UNIVERSITÉ DE MONTRÉAL

DEVELOPMENT OF A CRITICALLY EVALUATED THERMODYNAMIC DATABASE FOR THE SYSTEMS CONTAINING ALKALINE-EARTH OXIDES

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DEVELOPMENT OF A CRITICALLY EVALUATED THERMODYNAMIC DATABASE FOR THE SYSTEMS CONTAINING ALKALINE-EARTH OXIDES

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DEDICATION

I want to dedicate this thesis to my family in India.

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RÉSUMÉ

Dans un système thermodynamique multicomposant, les relations de phases entre les constituants sont généralement très complexes. En particulier, les systèmes à base d'oxydes sont souvent très difficiles à étudier en raison des températures très élevées et de l'action corrosive des laitiers. A cause de ces difficultés, de grandes incohérences et dispersions sont souvent observées parmi les données expérimentales disponibles dans la littérature. Afin d'étudier et de comprendre de manière efficace les relations de phases complexes, il est très utile de développer des banques de données thermodynamiques contenant les paramètres optimisés d'un modèle d'énergie libre de Gibbs, permettant de dériver les propriétés thermodynamiques de toutes les phases en fonction de la température et de la composition. Dans une optimisation thermodynamique, les paramètres ajustables du modèle d'énergie libre de Gibbs sont calculés en utilisant simultanément toutes les données thermodynamiques et d'équilibres de phases disponibles afin d'obtenir un ensemble d'équations en fonction de la température et de la composition. Les données thermodynamiques, telles que les activités, peuvent aider à évaluer les diagrammes de phases, et les informations sur les équilibres de phases peuvent être utilisées pour déduire les propriétés thermodynamiques. Ainsi, il est souvent possible de résoudre les divergences observées entre les données expérimentales disponibles. A partir des équations du modèle, toutes les propriétés thermodynamiques et les diagrammes de phases peuvent être calculés rétrospectivement. Il est également possible d'effectuer des interpolations et extrapolations de manière cohérente d'un point de vue thermodynamique. Les données sont ainsi rendues auto-cohérentes et, conformément aux principes thermodynamiques, les données expérimentales disponibles sont reproduites par un petit jeu de paramètres du modèle; ce qui est idéal pour le stockage informatique.

Dans le cadre d'un vaste projet de recherche au Centre de Recherche en Calcul Thermochimique (CRCT) au sein de l'Ecole Polytechnique de Montréal, nous avons développé une banque de données thermodynamiques pour les systèmes d'oxydes multicomposants. Cette thèse consiste en l'ajout des composants SrO et BaO à la banque de données multicomposante existant déjà pour le système SiO₂-B₂O₃-Al₂O₃-CaO-MgO. Au fil des années, en collaboration avec de nombreuses compagnies industrielles, une banque de données thermodynamiques a été développée pour le système SiO₂-B₂O₃-Al₂O₃-CaO-MgO de manière tout à fait satisfaisante. L'objectif du présent travail est d'améliorer l'applicabilité de cette banque de données en y ajoutant les nouveaux composants SrO et BaO. Les banques de données élaborées dans ce travail seront d'une importance particulière pour les industries des verres et de l'acier.

Dans le système SiO₂-B₂O₃-Al₂O₃-CaO-MgO-BaO-SrO, il y a 11 sous-systèmes binaires et 25 sous-systèmes ternaires contenant soit BaO, soit SrO ou bien les deux à la fois. Pour la plupart de ces systèmes binaires, et pour aucun de ces systèmes ternaires, des « optimisations » thermodynamiques sont déjà disponibles dans la littérature. Dans cette thèse, nous présentons l'évaluation et l'optimisation thermodynamique de 11 sous-systèmes binaires, 17 sous-systèmes ternaires et 5 sous-systèmes quaternaires contenant BaO et/ou SrO issus du système SiO₂-B₂O₃-Al₂O₃-CaO-MgO-BaO-SrO. Toutes ces optimisations thermodynamiques ont été effectuées en se basant sur les données expérimentales disponibles dans la littérature, à l'exception du système SrO-B₂O₃-SiO₂ qui a été optimisé à partir de données expérimentales obtenues dans le présent travail en conjonction avec les données issues de la littérature.

Dans cette thèse, tous les calculs ont été réalisés à l'aide du logiciel FactSage[™] de calcul d'équilibres thermodynamiques. Le Modèle Quasichimique Modifié (MQM) prenant en compte l'ordre à courte distance a été utilisé pour la phase liquide. Tous les systèmes binaires ont été évalués de manière critique et optimisés à partir des données thermodynamiques et d'équilibre de phases disponibles dans la littérature. Les paramètres du modèle obtenus ont été utilisés pour représenter les énergies de Gibbs de toutes les phases en fonction de la température et de la composition. Les paramètres binaires du modèle ont été utilisés pour estimer les propriétés thermodynamiques des phases dans les systèmes ternaires. Des modèles « géométriques » appropriés ont été utilisés pour ces estimations. Les diagrammes de phases ternaires ont été calculés et comparés avec les données expérimentales disponibles. Des paramètres d'interaction ternaires ont également été ajoutés lorsque cela était nécessaire.

La première partie de cette thèse est consacrée à une revue exhaustive de la littérature sur le thème de la modélisation thermodynamique et des techniques expérimentales de détermination de diagrammes de phases. Les chapitres suivants comprennent la revue de la littérature ainsi que les optimisations thermodynamiques des différents systèmes. La dernière partie de cette thèse est consacrée à la présentation du travail expérimental (trempe et EPMA) effectué pour le système SrO-B₂O₃-SiO₂.

ABSTRACT

In a thermodynamic system which contains several elements, the phase relationships among the components are usually very complex. Especially, systems containing oxides are generally very difficult to investigate owing to the very high experimental temperatures and corrosive action of slags. Due to such difficulties, large inconsistencies are often observed among the available experimental data. In order to investigate and understand the complex phase relationships effectively, it is very useful to develop thermodynamic databases containing optimized model parameters giving the thermodynamic properties of all phases as functions of temperature and composition. In a thermodynamic optimization, adjustable model parameters are calculated using, simultaneously, all available thermodynamic and phase-equilibrium data in order to obtain one set of model equations as functions of temperature and composition. Thermodynamic data, such as activities, can aid in the evaluation of the phase diagrams, and information on phase equilibria can be used to deduce thermodynamic properties. Thus, it is frequently possible to resolve discrepancies in the available data. From the model equations, all the thermodynamic properties and phase diagrams can be back-calculated, and interpolations and extrapolations can be made in a thermodynamically correct manner. The data are thereby rendered self-consistent and consistent with thermodynamic principles, and the available data are distilled into a small set of model parameters, ideal for computer storage.

As part of a broader research project at the *Centre de Recherche en Calcul Thermochimique* (CRCT), Ecole Polytechnique to develop a thermodynamic database for multicomponent oxide systems, this thesis deals with the addition of components SrO and BaO to the existing

multicomponent database of the $SiO_2-B_2O_3-Al_2O_3-CaO-MgO$ system. Over the years, in collaboration with many industrial companies, a thermodynamic database for the $SiO_2-B_2O_3-Al_2O_3-CaO-MgO$ system has been built quite satisfactorily. The aim of the present work was to improve the applicability of this five component database by adding SrO and BaO to it. The databases prepared in this work will be of special importance to the glass and steel industries.

In the SiO₂-B₂O₃-Al₂O₃-CaO-MgO-BaO-SrO system there are 11 binary systems and 25 ternary systems which contain either BaO or SrO or both. For most of these binary systems, and for none of these ternary systems, is there a previous thermodynamic optimization available in the literature. In this thesis, thermodynamic evaluation and optimization for the 11 binary, 17 ternary and 5 quaternary BaO- and SrO- containing systems in the SiO₂-B₂O₃-Al₂O₃-CaO-MgO-BaO-SrO system is presented. All these thermodynamic optimizations were performed based on the experimental data available in the literature, except for the SrO-B₂O₃-SiO₂ system. This latter system was optimized on the basis of a few experimental data points generated in the present work together with the data from the literature.

In the present work, all the calculations were performed using the FactSageTM thermochemical software. The Modified Quasichemical Model (MQM), which is capable of taking short-range ordering into account, was used for the liquid phase. All the binary systems were critically evaluated and optimized using available phase equilibrium and thermodynamic data. The model parameters obtained as a result of this simultaneous optimization were used to represent the Gibbs energies of all phases as functions of temperature and composition. Optimized binary

model parameters were used to estimate the thermodynamic properties of phases in the ternary systems. Proper "geometric" models were used for these estimations. Ternary phase diagram were calculated and compared with available experimental data. Wherever required, ternary interaction parameters were also added.

The first part of this thesis comprises a general literature review on the subject of thermodynamic modeling and experimental techniques for phase diagram determination. The next chapters include the literature review and the thermodynamic optimizations of the various systems. The last part of the thesis is the presentation of experiments performed in the present work, by quenching and EPMA, in the SrO-B₂O₃-SiO₂ system. The experiments were designed to generate the maximum amount of information with the minimum number of experiments using the thermodynamic optimization, based only on the data available in the literature, as a guide. These newly-obtained data improved the (preceding) thermodynamic optimization, based on the experimental data in the literature, of this ternary system.

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C_p	Molar heat capacity (J/mol·K)
$G^0_{\ i}$	Standard Gibbs energy of i (J/mol)
G^m	Gibbs energy of solution (J)
G^{E}	Excess Gibbs energy in solution (J)
g^E	Molar excess Gibbs energy in solution (J/mol)
g^0_i	Molar Gibbs energy of <i>i</i> (J/mol)
$\varDelta g_{ij}$	Gibbs energy change for the formation of two moles of i - j pairs (J)
$H^0_{\ i}$	Standard enthalpy of i relative to a standard elemental reference (J/mol)
ΔH	Molar enthalpy of mixing (J/mol)
ΔH_T	Enthalpy of formation of the compound from elements (J/mol)
n _{ij}	Number of moles of <i>i</i> - <i>j</i> bonds
q^{ij}_{AB}	Excess interaction parameter between A and B (J/mol)
S^{0}_{i}	Standard entropy of component i (J/mol·K)
ΔS_T	Entropy of formation of the compound from elements (J/mol·K)
ΔS^{conf}	Molar configurational entropy of solution (J/mol·K)
S ^{non-conf}	Molar non-configurational entropy of solution (J/mol·K)
n_i	Number of moles of component <i>i</i>
Т	Absolute temperature (K)
wt. %	Weight percent
<i>Yi</i>	Site fraction of component <i>i</i>
Y_i	Coordination-equivalent fractions
X_i	Mole fraction of component <i>i</i> in solution
X_{ij}	Pair fraction of <i>i</i> - <i>j</i> pairs
Z_i	Coordination number of <i>i</i>
Z^{i}_{ii}	The values of Z_i when all the nearest neighbors of an <i>i</i> are <i>i</i> 's
Z^{i}_{ij}	The values of Z_i when all the nearest neighbors of an <i>i</i> are <i>j</i> 's

LIST OF SYMBOLS

INTRODUCTION

In a thermodynamic system which contains several elements, the phase relationships among the components are very complex. Especially, the systems containing oxides are extremely difficult to investigate owing to the very high experimental temperatures and corrosive action of slags. Due to such difficulties in oxide systems, large inconsistencies are often observed among the available experimental data. In order to investigate and understand the complex phase relationships effectively, it is very useful to develop thermodynamic databases containing model parameters giving the thermodynamic properties of all phases as functions of temperature and composition.

Such thermodynamic databases are prepared by critical evaluation, modeling, and optimization. In a thermodynamic optimization, adjustable model parameters are calculated using, simultaneously, all available thermodynamic and phase-equilibrium data in order to obtain one set of model equations as functions of temperature and composition. Thermodynamic data, such as activities, can aid in the evaluation of the phase diagrams, and information on phase equilibria can be used to deduce thermodynamic properties. Thus, it is frequently possible to resolve discrepancies in the available data. From the model equations, all of the thermodynamic properties and phase diagrams can be back-calculated, and interpolations and extrapolations can be made in a thermodynamically correct manner. The data are thereby rendered self-consistent and consistent with thermodynamic principles, and the available data are distilled into a small set of model parameters, ideal for computer storage. In addition to the development of new models to represent the Gibbs energies of phases and the development of thermodynamic databases to describe the behavior of solutions, the *Centre de Recherche en Calcul Thermochimique* (CRCT) at Ecole Polytechnique, Montreal has developed the software FactSageTM (FactSage 2008). FactSageTM is the fusion of the FACT-Win/F*A*C*T and ChemSage/SOLGASMIX (Eriksson and Hack, 1990) thermochemcial packages that were founded 25 years ago. The FactSage package runs on a PC operating under Microsoft Windows and consists of a series of information, database, calculation and manipulation modules that enable one to access and manipulate databases for pure substances and solutions. Using FactSageTM one will be able to access the databases to calculate the amounts and compositions of all phases at equilibrium at any temperature and composition in multicomponent systems, to follow the course of equilibrium or non-equilibrium cooling, to calculate corresponding heat effects, *etc.* The phase diagrams and thermodynamic data generated by these databases will also be helpful in systematic planning of future experiments. This will greatly reduce the number of experiments required, and in turn resources and time will be saved.

As part of a broader research project at the *Centre de Recherche en Calcul Thermochimique* (CRCT), Ecole Polytechnique to develop a thermodynamic database for multicomponent oxide systems, the present work deals with the addition of the components SrO and BaO to the existing multicomponent database of the SiO₂-B₂O₃-Al₂O₃-CaO-MgO system. Over the years, in collaboration with many industrial companies, a thermodynamic database for the SiO₂-B₂O₃-Al₂O₃-CaO-MgO system has been built quite satisfactorily. SiO₂, B₂O₃, and Al₂O₃ are commercially important oxides used extensively in various industrial applications. CaO and MgO

oxides are used as network-modifiers in glasses. BaO and SrO are also very important oxides in many industrial applications. BaO is one of the major components in some of the optical glasses. BaO and SrO are used to block X-rays in cathode ray and TV tubes. BaO-SrO-Al₂O₃-SiO₂ is a key system to understand the degradation of uranium oxide and reaction with cement walls in nuclear power plants. SrO and BaO are vying with other oxides for many potential applications in the steel industry. BaO and SrO are now looked upon as future fluxing materials for refining of molten steel and ferro-alloys: removal of sulfur, phosphorous, carbon, and other impurities. The databases prepared in this project will be of special importance to these industries. In fact, this work is partially funded by three glass companies: Corning (USA), Schott (Germany), St-Gobain (Paris); and by a steel company, POSCO (South Korea). Moreover, for most of the SrO and BaO containing binary and higher-order oxide systems there is no thermodynamic assessment available in the literature. Hence, there are immense opportunities to critically evaluate these systems.

In the SiO₂-B₂O₃-Al₂O₃-CaO-MgO-BaO-SrO system there are 11 binary systems which contain either BaO or SrO (or both):

- 1. SrO-BaO
- 2. SrO-CaO
- 3. BaO-MgO
- 4. SrO-MgO
- 5. BaO-CaO
- 6. $SrO-SiO_2$

- 7. $BaO-SiO_2$
- 8. $SrO-Al_2O_3$
- 9. $BaO-Al_2O_3$
- 10. $BaO-B_2O_3$
- **11.** SrO-B₂O₃

In the present work, all of these 11 binary systems were critically evaluated and optimized.

And, in the SiO_2 -B₂O₃-Al₂O₃-CaO-MgO-BaO-SrO system there are 25 ternary systems which contain either BaO or SrO (or both):

- 1. BaO-SrO-SiO₂
- 2. CaO-SrO-SiO₂
- 3. $BaO-CaO-SiO_2$
- 4. SrO-MgO-SiO₂
- 5. BaO-MgO-SiO₂
- $6. \quad CaO\text{-}SrO\text{-}Al_2O_3$
- 7. BaO-CaO-Al₂O₃
- 8. SrO-BaO-Al₂O₃
- 9. BaO-MgO-Al₂O₃
- 10. BaO-Al₂O₃-SiO₂
- 11. SrO-Al₂O₃-SiO₂
- 12. BaO-B₂O₃-SiO₂
- 13. $SrO-B_2O_3-SiO_2$

14. BaO-B₂O₃-Al₂O₃

- 15. SrO-B₂O₃-Al₂O₃ 16. SrO-BaO-B₂O₃
- 17. BaO-CaO-B $_2O_3$
- 18. SrO-BaO-CaO
- 19. SrO-BaO-MgO
- 20. SrO-CaO- B_2O_3
- 21. SrO-CaO-MgO
- 22. SrO-MgO- B_2O_3
- $23.\,SrO\text{-}MgO\text{-}Al_2O_3$
- 24. BaO-CaO-MgO
- 25. BaO-MgO- B_2O_3

In the literature, whenever experimental data were available for these systems they were critically evaluated and optimized. A few experimental data for the higher-order (quaternary) system were also available. They were also evaluated and optimized.

In the present work, a few experimental data in the $SrO-B_2O_3$ -SiO₂ system, by quenching and EPMA, were also generated. The experiments were designed to generate the maximum amount of information with the minimum number of experiments using the thermodynamic optimization, based only on the data available in the literature, as a guide. These newly obtained data improved the (preceding) thermodynamic optimization of this system.

The Modified Quasichemical Model (MQM) developed at the *Centre de Recherche en Calcul Thermochimique* at Ecole Polytechnique, Montreal was used to model the liquid phase. This model is capable of taking into account ordering or clustering in the liquid phase. The liquid phase is technologically one of the most important phases appearing in every system. The adequate representation of its Gibbs energy plays a decisive role in database preparation for multicomponent systems. This model has been satisfactorily used by its developers and others to model not only liquid oxides but also alloys, mattes and salts.

In the present work, first the binary systems containing BaO and SrO were critically evaluated. (All other binary sub-systems have been critically evaluated and optimized previously.) All available thermodynamic and phase diagram data for these systems were collected and critically assessed for their reliability. The Gibbs energies of all phases were represented by appropriate model equations. The parameters of these models were obtained by an optimization procedure using the FactSageTM (FactSage 2008) software. These binary parameters were then used along with the models to predict the thermodynamic properties and phase diagrams of the ternary systems. All available data on the ternary systems (containing BaO and SrO) were collected. The predictions for the ternary systems were compared with the available ternary data, and the models were refined through the inclusion of ternary parameters, where required, for those systems where sufficient data were available.

1. LITERATURE REVIEW

In this chapter a general review of the literature on the topic of evaluation and optimization of phase diagrams is given. A brief review of experimental techniques for phase diagram measurement is also presented. In this literature survey, the doctoral thesis by Jung (Jung, 2003) and masters thesis by Shukla (Shukla, 2008) on a similar work on database preparation for oxides and alloys were of immense help. The literature on specific systems optimized in the present work is not reviewed in this chapter as they are presented in the following chapters.

1.1. CALPHAD

Calphad is an acronym for the CALculation of PHAse Diagrams [Spencer (2008)]. It is better described as "The Computer Coupling of Phase Diagrams and Thermochemistry".

Kattner (Kattner, 1997) described phase diagrams as "visual representations of the equilibrium state of a material as a function of temperature, pressure and concentrations of the constituent components." They are, therefore, frequently hailed as basic blueprints or roadmaps for alloy design, development, processing and basic understanding. Pelton and Schmalzried (Pelton and Schmalzried, 1973) defined a phase diagram as "the geometrical representation of the loci of the thermodynamic parameters when equilibrium among phases under a specified set of conditions is established". Phase diagrams provide vital inputs required for addressing many technological problems involving multi-component, multi-phase equilibria.

The correlation between thermodynamics and phase equilibria was established more than a century ago by J.W. Gibbs. Later, J. J. van Laar (Van Laar, 1908) published his mathematical synthesis of hypothetical binary systems. With the advance of computing technology, construction of multicomponent thermodynamic databases began in the late 1960's. Kattner (Kattner, 1997) has summarized some early examples, between 1908 and 1970, of mathematical calculations of phase diagrams. In 1970 Kaufman and Bernstein (Kaufman and Bernstein, 1970) summarized the general features of the calculation of phase diagrams and also presented listings of computer programs. In 1973 Larry Kaufman organized the first project meeting of the international CALPHAD group.

Under the CALPHAD technique, all types of thermodynamic information such as phase diagrams, enthalpy of mixing in a phase, activities *etc.* are critically evaluated and optimized simultaneously, using proper thermodynamic models, in order to construct multicomponent databases. The thermodynamic models required to represent the thermochemistry of phases have also been developed. A model capable of closely reflecting the thermochemical properties of a phase with a minimum number of adjustable parameters should be chosen. Also, these models should be based on a good physical microscopic picture of a solution to obtain better predictions in multicomponent systems using these models from lower-order optimized parameters.

Normally a software package capable of performing multivariable optimizations is used in the optimization process. All the input data are back-calculated from the single set of model parameters obtained from the optimization. The databases containing model parameters for
lower-order (binary and ternary) systems are used to predict the thermodynamic properties in multicomponent systems. There are various techniques (Section 1.2.3) to extrapolate the Gibbs energy from binary systems into higher-order systems. In case these predictions are not able to reproduce the available data in the higher-order system within the experimental error limits, then higher-order interaction parameters is included to reproduce the available data.

Recently, new approaches to thermodynamic modeling have been conducted with the advent of computing technologies. First-principles calculations can be cited in this area. A first-principles calculation starts from quantum mechanics to examine the fundamental properties of materials such as which structure is stable at a certain temperature and pressure. First-principles calculations are extensively used in conjunction with the "Cluster Variation Method" (CVM) which was introduced in the 1950's by Kikuchi (Kikuchi, 1951) who introduced this method to treat order-disorder phenomena in solid phases. Although these calculations are computationally very intensive, enormous progress in recent years in the area of computing techniques have made them easier.

Nevertheless, these techniques are still in their nascent stages and cannot be satisfactorily applied to complex systems. The phase diagrams predicted by these techniques are generally approximately correct but currently still lack sufficient accuracy for practical applications. In conclusion, the development of thermodynamic databases for applications in complex industrial processes can be done by the CALPHAD technique, although first-principles calculations can often provide reasonable estimations of certain properties, particularly enthalpies of stoichiometric solids, when experimental data are lacking.

1.2 Thermodynamic modeling

Thermodynamic models are required to adequately represent the thermodynamic properties of materials. Complex solutions require sophisticated and refined models for the proper representation of their thermochemical properties. A good model should be able to represent the thermodynamic properties with just a small numbers of adjustable parameters. For this, the model should be based on the structure of the solution to adequately represent the configurational entropy of the solution. Also these models have high predictive capability in higher-order systems. Hence, models should be developed which can describe the configurational entropy of the solution of large arbitrary model parameters.

The standard Gibbs energy of a pure component i is written as:

$$G_{i}^{0} = H_{i}^{0} - TS_{i}^{0}$$
(1.2.1)

where G_{i}^{0} , H_{i}^{0} , and S_{i}^{0} are respectively the standard Gibbs energy, enthalpy (relative to standard elemental reference (SER) state) and entropy of *i*, and *T* is the absolute temperature.

When two components A and B are mixed then the energy of the solution depends upon the interaction between the A and B atoms or molecules. The Gibbs energy of a solution in which

there is no change in its energy because of mixing i.e. the value of the A-B bond energy is the average of that of the A-A and B-B bonds is an ideal solution for which:

$$G^{m} = g^{0}_{A} n_{A} + g^{0}_{B} n_{B} - T\Delta S^{conf}$$

$$(1.2.2)$$

where G^m is the Gibbs energy of the solution, g^0_i is the molar Gibbs energy of component *i*, and ΔS^{conf} is configurational entropy obtained by randomly mixing n_A moles of A and n_B mole of B on the same sublattice:

$$\Delta S^{conf} = -R \left(n_A \ln X_A + n_B \ln X_B \right) \tag{1.2.3}$$

Practically however, all solutions do have interactions among the atoms mixing to form a solution. Such interactions can be called g^E , the molar excess Gibbs energy of the solution. In this case the energy of the solution is given by:

$$G^{m} = g^{0}_{\ A}n_{A} + g^{0}_{\ B}n_{B} - T\Delta S^{conf} + (n_{A} + n_{B}) g^{E}$$
(1.2.4)

 g^E is often expanded as a polynomial in the mole fractions as:

$$\mathbf{g}^E = \Sigma \, q^{ij}{}_{AB} \, X^i{}_A \, X^j{}_B \tag{1.2.5}$$

where the excess interaction parameters q_{AB}^{ij} (= a +bT +cT² +) may be temperature dependent.

In many cases, the thermodynamic properties of a binary solution can be described by using the expression in Eq. 1.2.5. Although it is satisfactory in binary systems which are not showing large deviations from ideality, problems arise when such an expression is used to predict the

thermodynamic properties of the higher-order systems from the model parameters of the lowerorder sub-systems. In this case, large arbitrary parameters are often needed in these higher-order systems to reproduce the available data. Even sometimes in a binary system also a large number of interaction parameters are needed in this simple polynomial based model in order to adequately represent all the thermodynamic properties of the system.

To adequately represent the thermodynamic properties of the liquid phase, Pelton and co-workers (Pelton, Degterov, Eriksson, Robelin and Dessureault, 2000) and Pelton and Chartrand (Pelton and Chartrand 2001) developed the Modified Quasichemical Model (MQM). They modified the classical quasichemical model by improving the configurational entropy term of the model. Other modifications were also made to make it more flexible and practical for real and complicated systems.

The MQM developed by Pelton *et al.* (Pelton, Degterov, Eriksson, Robelin and Dessureault, 2000) has been applied not only to simple metallic alloys but to liquid slags, sulphides, and salts. In fact, the utility of the MQM over a simple polynomial or random- mixing model can be better realized with those solutions which show more ordering than metallic solutions, and where the configurational entropy terms become more important. Simple models cannot take this ordering into account.

1.2.1 Modified Quasichemical Model (MQM)

In the present work the MQM was used to model the liquid phase in the binary and ternary systems. The model has been described in detail by Pelton and co-workers [Pelton, Decterov, Eriksson, Robelin, and Dessureault (2000); Pelton and Chartrand (2001); Chartrand and Pelton (2001); Pelton, Chartrand, and Eriksson (2001)]. A brief summary of this model is presented here.

In the MQM in the pair approximation, the following pair exchange reaction between atoms *A* and *B* on neighboring lattice sites is considered

$$(A-A)+(B-B)=2(A-B);$$
 Δg_{AB} (1.2.6)

where (i - j) represents a first-nearest-neighbor pair. The non-configurational Gibbs energy change for the formation of two moles of (A - B) pairs is Δg_{AB} .

In a binary silicate melt such as MO-SiO₂, one might identify the "A" and "B" particles with M and Si which mix on a cationic quasi-lattice. The tendency to ordering through the preferential formation of A-B pairs could then be identified with the formation of orthosilicate ions and the resultant creation of second-nearest neighbour A-B pairs. At the orthosilicate composition, M_2SiO_4 , a completely ordered solution could be considered to consist of only M^{2+} cations and SiO_4^{4-} anions. This is equivalent to saying that there are only M-Si and no Si-Si or M-M second-nearest neighbour pairs. A B-B pair would be identified as a Si-Si second-nearest neighbour pair joined by an "oxygen bridge", and a A-A pair is an $M^{2+}-M^{2+}$ second-nearest neighbour pair separated by an O^{2-} ion.

However, it must be stressed that the modified quasichemical theory as presented by Pelton and co-workers is not intended as a complete theory of silicate or slag (or any other liquid oxide phase) structure but as a mathematical formalism capable of reflecting structural changes in a solution. The model must has advantages of simplicity and generality and the characteristics required for relatively reliable interpolations and extrapolations.

Let n_A and n_B be the number of moles of A and B, n_{ij} be the number of moles of (i - j) pairs, and Z_A and Z_B be the coordination numbers of A and B. The pair fractions, mole fractions, and "coordination-equivalent" fractions are defined respectively as:

$$X_{ij} = n_{ij} / (n_{AA} + n_{BB} + n_{AB})$$
(1.2.7)

$$X_A = n_A / (n_A + n_B) = 1 - X_B \tag{1.2.8}$$

$$Y_{A} = Z_{A}n_{A}/(Z_{A}n_{A} + Z_{B}n_{B}) = Z_{A}X_{A}/(Z_{A}X_{A} + Z_{B}X_{B}) = 1 - Y_{B}$$
(1.2.9)

The following equations may be written:

$$Z_A X_A = 2n_{AA} + n_{AB} \tag{1.2.10}$$

$$Z_B X_B = 2n_{\rm BB} + n_{AB} \tag{1.2.11}$$

The Gibbs energy of the solution is given by:

$$G^{m} = \left(n_{A}g_{A}^{\circ} + n_{B}g_{B}^{\circ}\right) - T\Delta S^{\text{config}} + \left(n_{AB}/2\right)\Delta g_{AB}$$
(1.2.12)

$$= \left(n_A g_A^{\circ} + n_B g_B^{\circ} \right) - T \Delta S^{\text{config}} + g^E$$

(1.2.13)

where g_A° and g_B° are the molar Gibbs energies of the pure components and ΔS^{config} is the configurational entropy of mixing given by randomly distributing the (A-A), (B-B) and (A-B) pairs in the one-dimensional Ising approximation:

$$\Delta S^{\text{config}} = -R(n_A \ln X_A + n_B \ln X_B) - R[n_{AA} \ln(X_{AA}/Y_A^2) + n_{BB} \ln(X_{BB}/Y_B^2) + n_{AB} \ln(X_{AB}/2Y_A Y_B)]$$
(1.2.14)

 Δg_{AB} is expanded in terms of the pair fractions:

$$\Delta g_{AB} = \Delta g_{AB}^{\circ} + \sum_{i \ge 1} g_{AB}^{i0} X_{AA}^{i} + \sum_{j \ge 1} g_{AB}^{0j} X_{BB}^{j}$$
(1.2.15)

where Δg_{AB}° , g_{AB}^{i0} and g_{AB}^{0j} are the parameters of the model which may be functions of temperature.

The equilibrium pair distribution is calculated by setting

$$\left(\partial G/\partial n_{AB}\right)_{n_A,n_B} = 0 \tag{1.2.16}$$

(It should be noted that in the FactSage software pair fractions are calculated by Equilib module using the Gibbs energy minimization algorithm widely known as SOLGASMIX [Eriksson (1975)].

This gives the "equilibrium constant" for the "quasichemical reaction" of (Eq. 1):

$$\frac{X_{AB}^2}{X_{AA}X_{BB}} = 4\exp\left(-\frac{\Delta g_{AB}}{RT}\right)$$
(1.2.17)

As Δg_{AB} becomes progressively more negative, the reaction (Eq. 1) is shifted progressively to the right, and the calculated enthalpy and configurational entropy of mixing assume, respectively, the negative "V" and "m" shapes characteristic of SRO.

The composition of maximum SRO is determined by the ratio of the coordination numbers Z_B/Z_A , as given by the following equations:

$$\frac{1}{Z_A} = \frac{1}{Z_{AA}^A} \left(\frac{2n_{AA}}{2n_{AA} + n_{AB}}\right) + \frac{1}{Z_{AB}^A} \left(\frac{n_{AB}}{2n_{AA} + n_{AB}}\right)$$
(1.2.18)

$$\frac{1}{Z_B} = \frac{1}{Z_{BB}^B} \left(\frac{2n_{BB}}{2n_{BB} + n_{AB}}\right) + \frac{1}{Z_{BA}^B} \left(\frac{n_{AB}}{2n_{BB} + n_{AB}}\right)$$
(1.2.19)

where Z_{AA}^{A} and Z_{AB}^{A} are the values of Z_{A} respectively when all the nearest neighbors of an A are A's, and when all nearest neighbors of an A are B's, and where Z_{BB}^{B} and Z_{BA}^{B} are defined similarly.

In the systems where composition of SRO is known experimentally the ratio Z_B/Z_A is fixed by that value. For example, in the binary CaO-SiO₂ system, ordering is observed about X_{SiO2} (mole fraction) = 1/3. This ordering is generally attributed to the formation of othrosilicate ions. This fixes the Z_{Ca}/Z_{Si} to 1/2. Although the model is sensitive to the ratio of the coordination numbers, it is less sensitive to their absolute values. It must be noted that the use of the one-dimensional

Ising model in Eq. 1.2.14 introduces a mathematical approximation into the model. The $\Delta S^{\text{config}} = 0$, only when $\Delta g_{AB} = -\infty$ and $Z_A = Z_B = 2$. Therefore, for highly ordered solutions like liquid silicates (where $\Delta g_{AB} << 0$), better results are expected if coordination numbers equal to 2 are used. However, $Z_A = Z_B = 2$ will reproduce SRO at 50 mole% composition. To reproduce SRO at the desired composition, absolute values of Z_A and Z_B are chosen with the additional condition, along with the one that they should be closest to 2, that ΔS^{config} approaches zero when Δg_{AB} approaches $-\infty$. Pelton and Blander (1984) presented a detailed description on the choice of these coordination numbers. In the CaO-SiO₂ system, with this additional condition, the absolute value of Z_{Ca} is 1.37744375 and of Z_{Si} is 2.75488750. These values will reproduce SRO close to X_{SiO2} (mole fraction) = 1/3.

Recently, Saulov (Saulov, 2007) pointed out some issues which may provide a useful note of caution in the use of the MQM. Pelton and Chartrand (Pelton and Chartrand, 2007) replied on these issues that they rarely cause any problem in real systems. Saulov's issue on the stability calculations of the Gibbs energy of a solution phase by the MQM is due to the use of improbable and physically unlikely values of the quasichemical parameter Δg_{AB} . Saulov's suggestions on the use of coordination number as a function of mole fraction and the use of splines for the Gibbs energy of the quasichemical reaction are not of any particular advantages and their usage result in mathematically cumbersome expansions. Use of splines may be useful for binary systems, but then a simple general equation for multicomponent systems could not be written.

1.2.2 Charge compensation effect

Chartrand and Pelton (1999) reported that the assumptions of the MQM were inadequate in the case of Na₂O-Al₂O₃-SiO₂ solutions. They listed two features based on which model needed to be improved. The first feature was the liquidus of mullite in Fig. 1.2.1. This liquidus descends very steeply from the SiO₂-Al₂O₃ binary system to the SiO₂-NaAlO₂ join. This shows that liquid SiO₂-Al₂O₃ solutions are very strongly stabilized by the addition of Na₂O up to a molar Na:Al ratio of 1:1. The second feature was the liquidus along the SiO₂-NaAlO₂ join (Fig. 1.2.2, between the SiO₂ and NaAlSi₃O₈ phases). In the limit as X_{SiO2} approaches 1, the limiting slope of the SiO₂-liquidus is given by Raoult's law as:

$$\lim_{X_{SiO_2} \to 1} \frac{dX_{SiO_2}}{dT} = \frac{\Delta h_{f(SiO_2)}^0}{vRT_{fus(SiO_2)}^2}$$

where $\Delta h_{f(SiO_2)}^0$ and $T_{fus(SiO_2)}$ are the enthalpy and temperature of fusion of SiO₂ and *v* is the number of moles of independent atoms or ions introduced per mole of NaAlO₂ (or of NaAlSi₃O₈). The experimental points in Fig. 1.2.2 show that the limiting liquidus slope corresponds closely to *v* = 1. That is, Na⁺¹ and Al⁺³ enter into solution as (NaAl)⁺⁴ associates. The simple quasichemical model, however, predicts *v* = 2 in the limit as X_{SiO2} approaches 1.

Chartrand and Pelton (1999) reported that the above observations arise from a "charge compensation effect". They explained it as the replacement of Si^{+4} in the silica network by $(NaAl)^{+4}$ associates. The dissolution of alumina in silica by the replacement of Si^{+4} in the tetrahedral network by Al^{+3} is energetically unfavourable because it results in a negative charge centre. However, upon addition of Na₂O this negative charge can be compensated by a Na⁺ ion

placed next to the aluminum as illustrated in Fig. 1.2.3. Hence, the addition of Na₂O, up to a Na:Al ratio of 1:1, decreases the Gibbs energy of the solution markedly. To model this effect, Chartrand and Pelton (1999) considered the $(NaAl)^{+4}$ associates to be a separate species. The ternary solution is then formally treated as a quaternary solution with components NaO_{1/2}, AlO_{3/2}, SiO₂ and $(NaAl)O_2$ where the mole fraction X_{NaAlO2} gives the concentration of the $(NaAl)^{+4}$ associates, while $X_{NaO1/2}$ and $X_{AlO3/2}$ are the concentrations of "free" Na and Al. The formation of the $(NaAl)^{+4}$ associates is formally treated through the Gibbs energy change of the following reaction among the components:

 $NaO_{1/2} + AlO_{3/2} = (NaAl)O_2;$

$$g^{0}_{(\text{NaAIO2})} = g^{0}_{(\text{NaO1/2})} + g^{0}_{(\text{AI2O3})} + \Delta g^{0}_{(\text{NaAIO2})}$$

where, $g^{0}_{(NaAlO2)}$ is the standard Gibbs energy of the hypothetical pure component (NaAl)O₂. During optimization, the $\Delta g^{0}_{(NaAlO2)}$ was fixed by assuming a reasonable value which make the (NaAl)⁺⁴ associates practically unstable in the binary Na₂O-Al₂O₃ system.

The Gibbs energies of formation of the following second-nearest-neighbors pairs were also introduced so that $(NaAl)^{+4}$ associates can be stabilized in the SiO₂-rich region of the liquid solution (where the silica network is present).

$$(Si + Si) + (NaAl-NaAl) = 2(NaAl-Si); \quad \Delta g^{0}_{(NaAl)Si}$$
$$(Al-Al) + (NaAl-NaAl) = 2(NaAl-Al); \quad \Delta g^{0}_{(NaAl)Al}$$
$$(Na-Na) + (NaAl-NaAl) = 2(NaAl-Na); \quad \Delta g^{0}_{(NaAl)Na}$$

These Gibbs energies of formation were model parameters obtained by simultaneous optimization of all the available data.



Fig. 1.2.1 Experimentally determined liquidus surface of the Na₂O-Al₂O₃-SiO₂ system in the SiO₂-rich region (reproduced from (Chartrand and Pelton, 1999)).



Fig. 1.2.2 Calculated liquidus surface along the $NaAlSi_3O_8$ -SiO₂ join compared with experimental data (reproduced from (Chartrand and Pelton, 1999)).



Fig. 1.2.3 A simplified two-dimensional representation of the charge compensation effect in the SiO₂-rich melts (reproduced from (Chartrand and Pelton, 1999)).

1.2.3 Thermodynamic modeling of solids

Solid phases appear in phase diagrams as stoichiometric compounds, terminal solid solutions or stoichiometric compounds with ranges of homogeneity. Sometimes some compounds have such a large homogeneity range that they are called solutions with specific names.

The Gibbs energy function for any stoichiometric phase $A_x B_y$ per mole of atoms is represented as:

$$g^{A_{x}B_{y}}(T) = \frac{x}{x+y} g^{0}_{A} + \frac{y}{x+y} g^{0}_{B} + \Delta H_{T} - T\Delta S_{T}$$
(1.2.20)

where ΔH_T and ΔS_T are the enthalpy and entropy of formation of the compound from the states *i* and *j* of elements A and B respectively.

The terminal solid solutions appearing in a binary system are usually treated with a randommixing single-sublattice model. As the name suggests, this model assumes the random mixing of the atoms, one randomly replacing the other by substitution on lattice sites. The Gibbs energy of such a solution in which atoms A and B replace each other on lattice sites is given as:

$$G^{m} = (x \ g_{A}^{0} + x_{B} \ g_{B}^{0}) + RT[x_{A} \ln x_{A} + x_{B} \ln x_{B}] + g^{E}$$
(1.2.21)

Where, $G^{E} = \sum q_{AB}^{ij} (X_{A})^{i} (X_{B})^{j}$ and q_{AB}^{ij} are the model parameters.

The phases with two or more sublattices exhibiting ranges of homogeneity are modeled using sublattice models. The sublattice model with random-mixing on each sublattice in its most general form is called as Compound Energy Formalism (CEF). This formalism was advanced by Hillert who has given a detailed description (Hillert, 2000). In the CEF, the Gibbs energy per mole of solution in the compound (A, B)_P (D,E)_Q is given by;

$$G = y_{A} y_{D} G_{A:D} + y_{A} y_{E} G_{A:E} + y_{B} y_{D} G_{B:D} + y_{B}^{a} y_{E}^{b} G_{B:E} + PRT (y_{A} \ln y_{A} + y_{B} \ln y_{B}) + QRT (y_{D} \ln y_{D} + y_{E} \ln y_{E}) + (\sum_{k=D,E} y_{A} y_{B} y_{k} L_{AB:k} + \sum_{k=A,B} y_{k} y_{D} y_{E} L_{k:DE})$$
(1.2.22)

where, P and Q are the number of sites in each sublattice.

In the CEF the atoms are assumed to mix randomly on each sublattice. The interactions between the atoms on different sublattices are taken into account by the Gibbs energy of end members $G_{i:j}$, and interactions among the atoms on the same sublattice is taken into account by excess terms (the last term in the above equation). The Gibbs energy of end members $G_{i:j}$ and excess parameters $L_{ij:k}$ are the model parameters.

1.2.4 Extension to a ternary system from binary systems

To estimate the excess Gibbs energy of a ternary solution from optimized binary model parameters, several "geometric" models have been proposed. Pelton (Pelton, 2001) presented a detailed description of these models. Some of these models are illustrated in Fig. 1.2.1 (reproduced from (Pelton, 2001)). In all of these models the excess Gibbs energy (g^E in Eq.1. 2.13) at any composition p can be estimated from the binary interaction parameters or the excess Gibbs energy when the solution is modeled using the MQM is estimated as:

$$g^{E} = X_{12} \varDelta g_{12} / 2 + X_{13} \varDelta g_{13} / 2 + X_{23} \varDelta g_{23} / 2 + (ternary \ terms)$$
(1.2.23)

where Δg_{ij} is the Gibbs energy change for the reaction:

$$i - i + j - j = 2(i - j)$$
 (1.2.24)

If ternary data are available, they can be used to estimate the ternary interactions. However, these terms should not be large, otherwise doubt is cast upon the predictive ability of the model. These ternary terms are identically zero in the three binary sub- systems.

The Kohler and Muggianu models in Fig. 1.2.1 are "symmetric" models, whereas the Kohler/Toop and Muggianu/Toop models in Fig. 1.2.1 are "asymmetric" models inasmuch as one component is singled out. An asymmetric model is more physically reasonable than a symmetric model if component 2 and 3 are chemically similar while component 1 is chemically different. When g^E is large and Δg_{ij} depends strongly upon composition, a symmetric model and an

asymmetric model will give very different results. Pelton (Pelton, 2001) showed that improper use of these models can lead to thermodynamically inconsistent and unjustifiable results.

Pelton and Chartrand (Pelton and Chartrand, 2001) presented a detailed description of the estimation of the excess Gibbs energies in a ternary solution from binary model parameters when the MQM is used to model the liquid phase. If the data for the three binary subsystems of a ternary system have been optimized and the parameters are in the form of Eq. 1.2.15, when a symmetric Kohler-type approximation is chosen for the 1-2 subsystem, then Δg_{12} can be written:

$$\Delta g_{12} = \Delta g_{12}^{0} + \sum_{1 \le (i+j)} g_{12}^{ij} \left(\frac{X_{11}}{X_{11} + X_{12} + X_{22}} \right)^{i} \left(\frac{X_{22}}{X_{11} + X_{12} + X_{22}} \right)^{j}$$
(1.2.25)

If a Toop-type approximation is chosen, then Δg_{12} can be written:

$$\Delta g_{12} = \Delta g_{12}^0 + \sum_{1 \le (i+j)} g_{12}^{ij} X_{11}^i \left(X_{22} + X_{23} + X_{33} \right)^j$$
(1.2.26)

The form of these expressions was chosen because in the limit of a very small degree of shortrange ordering they reduce to the well-known Kohler and Kohler-Toop approximations with the Bragg-Williams random-mixing model. The FactSageTM thermodynamic software (FactSage, 2008) allows users to use any of these "geometric models" to increase the flexibility and the ability to estimate the Gibbs energy of ternary or multicomponent solutions from the optimized lower-order parameters.



Fig. 1.2.4 Some geometric models for estimating ternary thermodynamic properties from the optimized binary data (reproduced from Pelton, 2001).

1.2.5 Predictions using only binary parameters

The choice of a model must be based not only on how well it reproduces data in binary systems, but also on how well it predicts and represents properties of ternary solutions. Pelton and Kang (Pelton and Kang, 2007) showed how the MQM generally predicts better the property of ternary solutions from the optimized model parameters than does the random-mixing model.

In a ternary system A-B-C in which the binary solution A-B exhibits a strong tendency to shortrange ordering, while the B-C and C-A binary solutions are closer to ideality, positive deviations from ideal mixing behavior will be observed, centered along the A_xB_y -C join where A_xB_y is the binary composition of maximum short-range ordering. If the ordering in the A-B system is sufficiently large, then a miscibility gap is observed along the A_xB_y -C join. Such positive deviations are expected because the addition of C atoms breaks the energetically favored A-B pairs, and consequently the solution tends to maximize the number of A-B pairs by separating into A_xB_y -rich and C-rich solutions.

A Bragg-Williams model overestimates the positive deviations observed in such ternary systems. In fact, it may predict a miscibility gap when there is none experimentally observed. An associate model [(Luck, Gerling and Predel (1989); (Pelton and Kang, 2007)] in which the short-range ordering in the A-B binary solution is modeled as being due to A_xB_y molecules or associates, will not at all predict such deviations. The associate model simply predicts that, along the A_xB_y -C join, the solution is an ideal mixture of $A_x B_y$ associates and C atoms. The MQM, with proper choice of coordination numbers, predicts better such positive deviations along the $A_x B_y$ -C join.

Pelton and Kang (Pelton and Kang, 2007) also showed that usually the MQM better predicts extensions of binary miscibility gaps into a ternary system. A miscibility gap in a binary liquid phase modeled using the MQM is much flatter with a comparatively lower consolute temperature than is obtained by a random-mixing model. As a result, the MQM predicts a smaller extension of a binary miscibility gap into a ternary system.

