimates and DTA performs better on deterministic architecture. In short, deterministic analysis on the top of conventional cache or probabilistic analysis on the top of randomized cache is highly dependent on the particular characteristics of the hardware.

3.4.2 Probabilistic Analyzable Bus

Most of the work done so far for a probabilistic analyzable bus for multi-core systems are focused on the bus arbitration policies [47, 65]. But these bus policies are based on the fixed latency or bounded transactions which are not the case for real-time systems. Advance hierarchy bus (AHB) bus [13] based system focused on the efficient implementations of the RTL models. For example, [23] discussed several arbitration policies regarding latency and power dissipation. In recent years, we have seen very less amount of research focused on a probabilistically analyzable bus. The work accomplished in [41] is based on a probabilistically analyzable bus design for the multi-core processors. In [40], authors have achieved the analytical models of the probabilistic timing behavior for different bus designs. They showed PTA suitability. They proved that the bus design for a probabilistically analyzable system fulfilled all the requirements for the probabilistic systems. The bus drives WCET estimates with the same cost and complexity as in single-core processor. The achieved performance enhancement is 3.4 times for 8-cores and 6.6 times for 16-cores in comparison to single core performance. This paper, that was published in 2014 means a lot of potential left in this research topic, i.e. comparison of many different bus arbitration policies, (e.g. lotter, random-permutations, and multi-bandwidth bus arbitration). Javier Jalle *et al.* [41] analysed and extended the Advanced Microcontroller Bus Architecture (AMBA) [40] to enable time-composable WCET estimates by design. In this work, they modified the AMBA Advanced High-performance Bus (AHB) named Advanced High performance Real-time Bus which allows getting time composable and tight WCET estimates.

3.5 Time-Predictable Real-time systems

Despite the fact that the COTS processors are better than customized processors, the real-time systems community prefers to use a processor with a lower WCET bound [15]. Few research projects exist in the field of optimizing the hardware for WCET analysis [63]. A new research discipline is needed for time-predictable real-time systems which facilitate the concepts with techniques to improve analyzability to drive safe bounds on WCETs. All architectural components (processor, caches, memory, and bus) of a system need to be time-predictable. Critical real-time systems need to be time-predictable to prove the timeliness of all their time critical response [42]. There is no general definition for the term *time predictability*. However, there are few time-predictable processors that exist in the literature. Among them, the most recent is a java optimized processor proposed by Martin Schoeberl [59]. They have identified the problematic micro-architectural features of the standard processors and provide some alternative solutions. But their architectural enhancements are not yet implemented and tested on RISC based architectues. The use of java optimized processors for space applications is not feasible because of less data available in the market for verification and testing.

Similarly, Edwards et al. [30] argue that : "It is a time for the new era of processors whose temporal behavior is as easily controlled as their logical function". Berg et al. [16] define the time-predictable processor as: "recoverability from information loss in the analysis, minimal variations of the instruction timing, non interference between processor components, deterministic processor behavior, and comprehensive documentation". The author has proposed a five stage pipeline RISC processor, but this processor was not discussed in the context of WCET framework.

[37] provides the basic design strategy for a time-predictable processor: (1) separate data and instruction caches; (2) local update strategy for caches; (3) static branch prediction; and (4) limited out of order execution. But the author did not provide suggestions for additional or alternative features for a time-predictable processor. Although there are more few processors in this domain like VISA [7], SPEAR [29], and [67] these processors have different architectural features to support time predictability but none of them is analysed probabilistically.

Finally, a recent published paper [60] paper presents a solution for the time-predictable memory arbitration for a chip-multiprocessors. The memory of network-on-chip (NoC) is organized as a tree with time-division multiplexing (TDM) of accesses to the shared memory. The TDM based arbitration completely decouples processor cores and allows WCET analysis of the memory accesses on the individual cores without considering the tasks on the other cores. Furthermore, performed local, distributed arbitration according to the global TDM schedule. This solution avoids a central arbiter and scales to a large number of processors. A time-division multiplexing (TDM) arbiter is time-predictable. It allows for calculation of the WCET of a task executing on one processor core independently from tasks executing on other cores. However, this paper did not discuss the feasibility of calculating WCET on their design platform.

The work presented in [1] is based on the qualitative comparison of different timing techniques with different software and hardware configurations, and provides data to the user to choose particular hardware configuration with suitable timing techniques according to the desired level of pessimism. However, the safeness of WCET bound is not guaranteed due to the presence of discontinuous pathological cache patterns and variation of input test cases may affect the safe bound.

Similarly, the work presented in [25] is based on the timing analysis for the multipath program with the MBPTA analysis technique in which authors pay special attention to the number of observations required by the user to obtain the high-quality pWCET estimations. Their results proved that MBPTA based on EVT provides 15% less pessimism than SPTA techniques. This chapter discusses the implementation of probabilistically analyzable instruction and data cache for the ION-MIPS32 processor on FPGA. In order to make a probabilistic analyzable system, we develop the cache with random placement and replacement policies. This chapter discusses how random cache placement and replacement policies fulfills all the necessary requirements for the PTA techniques. We propose set-associative and direct-mapped cache to be analyzed with PTA techniques. We measured the pWCET bound for the probabilistic cache.

4.1 Introduction

As we discussed in Chapter 2 software timing predictability is the key requirement for the real-time systems. Traditional methods require in-depth knowledge that is not always available, and estimation can be extremely pessimistic when using cache memories [70]. To overcome these difficulties, Probabilistic Timing Analysis (PTA) is recently being introduced [21]. The difference between conventional and probabilistic timing analysis is that PTA uses event probabilities to compute a probabilistic WCET with a given confidence (pWCET). This means that the pWCET comes with a certain probability that it is underestimating the actual WCET. PTA can be applied statically (SPTA) or using measurements (MBPTA) [21]. SPTA is a mathematical model of the execution profile of an application, while MBPTA is the end-to-end measurement of an application running on a specific hardware system. For accuracy, the execution-time of a program must consist of *independent and identically distributed events*. This work contributes the measurements of the pWCET for a real-time programs without knowing the detailed knowledge of hardware model. We have promoted the actually execution on FPGA in terms on latency (cycle-count) and simulated it on Modelsim [50].

4.2 Inspiration

The work presented in this chapter is focused on applying the MBPTA technique to the timing values derived from the probabilistic system that is composed of the randomized cache. The FPGA implementation of a probabilistically analyzable cache is inspired by the simulation work presented in [45]. However, that work was done using a simulator and they did not discuss the effect of PTA techniques on timing bounds. The authors did not compare the level of pessimism incurred by the randomized cache analyzed by PTA techniques with those of a deterministic cache.

4.2.1 Cache Organization

A cache is a memory device that stores a subset of the data located in the main memory. Instructions executing on the processor that require data from memory initially search the cache. If the required data is found in the cache, a hit has occurred, if not, then it is a miss. There are three parameters which define the size of the cache: a) Number of Blocks in a cache b) Cache Size c) Tag-Width. We can determine the number of blocks and the tag-width in the cache with the following formulas.

Number of blocks in a cache = $Cache \ size/Block \ size$

Cache Size = The total size of the cache in Bytes

Block Size = Main Memory consists of blocks. Each block consists of 1 or more bytes. The number of bytes in each block determines the number of offset bits

Number of bits in Tag = Total bits - Index bits - Offset bits

In-order to understand the cache configuration and structure, we need to understand the following parameters.

- Memory Size: Determines the size of memory in Bytes, e.g. 256KB. The main memory size is used to determine the total number of bits in the physical memory.
- Cache Size: Determines the size of the cache in Bytes, e.g. 64KB.
- Block Size: Main Memory consists of blocks. Each block consists of 1 or more bytes. The number of bytes in each block determines the number of offset bits.
- Cache Scheme: There are different cache mapping schemes, e.g. Direct-mapped, Set-Associative, and Fully-Associative.

Example: - *Direct-Mapped cache* Consider the example of a direct-mapped cache shown in Figure 4.1 with the following parameters.

Memory size = $256KB = 2^{18}$: Block size = $2Bytes = 2^{18}$

Number of blocks in cache = Cache size/Block size $64KB/2B = 2^{16}/2^1 = 2^{15}$

Number of bits in Tag = Total bits - Index bits - Offset bits = 18 - 15 - 1 = 2

Example: - 4-way Set-Associative Consider the following example of a 4-way associatively mapped cache as shown in Figure 4.2 with the following parameters.

Memory size $= 256KB = 2^{18}$: Block size $= 2Bytes = 2^1$

Number of sets in cache = Cache size/(Set size * Block size) $64KB/(4blocks * 2B) = 2^{16}/(2^2 * 2^1) = 2^{13}$

Number of bits in Tag = Total bits - Index bits - Offset bits = 18 - 13 - 1 = 4

Address Bit Partitioning

TAG	INDEX	OFFSET
17 16	15 14 13 12 11 10 9 8 7 6 5 4 3 2 1	0
Compare Bits	Set Select Bits	Byte Select Bits

Figure 4.1 Address Bit Partitioning - Direct Mapped Cache.

Address Bit Partitioning

TAG	INDEX	OFFSET
17 16 15 14	13 12 11 10 9 8 7 6 5 4 3 2 1	0
Compare Bits	Set Select Bits	Byte Select Bits

Figure 4.2 Address Bit Partitioning - Set-Associative Cache.

4.2.2 Cache Mapping Scheme

There are three popular methods for mapping data in a cache memory.

- *Direct-Mapped Cache:* Data at a given address must be placed at a single specific location in the cache
- *Set-Associative Cache:* Data at a given address can be placed at any of a small set of cache locations
- Fully-Associative Cache: Data at a given address can be placed anywhere in the cache

4.2.3 Direct Mapped Cache

The direct-mapped cache is the simplest form of cache to implement. There is only one possible position for any memory location can be cached. There is no need to search the entire cache either the particular line contains the data or not. Unfortunately, the direct -mapped cache also has the worst performance, because again there is only one place that any address can be stored which causes contention problem frequently.

4.2.4 Fully Associative Cache

The fully-associative cache has the best cache hit ratio among all types of caches, because in a fully-associative cache, one cache line can hold any address. This means that the contention problem seen in the direct-mapped cache disappears as there is no dedicated single cache line that an address must use. However, the fully-associative cache suffers from problems involving searching the cache line. For example, if a cache consists of 16,384 lines, finding a particular address line is a computationally expensive task. Even with specialized hardware to do the searching, a performance penalty is incurred. And, this penalty occurs for all accesses to memory, whether a cache hit occurs or not. It needs more logic to determine which cache line to use when a new entry must be added (usually some form of a replacement algorithm is employed to decide which cache line to use next). As cache address line number increases, it incurrs overhead drastically in terms of cost, complexity, and execution-time.

4.2.5 Set Associative Cache

The set-associative cache is a good compromise between the direct-mapped and fully- associative caches. Consider the example of a 4-way set-associative cache. Each address can be cached in any of four sets, and each particular set acts as a direct-mapped cache and, and within the set find the appropriate cache-line (which is like the fully associative scheme).

4.2.6 Comparison

- The fully-associative cache mapping works the best, but it is complex to implement. Each tag line needs to be compared with the desired address tag field by the circuitry, which makes it very complex and expensive.
- The direct-mapped cache has the lowest performance, but it is the easiest to implement. It is often used for an instruction cache.
- The set-associative cache is a compromise between direct-mapped and fully-associative caches.
 The bigger the "sets" the better the performance, but the more complex and expensive.

4.3 Randomized Cache

Random caches are often used to make processing systems more predictable, such as the ARM Cortex series [13]. In this work, we used a random cache model that makes programs analyzable with MBPTA. The cache is developed in VHDL. The source code is available at [8] and it is configurable through generics: such as data and address bus widths, line size, cache line count, associativity, placement/replacement, and write policy.

