

Research Article

Plant Location Selection for Food Production by Considering the Regional and Seasonal Supply Vulnerability of Raw Materials

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Received 16 October 2018; Accepted 19 November 2018; Published 10 December 2018

Academic Editor: Thomas Hanne

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A production capacity analysis considering market demand and raw materials is very important to design a new plant. However, in the food processing industry, the supply uncertainty of raw materials is very high, depending on the production site and the harvest season, and further, it is not straightforward to analyze too complex food production systems by using an analytical optimization model. For these reasons, this study presents a simulation-based decision support model to select the right location for a new food processing plant. We first define three supply vulnerability factors from the standpoint of regional as well as seasonal instability and present an assessment method for supply vulnerability based on fuzzy quantification. The evaluated vulnerability scores are then converted into raw material supply variations for food production simulation to predict the quarterly production volume of a new food processing plant. The proposed selection procedure is illustrated using a case study of semiprocessed kimchi production. The best plant location is proposed where we can reduce and mitigate risks when supplying raw material, thereby producing a target production volume steadily.

1. Introduction

Plant design involves major business considerations, including market demand, plant location, nature of the product, construction and operation costs, production capacity, government policy, climate, and potential competitors [1–5]. In particular, strategic decisions for plant location and production capacity are the key for business success in the food processing industry since these decisions in the early plant design phase predetermine most of the plant operation cost.

The plant location decision has often been formulated as a cost optimization problem by converting the associated decision attributes into monetary values. This cost optimization model usually involves decision making regarding the following attributes: market demand, production and storage capacity, production cost, and supply reliability [6–12]. This optimization model has been extended by incorporating uncertainty—variation of population, changeable market trends, and unpredictable demand—into the decision-making process [13].

A food plant is usually located close to either customers or raw material growing regions, depending on the nature of the product. In addition, the daily production volume must be carefully planned to avoid shouldering the extra cost of excessive production [14, 15]. Thus, the plant location decision can be considered from a supply reliability standpoint. Although the stable supply of raw materials has often been assumed in previous production capacity analysis, this ideal assumption does not always hold in food production. In other words, there are many sources of uncertainty, including quality deterioration, seasonal variation of production quantity, unstable climate, and natural disasters [16, 17]. In general, a decision model for plant location selection requires a precise estimation of the production capacity of each prospective location for which several simulation-based methods have been proposed in the literature; it is not straightforward to analyze too complex food production systems by using an analytical optimization model [18–21].

This study presents a simulation-based decision support model to select the right location for a new food processing

plant. In particular, the simulation model of food production accounts for the supply uncertainty of raw materials depending on the production site and the harvest season in the food processing industry. However, it is very difficult to make precise decisions in complex and uncertain problems if the acquired data is imprecise or insufficient [22, 23]. In order to overcome this difficulty, we define the supply vulnerability factors of raw materials such as production quantity in a food-growing region, market demand, and distance. All these factors are assessed and aggregated to determine the degree of vulnerability in the form of fuzzy rules. The evaluated vulnerability scores are then converted into raw material supply variations for food production simulation to predict the quarterly production volume of a new food processing plant. For production simulation, we conduct the probability distribution analysis to estimate the supply failure rate and the duration of failure. Finally, we simulate the daily food production volume in all prospective plant locations and select a location that guarantees the production of the target quantity, despite the unstable supply of raw materials. The simulation results, in fact, help decision stakeholders make a relative rank order, even without sufficient supply failure data, and eventually, the final selection is made based on the relative ranking. The proposed selection procedure is illustrated using a case study of semiprocessed kimchi production.

2. Related Works

The plant location selection problem is normally considered as a part of supply chain network design. To minimize the total cost as well as determine an optimal flow path for a product, previous studies have focused on demand variations, because the quality of decisions can easily vary due to supply and demand uncertainty, ambiguous information, and various social problems in the global business network [9, 24, 25]. It is likely that a stochastic model, rather than a deterministic approach, can be used to express demand uncertainty. Wang et al. [7] used a stochastic programming model that implies uncertain demand to find a location that maximizes business profits. Amin and Zhang [9] also considered the demand and return uncertainty of a product through the stochastic programming model. Moreover, they included environmental factors, such as the use of eco-friendly materials and clean technology, and used the weighted sum method as well as the ε -constraint method for multiobject optimization. Gülpınar et al. [26] proposed two types of demand distributions (i.e., normal distribution and context intended distribution) regarding facility location in a dynamic environment. Besides that, Wagner and Neshat [27] applied the quantification method to assess supply chain vulnerability. Based on the graph theory, their method of quantifying vulnerability can be dynamically adapted, even if the supply chain is frequently redesigned. In short, the quantification of the supply vulnerability of a food production system must consider production variables such as the properties of food raw materials, changes in production quantities during different seasons, and dynamic market changes [28].

In addition to fuzzy-based research, several optimization models for supporting decision making have been proposed. Jouzdani et al. [29] proposed a fuzzy model that used a triangular membership function to deal with demand uncertainty in a dairy plant. They considered traffic congestion as an essential factor for selecting the location because the dairy industry is very sensitive to demand variations and the localization of the food industry usually affects supply chain costs. Çebi and Otay [1] proposed a fuzzy-based location selection model for a cement plant by considering various qualitative factors such as availability of resources, strategic factors, government policies, and environmental factors. Mirhadi Fard et al. [6] considered environmental, social, and economic impacts as qualitative decision criteria to choose a sustainable plant location. Moreover, they took into account continuously changing geographic information in the service region and specified spatial characteristics such as accessibility of raw materials and proximity to the market. Rezaei and Zarandi [30] proposed a fuzzy model for dealing with dynamic environments at the initial location of a plant. They also developed a simulation model to recognize any changes in the service region. Moreover, applying seasonal parameters is one solution for ensuring the reliability of a decision model for plant location. Ozgen and Gulsun [31] used triangular possibility distribution (a fundamental part of the possibility theory) to deal with supply and demand uncertainty, along with climate as a seasonal parameter. More specifically, they combined the possibility distribution with the fuzzy analytic hierarchy process (AHP) method to handle both the quantitative and qualitative factors in the decision-making process. However, it is difficult to decide the shape of a membership function for representing the aggregation of data set in fuzzy-based decision-making model; hence the specialist interviews are usually required. Fuzzy TOPSIS approaches have been proposed for selecting a plant location by linguistically evaluating the following criteria: availability of skilled workers, expansion possibility, availability of acquirement material, and investment cost [32]. Aqlan and Lam [33] proposed a fuzzy-based method for supply chain risk assessment and quantified aggregate information, such as expert knowledge, historical data, and supply chain structure, to identify potential risks. Deb and Bhattacharyya [18] proposed a distinct decision support system that uses a multifactor fuzzy inference system for facility layout planning. Dweiri and Meier [19] also applied fuzzy decision making to facility layout planning and used the distance between departments and their relationships for scoring the planned layout.