1.3 Experimental techniques for phase diagram determination

The different methods used in phase diagram determination involve procedures for examining the phase reactions and identifying the phases present. The experimental techniques used in phase equilibria studies can be divided into two main groups: dynamic and static methods. The dynamic method is based on the measurement of property change that occurs as the system is undergoing a phase transformation. Changes in several properties of a sample can be observed at the critical point of phase transformation. The most widely used dynamic techniques are thermal analysis (TA), differential thermal analysis (DTA), differential scanning calorimetry (DSC) and thermogravimetric analysis (TGA). These techniques are more accurate in those systems where equilibrium is readily obtained. The static methods are based on the *in situ* measurement of a property of a sample at the equilibrium state. In these techniques, all potentials of the systems are fixed until equilibrium is achieved, after which the sample is examined by chemical analysis, X-

ray diffraction (XRD) or metallography. These methods are more appropriate where reactions are slow.

Most phase diagrams are constructed by using of phase equilibria and property change data obtained by a variety of experimental methods. Invariably, there are differences between the data obtained from various investigations. There are no fixed rules that can be used to decide which data are to be preferred. However, there are several factors that are generally important in the experimental determination of phase equilibrium relations, such as:

- 1) Starting materials should be of high purity. Impurities can greatly influence phase equilibria.
- The area of contact among the constituents in starting materials should be maximized. Thorough mixing of fine-particle starting materials aids in the rapid attainment of equilibrium.
- 3) Sufficient time must be allowed at a given temperature to attain equilibrium.
- The presence of a liquid phase promotes attainment of equilibrium. For this purpose, a lower liquid viscosity is more effective than a higher.

Thus, apart from these general factors, there are many specific conditions relevant in the evaluation of the reliability of a particular experimental technique used for phase diagram determination. In the following pages, the main experimental techniques used in oxide phase diagram determination, their advantages and disadvantages, and the evaluation criteria are discussed.

1.3.1 Annealing and quenching techniques

These techniques are widely applied wherever reactions and phase transformations are quite slow and long times are required to reach equilibrium. This technique is applied to especially silicate and other ceramic melts as they are highly viscous and crystallize very slowly. In this technique, the compositions to be studied are equilibrated at a particular temperature, after which samples are quenched. Microscopic examination, XRD or chemical analyses of these samples then identify the phases present and their composition.

The first step in this technique is the preparation of the sample and its homogenization. Extreme care should be taken in the selection of starting materials if accurate composition is to be obtained. For example, the use of alkali oxides and La_2O_3 should be avoided because they form carbonates or hydrolyze in contact with the atmosphere. Similarly, it should be ascertained whether cations present in the starting materials can exist in different oxidation states. For example, wustite (ferrous oxide) does not have the composition FeO, CrO_2 loses oxygen on standing, and the composition of praseodymium, cerium, and terbium oxides depend upon their previous heat treatment and vary between $REO_{1.5}$ and REO_2 (RE=Rare Earth). If the pure component has a high vapor pressure, like PbO, then a significant amount of mass can be lost during equilibration.

After the starting materials are selected, attainment of equilibrium is favoured by treatment in several pre-processing steps such as precalcination, mixing, grinding, master slag formation etc.

Important here is the homogenization of the starting materials, in order to ensure uniform microstructures. They are homogenized by firing at high temperatures and then grinding. To obtain good homogenization, firings and grindings are repeated several times. Here it should be noted that firing is performed below the subsolidus temperature. If a liquid phase forms, then crystals will separate from the liquid and result in inhomogeneity. This may persist even after grinding to a powder. Sometimes high melting oxides like silica make attainment of equilibrium difficult to achieve. In such cases high melting oxide mixtures are pre-treated by melting them at lower temperatures and then rapidly cooled. These intermediate glassy master slags can then be used to prepare final mixtures for high-temperature equilibration.

After homogenization, samples are equilibrated for phase equilibria studies. The selection of crucibles used in this step is quite important. At these high temperatures sample reaction with the crucible material should be avoided; otherwise, the data obtained may be erroneous. Usually, platinum and iridium crucibles are used up to 2000 °C. However, if samples contain transition-metal ions, these ions can diffuse into the crucible material. Therefore, for samples containing transition-metal ions or for higher temperatures, crucibles made of refractory oxides like Al₂O₃ or ZrO₂, or refractory metals like tungsten, molybdenum, or tantalum are used. The refractory ceramic materials are not used when corrosive slags are under study. Platinum is suitable for oxidizing conditions; molybdenum and iron can be used in reducing or neutral gas atmospheres. However, despite these precautions, a final check should be performed for interaction between the sample and crucible. The material and thickness of the crucible also greatly affects the cooling rate, as it is the crucible material that first contacts the quenching medium.

Along with the material used in the crucible, its design is important in the annealing and quenching techniques because it is the crucible which comes in first contact with the quenching medium. Some of these designs are shown in Fig. 1.3.1. In crucibles the sample mass used is typically in the range of 1-50 g enabling convenient wet chemical analysis to be undertaken. In contrast, the slag mass used with envelopes and open support systems (Fig. 1.3.1) is of the order of 0.1 g or less. Open support systems use surface tension to hold the slag on the outside of the metal or compound substrate. On quenching, the slag comes into direct contact with the quenching medium resulting in rapid cooling. Normally the support is made of inert material or a primary phase material. This enables isothermal single-phase and multi-phase saturation experiments to be undertaken in those systems in which a suitable crucible material is not available. Thus, open support systems are advisable both where very high quenching rates are required and where some of the components are highly reactive and a suitable crucible material cannot be found. When reaction with crucibles is unavoidable, an electromagnetic levitation of metal drops can be used. In this case, slag is attached to the metal through surface tension forces. The principal difficulty in this technique is to obtain the levitation power, temperature ranges and stable temperature control. The temperature of the slag phase in this arrangement is determined indirectly through the metal droplet.



a crucible, metal, ceramic; b envelope, metal, ceramic; c open support, metal, primary phase; d levitated metal drop, metal

Fig. 1.3.1 Design of crucibles to support samples for slag phase equilibria determination [Jak and Hayes, 2004].

The very important step in quenching and annealing techniques is to decide the heating regime for the sample for equilibration. The time and thermal treatment required to achieve equilibrium depends upon the particular reaction system and conditions. For example, a peritectic reaction is quite slow because of diffusion from the primary phase for precipitation of the secondary phase. To avoid this slow diffusion, premelting can be done at high temperature where there is only liquid and then quenched to glass. This glass can then be equilibrated at the temperature of interest and the equilibrium phase can be obtained from metastable liquid. Otherwise, for melts having high viscosities and very low rates of crystallization a premelting temperature below the liquidus can be chosen. This will precipitate some primary phase which acts as seeds for further crystallization and reduces the time to achieve equilibrium.

If sufficient experiments have been performed on the system then the final results can be judged on the basis of consistency. There are also many other specific criteria. Results can be monitored as a function of time allotted to reach equilibrium. A metastable equilibrium which persists long enough can lead to erroneous conclusions. In this case, the sample should be equilibrated a second time. If the result does not change with second and subsequent equilibrations, it can be assumed that equilibrium has been achieved. The sample microstructure where equilibrium has been achieved shows uniformity in the distribution of phases and an absence of corroded crystals. In attaining equilibrium, it is good practice to approach equilibrium from both sides of the chosen composition. For example, a liquid of a given composition could be quenched from above the liquidus temperature and, also a sample of the same composition could be fired at sub-solidus temperatures. These two samples then could be equilibrated at the temperature of interest; if they show same results then it can be concluded with greater confidence that equilibrium has been achieved. Of course, this technique requires at least an approximate knowledge of liquidus and solidus temperatures.

After equilibration, the sample is then quenched for further examination. Quenching should be as rapid as possible to "freeze-in" the phases present at the equilibration temperature and to avoid diffusion. In the case of slags, water or brine is used as quenching medium. Liquid nitrogen can also be used in this case; however this results in the formation of a protective nitrogen gas atmosphere which affects the heat transfer and cooling rate. Nevertheless, liquid nitrogen is used as quenching medium where it is necessary to protect the outer layer of the sample from oxidation. There are other techniques for rapid solidification such as spinning wheels and piston and anvil devices. Moving surface devices such as the spinning wheel are suitable for low viscosity melts like metals and not for high viscosity ceramic melts.

After quenching, samples are characterized with techniques like XRD, optical microscopy or chemical analysis like EPMA. Sometimes even simple visual inspection provides useful information about phases in the quenched samples. If grains of different phases are sufficiently large and the phases are of different colors then the sample appears spotted. A small amount of colored phase which cannot be detected by XRD can be visually inspected. At temperatures below the liquidus and above the solidus, the sample may exhibit a slight rounding of sharp edges or sticking to the sample container. The presence of significant cracking and crumbling signifies the existence of an "unquenchable" phase transition. Optical microscopy is widely used to identify small amounts of a second phase. Samples quenched above the liquidus will not show the presence of crystalline phases but the samples below the liquidus will do so. The presence of rounded, corroded, or poorly distributed crystals indicates that equilibrium might have not been reached. XRD is often the most satisfactory method to identify the phases in the quenched samples.

One of the disadvantages of using this technique is that it is very difficult to find the exact temperature of phase transformation. Normally, this technique allows investigator to bracket the values instead of giving the exact temperature of transformation. It is a common assumption that during quenching all the phases present at equilibrium are "frozen-in", i.e., there is no change in phase assemblage. However, cases have been found, especially in metals, where the hightemperature phases cannot be retained while quenching and undergo decomposition or transformation. In such cases use of this technique alone will lead to erroneous results. This problem can be avoided by using hot stage microscopy or high-temperature XRD where samples are examined at high temperatures without quenching.

1.3.2 Segregation method for liquidus determination

This is a static method in which liquid of a given composition is held at a particular temperature T_x in Fig. 1.3.2, for a sufficient time for equilibrium to be established. Once the equilibrium has been established, the solid and liquid phases separate due to density differences. Here it must be ensured that equilibrium has been achieved by annealing the samples for different times at a given temperature. If the solid sinks, then a liquid sample may be drawn off using a ceramic suction tube; if it floats, then appropriate devices and methods are available to draw the liquid from beneath the surface. If there is only a very small density difference between solid and liquid, centrifuging can separate them. After separation of the phases, they are analyzed for their chemical compositions.



Fig. 1.3.2 The principle of the segregation method for investigating liquidus curves [Raynor, 1976].

This method is especially useful in determining steep liquidus where thermal analysis gives faulty results. An additional advantage of this method is that chemical analysis of the sample is done after the achievement of equilibrium; thus changes in bulk composition at high temperature do not affect the final results. However, feasibility of this method depends upon the accuracy of a clean separation of the liquid sample. The most common source of error here is the removal of small particles of solid along with the liquid, and this error becomes more probable as the density difference between solid and liquid becomes smaller.

1.3.3 Isothermal equilibration/quenching/microanalysis technique

This static technique is similar to quenching/annealing, but equilibration is done deliberately at subliquidus temperature as in the segregation method. Therefore this technique can be said to be a combination of quenching/annealing and segregation. Thus a bulk composition x is first isothermally equilibrated and then quenched. Analysis of the sample is performed by accurate electron probe X-ray microanalysis (EPMA). This method has been recently extensively used by Jak and Hayes [Jak and Hayes, 2004] for many oxide phase equilibria determinations. They have pointed out that many of the earlier techniques for oxide phase determination where isocompositional, which required the difficult task of controlling bulk sample composition at high temperature. Earlier studies were mainly based principally on annealing/quenching techniques which provided results that can only be bracketed to obtain solidus and liquidus. In the later method, unique values of solidus and liquidus data are obtained by EPMA analysis of the quenched sample. This method is especially useful in establishing the solidus where there is extensive solid solubility. Also, this method can be used to determine correctly phase equilibria accompanied by high vapor pressures, provided equilibrium between condensed phases have been reached. This method can be safely extended to double or multi-phase saturation without loss of accuracy. Thus, this approach greatly enhances the ability to provide accurate direct measurement of phase equilibria in complex multi-phase systems, and provides a wealth of important information on coexisting phases.

This technique differs in many respects from the conventional annealing/quenching techniques in phase characterization. After quenching, samples can be studied by XRD, optical microscopy and

other analytical methods. The application of modern EPMA techniques not only substantially increases analytical efficiency and accuracy but also provides important additional information.

EPMA analysis of a sample at a particular temperature provides liquidus and solidus data at that temperature. The same starting mixture can then be used at different temperatures to obtain the solidus and liquidus data at other temperatures. Moreover, the accuracy of EPMA is not dependent upon the minimum traceable amount present in the sample as it is in the case of XRD and DTA. In EPMA, any change in the bulk composition does not affect the final outcome, given that the sample remains in the same phase field. EPMA enables the glass composition to be measured as a function of position within the sample; therefore any inhomogeneity in the glass due to incomplete dissolution of one component or due to precipitation during quenching can be detected. Moreover coring can be detected in phases exhibiting solid solutions due to insufficient equilibration time.

In some cases, it is not possible to use EPMA alone to obtain an unequivocal identification of phases. For example, a compound may be present in more than one polymorphic form. In such cases, it is advisable to use other techniques like XRD or optical micrography to obtain a definite result.

1.3.4 Effect of oxygen partial pressure in oxide phase equilibria

Slag-gas equilibria play a very important role in phase diagram determination of oxides. In systems where each of the metal species exists in a single oxidation state the phase relations do not change with oxygen partial pressure of the system. However, transition metals, such as Fe, Mn, Ti and V can be present in more than one oxidation state. In slag systems containing these elements, the oxygen partial pressure of the system can have a significant effect on the liquidus temperatures and phase equilibria. One such example is presented by Kang and Lee [Kang and Lee, 2005] in the study of the MnO-SiO₂-TiO₂-Ti₂O₃ system. Mn and Ti are both transition metals and they have several valences in oxides; Mn⁺², Mn⁺³, Mn⁺⁴, Ti⁺², Ti⁺³ and Ti⁺⁴ depending on temperature, oxygen partial-pressure and phase in which they reside. Kang and Lee [Kang and Lee, 2005] studied the phase equilibria in the system by carefully controlling the oxygen partial pressure using a flowing CO/CO₂ gas mixture and CO with graphite holder. The results obtained by them at 1500 °C and different oxygen partial pressures are shown in Fig. 1.3.3.



Fig. 1.3.3 Phase equilibrium data in the MnO-SiO₂-TiO₂ system at 1500 °C under different oxygen partial pressure. [Kang and Lee, 2005].

Similarly, [Jak and Hayes, 2004] have shown the effect of oxygen partial pressure by FactSage calculations (Fig. 1.3.4) on the liquidus of the complex lead slag PbO-ZnO-FeO-Fe₂O₃-CaO-SiO₂. In this case the liquidus is displaced as much as 250 K in low lead slags for a change in oxygen partial pressure of six orders of magnitude. Jak and Hayes [Jak and Hayes, 2004] also reported that the difficulties in controlling the slag/gas phase equilibria are principal causes for inaccurate determination of many early experimental works on iron-containing slag systems. These difficulties include thermal segregation of gas mixtures, extensive equilibration times and problems in the control of gas ratios in dilute gas mixtures. For these reasons metal saturation techniques are normally preferred over gas equilibration.



Fig. 1.3.4 The effect of oxygen partial pressure in oxide phase equilibria.

1.3.5 Equilibration/quenching/refractive index

This is a static technique mainly used by Hageman et al. [Hageman et al., 1986] for determination of liquid immiscibility in ceramic melts. This technique involves equilibration of the liquid sample at the temperature where demixing is to be measured and then quenching of the sample followed by refractive index measurement of the two separated glasses. Composition of the glasses is obtained from a standard refractive index curve drawn from the measurements, See Fig. 1.3.5 of the single phase liquid.

Hageman et al. [Hageman et al., 1986] have pointed out that thermal history of a sample often plays an important role in achieving the equilibrium. At temperatures close to the monotectic temperature, demixing is relatively fast and takes only a few minutes to reach equilibrium. In the vicinity of critical temperature, however if a low rate of heating is followed by short period of equilibration, the sample will not reach the equilibrium. For example, in the CaO-SiO₂ melt, in the lower region of demixing an equilibration time of 25-40 minutes is sufficient, whereas in the upper region of demixing an equilibration time of 60 minutes is required.



Fig. 1.3.5 The miscibility gap in the CaO-SiO₂ system [Hageman et al., 1986].

1.3.6 X-ray diffraction techniques (XRD)

XRD techniques are based on the observation of the scattered intensity of an X-ray beam incident to a sample as a function of incident and scattered angle, polarization, and wavelength (energy). These techniques are used mainly qualitatively to identify the phases. The diffraction analysis will help in determining the number of phases present and the crystal structure of phases. In this analysis, to identify a phase, it is necessary that an appreciable quantity is present so that its diffraction pattern can be obtained. XRD coupled with micrography are very powerful techniques to identify phases.

Apart from its qualitative use, XRD can be used quantitatively to determine the phase boundaries, e.g., solid solubility of one component into another or extent of immiscibility in a solid phase. These techniques include measurement of the lattice spacings, by XRD, of a number of alloys equilibrated at a particular temperature and then quenched. Of course, the assumption is made that no decomposition occurs during quenching. As the samples are analyzed after quenching, this technique can be classified as a static technique. In a single phase region lattice spacing varies continuously with the composition. In two-phase regions, the composition of two phases being constant, lattice spacing is also constant with composition. A typical lattice spacing vs. composition curve is shown in Fig. 1.3.6. The *ab* part of the curve is the lattice spacing in a single phase region. This is considered to be constant within the temperature range of the After this, the constant lattice spacings in two phase regions at different experiment. temperatures, parts bc and de, are obtained. The intersection of the two parts of the curve gives the solubility limit. It is evident from Fig. 1.3.6 that points b (at T_H) and point d (at T₁) represent solid solubility limits. The accuracy of this method depends upon the accuracy with which the lattice-spacing vs. composition curve is measured and several precautions are necessary.



Fig. 1.3.6 Lattice spacing vs. composition curve for a binary system [Raynor, 1976].

The preparation of filings for final chemical analysis from the initial annealed and quenched ingots should be performed with utmost care. If filings are susceptible to contamination or oxidation, preparation should be done in an inert atmosphere. The adulteration of filings with carbonaceous material should be avoided by all means, otherwise, on subsequent annealing carbonaceous material is converted into carbon which interferes with chemical analysis. After preparation, filings must be annealed at the maximum possible temperature to relieve the stress introduced by the filing operation. From this stress-relieving temperature the filings are quenched and this, in certain cases, may cause quenching stress in the filings which may give slightly erroneous lattice spacings. The chemical analysis of the filings should be done at this stage because this analysis corresponds to filings which are actually exposed to X-rays.
The main advantage of this technique over micrographic and annealing/quenching techniques is that a single unique value is obtained for the solubility at a given temperature, whereas the other techniques give bracketed values.

During quantitative and qualitative application of XRD, the equilibrated samples are quenched and then exposed to X-rays. However, it is possible that the high-temperature phases cannot be retained during quenching. In such cases, samples maintained at high temperature are exposed to X-ray radiations and suitably protected from oxidation or contamination. This technique is usually called high-temperature XRD. The main difficulty when a diffractometer is used for hightemperature XRD is that of maintaining a uniform sample temperature (the sample is spread over a rather large area). This is avoided effectively by use of a spherical furnace which reduces thermal gradients and minimizes line broadening.

1.3.7 Thermal analysis

Thermal analysis is a non-isothermal dynamic technique whereby a sample is heated or cooled in a furnace, usually not exceeding 1 °C per minute, through a transformation. Some property of the sample changes as a consequence of the transformation. Fig. 1.3.7 depicts the basic principle behind a thermoanalytical instrument. The temperature of the sample is measured by a calibrated recording thermocouple. This recorded temperature, when correlated with a change in property, leads to the determination of phase boundaries. For example, when a liquid sample is cooled, say, to the liquidus temperature, latent heat is evolved as crystallization starts. This produces a thermal arrest which continues giving a constant temperature or a different slope to timetemperature plot until crystallization is complete. This time-temperature plots are shown in Fig. 1.3.8 where cooling curves at five compositions on a hypothetical binary system are shown. It can be seen that a slope change in temperature-time graph is an indication of a phase transformation. The first slope change in graphs 2 and 4 shows starting of solidification as the temperature of sample changes due to evolution of heat. The same constant temperature in graphs 2, 3 and 4 shows solidification has ceased and eutectic precipitation has started.



Fig. 1.3.7 Basic principle behind a thermoanalytical instrument [Hemminger and Sarge, 1999].



Fig. 1.3.8 Application of the cooling curve techniques for studying binary phase equilibria [Bergeron and Risbud, 1984].

A typical apparatus for such type of experiment consists of a dc amplifier to amplify the thermocouple signal and drive an XY recorder. Thermocouples are chosen to give the highest developed EMF consistent with their stability. Normally, large samples like 10 cm³ in volume are used in this experiment. If it is necessary to protect the sample from oxidation by air then an inert or reducing atmosphere or sealed container is used.

It must be noted that the above temperature-time graphs are for hypothetical case to illustrate the concept. Here onset of a phase transformation is very clearly defined. The cooling curve obtained for a real experiment is compared with its ideal counterpart in Fig. 1.3.9. In a real experiment a degree of supercooling is invariably observed. The temperature of the sample, being cooled below the phase transformation during supercooling, rises again. However, at the liquidus, the

temperature never rises all the way back up to the liquidus. Therefore some kind of extrapolation technique must be used to estimate the liquidus temperature. At the eutectic it is possible to regain the eutectic temperature, given that a large quantity of sample is solidifying to yield a sufficient amount of heat. Supercooling may be minimized by stirring or by administration of mechanical shock of the sample to induce nucleation.



Fig. 1.3.9 Real temperature-time curve obtained in experiments with its ideal counterpart. [Pelton, 2001].

Another important factor in thermal analysis is that the sample should be kept at uniform temperature. Temperature gradients in the sample will cause a part of the sample to solidify before the rest and consequently a rounded slope will be detected. This uniformity of temperature can be ensured by constantly stirring the sample or by the use of a furnace with a good constant temperature zone or by bubbling a gas through the sample. Also, care should be taken for volatilization or oxidation of the sample during repeated heating or cooling. If there is some sample loss or oxidation, the final composition of the sample cannot be taken as "weighed-out".

Usually, for a steep liquidus, the cooling curve method returns lower liquidus temperature than the true behaviour. The amount of solid precipitated at a steep liquidus (by applying the lever rule) can be said to be comparatively small and hence a small amount of heat is evolved. Therefore, unless sufficient amount of solid precipitates at temperature lower than the liquidus temperature, phase change cannot be detected. Hence, thermal analysis is less precise for steep liquidus determination.

Solidus temperatures are less precisely determined by cooling curves especially if precipitated solid is a solution. If a solid solution is precipitated then the solid will contain composition gradients and solidification will not stop at the solidus temperature. Also, precipitated solid will insulate the thermocouple from the sample and, by the time solidus temperature is reached, the sample temperature will have lagged well behind the furnace temperature. Thus, cooling curves are not an appropriate technique to determine the solidus temperature. Solidus temperatures are often measured by annealing the solid solutions obtained from cooling curve experiments at maximum possible temperature and then using heating curves. Peritectic reactions are also not precisely measured by thermal arrest as they are kinetically hindered and require enough time for completion.

Normally, oxide phase equilibria are not usually precisely measured by thermal analysis. The viscosity of the liquid is very high and crystallization from such high-viscosity liquid proceeds with great difficulty, and accordingly, the attainment of equilibrium under such conditions requires excessively long periods of time.

A variation of thermal analysis technique is Differential Thermal Analysis (DTA). The principle behind DTA is measurement of the temperature difference between the sample of interest and a reference sample which is inert during a heating or cooling cycle and whose thermal behavior is accurately known. The sample and reference material are placed in separate chambers within a furnace and a thermocouple is then placed in both chambers directly in contact with the sample and connected in series. The differential obtained from the temperature difference at both the thermocouple is amplified by a suitable dc amplifier to attain a greatly increased sensitivity. Thus it is very useful in determining the temperatures for phase changes. One of the disadvantages of using DTA is that, because of large surface to volume ratio of the small samples used, sample temperatures often do not increase sufficiently after supercooling. Also, it is more difficult to avoid supercooling in DTA as the samples cannot be stirred. Fig. 1.3.10 shows a schematic representation of DTA measurement.



Fig. 1.3.10 Schematic representation of DTA measurement [Hemminger and Sarge, 1999].

1.4 Modus operandi for thermodynamic optimization

All the calculations and optimizations in the present work were performed with the FactSageTM thermochemical software. The various steps followed in the present work which collectively come under the CALPHAD approach were:

- # The binary systems to be optimized during the present work were identified.
- # Collection of data in the literature for the system:

All the data in the literature on the thermodynamic properties of the chosen systems were collected. These data were phase diagram data, thermodynamic properties like enthalpy of mixing in a solution phase or enthalpy of formation for compounds, activity of constituents in a solution, *etc*. Sometimes data other than thermodynamic properties, such as magnetism or electrical conductivity, which can be helpful in evaluation of a system, were also collected. When enough data were not available in a lower-order binary system, data from a ternary system were used to deduce some necessary conclusions.

Selection of the appropriate thermodynamic model:

As stated previously, an adequate model representing the Gibbs energy functions for a phase is required. This is very important since a good physical model based on the structure of the phase increases the accuracy of predictions of solution properties in multicomponent systems. In the present work, the Modified Quasichemical Model (MQM) capable of taking into account ordering or clustering in the liquid phase was chosen. In the present work, the Gibbs energies of solid phases were written using formalisms presented by Eqs. 1.2.20-1.2.22. For this purpose, the crystal structures of the various solid phases were reviewed for proper distribution of components in different sublattices.

Critical evaluation of collected experimental data:

The experimental data by different authors were often found to differ from each other by more than the stated experimental error limits. Sometimes data were not thermodynamically consistent with each other. Therefore, all the available experimental data were evaluated on the basis of experimental techniques and thermodynamic consistency. When the accuracy of the experimental data was difficult to evaluate from the description of the experimental technique, their consistency or inconsistency was discernible during the simultaneous optimization of the data. Also, during evaluation of data it is very important to use original (raw) experimental data, not the derived quantities. Mostly, the derived quantities have more error limits than the original data.

Optimization of model parameters for the system:

After evaluation of the experimental data, optimization was performed on the basis of selected reliable data to obtain the values of the model parameters. In this stage, optimization software, the OptiSage module in FactSageTM, was quite useful.

OptiSage is an optimizer module which works on the principles of the Bayesian least squares technique. This module generates a consistent set of model parameters from a given set of experimental data which in turn are used to represent the Gibbs energies of phases. In simple words, OptiSage gives model parameters which can reproduce the input data. While using OptiSage to get the best fit, the researcher has to use his own judgment on the selection of parameters, such as which should be fixed or altered and if additional parameters have to be introduced. The convergence of the results in OptiSage depends upon the starting values given to the model parameters and the error limits set for the input data. Sometimes several steps are required to obtain the model parameters which can satisfactorily reproduce the input data. Also in some cases, it is easier and faster to obtain starting values from OptiSage, which can roughly reproduce the data, and then refine the fitting by the trial and error method. In the present work, the optimized parameters were obtained with the help of OptiSage or sometimes with both OptiSage and the trial and error method.

Back-calculation of all thermodynamic data and phase diagrams: Once satisfactory model parameters were obtained, all the thermodynamic data and experimental data were back-calculated for comparison with the optimized values.

Evaluation of ternary systems:

The presently obtained model parameters for the binary systems were combined with previously optimized binary parameters of the other binary sub-systems to estimate the Gibbs energies of solutions in the ternary systems using the techniques given in section 1.2.3. With the help of these Gibbs energies, evaluations and predictions were made for the ternary systems. Wherever required, ternary interaction parameters were also added.

2. THE UNARY AND BINARY SYSTEMS

In the present work, all the thermodynamic data for the CaO, MgO, Al₂O₃, B₂O₃ and SiO₂ phases were taken from the FToxide database. Over the years many assessments and thermodynamic optimizations have been performed using these data in the CRCT, Ecole Polytechnique. The thermodynamic data for these phases are quite well established in the FToxide database. As the present work involves incorporation of BaO and SrO into this big database, literature surveys and assessments were performed for the thermodynamic data of pure BaO and SrO phases. In the SiO₂-B₂O₃-Al₂O₃-CaO-MgO-BaO-SrO system there are 11 binary systems which contain either BaO or SrO (or both):

- 1. SrO-BaO
- 2. SrO-CaO
- 3. BaO-MgO
- 4. SrO-MgO
- 5. BaO-CaO
- 6. SrO-SiO₂
- 7.BaO-SiO₂
- 8. SrO-Al₂O₃
- 9. BaO-Al₂O₃
- 10. BaO-B₂O₃
- 11. $SrO-B_2O_3$

This chapter includes thermodynamic assessments and optimizations for the pure BaO and SrO phases and for these 11 binary systems.

2.1 Thermodynamic data for pure SrO

Risold, Hallstedt, and Gauckler (1996) reported an assessment of the Strontium-Oxygen system in which they reviewed the thermodynamic properties of SrO. The standard enthalpy of formation (ΔH^0_{298}), the standard entropy (S^0_{298}) and heat capacity (C_p) for SrO were taken from this publication. For the melting point of SrO, the lower melting point of 2430 °C reported by Schumacher (1926), using his hand-made apparatus, was preferred over the higher melting point of 2597 °C as accepted by Risold, et al. (1996). Our preferred value is also consistent with the measurement on pure SrO by Hanic, Chemekova, and Udalov (1979). The present accepted value agrees with the fact that the melting point of SrO is expected to be lower than the melting point of CaO, 2572 °C (following the trend that melting points of alkaline-earth oxides decreases while descending the periodic table), accepted by us in our previous work [Eriksson, Wu, Blander, and Pelton (1994)]. The enthalpy of melting for SrO and heat capacity for liquid SrO were taken from the only available values in the literature reported by Irgashov, Tarasov, and Chekhovskii (1985) using DSC. Thus, thermodynamic data for liquid SrO, based upon the above values, and the thermodynamic data of solid SrO taken from Risold, et al. (1996) are given in Table 2.1.

SrO (solid)	$\Delta H^{0}_{298} = -592.142$	$S_{298}^{0} = 53.580$	$Cp = 47.56 + 0.00614 T - 380000 T^{2} (298.15)$
	(kJ/mole) [Risold et al. '96]	(J/mol/K) [Risold et al. '96]	< T < 6000 K) [Risold et al. '96] (J/mol/K)
SrO (liquid)	$\Delta H^0_{fusion} = 80.950$	$\Delta S^{0}_{\text{fusion}} = 29.948$	C _p (liquid, SrO) = C _p (solid, SrO) (298.15< <i>T</i> <
	(kJ/mole) [Irgashov et al.	(J/mol/K)	2703 K) (J/mol/K)
	'85]		73.1 $(2703 < T < 3000 \text{ K}) (J/mol/K)$
	$T_{fusion} = 2430 \ ^{\circ}C$		[Irgashov et al. '85]
	[Schumacher '26]		

Table 2.1 Thermodynamic data for the unary phase SrO.

2.2 Thermodynamic data for pure BaO

Zimmermann, Hack, and Neuschutz (1995) and Zhou, Arroyave, Randall, and Liu (2005) performed a thermodynamic assessment and optimization of the Barium-Oxygen system. The JANAF [Stull and Prophet (1985)] thermochemical tables also contain data for the BaO solid and liquid phases. The final assessed values of the standard enthalpy of formation (ΔH^{0}_{298}), standard entropy (S^{0}_{298}) and temperature of melting for the BaO solid phase used by Zimmermann, et al. (1995) and Zhou, et al. (2005) in their optimizations are close to the values reported in the JANAF tables. No experimental measurements for the heat capacity of the liquid BaO phase and enthalpy of melting for the solid BaO phase could be found in the literature. These values were estimated in the JANAF tables. In the present work, all the thermodynamic data of the BaO solid and liquid phases were taken from JANAF [Stull and Prophet (1985)], which are also presented in Table 2.2.

	-		-
BaO (solid)	$\Delta H^{0}_{298} = -548.104$	$S^{0}_{298} = 72.069$	$Cp = 59.418 + 0.00818 T - 156351 T^2 - 3762 T^1$
	(kJ/mole)	(J/mol/K)	$-0.216 T^{0.5}$ (298.15 < T < 6000 K) (J/mol/K)
BaO (liquid)	$\Delta H^0_{fusion} = 59.000$	$\Delta S^{0}_{fusion} = 25.809$	C_p (liquid, BaO) = C_p (solid, BaO) (298.15< T <
	(kJ/mole)	(J/mol/K)	1600 K) (J/mol/K)
	$T_{fusion} = 2013 \ ^{\circ}C$		66.944 (1600 < T < 3000 K) (J/mol/K)

Table 2.2 Thermodynamic data for the unary phase BaO [Stull and Prophet (1985)].

2.3 The BaO-SrO, SrO-CaO, BaO-CaO, SrO-MgO and BaO-MgO systems

The optimized phase diagram for the BaO-SrO system is shown in Fig. 2.3.1 and optimized parameters are presented in Table 2.3. K. T. Jacob and Varghese (1995) measured the miscibility gap in the monoxide solid solution by lattice parameter measurements using XRD. These data are well reproduced in Fig. 2.3.1. The solid solution in Fig. 2.3.1 was modeled using a single-sublattice simple substitutional model (i.e., (Sr,Ba)O). Flidlider, Kovtunenko, Kiseleva, and Bundel (1966) measured the enthalpy of mixing in the monoxide phase by dissolving the samples prepared at 1150 °C in HCl. These data are compared with the present calculations in Fig. 2.3.2. Moreover, the experimental data in Figs. 2.3.1 and 2.3.2 are incompatible and cannot be simultaneously exactly fitted unless the entropy of mixing in the solid solution is assigned an unreasonable value. The small sub-regular term presented in Table 2.3.1 was required as the critical point composition is slightly shifted from the 50 mol% SrO composition. No phase diagram and thermodynamic data for the liquid phase in this system could be found in the literature. The liquid phase was assumed to be ideal in the present calculations.

The optimized phase diagram for the SrO-CaO system is shown in Fig. 2.3.3 and optimized parameters are presented in Table 2.3.1. K. Thomas Jacob and Waseda (1998) measured the miscibility gap in the monoxide solid solution by lattice parameters measurements using XRD. Roth (1990) also measured the extent of miscibility by unit cell measurements but the shape of the (im)miscibility curve determined by him was unusual. The solid solution in Fig. 2.3.3 was modeled using single-sublattice simple substitutional model (i.e., (Sr,Ca)O). Flidlider, et al. (1966), as in the BaO-SrO system, measured the enthalpy of mixing in the monoxide phase which is compared with the present calculations in Fig. 2.3.4. The small sub-regular term presented in Table was required as the critical point composition is slightly shifted from the 50 mol% SrO composition. No phase diagram and thermodynamic data for the liquid phase in this system could be found in the literature. The liquid phase was assumed to be ideal in the present calculations.

No phase diagram measurement in the literature could be found for the BaO-CaO system. Flidlider, et al. (1966), from the interpretation of their own calorimetric measurements, mentioned a very low mutual solubility among these solids. Van-der Kemp et al. (1994) calculated the phase diagram of this system by estimating the excess thermodynamic functions from the previously measured oxides and halides mixtures. Seo, Zhou, and Tsukihashi (2005) by molecular dynamics simulations estimated a liquidus similar to Van-der Kemp et al. (1994. As the BaO and CaO phases belong to the same structure, some amount of solid solubility among them can be expected. In the absence of any experimental data, the mutual solubility among the solid phases was estimated with the help of the following equation presented by Forland [Blander (1962)] to calculate the columbic energy change by mixing two ionic liquid salt systems with a common anion (a case similar to the present situation where Ba and Ca cations are mixing with oxide anion, but in a solid solution):

$$\Delta_{\varepsilon_{c}} = -e^{2} \left(\frac{1}{d_{1}} + \frac{1}{d_{2}} \right) \left(\frac{d_{1} - d_{2}}{d_{1} + d_{2}} \right)^{2}$$

where, Δ_{ε_c} = columbic energy change, e = electronic charge, d_i = sum of radii of the anion and the mixing cation *i*.

For the systems BaO-SrO, SrO-CaO and CaO-MgO where critical temperatures of the miscibility gaps are known, the value $-\frac{\Delta_{sc}}{e^2}$ was plotted against the critical temperature (the required ionic radii were taken from reference, (www.webelements.com (2012); O = 124pm, Ca = 114pm, Ba = 149pm). The straight line fit of these three points was extrapolated as shown in Fig. 2.3.5 to calculate the metastable critical temperature for the system BaO-CaO as 3033 °C. A regular solution parameter presented in Table 2.3.1 was used to reproduce this critical temperature. The solid solution was modeled using a single-sublattice simple substitutional model (i.e., (Ba,Ca)O). In the present calculations, the liquid phase in the BaO-CaO system was assumed ideal. The calculated phase diagram of the system is shown in Fig. 2.3.6.

Wartenberg and Prophet (1932) by equilibrium/quenching analysis measured the liquidus in the SrO-MgO system. No thermodynamic data or phase diagram data on mutual solubility of the two oxides could be found in the literature. As the two oxides belong to the same structure some

amount solid solubility can be expected. In the absence of any experimental data, the mutual solubility among the solid phases was estimated in the same way as in the BaO-CaO system (the required ionic radii were taken from reference, (www.webelements.com (2012); Sr = 132pm, Mg = 86 pm). The calculated extrapolated critical temperature (metastable) of immiscibility in this system is about 6800 °C (Fig. 2.3.5). A regular solution term presented in Table 2.3.1 was used to reproduce such a critical temperature. This gives negligible mutual solid solubility among the SrO and MgO phases. In the present calculations, the liquid phase was assumed as ideal. No effort was made to fit the experimental points of Wartenberg and Prophet because these points are not consistent with the melting points, which are comparatively better established in the literature, of the pure oxides (SrO and MgO). The present calculated phase diagram of the SrO-MgO system is shown in Fig. 2.3.7. Van-der Kemp, et al. (1994) calculated the phase diagram of this system by estimating the excess thermodynamic functions from the previously measured oxides and halides mixtures. Their calculated phase diagram also showed negligible solubility of SrO in MgO and a very small solubility of MgO in SrO.

Wartenberg and Prophet (1932) by equilibrium/quenching analysis measured the liquidus in the BaO-MgO system. No thermodynamic data or phase diagram data on mutual solubility of the two oxides could be found in the literature. As the two oxides belong to the same structure some amount of solid solubility can be expected. In the absence of any experimental data, the mutual solubility among the solid phases was estimated in the same way as in the BaO-CaO system. The calculated extrapolated critical temperature (metastable) of immiscibility in this system is above 9000 °C (Fig. 2.3.5). A regular solution term presented in Table 2.3.1 was used to reproduce such

a critical temperature. This gives negligible mutual solid solubility among the BaO and MgO phases. The calculated diagram of Van-der Kemp, et al. (1994) showed negligible solid solubility at either end of the phase diagram. In the present calculations, the liquid phase in the BaO-MgO system was assumed ideal and the calculated phase diagram is shown in Fig. 2.3.8. No effort was made to fit the experimental points of Wartenberg and Prophet because these points are not consistent with the melting points, which are comparatively better established in the literature, of the pure oxides (BaO and MgO).

Table 2.3.1 Optimized thermodynamic parameters (in Joules/mol) for the monoxide phase (Model parameters of Eq. 1.2.21).

Monoxide	
$q_{CaSr}^{11} = 27748 - 6.359 T$; $q_{CaSr}^{12} = -1674$	
$q_{BaSr}^{11} = 35698 - 8.870T$; $q_{BaSr}^{21} = -3138$	
$q_{BaCa}^{11} = 58600$	
$q_{SrMg}^{11} = 117000$	
$q_{BaMg}^{11} = 134000$	



Fig. 2.3.1 Optimized phase diagram of the BaO-SrO system



Fig. 2.3.2 Enthalpy of mixing in the BaO-SrO monoxide phase at 1150 °C.



Fig. 2.3.3 Optimized phase diagram of the SrO-CaO system.



Fig. 2.3.4 Enthalpy of mixing in the SrO-CaO monoxide phase at 1150 °C.



Fig. 2.3.5 Calculation of metastable critical temperature in alkaline-earth oxide systems.



Fig. 2.3.6 Calculated phase diagram of the BaO-CaO system.



Fig. 2.3.7 Calculated phase diagram of the SrO-MgO system.



Fig. 2.3.8 Calculated phase diagram of the BaO-MgO system.

2.4 The SrO-SiO₂ system

The optimized phase diagram of the system is shown in Fig. 2.4.1 and optimized thermodynamic properties are presented in Table 2.4.1. The optimized MQM parameters (and the coordination numbers) for the liquid phase are presented in Table 2.4.1. For these parameters, the same notations were used as used by Pelton and coworkers [Pelton, et al. (2000)]. No thermodynamic optimization for this system was found in the literature.

Eskola (1922) first studied the system by annealing and quenching techniques followed by optical microscopy. He reported Sr_2SiO_4 (Sr_2S) and $SrSiO_3$ (SrS) as the equilibrium solid phases. Later, Nurse (1952) by X-ray diffraction (XRD) reported the Sr_3SiO_5 (Sr_3S) as equilibrium phase. Fields, Dear, and Brown (1972) measured the solidus and liquidus in the SrO-rich side of the system by visual inspection using an oxygen-acetylene torch. They reported all the three silicates shown in Fig. 2.4.1 as equilibrium phases by XRD. Huntelaar, Cordfunke, and Scheele (1993) by DTA measured the liquidus and solidus from 48 to 75 mol% SiO₂. Ghanbari-Ahari and Brett (1988), while studying SrO-MgO-SiO₂ system by annealing and quenching techniques, reported some data on the silica-rich side of the binary system. Greig (1927) measured the monotectic temperature and liquidus by equilibration and quenching techniques. V. B. Hageman and Oonk (1986) measured the miscibility gap in the system by equilibration and refractive index measurement of the quenched samples. Ol'shansky (1951) by quenching techniques studied the miscibility gaps in the alkaline-earth oxide-silica melts and reported the critical temperature for the miscibility gap in the SrO-SiO₂ system. All these data are compared with the optimized phase

diagram in Fig. 2.4.1. The low-temperature decomposition of Sr_3S was calculated as 1200 °C. There is no experimental evidence to prove that this phase is stable below this temperature. But, the instability of the Sr_3S phase at lower temperatures (as shown in Fig. 2.4.1) helped in fitting phase diagram data at 1350 °C in the ternary $SrO-Al_2O_3-SiO_2$ system. Fields, et al., reported the Sr_3S as stable in their binary phase diagram till 1200 °C. Hence, in the absence of any experimental data, the low-temperature decomposition was chosen as 1200 °C. A similar phase Ca_3SiO_5 (C_3S) also decomposes at 1300 °C. But, it should be noted that more experimental work is required to corroborate the low-temperature decomposition of the Sr_3S phase as shown in Fig. 2.4.1.

Polymorphism in the Sr₂S phase has been extensively studied [Catti, Gazzoni, Ivaldi, and Zanini (1983);Catti and Gazzoni (1983);Catti, Gazzoni, and Ivaldi (1983);J. Liu, Duan, Mei, Smith, and Hardy (2002);Hahn and Eysel (1970);Pieper, Eysel, and Hahn (1972);Catti, Gazzoni, and Ivaldi (1984)]. All these authors agree that room-temperature form is isostructural with larnite, β -Ca₂SiO₄ (space group, P2₁/n). It undergoes polymorphic transformation at around 85 °C into the orthorhombic modification, similar to α '-Ca₂SiO₄ (space group, Pmcn). Pieper, et al. (1972) by DSC reported the enthalpy of this transformation as 213 J/mole. Hahn and Eysel (1970) predicted a further polymorphic transformation into high-K₂SO₄ structure, isotypic with α -Ca₂SiO₄ (space group, P $\overline{3}2$ /m) at higher temperature while studying the structure of similar silicates and germanates. In a different work from the same laboratory, Pieper, et al. (1972), by DTA reported that this transformation occurs above 1550 °C. Fields, et al. (1972) while studying the Ba₂SiO₄-Sr₂SiO₄ (B₂S-Sr₂S) system by optical and X-ray diffraction, noted two polymorphic forms of the

Sr₂S above 2100 °C and showed this conversion at about 1700 °C in the phase diagram. They also suggested that the high-temperature form is non-quenchable. In the present work, following the suggestion of Hahn and Eysel (1970) the high-temperature form is considered as isotypic with α -Ca₂SiO₄. The temperature of transformation is assumed to be 1700 °C and the enthalpy of transformation is calculated the same as for the α '- to α -Ca₂SiO₄ conversion (4.2 kJ), from the FTOXID database. As explained below, the heat capacities of all these polymorphs of Sr₂S were assumed identical. No stable polymorphic transformation at atmospheric pressure could be found in the literature for strontium metasilicate. It has the pseudowollastonite structure [Eskola (1922);Buckner and Roy (1960)], (space group, C2/c [Yang and Prewitt (1999)]).

The standard enthalpies of formation (ΔH^{0}_{298}) for the Sr₂S and SrS phases were measured by authors [Huntelaar, Cordfunke, and Ouweltjes (1992b);Barany, King, and Todd (1957);Nacken (1930)] using solution calorimetry at room temperature. These values are compared with the present calculations in Fig. 2.4.2. This figure also compares the present calculations with the calculations performed using the FTOXID database for similar alkaline-earth systems. Nacken (1930) also measured ΔH^{0}_{298} for barium silicates (see BaO-SiO₂ system). He reported much less negative values for ΔH^{0}_{298} for barium silicates than strontium silicates. However, the reverse is expected. In the BaO-SiO₂ system also his data are not consistent with the other available data. The S^{0}_{298} for strontium ortho- and meta-silicates were reported by Huntelaar, Cordfunke, and Westrum (1992) and Weller and Kelley (1964) from low-temperature heat capacities measurements by adiabatic calorimetry. The present optimized S^{0}_{298} are compared with these data in Table 2.4.1. It is worth mentioning here that in all these references, for the measurement of ΔH^{0}_{298} and S^{0}_{298} , ortho-silicate crystals were prepared by reacting starting materials in temperature ranges where the α' - modification is stable. No indication was given that crystals were quenched or slowly cooled from those temperatures to room temperature. However, the enthalpy of β (room-temperature modification) to α' transformation is quite low [Pieper, et al. (1972)]. Therefore, in the present calculations it was reasonably assumed that experiments were performed on the room-temperature modification. Huntelaar, et al. (1993) reported the enthalpy of fusion by calculating the area under the melting peak in DTA for SrS as 56 ± 6 kJ/mol. The present calculated value is 54.72 kJ/mol.