The random replacement policy randomly selects the cache line to evict and make a room for the

new memory address. This technique does not require to keep any information about the access history. Due to its simplicity, it has been used to analyse the system with PTA techniques. This technique also ensures that a) evictions across cache lines are independent b) the probabilities of evictions across cache lines are the same. For example, we have a *W*-way set-associative cache, the probability of any specific cache line to be evicted is $\frac{1}{W}$. Similarly, for the random placement policy, we have to ensure that the cache set in which a cache line is mapped is randomly selected. For example, assume that we have a cache with *S* sets. Then the probability of a particular cache set to be selected is $\frac{1}{S}$.

4.4 Cache Model

We developed our cache model in VHDL. The cache VHDL model is configurable. The cache model can be used with different data, address, and bus widths. The cache model can also be designed to integrate with different memory widths. There are configurable parameters which are used to make caches with different configurations. These configurable parameters are *cache line size, cache size, associativity, replacement policy, and write policy.* All parameters can be set through VHDL generics. The placement policy we used is random placement policy. We used two replacement policies: *LRU* and *random replacement* policies. The model supports *write-through* and *write-back* policies for data write. For cache misses, the cache model supports *write-allocate* and *no write-allocate*. In these order: we have *write-back* with *write-allocate, write-through* with *write-allocate* and *write-allocate*. The maximum associativity increases the power and energy consumption of the system. Therefore it is highly recommended to use an associativity between four and eight. In this work, we have used the following approach for the cache behavior

- 1. The cache uses a random replacement policy.
- 2. The cache uses a parametric random placement policy based on a hash function. The detailed design of the hash function given in Section 4.5.3.
- 3. The cache placement is deterministic for each benchmark execution, but randomized across executions.
- 4. We measure end-to-end execution-times for a series of benchmarks.

4.4.1 Instruction Cache Model

In this section, instruction cache, data cache, and basic state transitions are presented. The cache model is developed in Mealy state machine. To avoid fake bits, all the bits are set to zero when the cache powers up. The controller needs to clear all valid bits of indexes during the flush time and the processor is in **Flush** state, as shown in Figure 4.3.

After initializing the initial states, the controller is set to the **Compare Tag** state. In this state, the

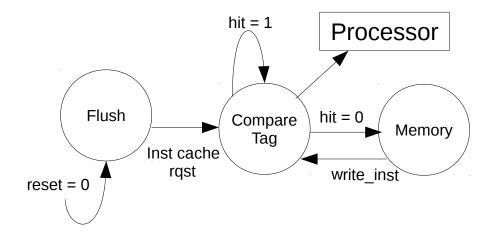


Figure 4.3 Instruction Cache State Machine.

controller needs to verify the tag of the instruction. The requested instruction from the processor either resides in the cache or not. If the requested instruction resides in the cache, a cache **hit** occurs and the instruction is delivered to the processor. If the requested instruction is unavailable, a *miss* occurs and the controller state changes to the **Memory** state. In this state, the cache needs to load a whole memory block into the cache line which contains the requested instruction. Then the state machine goes back to **Compare Tag** state. At this stage, the cache replacement policy works to replace cache lines.

4.4.2 Data Cache Model

Our data cache controller used the *write-back policy*. The flushing operation remains the same as for the instruction cache. Data cache remains in the **Idle** state and works only when it receives the request from the processor. Because data access requests from the processor are less than the instruction requests, it is better to keep data cache in **Idle** state and wait for the processor request. When the processor requests for reading or writing the data, the controller changes its state. For both requests, the controller checks if the data is in the cache or not. Suppose that the requested data is not available and the victim cache line is dirty. This means that the data cache line selected by the replacement policy is not in the memory (no copy in the memory). In this case, data is written back to the main memory. Then the requested data is copied from the main memory, put in the victim cache line (update cache) and processor reads the newly updated cache line. Figure 4.4 shows the data cache state machine.

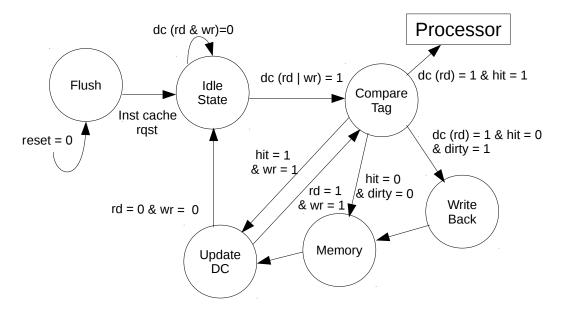


Figure 4.4 Data Cache State Machine.

Record	Signal Description
ic_in.addr	instruction cache address
ic_in.stall	stall the instruction cache
in_out.data	instruction from cache
dc_in.addr	request data address
dc_in.data	write data on write request
dc_in.mask	mask write
dc_in.rd	request for read
dc_in.wr	request for write
dc_out.data	return data from cache
dc_out.stall	stall data cache
mem_in.data	data from main memory
mem_in.stall	stall main memory
mem_out.addr	address to requested data
mem_out.data	on write request write data
mem_out.mask	mask write
mem_out.rd	request for read
out.wr	request for write

Table 4.1 VHDL Basic Signals Descriptions.

4.5 Hardware Implementation

4.5.1 Cache RTL Model

We implemented instruction and data caches for the Ion MIPS32 processor [56]. A completely novel, configurable cache design was implemented in VHDL and integrated with the Ion core. The cache is completely configurable (bus width, size, block size, policies, etc.) with VHDL generics and could be easily ported to other processor designs. Figure 4.5 shows the main components of our design:

- 1. The cache block contains the memory elements, as well as the logic to manage the placement policy (modulo) and replacement policies (random and least-recently-used).
- 2. A hash function block that operates on the index signal to the cache, randomizing the mapping between memory blocks and cache blocks.
- 3. A pseudo-random number generator (MT19937).
- 4. The Ion core, which provides a MIPS32 ISA and controls the whole system.

Our cache has three fundamentally novel features that enable probabilistic timing analysis:

- 1. A random **placement** policy which uses a parametric hash function to shuffle the initial placement of blocks in the cache memory.
- 2. A random **replacement** policy that uses high-quality random numbers to provide statisticallyverifiable guarantees that replacement events are uniformly distributed among the available cache blocks.

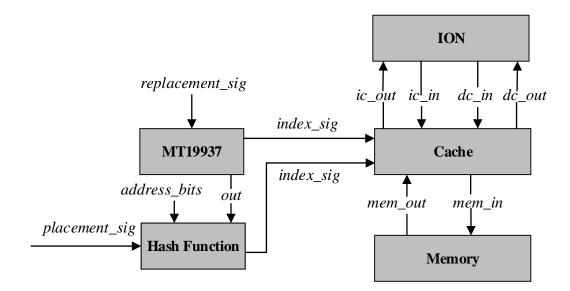


Figure 4.5 Structure of the Proposed Cache.

3. A high-quality pseudo-random number generation, with an extremely long period, to generate random bits for the implementation of the cache random policies.

4.5.2 Random Number Generation

In our cache design, we used the Mersenne Twister algorithm to generate random numbers. In particular, we used the MT19937 algorithm, which is considered as a good hardware solution for a random number generation [49]. MT19937 provides a uniform pseudo number pattern with a period of 2¹⁹⁹³⁷⁻¹, and a width of 32 or 54 bits. We used the OpenCores implementation of MT19937 [52]. The synthesis report shows that the maximum clock frequency the design can achieved is 147.016 MHz, with a throughput of 30 Megasamples per second.

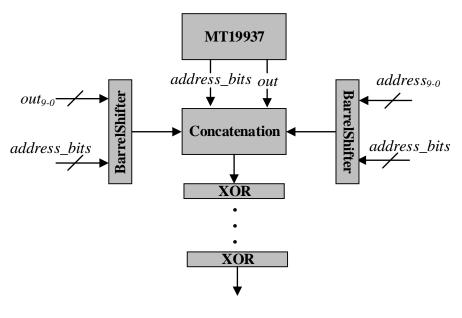
4.5.3 Parametric Hash Function

The idea of using a parametric hash function (PHF) is proposed by [45]. The purpose of using a parametric hash function is to get the index bits for random placement in a cache. The implementation for a parametric hash function is shown in Figure 4.6. This design is remodelled for this work, replacing their Multiply With Carry (MWC) random number generator with the MT19937, which increases the quality of the random numbers as well as the period. The redesign was driven by the fact that MWC does not pass some statistical normality tests [14], and its period might be insufficient for long running applications [32].

Standard placement assigns cache sets to memory addresses based on the index bits. If the placement policy assigns two memory addresses to the same cache set, they will systematically be in conflict. To deal with this deterministic nature, we randomized the timing behavior of the placement policy. To achieve this, we used a parametric hash function with a random number as an input. A random number provides a unique and constant cache set mapping for each address.

If the random number changes, the cache set to which the address is mapped changes. By changing random number only at a new execution, programs can be analyzed with end-to-end runs assuming that the cache is initially empty. The hash function is used to get the *index_bits*. Then these *index_bits* are used for cache placement. The hash function has two inputs 1) the *address_bits* 2) the output from random number generator signal *out*, as shown in Figure 4.6.

The hash function uses the barrel shifter which rotates the address bits based on the randomly generated bits from MT19937 block (random number generator block). Assumed 32-bit addresses the *address_bits* signal in Figure 4.6 needs 27 bits as 5 offsets bits were discarded. Similarly, the other block of barrel shifter uses some of its own bits to shift the original address bits. By doing this, we want to ensure that for different random numbers the mapping of that address changes (data mapped from memory to cache on different locations). This operation is done by the rightmost barrel shifter. Finally, all the original address bits, rotated address bits and bits



Index_bits

Figure 4.6 The Hash Function uses a Random Number, the Address Bits, and Four XOR Stages to Produce a Random Placement.

rotated by random number generator out signal are concatenated and XORed successively till we get desired *index_bits*.

4.6 Experimental Results

We present the RTL model of randomized L1 data and instruction caches. The caches use a highquality random number generator for random placement and replacement. Random placement is obtained with a parametric hash function that shuffles the association between memory addresses and cache blocks. The cache is integrated with the Ion MIPS32 processor, and verified to generate independent and identically distributed timing events, to apply MBPTA technique. We test our cache and MBPTA approach on a variety of benchmarks from the Mälardalen benchmark suite and show a noticeable improvement (5-15%) in terms of measured Worst Case Execution Time as well as enabling the identification of safe probabilistic WCET bounds. Table 4.6 and Table 4.7 show the prediction bounds obtained by applying MBPTA on the probabilistic cache, and also show the estimates obtained for the deterministic cache (modulo placement and LRU replacement) under the deterministic timing technique named reuse-distance [18]. For example in Figure 4.8 shows the pessimism between the probabilistic architecture and deterministic architecture for the application **crc**. Here, we observe that the probabilistic architecture provides less pessimism than the deterministic one as probabilistic architecture has less dependency on the execution history and required no knowledge of the hardware architecture.