Askin et al. [34] proposed a genetic algorithm-based method for warehouse location selection and determined the best capacity design for the selected warehouse. They also set the objective function to minimize costs due to demand variations, after which the optimal economic order quantity was derived to continuously adapt to the volatile inventory levels. However, metaheuristic optimization methods such as genetic algorithm-based optimization sometimes require a lot of time to find the optimal solution. Novaes et al. [35] used the Voronoi diagram, useful for conducting spatial analysis, to divide an urban region into service districts.

It is important to note that the process parameters of a production system, which determine the productivity of a plant, help decision makers improve the quality of their decision regarding location selection. In this regard, Silva and De La Figuera [36] proposed the integrated approach to find the best plant location using both a stochastic model of a manufacturing system and a deterministic location model. Their study examines the arrival time of customers as well as the processing time and capacity planning of the manufacturing system. Gebennini et al. [37] considered production lead time and delayed quantities of a product to determine demand variations and supply uncertainty. Consequently, in order to make more accurate decisions, various uncertain environmental factors need to be assessed by the appropriate quantification methods.

Vulnerability assessments usually underpin supply chain management due to the quantification of uncertain disturbances for mitigating risk [38, 39]. Albino et al. [40] proposed a quantification method to measure the vulnerability of a production system within a multisupplier network and evaluate critical aspects using two factors, i.e., process uncertainty and product mix variability. Petrovic et al. [41] developed the supply chain simulator to analyze the dynamic behaviour of a serial supply chain in an uncertain environment. For this purpose, they proposed discrete fuzzy sets for modeling uncertain situations in customer demand and external supply to determine the negative effects. Vorst et al. [42] identified sources of uncertainty (e.g., decision process time, order lead time, and order sales period) to improve supply chain performance and validated the trends predicted by the simulation model. Vljajic et al. [28] proposed an integrated framework for guiding food companies, in which supply chain robustness was defined to identify various disturbances through the classified sources of supply chain vulnerability, including external and internal sources that are either controllable or uncontrollable. However, their research mainly focused on internal sources of vulnerability to design robust food supply chains.

In the food industry, since fresh products have a limited shelf life, it is particularly difficult to have many goods in stock at all times [33]. Thus, supply chain management and production planning for fresh products should be carefully conducted when the inventory levels are low [43, 44]. It is important to note that the supply failure of raw materials caused by inaccurate demand predictions and tardiness of finished (or semifinished) products are major factors that trigger vulnerability, which can ultimately disrupt production. Furthermore, as the food industry becomes more globalized, the importance of optimal supply chain management has increasingly been emphasised [45].

Previous studies have seldom considered an integrated approach for selecting the best plant location using both stochastic simulation and vulnerability quantification, even though many studies have addressed simulation-based optimal layout design. Further, most of the studies considered the supply of raw materials to be relatively stable. Therefore, this study proposes an integrated approach that combines a supply vulnerability analysis and statistical simulation to deal with various uncertain factors (e.g.,

unstable supply of food raw materials) during plant location selection.

3. Simulation-Based Plant Location Selection

3.1. The Plant Location Problem

3.1.1. Cabbage Production Quantities and Supply Failure Data. The problem in hand is to select the best location for a new semiprocessed kimchi plant by using the imprecise information provided by our research partner, World Institute of Kimchi. This information includes food production conditions, plant operation data, and average supply failure data as shown in Figure 1.

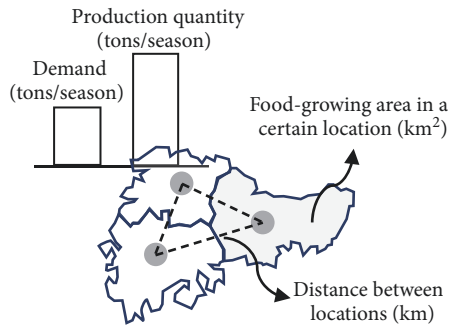
The proposed model for plant location selection is aimed at supporting decision makers when they have difficulty in estimating a suitable distribution form related to supply failures for simulation modeling due to the lack of information. In other words, we could not estimate a probability density function using the conventional distribution fitting because there was no detailed supplier failure information such as date and duration of each failure in a specific region. We approximated distribution forms by a fuzzy supply vulnerability analysis based on food production conditions and average supply failure data as shown in Figure 1. It is recommended for decision makers to choose normal, exponential, and gamma distributions that have been widely used for failure occurrence modeling in the literature.

Figure 2 illustrates the food production conditions for the eight prospective locations and the four seasons which include the production quantities in locations, the area of the production region, the demand for food raw materials, the number of customers, and the annual mean temperature. These conditions play critical roles in determining the seasonal production quantities.

It is assumed that the delivery distance for raw materials is related to the area of the production and, hence, the delivery time in a relatively large area is longer than that in a small area. For the sake of simplicity, other decisive factors, such as delivery cost per mile, taxation, plant construction, operation cost, and local government policies, are assumed to be the same for all locations.

3.1.2. Plant Location Selection Procedure. This section presents the basic ideas of plant location selection considering the unstable supply of food raw materials. In the food industry, unexpected conditions, such as natural disasters, abnormal climate, or the abandonment of cultivation, sometimes lead to shortfalls in the supply of raw materials. In this case, a food manufacturer should search for alternative sources for food raw materials in other regions. We take this supply shortage situation into account for a supply vulnerability factor, that is, the possibility of replacing raw material feedstock using alternative sources. It can be said that if the possibility is small, the supply vulnerability is high. The plant location selection procedure is illustrated by a case study of semiprocessed kimchi production. The case study was chosen upon the request of our research partner, World

Food production conditions in specific locations (detailed in Figure 2)



Average supply failure data

Supply failure information [#]	Average	Min.	Max.
Supply failure rate (occurrences per season)	1.5	0	5
Duration of a supply failure (day)	2.5	1	20

[#]: World Institute of Kimchi (<https://www.wikim.re.kr>)

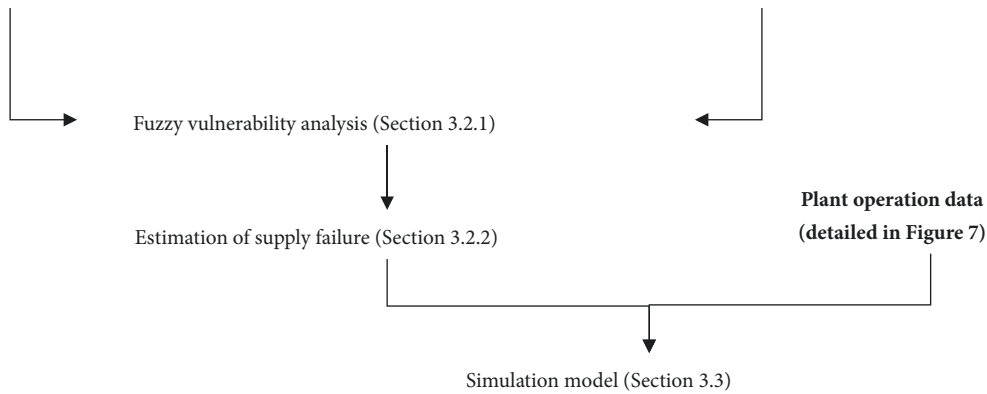


FIGURE 1: The given information for plant location selection.