Huntelaar, Cordfunke, and Westrum (1992) also measured the enthalpy increments ($H^{o}_{(T)} - H^{o}_{(25)}$) in the range 227 °C to 627 °C using isothermal calorimetry for the Sr₂S and SrS phases. These enthalpy increments were used to optimize the heat-capacity (C_p) equations, presented in Table 2.4.1, for these compounds. The enthalpy increments are compared with the present calculations in Figs. 2.4.3 and 2.4.4 respectively. In these temperature ranges the α '- modification of Sr₂S is stable, hence the optimized heat capacity belongs to this modification. However, in the absence of any other experimental data on the heat capacities of other polymorphs of Sr₂S they were assumed to be equal to the heat capacity of the α '- modification. The optimized heat capacities were extrapolated to higher temperatures as shown in Figs. 2.4.5 and 2.4.6 where they are also compared with the heat capacities obtained from the sum of the heat capacities of the constituent oxides. The optimized standard entropy (S^{0}_{298}) and entropy of formation, with oxides as reference standards (ΔS^{0}_{298}), are presented in Table 2.4.1. Róg, Langanke, Borchardt, and Schmalzried (1974) by EMF measured the Gibbs energy change of reactions which are compared with the present calculations in Figs. 2.4.7-2.4.9. The Gibbs energy of these solid phases were fixed, from the enthalpies and entropies of formation data (Table 2.4.1), and the present calculations differ from the data of Róg, et al. (1974). It is worth mentioning here that, by fitting Nacken's enthalpy of formation (keeping the entropies constant as previous values) for the Sr_2S and SrS phases, the calculated Gibbs energy change for the reaction (in which Sr_3S is not involved) in Fig. 2.4.9 deviates further from the present calculations. Hence, it can be said that Rog's data are inconsistent with the other available data.

Lopatin, Shugurov, Stolyarova, and Tyurnina (2006) measured the activities of SrO and SiO₂ in the system in the temperature range 1567-1697 °C by high-temperature mass spectrometry. The calculated activities at 1647 °C (as solid standard states) in the present work are compared with these data in Fig. 2.4.10 (the different experimental points at the same composition in Fig. 2.4.10 correspond to different temperatures; in the scale of this figure there is practically no difference in the calculated activities in this temperature range, therefore the present calculations were performed at 1647 °C). These data were not given much weight as they were found to be inconsistent with the phase diagram of the system. For example, at 1647 °C, they reported unit activity of SrO in two phase regions ($0.3 \le X_{SiO2} \le 0.4$) where SrO is not present. Also, it is evident that SrO activity measured by them at the SiO₂-rich region is unreasonably high. Moreover, the Gibbs energy of formation at 1647 °C of the Sr₂S phase calculated with the help of these activities is -138 kJ whereas the present optimized value is -228 kJ. The present work fits the standard enthalpy of formation, entropy and heat capacity of this phase quite well. The difference between the optimized Gibbs energy of formation at 1647 $^{\circ}$ C of the Sr₂S phase and the value obtained from the help of experimental activities suggest that these activities are not consistent with the other available thermodynamic data.

Richet and Bottinga (1985) by dropping melted samples into an ice-calorimeter (to a final glassy state) measured the enthalpy increments ($H_{(T)} - H_{(273)}$) in the liquid and glass (non-equilibrium liquid) phase for the composition SrS₂ (not for Sr₂S).Their data are compared with the present calculations in Fig. 2.4.11. It must be noted that for the exact comparison of these data, $H_{(273)}$ of the glassy phase is required, which is not available. The present calculations were performed by extrapolating the thermodynamic properties of the liquid phase to 0°C. However, it is evident in this figure that the optimized heat capacity agrees well with the experimental heat capacity (as the slope of the calculated curve is reasonably close to the experimental slope).

No data on the mutual solubility among the SrO and SiO₂ phases could be found in the literature. Moreover, their different crystal structures and the very large difference in the ionic radii of Sr and Si (Sr=132pm and Si=40pm [www.webelements.com (2012)]) also mitigate against any appreciable mutual solubility among them. Also, no data on the solid solubility in the solid phases appearing in the SrO-SiO₂ system were found. They were modeled as stoichiometric phases. The enthalpy of mixing and entropy of mixing at 3000 °C in the liquid phase in the SrO-SiO₂ is compared with the other alkaline-earth oxide-alumina systems in the next section (Figs. 2.5.6 and 2.5.7 respectively). The enthalpy of mixing follows the trend that it is expected to be more negative in the series CaO to BaO.

Table 2.4.1 Optimized thermodynamic parameters for the SrO-SiO₂ system.

Liquid phase (Quasichemical model parameters)				
$Z_{sisi}^{Si} = 2.75488750$	0; $Z_{SrSr}^{Sr} = 1.37744375$			
$\Delta g_{Sr-Si} = (-221752 J/mol$	$+ 17.614 T - 20920 X_{Sr-Sr} - 4602$	$24 X_{Si-Si} + 74475 X_{Si-Si}^{3} + (2)$	$267125 - 123.428 T) X_{\text{Si-Si}}^{11}$	
Solid phases				
ΔH^{0}_{298} (kJ/mole)				
Compound	Calculated, elements as reference	Calculated, oxides (stable at room- temperature) as reference	Experimental values, oxides (stable at room- temperature) as reference	
β-Sr ₂ SiO ₄	-2304.000	-209.000	-209.370 ± 1.000 [Barany et al., '57] -137.890 [Nacken, '30] -210.716 [Huntelaar et al., '92b] ^(a)	
α '-Sr ₂ SiO ₄	$\Delta H_{tr}^{0}(b) = 0.213$ [Hahn and Eysel, '70] (at 85 °C)			
α -Sr ₂ SiO ₄	$\Delta H_{tr}^{0 (b)} = 4.277 \text{ [estimated]}$ (at 1700 °C)			
SrSiO ₃	-1632.000	-129.200	-130.710 ± 0.670 [Barany et al., '57] -103.180 [Nacken, '30] -132.458 [Huntelaar et al., '92b] ^(a)	
Sr ₃ SiO ₅	- 2868.020	-180.900		
$S^{0}_{298}, \Delta S^{0}_{298} \& \Delta S^{0}_{tr} (J/mol/K)$				
Compound	Calculated value	Experimental values	ΔS^0_{298} , (calculated) oxides (stable at room-temperature) as reference	

β-Sr ₂ SiO ₄	155.600	153. 134 ± 1.255 [Weller and Kelly, '64] 155.440 \pm 0.250 [Huntelaar et al., '92]	6.980
SrSiO ₃	95.600	96.650±0.837 [Weller and Kelly, '64] 95.650±0.210 [Huntelaar et al., '92]	0.560
Sr ₃ SiO ₅	228.220		26.02
C _p (J/mol/K)			
Compound	Optimized C _p		
β , α' , α -Sr ₂ SiO ₄ SrSiO ₃	156 + 0.0235 T -2718797 T ² + 1.4E-5 T ² -5.4E-9 T ³ (25 < T < 2127 °C) 217.92 (2127 < T <2400 °C) 104 + 0.026 T -2113450 T ⁻² -1E-9 T ³ (25 < T < 2000 °C)		
Sr ₃ SiO ₅	$C_{p} (Sr_{2}SiO_{4}) + C_{p} (SrO)$		

^(a) In this ref. values of heat of formation from elements were given, so here they have been recalculated in terms of oxide by subtracting the heat of formation of oxides.

^(b) Enthalpy of transformation from Room-Temperature (RT) to Low-Temperature form (LT) (kJ/Mole).

^(c) Entropy of transformation from Room-Temperature (RT) to Low-Temperature form (LT) (J/mol/K).



Fig. 2.4.1 Optimized phase diagram of the SrO-SiO₂ system.



Fig. 2.4.2 Optimized standard enthalpy of formation in the alkaline-earth oxide-silica systems (All experimental points are for the SrO-SiO₂ system).



Fig. 2.4.3 Enthalpy increments $(H_{(T)} - H_{(298)})$ per mole of the Sr₂SiO₄ phase.



Fig. 2.4.4 Enthalpy increments $(H_{(T)} - H_{(298)})$ per mole of the SrSiO₃ phase.



Fig. 2.4.5 Optimized heat capacity of the Sr_2SiO_4 phase compared with the heat capacity obtained from sum of the constituent oxides.



Fig. 2.4.6 Optimized heat capacity of the $SrSiO_3$ phase compared with the heat capacity obtained from sum of the constituent oxides.



Fig. 2.4.7 Optimized Gibbs energy change in the reaction SrO+Sr₂SiO₄=Sr₃SiO₅.



Fig. 2.4.8 Optimized Gibbs energy change in the reaction $Sr_3SiO_5+SrSiO_3=Sr_2SiO_4$.



Fig. 2.4.9 Optimized Gibbs energy change in the reaction Sr₂SiO₄+SiO₂=2SrSiO₃.



Fig. 2.4.10 Optimized activity at 1647 $^{\circ}$ C (standard states are the respective solid phases) in the SrO-SiO₂ system.



Fig. 2.4.11 Enthalpy increments ($H_{(T)}$ - $H_{(273)}$) at the SrSi₂O₄ composition in the liquid and glass phase.

2.5 The BaO-SiO₂ system

The optimized phase diagram of the system is shown in Fig. 2.5.1 and optimized thermodynamic properties are presented in Table 2.5.1. The optimized MQM parameters (and the coordination numbers) for the liquid phase are presented in Table 2.5.1. For these parameters, the same notations were used as used by Pelton and coworkers [Pelton, et al. (2000)]. The BaO-SiO₂ system was optimized by Jung (2008). This optimization by Jung (2008) is presented here. Jung neglected the presence of two compounds (B_3S_5 and B_5S_8 in Fig. 2.5.1) in his optimization. These compounds were then later added during the present work. Cenerino, Chevalier, and Fischer (1992) presented an optimized phase diagram of the system. However, in this reference neither the data used for optimization nor optimized parameters were presented.

Eskola (1922) by quenching and optical microscopy first studied the system in the range 40-75 wt.% BaO. He reported congruent melting of BaSiO₃ (BS) and possible solid solution extending between the Ba₂Si₃O₈ (B₂S₃) and BaSi₂O₅ (BS₂) phases. Jaeger and Van Klooster (1916) by thermal analysis reported the melting point of BS as 1604 °C. Fields, et al. (1972) also reported this melting point very close to 1600 °C in their measured BaSiO₃-SrSiO₃ phase diagram. Roth and Levin (1959) by quenching followed by XRD and optical microscopy reinvestigated the phase diagram between the B₂S₃ and BS₂ phases. They found two additional compounds, Ba₅Si₈O₂₁ (B₅S₈) and Ba₃Si₅O₁₃ (B₃S₅) instead of the solid solution reported by Eskola (1922). The results of Roth and Levin (1959) were confirmed by Von Oehlschlegel (1971). Von Oehlschlegel also reported the decomposition of the B₃S₅ phase into B₅S₈ and BS₂ phases at 1300
°C. Von Oehlschlegel and Ohnmacht (1975) by quenching, optical microscopy and DTA studied the partial phase equilibria of the BaS₂-SiO₂ system. These data are compared with the present calculations in Fig. 2.5.1. There are XRD data [Glushkova and Keler (1957);Eysel (1970)] for the presence of the Ba₃SiO₅ (B₃S) phase. Pietro Appendino and Appendino Montorsi (1969), while studying the BaO-SrO-SiO₂ system, and Brisi and Appendino (1967), while studying the BaO-CaO-SiO₂ system, by quenching and XRD reported this phase as stable at 1100 °C. As the similar Sr₃S and C₃S phases decompose eutectoidly at lower temperature (see the SrO-SiO₂ section), the low-temperature decomposition for the B₃S phase was tentatively calculated as 1050 °C. No other phase diagram data for this compound could be found in the literature. In the present calculations, this compound was calculated to melt congruently similarly to Sr₃S (see SrO-SiO₂ section). The calculated melting temperature is tentative and further experimental work is required to confirm this.

There are different data on the melting temperature of the Ba₂SiO₄ (B₂S) phase. Toropov and Fedorov (1964) determined the melting point of B₂S as part of the phase diagram study for the Ca₂SiO₄-Ba₂SiO₄ (C₂S-B₂S) system. The method of the temperature determination was not specified. They claimed that the melting temperatures of B₂S measured in the previous studies [1820 °C by Braniski (1961); 1740 °C by Toropov, Galakhov, and Bondar (1954)] are lower than their measurement at 1960 °C due to partial contamination by BaCO₃ in the B₂S sample. Fields, et al. (1972) determined the melting point of B₂S as 2150 °C by visual observation with an optical pyrometer as part of the phase diagram study of the Ba₂SiO₄-Sr₂SiO₄ (B₂S-Sr₂S) section. During optimization, the melting point reported by Fields, et al. (1972) was found to fit much

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better with the other available phase diagram and thermodynamic data. Unlike C₂S and Sr₂S, only one crystalline phase for B₂S is known (α '-structure which is isostructural with α '-C₂S; unmodulated β -K₂SO₄ type).

Greig (1927) first investigated the possibility of a liquid miscibility gap in the BaO-SiO₂ system. He observed a very flat SiO₂ liquidus at about 1680 °C between 85 to 97 mole % SiO₂, and no stable liquid immiscibility was observed in his quenched samples. Ol'shansky (1951) claimed that no liquid phase separation occurs in the BaO-SiO₂ system between 1800 and 2570 °C. Argyle and Hummel (1963) by electron microscopic observation reported stable liquid immiscibility above 1655 °C in the range 5-25 mole % BaO. Later, Seward, Uhlmann, and Turnbull (1968) by optical microscopy reported a metastable miscibility gap with upper consolute point at about 10 mole % BaO and 1460 °C. However, they also reported that liquid immiscibility was even observed for the 10 mole% BaO sample quenched from 1725 °C under the TEM micrograph image. In the present calculations, it was found very difficult to suppress the liquid miscibility gap in high SiO₂ region with the reproduction of the flat liquidus of SiO₂ as reported by Argyle and Hummel (1963). The previous optimized phase diagram by Cenerino, et al. (1992) also predicted the stable liquid miscibility gap.

The standard enthalpy of formation (ΔH^{0}_{298}) for various barium silicates were measured by authors [Nacken (1930); Barany, et al. (1957); Huntelaar, Cordfunke, and Ouweltjes (1992a)] using solution calorimetry at room temperature. These data are well reproduced in Fig. 2.5.2. As

in the SrO-SiO₂ system, the data by Nacken (1930) differ considerably from the other available data. Also, Nacken (1930) reported ΔH^{0}_{298} of barium silicates much less negative than the strontium silicates. However, the reverse is expected. The standard entropies (S^{0}_{298}) for barium silicates were reported by Weller and Kelley (1964) using low-temperature heat capacity measurements by adiabatic calorimetry. These data are compared with the present optimized values in Table. 2.5.1. The heat capacities of B₂S and BS were taken from Barin (1995). These heat capacities are greater than the values obtained by adding the heat capacities of constituent oxides, which is in accordance with the case of the Sr₂S and SrS. For these strontium silicates, heat contents were measured up to 627 °C (see the SrO-SiO₂ section) and the optimized heat capacity is greater than that obtained by adding the heat capacities of constituent oxides. No high-temperature heat capacity or heat content measurements for the other barium silicates could be found in the literature. The heat capacities of other barium silicates are calculated from the sum of the constituent oxides, as shown in Table 2.5.1.

Rog (1980) by EMF measured the Gibbs energy of formation for barium silicates which are compared with the present calculations in Fig. 2.5.3. Unlike in similar work by the same author in the SrO-SiO₂ system (see the SrO-SiO₂ section), where the Gibbs energy change in the various EMF cells were presented in the form of fitted equations, here the Gibbs energies of formation for various silicates were presented in tabular form only for the three temperatures, 927, 1027 and 1127 °C. In this temperature range, on the scale of Fig. 2.5.3, there is practically no change in the values of the calculated Gibbs energies of formation for these compounds. The Gibbs energies of these compounds are fixed from the ΔH_{298}^0 and S_{298}^0 values (Table 2.5.1), Rog's data can be said to be inconsistent with these data. In the $SrO-SiO_2$ system also, Rog's data are not consistent with the other available data.

Tyurnina, Lopatin, Shugurov, and Stolyarova (2006) by Knudsen effusion mass spectrometry determined the activities of SiO₂ and BaO in the BaO-SiO₂ system in the range 1567-1697 °C. These activities are compared with the present calculations at 1637 °C in Fig. 2.5.4 (the different experimental points at the same composition in Fig. 2.5.4 correspond to different temperature; in the scale of this figure there is practically no difference in the calculated activities in this temperature range, therefore the present calculations were done at 1637 °C). It is also evident that the measured SiO₂ activity in the BaO-rich compositions is too high but activities in the SiO₂-rich compositions are comparatively better reproduced. Moreover, the Gibbs energy of formation at 1637 °C of the orthosilicate phase calculated with the help of these activities is -182 kJ whereas the present optimized value is -271 kJ. The present work fits the standard enthalpy of formation and entropy quite well, and the heat capacity of this phase is reasonably well known. The difference between the optimized Gibbs energy of formation at 1637 °C of the orthosilicate phase and the value obtained from the help of experimental activities suggest that these activities are not consistent with the other available thermodynamic data.

Richet and Bottinga (1985) by dropping melted samples into an ice-calorimeter (to final glassy state) measured the enthalpy increments ($H_{(T)} - H_{(273)}$) in the liquid and glass (non-equilibrium liquid) phase for the composition BaSi₃O₇. Their data are compared with the present calculations in Fig. 2.5.5. It must be noted that for the exact comparison of these data, $H_{(273)}$ of the glassy

phase is required, which is not available. The present calculations were performed by extrapolating the thermodynamic properties of the liquid phase to 0°C. However, it is evident in this figure that the optimized heat capacity agrees well with the experimental heat capacity (as the slope of the calculated curve is reasonably close to the experimental slope).

The enthalpy of mixing and entropy of mixing in the liquid phase at 3000 °C (temperature at which the liquid phase exists over the whole region in all the systems) in alkaline-earth oxidesilica systems are compared in Fig. 2.5.6 and 2.5.7 respectively. The enthalpy of mixing is expected to be more negative, i.e., more ordering is expected in the liquid phase in the series MgO to BaO. This trend can be observed in Fig. 2.5.6.

No data on the mutual solubility among the BaO and SiO_2 phases could be found in the literature. Moreover, their different crystal structures and the very large difference in the ionic radii of Ba and Si (Ba = 149 pm and Si = 40 pm, [www.webelements.com (2012)]) also mitigate against any appreciable mutual solubility among them. Also, no data on the solid solubility in the solid phases appearing in the BaO-SiO₂ system were found. They were modeled as stoichiometric phases.

Liquid phase (Quasichemical model parameters) $Z_{SiSi}^{Si} = 2.75488750; Z_{BaBa}^{Ba} = 1.37744375$ $\Delta g_{Ba-Si} = (-238969 + 19.455T) + (-87695 + 25.104) X_{Si-Si} + (-33679 + 38.087 T) X_{Si-Si}^{4} (243694 - 107.702 T$ X_{Si-Si}⁷ Solid phases ΔH^{0}_{298} (kJ/mole) Compound Calculated, Calculated, Experimental values, elements as reference oxides (stable at roomoxides (stable at room-temperature) as reference temperature) as reference Ba₃SiO₅ -245.000-2800.000Ba₂SiO₄ -2292.422 -285.500 -285.292 ± 4.200 [Huntelaar et al., '92a]^(a) -269.784 ± 1.171 [Barany et al., 57] -105.395 [Nacken, '30] BaSiO₃ -1617.258 -158.454 -147.596 ± 2.600 [Huntelaar et al., '92a]^(a) -159.117 ± 0.711 [Barany et al., 57] -84.554 [Nacken, '30] Ba₂Si₃O₈ -4173.220 -344.912 -344.845 ± 1.464 [Barany et al., 57] Ba₅Si₈O₂₁ -10895.534-869.414 $Ba_3Si_5O_{13}$ -6715.246 -517.434BaSi₂O₅ -2543.200-173.696 -172.715 ± 1.046 [Barany et al., 57]

Table 2.5.1 Optimized thermodynamic parameters (in Joules/mol) for the BaO-SiO₂ system.

 $S^{0}_{298}, \Delta S^{0}_{298} \& \Delta S^{0}_{tr} (J/mol/K)$

			0
Compound	Calculated	Experimental	ΔS_{298}^{0} , (calculated)
	value	values	oxides (stable at room-
			temperature) as reference
Ba ₃ SiO ₅	284.400		26.733
Ba ₂ SiO ₄	176.146	176.146 ± 1.674 [Weller and Kelly, '64]	-9.452
BaSiO ₃	108.784	109.620 ± 1.255 [Weller and Kelly, '64]	-4.745

Ba ₂ Si ₃ O ₈	260.450	258.153 ± 2.510	-8.068
Ba ₅ Si ₈ O ₂₁	672.200	[Weller and Kelly, '64]	-19.825
Ba ₃ Si ₅ O ₁₃	415.400		-8.107
BaSi ₂ O ₅	153.400		-1.589
		153.134 ± 1.674	
		[Weller and Kelly,	
		·64]	
Compound	Optimized C _p	3	
Ba ₃ SiO ₅	$3 C_p(BaO) + C_p(SiO_2, Qu)$	artz(h))	
Ba_2SiO_4	153.553 + 0.0430 <i>T</i> - 2790	728 T ⁻² [Barin (1995)]	$(25 < T < 1700 \ ^{\circ}\text{C})$
Ba_2SiO_4 $BaSiO_3$	153.553 + 0.0430 <i>T</i> -2790 100.249+ 0.0387 <i>T</i> -1959	$728 T^{-2}$ [Barin (1995)] $786 T^{-2}$ [Barin (1995)]	$(25 < T < 1700 \ ^{\circ}\text{C})$ $(25 < T < 2200 \ ^{\circ}\text{C})$
Ba ₂ SiO ₄ BaSiO ₃ Ba ₂ Si ₃ O ₈	153.553 + 0.0430 <i>T</i> -2790 100.249+ 0.0387 <i>T</i> -1959 2 C _p (BaO) + 3 C _p (SiO ₂ , Q	 728 T⁻² [Barin (1995)] 786 T⁻² [Barin (1995)] uartz(h)) 	$(25 < T < 1700 \ ^{\circ}\text{C})$ $(25 < T < 2200 \ ^{\circ}\text{C})$
$Ba_{2}SiO_{4}$ $BaSiO_{3}$ $Ba_{2}Si_{3}O_{8}$ $Ba_{5}Si_{8}O_{21}$	153.553 + 0.0430 T - 2790 100.249+ 0.0387 T - 1959' 2 C _p (BaO) + 3 C _p (SiO ₂ , Q 5 C _p (BaO) + 8 C _p (SiO ₂ , Q	 728 T⁻² [Barin (1995)] 786 T⁻² [Barin (1995)] uartz(h)) uartz(h)) 	$(25 < T < 1700 \ ^{\circ}\text{C})$ ($25 < T < 2200 \ ^{\circ}\text{C})$
$Ba_{2}SiO_{4}$ $BaSiO_{3}$ $Ba_{2}Si_{3}O_{8}$ $Ba_{5}Si_{8}O_{21}$ $Ba_{3}Si_{5}O_{13}$	153.553 + 0.0430 T - 2790 $100.249 + 0.0387 T - 1959^{\circ}$ $2 C_{p}(BaO) + 3 C_{p}(SiO_{2}, Q)$ $5 C_{p}(BaO) + 8 C_{p}(SiO_{2}, Q)$ $3 C_{p}(BaO) + 5 C_{p}(SiO_{2}, Q)$	 728 T⁻² [Barin (1995)] 786 T⁻² [Barin (1995)] uartz(h)) uartz(h)) 	$(25 < T < 1700 \ ^{\circ}\text{C})$ $(25 < T < 2200 \ ^{\circ}\text{C})$

^(a) In this refs. values of heat of formation from elements were given, so they have been recalculated in terms of oxide by subtracting the heat of formation of oxides.



Fig. 2.5.1 Optimized phase diagram of the BaO-SiO₂ system.



Fig. 2.5.2 Optimized enthalpies of formation (ΔH^{0}_{298}) in the barium silicates.



Fig. 2.5.3 Optimized Gibbs energy of formation at 1027 °C in barium silicates.



Fig. 2.5.4 Optimized activity of BaO and SiO₂ at 1637 $^{\circ}$ C (standard states are respective solid phases) in the BaO-SiO₂ system.



Fig. 2.5.5 Enthalpy increments $(H_{(T)}-H_{(273)})$ at the BaSi₃O₇ composition in the liquid and glass phase.



Fig. 2.5.6 Enthalpies of mixing in the liquid phase at 3000 °C in the alkaline-earth oxide -silica systems.



Fig. 2.5.7 Entropies of mixing in the liquid phase at 3000 °C in the alkaline-earth oxide-silica system.

2.6 The SrO-Al₂O₃ system

The optimized phase diagram of the system is shown in Fig. 2.6.1 and optimized thermodynamic parameters are presented in Table 2.6.1. The optimized MQM parameters (and the coordination numbers) for the liquid phase are presented in Table 2.6.1. For these parameters, the same notations were used as used by Pelton and coworkers [Pelton, et al. (2000)]. Ye, Zhuang, Wang, Yuan, and Qiao (2007) optimized this system, treating the liquid phase by two-sublattice model for ionic solutions. In this work, however, the thermodynamic data of Bokeriya, Tsagareishvili, and Gvelesiani (1970b) and Levitskii, Skolis, Chentsov, and Golovanova (1972) were not taken into account.

In the SrO-Al₂O₃-SiO₂ system, to obtain the optimal fit of the available data, an additional component in the form of SrAl₂ associate was added to the liquid phase, i.e. SrAl₂O₄ was considered a separate component in the binary SrO-Al₂O₃ system (along with SrO and Al₂O₃). The optimized Gibbs energy of this component (SrAl₂ associate) and its coordination number in the liquid phase is presented in Table 2.6.1. Practically, these SrAl₂ associates are not stable in the binary SrO-Al₂O₃-SiO₂ system, especially in the SiO₂-rich corner. In the SrO-Al₂O₃ system, at 2050 °C and at $X_{Al2O3} = 0.5$, the mole fraction of these associates is only 4.4 x 10⁻⁴.

Hanic, et al. (1979) by DTA and high-temperature XRD, and Massazza (1959) by quenching and optical micrography techniques, reported SrO.2Al₂O₃ (SA₂), SrO.Al₂O₃ (SA) and 3SrO.Al₂O₃ (S₃A) as congruently melting compounds and 4SrO.Al₂O₃ (S₄A) and SrO.6Al₂O₃ (SA₆) as

incongruently melting compounds. Both Hanic, et al. (1979) and Massazza (1959), reported a polymorphic transformation of S_4A , the lower form dissolving 2-3% of Al_2O_3 and undergoing low-temperature decomposition. Hanic, et al. (1979) reported the temperature of the transformation as 1450 °C and Massazza (1959) as 1320 °C. The low-temperature decomposition of S₄A was measured at 1130 °C and 1125 °C by Hanic, et al. (1979) and Massazza (1959) respectively. Starczewski (1964) by cooling curves and XRD reported S₃A and SA as congruently melting and S₄A, SA₂ and SA₆ as incongruently melting compounds. Kadyrova (1999) measured the melting point of the SA₆ compound while studying the CaO-SrO-Al₂O₃ system. His data were consistent with the liquidus data measured by Starczewski (1964). Starczewski (1964) did not report any structural variation of S₄A. In the present work, the temperature for this polymorphic transformation was calculated as 1450 °C and the enthalpy of transformation was estimated from the standard enthalpy of formation [Brisi and Abbattista (1960)] determined by room-temperature solution calorimetry on the two polymorphs obtained by quenching. Bokeriya, et al. (1970b) by DTA reported a phase transformation for SA at 659 °C. Ito, Banno, Suzuki, and Inagaki (1977) by XRD reported this transformation to occur at 650 °C. Recently, Rodehorst, Carpenter, Marion, and Henderson (2003) summarized reported data on this transformation and studied the transformation by infrared powder absorption spectroscopy. They reported this transformation at about 677 °C.

P. Appendino (1972) observed that long annealing (of more than 200 hours at 1400 °C) resulted in partial decomposition of SA_2 synthesized from the melt. He concluded that this compound forms from the melt and is stable only close to its melting point and then decomposes. Teoreanu and Ciocea (1978), while studying the SrAl₂O₄-BaAl₂O₄-Al₂O₃ system, did not find this compound in their annealing the raw materials for 20 hours at 1700 °C. Capron and Douy (2002) by amorphous precursors and XRD reported SA₂ to be stable only at temperatures close to its melting point and below 1100 °C; at intermediate temperatures it cannot crystallize. They also reported, by the same techniques, a new compound, 4SrO.7Al₂O₃ (S₄A₇), stable between 1100 °C to 1500 °C. Hanic, et al. (1979) reported that SA₂ is stable below its melting point. Ye, et al. (2007) also calculated this phase as stable down to lower temperatures. In the present work, SA₂ was considered stable from its melting point to room temperature and the stability of S₄A₇ was calculated according to the data of Capron and Douy (2002).

Dear (1957) by XRD reported the presence of 5SrO.Al₂O₃ (S₅A) with congruently melting behavior. Later, Jiang, Zhang, Huang, Jia, and Guo (2007) synthesized S₅A by the precursor method and studied its optical properties. In the present work, this compound is included as a stable phase with incongruent melting in order to be consistent with the SrO-rich liquidus reported by Hanic, et al. (1979) and Massazza (1959).

Bokeriya, et al. (1970b) performed calorimetric measurements to report the enthalpy increments $(H_{(T)}-H_{(298)})$ for SA which were fitted to obtain the heat capacity (C_p) equations presented in Table 2.6.1. These enthalpy increments are compared with the present calculations, in two different scales, in Fig. 2.6.2 and Fig. 2.6.3. The optimized heat capacity for SA was found to be close to the heat capacity obtained from adding the heat capacities of constituent oxides (C_p (SA) = C_p (SrO, solid) + C_p (Al₂O₃, corundum). Therefore, our estimations for the heat capacity of

compounds other than SA in Table 2.6.1 are reasonable. The enthalpy of transformation of SA from the low-temperature to the high-temperature form was calculated to be 2 kJ/mole by fitting the data in Fig. 2.6.3. The optimized standard entropy (S_{298}^0) and entropy of formation with oxides as reference standards (ΔS_{298}^0) are presented in Table 2.6.1. The ΔS_{298}^0 values are always less than 10 J/(atom of metal) which is reasonable.

Brisi and Abbattista (1960), Massazza (1961) and Massazza and Cannas (1961) by solution calorimetry at room temperature reported enthalpies of formation of some intermediate compounds (ΔH^{0}_{298}). These data are well reproduced as shown in Fig. 2.6.4. Levitskii, et al. (1972) by EMF using the cell (+)Pt,O₂|Sr₃Al₂O₆, SrAl₂O₄, SrF₂|CaF₂|SrO, SrF₂| Pt,O₂(-) reported the Gibbs energy change for the reaction, 2SrO + SA = S₃A. These data are reasonably well reproduced as shown in Fig. 2.6.5.

No data on the mutual solubility among the SrO and Al_2O_3 phases could be found in the literature. Moreover, their different crystal structures and the very large difference in the ionic radii of Sr and Al (Sr = 132m and Al = 67.5 pm, [www.webelements.com (2012)]) also mitigate against any appreciable mutual solubility among them. Also, no data on the solid solubility in the solid phases (except for the low-temperature S₄A phase) appearing in the SrO-Al₂O₃ system were found. They were modeled as stoichiometric phases. Hanic, et al. (1979) reported small solubility of Al_2O_3 (1-2 mol%) in the "low-temperature" S₄A which was neglected in the present calculations.

The enthalpy of mixing and entropy of mixing at 3000 °C in the liquid phase in the SrO-Al₂O₃ is compared with the other alkaline-earth oxide-alumina systems in the next section (Figs. 2.7.7 and 2.7.8 respectively). The enthalpy of mixing follows the trend that it is expected to be more negative in the series CaO to BaO.

Table 2.6.1 Optimized thermodynamic parameters for the SrO-Al₂O₃ system.

Liquid phase (Quasichemical model parameters)					
$Z_{AIA}^{Al} = 2.06616563; Z_{SSSr}^{Sr} = 1.37744375; Z_{SSAL}^{SrAL_2} = 5.50977500; Z_{SSA}^{Sr} = 2.75488750; Z_{AISr}^{Al} = 1.37744375$					
$\Delta g_{\text{Sr-Al}} = (-138072 + 16.736 \text{ T}) - 117989 \text{ X}_{\text{SrSr}} - 16736 \text{ X}_{\text{AlAl}} \text{ J/mol}$					
$g^{0}_{SrAl2} = g^{0}(SrO,Liq) + g^{0}(Al_{2}O_{3},Liq) - 112968 + 2.092 T J/mol$					
Solid Phases					
ΔH^{0}_{298} (kJ/mo	le)				
Compound	Calculated, elements as reference	Calculated, oxides (stable at room- temperature) as reference	Experimental, oxides (stable at room- temperature) as reference		
Sr ₅ Al ₂ O ₈	-4730.769	-94.319			
LT- Sr ₄ Al ₂ O ₇	-4135.526	-91.226	-92.717 ± 5.439 [Brisi and Abbattista, '60]		
HT- Sr ₄ Al ₂ O ₇	$\Delta H_{trans}^{*} = 8.000 \text{ (at } 1450 \text{ °C)}$		$\Delta H_{trans}^{*} (exp) = 11.255 [Brisi and Abbattista, '60]$		
Sr ₃ Al ₂ O ₆	-3545.865	-93.715	-97.738 ± 4.184 [Brisi and Abbattista, '60] -87.905 [Massazza and Cannas '61]		
LT-SrAl ₂ O ₄	-2349.245	-81.395	-79.203 ± 2.929 [Brisi and Abbattista, '60]		
$HT-SrAl_2O_4$	$\Delta H_{trans}^{*} = 2.000 \text{ (at 659 °C)}$				
$SrAl_4O_7$	-4035.000	-91.450			
$Sr_4Al_{14}O_{25}$	-14446.205	-347.705			
SrAl ₁₂ O ₁₉	-10755.475	-109.125			
$S_{298}^{0} \Delta S_{298}^{0}$ and C_{p} (J/mol/K)					
Compound	S_{298}^{0} ΔS_{298}^{0} , (calculated) oxide (stable at room temperature) as reference	s - C _p			
$Sr_5Al_2O_8$	363.000 44.280	$C_p = \overline{4 C_p (SrC)}$	$(HT-SrAl_2O_4)$		
LT- Sr ₄ Al ₂ O ₇	308.000 42.860	$C_p = 3 C_p (SrC)$	$\mathbf{O}) + \mathbf{C}_{\mathrm{p}} \left(\mathrm{HT}\text{-}\mathbf{SrAl}_{2}\mathbf{O}_{4}\right)$		

HT- Sr ₄ Al ₂ O ₇		$\Delta S_{\text{trans}}^{**} = 4.643$ (at 1450 °C)	$C_{p} = 3 C_{p} (SrO) + C_{p} (HT-SrAl_{2}O_{4})$
Sr ₃ Al ₂ O ₆	249.000	37.440	$C_{p} = 2 C_{p} (SrO) + C_{p} (HT-SrAl_{2}O_{4})$
LT-SrAl ₂ O ₄	124.000	19.600	158 + 0.031 T –3813450 T^{-2} –8E–9 T^3 ; (298 < $T <$ 2400)
HT-SrAl ₂ O ₄		$\Delta S_{\text{trans}}^{**} = 2.146$ (at 659 °C)	157 + 0.026 T - 3613450 T ⁻² - 2E-9 T ³ ; (298 < T < 3000)
$SrAl_4O_7$	181.000	25.780	$C_p = C_p (HT-SrAl_2O_4) + C_p (Al_2O_3 (Corundum))$
Sr ₄ Al ₁₄ O ₂₅	676.000	105.940	$C_{p} = 4 C_{p} (SrO) + 7 C_{p} (Al_{2}O_{3})$
SrAl ₁₂ O ₁₉	388.000	29.500	$C_{p} = C_{p} (HT-SrAl_{2}O_{4}) + 5 C_{p} (Al_{2}O_{3} (Corundum))$

* Enthalpy of transformation from the low-temperature to the high-temperature $SrAl_2O_4$ (kJ/Mole). ** Entropy of transformation from the low-temperature to the high-temperature $SrAl_2O_4$ (J/mol/K).



Fig. 2.6.1 Optimized phase diagram of the SrO-Al₂O₃ system.



Fig. 2.6.2 Heat increments $(H_{(T)} - H_{(298)})$ per mole of the SrAl₂O₄ phase.



Fig. 2.6.3 Average heat capacity $[(H_{(T)} - H_{(298)})/(T - 298)]$ per mole of the SrAl₂O₄ phase.



Fig. 2.6.4 Optimized standard enthalpy of formation (ΔH^{0}_{298}) in the SrO-Al₂O₃ system.



Fig. 2.6.5 Optimized Gibbs energy change in the reaction $2SrO + SrAl_2O_4 = Sr_3Al_2O_6$.

2.7 The BaO-Al₂O₃ system

The optimized phase diagram of the system is shown in Fig. 2.7.1 and optimized thermodynamic parameters are presented in Table 2.7.1. The optimized MQM parameters (and the coordination numbers) for the liquid phase are presented in Table 2.7.1. For these parameters, the same notations were used as used by Pelton and coworkers [Pelton, et al. (2000)]. Ye, Zhuang, Deng, Yuan, and Qiao (2006) optimized this system treating the liquid phase by a two-sublattice model for ionic solutions. In this work, however, the thermodynamic data by Bokeriya, Tsagareishvili, and Gvelesiani (1970a) and mass spectrometric data of Hilpert, Beske, and Naoumidis (1975) and Hilpert, Naoumidis, and Wolff (1975) were not taken into account.

In the BaO-Al₂O₃-SiO₂ system, to obtain the optimal fit of the available data, an additional component in the form of BaAl₂ associate was added to the liquid phase, i.e. BaAl₂O₄ was considered a separate component in the binary BaO-Al₂O₃ system (along with BaO and Al₂O₃). The optimized Gibbs energy of this component (BaAl₂ associate) and its coordination number in the liquid phase is presented in Table 2.7.1. Practically, these BaAl₂ associates are not stable in the binary BaO-Al₂O₃ system. They are stable in the ternary BaO-Al₂O₃-SiO₂ system, especially in the SiO₂-rich corner. In the BaO-Al₂O₃ system, at 2000 °C and at $X_{Al2O3} = 0.5$, the mole fraction of these associates is only 4.2 x 10⁻⁴ mole.

Purt (1960), by thermal analysis and XRD, and Toropov and Galakhov (1952), by quenching techniques, studied the system and reported $3BaO.Al_2O_3$ (B₃A), $BaO.Al_2O_3$ (BA) and $BaO.6Al_2O_3$ (BA₆) as stable compounds. The difference in the calculated phase diagram (Fig.

2.7.1) from these findings is discussed below. F. P. Glasser (1974) reported a polymorphic transformation of B₃A phase at 450 °C. The enthalpy of transformation could not be found in the literature. In the present work, this transformation is shown in Fig. 2.7.1 on the assumption that the thermodynamic properties for the high-temperature form are identical to the low-temperature form. Bokeriya, et al. (1970a) by thermal analysis, reported a polymorphic transformation of BA at 327 °C. Recently, Rodehorst, et al. (2003) summarized the reported data on this transformation and studied the transformation by infrared powder absorption spectroscopy. They reported this transformation as about 127 °C. Mateika and Laudan (1979) studied the BA₆-Al₂O₃ region of the system by microscopic visual observation of the melting points and identification of the phases by XRD. There are various investigations [Haberey, Oehlschlegel, and Sahl (1977);S. Kimura, Bannai, and Shindo (1982); Iyi, Takekawa, Bando, and Kimura (1983); Iyi, Inoue, Takekawa, and Kimura (1984); Iyi, Inoue, Takekawa, and Kimura (1985)] which report that, in the aluminumrich region, instead of a single BaA_6 phase there are two distinct phases on either side of the stoichiometric composition BaA₆, i.e. one with more Al₂O₃ and other deficient in it (called here as Al₂O₃-rich and Al₂O₃-deficinet phases). The stoichiometries of these compounds reported in these references differ slightly. Stevels (1978) and Mateika and Laudan (1979) reported that there is one phase but with a range of solid solubility. Gobbels, Kimura, and Woermann (1998) while studying the BaO-MgO-Al₂O₃ system showed two distinct phases in their phase diagrams with chemical formulae Ba_{1.21}Al₁₁O_{17.71} and Ba_{0.75}Al₁₁O_{17.25}. Iyi, et al. (1983) reported hexagonal structure for the Al₂O₃-rich phase with space group P6₃/mmc and also a hexagonal structure for the Al₂O₃-deficient phase but different space group $P\overline{6}$. The SrA₆ (SrAl₁₂O₁₉) and CA₆ (CaAl₁₂O₁₉) phases are also reported [K. Kimura, Ohgaki, Tanaka, Morikawa, and Marumo (1990); Kang, Park, Kim, and Choi (2009); Utsunomiya, Tanaka, Morikawa, Marumo, and Kojima (1988)] to have hexagonal structure with the space group P6₃/mmc. Kadyrova and coworkers [Kadyrova and Daminova (1997; Kadyrova, Syrazhiddinov, and Tuganova (1996)] by quenching and XRD reported the BA₆ as the only stable phase in this region while studying the BA₆-CA₆ and BA₆-SA₆ sections. They reported complete solubility among the BA₆-CA₆ and BA₆-SA₆ phases. In the present work instead of considering an Al₂O₃-rich phase, close to the BA₆ composition, as stable, stoichiometric BA₆ phase was considered stable as it helped in fitting the higher-order phase diagram data of Kadyrova and coworkers. The Al₂O₃-deficient compound was taking into account in the present work as stoichiometric Ba₁₁Al₁₀₀O₁₆₁. This stoichiometry corresponds to the chemical formula Ba_{1.21}Al₁₁O_{17.71} for this compound as reported by Gobbels, et al. (1998) in their phase diagrams for the BaO-MgO-Al₂O₃ systems. It must be noted that this stoichiometry is tentative and more experimental work is required to correctly establish it.

Pietro Appendino (1971) by XRD studied the most basic region, BaO-B₃A, of the phase diagram and reported five compounds, 4BaO.Al₂O₃ (B₄A) stable above 940°, 5BaO.Al₂O₃ (B₅A) stable below 940°, 7BaO.Al₂O₃ (B₇A) stable below 1050°, 8BaO.Al₂O₃ (B₈A) stable above 1050°, and 10BaO.Al₂O₃ (B₁₀A) stable below 1130°. Kovba, Lykova, Antipov, Paromova, and Rozanova (1987) by XRD also reported all these phases as stable. They also reported a congruent melting point of 1560 °C for the compound B₄A. In the present work also, all these phases were calculated as stable as shown in Fig. 2.7.1. The decomposition temperatures of these phases into other solid phases were calculated based upon the temperature ranges of stability reported by Pietro Appendino (1971). Much experimental work is, however, required to establish these data accurately. The present calculated congruent melting temperature for B₄A is 1575 °C. Hilpert, Beske, et al. (1975) and Hilpert, Naoumidis, et al. (1975) reported the equilibrium partial pressures of BaO gas, by mass spectrometry at different compositions over a range of temperatures which are compared with the present calculations in Figs. 2.7.2 to 2.7.4. The thermodynamic data for BaO gas were taken from JANAF thermochemical tables [Stull and Prophet (1985)]. Experimental data in Fig. 2.7.2 show no evidence for the appearance of the liquid phase until 1820 °C (no change in the slope of experimental points). However, if liquidus data of Purt (1960) and Toropov and Galakhov (1952) are respected then the liquid phase appears below this temperature. Also, Mateika and Laudan (1979) reported that the eutectic lies in this region at about 1860 °C. Hence, no liquid phase can lie below this temperature, which is consistent with the data of Hilpert, Naoumidis, et al. (1975). Moreover, seeing the inconsistency of the two sets of liquidus data, preference was given in the present work to fit the data of Mateika and Laudan (1979) and mass spectrometric data of Hilpert, Beske, et al. (1975) and Hilpert, Naoumidis, et al. (1975). The optimal fit of these data gives the melting temperature of the BA phase as 2285 °C. If the experimental melting temperatures for the BA phase in Fig. 2.7.1 were fitted, then it would cause the liquid phase to appear below 1820 °C which was inconsistent with the liquidus data of Mateika and Laudan (1979) and mass spectrometric data of Hilpert and coworkers. As preference was given to these liquidus and mass spectrometric data and there is no other experimental datum on the melting temperature of the BA phase, it was tentatively calculated (shown as dashed line in Fig. 2.7.1) as 2285 °C. Similarly, Hilpert, Beske, et al. (1975) reported partial pressures of BaO gas at the composition $1.1BaO + 0.9Al_2O_3$ (Fig. 2.7.3). The present calculations are consistent with these data at temperatures where only solid phases (B₃A and BA) are in equilibrium. However, at temperatures greater than 1580 °C, temperatures at which the liquid phase is in equilibrium with the BA phase, reported partial pressures of BaO are inconsistent with the present calculations (Fig. 2.7.3). Hilpert, Beske, et al. (1975) acknowledged the loss of BaO due to vaporization at this composition and at temperature greater than 1580 °C. It must be noted that the experimental partial pressures in Fig. 2.7.3 at temperature greater than 1580 °C are identical to the one reported for the composition 0.9BaO + $1.1Al_2O_3$. Possibly, because of excessive vaporization of BaO, Hilpert, Beske, et al. (1975) could not keep the starting composition of $1.1BaO + 0.9Al_2O_3$ fixed which led them to measure the decreased partial pressure of BaO. The drastic change in the experimental vapor pressure of BaO (at temperatures greater than 1580 °C) due to melting of B₃A and appearance of liquid phase is not possible. And, it can be said that more work is required to corroborate these data. Hilpert, Beske, et al. (1975) reported partial pressure of BaO gas for the composition $1BaO + 6.4 Al_2O_3$ which are reasonably well fitted in Fig. 2.7.4.

