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# Singlet model interference effects with high scale UV physics 

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#### Abstract

One of the simplest extensions of the Standard Model (SM) is the addition of a scalar gauge singlet, $S$. If $S$ is not forbidden by a symmetry from mixing with the Standard Model Higgs boson, the mixing will generate non-SM rates for Higgs production and decays. In general, there could also be unknown high energy physics that generates additional effective low energy interactions. We show that interference effects between the scalar resonance of the singlet model and the effective field theory (EFT) operators can have significant effects in the Higgs sector. We examine a non- $Z_{2}$ symmetric scalar singlet model and demonstrate that a fit to the 125 GeV Higgs boson couplings and to limits on high mass resonances, $S$, exhibit an interesting structure and possible large cancellations of effects between the resonance contribution and the new EFT interactions, that invalidate conclusions based on the renormalizable singlet model alone.


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## I. INTRODUCTION

Among the simplest extensions of the Standard Model (SM) is the addition of a gauge singlet scalar particle, $S$. The singlet particle couples to SM particles through its mixing with the SM-like 125 GeV Higgs boson. In general, there can be additional interactions between the $S$ and the gauge bosons, which can be parametrized as effective field theory (EFT) dimension-5 couplings. The source of these effective interactions is not relevant for our discussion, and our focus is on the consequences of the interference effects between the heavy scalar resonance and the EFT operators. Since there are a relatively few number of EFT operators coupling the singlet to the $S U(3) \times S U(2) \times U(1)$ gauge bosons, it is possible to obtain interesting limits on the theory, despite the addition of new parameters.

In the absence of a $Z_{2}$ symmetry, the singlet model allows cubic and linear self-coupling terms in the scalar potential and a strong first order electroweak phase transition is possible for certain values of the parameter space [1-5], making this theory highly motivated phenomenologically. We begin by examining restrictions on the parameters of the non $-Z_{2}$ symmetric model from the measured 125 GeV Higgs couplings and from the requirement that the electroweak minimum be the absolute minima of the potential. We then include LHC limits on heavy resonances that decay into SM particles (assuming that there are no additional light particles). Novel features of our analysis are the insistence that the parameters satisfy the minimization condition of the potential and our inclusion of interference effects between the SM contributions to the Higgs widths and the contributions from the EFT interactions.

These interference effects can be large and significantly change the allowed regions of parameter space.

In Sec. II, we review the singlet model and the EFT interactions, along with compact expressions for the decay widths. Section III discusses constraints from the 125 GeV Higgs, and Sec. IV contains our limits on the properties of both the 125 scalar and EFT coefficients, and a discussion of the size of the allowed mixing between the SM-like and heavy scalars in the presence of EFT coefficients. Section V contains some conclusions.

## II. MODEL CONSIDERATIONS

## A. Singlet plus EFT Model

We consider a model containing the SM Higgs doublet, $H$, and an additional scalar singlet, $S$. The most general renormalizable scalar potential is

$$
\begin{align*}
V(H, S)= & -\mu^{2} H^{\dagger} H+\lambda\left(H^{\dagger} H\right)^{2}+\frac{a_{1}}{2} H^{\dagger} H S+\frac{a_{2}}{2} H^{\dagger} H S^{2} \\
& +b_{1} S+\frac{b_{2}}{2} S^{2}+\frac{b_{3}}{3} S^{3}+\frac{b_{4}}{4} S^{4} \tag{1}
\end{align*}
$$

The singlet model has been examined in some detail in the literature $[1,2,6-12]$ and so our discussion is appropriately brief. If there is a $Z_{2}$ symmetry $S \rightarrow-S$, then $a_{1}=b_{1}=b_{3}=0$. The $Z_{2}$ nonsymmetric model is, however, particularly interesting since it is possible to arrange the parameters in such a way as to obtain a strong first order phase transition [1-5,13].

The neutral scalar components of the doublet $H$ and singlet $S$ are denoted by $\phi_{0}=(h+v) / \sqrt{2}$ and $S=s+x$, where the vacuum expectation values are $\left\langle\phi_{0}\right\rangle=\frac{v}{\sqrt{2}}$ and $\langle S\rangle=x$. We require that the global minimum of the
potential correspond to the electroweak symmetry breaking (EWSB) minimum, $v=v_{\mathrm{EW}}=246 \mathrm{GeV}$ [1,9], which places significant constraints on the allowed parameters. Note that a shift of the singlet field by $S \rightarrow S+\Delta_{S}$ is just a redefinition of the parameters of Eq. (1), and we are free to choose our electroweak symmmetry breaking minimum as $(v, x) \equiv\left(v_{\text {EW }}, 0\right) .{ }^{1}$