Institute of Kimchi, who are aiming to construct a new kimchi processing plant in a suitable location.

Kimchi is a traditional Korean side dish made by combining cabbage and other fermented vegetables in a salted brine. Recently, there has been a strong customer demand for semiprocessed kimchi and, hence, many food manufacturers have focused their attention on building new semiprocessed kimchi plants that can automatically produce salted cabbage on a large scale. The main raw materials for this process include a considerable amount of cabbage, salt, and water, of which the stable supply of cabbage is the most important, irrespective of seasonal and regional variations.

As illustrated in Figure 3, the plant location selection procedure involves the supply vulnerability analysis by estimating supply failure rates and failure durations and stochastic simulation as follows:

Step 1 (vulnerability analysis). Quantify the fuzzy supply vulnerability from the standpoint of regional and seasonal instability in the supply of raw materials.

Step 2 (simulation modeling).

- (i) Convert the quantified supply vulnerability scores (the instability level of raw material supply in a specific region) into raw material supply variations.
- (ii) Estimate supply failure rates (the number of supply failure occurrences per season) from the supply vulnerability scores.

- (iii) Adjust the probability density functions for the supply failure durations (inter-supply failure time).

- (iv) Specify production process parameters (e.g., malfunction rate, processing time).

Step 3 (simulation-based location selection).

- (i) Adjust the daily utilization of a production system.
- (ii) Calculate a target production volume and an estimated production volume using the adjusted daily utilization.
- (iii) Determine the best plant location.

Table 1 summarizes the variables used in the production volume estimation for the proposed method.

3.2. Supply Failure Estimation by a Fuzzy Vulnerability Analysis

3.2.1. Fuzzy Vulnerability Analysis. For supply failure estimation, the supply vulnerability of food raw materials is incorporated into the simulation model in which three main vulnerability factors are involved: raw material availability, production efficiency of raw material, and possibility of replacing raw material feedstock using alternative sources.

- (1) *Raw material availability* assesses whether the amount of raw materials meets the market demand, including the current consumption by competitors in a prospective plant location. It can be

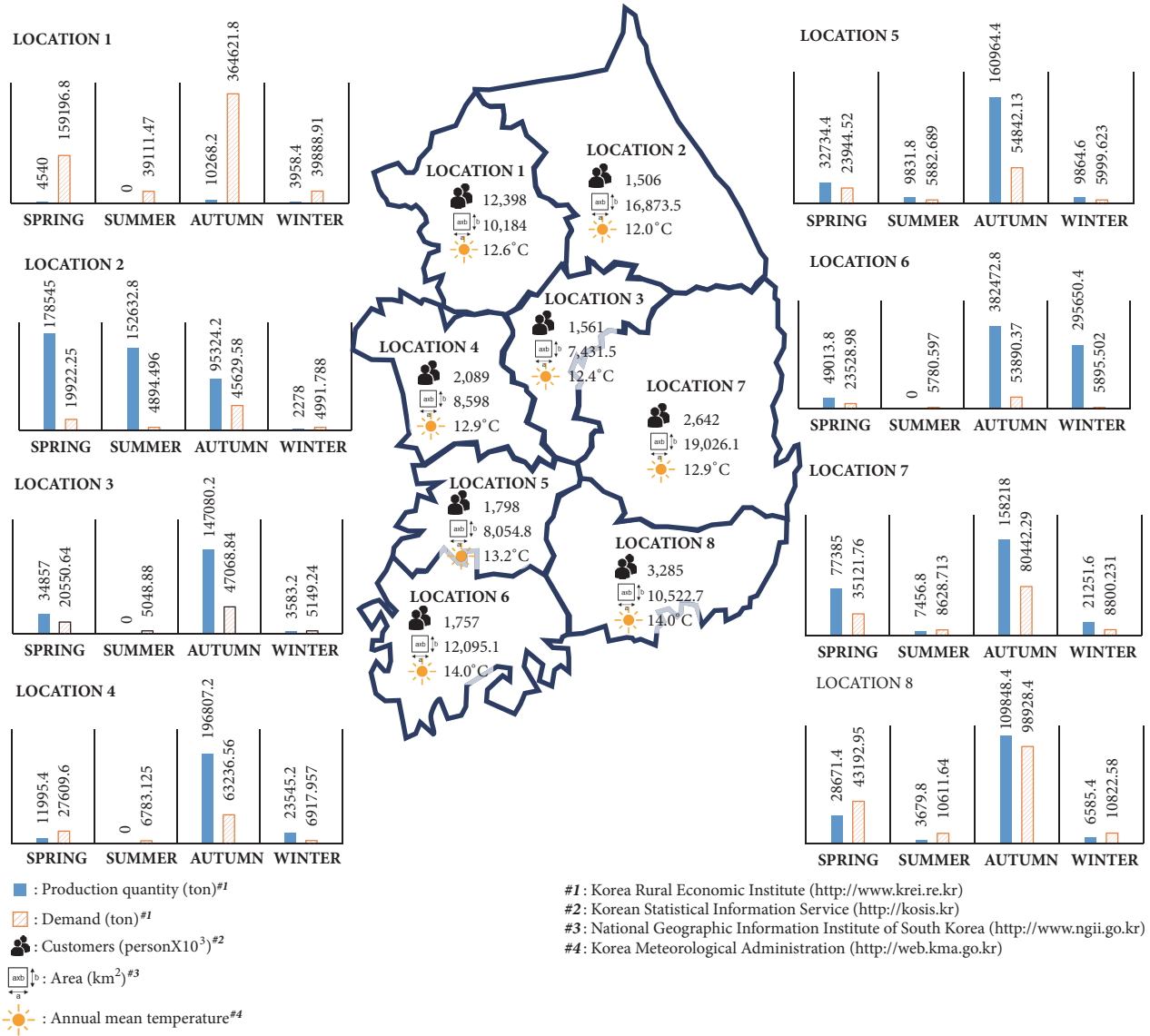
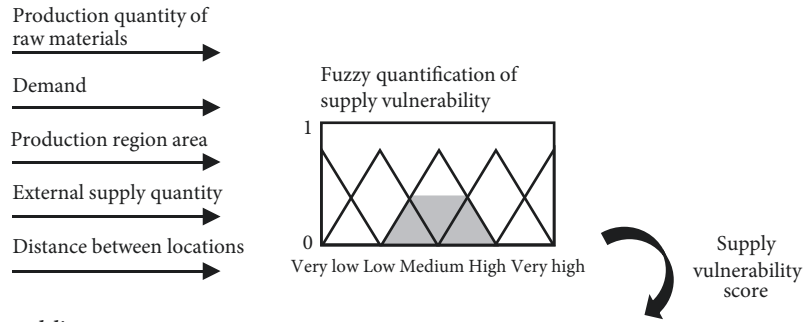


FIGURE 2: The given information of the production conditions for eight plant location candidates.