Peppler and Newman (1951) by solution calorimetry determined the standard enthalpy of formation (ΔH^{0}_{298}) for the BA and B₃A phases. These data were used as enthalpy of formation for these compounds as shown in Table 2.7.1. Bokeriya, et al. (1970a) performed calorimetric measurements to determine heat contents (H_T – H₂₉₈) for the BA phase. These data are compared with the present calculations, in two difference scales, in Figs. 2.7.5 and 2.7.6. The temperature and enthalpy of transformation from low-temperature to high-temperature BA was obtained by fitting the data shown in Fig. 2.7.6 as were heat capacity (C_p) values for these phases in Table 2.7.1. The optimized heat capacity for BA was found to be close to the heat capacity obtained from adding the heat capacities of constituent oxides (C_p (BA) = Cp (BaO, solid) + C_p (Al₂O₃, corrundum). The optimized standard entropy (S^{0}_{298}) and entropy of formation with oxides as

reference standards (ΔS^{0}_{298}) are presented in Table 2.7.1. The data of Hilpert, Beske, et al. (1975) and Hilpert, Naoumidis, et al. (1975) were used to optimize the entropies of the BA, B₃A and BA₆ phases. The ΔS^{0}_{298} values of other phases are always less than 8 J/(atom of metal) which is quite reasonable.

No data on the mutual solubility among the BaO and Al_2O_3 phases could be found in the literature. Moreover, their different crystal structures and the very large difference in the ionic radii of Ba and Al (Ba = 149 pm and Al = 67.5 pm, [www.webelements.com (2012)]) also mitigate against any appreciable mutual solubility among them. Also, no data on the solid solubility in the solid phases appearing in the BaO-Al₂O₃ system were found. They were modeled as stoichiometric phases.

The enthalpy of mixing and entropy of mixing at 3000 °C in the liquid phase in the alkaline-earth oxide-alumina systems are compared in Figs. 2.7.7 and 2.7.8 respectively. The enthalpy of mixing follows the trend that it is expected to be more negative in the series CaO to BaO.

Liquid phase (Quasiche	emical model param	ieters)			
$Z_{Alal}^{Al} = 2.06616563;$	$Z_{BaBa}^{Ba} = 1.3774$	4375; Z_{BaA}^{BaA}	$\frac{l_2}{l_2 BaAl_2} = 5.5097750$	00; $Z_{BaAl}^{Ba} = 2.75488750; \qquad Z_{AlBa}^{Al} =$	
1.37744375					
$\Delta g_{BaAl} = (-150624 + 1)$	6.736 T) – 112968 Z	X _{BaBa}			
$g^{\theta}_{BaAl2} = g^{\theta}(BaO,Liq.)$	$+ g^{0}(Al_{2}O_{3},Liq.) - 1$	38072 + 2.092	Т		
Solid Phases					
ΔH^{0}_{298} (kJ/mole)					
Compound	Calculated from e	lements	Calculated oxides (stable at room- temperature) as reference	Experimental, (calculated) oxides (stable at room-temperature) as reference	
$Ba_{10}Al_2O_{13}$	-7350.532		-193.792		
$Ba_8Al_2O_{11}$	-6180.905		-120.373		
$Ba_7Al_2O_{10}$	-5705.000		-192.572		
$Ba_4Al_2O_7$	-4036.020		-167.904		
$Ba_5Al_2O_8$	-4608.012		-191.792		
$Ba_3Al_2O_6$	-3504.317		-184.305	-184.305 [Peppler and Newman,	
LT-BaAl ₂ O ₄	-2324.178		-100.374	-100.374 [Peppler and Newman, '51]	
HT-BaAl ₂ O ₄	$\Delta H_{\text{trans}}^* = 1.400$ (at 327 °C)			1	
$BaA_{12}O_{19}$	-10732.000		-129.696		
Ba ₁₁ Al ₁₀₀ O ₁₆₁	-91201.047		-1386.903		
S_{298}^{0} , ΔS_{298}^{0} and C_p (J/mol/K)					
Compound	S ⁰ ₂₉₈	ΔS^{θ}_{298} oxides (stable at room- temperature) as reference	C _p		
Ba ₁₀ Al ₂ O ₁₃	777.600	6.091	C _p (HT-BaAl	$P_{2}O_{4}) + 9 C_{p} (BaO)$	
$Ba_8Al_2O_{11}$	693.000	65.628	C _p (HT-BaAl	$I_2O_4) + 7 C_p (BaO)$	
$Ba_7Al_2O_{10}$	562.100	6.798	C _p (HT-BaAl	$(2O_4) + 6 C_p (BaO)$	
$Ba_4Al_2O_7$	369.000	29.905	C _p (HT-BaAl	$_{2}O_{4}) + 3 C_{p} (BaO)$	
$Ba_5Al_2O_8$	418.200	7.036	C _p (HT-BaAl	$_{2}O_{4}) + 4 C_{p} (BaO)$	
Ba ₃ Al ₂ O ₆	280.000	12.974	C _p (HT-BaAl	$_{2}O_{4}) + 2 C_{p} (BaO)$	
LT-BaAl ₂ O ₄	158.000	35.112	170.5 + 0.022 610 K)	2 T –5613450 T^{-2} (298.15 < T <	

Table 2.7.1 Optimized thermodynamic parameters (in Joules/mol) for the BaO-Al₂O₃ system.

HT-BaAl ₂ O ₄	$\Delta S_{\text{trans}}^{**} = 2.500$ (at 327 °C)		138 + 0.032 T ($610 < T < 2500$ K)
$BaA_{12}O_{19}$	400.200	23.211	$C_p (HT-BaAl_2O_4) + 5 C_p (Al_2O_3, Corrundum)$
$Ba_{11}Al_{100}O_{161}$	3595.060	261.301	11 C_p (HT-BaAl ₂ O ₄) + 39 C_p (Al ₂ O ₃ , Corrundum)

^{*} Enthalpy of transformation from the low-temperature to the high-temperature $BaAl_2O_4$ (kJ/Mole). ^{**} Entropy of transformation from the low-temperature to the high-temperature $BaAl_2O_4$ (J/mol/K).



Fig. 2.7.1 Optimized phase diagram of the BaO-Al₂O₃ system.



Fig. 2.7.2 Equilibrium partial pressure of BaO (g) at the composition $0.9 \text{ BaO} + 1.1 \text{ Al}_2\text{O}_3$.



Fig. 2.7.3 Equilibrium partial pressure of BaO (g) at the composition $1.1 \text{ BaO} + 0.9 \text{ Al}_2\text{O}_3$.



Fig. 2.7.4 Equilibrium partial pressure of BaO (g) at the composition $1BaO + 6.4 Al_2O_3$.



Fig. 2.7.5 Enthalpy increments $(H_{(T)} - H_{(298)})$ for per mole of the BaAl₂O₄ phase.



Fig. 2.7.6 Average heat capacity $[(H_{(T)} - H_{(298)})/(T - 298)]$ of the BaAl₂O₄ phase (per mole).



Fig. 2.7.7 Enthalpy of mixing at 2000 °C in the liquid phase in the alkaline-earth oxide-alumina systems.



Fig. 2.7.8 Entropy of mixing at 2000 °C in the liquid phase in the alkaline-earth oxide-alumina systems.

2.8 The BaO-B₂O₃ system

The optimized phase diagram of the system is shown in Fig. 2.8.1 and optimized parameters are presented in Table 2.8.1. The optimized MQM parameters (and the coordination numbers) for the liquid phase are presented in Table 2.8.1. For these parameters, the same notations were used as used by Pelton and coworkers [Pelton, et al. (2000)]. Yu, Chen, and Jin (1999) optimized the system, modeling the liquid phase by two-sublattice ionic solution model.

Guertler (1904) studied the system by cooling curve analysis and reported $3BaO.B_2O_3$ (Ba₃B), 2BaO.B₂O₃ (Ba₂B), and BaO.B₂O₃ (BaB) as equilibrium phases. Carli (1927) also used the same technique to report BaO.4B₂O₃ (BaB₄), BaO.3B₂O₃ (BaB₃), and BaO.2B₂O₃ (BaB₂) as equilibrium phases. Later, Levin and McMurdie (1949), by quenching techniques, reported the phases shown in Fig. 2.8.1. However, they did not find the Ba_2B and BaB_3 phases. Hamilton, Cleek, and Grauer (1958), while studying the ternary system $BaO-B_2O_3-SiO_2$ by thermal analysis, reported a few melting temperatures in the binary system. Meshalkin and Kaplun (2005) by thermal analysis studied the system from 32 to 67 mol% B₂O₃. They reported the presence of the phase Ba₂B with a peritectic melting point and bounded low-temperature stability. They also reported the presence of a metastable phase 2BaO.3B₂O₃. Huebner (1969) by XRD reported $2BaO.5B_2O_3$ (Ba₂B₅), Ba₂B and $4BaO.B_2O_3$ (Ba₄B) as stable phases. In the present work, the Ba₂B is included as an equilibrium phase as it was also reported by Guertler (1904) and Meshalkin and Kaplun (2005). Meshalkin and Kaplun (2005) reported the stability range for the phase Ba₂B as 850-1125 °C. The temperature for low-temperature decomposition was tentative. In the present calculations, for an optimal fit of the available liquidus data, the stability of this phase was calculated as shown in Fig. 2.8.1. Hovhannisyan (2006) studied the system by XRD and DTA and reported all the phases shown in Fig. 2.8.1 as stable. As the Ba_2B_5 phase was reported stable by both Hovhannisyan (2006) and Huebner (1969), this phase was considered as stable in the present calculations also. Wang, Huang, and Liang (1984) while studying the SrO-BaO-B₂O₃ ternary system reported Ba₄B as a stable phase. In their phase diagrams, this phase was found to be stable till 920 °C. No other data on this phase could be found in the literature. In the present calculations, this phase was tentatively calculated to decompose into BaO and Ba₃B phases at around 1000 °C. The BaB₃ phase reported by Carli (1927) was not considered stable, and further experiments are required to confirm its presence. Several authors [Levin and McMurdie (1949);Ohta, Morinaga, and Yanagase (1982);V. B. M. Hageman and Oonk (1979);V. B. M. Hageman and Oonk (1987);Levin and Cleek (1958);Clemens, Yoshiyagawa, and Tomozawa (1981);Crichton and Tomozawa (1997)] studied the liquid immiscibility in the system (Fig. 2.8.1). The boundary of the miscibility gap determined by Ohta, et al. (1982) using a handmade apparatus, for the hot-thermocouple method, and by Hageman and Oonk [V. B. M. Hageman and Oonk (1979) and V. B. M. Hageman and Oonk (1987)], using equilibration and quenching followed by refractive index measurements, were found to agree closely.

Huebner (1969) by XRD, Liang and Huang (1982) by XRD and DTA, and Kouta, Kuwano, Suda, Ishizawa, and Marumo (1994) by high-temperature XRD reported a phase transformation of the BaB phase at about 925 °C. In the present work, this transformation was neglected because the enthalpy of the transformation could not be found in the literature. A single phase BaB₂O₄, stable up to room temperature, was considered. For the sake of presentation, this transformation is shown in Fig. 2.8.1 by assuming the thermodynamic properties of the high-temperature phase to be the same as the low-temperature phase.

Cordfunke, Konings, Van der Laan, and Ouweltjes (1993) and Z.-H. Liu, Wang, and Huang (2007) using solution calorimetry reported ΔH^{0}_{298} for the phases Ba₃B and BaB respectively. The results of Cordfunke, et al. (1993) for ΔH^{0}_{298} (from elements) of Ba₃B was –2344.2 kJ/mole. ΔH^{0}_{298} of Ba₃B calculated with reference to oxides (i.e. BaO and B₂O₃), is a positive quantity, 572.048 kJ/mole. Such a positive value is highly unrealistic unless this compound is not stable at room temperature. It is worth mentioning here that for this determination Cordfunke, et al. (1993) required ΔH^{0}_{298} for BaCl₂ as the solution medium taken in the calorimetry was HCl(aq). The value used by them as –1604.2 kJ/mole from the literature is in gross error with the value from the FTSALT database which is –2575.7 kJ/mole. Thus in the present work, the ΔH^{0}_{298} of Ba₃B was recalculated by using ΔH^{0}_{298} for BaCl₂ from the FTSALT database and all the other required data from Cordfunke, et al. (1993). The value obtained was –3359.9 kJ/mole. This was presented in Fig. 2.8.2 with the label corrected value.

Asano and Kou [Asano and Kou (1989); Asano and Kou (1990)] by the massspectrometric/Kudsen effusion method measured the partial pressure of B_2O_3 gas over the BaB liquid, BaB₂ liquid and Ba₃B solid phases. In the present calculations the data for the B₂O₃ gas were taken from JANAF Thermochemical Tables (1985). The present calculations are consistent with these measurements for the BaB and BaB₂ liquids as shown in Figs. 2.8.3 and 2.8.4. However, the present work does not fit these data for the Ba₃B solid phase (Fig. 2.8.5). It was observed that these data for the Ba₃B phase can be fitted well with a H^{0}_{298} value which is much less negative than the presently calculated or with a very negative ΔS^{0}_{298} value. Such a value of H^{0}_{298} for the Ba₃B phase, and consequently for the BaB phase in an optimal fit, will exacerbate the fit in Fig. 2.8.2. A very negative ΔS^{0}_{298} is also unreasonable. Hence the data by Asano and Kou for the solid Ba₃B phase were given less weight.

The enthalpy increments ($H_T - H_{25}$) for the phase Ba₃B were measured by Cordfunke, et al. (1993) using drop calorimetry, and are well reproduced in Fig 2.8.6. Stewart and Rindone (1963) by high-temperature calorimetry reported enthalpy increments ($H_T - H_{298}$) for solid and liquid BaB₂ (Fig. 2.8.7) and BaB₄ (Fig. 2.8.8) phases. These enthalpy increments were used to obtain the heat capacities (C_p) for the solid phases presented in Table 2.8.1. In the present calculations, the heat capacity of the liquid phase was calculated by adding the heat capacities of the constituent oxides. Hence, there is disagreement with the data in the liquid region as shown in Figs. 2.8.7 and 2.8.8. The data for the crystals are well reproduced.

Muller and Demirok (1989) measured the integral enthalpy of mixing by dropping samples containing an intimate mixture of crystalline BaO and amorphous B_2O_3 at room temperature into a calorimeter maintained at 1278 °C. Exact fitting of these enthalpy data gives a larger miscibility gap than calculated in Fig. 2.8.1, which is in disagreement with the available different sets of data. Hence, the enthalpy of mixing was fitted as shown in Fig. 2.8.9. The optimized standard entropy (S_{298}^0) and entropy of formation with oxides as reference standards (ΔS_{298}^0) are presented in Table 2.8.1. The ΔS_{298}^0 values are always less than 12 J/(atom of metal), which is reasonable.

No data on the mutual solubility among the BaO and B_2O_3 phases could be found in the literature. Moreover, their different crystal structures and the very large difference in the ionic radii of Ba and B (Ba = 149 pm and B = 25 pm, [www.webelements.com (2012)]) also mitigate against any appreciable mutual solubility among them. Also, no data on the solid solubility in the solid phases appearing in the BaO-Al₂O₃ system were found. They were modeled as stoichiometric phases.

The enthalpy of mixing, at 2500 °C, and the entropy of mixing, at 1500 °C, in the liquid phase in the BaO-B₂O₃ system is compared with the other alkaline-earth oxide-boron oxide systems in the next section (Figs. 2.9.6 and 2.9.7 respectively). The enthalpy of mixing follows the trend that it is expected to be more negative in the series CaO to BaO.

$Z_{BB}^{\scriptscriptstyle B} = 2.06616563; Z_{BaBa}^{\scriptscriptstyle Bd} = 1.37744375$					
$\Delta g_{BaB} = -209200 - 2000$	121336 X _{BB}	$-41840 X_{BB}^{4} + (175)$	5728 – 48.116 T) 2	X_{BB}^{7}	
Solid Phases					
ΔH^{0}_{298} (kJ/mole)					
Compound	Calculated from elements		Calculated, oxides (stable at room- temperature) as reference	Experimental From elements ^(a)	
$Ba_4B_2O_7$	-3826.104		-361.752		
$Ba_3B_2O_6$	-3276.000		-359.752	-3359.961 ± 5.8 [Cordfunke et al., '93] ^(b)	
$Ba_2B_2O_5$	-2576.500		-208.356		
BaB_2O_4	-2004.300		-184.260	-2020.300 ± 1.7 [Liu et al., '07]	
$Ba_{2}B_{10}O_{17}$	-7810.012		-354.124		
BaB_4O_7	-3270.438		-178.462	-3237.899 ^(c)	
Compound	S ⁰ ₂₉₈	ΔS^{0}_{298} calculated, oxides (stable at room- temperature) as reference	ΔS^{0}_{298} calculated, compounds used calculate heat ca as reference	C_p (298.15 < T < 2000 K) d to apacities	
Ba ₄ B ₂ O ₇	380.500	38.274	-1.569	$C_p(BaO) + C_p(Ba_3B_2O_6)$	
Ba ₃ B ₂ O ₆	310.000	39.843		$257 + 0.028 \ T - 5500000 \ T^{-2}$	
$Ba_2B_2O_5$	280.000	81.912	64.431	$C_p(BaO) + C_p(BaO.B_2O_3)$	
BaB_2O_4	143.500	17.481	-9.0345	$0.5 (C_p(BaO) + C_p(BaO.2B_2O_3))$	
$Ba_2B_{10}O_{17}$	538.550	124.662	18.600	$C_p(B_2O_3) + 2 C_p(BaO.2B_2O_3)$	
BaB_4O_7	233.000	53.031		$223 + 0.048 \ T - 6000000 \ T^{-2}$	
BaB ₈ O ₁₃	390.000	102.131		$400 + 0.102 T - 14000000 T^{-2}$	

Table 2.8.1 Optimized thermodynamic parameters (in Joules/mol) for the BaO-B₂O₃ system. Liquid phase (Quasichemical model parameters)

Ra

^(a) In all these references the enthalpy of formation was reported with reference to elements. ^(b) Corrected value (see text).

^(c) Calculated from the enthalpy of mixing for the liquid phase (Muller and Demirok (1989)), enthalpy of melting and heat capacity for the respective solid phases (Stewart and Rindone (1963).



Fig. 2.8.1 Optimized phase diagram of the BaO-B₂O₃ system.



Fig. 2.8.2 Optimized standard enthalpy of formation of intermediate compounds in the BaO-B₂O₃ system.


Fig. 2.8.3 Optimized partial pressure of B₂O₃ at the BaB₂O₄ composition.



Fig. 2.8.4 Optimized partial pressure of B_2O_3 at the BaB_4O_7 composition.



Fig. 2.8.5 Optimized partial pressure of B_2O_3 at the $Ba_3B_2O_6$ composition.



Fig. 2.8.6 Optimized enthalpy increments $(H_{(T)} - H_{(298)})$ for the Ba₃B₂O₆ phase.

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Fig. 2.8.7 Optimized enthalpy increments $(H_{(T)} - H_{(298)})$ (ref. state crystals) for the BaB₄O₇ phase.



Fig 2.8.8 Optimized enthalpy increments $(H_{(T)} - H_{(298)})$ (ref. state crystals) for the BaB₈O₁₃ phase.



Fig. 2.8.9 Optimized enthalpy of mixing (standard states: solid BaO and liquid B_2O_3) in the liquid phase.

2.9 The SrO- B_2O_3 system

The optimized phase diagram of the system is shown in Fig. 2.9.1 and optimized thermodynamic parameters are presented in Table 2.9.1. The optimized MQM parameters (and the coordination numbers) for the liquid phase are presented in Table 2.9.1. For these parameters, the same notations were used as used by Pelton and coworkers [Pelton, et al. (2000)]. Pan, Wang, and Jin (2004) optimized the system using a two-sublattice ionic solution model for the liquid phase.

Guertler (1904) studied the system by cooling curves and reported SrO.2B₂O₃ (SB₂), SrO.B₂O₃ (SB) and 2SrO.B₂O₃ (S₂B) as equilibrium phases. Witzmann and Beulich (1964) and Witzmann and Herzog (1964) by DTA measured the solid-liquid phase equilibria in the system. They reported these solid phases, except SrO.3B₂O₃ (SB₃), shown in Fig. 2.9.1 as stable. Hovhannisyan (2006) studied the system by XRD and DTA and reported all the phases shown in Fig 2.9.1 as stable. Chenot (1967) by XRD and DTA reported the presence of the SrO.3B₂O₃ phase and reported its peritectic melting at about 890 °C. Wang, et al. (1984) while studying the BaB-SB section by thermal analysis reported melting point of the SB phase. Ohta, et al. (1982) by a handmade apparatus, for the hot-thermocouple method, V. B. M. Hageman and Oonk (1987) (equilibration and quenching followed by refractive index measurements), Konishi et al. (2000) (in-situ observation of phase separation and microscopic analyses by EPMA) and Crichton and Tomozawa (1997) (equilibration and quenching) measured the immiscibility in the system. Their data are shown in Fig. 2.9.1.

Z.-H. Liu and Huang (2006) by solution calorimetry determined the standard enthalpy of formation (ΔH^{0}_{298}) for the SB phase. This datum was used as enthalpy of formation for this compound as shown in Table 2.9.1. Asano and Kou (1988) by Knudsen-effusion mass spectrometry reported B_2O_3 vapor pressure over SB solid and liquid phases. These data are compared with the present calculations in Fig. 2.9.2. In the present calculations, the data for pure B₂O₃ gas were taken from JANAF Thermochemical Tables (1985). Stewart and Rindone (1963) by high-temperature calorimetry measured the enthalpy increments (H_T-H₂₉₈) for the liquid and solid SB₂ phases. The increments for the solid phase in Fig. 2.9.3 were used to obtain the heat capacity (C_p) for the SB₂ phase presented in Table 2.9.1. The optimized heat capacity is close to the one obtained by adding the heat capacities of the constituent oxides. The enthalpy increments for liquid (and glass) SB_2 phases are plotted in Fig. 2.9.4. It should be noted that, as in the BaO-B₂O₃ system, the same authors [Stewart and Rindone (1963)] did not report for this phase the heat of devitrification (H_{Crystal}-H_{Glass}) at 25 °C. Thus, the two sets of data could not be plotted on same scale with reference to crystals at room temperature as in the BaO- B_2O_3 system. Nagel, Eagan, and Bergeron (1970) measured the enthalpy of fusion by DTA of the compound SB_2 . Their measured value is 139.746 kJ/mole and the present calculate value is 142.170kJ/mole. For the other solid phases in the SrO-B₂O₃ system, the heat capacity was calculated by adding the heat capacities of constituent oxides as shown in Table 2.9.1. No other thermodynamic data on the system could be found in the literature. The optimized standard entropy (S^{0}_{298}) and entropy of formation with oxides as reference standards (ΔS^{0}_{298}) are presented in Table 2.9.1. The ΔS^{0}_{298} values are always less than 9 J/(atom of metal), which is reasonable.

No data on the mutual solubility among the SrO and B_2O_3 phases could be found in the literature. Moreover, their different crystal structures and the very large difference in the ionic radii of Sr and B (Sr = 132 pm and B = 25 pm, [www.webelements.com (2012)]) also mitigate against any appreciable mutual solubility among them. Also, no data on the solid solubility in the solid phases appearing in the SrO- B_2O_3 system were found. They were modeled as stoichiometric phases.

The standard enthalpies of formation for intermediate compounds, enthalpies of mixing (at 2500 °C) and entropies of mixing (at 1500 °C) in the liquid phase in the alkaline-earth oxide-boron trioxide systems are compared in Figs. 2.9.5 to 2.9.7.

Liquid phase (Quasichemical model parameters)					
$Z_{BB}^{B} = 2.06616563; Z_{SrSr}^{Sr} = 1.37744375$					
$\Delta g_{SrB} = -188280 - 10878$	$4 X_{BB} + (154808 - 4)$	6.024 <i>T</i>) X_{BB}^{8}			
Solid Phases					
ΔH^{0}_{298} (kJ/mole)					
Compound	Calculated from elements		Calculated, oxides (stable at room- temperature) as reference	Experimental from elements	
$Sr_3B_2O_6$	-3350.000		-301.614		
$Sr_2B_2O_5$	-2715.000		-258.764		
SrB_2O_4	-2038.400		-174.314	-2038.400 ± 1.700 [Liu and Huang ('06)] ^(a)	
SrB_4O_7	-3310.000		-173.978	Trueng (00)]	
$\mathrm{SrB}_6\mathrm{O}_{10}$	-4585.951		-177.993		
S_{298}^{0} , ΔS_{298}^{0} and C_{p} (J/mol/K)					
Compound	S ⁰ ₂₉₈	ΔS^0_{298} calculated, oxides (stable at room- temperature) as reference	C _p		
$Sr_3B_2O_6$	230.000	15.310	$3 C_p(SrO) + C_p(B_2O_3)$		
$Sr_2B_2O_5$	165.000	3.890	$2 C_p(SrO) + C_p(B_2O_3)$		
SrB ₂ O ₄	107.550	0.020	C _p ($SrO) + C_p(B_2O_3)$	
SrB_4O_7	193.000	31.520	195	$5 + 0.1 T - 7000000 T^2$	
SrB ₆ O ₁₀ ^(a) In this ref. heat of formation was reported with reference to	258.000	42.570	C _p ($(SrO) + 3 C_p(B_2O_3)$	

Table 2.9.1. Optimized thermodynamic parameters (in Joules/mol) for the SrO- B_2O_3 system.

elements only.



Fig. 2.9.1 Optimized phase diagram of the SrO-B₂O₃ system.



Fig. 2.9.2 Optimized vapor pressure of the B₂O₃ over SrB₂O₄ composition.



Fig. 2.9.3 Optimized enthalpy increments in the SrB₄O₇ (standard state: crystals) phase.



Fig. 2.9.4 Optimized enthalpy increments in the SrB_4O_7 (standard state: liquid at 25 °C) liquid phase.



Fig. 2.9.5 Standard enthalpies of formation in alkaline-earth oxide-boron trioxide systems.



Fig. 2.9.6 Enthalpy of mixing at 2500 °C in alkaline-earth oxide-boron trioxide systems.



Fig. 2.9.7 Entropy of mixing in the liquid phase at 1500 °C in alkaline-earth oxide-boron trioxide systems.

3. THE TERNARY AND HIGHER-ORDER SYSTEMS

In the SiO₂-B₂O₃-Al₂O₃-CaO-MgO-BaO-SrO system there are 25 ternary systems which contain either BaO or SrO (or both):

1.BaO-SrO-SiO₂

 $2.CaO\text{-}SrO\text{-}SiO_2$

 $3.BaO\text{-}CaO\text{-}SiO_2$

4.SrO-MgO-SiO₂

5.BaO-MgO-SiO₂

6.CaO-SrO-Al₂O₃

 $7.BaO-CaO-Al_2O_3$

8.SrO-BaO-Al₂O₃

9.BaO-MgO-Al₂O₃

 $10.BaO\text{-}Al_2O_3\text{-}SiO_2$

 $11. SrO\text{-}Al_2O_3\text{-}SiO_2$

 $12.BaO\text{-}B_2O_3\text{-}SiO_2$

 $13.SrO\text{-}B_2O_3\text{-}SiO_2$

 $14.BaO\text{-}B_2O_3\text{-}Al_2O_3$

 $15. SrO\text{-}B_2O_3\text{-}Al_2O_3$

16.SrO-BaO-B₂O₃

17.BaO-CaO-B₂O₃

18.SrO-BaO-CaO

19.SrO-BaO-MgO

20.SrO-CaO-B₂O₃ 21.SrO-CaO-MgO 22.SrO-MgO-B₂O₃ 23.SrO-MgO-Al₂O₃ 24.BaO-CaO-MgO 25.BaO-MgO-B₂O₃

Out of these 25, for 17 ternary systems (1 to 17) ternary data were found in the literature. Assessment and optimization of these data is presented in this chapter. For rest of the eight systems (from 18 to 25) no ternary data were found in the literature. Some data were available for the higher-order (quaternary) systems. They are also included in this chapter.

3.1 The BaO-SrO-SiO₂ system

The Gibbs energy of the liquid phase in the ternary system was estimated from the corresponding binary sub-systems by treating SiO_2 as asymmetric component [Pelton and Chartrand (2001)]. No ternary interaction parameter was required to reproduce the available data.

The optimized phase diagram of the SrS-BS section is shown in Fig. 3.1.1 and optimized thermodynamic parameters are presented in Table 3.1.1. The SrS phase has the pseudowollastonite structure [Eskola (1922), Buckner and Roy (1960)], space group, C2/c [Yang and Prewitt (1999)], whereas BS is isotypic with BaGeO₃ (space group $P2_12_12_1$) [Grosse, Tillmanns, and Mineral (1974)]. As the two phases are of different structure and Winkle and Muan (1973) also reported the two terminal solid solutions as different phases, in the present

work they were modeled as different phases using single-sublattice simple substitutional models (i.e., (Sr,Ba)SiO₃ and (Ba,Sr)SiO₃). It should be noted that in Table 3.1.1 the Gibbs energies of unstable end-members and excess interaction parameters are presented. The Gibbs energy of stable end-members can be found in the tables in the corresponding binary system.

Fields, et al. (1972) measured the melting and solidus points in the SrS-BS section by DTA, and the points above 1500 °C by the oxy-acetylene torch method followed by visual observations. Winkle and Muan (1973) measured the phase diagram by quenching techniques followed by identification of phases by XRD and microscopic methods. They suggested the liquid (glass) observed by Fields, et al. (1972) at temperatures far below their liquidus data as metastable supercooled liquid. Later, Huntelaar and Cordfunke (1993) by DTA reported a phase diagram consistent with that of Winkle and Muan (1973).

The B₂S phase is reported [Catti, Gazzoni, and Ivaldi (1983), Pieper, et al. (1972), Hahn and Eysel (1970)] to have an orthorhombic structure, isostructural with α '-Ca₂SiO₄ (C₂S). Hahn and Eysel (1970) predicted the high-temperature polymorphic transformation into high-K₂SO₄ structure (isostructural with α -C₂S) for this phase in line with the structure of similar silicates and germanates. However, no experiments corroborating this prediction in the literature could be found. During experimental investigation on this section Fields, et al. (1972) did not note any α -polymorph for the B₂S and reported only α '- polymorph as stable. In the present work also, only α '- B₂S was considered stable. The Sr₂S phase contains both the α '- and α - polymorphs. Several authors [Fields, et al. (1972), Pieper, et al. (1972), Henning and Paeselt (1965a), O'Daniel and

Tscheischwili (1942), Paeselt and Henning (1968), Grebenshchikov and Shitova (1970)] reported complete solubility in the temperatures corresponding to stability of the α '-phase (orthorhombic) in the Sr₂S-B₂S section.

Fields, et al. (1972) by the oxygen-acetylene torch method reported phase diagram data for this section as shown in Fig. 3.1.2. The slope of the liquidus reported by them is dubious. Moreover, keeping in view the inconsistency of their data with other available data in Fig. 3.1.1, the data in Fig. 3.1.2 are questionable. Hence, further experimental work is required to establish the phase diagram for this section. The present calculated phase diagram for this section is shown in Fig. 3.1.3. In the present calculations, an ideal solution between the α '-polymorphs was assumed. The solubility of Ba in the α -Sr₂S was calculated tentatively. The lattice stability of B₂S in the α -phase was fixed from the B₂S-C₂S phase diagram.

Fields, et al. (1972) by quenching, XRD and optical microscopy reported phase relationships among solid phases (Fig. 3.1.4) in the temperature ranges 1220 to 1275 °C. This can be compared with the present calculated isothermal section at 1250 °C in Fig. 3.1.5 (the calculated phase relationships do not change in the range 1220 to 1275 °C). The phase relationships presented in Fig. 3.1.4 are erroneous because B_2S is shown in equilibrium with SrS which is not possible; tie lines between BS rich solid solution and orthosilicate solution intervene in the B_2S -SrS join, as shown in Fig. 3.1.5. No effort was made, in the absence of any conclusive data, to destabilize the liquid phase appearing at this temperature, contrary to data of Fields, et al. (1972). Fields, et al. (1972) also reported that the ternary compound BaSrSi₃O₈ (BSrS₃) melts at 1275 °C to Liquid + SrS phases and decomposes at 1220 °C into $BS_2 + SrS$ phases. The XRD data of this phase was also given. In the present calculations, the melting point of $BSrS_3$ at 1275 °C reported by Fields et al. is reproduced closely at 1272 °C. This compound melts into Liquid+Pseudowoll. and decomposes into $BS_2+SrS+SiO_2$ at 1184 °C. The present calculated liquidus (polythermal) projection for the BaO-SrO-SiO₂ system is presented in Fig. 3.1.6.

Pietro Appendino and Appendino Montorsi (1969) by quenching and XRD reported the phase B_2SrS_3 as stable on the BS-SrS section. However, other investigations [Fields, et al. (1972), Winkle and Muan (1973)] did not report this phase as stable. Therefore, in the present calculations this phase was neglected. They reported another ternary compound SrB_5S_{10} . Later investigation of Fields, et al. (1972) in the range 1220-1275 °C did not report this phase as stable. In the literature, no other experimental data on this phase could be found. More experimental work is required to prove the presence of this phase. Hence, SrB_5S_{10} was not considered stable in the present calculations.

The phases B_2S_3 and $BSrS_3$ have the same stoichiometry and some amount of mutual solubility among these solid phases can be expected because of similarity between Ba and Sr atoms. No experimental data on such solubility could be found in the literature. The similarity in the structure of these two phases will further enhance the possibility of mutual solid solubility. There are data on crystal structure [Hesse and Liebau (1980)] for the phase B_2S_3 ; however, no such data could be found for the BSrS₃ phase. In the absence of sufficient experimental data the mutual solubility among these phases was neglected. The B_3S and Sr_3S phases also have the same stoichiometry. Pietro Appendino and Appendino Montorsi (1969) by XRD reported about 20 mol% solubility of Sr at 1100 °C in the B₃S phase. However, they did not report Sr₃S as a stable compound. Fields, et al. (1972) presented references reporting Sr₃S to be isostructural with B₃S (tetragonal structure with space group P4/mmc). Tillmanns and Grosse (1978) also reported tetragonal structure for the B₃S phase. Therefore, in the present calculations also these phases were considered isostructural. An ideal solution was assumed between the Sr₃S and B₃S phases. This assumption reproduced the extent of solubility of Sr₃S in B₃S at 1100 °C (20 mol%) as reported by Pietro Appendino and Appendino Montorsi (1969).

Table 3.1.1 Optimized thermodynamic parameters, in Joules, (Gibbs energies of hypothetical end-members and excess interaction parameters) in the BaO-SrO-SiO₂ system.

BaSrSi ₃ O ₈
$ \Delta H^{0}_{298} = -4141085 \text{ J/mol} \qquad S^{0}_{298} = 271.000 \text{ J/mol/K} \qquad \Delta S^{0}_{298}^{(a)} = 20.971 \qquad \Delta S^{0}_{298}^{(b)} = 22.409 $ $ C_{p} = C_{p} (BaSiO_{3}) + C_{p} (SrSiO_{3}) + C_{p} (SiO_{2}(S2)) $
$T_{m}^{(c)} = 1272 \ ^{\circ}C$
Pseudowollastonite $G^{0}(BaSiO_{3}, Pseudowoll.) = G^{0}(BaSiO_{3}) + 15481$
BaSiO ₃ solid solution (ss)
G^{0} (SrSiO ₃ , ss) = G^{0} (SrSiO ₃) + 8368
α '-Sr ₂ SiO ₄ (α '-C ₂ S) ^(d)
$\mathbf{q}_{\mathrm{BaSr}}=0$
α -Sr ₂ SiO ₄ (α -C ₂ S) ^(d)
$G^{0}(Ba_{2}SiO_{4}, \alpha) = G^{0}(Ba_{2}SiO_{4}, \alpha') + 8786$
(Ba-Sr) ₃ SiO ₅ solid solution
$q_{BaSr} = 0$
Monoxide
$q_{BaSr}^{11} = 35698 - 8.870 T$; $q_{BaSr}^{21} = -3138$

*Here $G^{0}(A,x)$ refers to Gibb energy of A with x as reference state.

^(a) from oxides (stable at room-temperature) as reference ^(b) from compounds used to calculated heat capacity^(c) congruent melting^(d) these α - and α '- phases are same as the α -C₂S and α '-C₂S



Fig. 3.1.1 Optimized phase diagram for the SrSiO₃-BaSiO₃ system.



Fig. 3.1.2 The Ba₂SiO₄-Sr₂SiO₄ section as reported by Fields et al.



Fig. 3.1.3 Optimized phase diagram for the section Ba₂SiO₄-Sr₂SiO₄.



Fig. 3.1.4 Compatibility relations determined by Fields et al. in the temperature ranges 1220-1275 $^{\circ}$ C.



Fig. 3.1.5 Present calculated isothermal section at 1250 °C in the BaO-SrO-SiO₂ system.



Fig. 3.1.6 Present calculated liquidus (polythermal) projection for the BaO-SrO-SiO₂ system (isotherms were drawn at the interval of 100 $^{\circ}$ C).

3.2 The CaO-SrO-SiO₂ system

The Gibbs energy of the liquid phase in the ternary system was estimated from the corresponding binary sub-systems by treating SiO_2 as asymmetric component [Pelton and Chartrand (2001)]. Small ternary interaction parameters presented in Table 3.2.1 were used to reproduce the available data. This term was required to obtain an optimal fit in the CaSiO₃-SrSiO₃-BaSiO₃ system (Sec. 3.4).

As reported earlier (in the SrO-SiO₂ binary system) Ca₂SiO₄ and Sr₂SiO₄ have isostructural polymorphs (α - and α '-Ca₂SiO₄). Hence, solubility between corresponding phases in the two endmembers is expected. Several authors [Massazza (1955), Toropov and Konovalov (1943), Catti, et al. (1984), Paeselt and Henning (1968), Henning and Paeselt (1965b) reported complete solubility (in the temperature ranges corresponding to stability of orthorhombic (α '-Ca₂SiO₄) phase) in this section but no data establishing phase boundaries could be found in the literature. In the present calculations, ideal solutions were assumed for both the α ' and α phases.

The optimized phase diagram of the system is shown in Fig. 3.2.1 and optimized thermodynamic parameters are presented in Table 3.2.1. Eskola (1922) first studied the system by quenching techniques and optical microscopy and reported the liquidus and solidus points. Eskola (1922) reported only one form of SrSiO₃ isomorphous with pseudowollastonite-CaSiO₃. Winkle and Muan (1973) corroborated Eskola's data of complete solubility between the two metasilicates at 1300 °C. Moir, Gard, and Glasser (1975) reported that SrSiO₃ exists in two different polytypes (polytypism is a special case of polymorphism where compounds have nearly identical structure

and composition but differ only in their stacking sequence). The form which is thermodynamically less stable is isomorphous with pseudowollastonite. They also reported the presence of two-polytype regions between the compositions 50-60% CaSiO₃. However, they could not establish the exact phase boundary for this two-polytype region. In the present calculations, this polytypism was ignored and one form of SrSiO₃ isomorphous with pseudowollastonite-CaSiO₃, as also reported by Eskola (1922) and Winkle and Muan (1973), was considered. As these polytypes differ very slightly in their structure their Gibbs energies are supposed to be practically the same. Buckner and Roy (1960) reported subsolidus phase equilibria which are compared with the present calculations in Fig. 3.2.1. They also suggested the presence of a phase, below 700 °C, named μ -(Ca,Sr)SiO₃. More evidence and exact phase diagram data are required to model this phase. In the present work, any presence of such phase was neglected and the system was modeled as shown in Fig. 3.2.1. The solid solutions in Fig. 3.2.1 were modeled using single-sublattice simple substitutional model (i.e., (Ca,Sr)SiO₃ and (Sr,Ca)SiO₃).

Butt, Timashev, and Kaushanskii (1965) by XRD reported the solubility limit of Sr in the C₃S phase at 1450 °C as 0.035 mole. Boikova, Paramonova, and Domanskii (1972) by XRD reported the solubility limit of Ca in the Sr₃S phase at about 1600 °C phase as 0.11 mole. C₃S is known to exist in different crystal structures [Emanuelson, Solberg, Evju, and Hansen (2001)] but all of them are different from the crystal structure of Sr₃S phase (tetragonal structure, space group P4/mmc). These mutual solid solubilities in the C₃S-Sr₃S section was reproduced by treating both the end-members as different phases and modeling the solution using single-sublattice simple

substitutional model(i.e., $[Ca,Sr]_3SiO_5$, $[Sr,Ca]_3SiO_5$). The optimized parameters for these solutions are presented in Table 3.2.1.The present calculated liquidus (polythermal) projection for the CaO-SrO-SiO₂ system is presented in Fig. 3.2.2.

Table 3.2.1 Optimized thermodynamic parameters, in Joules, (Gibbs energies of hypothetical end-members and excess interaction parameters) in the CaO-SrO-SiO₂ system.

Pseudowollastonite
$q_{CaSr}^{11} = 5439$
Wollastonite
$G^{0}(SrSiO_{3}, Woll.) = G^{0}(SrSiO_{3}, Pseudowoll.) + 33472$
α '-Ca ₂ SiO ₄ (α '-C ₂ S)
$q_{CaSr} = 0$
α -Ca ₂ SiO ₄ (α -C ₂ S)
$q_{CaSr} = 0$
Sr ₃ S solid solution
$G^{0}(Ca_{3}SiO_{5}, Sr_{3}S) = G^{0}(Ca_{3}SiO_{5}) + 14226$
C ₃ S solid solution
$G^{0}(Sr_{3}SiO_{5}, C_{3}S) = G^{0}(Sr_{3}SiO_{5}) + 4184$
Liquid
$g_{CaSi(Sr)}^{001} = -4184$; $g_{SrSi(Ca)}^{001} = -4184$
Monoxide
$q_{CaSr}^{11} = 27748 - 6.359 T$; $q_{CaSr}^{12} = -1674$

**Here $G^{0}(A,x)$ refers to Gibb energy of A with x as reference state.



Fig. 3.2.1 Optimized phase diagram for the CaSiO₃-SrSiO₃ system.



Fig. 3.2.2 Present calculated liquidus (polythermal) projection of the CaO-SrO-SiO₂ system (isotherms were drawn at the interval of 100 °C).

3.3 The BaO-CaO-SiO₂ system

The Gibbs energy of the liquid phase in the ternary system was estimated from the corresponding binary sub-systems by treating SiO_2 as asymmetric component [Pelton and Chartrand (2001)]. The small ternary interaction parameters used for the liquid phase are presented in Table 3.3.1.

The optimized phase diagram of the system CS-BS is shown in Fig. 3.3.1 and optimized thermodynamic parameters are presented in Table 3.3.1. Eskola (1922) reported the presence of a stoichiometric compound BaCa₂Si₃O₉ from quenching techniques followed by optical microscopy. Later, Winkle and Muan (1973) by quenching techniques and XRD studied the section. They reported the presence of terminal solid solutions along with a range of homogeneity for the compound BaCa₂Si₃O₉ (which were not reported by Eskola (1922)). L. S. D. Glasser and Glasser (1968) reported a triclinic structure (space group P1) for this compound. They reported three distinct cation sublattices, two for Ca and one for Ba. This compound is also a naturally occurring mineral (walstromite). Doersam, Liebscher, Wunder, Franz, and Gottschalk (2009) reported the crystal structure for the (Ca,Sr)-walstromite phase, which is stable only at high pressures. They also reported three distinct cation sublattices for this compound, two predominantly filled by Ca and Sr each, and the third one by both. Following these findings, in the present work, the BaCa₂Si₃O₉ phase was also modeled having three distinct cation sublattices, one filled by Ca only and two others by both Ba and Ca. The phase was modeled as [Ba,Ca][Ba,Ca]CaSi₃O₉ using the compound energy formalism (This phase is labelled I-phase in Fig. 3.3.1). It is clear in Fig. 3.3.1 that non-stoichiometry of this phase is present on both sides of the BaCa₂Si₃O₉ composition. Hence, Ba and Ca are expected to be present on two of the other sublattices, if the third one is filled by Ca only. Since $CaSiO_3$ and $BaSiO_3$ have different crystal structures, the terminal solid solutions in Fig. 3.3.1 were modeled as different solid solutions using the single sublattice simple substitutional model (i.e., (Ca,Ba)SiO₃ and (Ba,Ca)SiO₃).

The optimized phase diagram for the C₂S-B₂S join is shown in Fig. 3.3.2. As reported earlier, the C₂S phase exists in α - and α '- polymorphs, whereas only the α '- phase is stable for B₂S. The α - and α '- solid solutions in Fig. 3.3.2 were modeled using the single-sublattice simple substitutional model, i.e. [Ca,Ba]₂SiO₄. All the authors listed below who investigated the C₂S-B₂S solid phase relationships below 1500 °C did not find any appreciable solubility of Ca in the B₂S phase. Hence, as shown in Fig. 3.3.2, practically no solubility of Ca in B₂S phase was assumed below 1500 °C. However, according to the present calculation (Fig. 3.3.2) a small solubility of Ca in the B₂S was calculated above 1500 °C. There are, however, no experimental data in the literature to corroborate this solubility.

Brisi and Appendino [Brisi and Appendino (1965); Brisi (1963)] by quenching and XRD, reported 21 mol% solubility at 1200 °C and 28 mol% solubility at 1350 °C of Ba in Ca₂SiO₄ phase. (They did not specify α - and α '- phases). They also reported the presence of a ternary compound on the C₂S-B₂S join with a range of homogeneity (shown by experimental points in Fig. 3.3.2) which they called T phase. Following Brisi and Appendino (1965) this phase was named T in Fig. 3.3.2. Nadachowski and Grylicki (1959) by quenching and metallography studied the B₂S-C₂S section and their data are shown in Fig. 3.3.2. They reported the T phase as B₅C₃S₄ (it is unclear in the publication what led them to conclude this stoichiometry). Toropov

and Fedorov (1964) studied the C_2S-B_2S section by quenching followed by optical microscopy and XRD. These data are shown in Fig. 3.3.2. They reported the T phase as $B_6C_4S_5$, solely based on the maximum in their liquidus data. Matkovic, Popovic, Grzeta, and Halle (1986) by XRD and DTA studied the C₂S-B₂S section. They reported a new orthorhombic phase which they called "X phase" with composition Ba_{0.48}Ca_{1.52}S. They also reported eutectoid decomposition of this phase at 1140 °X. Thompson, Withers, and Hyde (1987) by XRD and electron diffraction studied the section. They corroborated the presence of the X phase and reported another new phase, with distorted hexagonal crystal structure, which they call "Y phase". They showed Y phase to be stable around 1150 to 1325 °C in their phase diagram. Thompson, et al. (1987) also reported a small range of homogeneity (2 mol%) for these X and Y phases. No other experimental data on crystal structures or stoichiometries of these two phases could be found in the literature. In the present calculations, the X phase was modeled as stoichiometric B₂C₆S₄, which very closely corresponds to the composition of the X phase as reported by Matkovic, et al. (1986). Thompson, et al. (1987) reported the Y phase as stable at 30-32 mol% of Ba₂SiO₄. In the present work, this compound was molded as stoichiometric B₂C₄S₃. However, these stoichiometries are approximate and more experiments are required to establish them correctly. Matkovic, et al. (1986), Thompson, et al. (1987) and Fukuda, Maki, and Adachi (1992) by XRD reported that the T phase has a crystal structure derived from hexagonal α -Ca₂SiO₄. Fukuda, et al. (1992) also suggested a probable space group of $P\bar{3}m1$ for the T phase, the same as for α -Ca₂SiO₄. No experimental data on the number of sublattices and cation distributions among the different sublattices in the T phase could be found in the literature. However, α -Ca₂SiO₄ is known [Mumme, Cranswick, and Chakoumakos (1996)] to have three distinct sublattices for Ca ions with site occupancy 2,1,1 in a unit cell. Following these data and the similarity between the T phase and α -Ca₂SiO₄, the T phase was also modeled having three distinct cation sublattices with site occupancy 2,1,1 as Ba₂Ca[Ba,Ca]Si₂O₈.