The physical scalars are mixtures of $h$ and $s$, and the scalar mixing is parametrized as

$$
\binom{h_{1}}{h_{2}}=\left(\begin{array}{cc}
\cos \theta & \sin \theta  \tag{2}\\
-\sin \theta & \cos \theta
\end{array}\right)\binom{h}{s},
$$

where $h_{1,2}$ are the mass eigenstates with masses $m_{1}, m_{2}$. The parameters of the scalar potential can be solved for in terms of the physical masses and mixing,

$$
\begin{align*}
a_{1} & =\frac{m_{1}^{2}-m_{2}^{2}}{v} \sin 2 \theta, \\
b_{2}+\frac{a_{2}}{2} v^{2} & =m_{1}^{2} \sin ^{2} \theta+m_{2}^{2} \cos ^{2} \theta, \\
\lambda & =\frac{m_{1}^{2} \cos ^{2} \theta+m_{2}^{2} \sin ^{2} \theta}{2 v^{2}} \\
\mu^{2} & =\lambda v^{2} \\
b_{1} & =-\frac{v^{2}}{4} a_{1} \tag{3}
\end{align*}
$$

Our free parameters are then

$$
\begin{align*}
m_{1} & =125 \mathrm{GeV}, \quad m_{2}, \theta, v_{\mathrm{EW}}=246 \mathrm{GeV} \\
x & =0, a_{2}, b_{3}, b_{4} \tag{4}
\end{align*}
$$

The couplings of the $h_{1}$ to SM particles are suppressed by $\cos \theta$ and both ATLAS and CMS have obtained limits from the measured couplings. ATLAS finds at $95 \%$ confidence level, $\sin \theta \leq .35$, assuming no branching ratio to invisible particles [14]. Using the fitted global signal strength for the SM Higgs boson, $\mu=1.03_{-0.15}^{+0.17}$ [15], a $95 \%$ confidence level limit can be extracted, $\sin \theta \leq .51$. In the absence of the EFT coefficients, a fit to the oblique parameters also restricts $\sin \theta[2,8,9,16]$, but the limit from Higgs coupling measurements is stronger.

The limits on $\sin \theta$ can be significantly altered, however, when the EFT operators are included. We postulate the $S U(3) \times S U(2) \times U(1)$ gauge invariant effective interactions,

$$
\begin{equation*}
L=g_{s}^{2} \frac{c_{g g}}{\Lambda} S G^{\mu \nu, A} G_{\mu \nu}^{A}+\frac{c_{W W}}{\Lambda} g^{2} S W^{\mu \nu, a} W_{\mu \nu}^{a}+\frac{c_{B B}}{\Lambda} g^{2} S B^{\mu \nu} B_{\mu \nu} \tag{5}
\end{equation*}
$$

[^0]that are assumed to arise from unknown UV physics at a scale $\Lambda$. The scalar couplings to gauge bosons are suppressed by the appropriate factor of $\cos \theta$ or $\sin \theta$ and receive additional contributions from the interactions of Eq. (5). There is an interplay of effects between the singlet-SM mixing of Eq. (2) and the EFT contributions from Eq. (5), which requires that we fit the data to the complete model $[17,18]$.

Finally, we need the self-interactions of the Higgs bosons in the basis of the mass eigenstates $h_{1}$ and $h_{2}$,

$$
\begin{equation*}
V_{\text {self }} \supset \frac{\lambda_{111}}{3!} h_{1}^{3}+\frac{\lambda_{211}}{2!} h_{2} h_{1}^{2}+\cdots \tag{6}
\end{equation*}
$$

where $[8,9]$

$$
\begin{align*}
\lambda_{111}= & 2 s_{\theta}^{3} b_{3}+\frac{3 a_{1}}{2} s_{\theta} c_{\theta}^{2}+3 a_{2} s_{\theta}^{2} c_{\theta} v+6 c_{\theta}^{3} \lambda v, \\
\lambda_{211}= & 2 s_{\theta}^{2} c_{\theta} b_{3}+\frac{a_{1}}{2} c_{\theta}\left(c_{\theta}^{2}-2 s_{\theta}^{2}\right) \\
& +\left(2 c_{\theta}^{2}-s_{\theta}^{2}\right) s_{\theta} v a_{2}-6 \lambda s_{\theta} c_{\theta}^{2} v . \tag{7}
\end{align*}
$$

and we abbreviate $s_{\theta}=\sin \theta, c_{\theta}=\cos \theta$ and assume $\sin \theta>0$. In the small angle limit, to $\mathcal{O}\left(s_{\theta}^{2}\right)$,