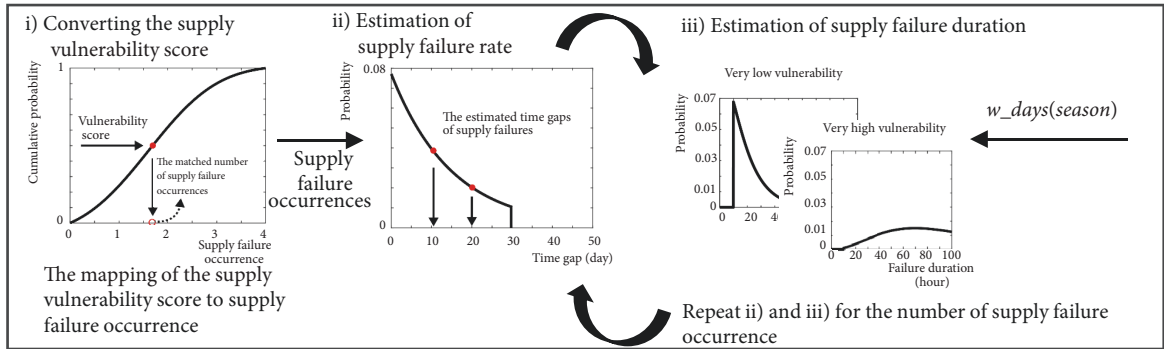
TABLE 1: Variables used in the production volume estimation.

Variables	Description	Unit
$P_T(\text{season})$	Target production volume	ton
$P_E(\text{location, season})$	Estimated production volume	ton
$w_days(\text{season})$	Total number of work days	day
w_hours	Maximum work hours per day	hour
$daily_util(\text{season})$	Daily utilization of a production system	%
$adj_daily_util(\text{location, season})$	Adjusted daily utilization of a production system	%
$prod_vol$	Production volume per hour	ton/hour
total utilization of a production system in the face of supply failures	-	hour
total utilization of a production system per season	-	hour
$supply_failure_time(\text{location, season})$	Total interruption time due to supply failures	hour

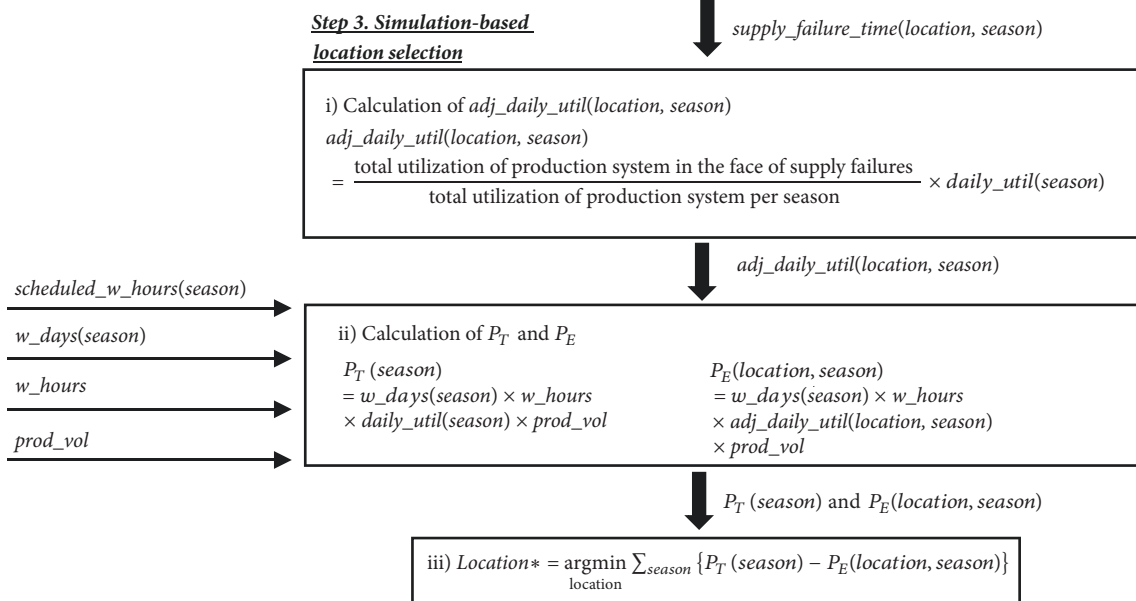
Step 1. Vulnerability analysis



Step 2. Simulation modeling



Step 3. Simulation-based location selection



- $w_days(season)$: the total work days during a particular season
- w_hours : the maximum work hours per day
- $daily_util(season)$: the daily utilization of the production system with respect to daily demand and production quantities
- $schedule_w_hours(season)$: the scheduled work hours per day for a particular season
- $prod_vol$: the production volume per hour (tons/hour)

FIGURE 3: The simulation-based selection procedure of a food plant location according to supply vulnerability.

linguistically assessed by considering the ratio of production quantity(location, season) to demand (location, season). production quantity(location, season) is the total amount of raw material growing in a location during a particular season, while

demand(location, season) is the market demand in a location during a particular season.

(2) *Production efficiency of raw materials* represents the proportion of the production quantity, relative to the food-growing area in a certain location. It can be said

TABLE 2: Fuzzy input data for the supply vulnerability of raw material.

Location	Season	RA	PE	PR	SVL	Location	Season	RA	PE	PR	SVL
1	Spring	L	L	H	H	5	Spring	H	L	L	M
	Summer	L	L	H	H		Summer	H	L	H	L
	Fall	L	H	H	L		Fall	H	H	H	VL
	Winter	H	L	L	M		Winter	H	H	L	VL
2	Spring	H	L	L	M	6	Spring	H	L	L	M
	Summer	H	L	L	M		Summer	L	L	L	VH
	Fall	H	H	H	VL		Fall	H	H	H	VL
	Winter	L	L	L	VH		Winter	H	H	L	VL
3	Spring	H	L	L	M	7	Spring	H	L	L	M
	Summer	L	L	H	H		Summer	H	L	L	M
	Fall	H	H	H	VL		Fall	H	H	H	VL
	Winter	L	H	L	H		Winter	H	L	L	M
4	Spring	L	L	L	VH	8	Spring	L	H	L	H
	Summer	L	L	L	VH		Summer	L	L	L	VH
	Fall	H	H	H	VL		Fall	H	H	H	VL
	Winter	H	H	L	L		Winter	L	H	L	H

Note: RA: raw material availability; PE: production efficiency; PR: possibility of replacing raw material feedstock; SVL: supply vulnerability level; VH: very high; H: high; M: medium; L: low; VL: very low.

that the higher the production efficiency, the smaller the supply vulnerability.

- (3) Possibility of replacing raw material feedstock using alternative sources represents easy accessibility of raw materials from the neighboring region, based on the fact that insufficient raw materials in a certain location can be supplemented from other locations, and it can be assessed (imprecisely) by the normalized ratio $(1/n) \sum_{i=1}^n (\text{surplus}_i / \text{distance}_i)$. Furthermore, n is the number of other locations that can support the insufficient raw materials for the location being assessed, surplus_i is the surplus of raw materials in the i^{th} location, and distance_i is the average distance between the prospective location and the i^{th} location that will affect delivery efficiency.