Brisi and Appendino (1967) reported an isothermal section (Fig. 3.3.3 at 1100 °C which is compared with the present calculations in Fig. 3.3.4. They reported a compound with approximate composition $C_{0.1}B_{0.9}S$ as stable on the BS-CS join. The presence of this compound was not reported by Eskola (1922), Winkle and Muan (1973) and Toropov, Galakhov, and Bondar (1956). No other experimental data on the stability of this compound could be found in the literature. As the present calculations in Fig. 3.3.4 show, it is the T phase which is in equilibrium with the B_2S_3 and BS phases close to this composition. In the present calculations the presence of the compound $C_{0.1}B_{0.9}S$ was neglected. Also, the present calculations disagree with Brisi and Appendino (1967) on the equilibrium of the 2CaO.BaO.3SiO₂ (Fig. 3.3.3; in the present calculations 2CaO.BaO.3SiO₂ was modeled as T-phase) with C₂S and C₃S₂ phases along with extent of stability of the C₂S solid solution at 1100 °C. The exact reproduction of these data with the other experimental data on the B₂S-C₂S and BS-CS join was found very difficult. The present calculated liquidus (polythermal) projection for the BaO-CaO-SiO₂ ternary system is presented in Fig. 3.3.5.

No data on the mutual solubility between the C_3S and B_3S phases could be found in the literature. Moreover, as reported previously, there is not much solubility between the C_3S and Sr_3S phases. The bigger size difference between the Ca and Ba atoms would further mitigate against any appreciable solid solubility between the C_3S and B_3S phases. Brisi and Appendino (1967) also at 1100 °C did not report any solubility of Ca in the B₃S phase. In the present, solubility between

these phases was ignored.

Table 3.3.1 Optimized thermodynamic parameters, in Joules, (Gibbs energies of hypothetical end-members and excess interaction parameters) in the BaO-CaO-SiO₂ system**.

Psaudowellastenita (Psaudo)
$G^{0}(BaSiO_{3}, Pseudowoll.) = G^{0}(BaSiO_{3}) + 15481$
$q_{BaCa} = 25104$
Wollastonite (Woll.)
$\frac{G^{\circ}(BaSiO_3, Woll.) = G^{\circ}(BaSiO_3) + 37656}{D_{\circ}(BaSiO_3, Woll.) = G^{\circ}(BaSiO_3) + 37656}$
$BaSiO_3$ solid solution (ss)
G^0 (CaSiO ₃ , ss) = G^0 (CaSiO ₃) + 45229 - 19.018 T
α '-Ca ₂ SiO ₄ (α '-C ₂ S)
$q_{BaCa}^{11} = 41840$
$q_{BaCa}^{21} = -135980 + 58.576 \ T$
α -Ca ₂ SiO ₄ (α -C ₂ S)
$G^{0}(Ba_{2}SiO_{4}, \alpha) = G^{0}(Ba_{2}SiO_{4}, \alpha') + 8786$
Monoxide
$q_{CaBa}^{11} = 58600$
I-phase [Ca,Ba][Ca,Ba]CaSi ₃ O ₉
$G^{0}([Ca][Ca]CaSi_{3}O_{9}) = 3 G^{0}(CaSiO_{3}, Woll.) + 12552$
$G^{0}([Ca][Ba]CaSi_{3}O_{9}) = 2 G^{0}(CaSiO_{3}, Woll.) + G^{0}(BaSiO_{3}) - 6579$
$G^{0}([Ba][Ca]CaSi_{3}O_{9}) - G^{0}([Ca][Ba]CaSi_{3}O_{9}) = 30543$
$G^{0}([Ca][Ca]CaSi_{3}O_{9}) + G^{0}([Ba][Ba]CaSi_{3}O_{9}) = G^{0}([Ca][Ba]CaSi_{3}O_{9}) + G^{0}([Ba][Ca]CaSi_{3}O_{9}) $
T-phase $(Ba_2Ca[Ba,Ca]Si_2O_8)$
$G^{0}(Ba_{2}Ca[Ba]Si_{2}O_{8}) = -57831 + 6.973 T$
$G^{0}(Ba_{2}Ca[Ba]Si_{2}O_{8}) = 32342 - 48.116 T$
Liquid
$g^{001}_{BaSi(Ca)} = -4602; g^{001}_{CaSi(Ba)} = -4937$
X phase $(B_2C_6S_4)$
$\Delta H^{0}_{298} = -9298830 S^{0}_{298} = 535.126 \text{ J/mol/K} \qquad \Delta S^{0}_{298}{}^{(a)} = -1.352 \qquad \Delta S^{0}_{298}{}^{(b)} = 0$
$C_p = C_p (Ba_2SiO_4) + 3 C_p (Ca_2SiO_4, \gamma)$
$T_d^{(c)}$ = 1140 °C, Exp: 1140 °C [Matkovic et al., '86]
Y phase $(B_2C_4S_3)$
$\Delta H^{0}_{298} = -6902850 S^{0}_{298} = 460.450 \text{ J/mol/K} \qquad \Delta S^{0}_{298}{}^{(a)} = 40.932 \qquad \Delta S^{0}_{298}{}^{(b)} = -11.273$
$C_p = C_p (Ba_2SiO_4) + 2 C_p (Ca_2SiO_4, \alpha')$

**Here $G^{0}(A,x)$ refers to Gibb energy of A with x as reference state. ^(a) oxides (stable at room-temperature) as reference. ^(b) compounds used to calculated heat capacity as reference. ^(c) eutectoid decomposition



Fig. 3.3.1 Optimized phase diagram for the CaSiO₃-BaSiO₃ system.



Fig. 3.3.2 Optimized phase diagram for the Ca₂SiO₄-Ba₂SiO₄ system.



Fig. 3.3.3 An isothermal section at 1100 °C as reported by Brisi and Appendino.



Fig. 3.3.4 Optimized isothermal section in the BaO-CaO-SiO₂ ternary system.



Fig. 3.3.5 Present calculated liquidus (polythermal) projection for the BaO-CaO-SiO₂ system (isotherms were drawn at the interval of 100 °C).

3.4 The CaSiO₃-SrSiO₃-BaSiO₃ system

Winkle and Muan (1973) by quenching techniques and XRD reported phase relations in the temperature range 1225-1275 °C in the CaSiO₃-SrSiO₃-BaSiO₃ system. These data are reasonably well reproduced in the present calculated isothermal section at 1250 °C in Fig. 3.4.1. The Gibbs energy of the liquid phase was estimated from the corresponding binary subsystems treating silica as the asymmetric component [Pelton and Chartrand (2001)]. As can be seen in Fig.

3.4.1, the data of Winkle and Muan (1973) show solubility of Sr in the BaCa₂Si₃O₉ phase. In the present calculations, the solubility was taken into account by introducing Sr into both the sublattices filled by Ba and Ca, i.e. the phase was modeled as [Ba,Ca,Sr][Ba,Ca,Sr]CaSi₃O₉. The optimized parameters of this phase are presented in Table 3.4.1. The primary phase fields region reported by Winkle and Muan (1973) are well reproduced in Fig. 3.4.2. Winkle and Muan (1973) reported a ternary eutectic at 1275 °C with liquid composition of 20 mol% CaSiO₃, 39 mol% SrSiO₃ and 41 mol% BaSiO₃. The present calculated eutectic temperature is 1303 °C and composition is 24.3 mol% CaSiO₃, 34.2 mol% SrSiO₃ and 41.5 mol% BaSiO₃.

Table 3.4.1 Optimized thermodynamic parameters, in Joules, for the I-Phase: [Ba,Ca,Sr][Ba,Ca,Sr]CaSi₃O₉.*

I-phase [Ca,Ba][Ca,Ba]CaSi ₃ O ₉
$G^{0}([Ca][Sr]CaSi_{3}O_{9}) = 2 G^{0}(CaSiO_{3}, Woll.) + G^{0}(SrSiO_{3}) + 7326$
$G^{0}([Sr][Ca]CaSi_{3}O_{9}) - G^{0}([Ca][Sr]CaSi_{3}O_{9}) = 1674$
$G^{0}([Ba][Sr]CaSi_{3}O_{9}) - G^{0}([Sr][Ba]CaSi_{3}O_{9}) = -20920$
$G^{0}([Ca][Ca]CaSi_{3}O_{9}) + G^{0}([Sr][Sr]CaSi_{3}O_{9}) = G^{0}([Ca][Sr]CaSi_{3}O_{9}) + G^{0}([Sr][Ca]CaSi_{3}O_{9})$
$G^{0}([Sr][Sr]CaSi_{3}O_{9}) + G^{0}([Ba][Ba]CaSi_{3}O_{9}) = G^{0}([Ba][Sr]CaSi_{3}O_{9}) + G^{0}([Sr][Ba]CaSi_{3}O_{9})$
+ 33472

* Only the Gibbs energy of the end-members containing Sr are presented here; the Gibbs energies of other end-members are presented in the CaO-BaO-SiO₂ section



Fig. 3.4.1 Calculated isothermal section at 1250 °C in the SrSiO₃-CaSiO₃ -BaSiO₃ system.



Fig. 3.4.2 The polythermal projection of the SrSiO₃-CaSiO₃-BaSiO₃ system.

3.5 The SrO-MgO-SiO₂ system

Ghanbari-Ahari and Brett (1988) by XRD coupled with optical microscopy and EPMA studied this ternary system and reported isothermal sections over a range of temperature from 1200 and 1700 °C. The present calculated isothermal sections between 1200 and 1700 °C are reasonably well reproduced in Figs. 3.5.1-3.5.6. The Gibbs energy of the liquid phase in the ternary system was estimated from the corresponding binary systems by treating SiO₂ as asymmetric component [Pelton and Chartrand (2001)]. The liquid interaction parameters presented in Table 3.5.1 were also used to reproduce these isothermal sections. Ghanbari-Ahari and Brett (1988) confirmed the presence of two ternary compounds $Sr_2MgSi_2O_7$ (Sr_2MS_2), incongruent melting point of 1560 ± 15 °C, shown as T1 and Sr₃MgSi₂O₈ (Sr₃MS₂), melting point above 1700 °C, shown as T2 in Figs. 3.5.1-3.5.6. In the present calculations, both these phases were modeled as stoichiometric and the optimized parameters for these compounds are presented in Table 3.5.1. Massazza (1962) by quenching reported melting of the SrMS₂ phase as 1625 °C. Klasens, Hoekstra, and Cox (1957) while studying ultraviolet fluorescence of some ternary silicates also reported these two compounds. They reported XRD data for the Sr_2MS_2 and Sr_3MS_2 compounds which were indexed by them to the isomorphous Ca₂MgSi₂O₇ (akermanite) and Ca₃MgSi₂O₈ (merwinite) structures respectively. Ghanbari-Ahari and Brett (1988) also mentioned that analogues of diopside (CaMgSi₂ O_6) and monticellite (CaMgSiO₄) do not exist in the SrO-MgO-SiO₂ system. The EPMA data of Ghanbari-Ahari and Brett (1988) at 1500 and 1600 °C show negligible (< 1wt.%) solid solubility among the Mg_2SiO_4 -Sr₂SiO₄ and the $MgSiO_3$ -SrSiO₃ phases. The different crystal structures (Mg₂SiO₄ has olivine, Sr₂SiO₄ has α '-Ca₂SiO₄, MgSiO₃ has various pyroxenes, and SrSiO₃ has pseudowollastonite structures) and large difference between ionic radii of Mg and Sr mitigate against any appreciable mutual solid solubility among
these phases. Hence, in the present calculations as well these mutual solubilities were calculated as negligible at all the temperatures.

Huntelaar, Booij, Cordfunke, and Van der Laan (1998) by low-temperature heat capacity measurement reported S_{298}^{o} and by solution calorimetry reported ΔH_{298}^{o} for the Sr₃MS₂ phase which are well reproduced as shown in Table 3.5.1. They also reported by high-temperature drop calorimetry the enthalpy increments (H_T – H₂₉₈) in the range 250-650 °C for this phase. These enthalpy increments were used to optimize the heat capacity of the Sr₃MS₂ phase presented in Table 3.5.1. These enthalpy increments are compared with the present calculations in Fig. 3.5.7. The optimized heat capacity function for the temperature range 250-650 °C was also used at temperatures above this. The optimized heat capacity is shown in Fig. 3.5.8 where it is also compared with the heat capacity obtained by adding the heat capacities of corresponding orthosilicates. No thermodynamic data for the Sr₂MS₂ phase were found in the literature. The present calculated liquidus (polythermal) projection for the SrO-MgO-SiO₂ system is presented in Fig. 3.5.9.

Table 3.5.1 Optimized thermodynamic parameters, in Joules, in the SrO-MgO-SiO₂ system.

Sr ₃ MgSi ₂ O ₈	
$\Delta H^{0}_{298} = -4578300 \text{ J/mol} \qquad \Delta H^{0}_{298}, \text{Experimental} = -4$	575300 ± 5100 J/mol
$S_{298}^{0} = 280.150 \text{ J/mol/K}$ [Huntelaar et al., '98] [Huntelaar et al., '98] [Huntelaar et al., '98]	$\Delta S_{298}^{0} = 9.539$
$C_p = 303 + 0.06 T - 6040000 T^2$	$T_m^{(c)} = 1774$ °C; Exp.> 1700 °C [Ghanbari-Ahari and Brett, '88]
Sr ₂ MgSi ₂ O ₇	
$\Delta H^0_{298} = -3897000 J/mol$	
$S_{298}^0 = 230.879 \text{ J/mol/K}$ $\Delta S_{298}^{0(a)} = 13.858$	$\Delta S^{0}_{298}{}^{(b)} = 0$
$C_p = C_p (SrSiO_3) + C_p (MgSiO_3, protoenstatite) + C_p(SrO)$	$T_m^{(c)} = 1584$ °C; Exp. = 1560 ± 15 °C [Ghanbari-Ahari and Brett, '88] Exp. = 1625 ± 10 °C [Magaagga '62]
Monoxide (in Joules)	$Exp. = 1025 \pm 10$ C [Massazza, 02]
$q^{11}_{\rm SrMg} = 117000$	
α '-Mg ₂ SiO ₄ ^(e)	
$G^{0}(Mg_{2}SiO_{4}, \alpha') = G^{0}(Mg_{2}SiO_{4}) + 85772$	
α -Mg ₂ SiO ₄ ^(e)	
$G^{0}(Mg_{2}SiO_{4}, \alpha) = G^{0}(Mg_{2}SiO_{4}) + 83680$	
Liquid phase (Ternary interaction parameters) (in Joules)	
$q_{SiMg(Sr)}^{I0I} = -14644 - 26.3592 T$ $q_{SiMg(Sr)}^{04I} = 627600$	
^(a) oxides (stable at room temperature) as reference ^(b) compounds used to calculate heat capacity as reference ^(c) incongruent melting temperature ^(e) Mg ₂ SiO ₄ is an end-member in the α ' and α orthosilicate ph	ases



Fig. 3.5.1 Calculated isothermal section at 1200 °C.



Fig. 3.5.2 Calculated isothermal section at 1300 °C.



Fig. 3.5.3 Calculated isothermal section at 1400 °C.



Fig. 3.5.4 Calculated isothermal section at 1500 °C.



Fig. 3.5.5 Calculated isothermal section at 1600 °C.



Fig. 3.5.6 Calculated isothermal section at 1700 °C.



Fig. 3.5.7 Enthalpy increments $(H_{(T)} - H_{(298)})$ in the Sr₃MgSi₂O₈ phase.



Fig. 3.5.8 Optimized heat capacity of the $Sr_3MgSi_2O_8$ phase compared with the sum of the heat capacity of the orthosilicates.



Fig. 3.5.9 Present calculated liquidus (polythermal) projection for the SrO-MgO-SiO₂ system (isotherms were drawn at the interval of 100 °C).

3.6 The CaO-SrO-MgO-SiO₂ system

Massazza and Fadda (1964) and Massazza (1962) studied the Ca₂MgSi₂O₇-Sr₂MgSi₂O₇ (C₂MS₂-Sr₂MS₂) and Ca₃MgSi₂O₈-Sr₃MgSi₂O₈ (C₃MS₂-Sr₃MS₂) sections in this quaternary system. As reported in the SrO-MgO-SiO₂ system, Sr₂MS₂ is isostructural with C₂MS₂ and Sr₃MS₂ is isostructural with C₃MS₂. Massazza and Fadda (1964), Barry (1968) and Ruez (1971) reported complete solubility among the C₃MS₂ and Sr₃MS₂ phases but did not report any phase diagram points in this section. Massazza (1962) reported complete solubility among the C₂MS₂ and

 Sr_2MS_2 phases and reported phase diagram points on the C_2MS_2 - Sr_2MS_2 section. The optimal fit of these data is presented in Fig. 3.6.1. An ideal solution was assumed between the C_3MS_2 - Sr_3MS_2 phases. The solid solutions among the C_2MS_2 - Sr_2MS_2 and C_3MS_2 - Sr_3MS_2 phases were modeled using the single sublattice substitutional random-mixing model. Interaction parameters presented in Table 3.6.1 were also used for the C_2MS_2 - Sr_2MS_2 solid solution. In Fig. 3.6.1 the present calculations disagree with the experimental data on the appearance of the merwinite phase [(Ca,Sr)₃MgSi₂O₈ in Fig. 3.6.1]. The Gibbs energies of the end-members (C_3MS_2 - Sr_3MS_2) for this phase are fixed from the optimizations of the respective ternary systems. During calculations, in an effort to stabilize the merwinite phase, a negative interaction parameter was used but it did not help in fitting the stability of the merwinite phase in Fig. 3.6.1. It can be said that more experimental work is required to corroborate Massazza's data on the stability of merwinite phase in the C_2MS_2 - Sr_2MS_2 section. Also, some phase diagram data on the C_3MS_2 - Sr_3MS_2 section will also be helpful in fixing the stability of the merwinite phase.

Benna and co-workers [Benna (1982); Benna, Chiari, and Bruno (1987)] by quenching and XRD studied the Sr substitution in the diopside (CaMgSi₂O₆, clinopyrexene structure, C2/c) phase. As previously stated, the Sr analogue of diopside phase does not exist in the SrO-MgO-SiO₂ system. The data by Benna and co-workers are compared with the present calculations in Fig. 3.6.2. In our previous studies, the diopside phase was modeled as [Ca,Mg][Mg]Si₂O₆. Benna, et al. (1987) also reported that Sr enters the site with Ca and Mg and the second sublattice is filled by Mg only. Therefore, the diopside solution in Fig. 3.6.2 was modeled as [Ca,Mg,Sr][Mg]Si₂O₆. The optimized parameters are presented in Table 3.6.1. In the region where Benna, et al. (1987)

reported one phase diopside as stable (black triangles in Fig. 3.6.2), the present calculations show limited amounts of wollastonite and pseudowollastonite phases as stable, together with diopside. The reason for this is that the diopside phase, at the higher temperatures, on the CaSiO₃-MgSiO₃ join does not exactly lie on the 50-50 (CaMgSi₂O₆) composition (This can be seen in our previous study of the CaO-MgO-SiO₂ system) and is slightly off from it. Therefore, when the phase diagram is drawn on the CaMgSi₂O₆-SrMgSi₂O₆ join these two phases appear in very small amounts. Benna, et al. (1987), probably, could not detect the presence of small amounts of wollastonite phases in their investigations.

Table 3.6.1 Optimized thermodynamic parameters, in joules, in the CaO-SrO-MgO-SiO₂ system.

(Ca,Sr) ₃ MgSi ₂ O ₈
$q^{11} = 0$
$(Ca,Sr)_2MgSi_2O_7$ $q^{21} = 5021$
Diopside $([Ca,Mg,Sr][Mg]Si_2O_6)^{(a)}$
$G^{0}([Sr][Mg]Si_{2}O_{6} = G^{0}(SrSiO_{3}) + G^{0}(MgSiO_{3}, proto-enstatite)$
y_{Sr-Mg}^{00} (b) = 25304 + 2.358 T
y_{Sr-Mg}^{01} (b) = 3019

^(a) The Gibbs energy of the end-member containing Sr only is presented here; the Gibbs energy of the other end members can be found in the previous work by Jung (2003) on CaO-MgO-SiO₂ system.

^(b) These are the same parameters as used for the Ca-Mg interaction in the previous work by Jung (2003).



Fig. 3.6.1 Optimized phase diagram of the Ca₂MgSi₂O₇-Sr₂MgSi₂O₇ system.



Fig. 3.6.2 Optimized phase diagram for the CaMgSi₂O₆-SrMgSi₂O₆ join.

3.7 The BaO-MgO-SiO₂ system

The Gibbs energy of the liquid phase in this ternary system was estimated from the corresponding binary systems by treating SiO_2 as asymmetric component [Pelton and Chartrand (2001)]. The liquid interaction parameters presented in Table 3.7.1 was also used to obtain the optimal fit of the available data.

Klasens, et al. (1957) studied ultraviolet fluorescence in some ternary silicate compounds activated by lead. They reported four compounds in the system BaO-MgO-SiO₂: BaO.MgO.SiO₂ (BMS), BaO.2MgO.2SiO₂ (BM₂S₂), 2BaO.MgO.2SiO₂ (B₂MS₂), 3BaO.MgO.2SiO₂ (B₃MS₂). Barry (1968) also studied luminescence in the compound B₃MS₂ (along with 3SrO.MgO.2SiO₂ (Sr₃MS₂) and 3CaO.MgO.2SiO₂ (C₃MS₂)). Klasens, et al. (1957) indexed B₃MS₂ as having the merwinite (C₃MS₂) structure. Shimizu, Kimata, and Iida (1995) indexed B₂MS₂ as millilitre (Ca₂MgSi₂O₇) structure. For the BMS phase B. Liu and Barbier (1993) reported a hexagonal crystal structure (with space group P6₃). Argyle and Hummel (1965) by quenching studies reported all those phases reported by Klasens, et al. (1957) as stable along with one extra compound, BaMgSi₃O₈ (BMS₃).

Nadachowski and Grylicki (1959) studied the $Ba_2SiO_4-Mg_2SiO_4$ (B_2S-M_2S) section and reported it as a true binary join with BMS and $BaO.3MgO.2SiO_2$ (BM_3S_2) compounds. Vulkov, Stavrakeva, and Ivanova (1981) also reported it as a binary join with all three BMS, B_3MS_2 and BM_3S_2 as stable compounds. However, Klasens, et al. (1957) and Argyle and Hummel (1965) did not report this section as a true binary join, neither did they report BM_3S_2 as stable compound. No other experimental data on stability of the BM_3S_2 phase could be found in the literature. In the present work, this phase was not considered as stable.

Argyle and Hummel (1965) by quenching studies reported sub-solidus phase equilibria. Their data are presented in Table 3.7.1 and compared with the present calculations. Argyle and Hummel (1965) presented an isothermal section, based on these data, as shown in Fig. 3.7.1. However, they did not specify the temperature for this section. Presumably, they believed the phase assemblages did not change in the temperature range of their study. However, the present calculations show that phase assemblages change with temperature. For example, they reported BMS₃ to be in equilibrium with the MS phase (Fig. 3.7.1). As can be seen in Table 3.7.1, the only data to corroborate this equilibrium are at 950 °C. The present calculated isothermal section at 950 °C shows this phase to be in equilibrium (Fig. 3.7.2) but at a higher temperature (1000 °C) this is not the case as shown in Fig. 3.7.3 (the exact change occur at about 980°C). However, more experimental data are required to corroborate this change. Also, Argyle and Hummel (1965) and Klasens, et al. (1957), based on experimental data below 1100 °C, reported BM₂S₂ to be in equilibrium with MgO (Fig. 3.7.1). According to the present calculations, MgO is in equilibrium with BM₂S₂ at 1200 °C. However, at and above 1250 °C, instead of these two, BMS and M₂S are in equilibrium (Fig. 3.7.4) and B_2S-M_2S behaves as a true binary join. It should be noted that Nadachowski and Grylicki (1959) and Vulkov, et al. (1981) reported B₂S-M₂S as a true binary join, with an extra compound BM₃S₂ whose presence is neglected here, and all their investigations were above 1200 °C. So it is possible that B₂S-M₂S behaves as a true binary join, with the BM₃S₂ phase stable only at the higher temperatures. Below 1200 °C, the BM₃S₂ phase

decomposes into BM_2S_2 and MgO as shown in Fig. 3.7.4. However, more experimental evidence is required to prove this and the presence of BM_3S_2 was neglected in the present work. No experimental evidence on the mutual solid solubility among the phases of the same stoichiometry, i.e. the Mg_2SiO_4 - Ba_2SiO_4 and the $MgSiO_3$ - $BaSiO_3$ phases, could be found in the literature. Also, the different crystal structures (Mg_2SiO_4 has the olivine structure, Ba_2SiO_4 has the α '- Ca_2SiO_4 structure, $MgSiO_3$ has the various pyroxene structures, and $BaSiO_3$ has $BaGeO_3$ structure.) and large difference between ionic radii of Mg and Ba mitigate against any appreciable mutual solid solubility among these phases. Hence, in the present calculations as well these mutual solubilities were neglected. The present calculated liquidus (polythermal) projection for the BaO-MgO-SiO_2 system is presented in Fig. 3.7.5.

Argyle and Hummel (1965) also reported the nature and temperatures of melting for these ternary compounds along with low-temperature decomposition for BMS and BMS₃. These data can be compared with the present obtained results in Table 3.7.2. The Gibbs energy of the liquid phase in the ternary system was estimated from the corresponding binaries treating Si as asymmetric component [Pelton and Chartrand (2001)]. A small ternary interaction parameter, presented in Table 3.7.2., in the liquid phase was also used. The standard enthalpies (H^{0}_{298}) and standard entropies (S^{0}_{298}) for the solid phases presented in Table 3.7.2 were optimized based on the subsolidus phase equilibrium data in Table 3.7.1. No thermodynamic data for these solid phases could be found in the literature. The heat capacities for these phases were estimated as the sums of the constituent compounds and oxides, as shown in Table. 3.7.2. All the reported decomposition temperatures (Table. 3.7.2) are reasonably well reproduced except for the B₂MS₂

and BMS₃ phases. It was observed during the calculations that the values of H^{0}_{298} and S^{0}_{298} for the B₂MS₂ and BMS₃ phases, which reproduce the data in Table 3.7.1, invariably gave a high melting point and no low-temperature decomposition for the BMS₃ phase. For the BMS₃ phase, the X-ray reflections obtained by Argyle and Hummel (1965) were relatively weak. Argyle and Hummel (1965) at first thought this compound to be metastable. The only evidence based on which they concluded stability of this phases was that they heated a sample of this composition at 340 atm. (5000 psi) and 600 °C for 24 hours to obtain crystalline aggregates of BM₂S₂ and BaSi₂O₅ (BS₂). However, the same composition heated at 800 °C for 24 hours at 340 atm. (5000 psi) gave only BMS₃. It should be noted that they did not prove stability of this compound at 1 atm. pressure. In view of the difficulty faced in the present calculations, it can be said that more evidence is required to prove the stability of this phase. Moreover, some thermodynamic data for any of the ternary compounds in the BaO-MgO-SiO₂ system will also help in optimization by restricting the various degrees of freedom. The calculated standard entropies of formation (Table 3.7.2) for these compounds are quite reasonable as they are always less than 6 J/mol of metals.

SiO ₂	BaO	MgO	Temp.	Exp.	Present calculations (only those points are reported where present calculations differ from the experimental point) (tr=trace)
0.8	0.1	0.1	950	BMS ₃ +SiO ₂	(u-tuoo)
0.7	0.2	0.1	950	BMS ₃ +SiO ₂ +BS ₂	
0.66	0.17	0.17	950	BMS ₃ +SiO ₂	
0.65	0.1	0.25	950	BMS ₃ +SiO ₂ +MS	
0.62	0.25	0.13	950	BMS ₃ +BS ₂	BMS ₃ +BS ₂ +tr-BaSi ₂ Mg ₂ O ₇
0.6	0.25	0.15	950	BMS ₃ +BS ₂ +BM ₂ S ₂	
0.6	0.2	0.2	689	$BM_2S_2+BS_2$	BMS ₃
0.6	0.2	0.2	699	BMS ₂ +BS ₂ +tr BMS ₃	BMS ₃
0.6	0.2	0.2	704	BMS ₃	
0.6	0.2	0.2	723	BMS ₃	
0.6	0.2	0.2	770	BMS ₃	
0.6	0.2	0.2	950	BMS ₃	
0.6	0.2	0.2	1015	BMS ₃ +tr glass	BMS ₃
0.58	0.29	0.13	1100	$BM_2S_2\!\!+\!\!BS_2$	
0.57	0.33	0.1	1075	$BM_{2}S_{2}+B_{3}S_{5}$	$BS_2+BM_2S_2+B_5S_8$ (B ₃ S ₅ decomposes at
					1304 °C, see BaO-SiO ₂ section)
0.56	0.34	0.1	1100	$BM_{2}S_{2}+B_{5}S_{8}$	$BM_{2}S_{2}\!+\!B_{5}S_{8}\!+\!B_{2}S_{3}$
0.55	0.2	0.25	950	$BMS_3 \!\!+\! BM_2S_2$	
0.55	0.1	0.35	950	BMS ₃ +MS	
0.52	0.28	0.2	1050	$BM_2S_2 + B_3S_5 + BS_2$	$BM_2S_2+B_5S_8+BS_2(B_3S_5 \text{ decomposes at}$ 1304 °C, see BaO-SiO ₂ section)
0.51	0.19	0.3	950	$BM_2S_2 + BMS_3$	$BM_2S_2\!\!+\!BMS_3\!\!+\!MgSiO_3$
0.5	0.4	0.1	1000	$B_2MS_2 + B_2S_3$	
0.5	0.33	0.17	1050	$BM_2S_2{+}trB_2MS_2{+}B_2S_3$	
0.5	0.3	0.2	1100	$BM_{2}S_{2}+B_{2}S_{3}$	
0.5	0.25	0.25	1050	$BM_2S_2\!\!+\!BS_2$	
0.5	0.12	0.38	950	$BMS_3 \!\!+\! BM_2S_2 \!\!+\! MS$	
0.5	0.05	0.45	950	$BM_2S_2{+}trBMS_3{+}MS$	
0.46	0.15	0.39	950	$BM_2S_2\!\!+\!BMS_3\!\!+\!MS$	
0.45	0.45	0.1	1100	$BS+B_2MS_2$	
0.45	0.35	0.2	1100	$B_2MS_2\!\!+\!\!BM_2S_2\!\!+\!\!B_2S_3$	
0.45	0.1	0.45	1100	$BM_2S_2 + MS$	
0.43	0.28	0.29	1050	$BM_{2}S_{2}\!\!+\!\!B_{2}MS_{2}\!\!+\!\!B_{2}S_{3}$	
0.42	0.5	0.08	1050	$B_2MS_2 \!\!+\! BS \!\!+\! B_2S$	

Table 3.7.1 Experimental data of Argyle and Hummel (1965) compared with the present calculations.

0.4	0.4	0.2	1050	B_2MS_2	
0.4	0.4	0.2	1401	B_2MS_2	
0.4	0.4	0.2	1425	B_2MS_2	
0.4	0.4	0.2	1428	B_2MS_2 +trBMS+trGlass	B_2MS_2
0.4	0.3	0.3	1050	$B_2MS_2+BM_2S_2$	
0.4	0.2	0.4	1200	BM_2S_2	
0.4	0.1	0.5	1200	$M_2S{+}MS{+}BM_2S_2$	
0.4	0.05	0.55	1100	$BM_2S_2\!\!+\!\!M_2S\!\!+\!\!MS$	
0.38	0.5	0.125	1050	$B_2MS_2+B_2S$	
0.38	0.375	0.25	1050	B ₂ MS ₂ +BMS	
0.37	0.45	0.185	1050	$B_2MS_2\!\!+\!B_3MS_2$	$B_2MS_2+B_3MS_2+BMS$
0.37	0.27	0.365	980	$B_2MS_2\!\!+\!BM_2S_2\!\!+\!MgO$	$BMS+BM_2S_2$
0.37	0.27	0.365	1100	$BMS + BM_2S_2$	
0.36	0.09	0.55	1100	$M_2S{+}BM_2S_2$	$M_2S + BM_2S_2 + MgO$
0.35	0.5	0.15	1050	$B_2MS_2 + B_3MS_2 + B_2S$	
0.35	0.4	0.25	1050	$B_2MS_2\!\!+\!B_3MS_2\!\!+\!BMS$	
0.35	0.3	0.35	1100	$BM_2S_2 + BMS$	
0.33	0.567	0.1	1100	$B_3MS_2+B_2S$	B ₃ MS ₂ +B ₂ S+tr MgO
0.33	0.5	0.167	1100	B_3MS_2	B_3MS_2 +trMgO+ trB ₂ S)
0.33	0.267	0.4	980	B ₃ MS ₂ +B ₂ MS ₂ +tr MgO	BMS+BM ₂ S ₂ +MgO
0.33	0.4	0.267	1050	B_3MS_2+BMS	B ₃ MS ₂ +BMS+ tr MgO
0.33	0.333	0.333	980	B_2MS_2+MgO	$BMS + tr BM_2S_2 + tr B_3MS_2$
0.33	0.333	0.333	1010	B_2MS_2+MgO	$BMS + tr BM_2S_2 + tr B_3MS_2$
0.33	0.333	0.333	1016	$BMS {+} tr B_2 MS_2 {+} tr MgO$	$BMS + tr BM_2S_2 + tr B_3MS_2$
0.33	0.333	0.333	1022	BMS	$BMS + tr BM_2S_2 + tr B_3MS_2$
0.33	0.333	0.333	900	BM_2S_2+MgO	$B_2MS_2+MgO+B_3MS_2$
0.33	0.27	0.4	1100	$BM_2S_2+BMS+MgO$	
0.33	0.22	0.45	980	$B_2MS_2\!\!+\!\!BM_2S_2\!\!+\!\!trMgO$	BMS+MgO+BM ₂ S ₂
0.33	0.17	0.5	1100	BM_2S_2 +MgO	BMS+MgO+trBMS
0.33	0.11	0.56	1100	$BM_2S_2\!\!+\!\!M_2S\!\!+\!\!MgO$	
0.25	0.5	0.25	1200	B ₂ S+MgO	
0.25	0.3	0.45	1100	B ₃ MS ₂ +BMS+MgO	
0.25	0.25	0.5	1100	BMS+MgO	
0.25	0.18	0.57	1100	BMS+BM ₂ S ₂ +MgO	
0.25	0.05	0.7	1100	$BM_2S_2\!\!+\!\!M_2S\!\!+\!\!MgO$	
0.23	0.45	0.325	1100	B ₂ S+MgO	
0.2	0.4	0.4	1200	B ₂ S+MgO	
0.2	0.35	0.45	1100	B ₃ MS ₂ +B ₂ S+MgO	
0.2	0.3	0.5	1100	B ₃ MS ₂ +MgO	
0.2	0.1	0.7	1100	BM_2S_2 +MgO	
0.1	0.5	0.4	1300	B ₂ S+BaO+MgO	

BaMgSiO₄ (BMS) $\Delta H^{0}_{298} = -2198050 \text{ J/mol}$ $S_{298}^0 = 173.400 \text{ J/mol/K}$ $\Delta S^{0}_{298}{}^{(a)} = 19.632$ $T_m^{(c)} = 1642 \text{ °C}, \text{ Exp.}^{(b)} = 1640 \text{ [Argyle]}$ $\Delta S^{0}_{298}{}^{(e)} = 32.92$ $C_p = C_p (MgSiO_3, proto-enstatite) +$ Cp (BaO) and Hummel, '65] LT ^(d) (T,phases) = 1026, MgO+B₂MS₂+BM₂S₂ Exp. LT^(d) (T,phases)=1020, MgO+B₃MS₂ [Argyle and Hummel, '65] Ba₃MgSi₂O₈ (B₃MS₂) $\Delta S_{298}^{0}{}^{(a)} = 12.180$ $\Delta H^{0}_{298} = -4528000 \text{ J/mol}$ $S_{298}^0 = 323.400 \text{ J/mol/K}$ $T_m^{(c)} = 1605 \text{ °C}, \text{ Liq.+B}_2\text{S}, \text{ Exp.}^{(c)} = 1602 \text{ [Argyle and Hummel, '65]})$ $\Delta S_{298}^{0}^{(e)} = -2.678$ $C_p = 1.5 C_p (Ba_2 SiO_4) + 0.5 C_p (Mg_2 SiO_4)$ $Ba_2MgSi_2O_7$ (B_2MS_2) $\Delta S_{298}^{0}(a) = 0$ $\Delta H^{0}_{298} = -3868000 \text{ J/mol}$ $S_{298}^0 = 257.845 \text{J/mol/K}$ $C_p = C_p(Ba_2SiO_4) + C_p(MgSiO_3,S3) \Delta S_{298}^{(e)} = 3.836$ $T_{m}^{(b)} = 1479 \text{ °C}$ $Exp.^{(c)} = 1428, Liq. + BMS$ [Argyle and Hummel, '65] BaMg₂Si₂O₇ (BM₂S₂) $\Delta \overline{S}^{0}_{298}^{(a)} = 5.416$ $\Delta H^{0}_{298} = -3812000 \text{ J/mol}$ $S_{298}^0 = 208.200 \text{ J/mol/K}$ $C_p = C_p(Mg_2SiO_4) + C_p(BaSiO_3) \qquad \Delta S^{0}_{298}{}^{(e)} = -0.691$ $T_m^{(b)} = 1580 \text{ °C}, \text{ Exp.}^{(b)} = 1600 \text{ [Argyle]}$ and Hummel, '65] BaMgSi₃O₈ (BMS₃) $\Delta H^{0}_{298} = -4087084 \text{ J/mol}$ $S_{298}^0 = 230.000 \text{ J/mol/K}$ $\Delta S_{298}^{0}^{(a)} = -4.690$ $T_{m}^{(c)} = 1259 \text{ °C}, \text{Liq.} + BM_2S_2$ $C_p = C_p (BaSiO_3) + C_p (MgSiO_3(S3)) \Delta S_{298}^{(e)} = 6.600$ $Exp.^{(c)} = 1015$, Liq.+BM₂S₂ [Argyle and $+ C_{p} (SiO_{2}(S2))$ Hummel, '65] LT^(d) (T,phases)= No decomposition Exp. LT ^(d) (T,phases) = 700, $BM_2S_2+BS_2$ [Argyle and Hummel, '65] Monoxide (in Joules) $q^{11}_{BaMg} = 134000$

Table 3.7.2 Optimized thermodynamic parameters, in Joules, in the BaO-MgO-SiO₂ system.

 $g^{001}_{SiBa(Mg)} = -27614$

Liquid phase (Ternary interaction parameters) (in Joules)

- ^(a) Compounds used to calculate the respective heat capacities as reference
- ^(b) Congruent melting temperature
- ^(c) Incongruent melting temperature
- ^(d) Low-temperature decomposition
- ^(e) Oxides (stable at room-temperature) as reference



Fig. 3.7.1 Sub-solidus phase equilibria as reported by Argyle and Hummel.



Fig. 3.7.2 Optimized sub-solidus phase equilibria at 950 °C.



Fig. 3.7.3 Optimized sub-solidus phase equilibria in the temperature range 1000-1200 °C.



Fig. 3.7.4 Optimized sub-solidus phase equilibria at 1250 °C.



Fig. 3.7.5 Present calculated liquidus (polythermal) projection for the BaO-MgO-SiO₂ system (isotherms were drawn at the interval of 100 °C).

3.8 The BaO-SrO-MgO-SiO₂ system

Barry (1968) reported complete solubility between the isomorphous B_3MS_2 and S_3MS_2 phases (merwinite structure). No phase diagram data on this section could be found in the literature. In the present calculations, an ideal solution was assumed between these phases as also in the similar C_3MS_2 - S_3MS_2 system.

Shimizu, et al. (1995) and Mirbabaeva, Sirazhiddinov, and Grebenshchikov (1974) reported B_2MS_2 and Sr_2MS_2 as isomorphous (akermanite structure). Mirbabaeva, et al. (1974) by quenching and XRD also reported a phase diagram for the B₂MS₂-Sr₂MS₂ section. Their phase diagram data are compared with the present calculations in Fig. 3.8.1. As can be seen, these liquidus data are inconsistent with the calculated melting point of Sr₂MS₂. But, the present calculations agree with the melting data of Sr₂MS₂ by Ghanbari-Ahari and Brett (1988). Hence, the experimental data of Ghanbari-Ahari and Brett (1988) and Mirbabaeva, et al. (1974) are inconsistent and cannot be fitted simultaneously. Mirbabaeva, et al. (1974) by XRD also reported, at 1400°C, about 55 mol% solubility of B2MS2 in Sr2MS2 and about 10 mol% of Sr₂MS₂ in B₂MS₂. They reported, based on the liquidus data only, the presence of a compound Ba_{1.6}Sr_{0.4}MgSi₂O₇ on this section. No other reference in the literature stating this compound could be found. In the present calculations, this compound was neglected. More experimental work is required to prove its presence. In the present work, complete solubility between the B_2MS_2 and Sr_2MS_2 was tentatively calculated. The interaction parameter used in the similar C₂MS₂-SrMS₂ system was also used. However, more experimental work is required to correctly establish the phase diagram for this section.

Table 3.8.1 Optimized parameters, in joules, in the BaO-SrO-MgO-SiO₂ system. Merwinite (Ba,Sr)₃MgSi₂O₈

 $a^{11} = 0$

Akermanite $(Ca,Sr)_2MgSi_2O_7$ $q^{21} = 5021$



Fig. 3.8.1 Optimized phase diagram of the Sr₂MgSi₂O₇-Ba₂MgSi₂O₇ system.

3.9 The BaO-CaO-MgO-SiO₂ system

Klasens, et al. (1957) and Barry (1968) by XRD reported B_3MS_2 to be isostructural with C_3MS_2 (merwinite, space group $P2_1/a$). Yonesaki, Takei, Kumada, and Kinomura (2009) by XRD reported that B_3MS_2 has $K_3NaS_2O_8$ -type trigonal structure (with space group $P\overline{3}$ m1). Park, Hong, and Keszler (2009) by combined X-ray and neutron diffractometry reported that the B_3MS_2 crystal structure is closely related to merwinite, but that it crystallizes in a trigonal structure (with spacegroup $P\overline{3}$). In the present calculations, B_3MS_2 was considered isostructural with C_3MS_2 because, as reported earlier, complete solubility was calculated in the Sr_3MS_2 - B_3MS_2 and the C_3MS_2 - Sr_3MS_2 systems. Barry (1968), at 1200°C, reported mutual solubility in the system C_3MS_2 - B_3MS_2 and the presence of a compound $BaCa_2MgSi_2O_8$ (BC_2MS_2) and its stability region on this join. These data are well reproduced in Fig. 3.9.1. Nadachowski and Grylicki (1959) from

quenching and metallographic techniques, while studying the B₂S-M₂S-C₂S system, also reported the compound BC₂MS₂. In the literature this compound has been widely studied for its luminescence properties. Yonesaki, et al. (2009) by XRD reported the K₃NaS₂O₈-type structure (with space group $P\bar{3}m1$) for this phase. Park, et al. (2009) by neutron diffractometry reported a trigonal structure (with space group $P\bar{3}$). Park, et al. (2009) also reported three distinct cation sublattices, one each for Ba, Ca and Mg ions. Experimental data on cation distribution on different sublattices could not be found in the literature. As the data of Barry at 1200 °C show that non-stoichiometry of this phase exists on both the sides of the BC₂MS₂ composition, the phase was modeled as [Ba,Ca][Ca,Ba]₂MgSi₂O₈ using the compound energy formalism. The optimized parameters for this phase are presented in Table 3.9.1. No experimental data on the solubility of similar ions like Sr or Mg in this phase could be found in the literature. However, such solubilities cannot be completely ruled out, but in the absence of any experimental data they were neglected.

Nadachowski and Grylicki (1959) by quenching techniques reported an isothermal section at 1350 °C for the $B_2S-M_2S-C_2S$ system as shown in Fig. 3.9.2. The present calculated isothermal section is shown in Fig. 3.9.3. Nadachowski and Grylicki (1959) reported different phase equilibria on the C_2S-M_2S join than those calculated in Fig. 3.9.3 (optimized in our previous study based on numerous later studies). They also did not find the presence of the merwinite phase (B_3MS_2) in their studies. As reported in the ternary BaO-MgO-SiO₂ system the presence of BM₃S₂ was neglected in our calculations. Nadachowski and Grylicki (1959) did not report any appreciable solubility of Mg in the T phase. Hence, solubility of Mg in this phase was ignored.

The solubility of Sr in this phase cannot be completely ruled out. However, in the absence of any experimental evidence, this solubility was also ignored.

Shimizu, et al. (1995) and Mirbabaeva, et al. (1974) reported B_2MS_2 as isostructural with C_2MS_2 phase (akermanite structure). In the literature no data on the mutual solubility between these phases could be found. In the present calculations, an interaction parameter, identical to the one used for the C_3MS_2 - Sr_3MS_2 and Sr_3MS_2 - B_3MS_2 , was used. However, the Ba-Ca interactions in the B_2MS_2 - C_2MS_2 solid solution are supposed to be more positive in value (because of larger size difference between the Ba and Ca atoms) than the interaction between cations in the C_3MS_2 - Sr_3MS_2 and Sr_3MS_2 - B_3MS_2 systems. But, in the absence of any experimental data to evaluate the Ba-Ca interaction parameter, it was assumed to be the same as for the cations in the C_3MS_2 - Sr_3MS_2 and Sr_3MS_2 - B_3MS_2 systems.