$$
\begin{gather*}
\lambda_{111} \rightarrow 6 \lambda v+\frac{3}{2} a_{1} s_{\theta}+3 v s_{\theta}^{2}\left(a_{2}-3 \lambda\right) \\
\sim \frac{3 m_{1}^{2}}{v}+s_{\theta}^{2} \frac{3}{2 v}\left(m_{2}^{2}-4 m_{1}^{2}+2 a_{2} v^{2}\right)  \tag{8}\\
\lambda_{211} \rightarrow \frac{a_{1}}{2}+s_{\theta} v\left(-6 \lambda+2 a_{2}\right)+\frac{s_{\theta}^{2}}{4}\left(8 b_{3}-7 a_{1}\right) \\
\sim s_{\theta}\left(-\frac{3 m_{1}^{2}}{v}+2 v a_{2}\right)+\frac{s_{\theta} c_{\theta}}{2 v}\left(m_{1}^{2}-m_{2}^{2}\right)+2 b_{3} s_{\theta}^{2} . \tag{9}
\end{gather*}
$$

The restrictions on the parameters of the potential due to the requirement that the electroweak minimum be a global minimum were examined in Ref. [1,9]. In Fig. 1, we fix $b_{4}=1, \cos \theta=.94$ and show the allowed regions for $a_{2}$ and $b_{3}$ for different values of the heavy scalar mass, $m_{2}$. The areas of these regions increase with $b_{4}$, and the edges of the contours are completely fixed by the global minimum requirement as described in Ref. [9]. ${ }^{2}$ The regions become somewhat larger as $m_{2}$ increases for fixed $b_{4}$. In the softly broken $Z_{2}$ scenario of Ref. [5], a first order electroweak phase transition requires $a_{2}>\sim 9$. In the model without a $Z_{2}$ symmetry, a strong first order electroweak phase transition appears to be possible for $a_{2} \sim 1-2$, and negative $b_{3}$ [3],

[^1]



FIG. 1. Regions allowed by the requirement that the electroweak minimum be a global minimum for $\cos \theta=0.94, b_{4}=1$ and $m_{2}=400,600$, and 750 GeV [9].
although the maximum $m_{2}$ studied in this reference is 250 GeV .

The partial width of $h_{2} \rightarrow h_{1} h_{1}$ is

$$
\begin{equation*}
\Gamma\left(h_{2} \rightarrow h_{1} h_{1}\right)=\frac{\lambda_{211}^{2}}{32 \pi m_{2}} \sqrt{1-\frac{4 m_{1}^{2}}{m_{2}^{2}}} . \tag{10}
\end{equation*}
$$

In Fig. 2 we show the partial widths for $h_{2} \rightarrow h_{1} h_{1}$ using the allowed values of $b_{3}$ from Fig. 1 for each parameter point for representative values of the parameters. The width can potentially increase significantly as
the resonance mass increases. A measurement of the coupling $\lambda_{211}$ to sufficient precision could shed light on the values of $a_{2}$ and $b_{3}$. We note that in all cases, $\Gamma\left(h_{2} \rightarrow h_{1} h_{1}\right)_{\max } / m_{2} \sim 1 \%$, and so we are in a narrow width scenario.

## B. Results for decay widths

The decays of $h_{1}$ and $h_{2}$ are affected by the SM doubletsinglet mixing and by the EFT operators. Retaining the interference with the SM contributions, we find for the heavier state the following:

$$
\begin{align*}
\Gamma\left(h_{2} \rightarrow \gamma \gamma\right)= & \frac{e^{4} m_{2}^{3}}{4 \pi}\left|\sin \theta\left(\frac{\Sigma_{i} N_{c i} e_{i}^{2} F_{i}\left(\tau_{2 i}\right)}{32 \pi^{2} v}\right)+\cos \theta \frac{c_{\gamma \gamma}}{\Lambda}\right|^{2} \\
\Gamma\left(h_{2} \rightarrow g g\right)= & \frac{2 g_{s}^{4} m_{2}^{3}}{\pi}\left|\sin \theta \frac{\Sigma_{i} F_{i}\left(\tau_{2 i}\right)}{64 \pi^{2} v}+\cos \theta \frac{c_{g g}}{\Lambda}\right|^{2} \\
\Gamma\left(h_{2} \rightarrow Z Z\right)= & \frac{1}{32 \pi} \frac{m_{2}^{3}}{v^{2}} \sqrt{1-4 x_{2 Z}}\left\{2^{7} \cos ^{2} \theta \frac{c_{Z Z}^{2} M_{Z}^{4}}{\Lambda^{2} v^{2}}\left(1-4 x_{2 Z}+6 x_{2 Z}^{2}\right)\right. \\
& \left.+3 \cdot 2^{5} \cos \theta \sin \theta \frac{c_{Z Z} M_{Z}^{2}}{v \Lambda} x_{2 Z}\left(1-2 x_{2 Z}\right)+\sin ^{2} \theta\left(1-4 x_{2 Z}+12 x_{2 Z}^{2}\right)\right\} \\
\Gamma\left(h_{2} \rightarrow Z \gamma\right)= & \frac{e^{4} m_{2}^{3}}{2 \pi s_{W}^{2} c_{W}^{2}}\left(1-x_{2 Z}\right)^{3}\left|\sin \theta \frac{c_{W} s_{W}}{32 \pi^{2} v}\left(A_{F}+A_{W}\right)-\cos \theta \frac{c_{z \gamma}}{\Lambda}\right|^{2} \\
\Gamma\left(h_{2} \rightarrow W^{+} W^{-}\right)= & \frac{1}{16} \frac{m_{2}^{3}}{\pi v^{2}} \sqrt{1-4 x_{2 W}}\left\{2^{7} \cos ^{2} \theta \frac{c_{W W}^{2} M_{W}^{4}}{\Lambda^{2} v^{2}}\left(1-4 x_{2 W}+6 x_{2 W}^{2}\right)\right. \\
& \left.+3 \cdot 2^{5} \cos \theta \sin \theta \frac{c_{W W} M_{W}^{2}}{v \Lambda} x_{2 W}\left(1-2 x_{2 W}\right)+\sin ^{2} \theta\left(1-4 x_{2 W}+12 x_{2 W}^{2}\right)\right\} \\
\Gamma\left(h_{2} \rightarrow f \bar{f}\right)= & \sin ^{2} \theta \Gamma(h \rightarrow f \bar{f})_{\mathrm{SM}}, \tag{11}
\end{align*}
$$

where [19-21],



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FIG. 2. Allowed decay widths for $h_{2} \rightarrow h_{1} h_{1}$ assuming the parameters correspond to a global minimum of the potential for $b_{4}=1$, $\cos \theta=0.94$, and $m_{2}=400,600$ and 750 GeV .

$$
\begin{aligned}
F_{i}\left(\tau_{2 i}\right) & =-2 \tau_{2 i}\left(1+\left(1-\tau_{2 i}\right) f\left(\tau_{2 i}\right)\right) \text { for fermions } \\
F_{W}\left(\tau_{2 W}\right) & =2+3 \tau_{2 W}+3 \tau_{2 W}\left(2-\tau_{2 W}\right) f\left(\tau_{2 W}\right)
\end{aligned}
$$

for gauge bosons

$$
\begin{align*}
x_{i V} & =\frac{M_{V}^{2}}{m_{i}^{2}} \\
c_{\gamma \gamma} & =c_{W W}+c_{B B} \\
c_{Z Z} & =c_{W}^{4} c_{W W}+s_{W}^{4} c_{B B} \\
c_{Z \gamma} & =c_{B B} s_{W}^{2}-c_{W W} c_{W}^{2}, \tag{12}
\end{align*}
$$

and $e_{i}$ is the electric charge of particle $i, c_{W}=M_{W} / M_{Z}$, $N_{c i}=3(1)$ for quarks (leptons), $\tau_{2 i}=\frac{4 M_{i}^{2}}{m_{2}^{2}}, M_{i}$ is the mass of the appropriate fermion or the $W$ boson, $A_{F}$ and $A_{W}$ are given in Ref. [19], and

$$
\begin{align*}
f(\tau) & =\left[\sin ^{-1}\left(\frac{1}{\sqrt{\tau}}\right)\right]^{2}, \quad \text { if } \tau \geq 1 \\
& =-\frac{1}{4}\left[\ln \left(\frac{1+\sqrt{1-\tau}}{1-\sqrt{1-\tau}}\right)-i \pi\right]^{2} \quad \text { if } \tau<1 \tag{13}
\end{align*}
$$