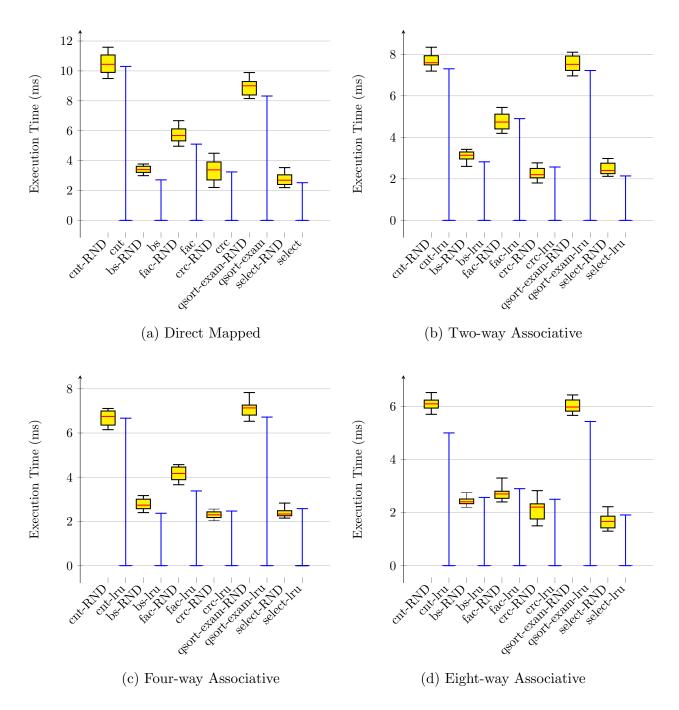


Figure 4.7 Execution-Time Measurement.

4.6.1 Achieving i.i.d Property

We used random placement and random replacement policies with the guarantee that observed execution-times fulfill the property of MBPTA that is essential to apply probabilistic technique. In order to test independence we used Wald-Wolfowitz independence test [34]. We used a 5%

	Available resources	Deterministic cache	Probabilistic cache	Hash function	Random generator	Overhead (%)
LUT Flip Flop	17708	1904	1792	656	117	4.36%
Slice LUTs	69120	6026	5637	660	419	1.56~%

Table 4.2 Resource Utilization and Overhead (Virtex-5).

significance level, a typical value for these types of tests [45]. The independence test gets successful if the obtained absolute values are lower than 1.96, and higher otherwise [45]. Table 4.3 shows the independent tests results.

We used Kolmogorov-Smirnov [34] test to verify the observed execution-times are identically distributed. The significance threshold set for this test is 0.05. If the test values are above the significance level, the result is considered pass, and fail otherwise. Table 4.4 shows the independent distribution tests results.

The architecture used in our experiments is the OpenCores Ion MIPS32 processor. We integrated instruction and data caches, and we implemented the whole system on the Xilinx ML505 FPGA evaluation board, using the XC5VLX110T chip, Xilinx ISE-14.4 and ModelSim 10.1.a. We used two separate 4-KB cache memories for data and instructions, both with a 32-byte line size. To evaluate our design, we used Mälardalen real-time benchmark [35] suite. We selected six benchmarks: *cnt*, *bs*, *fac*, *crc*, *qsort-exam* and *select*. These benchmarks use arrays and matrices, and have nested loops structures which are ideal to test our design [6]. We omitted those benchmarks using external libraries and unstructured code to simplify the software implementation and data collection.

Each benchmark is run on multiple cache configurations profiles, and derived its execution-time profile using MBPTA, with 1000 runs per profile to approximate a normal distribution. We compared our results (RND) with a standard Least-Recently-Used (LRU) cache policy implementation. Table 4.2 shows the resource utilization and overhead of the probabilistic cache, the main source of overhead are due the extra logic consumed by the hash function and random number generator, but the overhead we observed is negligible as compared with the resources available on the

Benchmark	DM	2-way SA	4-way SA	8-way SA
cnt	0.82	0.87	0.63	0.07
bs	0.51	0.75	0.11	0.23
fac	0.33	0.76	0.44	0.53
crc	0.17	0.27	0.37	0.51
qsort-exam	1.26	0.41	0.33	0.03
select	0.39	1.24	0.63	1.12

Table 4.3 Independence Tests.

Benchmark	DM	2-way SA	4-way SA	8-way SA
cnt	0.43	0.65	0.28	0.54
bs	0.97	0.70	0.34	0.36
fac	0.81	0.39	0.74	0.28
crc	0.48	0.40	0.12	0.96
qsort-exam	0.39	0.93	0.73	0.54
select	0.35	0.93	0.41	0.28

Table 4.4 Identical Distribution Tests.

Virtex-5. This design gives freedom that we can integrate different IP-cores and other functionalities in our design. Starting from the direct-mapped cache with random placement, we observed the execution-time taken by the benchmarks is more than that by the set-associative cache. This is due to the fact that if we increase the associativity, the number of cache misses are reduced and it helps to increase the execution-time. Increasing the associativity also helps to improve the prediction as the execution-time getting decrease also helps to smoothing the uniform distribution of the execution-times as a result obtained trustworthy and tight estimates. Figures 4.7 shows the timing distributions for all benchmarks on our cache from direct-mapped to 8-way associative, respectively. As an added advantage, our random cache shows a 19% improvement in worst case execution-time w.r.t to a direct-mapped cache, 11% for 2-way cache, 8% for a 4-way cache, and 6% for an 8-way cache. As expected, LRU gets closer to RND as the number of ways increases: the number of conflict misses is greatly reduced by additional ways.

Moreover, we have observed the pWCET estimates obtained with the MBPTA technique as explained in Section2.1.2. The MBPTA method based on the EVT on the execution runs and observed the pWCET estimates. Table 4.5 shows the pWCET obtained with MBPTA for the multiple random placement/replacement cache configurations. We consider the pWCET estimates at the exceedance probability (the probability that the execution-time will exceed the predicted value) of

Benchmark	Direct		2-way	V	4-way	V	8-way	y
_	T_m	T_p	$\overline{T_m}$	T_p	$\overline{T_m}$	T_p	$\overline{T_m}$	T_p
cnt	11.58	15.35	8.30	9.76	7.11	8.75	6.52	7.90
bs	3.77	6.10	3.42	5.06	3.17	4.22	2.75	3.77
fac	6.67	9.31	5.44	7.42	4.62	6.36	3.33	3.95
crc	4.49	7.23	2.50	5.06	2.77	4.90	2.82	4.29
qsort-exam	9.98	12.08	9.10	11.18	7.83	10.26	6.43	8.34
select	3.80	5.43	2.98	4.55	2.59	3.44	2.22	3.02

Table 4.5 Predicted pWCET (T_p) at 10^{-3} Exceedance Probability versus Measured WCET (T_m) for the RND Cache. Times are shown in milliseconds.

 10^{-3} , as this is compatible with our number of simulations (1000 runs). The data show that the pWCET is a very tight bound for the measured WCET.

We observed a set-associative cache with random placement and replacement provide the tight pWCET estimates as comparing it with the LRU policy. Similarly, we observed that the estimates provided by random policies provided much tight estimates as cache associativity increases. On average, we observed that the estimation is improved from 2-way set-associative to 8-way set-associative, e.g. the prediction time observed for the *cnt* the difference between measured time and predicted time is 3.77 ms which is reduced for the 8-way set-associative to 1.38 ms. Table 4.5 summarizes all the pWCET. Random replacement policy has a lower probability of cache conflicts which helps to improve the execution-time and provide less pessimism in prediction under the MBPTA technique. Indeed, random placement and replacement policies provide the best hardware platform to PTA techniques to the estimates of pWCET with less pessimism.

In summary, our tests show that our random cache implementation can successfully provide a probabilistically analyzable cache on FPGA: MBPTA can be applied to provide safe bounds with arbitrary accuracy. In short, compared to deterministic cache the observed execution-time is 19% improved for direct-mapped cache, 11% improved for 2-way, 8% and 6% improvement observed for 4-way and 8-way respectively. Consider a benchmark **qsort-exam** in Table 4.6 the prediction bound obtained under the probabilistic cache is 8.34 ms and the prediction bound obtained under the deterministic cache is 11.09 ms which is about 28.30 % more than the probabilistic cache.

The improvement factor for higher associativity is not much higher because for the deterministic cache (modulo placement and LRU replacement) policies also works quite good as associativity increases, which decreases the room for further improvement. Table 4.6 and Table 4.7 shows the pWCET estimates obtained with MBPTA for the probabilistic cache that reduces the pWCET estimates over deterministic cache (*modulo placement and LRU replacement*) analyzed with DTA technique [18]. These measurements give us confidence for WCET bounds. The WCET analysis

Benchmark				
	Deterministic Cache (WCET)	Prediction bound	Probabilistic Cache (WCET)	Prediction bound
cnt	5.04	10.33	6.52	7.90
bs	2.57	6.77	2.75	3.77
fac	2.93	5.45	3.33	3.95
crc	2.50	6.13	2.82	4.29
qsort-exam	5.43	11.09	6.43	8.34
select	3.91	5.34	4.12	5.18

Table 4.6 Deterministic/Probabilistic WCETs and respective Bounds.

	Pessimism Difference(%)					
	cnt	bs	fac	crc	qsort	select
Deterministic cache Probabilistic cache				-		

Table 4.7 Pessimism between Predicted pWCETs at 10^{-3} Exceedance Probability versus Deterministic Cache.

gives a safe and trustworthy bound, and this bound may be less conservative as compared it with the bounds obtained for the deterministic cache with deterministic timing technique. Furthermore, the WCET gives no general guarantee that we have knowledge about the worse-case path. The measured WCET gives an upper bound of the pessimism of the WCET analysis. In this work we provide a real execution-time profile on probabilistic cache which is generally not as much over estimated as we seen in Table 4.6. The difference between the deterministic cache execution-time and its associated prediction bounds is more pessimistic than the difference between the probabilistic cache execution-time and its associated prediction bounds.

In this work, we make it possible to use a probabilistic approach in an FPGA's. This work also helps to make it possible to use probabilistic timing technique in real-time systems.

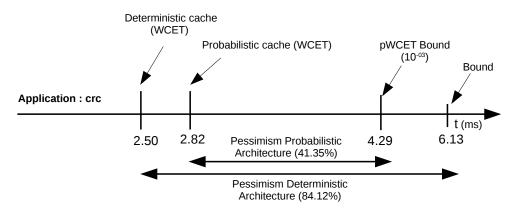


Figure 4.8 Pessimism between Predicted pWCETs at 10^{-3} Exceedance Probability versus Deterministic Cache.

CHAPTER 5 CACHE DESIGN CONSIDERATIONS TO IMPROVE TIMING ANALYSIS BOUNDS

In this chapter, we discuss the comparison between probabilistic timing analysis techniques — SPTA and MBPTA — for time- prediction estimates. We also discuss how we modified the LEON-3 processor's caches to make it applicable for the probabilistic timing techniques. We use random placement and replacement policies for caches and applied probabilistic timing analysis techniques under varying cache configurations to measure the pessimism associated with each cache configuration. The purpose of this work is to find the time- prediction estimates with measurements done on the processor to help real-time system designer to evaluate the level of pessimism for different cache architectures using probabilistic timing analysis techniques. We also identified the strengths and limitations of each technique for time- prediction that helps designers to design the processor's architecture to observe the level of pessimism that is associated with the timing analysis techniques.

5.1 Introduction

As discussed in Chapter4, we used the same strategy — hash function and random number generator — for cache randomization. We used randomization for cache placement and replacement policies. The PTA techniques are used to provide probabilistic WCET estimates for arbitrarily low probabilities. The estimates and level of pessimism offered by the PTA techniques are less pessimistic than those by the deterministic timing techniques [1]. We measured pWCET estimates with both variants of PTA — SPTA and MBPTA. This work is mainly focused on the study of pessimism under different cache configurations while applying PTA techniques. We studied and discussed which technique offered less pessimism, how these techniques are useful for the time-prediction under varying cache configuration and how pessimism varies under different cache configurations. We also compared the PTA techniques with the timing values obtained from the deterministic architecture in which a randomized cache is replaced with a *Least-recently used (LRU)* cache. However, both approaches need specific hardware and software conditions [1]. For instance, DTA techniques perform better on a deterministic architecture with time-deterministic caches (Least Recently Used replacement policy), whereas, PTA techniques performed better on a time-randomized architecture [1, 9]. The contributions of this work are:

— In this work, we focused on the time predictability under different cache choices. We have applied PTA techniques (MBPTA and SPTA) on the Mälardalen benchmark [35]. We identified the limits and strengths of both methods that show pessimism varies under varying cache parameters on the randomized hardware equiped with the time-randomized cache [9].