Table 3.9.1 Optimized thermodynamic parameters, in joules, in the BaO-CaO-MgO-SiO $_2$ system.

Merwinite (Ba,Ca) ₃ MgSi ₂ O ₈
$q^{11} = 41840$
Akermanite (Ba,Ca) ₂ MgSi ₂ O ₇
$q^{21} = 5021$
$[Ba,Ca][Ca,Ba]_2MgSi_2O_8 (BC_2MS_2)$
$G^{0}[Ba]_{2}MgSi_{2}O_{8} = G^{0}(Ba_{3}MgSi_{2}O_{8}) + 17154$
$G^{0}[Ca]_{2}MgSi_{2}O_{8} = G^{0}(Ca_{3}MgSi_{2}O_{8}) + 10878$
$G^{0}[Ca][Ba]_{2}MgSi_{2}O_{8} - G^{0}[Ba][Ca]_{2}MgSi_{2}O_{8} = 58576$
$G^{0}[Ba]_{2}MgSi_{2}O_{8} + G^{0}[Ca]_{2}MgSi_{2}O_{8} = G^{0}[Ca][Ba]_{2}MgSi_{2}O_{8} + G^{0}[Ba][Ca]_{2}MgSi_{2}O_{8} + G^{0}[Ba][Ca]_{2}MgSi_{2}O_{8} + G^{0}[Ca][Ca]_{2}MgSi_{2}O_{8} + G^{0}[Ca][Ca][Ca]_{2}MgSi_{2}O_{8} + G^{0}[Ca][Ca][Ca]_{2}MgSi_{2}O_{8} + G^{0}[Ca][Ca][Ca]_{2}MgSi_{2}O_{8} + G^{0}[Ca][Ca][Ca][Ca][Ca][Ca][Ca][Ca][Ca][Ca]$



Fig. 3.9.1 Calculated isothermal section at 1200 °C in the BaO-CaO-MgO-SiO₂ system.



Fig. 3.9.2 Isothermal section at 1350 °C as reported by Nadachowski and Grylicki.



Fig. 3.9.3 Calculated isothermal section at 1350 °C in the BaO-CaO-MgO-SiO₂ system.

3.10 The CaO-SrO-Al₂O₃ system

The Gibbs energy of the liquid phase in the ternary CaO-SrO-Al₂O₃ system was estimated from the corresponding binary systems by treating Al_2O_3 as asymmetric component [Pelton and Chartrand (2001)]. A small liquid interaction parameter presented in Table 3.10.1 was also used. The optimized Gibbs energies of the unstable end-members are presented in Table 3.10.1. The Gibbs energy of the stable end-members can be found from the corresponding binary system.

Massazza and Cannas (1959) by quenching and optical microscopy investigated the ternary system and reported complete solubility at 1400 °C between the SrO.Al₂O₃-CaO.Al₂O₃ (SA-CA)

phases. However, later findings of Ito, et al. (1977) and of Kuroki, Saito, Matsui, and Morita (2009) by XRD disproved the complete solubility between the SA-CA system. Prodjosantoso and Kennedy (2003) by synchrotron powder diffraction methods reported data similar to Ito, et al. (1977) and Kuroki, et al. (2009). These data are compared with the present calculations in Fig. 3.10.1. The CA phase has a monoclinic crystal structure (space group, P21/n) [Dougill (1957); Fu, Dong, Liu, and Wang (2010)]. The room temperature form of the SA phase is monoclinic (space group, P2₁) which transforms at around 650 °C into P6₃22 symmetry [Rodehorst, et al. (2003)]. Prodjosantoso and Kennedy (2003) indexed the calcium-rich solid solution in the SA-CA system as P21/n space group and strontium-rich solid solution as P2₁ space group. As the two phases are not isostructural, they were modeled differently using single-sublattice substitutional model (i.e. (Ca,Sr)Al₂O₄, α in Fig. 3.10.1 and (Sr,Ca)Al₂O₄, β in Fig. 3.10.1). The lowtemperature SA and the CA phase belong to a different space group; hence they were treated as different phases. An interaction term presented in Table 3.10.1 was used, in the absence of any experimental evidence, to tentatively calculate practically no solubility of Ca in the lowtemperature SA phase.

Massazza and Sirchia (1959) by quenching and microscopic observation reported complete solid solubility at about 1500 °C among the phases 3SrO.Al₂O₃-3CaO.Al₂O₃ (S₃A-C₃A). F. P. Glasser (1974) reported that there exist two ordered phases in this section in the ranges 10-60 mol% S₃A and 70-90 mol% S₃A. Later, Prodjosantoso, Kennedy, and Hunter (2000) by synchrotron powder diffraction methods reported complete solubility at 1100 °C among these phases. The S₃A and C₃A phases have cubic crystal structures (space group, Pa3) [Prodjosantoso, et al. (2000);

Mondal and Jeffrey (1975); McMurdie; Chakoumakos, Lager, and Fernandez-Baca (1992)]. In the present work, complete solid solubility between these phases was calculated as shown in Fig. 3.10.2 and this solution was modeled using the single-sublattice substitutional model (i.e. $(Ca,Sr)_3Al_2O_4$, labeled $(S,C)_3A$ in Fig. 3.10.2. Prodjosantoso, et al. (2000) in their experiments prepared the samples through a series of heating in the temperature range 700-1000 °C. They reported that "even prolonged heating contained appreciable amounts of secondary phases and/or unreacted components" (No data on which phases and the amount precipitated were reported). Finally, they annealed the samples at 1100 °C for 72 hours and by XRD found just one phase. According to the present calculations, the $(S,C)_3A$ phase decomposes into the β phase as shown in Fig. 3.10.2 at lower temperatures. In fact, this could be the reason why Prodjosantoso, et al. (2000) obtained intermediate phases in the samples which were annealed at temperatures in the range 700-1000 °C for 24 hours. A small excess interaction term presented in Table 3.10.1 was also used for the $(S,C)_3A$ phase. This term was necessary to make the solid solution stable at 1100 °C. Massazza and Sirchia (1959) reported phase diagram data for the S₃A-C₃A section which are compared with the present calculations in Fig. 3.10.2. In this section, F. P. Glasser (1974) by microscopic observation at 1435 °C between 70 and 95 wt.% S₃A noted signs of incongruent melting. However, the data by Massazza and Sirchia (1959) show a single phase (S,C)₃A solid solution stable at this temperature. The present calculations disagree with the data of Massazza and Sirchia (1959) on the extensive stability of the S_4A phase in this section. The ΔH_{298}^0 of the S₄A phase and the stability range for this phase are reproduced quite well in the binary SrO-Al₂O₃ system. Hence, the Gibbs energy of the S₄A phase is fixed and the extensive stability of S₄A phase in this section was not reproduced as reported by Massazza and Sirchia (1959). Probably, more experimental work is required to prove these results.

Massazza and Cannas (1959) by optical microscopy reported complete solubility in the CaAl₄O₇-SrAl₄O₇ system. There are data [Ponomarev, Kheiker, and Belov (1970), Boyko and Wisnyi (1957)] on the similarity of the structures of these phases. No phase diagram data on this section could be found in the literature. In the present calculations, an ideal solution between these two end-members was assumed.

Massazza and Cannas (1959) by quenching and microscopic observation reported complete solid solubility between the end-members $SrAl_{12}O_{19}$ -Ca $Al_{12}O_{19}$ (SA₆-CA₆). There are references [K. Kimura, et al. (1990); Kang, et al. (2009); Utsunomiya, et al. (1988)] in the literature proving hexagonal structure with the space group P6₃/mmc for these phases. Kadyrova (1999) also reported complete solubility between these compounds. In the present calculations an ideal solution was assumed between these compounds to calculate the phase diagram shown in Fig. 3.10.3. Kadyrova (1999) using a high-temperature electro vacuum micro-furnace also measured melting temperatures at some compositions (Fig. 3.10.3). His data for the melting of the CA₆ phase are not consistent with the phase diagram for the CaO-Al₂O₃ system from the ftoxide database (L.H.S. of Fig. 3.10.3). Otherwise, these data are consistent with the calculations in Fig. 3.10.3.

Kuroki, et al. (2009) et al. by in-situ observation using CSLM coupled with XRD predicted a part of an isothermal cross section at 1700 °C as shown in Fig. 3.10.4 (in this figure only the stability region of the liquid, α and β phases were experimentally measured). These results can be

compared with the present calculations in Fig. 3.10.5. Here, the exact reproduction of the three phase region (Liquid + α + β) was found to be very difficult. The extent of solubility at this temperature in the α and β phases is fixed by the phase diagram in Fig. 3.10.1. Moreover, the liquidus boundary is reasonably well reproduced. The present calculated liquidus (polythermal) projection for the CaO-SrO-Al₂O₃ system is presented in Fig. 3.10.6.

Table 3.10.1 Optimized thermodynamic parameters, in Joules, in the SrO-CaO-Al₂O₃ system.

α ([Ca,Sr]Al ₂ O ₄)
$G^{0}(\text{SrAl}_{2}\text{O}_{4}, \alpha) = G^{0}(\text{SrAl}_{2}\text{O}_{4}, \text{HT}) + (15564 - 6.318 T); \ q^{11}_{CaSr} = (4184 - 5.021 T)$
β ([Sr,Ca]Al ₂ O ₄)
$G^{0}(\text{CaAl}_{2}\text{O}_{4},\beta) = G^{0}(\text{CaAl}_{2}\text{O}_{4}) + (30125 - 8.368 T); q^{11}_{CaSr} = (-29288 + 12.594 T)$
Low-temperature Sr-aluminate solution (LTSrss)
$G^{0}(CaAl_{2}O_{4}, LTSrss) = G^{0}(CaAl_{2}O_{4}) + 42000$
(S,C) ₃ A ([Ca,Sr] ₃ Al ₂ O ₆)
$q^{II}{}_{CaSr} = -6276$
$(S,C)A_2([Ca,Sr]Al_4O_7)$
$-q^{II}_{CaSr} = 0$
$(S,C)A_6([Ca,Sr]Al_{12}O_{19})$
$q^{II}{}_{CaSr} = 0$
Liquid
$\Delta g^{001}_{SrSi(Ca)} = -14644$

** Here $G^{0}(A, x)$ refers to Gibb energy of A with x as reference state.



Fig. 3.10.1 Optimized phase diagram of the CaAl₂O₄-SrAl₂O₄ system.



Fig. 3.10.2 Optimized phase diagram of the Ca₃Al₂O₆-Sr₃Al₂O₆ system.



Fig. 3.10.3 Optimized phase diagram of the CaAl₁₂O₁₉-SrAl₁₂O₁₉ system.



Fig. 3.10.4 The isothermal section at 1700 °C in the CaO-SrO-Al₂O₃ system as reported by Kuroki et al.



Fig. 3.10.5 Calculated isothermal section of the CaO-SrO-Al₂O₃ system at 1700 °C.



Fig. 3.10.6 Calculated liquidus (polythermal) projection for the CaO-SrO-Al₂O₃ system (isotherms were drawn at the interval of 100 $^{\circ}$ C).

3.11 The BaO-CaO-Al₂O₃ system

The Gibbs energy of the liquid phase in the BaO-CaO-Al₂O₃ ternary was calculated from corresponding binary systems by treating Al_2O_3 as asymmetric component [Pelton and Chartrand (2001)]. No ternary interaction parameters were used for the liquid phase. The optimized parameters for the system are presented in Table 3.11.1. For solid solutions, the Gibbs energies of unstable end-members are presented and Gibbs energy of stable end-members can be found in the tables for the corresponding binary systems.

Ito, Banno, Suzuki, and Inagaki (1979) determined the solid solubility in the BaAl₂O₄ (BA)-CaAl₂O₄(CA) system by lattice parameter measurements (XRD). These data are compared with the present calculations in Fig. 3.11.1.The room-temperature form of BA has hexagonal structure (space group, P6₃) which undergoes transformation at about 327 °C into P6₃22 symmetry [Rodehorst, et al. (2003)]. The CA phase has monoclinic structure (space group, P21/n) [Dougill (1957); Fu, et al. (2010)]. As the two phases have different structures, they were modeled differently using single-sublattice substitution model (i.e. (Ca,Ba)Al₂O₄, α in Fig. 3.11.1 and (Ba,Ca)Al₂O₄, β in Fig. 3.11.1. The low-temperature BA and the CA phase belong to different space group; hence they were treated as different phases. An interaction term presented in Table 3.11.1 was used, in the absence of any experimental evidence, to tentatively calculate practically no solubility of Ca in the low-temperature BA phase.

Brisi and Montorsi (1962) by XRD reported an isothermal section (Fig. 3.11.2) for the BaO-CaO-Al₂O₃ system at 1250 °C. The present calculated isothermal section at 1250 °C is shown in Fig. 3.11.3. Appendino (1972b) by equilibration and quenching techniques reported 10% Ca solubility in the Ba₄Al₂O₇ (B₄A) phase and 2.5% Ca solubility in the Ba₈Al₂O₁₁ (B₈A) phase at 1250 °C. Appendino (1972b) by XRD reported the presence of a ternary compound Ba₃CaAl₂O₇ (B₃CA), denoted by T2 in Fig. 3.11.3, and suggested its composition varies in the range 2-3% CaO. In Fig. 3.11.2, Brisi and Montorsi (1962) reported solubility of Ca in B₃A but not of Ba in C₃A. There are different data on the crystal structure of B_3A . Antipov, Lykova, Paromova, Rozanova, and Kovba (1987) reported a cubic structure with space group Pa3. Walz, Heinau, Nick, and Curda (1994) reported an orthorhombic structure, whereas Lazic, Kahlenberg, Kaindl, and Kremenovic (2009) reported cubic structure with space group P2₁3. As reported earlier, C_3A and S₃A have the same cubic structure with space group Pa3 and form a continuous solid solution. Appendino (1972a) by quenching and XRD reported complete solubility of S₃A and B₃A, which implies that the two are of the same structure. Therefore, in the present work the B₃A phase was considered isostructural with S_3A and C_3A , as also reported by Antipov, et al. (1987). In Fig. 3.11.3, the solid solution between B_3A and C_3A was modeled using the single sublattice substitution model. A negative interaction parameter presented in Table 3.11.1 was used for the (B,C)₃A phase to reproduce the data reported by Brisi and Montorsi (1962).

Massazza (1963) by optical microscopy reported an isothermal section at 1400 °C (Fig. 3.11.4). The present calculated isothermal section at 1400 °C is shown in Fig. 3.11.5. The phase equilibria reported by Massazza (1963) were qualitatively the same as reported by Brisi and Montorsi (1962), except that Massazza (1963) reported a range of homogeneity (4-5% CaO) for the ternary compound Ca₂BaAl₈O₁₅ (C₂BA₄), denoted by T1 in Fig. 3.11.3. Brisi and Montorsi (1962)

reported this compound as stoichiometric. In the present work, both the ternary phases, C_2BA_4 (T1) and B_3CA (T2), were modeled as stoichiometric phases. The optimized parameters for these phases are presented in Table 3.11.1. The calculated melting temperatures of these compounds are also quite reasonable.

The present calculations at 1400 °C disagree with Massazza (1963) on account of the appearance of the liquid phase adjacent to the CaO-Al₂O₃ boundary. It was calculated that this liquid phase would not appear had the phase $Ca_{12}Al_{14}O_{33}$, whose stability in the binary CaO-Al₂O₃ is debatable, been included. However, as reported by Eriksson and Pelton (1993) and more recently by Duran et al. (2008), the $Ca_{12}Al_{14}O_{33}$ phase is stable only in humid air. Massazza's work was possibly contaminated by humidity. In the present work, the data for the CaO-Al₂O₃ system are taken from Eriksson and Pelton (1993) which does not contain the $Ca_{12}Al_{14}O_{33}$ phase; hence this phase was also not considered in the ternary calculations.

It can be seen that Brisi and Montorsi (1962) reported no solubility, and Massazza (1963) reported very little, among the BaAl₁₂O₁₉ (BA₆)-CaAl₁₂O₁₉ (CA₆) phases. However, Kadyrova and Daminova (1997) reported complete solubility among these phases. The CA₆ and BA₆ phases are reported [Kang, et al. (2009);Utsunomiya, et al. (1988); Delacarte, Kahn-Harari, and Thery (1993)] to have hexagonal structure with the space group P6₃/mmc. In the present calculations, an ideal solution was assumed (labelled [B,C]A₆) in Fig. 3.11.6) between the phases CA₆ and BA₆ which have the same structure and space group. Kadyrova and Daminova (1997) also measured the melting and liquidus temperatures on the BA₆-CA₆ join. However, the
topology of the phase diagram reported by them is dubious because their data show congruent melting behavior at the BA₆ composition whereas it is most likely peritectic (see Fig. 2.7.1) Their data on the BA₆-CA₆ section are compared with the present calculated phase diagram in Fig. 3.11.6. As is evident, little weight was given to the solidus and liquidus data points. The present calculated liquidus (polythermal) projection for the the BaO-CaO-Al₂O₃ system is presented in Fig. 3.11.7.

$Ca_2BaAl_8O_{15}(T1)$						
$\Delta H^0_{298} = -8680482$	$S^0_{298} = 438.646 \text{ J/mol/K}$	$C_p = C_p(BA (HT)) + C_p(CA)$	$T_{m}^{(c)} = 1695 \ ^{\circ}C$			
	$\Delta S^{0}_{298}{}^{(a)} = 0$	C _p (CA ₂) J/mol/K				
	$\Delta S^{0}_{298}{}^{(b)} = 87.797$					
Ba ₃ CaAl ₂ O ₇ (T2)						
$\Delta H^{0}_{298} = -4110102$	$S_{298}^0 = 343.750 \text{ J/mol/K}$	$C_p = C_p(B_3A) + C_p(CaO)$	$T_{m}^{(c)} = 1585 \text{ °C}$			
	$\Delta S^{0}_{298}{}^{(a)} = 0$	J/mol/K				
	$\Delta S^{0}_{298}{}^{(b)} = 38.973$					
β ([Ba,Ca]Al ₂ O ₄)						
$G^0(CaAl_2O_4, \beta) = G^0(CaAl_2O_4)$	D_4) + (30125 – 8.368 T) J; q^4	$I_{BaCa}^{I} = (50208 - 25.104 T) J$				
α ([Ca,Ba]Al ₂ O ₄)						
$G^{0}(BaAl_{2}O_{4}, \alpha) = G^{0}(BaAl_{2}O_{4}, \alpha)$	$D_4) + 4184 J$					
Low-temperature Ba-alumin	ate solution (LTBass)					
$G^{0}(CaAl_{2}O_{4}, LTBass) = G^{0}(CaAl_{2}O_{4}) + 42000$						
$(B,C)_3A$ ($[Ba,Ca]_3Al_2O_6$)						
$q^{21}{}_{BaCa} = -33472 \text{ J}$						
B_4Ass ([Ba,Ca] ₄ Al ₂ O ₇)						
$G^{0}(Ca_{4}Al_{2}O_{7}, B_{4}Ass) = G^{0}(Ca_{3}Al_{2}O_{6}) + G^{0}(CaO) + 83680 J; q^{11}_{BaCa} = -41840 J$						
B_8Ass ([Ba,Ca] ₈ Al ₂ O ₇)						
$G^{0}(Ca_{8}Al_{2}O_{11}, B_{8}Ass) = G^{0}(Ca_{3}Al_{2}O_{6}) + 5 G^{0}(CaO) + 146440 J$						
$[B,C]A_6ss ([Ba,Ca]Al_{12}O_{19})$						
$q_{BaCa} = 0$						
[*] Here $G^{0}(A,x)$ refers to Gibb energy of A with x as reference state.						
^{a)} compounds used to calculate heat capacity as reference						

Table 3.11.1 Optimized thermodynamic parameters, in Joules, in the BaO-CaO-Al₂O₃ system.*

compounds used to calculate heat capacity as reference

^(b) oxides (stable at room-temperature) as reference

^(c) incongruent melting temperature



Fig. 3.11.1 Optimized phase diagram of the BaAl₂O₄-CaAl₂O₄ system.



Fig. 3.11.2 Isothermal section at 1250 °C as reported by Brisi and Montorsi.



Fig. 3.11.3 Optimized isothermal section at 1250 °C in the BaO-CaO-Al₂O₃ system.



Fig. 3.11.4. Isothermal section at 1400 °C as reported by Massazza.



Fig. 3.11.5 Optimized isothermal section at 1400 °C in the BaO-CaO-Al₂O₃ system.



Fig. 3.11.6 Optimized phase diagram of the section CaA₁₂O₁₉-BaAl₁₂O₁₉.



Fig. 3.11.7 Present calculated liquidus (polythermal) projection for the BaO-CaO-Al₂O₃ system (isotherms were drawn at the interval of 100 °C).

3.12 The SrO-BaO-Al₂O₃ system

The Gibbs energy of the liquid phase in the SrO-BaO-Al₂O₃ ternary was calculated from the corresponding binary systems by treating Al₂O₃ as asymmetric component [Pelton and Chartrand (2001)]. No ternary interaction parameters were used for the liquid phase. The optimized parameters for the system are presented in Table. 3.12.1. For solid solutions, the Gibbs energies of unstable end-members are presented and Gibbs energies of stable end-members can be found in the sections on the corresponding binary systems.

Ito, et al. (1979) by XRD reported complete solubility among the high temperature polymorphs in the BaAl₂O₄-SrAl₂O₄ (BA-SA) section. These high-temperature polymorphs are isostructural and have P6₃22 symmetry [Rodehorst, et al. (2003)]. Rodehorst, et al. (2003) studied the solubilities in this section by infrared powder absorption spectroscopy and presented a schematic phase diagram depicting the first- and second-order transitions as shown in Fig. 3.12.1. They also reported complete solubility in the BA-SA section at higher temperatures. In the present calculations as well, an ideal solution was calculated among these high-temperature polymorphs as shown in Fig. 3.12.2 (which shows first order transitions only). This solution (β in Fig. 3.12.2) was modeled using a single-sublattice simple substitutional model (i.e., [Ba,Sr]Al₂O₄). Henderson and Taylor (1982) by thermal analysis measured the solubility in the low-temperature isomorph of the $SrAl_2O_4$ phase which is monoclinic in structure with space group $P2_1$ [Rodehorst, et al. (2003)]. No data in the literature could be found for the solubility of Sr in lowtemperature BA, which has a hexagonal structure with space group $P6_3$ [Rodehorst, et al. (2003)]. In the present calculations, Sr solubility in the low-temperature BA phase was tentatively calculated based on the schematic diagram of Rodehorst, et al. (2003). The low temperature (LT) solid solutions in Fig. 3.12.2 were also modeled using a single-sublattice simple substitutional model (i.e., [Ba,Sr]Al₂O₄ and [Sr,Ba]Al₂O₄].

Appendino (1972a) by quenching and XRD studies established an isothermal section at 1400 °C in the SrO-BaO-Al₂O₃ system as shown in Fig. 3.12.3. This figure can be compared with the present calculated isothermal section at 1400 °C in Fig. 3.12.4. As reported earlier, B_3A and S_3A phases have a cubic structure with space group Pa3. In the present calculations, complete

solubility was calculated among these phases as reported by Appendino (1972a). The solution was modeled using the single-sublattice substitutional model and an excess interaction parameter, presented in Table 3.12.1, was used to reproduce the data of Appendino (1972a) in Fig. 3.12.3. In the Ba₃Al₂O₆-Sr₃Al₂O₆ (B₃A-S₃A) section, F. P. Glasser (1974) by quenching, XRD and crystallographic studies reported two ordered phases at 1370 °C. The first has a homogeneity range between 10 and 20 mol% B₃A, and the second one from 30 to 90% B₃A. F. P. Glasser (1974) also noted signs of incongruent melting between compositions 70 and 95 mol% S₃A at 1435 °C. According to the present calculations no liquid phase appears on this section until about 1600 °C. As reported earlier, his similar data in the in the Ca₃Al₂O₆-Sr₃Al₂O₆ (C₃A-S₃A) section are not in agreement with the available data. More experimental work is required to corroborate F. P. Glasser (1974)'s observations of incongruent melting at this temperature.

Appendino (1972a), on the Ba₄Al₂O₇-Sr₄Al₂O₇ (B₄A-S₄A) join, reported a ternary compound 2BaO.2SrO.Al₂O₃ (B₂S₂A). No thermodynamic data for this phase could be found in the literature. Appendino (1972a), apart from the terminal solid solutions and the ternary compound, reported one more phase (a solid solution as can be seen in Fig. 3.12.3). No X-ray data for this phase were given by Appendino (1972a). No data on the crystal structure of the S₄A phase could be found in the literature. The B₄A phase is orthorhombic in structure with space group Cmca [Kahlenberg (2001)]. In the present calculations, the S₄A was assumed to be isostructural with the B₄A and complete solubility was calculated between these two phases. This solid solution was modeled using the single-sublattice simple substitutional model (i.e., $[Ba,Sr]_4Al_2O_7$). The ternary compound reported by Appendino was neglected. Terminal solid solubility in the

Ba₈Al₂O₁₁ phase at 1400 °C as reported by Appendino (1972a) was reproduced in Fig. 3.12.4. The solid solution was modeled using the single-sublattice simple substitutional model (i.e., [Ba,Sr]₈Al₂O₁₁]). Teoreanu and Ciocea (1978) by quenching and XRD studied the BaAl₂O₄-SrAl₂O₄-Al₂O₃ section of the ternary system at 1700 °C and reported the same phase assemblage as reported by Appendino (1972a). Teoreanu and Ciocea (1978), at 1700 °C, and Appendino (1972a), at 1400 °C, did not report SA₂ and S₄A₇ as stable phases. However, as reported in the binary SrO-Al₂O₃ section, these phases are considered stable in the present calculations; hence they appear in Fig. 3.12.4.

Teoreanu and Ciocea (1978) at 1700 °C, and Appendino (1972a) at 1400 °C, reported no solubility in the (BaAl₁₂O₁₉-SrAl₁₂O₁₉) BA₆-SA₆ section. However, Kadyrova, et al. (1996) reported complete solubility in this section at 1400 and 1500 °C. As reported earlier, the BA₆ and SA₆ phases have the same hexagonal structure and space group, P6₃/mmc. In the present calculations, an ideal solution was assumed between BA₆ and SA₆. Kadyrova, et al. (1996) also measured the melting temperature and liquidus temperatures on the BA₆-CA₆ join. However, the topology of the phase diagram reported by them is dubious because their data show congruent melting behavior at the BA₆ composition, whereas it is most likely peritectic (see Fig. 2.7.1). These data on the BA₆-SA₆ section are compared with the present calculations in Fig. 3.12.5. The present calculated liquidus (polythermal) projection for the SrO-BaO-Al₂O₃ system is presented in Fig. 3.12.6.

Table 3.12.1 Optimized thermodynamic parameters, in Joules, in the SrO-BaO-Al₂O₃ system.

β ([Sr,Ba]Al ₂ O ₄)
$q^{11}_{BaSr} = 0$
Low-temperature Sr-aluminate solution (LTSrss) ([Sr,Ba]Al ₂ O ₄)
$G^{0}(BaAl_{2}O_{4}, (LTSrss)) = G^{0}(BaAl_{2}O_{4}) + 4184$
$q^{11}_{BaSr} = -2929$
Low-temperature Ba-aluminate solution (LTBass) ([Ba,Sr]Al ₂ O ₄)
$G^{0}(SrAl_{2}O_{4}, (LTBass) = G^{0}(SrAl_{2}O_{4}) + 20920$
$(B,S)_{3}A$ ([Ba,Sr] ₃ Al ₂ O ₆)
$q^{11}_{\text{BaSr}} = 0$
$(B,S)_4A ([Ba,Sr]_4Al_2O_7)$
$q^{11}_{\text{ BaSr}} = 0$
$(B,S)_{8}A$ ([Ba,Sr] ₈ Al ₂ O ₁₁
$G^{0}(Sr_{8}Al_{2}O_{11}, B_{8}A ss) = 8 G^{0}(SrO) + G^{0}(Al_{2}O_{3}) + 4184$



Fig. 3.12.1 A schematic phase diagram for the $SrAl_2O_4$ -Ba Al_2O_4 section as reported by Rodehorst et al. (The transitions from C2 to P2₁ and P6₃22 to P6₃ ($\sqrt{3A}$) are of second order character).



Fig. 3.12.2 Optimized phase diagram of the SrAl₂O₄-BaAl₂O₄ section.



Fig. 3.12.3 Isothermal section of the SrO-BaO-Al₂O₃ system at 1400 $^{\circ}$ C as reported by Appendino.



Fig. 3.12.4 Optimized isothermal section of the SrO-BaO-Al₂O₃ system at 1400 °C.



Fig. 3.12.5 Optimized phase diagram of the section SrAl₁₂O₁₉- BaAl₁₂O₁₉.



Fig. 3.12.6 Present calculated liquidus (polythermal) projection for the SrO-BaO-Al₂O₃ system (isotherms were drawn at the interval of 100 °C).

3.13 The CaAl₂O₄-SrAl₂O₄-BaAl₂O₄ system

Ito, et al. (1979) by XRD also reported an isothermal section at 1300 °C for the system CA-SA-BA. These data are reasonably well reproduced in Fig. 12.6.



Fig. 3.13.1 Optimized isothermal section at 1300 °C in the CaAl₂O₄-SrAl₂O₄-BaAl₂O₄ system.

3.14 The BaO-MgO-Al₂O₃ system

Gobbels, et al. (1998) by quenching and EPMA determined the phase relationships at 1800 °C in the Al-rich part of the ternary system as shown in Fig. 3.14.1. They reported BaMgAl₁₀O₁₇ (BMA₅) as a stable ternary compound and presented references on its similarity of structure (space group, P6₃/mmc) with the binary phase close to the BA₆ composition, called Al₂O₃-rich phase in the present work (see BaO-Al₂O₃ section). They also proved experimentally the presence of continuous solid solution (BAM-I_{ss} in Fig. 3.14.1) at 1800 °C among these two phases. As reported earlier, in the present calculations the Al₂O₃-rich phase was taken into account as stoichiometric BA₆ phase. In the present calculations, an ideal single-sublattice substitutional solution was assumed among the BMA₅ and BA₆ phases (the association of BaMg was considered as one particle; replacing Ba in the BA₆ phase). As can be seen in Fig. 3.14.1, Gobbels, et al. (1998) reported another stable ternary compound as BaMg₃Al₁₄O₂₅ (BM₃A₇) with very limited range of solubility (BAM-II_{ss} in Fig. 3.14.1). Nobuo Iyi, Gobbels, and Kimura (1998) reported hexagonal structure (space group, $P\overline{6}m2$) for this compound. In the present calculations, this phase was modeled as stoichiometric. The phase relationships reported by Gobbels, et al. (1998) can be compared with the present calculations in Fig. 3.14.2. Gobbels, et al. (1998) reported incongruent melting behavior for the BAM-II_{ss} phase (they did not report temperature of melting). In the present calculations, the incongruent melting temperature for this phase is 1945 °C. The Gibbs energy of the liquid phase in the ternary BaO-MgO-Al₂O₃ system was estimated from the constituent binary systems by treating Al₂O₃ as asymmetric component [Pelton and Chartrand (2001)]. No ternary parameters were required. The present calculated liquidus (polythermal) projection for the BaO-MgO-Al₂O₃ system is presented in Fig. 3.14.3.

Table 3.14.1 Optimized thermodynamic parameters, in Joules, in the BaO-MgO-Al₂O₃ system.

BMA ₅ -BA ₆ solid solution (BAM-lss)	
g^{0} (BaMgAl ₁₀ O ₁₇) = g^{0} (BA, HT) + g^{0} (MA, FACT) + 3 g^{0} (Al ₂ O ₃ , corr.) - 57218	
$q_{(BMA5-BA6)} = 0$	
$BaMg_{3}Al_{14}O_{25} (BM_{3}A_{7})$	
$\Delta H^0_{298} = -14346833 \text{ J/Mol}$ $S^0_{298} = 562.329 \text{ J/mol/K}$	$\Delta S^{0}_{298}{}^{(a)} = 0$
$T_{m}^{(b)} = 1945 \ ^{\circ}C$	
$C_p = 2 C_p (BA) + 6 C_p (MA, FACT53) + 6 (Al_2O_3, corr.) (298.15 < T < 2000 K)$	

^(a) from the compounds used to calculated the heat capacities

^(b) incongruent melting temperature



Fig. 3.14.1 Phase equilibria as reported by Gobbels et al.



Fig. 3.14.2 A part of the present calculated isothermal section at 1800 °C.



Fig. 3.14.3 Present calculated liquidus (polythermal) projection for the BaO-MgO-Al₂O₃ system (isotherms were drawn at the interval of 100 °C).

3.15 The BaO-Al₂O₃-SiO₂ system

In the BaO-Al₂O₃-SiO₂ system, to obtain the optimal fit of the available data, an additional component in the form of a $(BaAl_2)^{+8}$ associate was added to the liquid phase, i.e. $BaAl_2O_4$ was considered a separate component in the binary BaO-Al₂O₃ system (along with BaO and Al₂O₃). The introduction of these associates can be interpreted as the method to take the charge compensation effect (Chartrand and Pelton, 1999) into account. Chartrand and Pelton (1999)

introduced (NaAl)⁺⁴ associates to model the Na₂O-Al₂O₃-SiO₂ solutions. They explained that the dissolution of alumina in silica by the replacement of Si^{+4} in the tetrahedral network by Al^{+3} is energetically unfavourable because it results in a negative charge centre. However, upon addition of Na₂O this negative charge can be compensated by a Na⁺ ion placed next to the aluminum. In the BaO-Al₂O₃-SiO₂ system, replacement of one Si⁺⁴ in the tetrahedral network by one Al⁺³ and compensation by Ba⁺² will result in energetically unfavourable positive charge centre. This can be avoided by substituting two Si⁺⁴ ions next to each other by two Al⁺³ ions and Ba⁺² placed next to these aluminium ions. Thus, $(BaAl_2)^{+8}$ associates were treated as separate component of the liquid phase. The ternary solution was then formally treated as a quaternary solution with components BaO, Al₂O₃, SiO₂ and BaAl₂O₄. The standard Gibbs energy of the hypothetical pure component BaAl₂O₄, $g^{0}_{(BaAl2O4)}$, was fixed during optimization so that the $(BaAl_{2})^{+8}$ associates are practically unstable in the BaO-Al₂O₃ binary system. In the BaO-Al₂O₃ system, at 2000 °C and at $X_{A12O3} = 0.5$, the mole fraction of these associates is only 4.2 x 10⁻⁴. These associates were stabilized in the SiO₂-rich region of the ternary system by the help of a similar kind of Gibbs energies of formation model parameters as presented in Sec. 1.2.2 for the (NaAl)⁺⁴ associates. The present optimized parameters for the BaO-Al₂O₃-SiO₂ liquid phase are presented in Table 3.15.1. The Gibbs energy of the liquid phase in the BaO-Al₂O₃-SiO₂ system was calculated from the corresponding binary systems by treating SiO₂ as an asymmetric component i.e. BaO, Al₂O₃ and BaAl₂O₄ were kept in the same group (Pelton and Chartrand, 2001).

Thomas (1950) reported the primary phase fields in the composition ranges containing less than 30% Al₂O₃ and more than 20% SiO₂ by weight in the BaO-Al₂O₃-SiO₂ system by quenching,

petrography and XRD. Toropov, et al. (1954) studied the system by quenching and reported a polythermal liquidus projection for the ternary system. Foster and coworkers in a series of articles [Lin and Foster (1968); Foster and Lin (1969); Lin and Foster (1969); Semler and Foster (1969); Lin and Foster (1970); Semler and Foster (1970)] reported phase relationships in this ternary system mainly from quenching. Von Oehlschlegel and Ohnmacht (1975) studied the system by thermal analysis and quenching. All these studies agree on the presence of the ternary compound BaAl₂Si₂O₈ (BAS₂) as a stable phase. Lin and Foster (1968) presented a good literature review and performed experiments to study the polymorphism of BAS₂. They concluded that BAS₂ is monoclinic at room temperature, inverting reversibly to a hexagonal structure at 1590 °C. The hexagonal form is stable to the melting point at about 1760 °C. This polymorphic transformation at 1590 °C was taken into account by assuming, as no experimental data could be found in the literature, this enthalpy of transformation to be 100 J. However, more experimental work is required to accurately establish it.

Foster and Lin (1969) studied the BAS₂-SiO₂ section and presented its phase diagram. Foster and Lin (1969 also deduced the phase diagram of this section from the data of Thomas (1950) and Toropov, et al. (1954), who did not study this section separately. This deduced phase diagram showed SiO₂ to be incompatible with BAS₂. Foster and Lin (1969) presented arguments on the compatibility of silica with BAS₂. Later, Von Oehlschlegel and Ohnmacht (1975) also studied the BAS₂-SiO₂ system and proved the compatibility of silica with BAS₂. The data of Foster and Lin (1969) and Von Oehlschlegel and Ohnmacht (1975) are reasonably well reproduced in Fig. 3.15.1. The g^{00} and g^{05} parameters in Table 3.15.1 were used to fit this section. In a different work, Lin and Foster (1969) studied the BaSi₂O₅ (BS₂)-BAS₂ system. Lin and Foster (1969), from the data of Thomas (1950) and Toropov, et al. (1954) - who did not study this section separately - deduced a simple eutectic phase diagram for this section with substantial solid solution of BAS₂ in BS₂ close to the eutectic temperature. Lin and Foster (1969) also reported a simple eutectic phase diagram for this section but stated that there is no solubility of BAS_2 in BS_2 for compositions greater than 6% BAS_2 ; for smaller compositions they were unable to conclude anything from the experimental techniques employed. Von Oehlschlegel and Ohnmacht (1975) measured phase diagram for this section, in which phases $Ba_3Si_5O_{13}$ (B_3S_5) and Ba₅Si₈O₂₁ (B₅S₈) also appeared, contrary to the data of Lin and Foster (1969). Von Oehlschlegel and Ohnmacht (1975) also did not report any mutual solubility among these phases. The data of Lin and Foster (1969) and Von Oehlschlegel and Ohnmacht (1975) are reasonably well reproduced in Fig. 3.15.2. No mutual solubility among the terminal phases was considered in the present work. The g^{001} parameter in Table 3.15.1 was used to fit the BS₂-BAS₂ section. The positive enthalpy and temperature dependent entropy terms in the g^{001} parameter were required to simultaneously fit the eutectic temperature and liquidus data on this section.

Von Oehlschlegel and Ohnmacht (1975) also reported phase diagram for the sections BAS_2 - $Ba_2Si_3O_8$ (B_2S_3) and BAS_2 - $Ba_5Si_8O_{21}$ (B_5S_8). They reported a simple eutectic phase diagram for the section BAS_2 - B_2S_3 , whereas in the BAS_2 - B_5S_8 section the B_2S_3 phase also appeared. Their data are reasonably well reproduced in Figs. 3.15.3 and 3.15.4.

Semler and Foster (1969) studied the sections $BAS_2-Al_2O_3$ and BAS_2 -mullite. These data are well reproduced in Figs. 3.15.5 and 3.15.6 respectively. The mullite phase appearing in the Al_2O_3 -SiO₂ system was modeled as a non-stoichiometric phase [Swamy, Jung, and Decterov (2009)]. In the present calculations, to obtain an optimal fit of the available data, the BAS_2 -mullite section was calculated at the mullite composition $(Al_2O_3)_{0.65}(SiO_2)_{0.35}$.

Lin and Foster (1970) studied the primary phase field regions in the ternary sub-system BS₂-BAS₂-SiO₂. These data are compared with the present calculations in Fig. 3.15.7 which also contains data by Thomas (1950) and Toropov, et al. (1954). With the help of these data, Lin and Foster (1970) reported a ternary eutectic at 1122±7 °C and a composition of BaO 35.2, Al₂O₃ 9.5, and SiO₂ 55.3 wt.%. The present calculated ternary eutectic temperature is 1116 °C and composition of BaO 38.4, Al₂O₃ 7.2, and SiO₂ 54.8 wt.%. In a different work, Semler and Foster (1970) studied the ternary sub-system BAS₂-SiO₂-Al₂O₃. They reported primary phase fields for these phases and an isothermal section at 1400 °C. These data are compared with the present calculations in Figs. 3.15.7 and 3.15.8 respectively. Semler and Foster (1970) reported a ternary eutectic in this ternary-subsystem at 1296±3 °C and of composition BaO 19, Al₂O₃ 15, and SiO₂ 66 wt%. The present calculated ternary eutectic temperature is 1230 °C and composition BaO 17.0, Al₂O₃ 18.5, SiO₂ 64.5 wt%. As evident in Fig. 3.15.7, there is also disagreement with the data by Semler and Foster (1970) on the primary phase region of mullite phase in this region. In the present calculations, simultaneous fitting of this eutectic temperature, with the primary phase region and experimental data in Figs. 3.15.1 and 3.15.6 by Foster and coworkers, was found to be very difficult. The g^{101} and g^{102} parameters were used to simultaneously fit the experimental data in Fig. 3.15.6 and the ternary eutectic temperature reported by Semler and Foster. The positive enthalpy and negative entropy terms in these parameters were required to simultaneously fit the ternary eutectic temperature, which lie at comparatively lower temperature, and the liquids data in Fig. 3.15.6.

Toropov, et al. (1954), apart from BAS₂, reported another ternary compound of composition $3BaO.3Al_2O_3.2SiO_2$ (B₃A₃S₂). They reported this compound as non-stoichiometric, melting incongruently at 1550 °C into BA and liquid. There are data in the literature [Gebert (1968); Kockel and Oehlschlegel (1969)] for the presence of another ternary compound, BaAl₂SiO₆ (BAS). However, Toropov, et al. (1954) did not report this phase as stable. No other evidence in the literature on the presence of the B₃A₃S₂ phase could be found. In the present work, the BAS phase was included as stoichiometric phase and the presence of the B₃A₃S₂ phase, close to the BAS composition, was neglected.

Lapina, Semenov, and Khodakovskii (1989) performed calorimetric measurements to report a standard heat of formation (H_{298}^0) and enthalpy increment at 700 °C (H_{973} – H_{298}) for the BAS₂ compound. As shown in Table 3.15.1, this value of ΔH_{298}^0 was used for the BAS₂ phase. Chernyshova et al. (1991) by DSC measured the heat capacity for the compound in the temperature range 39-439 °C. Therefore, up to 439 °C the heat capacity equation reported by Chernyshova, et al. (1991) was used. Above this temperature, the heat capacity was extrapolated as shown in Fig. 3.15.9 where it is also compared with the sum of the heat capacities of constituent compounds. With the optimized heat capacity of the BAS₂ phase, the H_{973} – H_{298} value

reported by Lapina, et al. (1989) is well reproduced, as shown in Table 3.15.1. Other than these, no thermodynamic data for the ternary compounds were found in the literature. The calculated standard entropies of formation for the ternary compounds are less than 8 J/(mol of metal) which is quite reasonable.

 $\frac{Table \ 3.15.1 \ Optimized \ thermodynamic \ parameters, \ in \ Joules, \ in \ the \ BaO-Al_2O_3-SiO_2 \ system.}{LT-BaAl_2Si_2O_8 \ (BAS_2(LT))}$

0				
$\Delta H^{0}_{298} = -4244300 \text{ J/mol}$	Exp. = $-4244300 \pm 1200 \text{ J/mol}$ [Lapina et al., '89]			
H_{973} – $H_{298} = 191.885$ kJ/mol	Exp. = 190.600 ± 2.2 kJ/mol [Lapina et al., '89]			
$S_{298}^0 = 246.500, \qquad \Delta S_{298}^{0}{}^{(a)} = 40.691$				
$C_p = 261.05 + 0.0664 T - 5256000 T^2$ (298 < T < 712 K) [Chernyshova et al., '91]				
$C_p = 234 + 0.108 T - 2.5E-5 T^2 (712 < T < 2200 K)$				
HT-BaAl ₂ Si ₂ O ₈ (BAS ₂ (HT))				
$\Delta H^{tr} = 100 \text{ J}$ (at 1590 °C)				
$Cp = same as LT-BAS_2$				
$T_m^{(b)} = 1763$ °C, Experimental = 1760 [Lin and Foster, '	68]			
BaAl ₂ SiO ₆ (BAS)				
$\Delta H^{0}_{298} = -3333000 \qquad S^{0}_{298} = 171 \qquad \Delta S^{0}_{298}^{(a)} = 6.65$	51			
$C_p = C_p (BaO) + C_p (Al_2O_3) + C_p (SiO_2,S2) (298 < T < 200)$	00 K) $T_{\rm m}^{(b)} = 1673$			
Liquid phase (Ternary interaction parameters) (in Joules)				
$g^{\theta}_{BaAl2O4} = g^{\theta}(BaO, l) + g^{\theta}(Al_2O_3, l) - 138072 + 2.092 T$				
$g^{00}{}_{BaAl2-Si} = -56484$; $g^{05}{}_{BaAl2-Si} = 41840 - 14.644$ T				
$g^{001}_{BaA12-Si(Ba)} = 33472 - 41.840 T$				
$g^{I0I}_{BaAl2-Si(Al)} = 25104 - 71.128 T; g^{I02}_{BaAl2-Si(Al)} = 100416$	5 – 15.899 <i>T</i>			

(a) oxides (stable at room-temperature) as reference

^(b) congruent melting temperature



Fig. 3.15.1 Optimized phase diagram of the SiO₂-BaAl₂Si₂O₈ (BAS₂) section.



Fig. 3.15.2 Optimized phase diagram of the BaSi₂O₅(BS₂)-BaAl₂Si₂O₈ (BAS₂) section.



Fig. 3.15.3 Optimized phase diagram of the Ba₂Si₃O₈(B₂S₃)-BaAl₂Si₂O₈(BAS₂) section.



Fig. 3.15.4 Optimized phase diagram of the $Ba_5Si_8O_{21}(B_5S_8)$ - $BaAl_2Si_2O_8(BAS_2)$ section.



Fig. 3.15.5 Optimized phase diagram of the BaAl₂Si₂O₈ (BAS₂)-Al₂O₃ section.



Fig. 3.15.6 Optimized phase diagram of the BaAl₂Si₂O₈ (BAS₂)-Mullite (Al_{1.3}Si_{0.35}O_{2.65}) section.