Imprecise linguistic assessments of prospective locations with respect to each factor make it difficult to do a direct quantitative evaluation of supply vulnerabilities. Fuzzy quantification is normally performed by clustering and aggregation. Experts often describe their assessment results by using linguistic descriptors such as high, medium, and small. Further, to consider the effects of unknown exogenous factors, a fuzzy aggregation method can be employed. For example, this study divided the levels of vulnerability factor values into two subgroups (i.e., low and high) using a fuzzy c-means clustering method with a conventional triangular-shaped membership function [46]. We used Xie-Beni index S , compactness and separation function, for data clustering to define a membership function, and it is efficient for easy calculation [47].

$$S = \frac{\sum_{i=1}^c \sum_{k=1}^n u_{i,k}^2 \|V_i - X_k\|^2}{n \min_{i,j} \|V_i - V_j\|^2}, \quad (1)$$

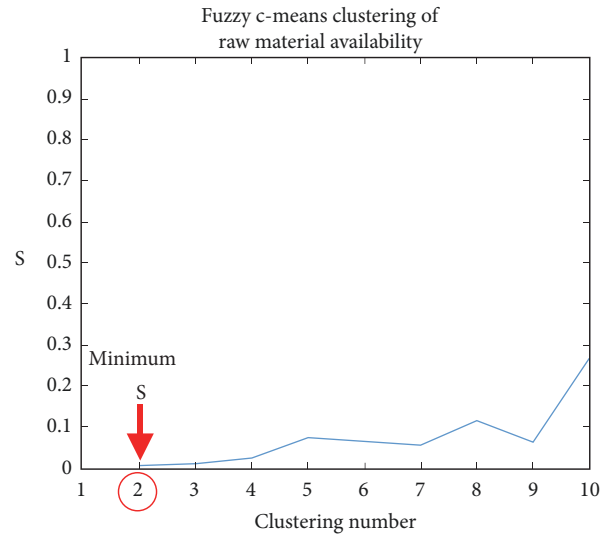


FIGURE 4: Fuzzy c-means clustering of raw material availability (S : Xie-Beni index).

where X_k is the k^{th} data point, V_i and V_j are cluster centroids, $u_{i,k}$ is the membership value of data X_k , and $\min_{i,j} \|V_i - V_j\|$ is the minimum distance between cluster centroids.

To find the optimal cluster number for fuzzy rules, it is necessary to find the minimum S . Figure 4 illustrates the clustering result of raw material availability, and the clustering number 2 that minimizes S will be selected as the level of vulnerability factor. Table 2 summarizes the fuzzy input data for the supply vulnerability of raw material. The conventional Mamdani method, which uses minimum implication and maximum aggregation, was employed, after which defuzzification was performed to derive an aggregated

TABLE 3: Summary of the supply vulnerability evaluation by fuzzy quantification.

Location	Season	RA	PE	PR	SVS	Location	Season	RA	PE	PR	SVS
1	Spring	7	4610	396	0.750	5	Spring	146	5244	210	0.459
	Summer	0	0	733	0.750		Summer	173	3779	432	0.250
	Fall	54	10746	620	0.250		Fall	302	10641	826	0.083
	Winter	128	3991	100	0.500		Winter	156	7187	210	0.104
2	Spring	939	4266	72	0.500	6	Spring	184	4901	153	0.500
	Summer	3302	3448	12	0.500		Summer	0	0	184	0.903
	Fall	231	9305	407	0.110		Fall	765	11574	378	0.113
	Winter	47	3831	80	0.899		Winter	1455	6072	42	0.161
3	Spring	159	4555	298	0.455	7	Spring	225	4451	196	0.500
	Summer	0	0	374	0.750		Summer	94	4041	293	0.541
	Fall	338	8696	694	0.093		Fall	211	10199	482	0.103
	Winter	71	5423	137	0.798		Winter	252	4381	89	0.500
4	Spring	41	4688	203	0.892	8	Spring	68	5641	176	0.757
	Summer	0	0	297	0.834		Summer	30	3800	215	0.899
	Fall	318	10253	628	0.092		Fall	114	11305	713	0.086
	Winter	368	5743	109	0.327		Winter	57	5703	125	0.755

Note: RA: raw material availability; PE: production efficiency; PR: possibility of replacing raw material feedstock; SVS: supply vulnerability score.

vulnerability score by means of finding the center of gravity as follows:

$$\text{Center of gravity} = \frac{\sum_{x=a}^b \mu_A(x) x}{\sum_{x=a}^b \mu_A(x)}, \quad (2)$$

where $a \leq x \leq b$, $a, b \in \mathbf{R}$, $\mu_A(x)$ is a membership function.

The score was normalized to have a range from 0 to 1, with 1 meaning highly vulnerable. Table 3 summarizes the supply vulnerability evaluation. Note that if food raw materials are not cultivated in a particular season and region, such that the production quantity is zero, the values of raw material availability and production efficiency of raw materials are calculated to be zero as shown in Table 3.

3.2.2. Estimation of Supply Failure Rate and Duration. This subsection describes how to derive the number of supply failure occurrences per season and the inter-supply failure time from the supply vulnerability scores. This information will provide the foundation for estimating the supply failure rate and the duration of each supply failure.

From the estimated probability distribution of failure occurrences, f_N , it is possible to identify an empirical relationship between the supply vulnerability scores and the failure occurrences. As shown in Figure 5, supply vulnerability is proportional to the cumulative probability of the supply failure occurrences. There are minimum and maximum numbers of failure occurrences during a particular season in the historical data. Thus, the random variable should be restricted for failure occurrences within a specific range. To do this, we employed truncated distribution models [48] for supply failure occurrence and duration.

The supply vulnerability score obtained in the previous subsection determined the parameters of gamma distribution (e.g., the shape parameter and the scale parameter), as shown in Figure 6. In addition, the parameters of gamma

distribution were adjusted according to the failure duration information obtained by the supply vulnerability analysis. This was achieved by multiplying the average failure duration by the vulnerability score [49]. The shape parameter α and scale parameter β of the truncated gamma distribution f_G were estimated using the moments method; i.e., $\hat{\alpha} = (\bar{\mu}/\bar{\sigma})^2$, $\hat{\beta} = \bar{\sigma}^2/\bar{\mu}$, where $\bar{\mu}$ is the mean value of the historical data for failure durations and $\bar{\sigma}$ is its standard deviation. To include the vulnerability score in the gamma distribution, this study mapped the peak point of gamma distribution to the vulnerability score in the center of the fuzzy membership function. In this case, 0.5 was set as the reference value for which the peak point of gamma distribution correlated with supply failures, moved either to the left (more stable) or to the right (more vulnerable) (see Figure 6). The shape and scale parameters can be adjusted by modifying the mean value as follows.