If we consider a model with no mixing with the SM Higgs, $\sin \theta=0$, we have approximately

$$
\begin{align*}
\Gamma\left(h_{2} \rightarrow \gamma \gamma\right)= & .04 c_{\gamma \gamma}^{2}\left(\frac{m_{2}}{600 \mathrm{GeV}}\right)^{3}\left(\frac{2 \mathrm{TeV}}{\Lambda(\mathrm{TeV})}\right)^{2} \mathrm{GeV} \\
\Gamma\left(h_{2} \rightarrow W^{+} W^{-}\right)= & 0.15 c_{W W}^{2}\left(\frac{m_{2}}{600 \mathrm{GeV}}\right)^{3} \\
& \times\left(\frac{2 \mathrm{TeV}}{\Lambda(\mathrm{TeV})}\right)^{2} \mathrm{GeV} \\
\Gamma\left(h_{2} \rightarrow Z Z\right)= & 1.2 c_{Z Z}^{2}\left(\frac{m_{2}}{600 \mathrm{GeV}}\right)^{3}\left(\frac{2 \mathrm{TeV}}{\Lambda(\mathrm{TeV})}\right)^{2} \mathrm{GeV} \\
\Gamma\left(h_{2} \rightarrow Z \gamma\right)= & 0.43 c_{Z \gamma}^{2}\left(\frac{m_{2}}{600 \mathrm{GeV}}\right)^{3} \\
& \times\left(\frac{2 \mathrm{TeV}}{\Lambda(\mathrm{TeV})}\right)^{2} \mathrm{GeV} \tag{14}
\end{align*}
$$

Note that Eq. (14) is an overconstrained result due to the relations of Eq. (12).

The lighter Higgs boson ( $m_{1}=125 \mathrm{GeV}$ ) decay widths are

$$
\begin{align*}
& \Gamma\left(h_{1} \rightarrow g g\right)=\frac{2 g_{s}^{4} m_{1}^{3}}{\pi}\left|-\cos \theta \frac{\Sigma_{i} F_{i}\left(\tau_{1 i}\right)}{64 \pi^{2} v}+\sin \theta \frac{c_{g g}}{\Lambda}\right|^{2} \\
& \Gamma\left(h_{1} \rightarrow \gamma \gamma\right)=\frac{e^{4} m_{1}^{3}}{4 \pi}\left|-\cos \theta\left(\frac{\Sigma_{i} N_{c i} e_{i}^{2} F_{i}\left(\tau_{1 i}\right)}{32 \pi^{2} v}\right)+\sin \theta \frac{c_{\gamma \gamma}}{\Lambda}\right|^{2} \\
& \Gamma\left(h_{1} \rightarrow W W^{*}\right)=\frac{18 g^{2} M_{W}^{4}}{\pi^{3} v^{2} m_{1}}\left\{\sin ^{2} \theta \frac{c_{W W}^{2}}{v^{2} \Lambda^{2}} m_{1}^{4} I_{3}\left(M_{W}\right)-\cos \theta \sin \theta \frac{c_{W W}}{4 v \Lambda} m_{1}^{2} I_{2}\left(M_{W}\right)+\frac{1}{64} \cos ^{2} \theta I_{1}\left(M_{W}\right)\right\} \\
& \Gamma\left(h_{1} \rightarrow Z Z^{*}\right)=\kappa \frac{2 g^{2} M_{Z}^{4}}{c_{W}^{2} \pi^{3} v^{2} m_{1}}\left\{\sin ^{2} \theta \frac{c_{Z Z}^{2}}{v^{2} \Lambda^{2}} m_{1}^{4} I_{3}\left(M_{Z}\right)-\cos \theta \sin \theta \frac{c_{Z Z}}{4 v \Lambda} m_{1}^{2} I_{2}\left(M_{Z}\right)+\frac{1}{64} \cos ^{2} \theta I_{1}\left(M_{Z}\right)\right\} \\
& \Gamma\left(h_{1} \rightarrow Z \gamma\right)=\frac{e^{4} m_{1}^{3}}{2 \pi s_{W}^{2} c_{W}^{2}}\left(1-x_{1 Z}\right)^{3}\left|\cos \theta \frac{c_{W} s_{W}}{32 \pi^{2} v}\left(A_{F}+A_{W}\right)+\sin \theta \frac{c_{z \gamma}}{\Lambda}\right|^{2} \\
& \Gamma\left(h_{1} \rightarrow f \bar{f}\right)=\cos ^{2} \theta \Gamma(h \rightarrow f \bar{f})_{\mathrm{SM}} \tag{15}
\end{align*}
$$

where,



FIG. 3. Branching ratio for (left-hand side) $h_{1} \rightarrow W W$, and (right-hand side) $h_{1} \rightarrow Z Z$ for representative values of the parameters.