Fig. 3.15.7 Polythermal projection of the BaO-Al₂O₃-SiO₂ system (for clarity, only univariant lines are shown).



Fig. 3.15.8 Isothermal section at 1400 °C in the BaO-Al₂O₃-SiO₂ system.



Fig. 3.15.9 Optimized heat capacity of the $BaAl_2Si_2O_8$ phase compared with other heat capacity schemes.

3.16 The SrO-Al₂O₃-SiO₂ system

In the $SrO-Al_2O_3-SiO_2$ system, to obtain the optimal fit of the available data an additional component in the form of (SrAl₂)⁺⁸ associates was added to the liquid phase. As explained in the BaO-Al₂O₃-SiO₂ system, the introduction of these associates can be interpreted as the method to take the charge compensation effect (Chartrand and Pelton, 1999) into account. This effect is explained as the substitution of two Si^{+4} ions, next to each other in the tetrahedral network, by two Al^{+3} ions. Sr^{+2} ion can be placed next to these aluminium ions to compensate the charge. Thus, $(SrAl_2)^{+8}$ associates were treated as separate component of the liquid phase. The ternary solution was then formally treated as a quaternary solution with components SrO, Al_2O_3 , SiO₂ and $SrAl_2O_4$. The standard Gibbs energy of the hypothetical pure component $SrAl_2O_4$, $g^0_{(SrAl_2O_4)}$, was fixed during optimization so that the $(SrAl_2)^{+8}$ associates are practically unstable in the SrO-Al₂O₃ binary system. In the SrO-Al₂O₃ system, at 2050 °C and at $X_{Al2O3} = 0.5$, the mole fraction of these associates is only 4.4 x 10⁻⁴ mole. The Gibbs energy of the liquid phase in the SrO- Al_2O_3 -SiO₂ system was calculated from the corresponding binary systems by treating SiO₂ as an asymmetric component i.e. SrO, Al₂O₃ and SrAl₂O₄ were kept in the same group (Pelton and Chartrand, 2001). The optimized parameters for the SrO-Al₂O₃-SiO₂ ternary systems are presented in Table 3.16.1. During simultaneous optimization, effort was made to use parameters for the liquid phase which are similar in form as obtained for the liquid phase in the BaO-Al₂O₃-SiO₂ system. The parameters which gave optimal fit of the available data in the SrO-Al₂O₃-SiO₂ system are presented in Table 3.16.1. It can be seen that all the parameters, except the g^{011} , are same in form as used for the BaO-Al₂O₃-SiO₂ system. The g^{011} parameter was required to obtain good fit in the SrO-rich regions.

Dear (1957a) by quenching techniques reported sub-solidus phase equilibria at 1350 °C, presented in Fig. 3.16.1, in the SrO-Al₂O₃-SiO₂ system. These phase equilibria can be compared with the present calculations in Fig. 3.16.2. The assumption of the low-temperature decomposition of the Sr₃S helped in fitting these data. Hence, this low-temperature decomposition was calculated in the binary SrO-SiO₂ system as shown in Fig. 2.4.1. However, more experimental work is required to corroborate this decomposition. Dear (1957a) did not find the liquid phase to be stable at 1350 °C at any composition. The binary eutectic temperature between the SrS and SiO₂ phases in the binary SrO-SiO₂ system is about 1350 °C. Therefore, the ternary eutectic between SrS, SiO₂ and SrAS₂ phase is expected to be below 1350 °C. In fact, similar eutectics in the CaO-Al₂O₃-SiO₂ and BaO-Al₂O₃-SiO₂ systems lie at 1184 and 1116 °C. There are data in the Sci-Glass database on liquidus temperatures at compositions in the subsystem SrS-SrAS₂-SiO₂ which show the presence of the liquid phase well below 1350 °C. However, exact fitting of these liquidus data will reproduce a eutectic below 1000 °C in this ternary subsystem. Therefore, these liquidus data were fitted as shown in Table 3.16.2 to reproduce the eutectic at 1179 °C (close to that of CaO-Al₂O₃-SiO₂ system). Moreover, in general, the liquidus temperatures reported in the Sci-Glass database are not true liquidus temperature. They are the temperatures below which solids (crystals) from within a few hours, generally within 6-12 h, and remain in the liquid [Wallenberger and Smrcek (2010)]. These temperatures are to check the resistance to the development of devitrification in the glass manufacturing conditions [Dumbaugh (1992)]. Dear reported three stable ternary phases: SrAl₂Si₂O₈ (SrAS₂), Sr₂Al₂SiO₇ (Sr₂AS), Sr₆Al₁₈Si₂O₃₇ (Sr₆A₉S₂). The optimized parameters for these phases are presented in Table. 3.16.1. As reported earlier, the S₄A₇ and SA₂ phases, which were not obtained by Dear (1957a) as equilibrium phases, are considered stable in the binary $SrO-Al_2O_3$ phase diagram. Hence, they appear in the present calculations at 1350 °C.

Starczewski (1964) by thermal analysis studied various isoplethal sections in the system and reported the data under the name "average temperature of melting". This name suggests that the thermal analysis peaks reported by Starczewski (1964) should correspond to the temperature at which melting starts at a particular composition (solidus or invariant temperature). The optimal fit of these data is presented in Figs. 3.16.3-3.16.18. It can be seen that the thermal peaks obtained by Starczewski (1964) correspond to various phase transitions, not necessarily to solidus or invariant temperatures. It must be noted that Starczewski (1964) reported higher melting temperatures than the other available experimental data by Hanic, et al. (1979) in the SrO-rich region in the binary SrO-Al₂O₃ system (see section SrO-Al₂O₃). The present calculations fit the data by Hanic, et al. (1979) comparatively better in this region. In the ternary isoplethal sections as well there is disagreement between Starczewski's higher melting temperatures at the SrO-rich compositions and the present calculations. In view of the inconsistency of Starczewski's data in the SrO-rich region in the binary SrO-Al₂O₃ system, his experimental data on the melting temperatures at the SrO-rich compositions in the ternary isopleths sections were given less weight. Starczewski (1964) reported congruent melting temperature of 1765 °C for the SrAS₂ phase and incongruent melting temperature of 1705 °C for the Sr₂AS phase. Bambauer, Schoeps, and Pentinghaus (1984) reported congruent melting point of the SrAS₂ phase at 1656 °C. The present calculated congruent melting temperatures for these phases are 1654 and 1704 °C

respectively. The present calculated liquidus (polythermal) projection for the $SrO-Al_2O_3-SiO_2$ system is presented in Fig. 3.16.20.

Lapina, et al. (1989) performed calorimetric measurements and reported the standard enthalpy of formation (H_{298}^0) and an enthalpy increment at 700 °C (H_{973} – H_{298}) for the SrAS₂ compound. As shown in Table 3.16.1, this value of ΔH_{298}^0 was used for the SrAS₂ phase. Chernyshova, et al. (1991) by DSC measured the heat capacity for the compound in the temperature range 39-439 °C. Their measured heat capacities were quite close to the heat capacity obtained by adding the heat capacities of constituent oxides. Therefore, up to 439 °C the heat capacity equation reported by Chernyshova, et al. (1991) was used and above this temperature the heat capacity was calculated as sum of the constituent oxides. This scheme of heat capacity is also plotted in Fig. 3.16.19 where it is compared with the heat capacity obtained by adding the heat capacities of constituent compounds. Using this scheme of heat capacity for the SrAS₂ phase, the $(H_{973}-H_{298})$ value reported by Lapina, et al. (1989) is well reproduced as shown in Table 3.16.1. Massazza and Fadda (1966) by solution calorimetry reported the standard heat of formation from oxides (ΔH^0_{298}) for the Sr₂AS phase which is compared with the present calculated value in Table 3.16.1. The present calculated value is more negative than was required to reproduce the data in Fig. 3.16.2 reported by Dear (1957a). The datum by Massazza and Fadda (1966) would make the Sr₂AS phase to decompose at the lower temperatures. The standard entropies of formation from oxides (ΔS^{0}_{298}) for the three ternary compounds are always less than 7 J/(mol of metal) which is quite reasonable.

 $\frac{Table \ 3.16.1 \ Optimized \ thermodynamic \ parameters, \ in \ Joules, \ in \ the \ SrO-Al_2O_3-SiO_2 \ system.}{SrAl_2Si_2O_8 \ (SrAS_2)}$

$\Delta H^{0}_{298} = -4248000 \text{ J/mol}$	Exp. = -4248000 ± 4700 J/mol [Lapina et al., '89]		
H_{973} – $H_{298} = 192.840$ kJ/mol	Exp. = 185.800 ± 1.8 kJ/mol [Lapina et al., '89]		
S ⁰ ₂₉₈ = 209.854 J/mol/K	$\Delta S_{298}^{0}{}^{(a)} = 22.534$ $\Delta S_{298}^{0}{}^{(a)} = -0.945$		
$T_m^{(c)} = 1654 \text{ °C}, \text{Exp.}^{(c)} = 1765 \text{ [Starczewski, '64]} \text{ Exp.}^{(c)} = 1656 \text{ [Bambauer et al, '84]}$			
$C_p = 269.59 + 0.05784 T - 5833000 T^2 (298 < T < 712 K)$ [Ch	ernyshova et al., '91]		
$C_p = C_p (SrO) + C_p (Al_2O_3) + 2 Cp (SiO_2,S2) (712 < T < 2000)$	K)		
$Sr_2Al_2SiO_7(Sr_2AS)$			
$\Delta H^{0}_{298} = -3989732 \qquad S^{0}_{298} = 235.700 \qquad \Delta S^{0}_{298} = 36.$	$\Delta S_{298}^{0(b)} = 12.221$		
$\Delta H^{0}_{298}{}^{(a)} = -219032 \qquad \qquad \text{Exp.} = -173050.24$	J/mol [Massazza and Fadda, '66]		
$C_p = C_p (SrSiO_3) + C_p (SrAl_2O_4, HT)$ (298<7<2000 K)	$T_m^{(c)} = 1704 \ ^{\circ}C, Exp.^{(d)} = 1705 \ [Starczewski, 64]$		
$Sr_{6}Al_{18}Si_{2}O_{37} (Sr_{6}A_{9}S_{2})$			
$\Delta H^{0}_{298} = -21133330 \qquad S^{0}_{298} = 992.000 \qquad \Delta S^{0}_{298} = 130$	$0.220 \qquad \Delta S^{0}_{298}{}^{(b)} = -8.933$		
$C_p = 6 C_p (SrAl_2O_4, HT) + 2 C_p (Al_2SiO_5, S1)(FACT) + 1 C_p$, (Al ₂ O ₃) (298 < T < 2000 K) $T_{\rm m}^{\rm (d)} = 1760 {}^{\circ}{\rm C}$		
Liquid phase (Ternary interaction parameters) (in Joules)			
$g^{0}_{SrAl2O4} = g^{0}(SrO,l) + g^{0}(Al_{2}O_{3},l) - 112968 + 2.092 T$			
$g^{00}_{SrAl2-Si} = -42677$; $g^{05}_{SrAl2-Si} = 33472 - 5.201 T$			
$g^{001}_{SrA12-Si(Sr)} = 39748 - 41.840 T$			
$g^{I0I}_{SrAl2-Si(Al)} = 50208 - 41.840 T$			
$g^{011}_{Si-Al(Sr)} = 146440$			

^(a) oxides (stable at room-temperature) as reference, ^(b) compounds used to calculate heat capacity as reference ^(c) congruent melting temperature, ^(d) incongruent melting temperature

Table 3.16.2	Calculated liquidus	temperature	compared	with the	experimental	data from	the Sci-
Glass databas	se.						

GNo	SiO2	Al2O3	SrO	Exp.	Present
62083	61.1	10.0	28.9	1260	1319
62084	61.2	12.8	26.0	1215	1425
62085	60.0	11.3	28.7	1215	1379
62086	60.0	14.1	25.9	1321	1466
62087	58.7	8.4	32.8	1163	1248
62088	58.8	11.2	30.0	1201	1380
62089	58.8	14.0	27.1	1308	1471
62090	57.6	11.2	31.2	1155	1386
62091	56.4	9.7	33.8	1145	1326
62092	56.4	11.1	32.4	1100	1388
62093	55.3	11.0	33.6	1145	1389
62094	56.2	11.0	34.8	1150	1381
62095	54.2	11.7	34.2	1160	1421
62096	51.9	10.8	37.2	1150	1397



Fig. 3.16.1 Solid-phase relationships at 1350 °C as reported by Dear.



Fig. 3.16.2 Present calculated isothermal section at 1350 °C.



Fig. 3.16.3 Optimized phase diagram of isoplethal section $Al_2O_3=0.10$ in the SrO- Al_2O_3 -SiO₂ system.



Fig. 3.16.4 Optimized phase diagram of isoplethal section $Al_2O_3=0.15$ in the SrO- Al_2O_3 -SiO₂ system.



Fig. 3.16.5 Optimized phase diagram of isoplethal section $Al_2O_3=0.20$ in the SrO- Al_2O_3 -SiO₂ system.



Fig. 3.16.6 Optimized phase diagram of isoplethal section $Al_2O_3=0.25$ in the SrO- Al_2O_3 -SiO₂ system.


Fig. 3.16.7 Optimized phase diagram of isoplethal section $Al_2O_3=0.30$ in the SrO- Al_2O_3 -SiO₂ system.



Fig. 3.16.8 Optimized phase diagram of isoplethal section $Al_2O_3=0.35$ in the SrO- Al_2O_3 -SiO₂ system.



Fig. 3.16.9 Optimized phase diagram of isoplethal section $Al_2O_3=0.40$ in the SrO- Al_2O_3 -SiO₂ system.



Fig. 3.16.10 Optimized phase diagram of isoplethal section $Al_2O_3=0.45$ in the SrO- Al_2O_3 -SiO₂ system.



Fig. 3.16.11 Optimized phase diagram of isoplethal section $Al_2O_3=0.50$ in the SrO- Al_2O_3 -SiO₂ system.



Fig. 3.16.12 Optimized phase diagram of isoplethal section $SiO_2=0.10$ in the SrO-Al₂O₃-SiO₂ system.



Fig. 3.16.13 Optimized phase diagram of isoplethal section $SiO_2=0.15$ in the SrO-Al₂O₃-SiO₂ system.



Fig. 3.16.14 Optimized phase diagram of isoplethal section $SiO_2=0.20$ in the SrO-Al₂O₃-SiO₂ system.



Fig. 3.16.15 Optimized phase diagram of isoplethal section $SiO_2=0.25$ in the SrO-Al₂O₃-SiO₂ system.



Fig. 3.16.16 Optimized phase diagram of isoplethal section $SiO_2=0.30$ in the SrO-Al₂O₃-SiO₂ system.



Fig. 3.16.17 Optimized phase diagram of isoplethal section $SiO_2=0.40$ in the SrO-Al₂O₃-SiO₂ system.



Fig. 3.16.18 Optimized phase diagram of isoplethal section $SiO_2=0.50$ in the SrO-Al₂O₃-SiO₂ system.



Fig. 3.16.19 Optimized heat capacity of the $SrAl_2Si_2O_8$ phase compared with the other heat capacity scheme.



Fig. 3.16.20 Present calculated liquidus (polythermal) projection for the SrO-Al₂O₃-SiO₂ system (isotherms were drawn at the interval of 100 $^{\circ}$ C).

3.17 The BaO-B₂O₃-SiO₂ system

The Gibbs energy of the liquid phase in the $BaO-B_2O_3-SiO_2$ ternary system was calculated from the corresponding binary systems by treating BaO as asymmetric component [Pelton and Chartrand (2001)]. The optimized parameters for this ternary system are presented in Table. 3.17.1. For the liquid phase, ternary interaction parameters presented in Table 3.17.1, were also used to obtain the optimal fit of the available data. Levin and Ugrinic (1953) performed a detailed study on the system by the classical quenching method. Their data are reasonably well reproduced in Figs. 3.17.1 to 3.17.7. Levin and Ugrinic (1953) reported continuous solubility between the binary phases BS_2 and B_2S_3 . However, as reported in the BaO-SiO₂ section, this binary system was optimized based on later investigations which disproved this complete solubility, reporting two stoichiometric compounds (B5S8 and B_3S_5) between these compositions. Therefore, the solid solubility between the phases BS_2 and B_2S_3 reported by Levin and Ugrinic (1953) does not appear in the present calculations. They also reported the presence of a ternary compound Ba₃B₆Si₂O₁₆ (Ba₃B₂S₂). No thermodynamic data for this phase could be found in the literature. This phase was modeled as stoichiometric and the optimized properties of this phase are presented in Table. 3.17.1. The liquidus temperature (the temperature at which first solid precipitates from the liquid phase) at various compositions as reported by Levin and Ugrinic (1953) are compared with the present calculations in Table 3.17.2. Hamilton, et al. (1958) by thermal analysis reported isoplethal sections (at constant BaO mol%) in this ternary system. The optimal fit of these data is presented in Figs. 3.17.8-3.17.13. Levin and Cleek (1958) with a temperature gradient apparatus determined dome temperatures (the boundary surface separating the two-liquid region from the one-liquid region). The samples were kept in open cells for 5 to 15 minutes in a horizontal tube furnace maintained in a stable temperature gradient. The quenched samples were then analyzed. The position in the gradient corresponding to the dome temperature was considered to lie midway between the sample-cell showing evidence of single-liquid formation and that showing two-liquid phases in petrographic examinations. In the present modeling, the reproduction of the two liquids region in Fig. 3.17.7, as reported by Levin and Ugrinic (1953), required much higher dome temperatures than reported by Levin and Cleek (1958) as shown in Table 3.17.3. It was observed during calculations that dome temperatures reported by Levin and Cleek (1958) could be fitted more closely had there be no stable immiscibility region in the binary BaO-SiO₂ system. As reported in the binary BaO-SiO₂ section that there are data reporting both stable and metastable immiscibility region in the silica region part of the BaO-SiO₂ system. But, it was found very difficult to suppress the sable liquid miscibility gap in the SiO₂ region simultaneously with the reproduction of the flat liquidus of SiO₂ as reported by Greig (1927). Hence, it can be said that more experimental work is required to corroborate the dome temperature data of Levin and Cleek (1958). For this ternary immiscibility gap, the monotectic temperature (Table 3.17.2) and monotectic composition (Fig. 3.17.7) are comparatively well reproduced.

Z. G. Tyurnina, Lopatin, and Stolyarova (2008), at 1377 °C and 1457 °C, by high-temperature mass spectrometry measured the activities in the BaO-B₂O₃-SiO₂ melt at constant BaO mol%. These activities are compared with the present calculated activities at 1427 °C (according to the present calculations, the activities at 1377 and 1457 °C are practically the same) in Figs. 3.17.14-3.17.18. (the different experimental points at the same composition in these figures correspond to the two different temperature; in the scale of these figures there is practically no difference in the calculated activities in this temperature range. Therefore the present calculations were performed at 1417 °C). It must be noted that Tyurnina and coworkers measured some of these activities in the two-phase liquid region (for $X_{BaO} = 0.1$ and 0.2). Achievement of equilibrium in such a highly viscous liquid phase, especially in the two-phase region, is quite sluggish. Tyurnina and coworkers did not mention in their publication the time given to samples to reach equilibrium. Moreover, careful analyses of their data make them dubious. For example, in Figs. 3.17.14-

3.17.18 the silica activity first increases and then decreases with increasing silica content. This is not possible because increasing silica content should increase silica activity. At $X_{BaO} = 0.5$ (Fig. 3.17.18), the BaO activity is higher than that of SiO_2 and B_2O_3 . In the present work, many ternary phase diagram data in this region and temperature range were reproduced quite well. Therefore, it seems unlikely that the present calculated BaO activities can deviate so much from the experimental data. More experimental work is required to corroborate these activities data from Tyurnina and coworkers.

Table 3.17.1 Optimized thermodynamic parameters, in Joules, in the BaO-B₂O₃-SiO₂ system.

$S^{0}_{298} = 577.500$ $\Delta S^{0}_{298} = 48.009$	$\Delta S^{0}_{298}{}^{(a)} = 116.523$	
290		
ters) (in Joules)		
	$S_{298}^{0} = 577.500$ $\Delta S_{298}^{0} = 48.009$ ters) (in Joules)	$S_{298}^{0} = 577.500 \qquad \Delta S_{298}^{0} = 116.523$ $\Delta S_{298}^{0} = 48.009 \qquad $

(a) oxides (stable at room-temperature) as reference (b) compounds used to calculate the heat capacity as reference

^(c) congruent melting temperature

Diff. S.No. SiO₂ Experimental Present BaO B_2O_3 -50 1 33.77 51.21 15.02 1066 1016 2 35.16 12.95 1103 1062 51.89 -41 3 39.23 53.83 6.94 1243 1224 -19 4 26.49 54.6 18.91 1002 984 -18 5 999 987 25.91 54.61 19.48 -12 15.78 6 29.28 54.94 1055 1021 -34 7 33.14 55.16 11.7 1150 1106 -44 8 37.49 55.58 6.93 1243 1230 -13 9 16.95 1050 1002 -48 27.36 55.69 1345 10 40.76 56.35 2.89 1349 4 11 38.14 56.56 5.3 1277 1288 11 1078 12 28.68 56.71 14.61 1048 -30 13 34.28 56.89 8.83 1214 1183 -31 14 29.91 57.25 12.84 1089 -41 1130 15 24.21 57.73 18.06 1023 992 -31 23.33 1005 991 -14 16 57.81 18.86 17 24.2 58.6 17.2 1048 1012 -36 18 23.22 59.15 17.63 1010 1007 -3 19 24.74 59.47 15.79 1049 1042 -7 20 26.18 -5 59.88 13.94 1085 1080 21 34.01 59.02 6.97 1238 1248 10 7 22 33.01 59.98 7.01 1244 1251 -5 23 23.63 60.21 16.16 1042 1037 3 24 27.76 60.41 11.83 1125 1128 25 24.98 60.49 14.53 1073 1070 -3 26 28.06 61.13 10.81 1152 1154 2 27 3 20.45 61.42 18.13 1000 1003 28 29.64 61.46 8.9 1201 1202 1 29 31.57 61.47 6.96 1245 1255 10 30 30.69 61.68 7.63 1226 1237 11 24.86 13.4 1089 1095 6 31 61.74 32 23 62.29 14.71 1064 1067 3 33 34.61 62.49 2.9 1365 1371 6 34 19.17 994 999 5 62.53 18.3 35 21.05 62.87 16.08 1040 1039 -1 36 19.2 63.42 1001 1013 12 17.38

Table 3.17.2 Liquidus temperature as reported by Levin and Ugrinic (Exp.) compared with the present calculations. (Compositions in wt.%)

37	33.36	63.59	3.05	1350	1366	16
38	26.07	64.8	9.13	1182	1192	10
39	18.13	64.92	16.95	1001	1017	16
40	18.78	66.01	15.21	1036	1044	8
41	15.13	66.62	18.25	976	979	3
42	21.23	67.15	11.62	1102	1112	10
43	23.68	67.22	9.1	1164	1173	9
44	14.35	67.52	18.13	947	970	23
45	15.68	67.65	16.67	982	997	15
46	22.31	67.81	9.88	1145	1146	1
47	15.71	68.48	15.81	995	1002	7
48	14.24	68.57	17.19	965	973	8
49	23.45	68.61	7.94	1237	1193	-44
50	12.3	70.02	17.68	964	965	1
51	14.07	70.22	15.71	1016	980	-36
52	21.1	71.04	7.86	1305	1212	-93
53	10.3	72.01	17.69	975	963	-12
54	15.87	72.08	12.05	1189	1074	-115
55	15.96	74.13	9.91	1250	1189	-61
56	6.91	74.93	18.16	961	993	32
57	12.23	75.69	12.08	1160	1188	28
58	5.7	76.06	18.24	950	1012	62
59	8.19	76.11	15.7	1038	1094	56
60	5.29	76.83	17.88	954	1034	80
61	4.86	77.61	17.53	959	1055	96
62	4.64	78.02	17.34	962	1065	103
63	16.04	76.01	7.95	1308	1335	27
64	12.75	76.71	10.54	1263	1276	13
65	10.23	77.99	11.78	1224	1277	53
66	5.48	78.4	16.12	1055	1121	66
67	7.85	78.72	13.43	1274	1235	-39
68	6.41	79.16	14.43	1223	1201	-22
69	2.42	77.82	19.76	910	931	21
70	3.54	80.04	16.42	1077	1098	21
71	1.9	83.05	15.05	1206	1165	-41
72	1.33	54.88	43.79	897	903	6
73	2.16	56.46	41.38	926	934	8
74	9.07	62.8	28.13	1002	1005	3
75	8.11	63.47	28.42	1028	1017	-11
76	6.01	64.93	29.06	1054	1042	-12
77	11.68	65.09	23.23	993	999	6

78	11.12	65.82	23.06	992	1004	12
79	12.94	66.98	20.08	969	984	15
80	11.48	67.22	21.3	984	998	14
81	7.03	69.41	23.56	1025	1035	10
82	4.69	69.58	25.73	1077	1059	-18
83	9.09	69.84	21.07	1003	1008	5
84	11.44	70.24	18.32	962	974	12
85	9.96	71.38	18.66	968	978	10
86	3.07	71.41	25.52	1057	1063	6
87	6.14	74.23	19.63	951	978	27
88	6.45	74.7	18.85	939	969	30
89	3	77	20	925	940	15
90	5.66	39.3	55.04	845	860	15
91	6.94	40.26	52.8	841	858	17
92	3.62	40.57	55.81	858	870	12
93	2.49	42.42	55.09	877	880	3
94	10.1	42.65	47.25	841	851	10
95	11.21	43.49	45.3	840	850	10
96	5.98	44.21	49.81	870	868	-2
97	7.31	46.25	46.44	885	862	-23
98	4.39	48.05	47.56	884	876	-8
99	4.55	48.55	46.9	884	876	-8
100	1.39	52.9	45.71	906	898	-8
101	1.94	53.69	44.37	897	893	-4
102	20	18	62	874	858	-16
103	33.65	23.24	43.11	830	847	17
104	15.38	29.63	54.99	841	857	16
105	7.69	32.33	59.98	861	859	-2
106	4.81	33.34	61.85	870	860	-10
107	2.4	34.18	63.42	875	845	-30
108	3.43	36.7	59.87	864	861	-3
109	5.44	37.62	56.94	854	815	-39
110	4.88	38.71	56.41	845	861	16
111	2.81	39.33	57.86	861	870	9
112	50	17.51	32.49	830	941	111
113	42.97	29.85	27.18	1018	1050	32
114	50.62	34.13	15.25	1350	1292	-58
115	18.55	42.63	38.82	915	930	15
116	8.81	39.28	51.91	826	856	30
117	11.12	40.36	48.52	838	852	14
118	13.2	41.37	45.43	834	847	13

119	14.17	41.81	44.02	860	859	-1
120	15.53	42.46	42.01	860	888	28
121	16.11	43.91	39.98	891	906	15
122	34.83	45.05	20.12	1102	1122	20
123	21.92	45.56	32.52	955	958	3
124	26.39	47.69	25.92	1101	968	-133
125	28.72	48.79	22.49	1008	964	-44
126	27.87	49.79	22.34	1005	967	-38
127	30.98	49.89	19.13	1015	957	-58
128	32.47	50.59	16.94	1032	977	-55
129	26.74	50.64	22.62	1002	975	-27
130	27.9	50.69	21.41	1005	972	-33
131	25.49	51.43	23.08	1000	981	-19
132	13.15	44.98	41.87	850	845	-5
133	14.26	45.8	39.94	897	898	1
134	8.08	47.43	44.49	904	883	-21
135	17.03	47.92	35.05	965	938	-27
136	8.77	48.49	42.74	924	903	-21
137	9.12	49.02	41.86	936	913	-23
138	4.79	49.25	45.96	890	877	-13
139	5.03	49.95	45.02	904	885	-19
140	20.91	50.85	28.24	986	979	-7
141	26.8	52.06	21.14	995	980	-15
142	22.58	52.09	25.33	997	989	-8
143	11.12	52.1	36.78	985	963	-22
144	2.69	53.41	43.9	900	889	-11
145	24.52	53.56	21.92	998	992	-6
146	15.56	53.66	30.78	1003	994	-9
147	18.71	54.11	27.18	1000	1001	1
148	21.31	54.32	24.37	1001	1001	0
149	6.17	54.38	39.45	957	949	-8
150	24.87	54.46	20.67	999	992	-7
151	9.26	55.24	35.5	988	982	-6
152	11.76	55.72	32.52	1002	998	-4
153	13.97	56.56	29.47	1005	1009	4
154	16.06	57.15	26.79	1008	1012	4
155	17.96	57.67	24.37	1008	1012	4
156	7.43	57.72	34.85	985	984	-1
157	18.51	57.83	23.66	1005	1010	5
158	20.06	58.11	21.83	1005	1005	0
159	15.22	58.3	26.48	1013	1014	1

160	21.86	58.63	19.51	1002	994	-8
161	21.75	59.82	18.43	997	996	-1
162	19.21	61.3	19.49	995	987	-8
163	11.07	61.41	27.52	1007	1003	-4
164	14.33	62.44	23.23	996	995	-1
165	15.56	63.13	21.31	998	984	-14
166	17.1	64.2	18.7	978	987	9
167	13.84	64.77	21.39	985	979	-6
168	12.49	65.41	22.1	972	992	20

Table 3.17.3 Dome temperatures as reported by Levin and Cleek (Exp.) compared with the present calculations (Cal.). (Compositions in wt.%).

BaO	B_2O_3	SiO ₂	Exp.	Cal.
31.8	65.5	2.7	864-877	1008
30.3	60.7	9	995-1004	1177
32.5	56.2	11.3	953	1170.9
22.8	64.9	12.3	1178	1342.7
10.4	77.2	12.4	1215	1345
36.5	46.1	17.4	915-918	1177.51
37.8	38.5	23.7	1010-1022	1224.03
35.5	40.2	24.3	1090	1298.98
22.7	52.8	24.5	1235	1498.04
10.4	65	24.6	1230	1458.19
42.8	29.3	27.9	960	1063.91
10.6	52.9	36.5	1260	1565.56
22.4	40.9	36.7	1285	1624.15
22.1	17.8	60.1	1370	1805.99
	BaO 31.8 30.3 32.5 22.8 10.4 36.5 37.8 35.5 22.7 10.4 42.8 10.6 22.4 22.1	BaO B_2O_3 31.865.530.360.732.556.222.864.910.477.236.546.137.838.535.540.222.752.810.46542.829.310.652.922.440.922.117.8	BaO B_2O_3 SiO_231.865.52.730.360.7932.556.211.322.864.912.310.477.212.436.546.117.437.838.523.735.540.224.322.752.824.510.46524.642.829.327.910.652.936.522.440.936.722.117.860.1	BaO B_2O_3 SiO_2Exp.31.865.52.7864-87730.360.79995-100432.556.211.395322.864.912.3117810.477.212.4121536.546.117.4915-91837.838.523.71010-102235.540.224.3109022.752.824.5123510.46524.6123042.829.327.996010.652.936.5126022.440.936.7128522.117.860.11370



Fig. 3.17.1 Optimized phase diagram of the BaSiO₃-BaB₂O₄ section.



Fig. 3.17.2 Optimized phase diagram of the BaB₂O₄-Ba₂Si₃O₈ section.



Fig. 3.17.3 Optimized phase diagram of the Ba₃Si₂B₆O₁₆-Ba₂Si₃O₈ section.



Fig. 3.17.4 Optimized phase diagram of the Ba₃Si₂B₆O₁₆-BaSi₂O₅ section.



Fig. 3.17.5 Optimized phase diagram of the Ba₃Si₂B₆O₁₆-BaB₂O₄ section.



Fig. 3.17.6 Optimized phase diagram of the Ba₃Si₂B₆O₁₆-BaB₄O₇ section.



Fig. 3.17.7 The present calculated polythermal projection of the $BaO-B_2O_3-SiO_2$ system comparing the primary phase regions reported by Levin and Ugrinic.



Fig. 3.17.8 Optimized isoplethal section at $X_{BaO}=0.245$.



Fig. 3.17.9 Optimized isoplethal section at $X_{BaO}=0.285$.



Fig. 3.17.10 Optimized isoplethal section at $X_{BaO}=0.325$.



Fig. 3.17.11 Optimized isoplethal section at $X_{\text{BaO}}=0.365$.



Fig. 3.17.12 Optimized isoplethal section at $X_{BaO}=0.405$.



Fig. 3.17.13 Optimized isoplethal section at $X_{BaO}=0.44$.



Fig. 3.17.14 Activities on the isoplethal section $X_{BaO} = 0.1$ in the BaO-B₂O₃-SiO₂ system at 1427 °C (Std. states; solid for BaO and SiO₂ and liquid for B₂O₃).



Fig. 3.17.15 Activities on the isoplethal section $X_{BaO} = 0.2$ in the BaO-B₂O₃-SiO₂ system at 1427 °C (Std. states; solid for BaO and SiO₂ and liquid for B₂O₃).



Fig. 3.17.16 Activities on the isoplethal section $X_{BaO} = 0.3$ in the BaO-B₂O₃-SiO₂ system at 1427 °C (Std. states; solid for BaO and SiO₂ and liquid for B₂O₃).



Fig. 3.17.17 Activities on the isoplethal section $X_{BaO} = 0.4$ in the BaO-B₂O₃-SiO₂ system at 1427 °C (Std. states; solid for BaO and SiO₂ and liquid for B₂O₃).



Fig. 3.17.18 Activities on the isoplethal section $X_{BaO} = 0.5$ in the BaO-B₂O₃-SiO₂ system at 1427 °C (Std. states; solid for BaO and SiO₂ and liquid for B₂O₃).

3.18 The SrO-B₂O₃-SiO₂ system

The Gibbs energy of the liquid phase in the $SrO-B_2O_3-SiO_2$ ternary system was calculated from the corresponding binary systems by treating SrO as asymmetric component [Pelton and Chartrand (2001)]. The optimized parameters for this ternary system are presented in Table 3.18.1. For the liquid phase, ternary interaction parameters presented in Table 3.18.1, were also used to obtain the optimal fit of the available data.

Baylor and Brown (1976b) reported sub-solidus phase equilibria, as shown in Fig. 3.18.1, in the SrO-B₂O₃-SiO₂ system. These phase equilibria can be compared with the present calculations at 400 °C (the temperature at which no liquid phase appears in this system) in Fig. 3.18.2 However, the present calculations give these same phase equilibria from room temperature to higher temperatures, by emitting the liquid phase from calculations at higher temperatures. Baylor and Brown (1976b) reported the presence of a stable ternary compound Sr₃B₂SiO₈ (Sr₃BS). No thermodynamic data for this phase could be found in the literature. The optimized parameters for this phase are presented in Table 3.18.1. Krzhizhanovskaya, Bubnova, Krivovichev, Belousova, and Filatov (2010) reported orthorhombic crystal structure with space group *Pnma* for this phase. N. G. Tyurnina, Belousova, Domanskii, Doronina, and Ugolkov (2010) by DTA reported a congruent melting temperature at 1180 °C for this compound. The present calculated congruent melting temperature is 1166 °C.

N. G. Tyurnina, et al. (2010), by DTA and high-temperature microscope melting techniques, measured eutectic and liquidus temperatures on some of the vertical sections in the SrO-B₂O₃-

SiO₂ system. The optimal fits of these data are presented in Figs. 3.18.3-3.18.6. In these figures the DTA peaks (Fig. 16.3) are comparatively better reproduced than the liquidus temperatures (Figs. 16.3-16.6) determined by high-temperature microscopic melting. N. G. Tyurnina, et al. (2010), while presenting the phase diagram for this section, acknowledged the inconsistency between their findings and melting temperatures for the binary phases from the literature. This inconsistency is also visible in the present calculated phase diagram for these sections. Moreover, they also reported that in the B₂O₃-rich samples they overestimated the liquidus temperature because of selective evaporation of B₂O₃ oxide. Hence, more experimental work is required to establish correctly the liquidus temperatures on these sections. In the present work, these data were optimized as shown in Figs. 3.18.3-3.18.6.

Baylor and Brown (1976a) by quenching techniques measured the one- and two-phase liquid regions in the temperature range 1100-1525 °C. Their data are reasonably well reproduced in Table 3.18.2. The compositions at which they obtained a two-phase liquid at equilibrium are also plotted in the Fig. 3.18.7 showing the primary phase field regions in the SrO-B₂O₃-SiO₂ system. This figure also contains the data reported by N. G. Tyurnina, et al. (2010), who also used quenching techniques, on the two-phase liquid region.

In the present work (see chapter 4), quenching experiments followed by EPMA analysis were performed to find the composition of the liquid phase in equilibrium with the SrS phase at 1150, 1050 and 1000 °C. The liquid composition obtained at these three temperatures is also plotted in Fig. 3.18.7 and the present optimization fits them reasonably well. In these experiments the

eutectic temperature comprising SrS, SB and SiO₂ phases was bracketed between 950 and 1000 $^{\circ}$ C. The present calculated eutectic temperature is 991 $^{\circ}$ C. The details of these experiments and results are presented in Chapter 4.

Stolyarova, Lopatin, and Shilov (2009), at 1447 °C and 1527 °C, by high-temperature mass spectrometry measured the activities in the SrO-B₂O₃-SiO₂ melt at constant SrO mol%. These activities are compared with the present calculations at 1487 °C (according to present calculations, the activities at 1447 and 1527 °C are practically the same) in Figs. 3.18.8-3.18.13 (the different experimental points at the same composition in these figures correspond to the two different temperatures; in the scale of these figures there is practically no difference in the calculated activities in this temperature range. Therefore the present calculations were performed at 1487 °C). It must be noted that Stolyarova and coworkers measured some of these activities in two-phase liquid region (for $X_{SrO} = 0.1$ and 0.2). Achievement of equilibrium in such a highly viscous liquid phase, especially in the two-phase region, is quite sluggish. Stolyarova and coworkers did not mention in their publication on the time given to samples to reach equilibrium. Also, the rate of increase in the SrO activity with increase in SrO content is too much. At X_{SrO} = 0.5 and 0.6 (Figs. 3.17.17 and 3.17.18), the SrO activity is more than that of SiO₂ and B₂O₃. It is hard to believe that the present optimized parameters which reasonably fit the other available experimental data will deviate so much from the data of Stolyarova and coworkers. More experimental work is required to corroborate the data by Stolyarova and coworkers.

	Table 3.18.1 O	ptimized thermod	ynamic parameters	s, in Joules	, in the SrO-B ₂ O	O_3 -Si O_2 system.
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Sr ₃ B ₂ SiO ₈ (Sr ₃ BSi)		
$\Delta H^0_{298} = -4342000 \text{ J/mol}$	${f S}^0_{298}=274.000\ \Delta {f S}^0_{298}^{(b)}=17.850$	$\Delta S^{0}_{298}{}^{(a)} = 10.254$
$T_m = 1180 \ ^{\circ}C^{(c)}$, Exp. = 1179 $\ ^{\circ}C^{(c)}$	270	
$C_p = C_p(Sr_2SiO_4, \alpha') + C_p(SrB_2O_4)$		
Liquid phase (Ternary interaction pa	rameters) (in Joules)	
$g_{\rm III}^{301}$ = 66944		
$g_{002}^{102}Si-Sr(B) = 54392$		
$g_{Si-Sr(B)}^{002} = -33472$		

^(a) from the compounds used to calculate heat capacity
^(b) from the oxides
^(c) incongruent melting

Table 3.18.2 1-phase and 2-phase liquid region as determined by Baylor and Brown (Exp.) compared with the present calculations (Cal.) (Compositions in mol).

SiO ₂	SrO	B_2O_3	T(C)	Exp.	Cal.
0.103	0.308	0.589	1100	1-liquid	1-liquid
0.104	0.261	0.635	1100	1-liquid	1-liquid
0.205	0.308	0.487	1250	1-liquid	1-liquid
0.206	0.258	0.536	1250	1-liquid	1-liquid
0.307	0.307	0.386	1325	1-liquid	1-liquid
0.405	0.304	0.291	1325	1-liquid	1-liquid
0.217	0.272	0.511	1250	1-liquid	1-liquid
0.404	0.346	0.250	1325	1-liquid	1-liquid
0.105	0.210	0.685	1100	2-liquids	2-liquids
0.103	0.030	0.867	1320	2-liquids	2-liquids
0.207	0.208	0.585	1250	2-liquids	2-liquids
0.307	0.256	0.437	1325	2-liquids	2-liquids
0.311	0.207	0.482	1325	2-liquids	2-liquids
0.303	0.030	0.667	1325	2-liquids	2-liquids
0.408	0.255	0.337	1325	2-liquids	2-liquids
0.409	0.204	0.387	1325	2-liquids	2-liquids
0.219	0.162	0.619	1275	2-liquids	2-liquids
0.221	0.110	0.669	1275	2-liquids	2-liquids
0.257	0.257	0.486	1275	2-liquids	2-liquids
0.272	0.218	0.510	1275	2-liquids	2-liquids
0.335	0.167	0.498	1335	2-liquids	2-liquids

0.400	0.286	0.314	1425	2-liquids	1-liquid
0.385	0.220	0.395	1425	2-liquids	2-liquids
0.388	0.166	0.446	1425	2-liquids	2-liquids
0.385	0.110	0.505	1425	2-liquids	2-liquids
0.541	0.324	0.135	1525	2-liquids	1-liquid
0.525	0.225	0.250	1525	2-liquids	2-liquids
0.642	0.129	0.229	1525	2-liquids	2-liquids
0.678	0.068	0.254	1525	2-liquids	2-liquids



Fig. 3.18.1 Sub solidus phase equilibria as reported by Baylor and Brown.



Fig. 3.18.2 Present calculated isothermal section at 400 °C in the SrO-B₂O₃-SiO₂ system.



Fig. 3.18.3 Optimized phase diagram of the section SrSiO₃-SrB₂O₄.



Fig. 3.18.4 Optimized phase diagram of the section Sr₂SiO₄-Sr₂B₂O₅.



Fig. 3.18.5 Optimized phase diagram of the section Sr₃SiO₅-Sr₃B₂O₆.



Fig. 3.18.6 Optimized phase diagram of the section $(SrO)_{0.7}(SiO_2)_{0.3}$ - $(SrO)_{0.7}(B_2O_3)_{0.3}$.



Fig. 3.18.7 Polythermal projection of the SrO-B₂O₃-SiO₂ system.



Fig. 3.18.8 Activities on the isoplethal section $X_{SrO} = 0.1$ in the SrO-B₂O₃-SiO₂ system at 1487 °C (Std. states; solid for SrO and SiO₂ and liquid for B₂O₃).



Fig. 3.18.9 Activities on the isoplethal section $X_{SrO} = 0.2$ in the SrO-B₂O₃-SiO₂ system at 1487 °C (Std. states; solid for SrO and SiO₂ and liquid for B₂O₃).



Fig. 3.18.10 Activities on the isoplethal section $X_{SrO} = 0.3$ in the SrO-B₂O₃-SiO₂ system at 1487 °C (Std. states; solid for SrO and SiO₂ and liquid for B₂O₃).



Fig. 3.18.11 Activities on the isoplethal section $X_{SrO} = 0.4$ in the SrO-B₂O₃-SiO₂ system at 1487 °C (Std. states; solid for SrO and SiO₂ and liquid for B₂O₃).


Fig. 3.18.12 Activities on the isoplethal section $X_{SrO} = 0.5$ in the SrO-B₂O₃-SiO₂ system at 1487 °C (Std. states; solid for SrO and SiO₂ and liquid for B₂O₃).



Fig. 3.18.13 Activities on the isoplethal section $X_{SrO} = 0.6$ in the SrO-B₂O₃-SiO₂ system at 1487 °C (Std. states; solid for SrO and SiO₂ and liquid for B₂O₃).

3.19 The BaO-SrO-B₂O₃ system

The Gibbs energy of the liquid phase in the BaO-SrO- B_2O_3 ternary system was calculated from the corresponding binary systems by treating B_2O_3 as asymmetric component [Pelton and Chartrand (2001)]. Small ternary interaction parameters present in Table 3.19.1 were also used to fit the available data. The optimized parameters for this ternary system are presented in Table 3.19.1.

Wang, et al. (1984) studied the system by quenching techniques, DTA and XRD. The data reported by them on the BaB₂-SrO and BaB-SB sections are reasonably well reproduced in Figs. 3.19.1 and 3.19.2. In Fig. 3.19.2, the difference between the calculated melting temperature of the BaB phase and experimental point of Wang, et al. (1984) is about 10 °C. However, the present optimal fit of the binary BaO-B₂O₃ system (Fig. 2.8.1) is very close to the melting point of the BaB phase, 1092 °C, reported by Ernest M. Levin and McMurdie (1949). The crystal structures of the low- and high-temperature forms of the BaB phase belong to R3*c* and R $\overline{3}$ *c* space group symmetries [Liebertz (1988)], whereas that of the SB phase belongs to the Pbcn space group symmetry [Kim et al. (1996)]. The BaB and SB solid solutions in Fig. 3.19.2 were treated as different phases using the single-sublattice random mixing model. No data on the solubility of Sr in the low-temperature form could be found in the literature. Moreover, the present calculations were performed by assuming the same thermodynamic properties for the low- and high-temperature forms (see the BaO-B₂O₃ section). Wang, et al. (1984) reported unindexed XRD data of a ternary compound Ba₅Sr₆B₁₀O₂₆ (B₅S₆B₁₀). No other data for this compound, neither on its

presence nor on its thermodynamic properties, could be found in the literature. In the present calculations, the presence of this compound was neglected.