$$\bar{\mu}^* = \bar{\mu} \times (0.5 + \text{Vulnerability Score}(\text{location}, \text{season})) \quad (3)$$

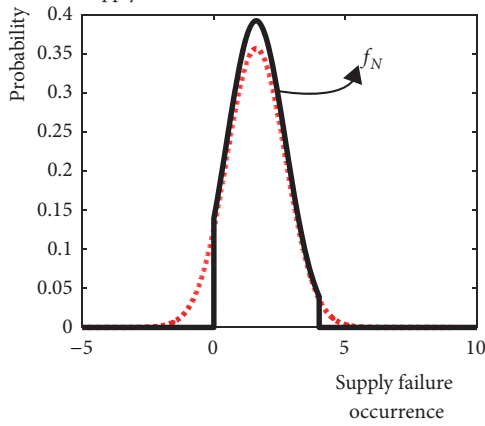
Finally, the obtained probabilistic distribution of supply failure duration simulates the daily utilization of a food production system in a location for a particular season, i.e., $\text{adj_daily_util}(\text{location}, \text{season})$ (see step 3 in Figure 3).

3.3. Simulation Model of Semiprocessed Kimchi Production.

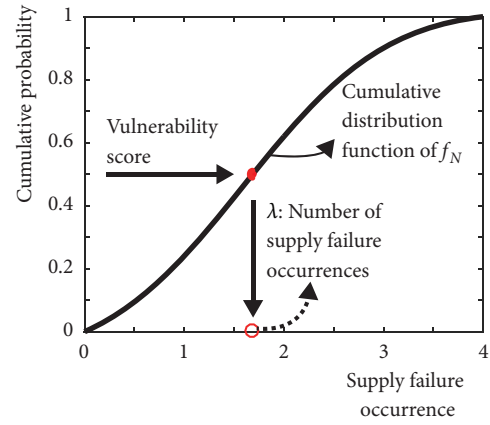
Initial conditions and process information for the simulation of semiprocessed kimchi production are given in Figure 7. The target production volume of a new plant is 2,000 tons/year. The initial inter-arrival time (IAT) of raw material supply is two days. The amount of raw material per order is set as twelve tons. Eight workers handle the entire production process and they work eight hours per day. The semiprocessed kimchi production process consists

1) The mapping process between the vulnerability score to the supply failure occurrences

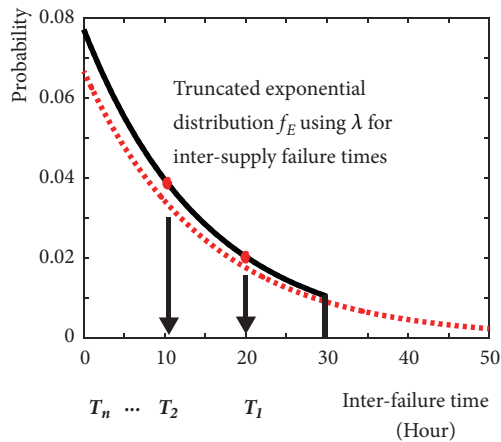
(i) Generation of probability density function f_N of truncated normal distribution from the history data of supply failure occurrences



(ii) Matching the vulnerability score to the cumulative probability of f_N



2) The estimation of supply failure rate



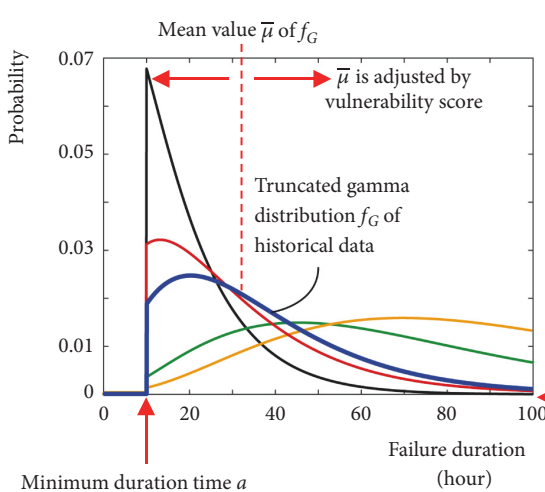
$$f_N(x; \bar{\mu}, \bar{\sigma}, a, b) = \frac{e\left(-\frac{(x-\bar{\mu})^2}{2\bar{\sigma}^2}\right)}{\sqrt{2\pi}\bar{\sigma} \left\{ \Phi\left[\frac{b-\bar{\mu}}{\bar{\sigma}}\right] - \Phi\left[\frac{a-\bar{\mu}}{\bar{\sigma}}\right] \right\}}$$

where Φ is the cumulative distribution function (CDF) of the probability density function (PDF) of the standard normal distribution, $a \leq x \leq b, a, b \in \mathbf{R}, \bar{\mu}$ is the mean value of historical data of supply failure occurrences, $\bar{\sigma}$ is the standard deviation of historical data

$$f_E(x; \lambda, b) = \lambda \frac{e^{-\lambda x}}{(1 - e^{-\lambda b})}$$

where λ is the number of supply failure occurrences, $0 \leq x \leq b$

FIGURE 5: Supply failure rate estimation for stochastic simulation.



$$f_G(x; \alpha, \beta, a, b) = \frac{\left(\frac{x}{\beta}\right)^{\alpha-1} e^{-\left(\frac{x}{\beta}\right)}}{\beta \left[\Gamma\left(\alpha, \frac{a}{\beta}\right) - \Gamma\left(\alpha, \frac{b}{\beta}\right) \right]}$$

where shape parameter $\alpha > 0$, scale parameter $\beta > 0$, a is the minimum supply failure rate of the historical data, b is the maximum supply failure rate of the historical data, $a \leq x \leq b$

FIGURE 6: Supply failure durations in the form of gamma distributions.