$$
\begin{align*}
& I_{1}\left(M_{W}\right)=\int_{0}^{\left(m_{1}-M_{W}\right)^{2}} d q^{2} \frac{q^{2}}{m_{1}^{2}}\left(1+\frac{1}{3} \frac{\hat{\lambda}\left(m_{1}^{2}, M_{W}^{2}, q^{2}\right)}{4 q^{2} M_{W}^{2}}\right) \frac{\hat{\lambda}^{1 / 2}\left(m_{1}^{2}, M_{W}^{2}, q^{2}\right)}{\left(q^{2}-M_{W}^{2}\right)^{2}+\Gamma_{W}^{2} M_{W}^{2}} \\
& I_{2}\left(M_{W}\right)=\int_{0}^{\left(m_{1}-M_{W}\right)^{2}} d q^{2} \frac{q^{2}}{m_{1}^{2}} \frac{M_{1}^{2}-M_{W}^{2}-q^{2}}{2 m_{1}^{2}} \frac{\hat{\lambda}^{1 / 2}\left(m_{1}^{2}, M_{W}^{2}, q^{2}\right)}{\left(q^{2}-M_{W}^{2}\right)^{2}+\Gamma_{W}^{2} M_{W}^{2}} \\
& I_{3}\left(M_{W}\right)=\int_{0}^{\left(m_{1}-M_{W}\right)^{2}} d q^{2} \frac{q^{2}}{m_{1}^{2}} \frac{3\left(m_{1}^{2}-M_{W}^{2}-q^{2}\right)^{2}-\hat{\lambda}\left(m_{1}^{2}, M_{W}^{2}, q^{2}\right)}{12 m_{1}^{4}} \frac{\hat{\lambda}^{1 / 2}\left(m_{1}^{2}, M_{W}^{2}, q^{2}\right)}{\left(q^{2}-M_{W}^{2}\right)^{2}+\Gamma_{W}^{2} M_{W}^{2}} \\
& \hat{\lambda}(x, y, z)=(x-y-z)^{2}-4 y z \tag{16}
\end{align*}
$$

$\tau_{1 i}=\frac{4 M_{i}^{2}}{m_{1}^{2}}$, the coefficient $\kappa$ is,

$$
\begin{align*}
\kappa & =3\left(\left(\frac{1}{2}-s_{W}^{2}\right)^{2}+s_{W}^{4}\right)+3 N_{c}\left(\left(-\frac{1}{2}+\frac{1}{3} s_{W}^{2}\right)^{2}+\frac{1}{9} s_{W}^{4}\right) \\
& +2 N_{c}\left(\left(\frac{1}{2}-\frac{2}{3} s_{W}^{2}\right)^{2}+\frac{4}{9} s_{W}^{4}\right) \\
= & 3.68 \tag{17}
\end{align*}
$$

with $N_{c}=3$ and $s_{W}^{2}=\sin ^{2} \theta_{W}=1-\frac{M_{W}^{2}}{M_{Z}^{2}}$.

Some typical branching ratios of $h_{1}$ into $W W$ and $Z Z$ normalized to the SM are shown in Fig. 3, and demonstrate little sensitivity to either $c_{B B}$ or $c_{W W}$ with subpercent level deviations. The branching ratios to $\gamma \gamma$ and $Z \gamma$ are shown in Fig. 4 and are very sensitive to $c_{W W}$ and $c_{B B}$, changing upwards of $50 \%$ from the SM values. This is due to the SM rate first occuring at one loop. We note that in the limit $c_{g g}=c_{W W}=c_{B B}=0$, all of the branching ratios are equal to their SM values for $\sin \theta=0$, and the deviations from 1 in Figs. 3 and 4 are a result of the interplay between the singlet mixing and the EFT operators. These figures retain only the linear terms in the EFT couplings, as we have


FIG. 4. Branching ratios for (left-hand side) $h_{1} \rightarrow \gamma \gamma$, and (right-hand side) $h_{1} \rightarrow Z \gamma$ for representative values of the parameters.
implicitly assumed $s_{\theta}$ is small and we note that the $c_{i}^{2}$ coefficients are always suppressed by $s_{\theta}^{2}$ for $h_{1}$ production [see Eq. (15)].

For completeness, we note that the hadronic cross section for production of $h_{1}$ or $h_{2}$ from gluon fusion is

$$
\begin{equation*}
\sigma\left(p p \rightarrow h_{i}\right)=\frac{\pi^{2}}{8 m_{i} S_{H}} \Gamma\left(h_{i} \rightarrow g g\right) L \tag{18}
\end{equation*}
$$

where

$$
\begin{equation*}
L=\int_{\ln (\sqrt{\zeta})}^{-\ln (\sqrt{\zeta})} d y g\left(\sqrt{\zeta} e^{y}\right) g\left(\sqrt{\zeta} e^{-y}\right) \tag{19}
\end{equation*}
$$

$\sqrt{S_{H}}$ is the hadronic center-of-mass energy and $\zeta=m_{i}^{2} / S_{H}$.