- We studied the prediction on a randomized hardware. We also discussed the predictability with cache enabled with a deterministic approach, i.e. a time-deterministic cache, e.g. *LRU*.
- The hardware and software environment remain the same for both timing techniques. We also compared the estimated WCET with the that from a deterministic approach.
- We varied the sensitivity of the cache parameters, e.g. *associativity, cache line size, and cache size.*
- Our work allows the cache designer to appropriately select the cache parameters to obtain the predictability goals by probabilistic timing analysis techniques.

5.2 WCET Estimation Techniques

5.2.1 Cache Overview

The cache contents can be organized in different ways. Each design is part of processor's architecture and have different power, timing, and functionality characteristics. The most common cache configurations are a) direct-mapped cache, b) fully-associative cache, and c) set-associative cache. The direct-mapped cache has a unique address for each stored data. Usually, modulo function is used as a placement function. On the other hand, the fully-associative cache does not use any placement function. Data from main memory can be stored in any physical cache line. Therefore, a fully-associative cache requires only replacement function to decide which cache line to evict. The LRU and random policies are usually used as a replacement function for a fully-associative caches. The last one is the set-associative cache which is a combination of direct and fully-associative caches. The number of sets in a cache is decided by the direct-mapped scheme and in each set the cache lines is determined by fully-associative scheme. Therefore, a set- associative cache has to implement both random placement and replacement policies. In this work, we have used set-associative caches.

5.3 Timing Techniques

5.3.1 Deterministic Timing Analysis

DTA techniques need a cycle-accurate model of the system and mathematical representation of the code to obtain the safe upper bound for the worst execution-time [69]. As discussed in Chapter 1, advancements in the architectural features and adoption of more complex systems lead to the *timing analysis wall* that limits the usage of deterministic timing techniques [72]. The DTA techniques are divided into two sub-categories named as *low-level analysis* and *high-level analysis* techniques. The *low-level analysis* techniques use the model of a processor architecture and *high-level analysis* techniques identify the longest execution path among all possible flows of the program for multi-path program analysis. The DTA techniques are applied at cache level, enabled with LRU replacement policy. For timing analysis, this technique needs a knowledge of all previous memory accesses made

by the program. This requires an accurate abstract cache model. Any flaw in that model, (e.g. addresses of some memory accesses are unknown) provides degradation of the WCET estimation. But in some cases, where required hardware and software detailed knowledge are available, DTA techniques provide the tightest WCET estimations. In this work, we did not use any specific DTA technique as this approach is out of the context of this work rather we used deterministic architecture (LRU-cache) to obtained the execution bound. The execution bound obtained from the deterministic architecture is enough to show that the level of pessimism is significantly high.

This section provides the overview of the timing analysis techniques that we used for the timeprediction analysis.

5.3.2 Measurement-Based Probabilistic Timing Analysis

MBPTA is a technique used to reduce the cost of acquiring the knowledge needed for computing trustworthy WCET bounds [24, 43]. MBPTA seeks to determine the WCET estimates for arbitrarily low probabilities of exceedance, namely probabilistic WCET (pWCET). This technique is based on the Extreme Value Theory (EVT) and provides an estimation of the WCET of a task or application running on a hardware platform. In order to defeat the dependence on the execution history, this technique employs randomization. Therefore, MBPTA technique uses the theory of rare events [21]. There are two rare event theories that fit the WCET estimation: theory of extreme values [34] and theory of large deviations [34]. To the best of our knowledge, EVT is the only implemented theory for WCET estimation so far. EVT provides an estimation for the maximum of a sequence of i.i.d random variables [39]. In this work, we have used the MBPTA technique that allows us to find the predicted time of the programs. We have obtained the pWCET estimations that can be applied with high confidence as an upper bound on the execution-time. The execution-times of the programs are observed for 1,000 times (runs). If those execution-times can be modeled with i.i.d random variables, then the pWCET of a program can be obtained by constructing an Empirical Cumulative Distribution Function (ECDF). As we are interested in the EVT and this theory is used to estimate the probability of occurrence of extremely large values that are *rare events*. EVT estimates the distribution function for either the maximal or the minimal values from n set of observations which are formed with the random variables. In short, EVT is used to estimate the extremes.

5.3.3 Modelling EVT for WCET

In order to model EVT for WCET estimates, consider an example of *i.i.d* random variables $\{X_1, X_2, ..., X_n\}$. Let M_n be the maximum value defined as $M_n = max\{X_1, X_2, ..., X_n\}$. Consider F as distribution function and there exits real number sequence (a_n, b_n) such that $a_n > 0$ and $\lim_{n\to\infty} P(\frac{M_n-b_n}{a_n} \leq x) = F(x)$. Then F belongs to either the *Gumbel*, the *Frechet*, or the *Weibull* family [31]. The function F denotes the distribution function of random variables. In our case, the random variables are used to construct the execution-times of the programs. We observed that the

execution-times of the programs follow this property by applying the Kolmogorov-Smirnov test [19] for identical distribution test and Wald-Wolfowitz [34] for independence test. Table 5.1 shows the values obtained by applying these two tests. We used the distribution to model the Cumulative Distribution Function (CDF) which has the following form:

$$F_{\xi}(x) = \begin{cases} e^{-(1+\xi \frac{x-\mu}{\sigma}\frac{1}{\xi})} & \xi \neq 0\\ e^{-e^{-\frac{x-\mu}{\sigma}}} & \xi = 0 \end{cases}$$

This equation is called Generalized Extreme Value distribution and is defined by three parameters: a) shape (ξ), b) scale (σ), and c) location (μ). We need to estimate these three parameters in order to find the sequence of real number (a_n, b_n). For Gumbel distribution, we used shape parameter ($\xi = 0$).

5.3.4 Steps in MBPTA

There are three main steps for MBPTA to povide pWCET estimates.

- The first step is to collect time measurements (execution-times) of the program. We observed them for 1,000 execution runs.
- In the second step, we modeled the original data with the Gumbel distribution. The original timing values are grouped into blocks of equal length, and then the block maxima method is applied. The maximum value observed in each block makes a new sample that is the block maximum series. The block maximum series is basically the worst-case distribution.
- Now we need to compute two remaining parameters, μ and σ that can be achieved by applying linear regression to the QQ-plot of our data.

5.3.5 Static Probabilistic Timing Analysis

The static version of the PTA technique named SPTA uses a model of a processor to derive a priori probabilities for the latency of the program instructions running on a processor [24]. This technique has recently been the subject of extensive studies [21]. In SPTA, the execution-time of a probability

[ud	cover	expint	fdct	jfdctint	qsort	select	cnt	
-			Ir	ndepen	dence Tes	t			
	0.81	0.92	0.84	0.67	0.77	0.69	0.85	0.93	
	Identical distribution Test								
	0.24	0.38	0.91	0.69	0.92	0.87	0.56	0.40	

Table 5.1 Independence and Identical Distribution Tests.

distribution for the individual instructions is determined statically from a processor model [24]. It means that the probabilities for the execution-time of each instruction are independent. Any executed instruction is either a cache hit, or a miss. This does not impact the probabilities of later instructions in a queue. Each instruction derives its probabilistic timing behavior that is represented with the help of an execution-time profile (ETP). The ETP of an instruction is expressed as $ETP(I_i) = \langle \vec{t_i}, \vec{p_i} \rangle$ where $\vec{t_i} = (t_i^1, t_i^2, ..., t_i^n)$ and $\vec{p_i} = (p_i^1, p_i^2, ..., p_i^N)$, with $\sum_{j=1}^{N_i} p_i^{N_j} = 1$. The convolution function is used to combine all the ETPs of the instructions to obtain the new ETP, which is used to represent the time distribution of all the convolved instructions. A probabilistic cache with evict-on-miss random replacement policy is introduced to reduced the WCET of the system, and it works as follows: when a cache miss happens, a cache block is selected randomly for the new entry from the main memory. Unlike the Least Recently Used (LRU) replacement policy, this random behavior avoids cases with low pathological occurrence probabilities, which are hard to test and predict, such as [21]. Therefore the WCET can be improved. Several formulas have been proposed for the SPTA analysis of probabilistic caches. [72] uses reuse window to calculate a probability of each memory address access, but this has been proved unsound by [21]. This is because, during the probability calculation, memory accesses are not independent from one another. Due to this lack of independence, the result of his formula is wrong in some cases. [21] proposed another formula for SPTA, as shown below. In this formula, N is the cache associativity and K is the reused distance. The reused distance represents the number of memory addresses between two continuous accesses to the same memory address.

Equation 2.1 represents the hit probability of each memory address in the cache. This equation takes the number of cache entries into account and when *reuse distance* is beyond its scope, the hit probability is 0. By using Equation 2.1, the pessimistic probabilities of all memory addresses are obtained, and they are independent of each other. Therefore, the overall probability distribution can be calculated by convolution of all probabilities. The Execution Time Profile is used to represent the timing information and its associated probability. In our work, the number of cycles is applied as timing information and thus we have:

$$ETP = \{(c_1, c_2, ...), (p_1, p_2, ...)\}$$

where c_i is the number of cycles, and p_i is its corresponding occurrence probability.

We propose an SPTA methodology for randomized caches, which computes the pWCET on singlepath program memory traces, i.e. the exceedance probabilities for the execution-time (the number of processor cycles). The estimation is performed by using state space techniques, and it is based on a non-homogeneous Markov chain model [62]. This method is developed by MIST lab. The details of this work are available [22], and in Appendix-A. We used this method for static probabilistic timing estimations. In this method, at every step, the current status of the system can be realized as a vector containing the probability of each state. The status of next step is computed using a transition matrix. To perform timing analysis, timing distribution vectors, which are used for the timing description and analysis, are assigned to each state. This approach can obtain tight pWCET estimates.

5.4 Prediction Evaluation Under Timing Techniques

It is hard to compare different timing analysis on the same hardware configuration. Each technique gives its best results on a particular hardware with specific conditions. The deterministic timing analysis techniques provide tightly bound WCET estimates on time-deterministic architectures. Whereas PTA techniques provide tightly bound probabilistic WCET estimates on time-randomized architectures. In this section, we study the prediction under different cache parameters, e.g. *associativity, size, line size.* We vary each of these three parameters and observe the impact of these parameters on *pessimism* under timing techniques. For SPTA and MBPTA, we set the exceedance threshold to 10^{-3} per run.

5.4.1 Cache Hardware Configuration

As discussed earlier, each time technique is suitable under a particular hardware configuration. We have two placement and replacement policies, namely deterministic/random placement and replacement policies. Each timing technique can be analyzed under different cache configurations. For example, a SDTA technique provides tight estimations if the cache replacement is LRU and the placement is modulo, but SPTA and MBPTA cannot be used with LRU and modulo policies as probabilistic techniques require randomization. Consider a case where the placement policy is time deterministic and the replacement policy is time randomized, in this case SDTA can be applied but the results are too pessimistic. MBPTA and SPTA can be applied with this configuration because each access has a probability of hit/miss. Consider a scenario in which we have randomized policies for both placement and replacement, in this case, SDTA gives very pessimistic results [1]. But we can apply SPTA and MBPTA techniques on a randomized hardware. However, MBPTA techniques were applied in the past with randomized placement and replacement and replacement and replacement. In this work, we apply both SPTA and MBPTA timing analysis techniques on a hardware platform enabled with randomized placement. In order to conclude this, we have two remarks:

- Deterministic timing techniques performed well on deterministic hardware.
- Probabilistic techniques required the hardware to be time-randomized. There has been a lot of work in the context of time deterministic architectures with deterministic techniques. We mainly focused on the time randomized hardware with PTA techniques in this work.