Wang, et al. (1984) by quenching techniques also reported a part of an isothermal section at 880 °C as shown in Fig. 3.19.3. As evident in Fig. 3.19.3, they reported about 40 % solubility of Sr in the Ba₄B phase. The thermodynamic equilibrium of BaB and Ba₄B solid solutions reported by Wang, et al. (1984) is incorrect as there are other binary phases, Ba_3B and Ba_2B (not shown in Fig. 3.19.3) between the BaB and Ba₄B which appear in the present calculations as shown in Fig. 3.19.4. In the present calculations, in view of this inconsistency in the diagram of Wang, et al. (1984), the solubility of Sr in Ba₄B reported by Wang, et al. (1984) was neglected. Also, there are some other phases in the SrO-BaO-B₂O₃ system which have the same stoichiometries: S₃B-Ba₃B, SB₂-BaB₂. The crystal structure of the S₃B phase belongs to the $R\bar{3}ch$ space group [Wei et al. (2001)]. No data on the crystal structure of the Ba₃B phase could be found in the literature. The S_3B and Ba_3B phases might be isomorphic and completely mutual soluble. During calculations, when an ideal solution was assumed between these two phases, this solid solution appeared in Fig. 3.19.1. However, such a solid solution was not reported by Wang, et al. (1984) in this section. Therefore, the possibility of complete solid solution between these two phases was neglected. If these two phases belong to different crystal structures then also because of chemical similarity between the Ba and Sr atoms some amount of mutual solid solubility between these phases can be expected. However, in the absence of any experimental data on such solubility it was neglected in the present calculations. Similarly, the SB₂ and BaB₂ phases are not isomorphic. The crystal structure of the SB_2 phase belongs to the Pmn21 space group [H. Liu, Guo, Fan, and Xu (1997)] whereas of that the BaB_2 phase belongs to the P21/c space group [Block and Perloff (1965)]. Here again, because of the absence of any experimental evidence, the possibility of some amount mutual solid solubility between these two phases was neglected. The present calculated liquidus (polythermal) projection for the BaO-SrO-B₂O₃ system is presented in Fig. 3.19.5.

Table 3.19.1 Optimized thermodynamic parameters, in Joules, in the BaO-SrO-B₂O₃ system.

$BaB_2O_4 \text{ solid solutions (BaB)}$ $g^0 (SrB_2O_4, BaB) = g^0 (SrB_2O_4) + 8786$
SrB ₂ O ₄ solid solutions (SrB)
g^{0} (BaB ₂ O ₄ , SrB) = g^{0} (BaB ₂ O ₄) + 13389
Liquid phase (Ternary interaction parameters)
$g_{\rm max}^{002}$ B-Sr(Ba) = 2510
$g^{002}_{B-Ba(Sr)} = 4184$



Fig. 3.19.1 Optimized phase diagram of the BaB₂O₄-SrO section.



Fig. 3.19.2 Optimized phase diagram of the BaB₂O₄-SrB₂O₄ section.



Fig. 3.19.3 Isothermal section at 880 $^{\circ}\mathrm{C}$ as reported by Wang et al.



Fig. 3.19.4 Optimized isothermal section at 880 °C in the BaO-SrO-B₂O₃ system.



Fig. 3.19.5 Present calculated liquidus (polythermal) projection for the BaO-SrO- B_2O_3 system (isotherms were drawn at the interval of 100 °C).

3.20 The BaO-CaO-B₂O₃ system

Ji, Liang, Xie, and Yu (1995) by quenching and XRD reported sub-solidus phase equilibria in the system as shown in Fig. 3.20.1. They equilibrated the B_2O_3 -rich ($B_2O_3 > 0.5$ mol) samples at 780 °C and other samples at 1040 °C. The exact compositions of the samples studied were not reported. The final results were reported in the form of Fig. 3.20.1. These data can be compared with the present calculations at 800 °C in Fig. 3.20.2. Ji, et al. (1995) reported three ternary compounds as stable: CaBa₂B₆O₁₂ (CBa₂B₃), CaBa₂B₂O₆ (CBa₂B), Ca₅Ba₂B₁₀O₂₂ (C₅Ba₂B₅). They indexed the crystal structure of CBa_2B_3 as $R\bar{3}c$ (isostructural to HT-BaB), of CBa_2B as P2or Pm and of C₅Ba₂B₅ as $P2_1$ space group symmetry. No other thermodynamic data for these compounds could be found in the literature. The present optimized thermodynamic parameters for these phases are presented in Table 3.20.1. As the CBa₂B₃ and HT-BaB phases are isostructural some solubility among these phases is expected (HT-BaB is stable above 925 °C). However, no experimental data proving this could be found. In the present calculations this solubility was neglected. The crystal structure of LT-BaB (space group R3c) differs from that of CBa_2B_3 . Hence, in the present calculations at 800 °C, no mutual solubility was assumed among these phases. Ji, et al. (1995) reported solubility of Ca in the Ba₄B phase at 800 °C as shown in Fig. 3.20.1. This solubility is reproduced in the present calculations in Fig. 3.20.2. The solid solution was treated with a single-sublattice random mixing model (i.e. $[Ba,Ca]_4B_2O_7]$).

The calculated melting temperatures of the ternary compounds in Table 3.20.1 are quite reasonable. Also, for all these compounds the entropies of formation (from the compounds used

to calculate the heat capacities in Table 3.20.1) are equal to zero. The Gibbs energy of the liquid phase in the ternary system was calculated from the corresponding binary systems by treating B_2O_3 as asymmetric component [Pelton and Chartrand (2001)]. The present calculated liquidus (polythermal) projection for the BaO-CaO-B₂O₃ system is presented in Fig. 3.20.3.

There are phases in the BaO-CaO-B₂O₃ system which have the same stoichiometries: C₃B-Ba₃B, CB-BaB,CB₂-BaB₂. Some amount of mutual solubility among these phases can be expected. The crystal structure of the C₃B phase belongs to the R3*c* space group [Vegas, Cano, and Garcia-Blanco (1975)]. No data on the crystal structure for the Ba₃B phase could be found in the literature. The crystal structure of the CB phase belongs to the Pnca space group [Zachariasen and Ziegler (1932)] whereas BaB (the low- and high-temperature polymorphs) belong to R3*c* and R $\overline{3}c$ space groups [Liebertz (1988)]. Thus the CB and BaB phases are not isostructural. However, CB₂ and BaB₂ belong to the same monoclinic P21/c space group [Kindermann (1978); Block and Perloff (1965)]. In the present calculations, in the absence of any experimental evidence, no mutual solubility was calculated among these phases with same stoichiometries. Moreover, a large size difference between the Ba and Ca atom would mitigate against any appreciable mutual solubility among these phases.

 $T \underbrace{ able \ 3.20.1 \ Optimized \ parameters \ in \ the \ BaO-CaO-B_2O_3 \ system.}_{CaBa_2B_6O_{12} \ (CBa_2B_3)}$

$\Delta H^0_{298} = -6104106 \text{ J}$	$S_{298}^0 = 367.371 \text{ J/mol/K}$	$\Delta S^{0}_{298}{}^{(a)} = 0$		
$T_{m}^{(b)} = 1111 \ ^{\circ}C$	$\Delta S^{0}_{298}{}^{(d)} = 23.633$			
$C_{p} = C_{p} (CB_{2}) + C_{p} (BaB) + Cp (BaO)$				
(298.15 < T < 1500 K)				
$CaBa_2B_2O_6(CBa_2B)$				
$\Delta H^0_{298} = -3365634 \text{ J}$	S ⁰ ₂₉₈ =249.139 J/mol/K	$\Delta S^{0}_{298}{}^{(a)} = 0$		
$T_{m}^{(c)} = 1138 \ ^{\circ}C$	$\Delta S^{0}_{298}{}^{(d)} = 13.301$			
$C_{p} = C_{p} (CB) + 2 C_{p} (BaO)$				
(298.15 < <i>T</i> < 1500 K)				
$Ca_5Ba_2B_{10}O_{22} (C_5Ba_2B_5)$				
$\Delta H^0_{298} = -11584338$	$S_{298}^0 = 669.142 \text{ J/mol/K}$	$\Delta S^{0}_{298}{}^{(a)} = 0$		
$T_{m}^{(c)} = 1086 \ ^{\circ}C$	$\Delta S^{0}_{298}{}^{(d)} = 66.504$			
$C_{p} = 5 C_{p} (CB) + 2 C_{p} (BaO)$				
(298.15 < T < 1500 K)				
[Ca,Ba]B ₈ O ₁₃ solid solution (ss)				
$G^{0}(CaB_{8}O_{13}, ss) = G^{0}(CaO) + 4G^{0}(B_{2}O_{3}) - 167360$ $q^{11}_{BaCa} = -62760$				

(a) compounds used to calculated the heat capacities as reference
(b) congruent melting temperature
(c) incongruent melting temperature
(d) oxides (stable at room-temperature) as reference



Fig. 3.20.1 Phase equilibria as reported by Ji et al.



Fig. 3.20.2 Optimized isothermal section at 800 °C in the BaO-CaO-B₂O₃ system.



Fig. 3.20.3 Present calculated liquidus (polythermal) projection of the BaO-CaO- B_2O_3 system (isotherms were drawn at the interval of 100 °C).

3.21 The BaO-Al₂O₃-B₂O₃ system

The estimations in this ternary system obtained from the optimized model parameters were far from experimental data. The reason for this could be the complex structure of the alumino-borate liquid phase. A relatively larger number of parameters for the liquid phase (Table 3.21.1) were required to fit the available data. The Gibbs energy of the liquid phase in the BaO-Al₂O₃-B₂O₃ system was calculated from the corresponding binary systems by treating B₂O₃ as an asymmetric component i.e. BaO, Al₂O₃ and BaAl₂O₄ were kept in the same group (Chartrand and Pelton, 2001). The BaO-Al₂O₃ binary system contains BaAl₂ associates see (Sec.2.7, BaO-Al₂O₃ and Sec. 3.15, BaO-Al₂O₃-SiO₂) as separate component in the liquid system. The $g^{0}_{BaAl2O4}$ (see Sec.2.7, BaO-Al₂O₃ and Sec. 3.15, BaO-Al₂O₃-SiO₂) was fixed from the optimization of the BaO-Al₂O₃-SiO₂ system. This value made these associates practically unstable in the BaO-Al₂O₃-B₂O₃ ternary system. Moreover, the presence of these associates is important in those systems where charge compensation effect occur. Such effect is not possible in this system, firstly because there is no imbalance of charge when B⁺³ is substituted by Al⁺³, and secondly because such substitution is less probable due to larger size difference between the radii of these two ions. The optimized parameters of the system are presented in Table 3.21.1.

Huebner (1970) by quenching and XRD reported an isothermal section at 700 °C, shown in Fig. 3.21.1. He reported six ternary compounds in the system: (BaO = Ba, Al₂O₃ = A, B₂O₃ = B): BaAB, BaAB₂, Ba₃A₂B₂, Ba₂AB₄, Ba₅A₂B₆, Ba₁₀AB. As is evident in Fig. 3.21.1, Huebner (1970) reported non-stoichiometry for the phase BaAB (SSII in Fig. 3.21.1) and solid solubility among the binary BaB and Ba₂B phases (SSI in Fig. 3.21.1). In the binary BaO-B₂O₃ system, there are no data for such solubility among these binary phases. Hence, this solubility was neglected in the present calculations. Also, there are no other data for the non-stoichiometric nature of the BaAB phase. In fact, later phase diagram measurements on the section BaAB-Al₂O₃ (Fig. 3.21.4) do not suggest this phase as non-stoichiometric. The phase relationships at 700 °C reported by Huebner (1970) can be compared with present calculations. Huebner (1970) did not find the liquid phase stable at 700 °C; however -according to the present optimization based

on other phase diagram data (Fig. 3.21.4)- the liquid phase appears at 700 °C as shown in Fig. 3.21.3. Huebner (1970), Miyazaki, Kimura, Maiwa, Nakamura, and Kannan (2004) and Hovhannisyan (2005), by DTA, determined melting behavior and temperatures for all the ternary compounds (except for $Ba_{10}AB$). All these data can be compared with the present calculated melting temperatures of these compounds in Table 3.21.1. In the present calculations the presence of $Ba_{10}AB$ was neglected, because further evidence is required to prove its stability. The optimized entropies of formation of the ternary compounds presented in Table 3.21.1 are always less than 10 J/(mol of metallic atoms) which is quite reasonable.

The phase diagram measurements on the BaAB-Al₂O₃ section by Kimura, Numazawa, and Sato (1997), Hovhannisyan (2003); Hovhannisyan (2004), and Toroyan, Oganesyan, and Kostanyan (1982), all by DTA, is well reproduced in Fig. 3.21.4. Hovhannisyan (2003) first reported congruent melting behavior for the BaAB phase, but later he reported [Hovhannisyan (2005)] incongruent behavior (into Liquid+Al₂O₃) for the same phase. Ye, Zeng, Wu, Huang, and Chen (1998) determined a trigonal structure in the *R*32 space group for the BaAB phase.

The calculated liquidus (polythermal) projection for the BaO-B₂O₃-Al₂O₃ system is presented in Fig. 3.21.5. As can be seen in this figure, the present calculations show small immiscibility in the liquid phase between the Ba₃B₂O₆ and BaAl₂O₄ primary phase regions. There are no experimental data to prove this immiscibility. In the present work, it was found very difficult to suppress this immiscibility in this region.

BaAlaBaOr (BaAB)		
$\Delta H^0_{298} = -3655840 \text{ J/mol}$	$S_{298}^0 = 243.500 \text{ J/mol/K}$	$\Delta S^{0}_{298}{}^{(a)} = 49.180$
$\Delta S^{0}_{298}{}^{(b)} = 66.661$		
$T_m = 985 \text{ °C}, I (Liq. + A_9B_2)$	Exp. (°C) = 910, C ^{[1];} 910, I ^[2] ; 995, I (Liq.+Al ₂ O ₃) ^[3]	
$C_{p} = C_{p} (BaB) + C_{p} (Al_{2}O_{3})$		
$BaAl_2B_4O_{10}$ ($BaAB_2$)		
$\Delta H^{0}_{298} = -5005576 \text{ J/mol}$	$S^0_{298} = 264.000 \text{ J/mol/K}$	$\Delta S^{0}_{298}{}^{(a)} = -19.820$
$\Delta S^{0}_{298}{}^{(b)} = 33.211$		
$T_m = 815 \text{ °C}, I (Liq.+A_9B_2)$	Exp. (°C) = 805, $C^{[1]}$; 785, $I^{[2]}$; 850, I (Liq.+A ₉ B ₂ +BaA)	B) ^[3]
$C_{p} = C_{p} (BaB_{2}) + C_{p} (Al_{2}O_{3})$		
$Ba_{3}Al_{4}B_{4}O_{15} (Ba_{3}A_{2}B_{2})$		
$\Delta H^{0}_{298} = -7925984 \text{ J/mol}$	$S^{0}_{298} = 638.000 \text{ J/mol/K}$	$\Delta S^{0}_{298}{}^{(a)} = 92.469$
$\Delta S^{0}_{298}{}^{(b)} = 212.253$		
$T_{\rm m} = 904 {}^{\rm o}{\rm C}, {\rm C}$	Exp. (°C) = 945, $C^{[1]}$; 900, $I^{[2]}$; 930, $C^{[3]}$	
$C_p = 2 C_p (BaA,HT) + C_p (BaB_2)$		
$Ba_2Al_2B_8O_{17} (Ba_2AB_4)$		
$\Delta H^{0}_{298} = -8280652 \text{ J/mol}$	$S^0_{298} = 514.000 \text{ J/mol/K}$	$\Delta S^{0}_{298}{}^{(a)} = -2.820$
$\Delta S^{0}_{298}{}^{(b)} = 103.242$		
$T_{m} = 802 \text{ °C}, C$	Exp. (°C) = 810, C ^[1] ; 810, I ^[2] ; 860, C ^[3]	
$C_p = C_p(Al_2O_3) + 2 C_p(BaB_2)$		
$Ba_5Al_4B_{12}O_{29}(Ba_5A_2B_6)$		
$\Delta H^{0}_{298} = -14557536 \text{ J/mol}$	$S^0_{298} = 1080.000 \text{ J/mol/K}$	$\Delta S^{0}_{298}{}^{(a)} = 68.469$
$\Delta S^{0}_{298}{}^{(b)} = 294.315$		
$T_m = 822 \circ C, I (Liq.+BaB)$	Exp. (°C) = 855, $C^{[1]}$; 820, $C^{[2]}$; 870, $C^{[3]}$	
$C_{p} = 2 C_{p} (BaA,HT) + 3 C_{p} (BaB)$		
Liquid phase (Ternary interaction	parameters) (in Joules)	
g_{002}^{003} B-Ba(Al) = -104600		
g_{001}^{002} B-Ba(Al) = -117152		
$g^{\mu}_{B-Ba(Al)} = -83680$		
(a) Erom the compounds used to	o calculated heat capacities	
^(b) From oxides	o carculated near capacities	
^[1] Hubner (1970)		
^[2] Miyazaki et al. (2004)		
^[3] Hovhannisyan (2005)		

Table 3.21.1 Optimized thermodynamic parameters, in Joules, in the BaO-Al₂O₃-B₂O₃ system (I = incongruent, C = congruent).



Fig. 3.21.1 Phase equilibria in the $BaO-B_2O_3-Al_2O_3$ system as reported by Hubner.



Fig. 3.21.2 Present calculated phase equilibria at 700 $^{\circ}$ C (by suspending liquid phase from calculations) in the BaO-B₂O₃-Al₂O₃ system.



Fig. 3.21.3 Present calculated phase equilibria at 700 °C in the BaO-B₂O₃-Al₂O₃ system.



Fig. 3.21.4 Optimized phase diagram of the BaB₂O₄-Al₂O₃ section.



Fig. 3.21.5 Present calculated liquidus (polythermal) projection of the BaO-B₂O₃-Al₂O₃ system (isotherms were drawn at the interval of 100 °C)..

3.22 The SrO-Al₂O₃-B₂O₃ system

The Gibbs energy of the liquid phase in the SrO-Al₂O₃-B₂O₃ system was calculated from the corresponding binary systems by treating B₂O₃ as an asymmetric component i.e. SrO, Al₂O₃ and SrAl₂O₄ were kept in the same group (Chartrand and Pelton, 2001). The SrO-Al₂O₃ binary system contains SrAl₂ associates see (Sec. 2.6, SrO-Al₂O₃ and Sec. 3.16, SrO-Al₂O₃-SiO₂) as separate component in the liquid system. The $g_{SrAl2O4}^{0}$ (see Sec. 2.6, SrO-Al₂O₃ and Sec. 3.16,

SrO-Al₂O₃-SiO₂) was fixed from the optimization of the SrO-Al₂O₃-SiO₂ system. This value made these associates practically unstable in the SrO-Al₂O₃-B₂O₃ ternary system. Moreover, the presence of these associates is important in those systems where charge compensation effect occur. Such effect is not possible in this system, firstly because there is no imbalance of charge when B^{+3} is substituted by Al⁺³, and secondly because such substitution is less probable due to larger size difference between the radii of these two ions. The optimized parameters of the SrO-Al₂O₃-B₂O₃ system are presented in Table 3.22.1. During simultaneous optimization, effort was made to use parameters for the liquid phase which are similar in form as obtained for the liquid phase in the BaO-Al₂O₃-B₂O₃ system are same in form as obtained for the BaO-Al₂O₃-B₂O₃ system.

Hovhannisyan (2003) reported phase diagram points on the SrB₂O₄-Al₂O₃ section which are reproduced well in Fig. 3.22.1. He reported, by XRD, SrAl₂B₂O₇ (SAB) as a stable phase on this section. He also reported incongruent melting of this compound at 1085 °C into Liquid + Al₂O₃. In a different work, Hovhannisyan (2005) by quenching and XRD reported another ternary compound, Sr₂Al₂B₂O₈ (S₂AB), melting incongruently at 950 °C into Liquid + SrAl₂O₄ (SA). According to the present calculations, this phase melts congruently at 950 °C. In the present calculations, while optimizing the thermodynamic properties for the S₂AB phase, care was taken that this phase must not appear on the SrB₂O₄-Al₂O₃ section. Analogously to the BaAB₂, Ba₃A₂B₂, Ba₂AB₄, Ba₅A₂B₆ compounds in the BaO-Al₂O₃-B₂O₃ system, Hovhannisyan (2005) performed annealing and quenching experiments to check the stability of SAB₂, S₃A₂B₂, S₂AB₄, S₅A₂B₅ compounds (SrO=S, Al₂O₃=A, B₂O₃=B). He concluded that these phases are not stable in the SrO-Al₂O₃-B₂O₃ system. The present calculated liquidus (polythermal) projection for the SrO-B₂O₃-Al₂O₃ system is presented in Fig. 3.22.2.

Table 3.22.1 Optimized thermodynamic parameters, in Joules, in the SrO-Al₂O₃-B₂O₃ system (I = incongruent, C = congruent).

SrAl ₂ B ₂ O ₇ (SAB)		
$\Delta H^{0}_{298} = -3676740 \text{ J/mol}$	$S^{0}_{298} = 209.500 \text{ J/mol/K}$	$\Delta S_{298}^{0}{}^{(a)} = 27.171$
$\Delta S^{0}_{298}{}^{(b)} = 51.150$		
$T_m = 1085 \text{ °C}, I (Liq. + A_9B)$	Exp. (°C) = 1085 °C, I (Liq.+Al ₂)	₂ O ₃) [Hovhannisyan (2003)]
$C_{p} = C_{p} (SA,HT) + C_{p} (B_{2}O_{3})$		
$Sr_2Al_2B_2O_8$ (S ₂ AB)		
$\Delta H^{0}_{298} = -4390315 \text{ J/mol}$	$S^{0}_{298} = 263.400 \text{ J/mol/K}$	$\Delta S^{0}_{298}{}^{(a)} = 27.991$
$\Delta S^{0}_{298}{}^{(b)} = 51.470$		
$T_{\rm m} = 950 {}^{\rm o}{\rm C}, {\rm C}$	Exp. (°C) = 950 °C, I (Liq.+SA)	[Hovhannisyan (2005)]
$C_{p} = C_{p} (SA,HT) + C_{p} (B_{2}O_{3}) + SrO$		
Liquid phase (Ternary interaction par	rameters) (in Joules)	
$g_{\rm acc}^{003}$ B-Sr(Al) = -104600		
$g_{\rm un}^{002}$ = -121336		
$g_{\rm and B-Sr(Al)}^{001} = -79496$		
$g^{011}_{\text{B-Sr(Al)}} = 41840$		

^(a) compounds used to calculate heat capacities as reference.

^(b) Oxides (stable at room-temperature) as reference



Fig. 3.22.1 Optimized phase diagram of the section SrB₂O₄-Al₂O₃



Fig. 3.22.2 Present calculated liquidus (polythermal) projection of the SrO- B_2O_3 -Al₂O₃ system (isotherms were drawn at the interval of 100 °C)..

3.23 Liquidus projection for some ternary systems

No phase diagram and thermodynamic data could be found in the literature for these systems:

SrO-BaO-CaO, SrO-BaO-MgO, SrO-CaO-MgO, BaO-CaO-MgO, SrO-MgO-Al₂O₃, SrO-CaO-B₂O₃. SrO-MgO-B₂O₃, BaO-MgO-B₂O₃

In this section liquidus (polythermal) projections, calculated from the optimized binary model parameters, for these ternary systems are presented.

The systems SrO-BaO-CaO, SrO-BaO-MgO, SrO-CaO-MgO and BaO-CaO-MgO have monoxide solution as the only stable solid phase. The stability of the monoxide phase and the Gibbs energy of the liquid phase in these ternary systems were calculated from the respective optimized binary parameters. The liquidus (polythermal) projections for these systems are presented in Figs. 3.23.1-3.23.4.

In the system SrO-MgO-Al₂O₃, the Gibbs energy of the liquid phase was calculated from the respective binary systems by treating Al₂O₃ as asymmetric component [Pelton and Chartrand (2001)]. The liquidus (polythermal) projections for this system is presented in Figs. 3.235. The mutual solid solubilities between the MgAl₂O₄ phase (spinel) and SrAl₂O₄ (monoclinic, P6₃22) were neglected since the different structures of these compounds and the large ionic size difference between the Sr and Mg atoms mitigate against any appreciable solid solubility between them.

In the systems SrO-CaO-B₂O₃, SrO-MgO-B₂O₃ and BaO-MgO-B₂O₃, the Gibbs energy of the liquid phase was calculated from the respective binary systems by treating B_2O_3 as asymmetric component [Pelton and Chartrand (2001)]. The liquidus (polythermal) projections for these systems are presented in Figs. 3.23.6-3.23-8. The various stoichiometric phases appearing in these respective binary systems have different structures. Some amount of solubility between the solid phases with similar stoichiometry cannot be ruled out completely. However, the mutual solid solubilities among the solid phases, in the absence of any experimental data, were neglected.



Fig. 3.23.1 Present calculated liquidus (polythermal) projection of the SrO-BaO-CaO system (isotherms were drawn at the interval of 100 °C).



Fig. 3.23.2 Present calculated liquidus (polythermal) projection of the SrO-BaO-MgO system (isotherms were drawn at the interval of 100 °C).



Fig. 3.23.3 Present calculated liquidus (polythermal) projection of the SrO-CaO-MgO system (isotherms were drawn at the interval of 100 °C).



Fig. 3.23.4 Present calculated liquidus (polythermal) projection of the BaO-CaO-MgO system (isotherms were drawn at the interval of 100 °C).



Fig. 3.23.5 Present calculated liquidus (polythermal) projection of the SrO-MgO-Al₂O₃ system (isotherms were drawn at the interval of 100 $^{\circ}$ C).



Fig. 3.23.6 Present calculated liquidus (polythermal) projection of the SrO-CaO- B_2O_3 system (isotherms were drawn at the interval of 100 °C).



Fig. 3.23.7 Present calculated liquidus (polythermal) projection of the SrO-MgO- B_2O_3 system (isotherms were drawn at the interval of 100 °C).



Fig. 3.23.8 Present calculated liquidus (polythermal) projection of the BaO-MgO-B₂O₃ system (isotherms were drawn at the interval of 100 $^{\circ}$ C).

3.23 Summary of the optimized phases

All the phases (in the binary and ternary systems) optimized in the present work are listed here (the elements listed inside round brackets () are solutes in the matrix formed by the elements in square brackets []):

Liquid phase, MgO-CaO-SrO-BaO-Al₂O₃-SiO₂-B₂O₃

Stoichiometric solid phases

Monoxide phase - [Ca,Mg,Sr,Ba,(Al)] O. The solubility of Al₂O₃ in this phase is very small.

Pseudowollastonite - [Ca,Sr,(Ba)]SiO₃.

Wollastonite - [Ca,(Ba,Sr,Mg)]SiO₃.

BaSiO₃ solid solution - [Ba,(Ca,Sr)]SiO₃.

 α '-Ca₂SiO₄ - [Ca,Sr,Ba,(Mg)]₂SiO₄. The solubility of Mg₂SiO₄ is very small.

 α -Ca₂SiO₄ - ([Ca,Sr,Ba,(Mg)]₂SiO₄). The solubility of Mg₂SiO₄ is very small.

 $Ba_{3}SiO_{5} \text{ or } Sr_{3}SiO_{5} \text{ solid solution - } [Ba,Sr,(Ca)]_{3}SiO_{5}.$

Ca₃SiO₅ solid solution - [Ca,(Sr,Ba)]₃SiO₅.

Walstromite (non-stoichiometric $BaCa_2Si_3O_9$) - [Ca,Ba,(Sr)][Ca,Ba,(Sr)]CaSi_3O_9. This phase is stable on the $CaSiO_3$ -BaSiO_3 section and the $SrSiO_3$ phase dissolves in it. But, this phase is not stable on the $CaSiO_3$ -SrSiO_3 and $BaSiO_3$ -SrSiO_3 sections.

T-phase - $Ba_2Ca[Ba,Ca]Si_2O_8$. This phase is stable on the Ca_2SiO_4 - Ba_2SiO_4 section. In the absence of any experimental data, the solubility of Mg_2SiO_4 and Sr_2SiO_4 is neglected.

[Ca,Sr,Ba]₂MgSi₂O₇ (Akermanite)

[Ca,Sr,Ba]₃MgSi₂O₈ (Merwinite)

Diopside (Clinopyroxene) - $[Ca,Mg,(Sr)]MgSi_2O_6$. In the absence of any experimental data, the solubility of Ba is neglected.

 $BaCa_2MgSi_2O_8$ - [Ba,Ca][Ca,Ba]_2MgSi_2O_8. This phase is stable on the Ba_3MgSi_2O_8-Ca_3MgSi_2O_8 section. In the absence of any experimental data, the solubility of Sr is neglected.

Strontium or **Barium meta-aluminate solid solution**, β - [Sr,Ba,(Ca)]Al₂O₄.

Calcium meta-aluminate solid solution, *α* - [Ca,(Sr,Ba)]Al₂O₄.

Low-temperature BaAl₂O₄ solution - [Ba,(Ca,Sr)]Al₂O₄.

Low-temperature SrAl₂O₄ solution - ([Sr,(Ba,Ca)]Al₂O₄.

Cubic phase - [Ca,Sr,Ba]₃Al₂O₆.

Strontium or Calcium di-aluminate solid solution - [Ca,Sr]Al₄O₇.

Hexa-aluminate solid solution - [Ca,Sr,Ba]Al₁₂O₁₉.

Tetra-barium or -strontium aluminate solid solution - [Ba,Sr,(Ca)]₄Al₂O₇.

Octa-barium aluminate solid solution - [Ba,(Ca,Sr)]₈Al₂O₇.

BaB₂O₄ solid solution - [Ba,(Sr)]B₂O₄.

 SrB_2O_4 solid solution - ([Sr,(Ba)]B_2O_4).

BaB₈O₁₃ solid solution - [Ba,(Sr,Ca)]B₈O₁₃.

4. EXPERIMENTAL INVESTIGATIONS IN THE SrO-B₂O₃-SiO₂ SYSTEM

In the present work, a few experimental data points in the SrO-B₂O₃-SiO₂ system were generated. The thermodynamic optimization for this system is presented in section 3.18. As can be seen there, very few ternary experimental data are available in the literature for this system. The only reliable data are for the boundaries of the miscibility gap in the ternary system. The fitting of these data depends largely on the Gibbs energy of the liquid phase. During thermodynamic optimization for this ternary system, a need for new experimental data was identified. New data were necessary to reduce the number of degrees of freedom. A few experiments were performed in the present work to fill this gap. These newly obtained data improved the thermodynamic optimization of this ternary system. These data can also be useful to various glass companies as this ternary system is an important component of many commercial glasses.

In the present work, two sets of experiments were performed. In the first set, a glass of composition A (Table 4.1) was used to determine the composition of the liquid phase at 1150 °C in equilibrium with the SiO₂ and SrSiO₃ (SrS) phases (Fig. 4.1). In the second set, a glass of composition B (Table 4.1) was used to determine the temperature of the eutectic comprising the SiO₂, SrS and SrB₂O₄ (SrB) phases. Equilibrium samples from composition B were also used to determine the composition of the liquid phase in equilibrium with the SiO₂ and SrS phases at 1050 and 1000 °C. In the present work the preceding optimization, based only on the data available in the literature of this ternary system, was used as a guide to choose compositions A and B. To find the liquid composition in equilibrium at 1150 °C with the SrS and SiO₂ phases, a

composition (composition A in Table 4.1) was chosen which lies inside the triangle formed by the SiO₂, SrS and liquid phases in the isothermal section at 1150 °C (Fig. 4.1). Care was taken that the point lay close to the liquid phase composition, so that a maximum amount of the liquid phase can be formed with a sufficient amount of the other phases (SrS and SiO₂). Similarly, a composition (composition B in Table 4.1) close to the calculated (in the preceding optimization) eutectic point comprising the SiO₂, SrS and SrB phases was chosen to investigate the eutectic temperature. Thus the experiments were designed to generate the maximum amount of information with the minimum number of experiments, using the preceding optimization (based only on the data available in the literature) as a guide.

The source of SrO was reagent grade SrO powder (99.9 wt%) from Sigma Aldrich. The source of B_2O_3 (99.98 wt%) and SiO₂ (99.8 wt%) were reagent grade powders from Alfa Aesar. Compositions A and B were prepared in batches of 3 g by mixing SrO, B_2O_3 and SiO₂ in appropriate proportions in an agate mortar filled with acetone for 60 min. Glasses were made by melting, in a platinum crucible, the sample of composition A, in a preheated box furnace at 1300 °C for 20 min, and the sample of composition B, in a preheated box furnace at 1250 °C for 20 min. It must be noted that 3 wt.% excess B_2O_3 was added to compensate any losses by volatilization during melting. The melt was quenched to room temperature in water in an open atmosphere to produce a clear transparent glass. The glass was then again crushed, ground and stored in a desiccator. To prevent the loss of material during long heat treatments, the glasses were encapsulated in platinum capsules and brought to different equilibration temperatures. The glass samples were heat treated inside a welded platinum capsule. The heat-treatment schedule of

these samples is given in Table 4.1. After the heat treatment, the capsules were quenched to room temperature in water in an open atmosphere.

The quenched capsules were then cast in epoxy and longitudinal polished sections of the charges were made for identification of the products in backscattered electron (BSE) images. Electron probe microanalysis (EPMA) of the quenched liquids was performed on the JEOL 8900 probe at McGill University using wavelength-dispersive spectrometry (WDS). An accelerating voltage of 15 kV was used with 20 nA beam current and counting times of 20 s on peaks and 10 s on backgrounds. The raw data were reduced with the ZAF corrections using strontium titanate (SrTiO₃), quartz (SiO₂), and titanium diboride (TiB₂). Many analyses were performed on the liquid phase and the data were converted to mass fractions of oxides and averaged.

The detection of boron by EPMA is not sufficiently good, especially if SiO_2 is present. Boron has small atoms and emits relatively weak X-rays. The situation is made worse by the presence of Si, since it absorbs X-rays emitted by boron. This can be seen in Table 4.2, where the total of the contents of SrO, B₂O₃, and SiO₂ does not add up to 100%. In the present work, the content of B₂O₃ was calculated by subtracting the contents of SrO and SiO₂ from 100%. In Table 4.2, these amounts - the one obtained by EPMA from analysis and the one recalculated by subtraction from difference - are reported. The BSE images of samples heat-treated at different temperatures are given in Figs. 4.2-4.6. At 1000 °C, Fig. 4.4 shows three phases (Liquid, SrS and SiO₂) in equilibrium. However, at 950 °C (Fig. 4.5), and 900 °C (Fig. 4.6) there are four phases visible (the fourth phase is SrB). The WDS spectrum for these four phases is presented in Fig. 4.7 (boron was not scanned here). The temperature 950 °C should lie below the eutectic temperature, since in a ternary system four phases cannot remain in equilibrium. In other words, the liquid in Figs. 4.5 and 4.6 is metastable. Upon further heat treatment for a sufficient length of time, the liquid phase would disappear at this temperature. These results thus bracket the eutectic temperature between 950 and 1000 °C. The compositional analyses of the liquid phase in equilibrium with the SrS and SiO₂ phases at 1150, 1050 and 1000 °C are presented in Table 4.2. The preceding optimization of this ternary system, based only on the data from the literature, was refined to fit the experimental data obtained in the present work. The present final optimized value of the eutectic temperature is 991 °C. The average values of the liquid composition are reasonably well fitted in Fig. 4.1; these are same points which are plotted in Fig. 3.18.7, but in mole fraction.

Composition	A (mass %)	Composition B (mass %)	
$SiO_2 = 46.98$ SrO = 47.72	}	$SiO_2 = 37.56$ SrO = 43.59	
$B_2O_3 = 5.39$		$B_2O_3 = 18.84$	
Melted for 20 min at 1300 °C to form sample 1		Melted for 20 min at 1250 °C to form samples 2 to 5	
	Temperature (°C)	Days	
Sample 1	1150	10	
Sample 2	1050	15	
Sample 3	1000	15	
Sample 4	950	20	
Sample 5	900	20	

Table 4.1 Compositions studied and different heat treatment of sample in the $SrO-B_2O_3-SiO_2$ system.

Table 4.2 Composition analysis of the liquid phase by EPMA in equilibrium with SiO₂ and SrSiO₃ at 1150 °C (Sample 1) 1050 °C (Sample 2) and 1000 °C Sample 3 (Compositions in mass % and B_2O_3 (from difference) = 100-SrO-SiO₂).

Name	$\underset{analysis)}{B_2O_3(\mathrm{from}}$	SrO	SiO ₂	Total	B_2O_3 (from difference)
Sample 1	6.0	43.1	44.7	93.8	12.2
Sample 1	8.8	43.9	45.1	97.8	11.0
Sample 1	7.4	43.1	45.0	95.5	11.9
Sample 1	7.3	44.2	44.7	96.2	11.1
Sample 1	7.0	43.9	44.1	95.0	12.0
Sample 1	7.4	43.5	45.0	95.8	11.5
Sample 1	8.5	44.2	44.9	97.7	10.9
Sample 1	7.8	44.7	45.1	97.5	10.2

Sample 1	9.0	42.5	45.4	96.9	12.2
Sample 1	7.9	43.9	45.3	97.1	10.8
Average Std.	7.7	43.7	44.9	96.3	11.4
Deviation	0.91	0.65	0.36	1.30	0.67
Sample 2	9.0	45.2	37.0	91.2	17.7
Sample 2	9.7	44.9	37.0	91.5	18.1
Sample 2	8.9	46.1	37.6	92.5	16.4
Sample 2	11.0	45.6	37.2	93.8	17.2
Sample 2	10.3	45.8	37.3	93.4	16.9
Average Std.	9.8	45.5	37.2	92.5	17.3
Deviation	0.92	0.46	0.23	1.14	0.68
Sample 3	13.8	45.6	33.7	93.1	20.7
Sample 3	11.1	45.4	33.7	90.2	20.9
Sample 3	10.6	45.3	34.2	90.2	20.5
Sample 3	14.0	45.4	33.7	93.0	20.9
Sample 3	11.9	44.5	33.8	90.2	21.7
Average Std.	12.3	45.2	33.8	91.3	20.9
Deviation	1.52	0.45	0.23	1.59	0.48



Fig. 4.1 The liquid phase in equilibrium with SiO₂ and SrSiO₃ phases.



Fig. 4.2 BSE image of sample 1 (1150 °C).


Fig. 4.3 BSE image of sample 2 (1050 $^{\circ}$ C).



Fig. 4.4 BSE image of sample 3 (1000 $^{\circ}\text{C}$).



Fig. 4.5 BSE image of sample 4 (950 $^{\circ}\text{C}).$



Fig. 4.6 BSE image of sample 5 (900 $^{\circ}\text{C}\text{)}.$



Fig 4.7 WDS spectra of the four phases (boron was not scanned here).

CONCLUSIONS

As the aim of the present work was to prepare a critically evaluated thermodynamic database as part of a broader research project to develop a multicomponent database for the CaO-MgO-BaO-SrO-Al₂O₃-B₂O₃-SiO₂ system, 11 binary, 17 ternary and 5 quaternary were critically evaluated and optimized. All the available thermodynamic and phase equilibria data were critically evaluated in order to obtain one set of optimized model parameters representing the Gibbs energies of all the phases in these systems. The reliable experimental data were reproduced within the experimental error limits. The Modified Quasichemcial Model (MQM), capable of taking into account short-range ordering in the solutions, was used to model the liquid phase. The optimized enthalpies of mixing in the liquid phase in the binary systems containing SiO₂, Al₂O₃ and B_2O_3 are quite negative and of the order of -100 kJ/mol of oxides . This is an indication of strong short-range ordering in the liquid phase.

No reliable experimental data are available for the liquid phase in the BaO-SrO, BaO-CaO, BaO-MgO, SrO-CaO and SrO-MgO systems (Sec. 2.3). The liquid in these systems was assumed to be an ideal solution. Phase diagram data for the miscibility gap in the monoxide phase in the BaO-SrO and SrO-CaO systems were reproduced well. Interaction parameters for the monoxide phase in the BaO-CaO, BaO-MgO and SrO-MgO systems were estimated, in the absence of any experimental data in the literature, by an ionic radii function from the literature (Sec. 2.3).

The thermodynamic properties of the solid phases in the $SrO-SiO_2$ (Sec. 2.4) and $BaO-SiO_2$ (Sec. 2.5) systems are better known in the literature than the thermodynamic properties of the liquid

phase in these systems. The ΔH^{0}_{298} and S^{0}_{298} of the ortho- and meta-silicates in these systems are well reproduced in the present work. All the phase diagram and thermodynamic data were simultaneously optimized to obtain the thermodynamic properties of the liquid phase. The available phase diagram data in these systems were reproduced quite satisfactorily.

The different phase diagram data available in the literature for the SrO-Al₂O₃ system are not very consistent (Sec. 2.6). The same is true of the BaO-Al₂O₃ system (Sec. 2.7). This caused a difficulty in fitting the available data in these binary systems. The final decision on the optimized thermodynamic parameters for these binary systems was based also upon the optimization of the ternary systems containing these binary systems. In such cases higher-order phase diagram data are helpful in deciding the efficacy and reliability of the binary optimized parameters.

The different phase diagram and thermodynamic data in the BaO-B₂O₃ (Sec. 2.8) and SrO-B₂O₃ (Sec. 2.9) system were well reproduced. The BaO-B₂O₃ system is the only system among those optimized in this work in which there are enthalpy of mixing data in the liquid phase. These data were reasonably well reproduced. In the literature, mass spectrometric measurements of the B₂O₃ gas was used to report the enthalpy of formation for some of the solid phases in these binary systems. In the present work, the original data of B₂O₃ vapor pressure, rather than the derived quantity in terms of enthalpy of formation for the solid phases, were used in the optimization.

All the available data in the BaO-SrO-SiO₂ (Sec. 3.1) CaO-SrO-SiO₂ (Sec 3.2), and BaO-CaO-SiO₂ (Sec 3.3) systems were well reproduced. No ternary interaction parameter was required for

the liquid phase in the BaO-SrO-SiO₂ system and very small interaction parameters were used for the liquid phase in the CaO-SrO-SiO₂, and BaO-CaO-SiO₂ systems. The optimized thermodynamic parameters from these systems reproduced reasonably well the available data in the higher-order CaSiO₃-SrSiO₃-BaSiO₃ system (Sec. 3.4). The solubility limits of the various solid phases such as wollastonite, pseudowollostanite, walstromite, appearing in these systems were well reproduced.

The various phase diagram data in the temperature range 1200-1700 °C for the SrO-MgO-SiO₂ system (Sec. 3.5) are well reproduced. The diopside phase (a stable phase in the CaO-MgO-SiO₂ system) is not stable in the SrO-MgO-SiO₂ system. However, there are reported data for the solubility of strontium in this phase. This solubility limit was well reproduced together with the other phase diagram data in the CaO-SrO-MgO-SiO₂ (Sec. 3.6) system.

No thermodynamic data are available for the five ternary compounds in the BaO-MgO-SiO₂ system (Sec. 3.7). The available phase diagram data in this system are reasonably well reproduced. However, during optimization the need was discovered to restrict the various degrees of freedom for some thermodynamic data for these ternary compounds. No reliable phase diagram data were present for the BaO-SrO-MgO-SiO₂ system (Sec. 3.8). The only available data on the akermanite section in this system were tentatively optimized. The solubility limits in the merwinite section in the BaO-CaO-MgO-SiO₂ (Sec. 3.9) system were well reproduced.

All the available data in the CaO-SrO-Al₂O₃ (Sec. 3.10), BaO-CaO-Al₂O₃ (Sec 3.11) and BaO-SrO-Al₂O₃ (Sec. 3.12) systems were well reproduced. No ternary interaction parameters were required for the liquid phase in the BaO-SrO-Al₂O₃ and BaO-CaO-Al₂O₃ systems. A very small interaction parameter was used for the liquid phase in the CaO-SrO-Al₂O₃ system. The solubility limits in the metaaluminate phases in these systems were well reproduced. The optimized thermodynamic parameters for these metaaluminates well reproduced the available data in the higher-order CaAl₂O₄-SrAl₂O₄-BaAl₂O₄ system (Sec. 3.13). The BaO-MgO-Al₂O₃ system (3.14) is relatively less well determined. In fact, only a few data on the solid phase equilibria in the Al₂O₃-rich corner are available in the literature. The Gibbs energy of the liquid phase in this system was estimated solely from the corresponding binary systems.

For the alumino-silicate systems BaO-Al₂O₃-SiO₂ (Sec. 3.15) and SrO-Al₂O₃-SiO₂ (Sec. 3.16) which have complex liquid structures, BaAl₂ and SrAl₂ associates were included as a separate component, to take into account the charge compensation effect, of the liquid phase. The thermodynamic modeling of such liquid solutions by double substitution of Si atoms by Al atoms has not been reported before in the literature. This double substitution method has been used first time in the present work. This helped in fitting the available data in these systems. These associates are practically unstable in these binary systems, but are stable in appreciable amounts in the ternary systems in the SiO₂-rich corner. In the alumino-borate systems BaO-Al₂O₃-B₂O₃ (Sec. 3.21) and SrO-Al₂O₃-B₂O₃ (Sec. 3.22), relatively large numbers of parameters were required to fit the available data. The reason for this could again be the complex structure of the liquid phase in these systems. The MQM is not intended to provide a complete theory for these complex liquid structures. It is rather a mathematical formalism capable of properly reflecting

structural changes in a solution. It has the characteristics required for relatively reliable interpolations and extrapolations. Hence, sometimes these methods, such as introducing a separate component in the liquid phase or using a large number of parameters, might be required to fit the available data.

The available phase diagram data in the BaO-SrO-B₂O₃ system (Sec. 3.19) were reasonably well reproduced. Very small interaction parameters in the liquid phase were used. The solubility limits of the solid metaborate phases were well reproduced. In the literature, no reported phase diagram data are available for the liquid phase in the BaO-CaO-B₂O₃ system (Sec. 3.20). The Gibbs energy of the liquid phase in this system was estimated solely from the corresponding binary systems. The reported subsolidus phase equilibria were well reproduced. The thermodynamic properties of the three ternary components in this system were optimized on the basis of these subsolidus phase equilibria.

The BaO-B₂O₃-SiO₂ system (Sec. 3.17) has been well studied and all the data were reasonably well reproduced. Ternary interaction parameters were also added for optimal fit of the available data. In the present work, a few experiments were performed in the SrO-B₂O₃-SiO₂ system (Chapter 4) to fill the gap caused by missing data in this system. These newly obtained data improved the thermodynamic optimization of this system (Sec. 3.18). The experiments were designed to generate the maximum amount of information with a minimum number of experiments using the preceding optimization (based only on the data available in the literature) as a guide. The reported activities, obtained by high-temperature mass spectrometry, for the

liquid phase in the $BaO-B_2O_3-SiO_2$ and $SrO-B_2O_3-SiO_2$ systems were given less weight during optimization of the available data. More experimental work is required to corroborate these data.

For the eight ternary systems (in the present seven-component system) where no experimental data were available, the Gibbs energy of the liquid phase was estimated from the corresponding binary systems using different "geometric model". The use of future experimental data on these systems will enhance the applicability of the databases prepared in the present work. The present optimized thermodynamic parameters will be incorporated into the FToxide database of the FactSage thermochemical software and be made available to users for various applications.

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