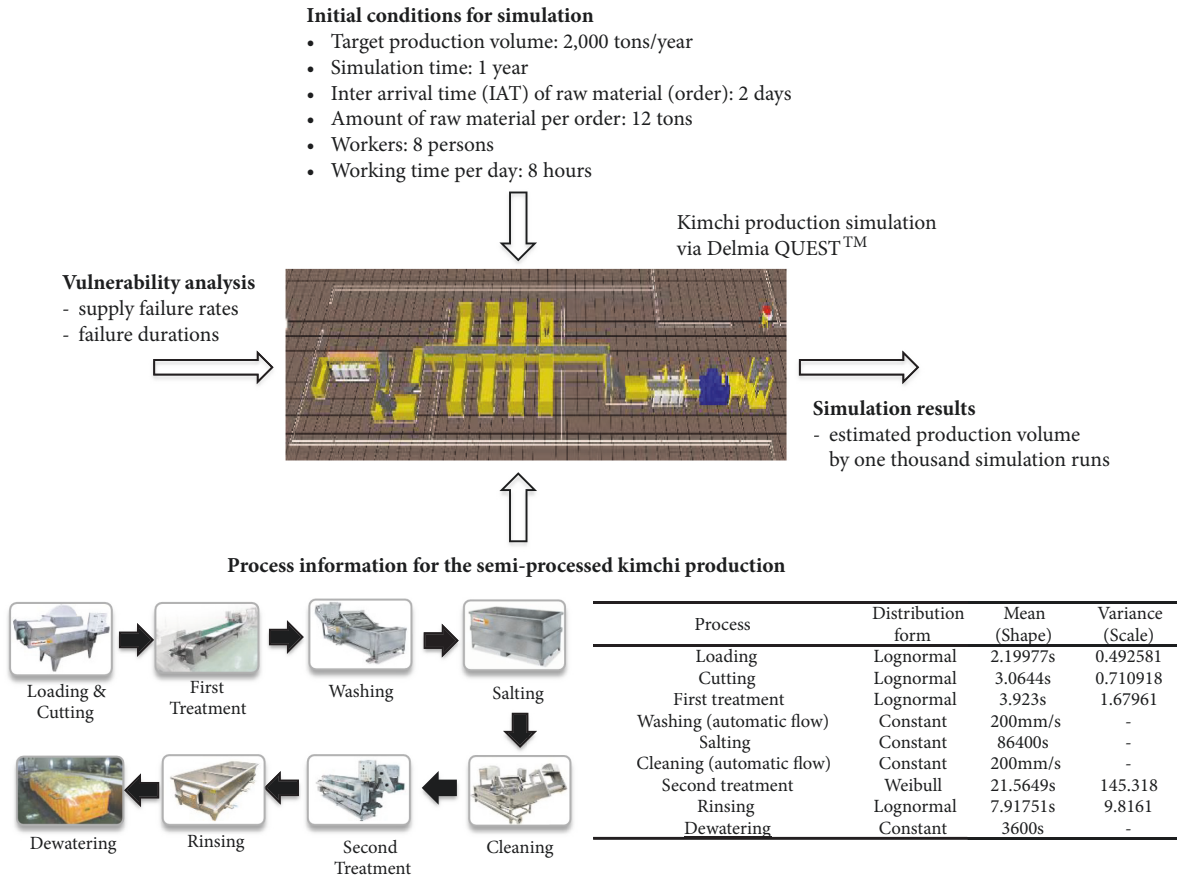


FIGURE 7: Initial conditions and process information for the simulation of semiprocessed kimchi production.

of nine processes: loading, cutting, first treatment, washing, salting, cleaning, second treatment, rinsing, and dewatering. The operation time information of each process is given in Figure 7. The vulnerability analysis was performed to provide the supply vulnerability scores, then the supply failure rates and durations are estimated in order to adjust IAT of raw material supply during simulation.

In the simulation, raw material supply continues to produce a demand quantity. In other words, twelve tons of raw material will be supplied every two days until the simulated production volume meets the demand quantity. For this reason, there is no oversupply of raw material in the simulation. On the other hand, in case of supply failure in the simulation, the production volume cannot meet the demand quantity in the required production time, and therefore an estimated production volume is always less than a planned target production volume.

We used a commercial software, Delmia QUEST™, to simulate semiprocessed kimchi production. The QUEST model consists of six main simulation elements: part (cabbage), source (part input), sink (processed part output), machine, labor, and buffer. Refer to Figure 7 for the detailed process information. The average simulation run time for one year production without 3D animation was 39 minutes (CPU: Intel Core i7-7700 3.6GHz, RAM: 16GB).

In summary, we conducted food production simulations by considering seasonal supply variations for more detailed evaluation. However, the proposed plant location selection model aims to rank order of prospective plant locations with respect to decision attributes such as production quantity of raw materials, demand, and food-growing area in a certain location. Therefore, the rank-ordering is still possible even in the case that there is no significant difference in the seasonal supply variations.

3.4. *The Best Location Selection of New Kimchi Plant.* In this study, the best plant location is the one where a planned target production volume can be steadily produced, despite the unstable supply of raw materials. It is formulated as follows:

$$\begin{aligned}
 & \text{Location*} \\
 & = \arg \min_{\text{location}} \sum_{\text{season}} \{P_T(\text{season}) - P_E(\text{location}, \text{season})\} \quad (4)
 \end{aligned}$$

where P_T is the target production volume for the new plant and P_E is the estimated production volume, considering the regional and seasonal supply vulnerability of food raw materials for the prospective location. The target production volume for a particular season, $P_T(\text{season})$, is determined by:

$$\begin{aligned}
 P_T(\text{season}) &= w_days(\text{season}) \times w_hours \\
 &\quad \times \text{daily_util}(\text{season}) \times \text{prod_vol} \quad (5)
 \end{aligned}$$

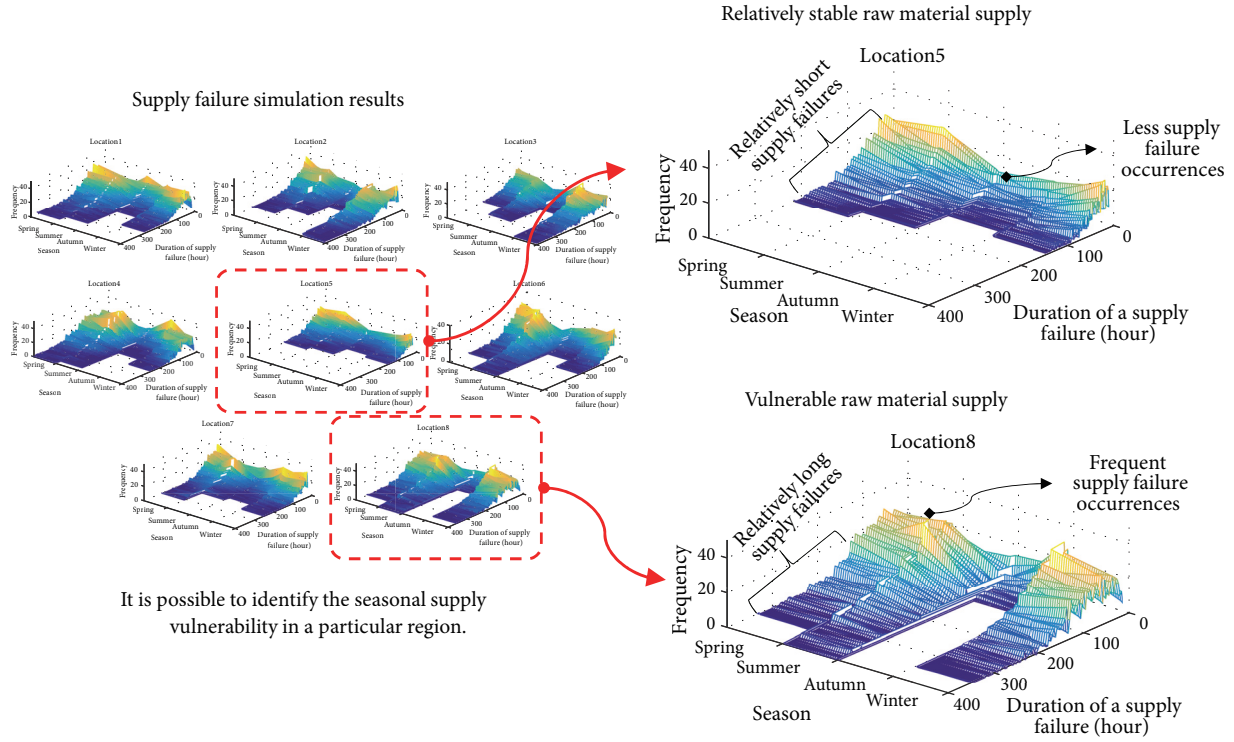


FIGURE 8: The simulation results of supply failure in locations for a year; repetition of simulation: 1,000 times; supply failure rate (occurrences/season): average 1.5, min. 0, max. 5; duration of a supply failure (day): average 2.5, min. 1, max. 20.