5.5 Experimental Setup

We chose eight benchmarks from the Mälardalen WCET suite [35] for the analysis of a level of pessimism under different timing techniques. All experiments are conducted on a Leon-3 processor, C-codes compiled with gcc 4.8.4 with no optimization of the binary code. As discussed in section 5.1, the timing analysis techniques are used in terms of pessimism under varying cache architecture. In this section, we described each timing technique for probabilistic and deterministic cache configurations according to its experimental setup.

- 1. The SPTA method is applied on the address traces, which are obtained by running the benchmark on the Leon-3 processor. The results for the SPTA method are obtained by applying the formulas presented in section 5.3.1. The SPTA method is applied on the 1000 execution runs in ETP.
- 2. Our MBPTA method is based on the EVT as discussed in section 5.3.2. The MBPTA results are based on the 1000 runs of each benchmark running on the Leon-3 processor, which showed to be sufficient for MBPTA measurements [20]. As MBPTA is based on the property that each run ensures the i.i.d property [24]. The Kolmogorov-Smirnov test is performed on the execution-time measurements with a significance level of $\alpha = 0.05$ to prove all the timing measurements are identical. Table 5.1 shows that all benchmarks runs fulfill the *i.i.d* property.
- 3. We also obtained the WCET estimates for the deterministic cache enabled with the *modulo* placement and LRU replacement policies.

5.5.1 Cache Setup

It is not an easy task to compare SPTA and MBPTA techniques for the time-prediction on the same platform as each technique can be more suited to a specific software and hardware platform. A fair comparison between them can be made by choosing a suitable cache setup. Starting from a cache placement and replacement policy, we select time-randomized placement and replacement for SPTA and MBPTA. As discussed in [1], the combination of time randomized placement and time deterministic replacement provides no advantage over the other combinations (e.g. time-deterministic placement/replacement). Similarly, the results for the time randomized placement and time randomized replacement for SDTA is *very pessimistic*. The best suitable cache configuration for PTA has time-randomized placement and time-randomized replacement [1]. In short, to produce an accurate prediction of WCET estimates, the time-deterministic hardware is suitable for the DTA and time-randomized hardware is suitable for PTA.

5.6 Experimental Evaluation

We study the influence of *associativity, cache size, and line size* on the WCET estimates for the time-prediction.

5.6.1 Prediction Analysis under Associativity

The impact and behavior of the time-prediction associated with MBPTA and SPTA under varying associativity is discussed in this section. We also study how cache associativity can counter pessimism. Figure 5.1 shows how pessimism varies by changing the cache associativity by applying MBPTA technique. We used three set-associative(SA) cache structures. The cache configuration we used are: SA-2, SA-4, and SA-8 with 2 kB size and 32 bytes line size. We conclude with the following observations (O) under this cache configuration.

MBPTA:

O-1.1: The associativity helps to minimize the pessimism because with higher associativity the cache hit ratio improves. The execution-time is also decreased at higher associativity. The higher the associativity, the lower is the execution-time. Increasing the associativity also improves the prediction estimation because at higher associativity the execution-time distribution getting smooth provide tighter estimates.

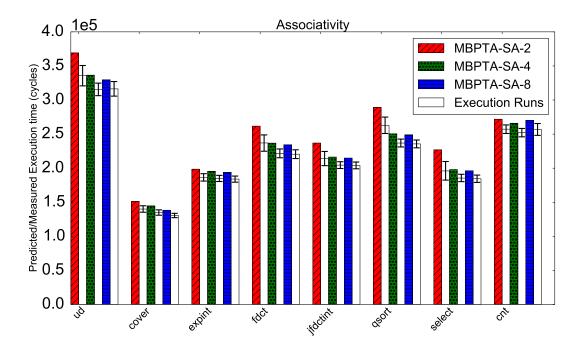


Figure 5.1 Impact on Time-Prediction by varying Associativity-MBPTA.

O-1.2: The predicted time (pWCET) is getting closer to the maximum execution-time of a C-code running on a processor by varying the associativity. The higher the associativity, the smaller is the overestimation. For example, for the cache with the associativity-2 (SA-2), the time-prediction is varied between 5.09% to 3.11%. This pessimism is decreased from 4.26% to 1.33% as shown in Figure 5.1 and summarizes in Table 5.2.

SPTA:

O-1.3: The SPTA technique is applied on the address traces of the code. The first observation is about performance: the SPTA performance is not as predictable as we observed for MBPTA. The pessimism is always higher for SPTA as compared with MBPTA as shown in Table 5.2.

O-1.4: The computed pWCETs does not depend on the associativity. Because of the overestimations added by the equation described in section 5.3.5, the pessimism does not decrease at higher cache associativity analysed through SPTA. This is due to the fact that the randomized cache needs to ensure the number of misses to ensure independence tests.

O-1.5: However, we have observed that the pessimism is improved within SPTA at higher associativity. Particularly, for the *jfdctint, cnt* the pessimism is decreased by 7.76% and 10.46% respectively. But pessimism is still higher than we found for the MBPTA.

O-1.6: The average difference between the predicted time and the maximum execution-time for the SPTA is 3.07% and 1.77% for the MBPTA.

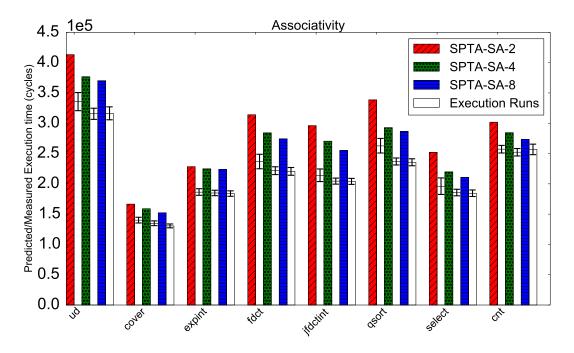


Figure 5.2 Impact on Time-Prediction by varying Associativity-SPTA.

5.6.2 Prediction Analysis under Cache Size

We study the effects of the cache size on time-prediction. The level of pessimism achieved varying the cache size is discussed in this section. We performed our test on three different sizes (2 kB, 4 kB, and 8 kB) with 2-way associative cache (SA-2), and the line size is 32-bytes.

MBPTA:

The impact of changing the cache size on the time-prediction by employing MBPTA is being studied. Figure 5.3 shows how much pessimism is varied by varying the cache size. We conclude with the following observations under this cache configuration.

O-2.1: The prediction difference between the predicted time and the maximum execution-time is decreased by increasing the cache size. The level of pessimism is decreased from 5.01% to 0.43% by increasing the size from 2-kB to 8-kB as summarized in Table 5.4. Increasing in the cache size helps to fit the binary code size into the cache and this ultimately improves the cache hit ratio.

O-2.2: Increasing the cache size helps to decrease the pWCET estimate. It results in a less pessimistic prediction time. Figure 5.3 shows the effects on the time-prediction under different cache sizes.

SPTA:

O-2.3: The behavior obtained by varying the cache size is almost the same the one observed when varying the *associativity*. The pessimistic value is quite higher, that is in between 1.25% and 3.53% as shown in the Table 5.4.

O-2.4: The average pessimistic difference between the predicted time and the actual execution-time

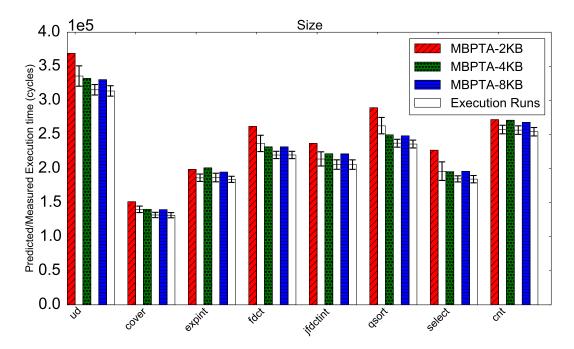


Figure 5.3 Impact on Time-Prediction by varying Cache Size-MBPTA.

from 2-kB to 8-kB is 2.38%. Whereas, for MBPTA, this difference factor is reduced to 1.93%. SPTA pessimistic nature does not help to minimize the level of pessimism as much MBPTA does.

5.6.3 Prediction Analysis under Line Size

The impact of the line size on the prediction is shown in Figure 5.5 when applying MBPTA and Figure 5.6 when applying SPTA. We have used two cachelines, i.e. 16-bytes line size and 32-bytes line size with the 4-way associativity, and the capacity is 4-kB. Data and instruction caches are used with the same parameters.

MBPTA:

O-3.1: We have observed that an increase in the line size decreases the pWCET estimate. Because larger cache lines minimize the number of loads from the memory that helps to reduce pessimism. As we observe from Figure 5.5, the average reduction in predicted time is 1.87%.

SPTA:

O-3.2: We observed the same behavior by varying the line size with SPTA as with MBPTA. The improvement factor is shown in Table 5.4. The difference between the predicted time and the maximum execution-time for SPTA by varying the line size is remarkably improved compared to varying the associativity and sizes. This is due to the fact that by increasing the line-size helps to minimize the number of loads from the memory as a result improve execution-time and prediction. For example, consider the test case Ud with associativity-4 (SA-4), the level of pessimism goes from 16.39% to 6.14% considering the same configuration by varying only the line size.

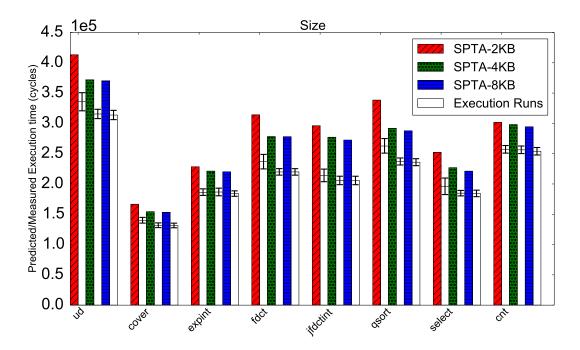


Figure 5.4 Impact on Time-Prediction by varying Cache Size-SPTA.

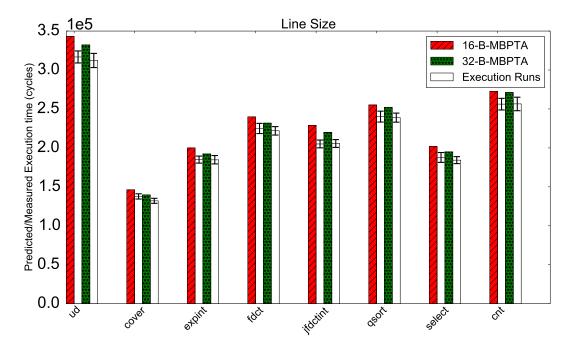


Figure 5.5 Impact on Time-Prediction by varying Cacheline-MBPTA.