## III. CONSTRAINTS FROM $\boldsymbol{h}_{\mathbf{1}}$

The measurements of SM Higgs couplings place stringent restrictions on the allowed parameters of the model. Both ATLAS and CMS limit the mixing angle, $\theta$, in the singlet model in the case $c_{g g}=c_{W W}=c_{B B}=0$, as discussed in the previous section. These limits are significantly affected by the addition of the EFT operators. We fit to the parameters of our model using the combined ATLAS/CMS 8 TeV results [15]. The simplest possible limit is obtained by a fit to the overall gluon fusion signal strength for $h_{1}$,

$$
\begin{equation*}
\mu_{g g F}=1.03_{-.15}^{+.17} \tag{20}
\end{equation*}
$$

The $95 \%$ confidence level limit from the $g g F$ signal strength is shown in Fig. 5. This fit demonstrates the cancellations between the contributions of the singlet model and the contributions of the EFT coefficients. For $s_{\theta}=0$, the EFT operators do not contribute to $h_{1}$ decay, and so there is no limit on $c_{g g}$ (the lower band extending across all $c_{g g}$ values). For $s_{\theta}=1$, the SM contributions vanish, and the observed $h_{1}$ production rate is obtained by adjusting $c_{g g}$ (we have only plotted allowed values). For small $c_{g g}$, we observe the interplay of the mixing and EFT contributions, and larger values of $s_{\theta}$ are allowed than in the $c_{g g}=0$ limit. In this plot, we retain only the linear contributions in $c_{g g}$. If the $c_{g g}^{2}$ terms become numerically relevant, then the dimension-6 terms must be included in the EFT of Eq. (5).

In Fig. 5, we also fit the $h_{1}$ coupling strengths [15] using the 6 parameter fit to the $g g$ initial state at 8 TeV ,

$$
\begin{align*}
\mu_{F}^{\gamma \gamma} & =1.13_{-.21}^{+.24} & \mu_{F}^{W W}=1.08_{-.19}^{.22} \\
\mu_{F}^{Z Z} & =1.29_{-.25}^{.29} & \mu_{F}^{b b}=.66_{-.28}^{+.37} \\
\mu_{F}^{\tau \tau} & =1.07_{-.28}^{+.35} . & \tag{21}
\end{align*}
$$



FIG. 5. 95\% confidence level allowed regions using the gluon fusion signal strength for $h_{1}$ production (red) and allowed regions derived from fits to the signal strengths given in Eq. (21) (black) [15] with $\Lambda=2 \mathrm{TeV}$. Only the linear terms in the EFT expansion are included.

These are labeled as "h1 95\% C.L. fits." The results of the two fits are quite similar.

## IV. CONSTRAINTS FROM $\boldsymbol{h}_{\mathbf{2}}$

We turn now to a joint examination of the measured properties of the $h_{1}$ as given in Eq. (21) and the experimental limits on heavy resonances shown in Tables I and II for heavy scalars with masses of $m_{2}=400,600$ and 750 GeV decaying to SM particles using the results of Eq. (11). We calculate the signal rates at leading order in QCD and normalize to the recommended values for the SM production rates from the LHC Higgs Cross Section Working Group [22] given in Table III.

Figure 6 shows the regions excluded from the restrictions from resonance searches at 8 TeV and 13 TeV . For $\sin \theta=0$, there is now an upper limit to $c_{g g}$ that arises from the dijet searches. The region at $\sin \theta=1$, present in the $h_{1}$ fits, largely vanishes at $m_{2}=600$ and 750 GeV , and is greatly reduced at $m_{2}=400 \mathrm{GeV}$. The excluded region

TABLE I. $95 \%$ C.L. LHC limits on $\sigma \cdot B R$ for heavy resonances at $\sqrt{S_{H}}=8 \mathrm{TeV}$. Asterisks indicate that there are no current bounds in these channels.