where $w_days (season)$ is the total number of work days during a particular season, w_hours denotes the maximum work hours per day, and $daily_util (season)$ indicates the daily utilization of the production system with respect to daily demand and production quantities. In addition, the daily utilization is given by the ratio of the scheduled work hours per day ($scheduled_w_hours$) to w_hours , and $prod_vol$ is the production volume per hour (tons/hour). In general, $daily_util (season)$ is assumed to be sensitive to seasonal demand to maximize the utilization of the production system.

Conversely, the estimated production volume in a location for a particular season, $P_E(location, season)$, is obtained by the following.

$$P_E (location, season) = w_days (season) \times w_hours \times adj_daily_util (location, season) \times prod_vol \quad (6)$$

The adjusted daily utilization of the production system, $adj_daily_util (location, season)$, is determined by the following simulation analysis:

$$adj_daily_util (location, season) = \frac{\text{total utilization of a production system in the face of supply failures}}{\text{total utilization of a production system per season}} \times daily_util (season) \quad (7)$$

where

- (i) total utilization of a production system per season = $w_days(season) \times w_hours \times daily_util(season)$,
- (ii) total utilization of a production system in the face of supply failures = $w_days(season) \times w_hours \times daily_util(season) - supply_failure_time(location, season)$.

The supply failure time, $supply_failure_time (location, season)$, represents the total interruption time due to supply

failures during which normal food processing is impossible for a particular season at a certain location.

3.5. Results and Discussion. Figure 8 illustrates the simulation results of supply failure durations in each prospective location for one year. There are more frequent supply failures for a relatively long duration in location 8, particularly during spring, summer, and winter, whereas it can be said that the supply of food raw materials in location 5 is relatively

TABLE 4: The simulated daily utilization of a new plant in each location and the gap between the target production volume and the simulated production volume.

Location	The Estimated Supply Failure Duration (hour)				adj_daily_util	$\sum_{season} (P_T - P_E)$
	Spring	Summer	Autumn	Winter		
1	64.55	66.31	17.43	36.75	0.895	1850.52
2	38.30	37.71	8.27	95.93	0.898	1802.10
3	32.27	60.10	8.18	70.93	0.903	1714.88
4	91.33	76.53	7.23	22.67	0.888	1977.69
5*	33.93	18.45	7.06	7.53	0.962	669.67
6	36.84	97.52	8.28	35.10	0.899	1777.44
7	35.80	41.22	7.40	37.05	0.931	1214.68
8	67.39	92.49	7.58	66.84	0.867	2342.98

Note: $w_days(season) = 55$ days; $daily_util(season) = 1$; $w_hours = 8$ hours; $prod_vol = 10$ tonnes/hour. It is assumed that $w_days(season)$ and $daily_util(season)$ of each season are the adjusted daily utilization of the production system and the target production volume in one year is 17,600 tons.

TABLE 5: An example of the supply failure occurrences in location 8 (one year simulation).

Supply failure no.	Season	Delay (sec.)	Simulation clock (sec.) $\times 10^6$
1	Spring	131,994	2.2464
2	Spring	119,676	4.79759
3	Summer	136,321	7.33647
4	Summer	146,399	9.89199
5	Summer	105,495	12.4576
6	Autumn	87,110	14.9823
7	Autumn	90,635	17.4886
8	Winter	124,373	19.9984
9	Winter	112,405	22.542

stable, owing to less failure occurrences and shorter failure durations.

Table 4 summarizes the estimated supply failure duration for the four seasons, the simulation results of $adj_daily_util(location, season)$, the estimated production volume P_E in one year, and the gap between the target production volume P_T and P_E in one year. In addition, it is assumed that the total number of work days during a particular season $w_days(season)$ is 55 days, the maximum work hours per day w_hours is 8 hours, the daily utilization of the production system with respect to daily demand and production quantities $daily_util(season)$ is full (namely, 1), the production volume per hour $prod_vol$ is 10 tons/hour, and the target production volume in one year is 17,600 tons. The simulation results show that location 5 is the best prospective location in which the planned target production volume can be steadily achieved, despite the unstable supply of raw materials. As summarized in Table 4, the estimated supply failure duration in autumn is relatively short compared to the other seasons. This is because autumn is the harvest season, and thus raw material supply is relatively stable. Table 5 shows an example of supply failure occurrences in location 8 according to the result of one year simulation by using Delmia QUEST™, and the simulation result also shows that the supply failures in autumn are relatively shorter than the other seasons.

4. Conclusion

This study proposed a plant location selection procedure by simulating the daily production volume and considering the supply failures of food raw materials. This process mainly consisted of quantifying the supply vulnerability of raw materials and incorporating the quantified vulnerability scores into the stochastic simulation. We proposed the three vulnerability factors: raw material availability, production efficiency of raw materials, and possibility of replacing raw material feedstock using alternative sources, in order to quantify the regional and seasonal supply vulnerability of raw materials. These factors were then incorporated into fuzzy quantification to estimate supply vulnerability scores. The estimated supply failure information included the time gaps between failures and the duration of each failure. This information was used to determine the adjusted daily utilization and the production volume of a prospective food production plant.

The proposed simulation model will be useful for decision makers to ordinally rank plant location candidates by relative comparison of simulated production volumes. However, it is not recommended to consider the estimated production volume as a cardinal performance measure of a candidate location due to the approximated supply failure distributions with the given imprecise information. In other

words, the proposed fuzzy vulnerability quantification and supply failure estimation methods enable simulation-based decision making even if supply failure data are not enough to estimate a probability density function using a conventional distribution fitting method.

The findings of this study can be applied and extended for two purposes: (1) to allow practitioners to effectively rank the prospective locations during the decision-making process and (2) to forecast the daily production volume of a plant in a particular location, given enough historical data, which is essential for detailed layout planning.

Data Availability

The supply failure data, food production conditions, and plant operation data used to support the findings of this study are included within the article.

Conflicts of Interest

The authors declare that they have no conflicts of interest.

Acknowledgments

This work was supported by the Korea Institute for Advancement of Technology under a research grant (no. P01070019) funded by the Ministry of Trade, Industry and Energy.

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