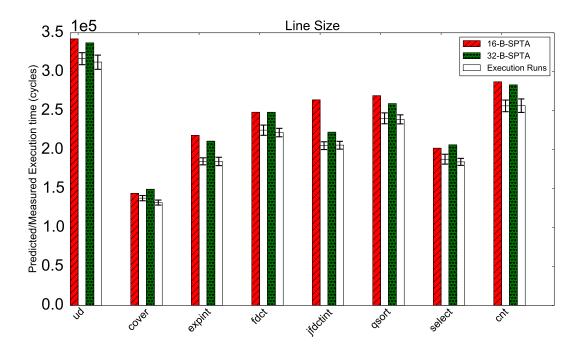


Figure 5.6 Impact on Time-Prediction by varying Cacheline-MBPTA.

Summary: Figure 5.7 shows a comparison between the deterministic cache enabled with modulo placement and LRU replacement for probabilistic cache used MBPTA and SPTA it also shows the comparison with the maximum measured execution-time. The result presented in Figure 5.7 is derived from the cache configuration SA-4, size-2 kB, and line-size-32 byte. We observed that

Benchmark						
	Associativity SA-2 to SA-8 MBPTA	Associativity SA-2 to SA-8 SPTA	Size SA 2-8 kB MBPTA	Size SA 2-8 kB SPTA	Line size SA 16-32 B MBPTA	Line size SA 16-32 B SPTA
ud	4.26	3.96	2.27	2.26	2.43	2.37
cover	1.24	1.23	1.13	1.41	0.45	0.52
expint	0.95	0.43	0.43	2.21	4.12	3.27
fdct	1.70	4.18	1.99	2.06	1.58	1.81
jfdctint	2.74	7.76	1.57	3.13	4.49	3.23
qsort-exam	2.21	3.82	2.70	3.53	0.15	0.70
select	4.80	7.93	5.01	3.21	0.88	0.62
cnt	1.33	10.46	0.35	1.25	1.11	0.82

Table 5.2 Level of Pessimism Introduced by varying Cache Parameters.

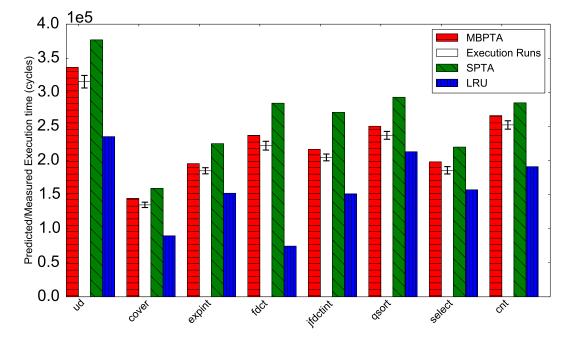


Figure 5.7 Comparison between Time-Prediction via Timing Techniques and Maximum Execution-Time.

the level of pessimism associated with a deterministic cache (analyzed with DTA) is higher than MBPTA and SPTA (probabilistic cache) as compared to the maximum execution-time. Performance in terms of prediction is lower for the deterministic cache. We observed that the prediction obtained with MBPTA and SPTA is closer to the actual execution-time. The results obtained for the deterministic cache are underestimated and they are quite far from the real execution-time as shown in Figure 5.7 and summarized in Table 5.3. This also proves the point we made in section 5.1, that probabilistic techniques performed well with randomized architecture. This result also shows a comprehensive qualitative analysis that each technique is particularly suitable for specific set of

Benchmark					
	Deterministic Cache (WCET)	Prediction bound	Probabilistic Cache (WCET)	Prediction bound (MBPTA)	Prediction bound (SPTA)
ud	235050	386920	324950	376500	376880
cover	107894	159792	138798	154526	158978
expint	152020	234689	189380	225458	224776
fdct	217066	291194	218092	234587	284119
jfdctint	150850	270891	209487	266357	270446
qsort	212880	294480	242609	280291	292840
select	157060	224975	190812	217977	219754
cnt	190980	289654	258480	285921	286535

Table 5.3 Deterministic/Probabilistic WCETs and respective Execution Bounds.

Table 5.4 Pessimism between Predicted pWCETs at 10^{-3} Exceedance Probability versus Deterministic Cache.

	Pessimism Difference($\%$)							
	ud	$\overline{\mathrm{cover}}$	$\overline{\operatorname{expint}}$	fdct	jfdctint	$\overline{\operatorname{qsort}}$	select	cnt
Deterministic cache	49.67	39.55	43.80	29.13	57.55	33.09	36.22	41.38
Probabilistic cache (MBPTA)	14.70	10.72	17.39	7.07	23.90	14.41	13.29	10.08
Probabilistic cache (SPTA)	14.80	13.55	17.09	26.29	25.40	18.70	14.10	10.30

software and hardware. SPTA shows more pessimism than MBPTA because SPTA is more sensitive to the knowledge of referenced addresses. It means EVT based MBPTA provides tightest pWCET estimations compared to SPTA.

Similarly, Table 5.3 shows the deterministic and probabilistic WCETs and respective bounds. These

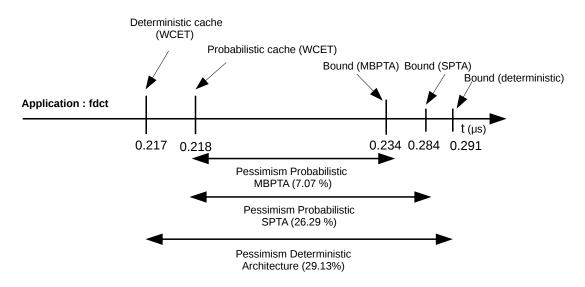


Figure 5.8 Pessimism between Predicted pWCETs at 10^{-3} Exceedance Probability versus Deterministic Cache.

results can be summarized in Table 5.4 which shows the pessimism difference between the MBPTA, SPTA, and deterministic cache. We used application **fdct** to elaborate the pessimism obtained by MBPTA is minimum as compared it with the SPTA and deterministic architecture shown in Figure 5.8. In summary, our tests show that the randomized cache can be used to apply MBPTA and SPTA techniques to find the time-predictions and associated pessimism. In short, compared to deterministic cache the observed execution-time and associated pessimism is improved for probabilistic cache. The difference between the deterministic cache execution-time and its associated prediction bounds is more pessimistic than the difference between the probabilistic cache execution-time and its associated prediction bounds.

CHAPTER 6 DISCUSSION

The main ideas of the work presented in this thesis are the design of a probabilistic system and analysis of this system with probabilistic timing analysis techniques to measure the time- prediction in terms of pWCET.

To get promising results and make the system probabilistically analyzable, a randomized cache is used. The randomized cache fulfills the requirements that are necessary for the probabilistic timing techniques, e.g., the *i.i.d* property. Probabilistic timing techniques in both variants—static and measurement-based techniques—are used. The MBPTA used the execution-time of the program. The execution-time is obtained by running the benchmark which comprises of C-code on the randomized hardware. The timing information is given to the MBPTA method and produced a tight pWCET estimation bound. Second, we used an SPTA method which used memory traces to find an upper bound for the WCET.

The PTA techniques produced probabilistically accurate WCET estimations that helped to find the execution bounds. The WCET estimation observed under probabilistic methods provided less pessimism when compared to the execution bound found on a deterministic architecture, e.g., a *lru* cache.

In accordance with the literature, to achieve the necessary requirements for the probabilistic techniques [21], a randomized cache is used under PTA techniques. The randomized cache is used to generate randomization of the timing behavior. Randomized placement and replacement policies is adopted in this work. A parametric hash function is used for the random placement policy, and a random number generator is used for the random replacement policy. Then, the randomized cache is integrated with the processors. We used two processors: MIPS-32 and Leon-3. The Mälardalen real-time benchmark is used for in our tests. The C-code is compiled with gcc and machine code is fed to the processors. We executed the same C-code/application several thousand times to obtain the execution-time measurements profile. The measurements we got consist of different timing values which correspond to the execution-times of the benchmark. To verify whether these timing values fulfill the requirements for PTA techniques, independence and identical distribution tests are applied on the timing values. After the successful verification of independence and identical distribution, measurement and static probabilistic techniques are used to establish the probabilistic WCET bound.

The PTA approach incurred the timing analysis wall. The static timing analysis methods failed to find solutions for the WCET estimation for complex hardware systems. This is because—as the complexity of the system is increased—driving the accurate, detailed knowledge of the hardware model is a cumbersome job. Furthermore, obtaining the detailed knowledge of the timing behavior of the program in the presence of varying hardware condition (e.g., knowledge of all previously executed instructions) is also a difficult job. Due to these limitations, PTA techniques emerged that are capable of removing the requirements for the detailed knowledge of the hardware and producing tightly bound WCET estimations. The obtained tight WCET estimations had less dependence on the execution history and required less platform knowledge. The lack of platform knowledge had an influence on the WCET estimations and provided execution bounds that are independent of the platform knowledge. We believe that the required knowledge needed to achieve reliable pWCET bounds can be accomplished by using the hardware platform whose execution-time does not depend on the execution history. The results obtained by applying PTA techniques on the randomized hardware are less pessimistic WCET estimations as compared with the deterministic timing analysis approach.

We discovered that the pessimism associated with PTA techniques is closed enough to the actual measurement as compared to the static approach. The primary objective of the PTA techniques is to provide a tight WCET estimation that is safe enough for the software program and to keep the overall system failure rate lower than the derived bound. The measurement-based probabilistic technique provides a pWCET estimation. The estimation achieved under MBPTA technique is end-to-end runs of a program. The pWCET observed under MBPTA is less pessimistic as compared to the static probabilistic method. In fact, MBPTA derived tight bounds are based on the actual observations rather than the convolution operation which are used by SPTA. To give evidence for our argument—that the pWCET estimations observed under the probabilistic techniques had less pessimistic and tightly bound to the actual measurements rather than the deterministic approach—we used a deterministic architecture, i.e. a LRU replacement and modulo placement. The deterministic approach had a better average performance but provides a high level of pessimism that sets the actual bound away from the real measurements. Setting the pWCET bound away from the actual measurements did not help real-time system designers to design a system with better schedulability analysis and best resource consumption.

The work accomplished so far in real-time systems timing analysis is mainly based on simulators rather than real hardware. The results and mathematical foundations presented in [44], [1], [45] support our findings. We can relate our findings to the work presented in the literature to support our work. As suggested by the work presented in [53], we found that the pWCET of a program under varying memory layout is suitable to apply PTA techniques. The authors used different memory layouts to get different timing values. The performance degrades with random policies as compared to other deterministic policies but it had an acceptable average case performance. Based on this observation, the authors developed their PTA techniques by using associative caches with random replacement policies [45]. We used the same strategy using randomized cache placement and replacement policies and analyzed the whole system with PTA techniques. We observed that it coincided with the theory and the general perception about the PTA techniques. The PTA techniques provide tightly bound pessimism associated with pWCET rather than improving the best execution-time. It is arguable that PTA techniques on randomized architectures are not suitable to improve the average case performance. Why should it be used in real-time systems? In real-time systems, the main focus is on the accurate prediction rather than average case performance improvement. Probabilistic techniques allow reducing the overestimation produced by traditional timing analysis approaches. This work is focused on single core architectures to develop a methodology to apply PTA techniques. The probabilistic approach on a multi-core architecture will be a best possible extension of this work. The problem associated with the use of multi-core architecture in real-time systems is task allocation. It is a challenging task to predict how the task will interact with each other in shared hardware resources. We believed that probabilistic techniques will be a promising solution to find pWCET bound for a multi-core architecture. Moreover, by employing an L2 cache, it will be interesting to see that how it influences the time predictability. Finally, an extension of this work could be the creation of a whole hardware architecture randomized with a randomized bus, TLBs, in order to measure the effects that randomization may introduce on the other components for pWCET estimation.

CHAPTER 7 CONCLUSION

The implementation of a time-predictable architecture, analyzed by probabilistic timing analysis (PTA) techniques is presented. As our target domain is a real-time industry, we stressed the importance of the worst-case execution-time (WCET) estimation. We redefined the concept of execution-time profiles to describe the probabilistic timing behaviour of our sources. The motivation of this work is based on the following observation:

The static WCET analysis is a complex technique mainly due to the necessity of building an asprecise-as-possible view of the impact of the execution history on the hardware state at each execution of the program. The over-approximation of this impact may degrade the accuracy of the WCET estimation. To overcome the modeling of the execution history, a probabilistic approach can be used to randomize the timing behaviour of a hardware component, e.g., a randomized cache. The randomization results in a smooth distribution of the execution-time probabilities. Then, a WCET probability distribution is computed using a technique named MBPTA based on EVT. To measure the execution-time probability distribution for individual operations, e.g., memory accesses, a technique is developed, named SPTA.

In the presence of a cache, accurate WCET estimation is a complex process. In this work, we analyzed randomized architecture with probabilistic timing analysis techniques. We verified that the probabilistic timing techniques, both static and measurement-based guaranteed the tightly bound WCET estimation if applied to the randomized architecture. Both probabilistic techniques MBPTA and SPTA offered various trade-offs regarding the performance, suitability, and pessimism.

The investigation of new timing analysis techniques is an unavoidable need because of the growing complexity of a modern computing system. The probabilistic timing techniques help to analyze complex computing systems to find the execution bound where meeting the deadline is the primary concern such as aerospace computing systems. This research has a potential to make computing systems smarter, more reliable, and easier to design and program. As PTA techniques have less dependency on the execution history, they give to the designer the ability to design a system with more freedom and suitability according to the requirements.

The work presented here is centered around a probabilistically analyzable randomized cache. Our randomized cache can be integrated with any processor to make the foundation for a probabilistically analyzable computing system. We implemented the RTL model of a randomized L1 data and instruction cache. This cache used a high-quality random number generator for random placement and replacement. Random placement is obtained with a parametric hash function that shuffles the association between memory addresses and cache blocks. The cache is integrated with the Ion MIPS32 processor, and verified to generate independent and identically distributed timing events so that MBPTA can be applied. We test our cache and PTA approach on a variety of C-code

sources from the Mälardalen benchmark suite and show a noticeable improvement (5-15%) in terms of measured Worst Case Execution Time (WCET) as well as enabling the identification of safe probabilistic WCET (pWCET) bounds.

We used PTA techniques for time-prediction and to find the level of pessimism by varying cache parameters. Levels of pessimism are evaluated under measurement and static probabilistic timing techniques. Our results are supported by the quantitative data and they can help user to choose better timing analysis techniques. The cache parameters are also adjustable with reference of an affordable pessimism. By varying cache parameters, we analyzed pWCET bound with both SPTA and MBPTA techniques. We observed that SPTA is more pessimistic than MBPTA. Extending this work to a multi-processor with a randomized bus will be a good idea for future work.

The research that we conducted proved the effectiveness of probabilistic timing analysis. Furthermore, our most recent results demonstrated that probabilistic timing technique is a promising approach for the future timing analysis techniques for a real-time system.

Through this research, we hope to be able to have an impact on how computer engineers and system designers will think of the probabilistic computing in near future, and contribute to creating the next generation of a real-time embedded systems for aerospace industry. At the same time, we think that our results will make decisive steps ahead in a relatively unexplored research area: integration of fault-tolerance techniques in time-predictable computer architecture.

REFERENCES

- Abella, Jaume and Hardy, Damien and Puaut, Isabelle and Quinones, Eduardo and Cazorla, Francisco J (2014). On the comparison of deterministic and probabilistic wcet estimation techniques. *Real-Time Systems (ECRTS), 2014 26th Euromicro Conference on.* IEEE, 266– 275.
- [2] Aeroflex-Gaisler (2016). The leon3 processor. http://www.gaisler.com.
- [3] Altmeyer, Sebastian and Cucu-Grosjean, Liliana and Davis, Robert I. (2015). Static probabilistic timing analysis for real-time systems using random replacement caches. *Real-Time* Syst., 51(1), 77–123.
- [4] Altmeyer, S. and Davis, R.I (2014). On the correctness, optimality and precision of static probabilistic timing analysis. Design, Automation and Test in Europe Conference and Exhibition (DATE), 2014. 1–6.
- [5] Altmeyer, Sebastian and Davis, Robert and others (2014). On the correctness, optimality and precision of static probabilistic timing analysis. *Design, Automation and Test in Europe Conference and Exhibition (DATE), 2014.* IEEE, 1–6.
- [6] F. Amoset and others (1991). Worst-case execution time analysis for a java processor. Journal of Algorithms, 12(4), 685–6–99.
- [7] Anantaraman, Aravindh and Seth, Kiran and Patil, Kaustubh and Rotenberg, Eric and Mueller, Frank (2003). Virtual simple architecture (visa): exceeding the complexity limit in safe real-time systems. ACM SIGARCH Computer Architecture News. ACM, vol. 31, 350–361.
- [8] Anwar, Hassan (2016). Probabilistically analysable cache. http://git.mistlab.ca/hanwar.
- [9] Anwar, Hassan and Chen, Chao and Beltrame, Giovanni (2015). A probabilistically analysable cache implementation on fpga. New Circuits and Systems Conference (NEWCAS), 2015 IEEE 13th International. IEEE, 1–4.
- [10] Anwar, hassan and Chen, Chao and Beltrame, Giovanni (2015). A probabilistically analysable cache implementation on fpga. New Circuit and System (NEWCAS), 2015 15th International Conference on. IEEE, 1–4.
- [11] H. Anwar and M. Daneshtalab and M. Ebrahimi and J. Plosila and H. Tenhunen and S. Dytckov and G. Beltrame (2014). Parameterized AES-based crypto processor for FPGAs. Digital System Design (DSD), 2014 17th Euromicro Conference on. 465–472.
- [12] Anwar, Hassan and Jafri, Syed and Dytckov, Sergei and Daneshtalab, Masoud and Ebrahimi, Masoumeh and Hemani, Ahmed and Posila, J. and Beltrame, G. and Tehunen, H. (2014). Exploring spiking neural network on coarse-grain reconfigurable architectures. *Proceedings of International Workshop on Manycore Embedded Systems*. ACM, New York, NY, USA, MES '14, 64–67.

- [13] ARM (2015). Cortex-M Core. http://www.arm.com/products/processors/cortex-m.
- [14] Bandyopadhyay, S. and Bhattacharya, R. (2015). Discrete and Continuous Simulation: Theory and Practice. CRC Press.
- [15] Bate, Iain and Conmy, Philippa and Kelly, Tim and McDermid, John (2001). Use of modern processors in safety-critical applications. *The Computer Journal*, 44(6), 531–543.
- [16] Christoph Berg and Jakob Engblom and Reinhard Wilhelm (2004). Requirements for and design of a processor with predictable timing. L. Thiele et R. Wilhelm, éditeurs, *Perspectives Workshop: Design of Systems with Predictable Behaviour*. Internationales Begegnungs- und Forschungszentrum für Informatik (IBFI), Schloss Dagstuhl, Germany, Dagstuhl, Germany, no. 03471 Dagstuhl Seminar Proceedings, 1–20.
- [17] Bernat, Guillem and Colin, Anotione and Petters, Stefan M (2002). Weet analysis of probabilistic hard real-time systems. *Real-Time Systems Symposium*, 2002. RTSS 2002. 23rd IEEE. IEEE, 279–288.
- [18] Beyls, Kristof and Hollander, Erik (2001). Reuse distance as a metric for cache behavior. Proceedings of the IASTED Conference on Parallel and Distributed Computing and systems. vol. 14, 350–360.
- [19] Boslaugh, Sarah and Watters, Paul Andrew (2008). Statistics in a nutshell a desktop quick reference. O'Reilly.
- [20] Cazorla, Francisco J and Vardanega, Tullio and Quiñones, Eduardo and Abella, Jaume (2013).
 Upper-bounding program execution time with extreme value theory. WCET. 64–76.
- [21] F. J. Cazorla and others (2013). Proartis: Probabilistically analyzable real-time systems. ACM Trans. Embed. Comput. Syst., 12(2s), 94:1–94:26.
- [22] Chaen, Chao and Santinelli, Luca Hugues and Beltrame, Giovanni (2016). Static probabilistic timing analysis in presence of faults. Proceedings of the 11th IEEE International Symposium on Industrial Embedded Systems. 1–10.
- [23] Conti, Massimo and Caldari, Marco and Vece, Giovanni B and Orcioni, Simone and Turchetti, Claudio (2004). Performance analysis of different arbitration algorithms of the amba abb bus. Proceedings of the 41st annual Design Automation Conference. ACM, 618–621.
- [24] G. Cucu and others (2012). Measurement-based probabilistic timing analysis for multi-path programs. *Real-Time Systems (ECRTS)*, 2012 24th Euromicro Conference on. 91–101.
- [25] Cucu-Grosjean, L. and Santinelli, L. and Houston, M. and Lo, C. and Vardanega, T. and Kosmidis, L. and Abella, J. and Mezzetti, E. and Quinones, E. and Cazorla, F.J. (2012). Measurement-based probabilistic timing analysis for multi-path programs. *Real-Time Systems* (ECRTS), 2012 24th Euromicro Conference on. 91–101.
- [26] David, Laurent and Puaut, Isabelle (2004). Static determination of probabilistic execution times. Proceedings of the 16th Euromicro Conference on Real-Time Systems. ECRTS '04, 223–230.

- [27] Davis, Robert and Santinelli, Luca and Altmeyer, Sebastian and Maiza, Claire and Cucu-Grosjean, Liliana and others (2013). Analysis of probabilistic cache related pre-emption delays. *Real-Time Systems (ECRTS), 2013 25th Euromicro Conference on.* IEEE, 168–179.
- [28] Davis, Robert I (2013). Improvements to static probabilistic timing analysis for systems with random cache replacement policies. 2013 4th Real-Time Scheduling Open Problems Seminar, RTSOPS'13. 1–3.
- [29] Delvai, Martin and Huber, Wolfgang and Puschner, Peter and Steininger, Andreas (2003). Processor support for temporal predictability-the spear design example. *Real-Time Systems*, 2003. Proceedings. 15th Euromicro Conference on. IEEE, 169–176.
- [30] Edwards, Stephen A and Lee, Edward A (2007). The case for the precision timed (pret) machine. *Proceedings of the 44th annual Design Automation Conference*. ACM, 264–265.
- [31] Gnedenko, Boris (1943). Sur la distribution limite du terme maximum d'une serie aleatoire. Annals of mathematics, 423–453.
- [32] Goresky, Mark and Klapper, Andrew (2003). Efficient multiply-with-carry random number generators with maximal period. ACM Trans. Model. Comput. Simul., 13(4), 310–321.
- [33] Griffin, David and Lesage, Benjamin and Burns, Alan and Davis, Robert I. (2014). Static probabilistic timing analysis of random replacement caches using lossy compression. *Proceedings* of the 22Nd International Conference on Real-Time Networks and Systems. ACM, New York, NY, USA, RTNS '14, 289:289–289:298.
- [34] Gumbel, Emil Julius and Lieblein, Julius (1954). Statistical theory of extreme values and some practical applications: a series of lectures, vol. 33. US Government Printing Office Washington.
- [35] Jan Gustafsson and Adam Betts and Andreas Ermedahl and Björn Lisper (2010). The Mälardalen WCET benchmarks – past, present and future. B. Lisper, éditeur, WCET2010. OCG, Brussels, Belgium, 137–147.
- [36] Hansen, Jeffery and Hissam, Scott A and Moreno, Gabriel A (2009). Statistical-based wcet estimation and validation. Proceedings of the 9th Intl. Workshop on Worst-Case Execution Time (WCET) Analysis. 1–10.
- [37] Heckmann, Reinhold and Langenbach, Marc and Thesing, Stephan and Wilhelm, Reinhard (2003). The influence of processor architecture on the design and the results of wcet tools. *Proceedings of the IEEE*, 91(7), 1038–1054.
- [38] Heimdahl, Mats PE (2007). Safety and software intensive systems: Challenges old and new. 2007 Future of Software Engineering. IEEE Computer Society, 137–152.
- [39] Hoeffding, Wassily (1963). Probability inequalities for sums of bounded random variables. Journal of the American statistical association, 58(301), 13–30.
- [40] Jalle, Javier and Abella, Jaume and Quinones, Eduardo and Fossati, Luca and Zulianello, Marco and Cazorla, Francisco J (2014). Ahrb: A high-performance time-composable amba

ahb bus. Real-Time and Embedded Technology and Applications Symposium (RTAS), 2014 IEEE 20th. IEEE, 225–236.

- [41] Jalle, Javier and Kosmidis, Leonidas and Abella, Jaume and Quiñones, Eduardo and Cazorla, Francisco J. (2014). Bus designs for time-probabilistic multicore processors. Proceedings of the Conference on Design, Automation & Test in Europe. European Design and Automation Association, 3001 Leuven, Belgium, Belgium, DATE '14, 50:1–50:6.
- [42] Kirner, Raimund and Puschner, Peter (2010). Time-predictable computing. Software Technologies for Embedded and Ubiquitous Systems, Springer. 23–34.
- [43] Kosmidis, Leonidas and Abella, Jaume and Wartel, Franck and Quinones, Eduardo and Colin, Antoine and Cazorla, Francisco J (2014). Pub: path upper-bounding for measurement-based probabilistic timing analysis. *Real-Time Systems (ECRTS), 2014 26th Euromicro Conference* on. IEEE, 276–287.
- [44] Kosmidis, Leonidas and Quinones, Eduardo and Abella, Jaume and Vardanega, Tullio and Broster, Ian and Cazorla, Francisco J (2014). Measurement-based probabilistic timing analysis and its impact on processor architecture. *Digital System Design (DSD), 2014 17th Euromicro Conference on.* IEEE, 401–410.
- [45] Kosmidis, Leonidas and others (2013). A cache design for probabilistically analysable real-time systems. Proceedings of the Conference on Design, Automation and Test in Europe. DATE '13, 513–518.
- [46] Kreuzinger, Jochen and Marston, R and Ungerer, Th and Brinkschulte, Uwe and Krakowski, C (1999). The komodo project: Thread-based event handling supported by a multithreaded java microcontroller. *EUROMICRO Conference*, 1999. Proceedings. 25th. IEEE, vol. 2, 122–128.
- [47] Lahiri, Kanishka and Raghunathan, Anand and Lakshminarayana, Ganesh (2001). Lotterybus: A new high-performance communication architecture for system-on-chip designs. *Proceedings* of the 38th annual Design Automation Conference. ACM, 15–20.
- [48] Malik, Sharad and Martonosi, Margaret and Li, Yau-Tsun Steven (1997). Static timing analysis of embedded software. *Proceedings of the 34th Annual Design Automation Conference*. ACM, New York, NY, USA, DAC '97, 147–152.
- [49] Matsumoto, Makoto and others (1998). Mersenne twister: A 623-dimensionally equidistributed uniform pseudo-random number generator. ACM Trans. Model. Comput. Simul., 8(1), 3–30.
- [50] MENTOR GRAPHICS (accessed 2016). Modelsim. http://www.modelsim.com.
- [51] Mezzetti, Enrico and Ziccardi, Marco and Vardanega, Tullio and Abella, Jaume and Quiñones, Eduardo and Cazorla, Francisco J (2015). Randomized caches can be pretty useful to hard real-time systems. *Leibniz Transactions on Embedded Systems*, 2(1), 01–1.
- [52] Opencores (2016). Complex gaussian pseudo random number generator. http://opencores. org/project/complex-gaussian-pseudo-random-number-generator.

- [53] Quinones, Eduardo and Berger, Emery D and Bernat, Guillem and Cazorla, Francisco J (2009). Using randomized caches in probabilistic real-time systems. *Real-Time Systems*, 2009. ECRTS'09. 21st Euromicro Conference on. IEEE, 129–138.
- [54] Reineke, Jan (2014). Randomized caches considered harmful in hard real-time systems. Leibniz Transactions on Embedded Systems, 1(1), 03–1.
- [55] Reineke, Jan and Grund, Daniel and Berg, Christoph and Wilhelm, Reinhard (2007). Timing predictability of cache replacement policies. *Real-Time Syst.*, 37(2), 99–122.
- [56] Ruiz, José Antonio (2016). The ION processor. https://github.com/jaruiz/ION.
- [57] Santinelli, Luca and Cucu-Grosjean, Liliana (2011). Toward probabilistic real-time calculus. SIGBED Rev., 8(1), 54–61.
- [58] Schoeberl, Martin (2009). Time-predictable computer architecture. *EURASIP J. Embedded* Syst., 2009, 2:1–2:17.
- [59] Schoeberl, Martin (2009). Time-predictable computer architecture. EURASIP Journal on Embedded Systems, 2009, 2.
- [60] Schoeberl, Martin and Chong, David Vh and Puffitsch, Wolfgang and Sparsø, Jens (2014). A time-predictable memory network-on-chip. 14th International Workshop on Worst-Case Execution Time Analysis. 53.
- [61] Schoeberl, Martin and Schleuniger, Pascal and Puffitsch, Wolfgang and Brandner, Florian and Probst, Christian W and Karlsson, Sven and Thorn, Tommy (2011). Towards a timepredictable dual-issue microprocessor: The patmos approach. *Bringing Theory to Practice: Predictability and Performance in Embedded Systems.* vol. 18, 11–21.
- [62] Serfozo, Richard (2009). Basics of applied stochastic processes. Springer.
- [63] Thiele, Lothar and Wilhelm, Reinhard (2004). Design for timing predictability. *Real-Time Systems*, 28(2-3), 157–177.
- [64] Topham, Nigel and González, Antonio (1999). Randomized cache placement for eliminating conflicts. *IEEE Trans. Comput.*, 48(2), 185–192.
- [65] Udipi, Aniruddha N and Muralimanohar, Naveen and Balasubramonian, Rajeev (2010). Towards scalable, energy-efficient, bus-based on-chip networks. *High Performance Computer* Architecture (HPCA), 2010 IEEE 16th International Symposium on. IEEE, 1–12.
- [66] Ungerer, Theo and Cazorla, Francisco and Casse, Hugues and Uhrig, Sascha and Guliashvili, Irakli and Houston, Michael and Kluge, Floria and Metzlaff, Stefan and Mische, Jorg and Sainrat, Pascal and others (2010). Merasa: Multicore execution of hard real-time applications supporting analyzability. *IEEE Micro*, (5), 66–75.
- [67] Whitham, Jack (2008). Real-time processor architectures for worst case execution time reduction. Thèse de doctorat, University of York.
- [68] Wilhelm, R (2005). Determining bounds on execution times. handbook on embedded systems.

- [69] Wilhelm, Reinhard and Engblom, Jakob and Ermedahl, Andreas and Holsti, Niklas and Thesing, Stephan and Whalley, David and Bernat, Guillem and Ferdinand, Christian and Heckmann, Reinhold and Mitra, Tulika and others (2008). The worst-case execution-time problem—overview of methods and survey of tools. ACM Transactions on Embedded Computing Systems (TECS), 7(3), 36.
- [70] R. Wilhelm and others (2008). The worst-case execution-time problem overview of methods and survey of tools. ACM Trans. Embed. Comput. Syst., 7(3), 36:1–36:53.
- [71] Wolf, Fabian and Kruse, Judita and Ernst, Rolf (2002). Timing and power measurement in static software analysis. *Microelectronics journal*, 33(1), 91–100.
- [72] Zhou, Shuchang (2010). An efficient simulation algorithm for cache of random replacement policy. C. Ding, Z. Shao et R. Zheng, éditeurs, *Network and Parallel Computing*. Springer Berlin Heidelberg, vol. 6289 de *Lecture Notes in Computer Science*, 144–154.

APPENDIX A MARKOV MODEL FOR SPTA

The SPTA method used in this work is based on the Markov chains. This method is applied to a set associative cache in which the analysis of each cache set can be performed separately as a fully associative cache. The method uses a memory trace as the input, and computes a pWCET as the output. This method is based on the system states, which are similar to other accurate SPTA approaches [4, 33] for random caches.

A Markov chain is a random process that describes how a system undergoes transitions from one state to another state. It poses a property that the probability distribution of the future state of a system depends only on the current state, such a system forms a Markov chain. The current state explains the status of the system, and the transition matrix describes how the system transits into the future state. For a cache with evict-on-miss random replacement policy, every time a cache miss occurs, a cache block is randomly selected and replaced with the new content of a memory. As a result, there may be different data in the cache at different times, i.e. the memory contents of the cache changes with time. To illustrate the status of the system, s_i is defined as the memory layout of the cache and $|s_i|$ is the number of elements in this state. In-order to show how to construct states from a trace of memory access by a task. Consider an example with a task τ and a 2-way cache. The memory accesses from τ are a, d, c, a, d. Then we can define the state space as $s_0 = \emptyset$, $s_1 = \{a\}$, $s_2 = \{d\}$, $s_3 = \{c\}$, $s_4 = \{a, d\}$, $s_5 = \{a, c\}$, $s_6 = \{d, c\}$. We can see that all memory contents are included in the states, and $|s_0| = 0, |s_i| = 1 : i = 1, 2, 3, |s_i| = 2 : i = 4, 5, 6.$

Each program step means as an access to a new memory address. Every time a memory address is accessed, the system takes 1 time step and the system state may change. Each possible state of the system, i.e. memory content, at a given step is associated with a probability.

The \overline{S} is used to represent state occurrence probability vector:

$$\overline{S} = [Pr(s_0), Pr(s_1), \cdots], \tag{A.1}$$

where $Pr(s_i)$ is the probability of the state s_i . With *m* being the number of different memory addresses in the program, and *l* being minimal value between cache associativity and *m*, the number of states can be calculated as:

$$\sum_{k=0}^{l} \begin{pmatrix} m \\ k \end{pmatrix}. \tag{A.2}$$

The transition matrix \overline{P} needs to define which describes how one state varies move from present

state to the next state. It is represented as:

$$\overline{P} = \begin{pmatrix} p_{0\to0}, & p_{0\to1}, & \cdots \\ p_{1\to0}, & p_{1\to1}, & \cdots \\ \vdots & \vdots & \ddots \end{pmatrix},$$
(A.3)

where $p_{i\to j}$ is the probability for the system to go from state s_i to state s_j . In this method, $p_{i\to j}$ varies constantly, because it depends on the present system state and the memory accesses. At each step, the system may access different memory addresses and its state may change. Consequently, the transition probability $p_{i\to j}$ may change and this is known as a non-homogeneous Markov chain model.

Consider \overline{S}_k and \overline{P}_k are the state probability vector and the transition matrix at step k, respectively, then we have

$$\overline{S}_{k+1} = \overline{S}_k \overline{P}_k. \tag{A.4}$$

We can see that the state of the system for next step only depends on current state and the transition matrix.