| Channel | $m_{2}=400 \mathrm{GeV}$ | $m_{2}=600 \mathrm{GeV}$ | $m_{2}=750 \mathrm{GeV}$ |
| :--- | :--- | :--- | :--- |
| $W W$ | $0.362 \mathrm{pb}[23]$ | $0.118 \mathrm{pb}[23]$ | $0.0361 \mathrm{pb}[23]$ |
| $Z Z$ | $0.0648 \mathrm{pb}[24]$ | $0.0218 \mathrm{pb}[24]$ | $0.0118 \mathrm{pb}[24]$ |
| $t \bar{t}$ | $\quad *$ | $1.2 \mathrm{pb}[25]$ | $0.71 \mathrm{pb}[25]$ |
| $Z \gamma$ | $0.00720 \mathrm{pb}[26]$ | $0.00296 \mathrm{pb}[26]$ | $0.00402 \mathrm{pb}[26]$ |
| $\tau^{+} \tau^{-}$ | $0.087 \mathrm{pb}[27]$ | $0.020 \mathrm{pb}[27]$ | $0.012 \mathrm{pb}[27]$ |
| $j j$ | $\quad *$ | $3.76 \mathrm{pb}[28]$ | $1.79 \mathrm{pb}[28]$ |
| $h_{1} h_{1}$ | $0.442 \mathrm{pb}[29]$ | $0.137 \mathrm{pb}[29]$ | $0.0498 \mathrm{pb}[29]$ |
| $\gamma \gamma$ | $0.00215 \mathrm{pb}[30]$ | $0.000666 \mathrm{pb}[31]$ | $0.00129 \mathrm{pb} \mathrm{[30]}$ |

TABLE II. 95\% C.L. LHC limits on $\sigma \cdot B R$ for heavy resonances at $\sqrt{S_{H}}=13 \mathrm{TeV}$. Asterisks indicate that there are no current bounds in these channels.

| Channel | $m_{2}=400 \mathrm{GeV}$ | $m_{2}=600 \mathrm{GeV}$ | $m_{2}=750 \mathrm{GeV}$ |
| :--- | :--- | :---: | :--- |
| $W W$ | $1.4 \mathrm{pb}[32]$ | $0.5 \mathrm{pb}[32]$ | $0.31 \mathrm{pb}[32]$ |
| $Z Z$ | $0.210 \mathrm{pb}[33]$ | $0.083 \mathrm{pb}[34]$ | $0.043 \mathrm{pb}[34]$ |
| $Z \gamma$ | $0.041 \mathrm{pb}[35]$ | $.013 \mathrm{pb}[35]$ | $0.010 \mathrm{pb}[35]$ |
| $\tau^{+} \tau^{-}$ | $0.27 \mathrm{pb}[36]$ | $0.053 \mathrm{pb} \mathrm{[36]}$ | $0.030 \mathrm{pb} \mathrm{[36]}$ |
| $j j$ | $\quad *$ | $21.4 \mathrm{pb} \mathrm{[37]}$ | $9.54 \mathrm{pb}[37]$ |
| $h_{1} h_{1}$ | $5.9 \mathrm{pb}[38]$ | $1.6 \mathrm{pb}[38]$ | $0.85 \mathrm{pb}[38]$ |
| $\gamma \gamma$ | $0.0018 \mathrm{pb}[39]$ | $0.0015 \mathrm{pb}[39]$ | $0.00068 \mathrm{pb}[39]$ |
| $b \bar{b}$ | $\quad *$ | $5.1 \mathrm{pb} \mathrm{[40]}$ | $5.2 \mathrm{pb}[40]$ |

TABLE III. Theoretical cross sections at NNLO + NNLL for heavy scalar resonances from the LHC Higgs Cross Section Working Group [22].

|  | $8 \mathrm{TeV}, \sigma\left(p p \rightarrow h_{2}\right)$ | $13 \mathrm{TeV}, \sigma\left(p p \rightarrow h_{2}\right)$ |
| :--- | :---: | :---: |
| $m_{2}=400 \mathrm{GeV}$ | 3.01 pb | 9.52 pb |
| $m_{2}=600 \mathrm{GeV}$ | 0.52 pb | 2.01 pb |
| $m_{2}=750 \mathrm{GeV}$ | 0.15 pb | 0.64 pb |

shows little sensitivity to the parameter of the scalar potential. The counting of small parameters is different for the $h_{2}$ decays than in the $h_{1}$ case. If we treat both $s_{\theta}$ and $c_{i}$ as small parameters, then the $c_{i}^{2}$ contributions to $h_{2}$ decays are of the same order as the terms independent of the $c_{i}$. Hence for the $h_{2}$ decays, we include the $c_{i}^{2}$ contributions.

In Fig. 7, we plot the regions allowed by both $h_{1}$ coupling fits and resonance searches. We see that the large $c_{g g}$ regions that are allowed by the coupling constant fits are eliminated by the resonance search limits for $m_{2}=600 \mathrm{GeV}$ and 750 GeV . Considering all constraints, for $m_{2}=600$ and 750 GeV we find $|\sin \theta| \lesssim 0.6$. For $m_{2}=400 \mathrm{GeV}$, the resonance searches are less restrictive for positive $\sin \theta$ and the limit is $\sin \theta \gtrsim-0.4$. For all masses these limits are much weaker than $|\sin \theta| \leq 0.35$ [14] in the renormalizable model without the EFT operators in Eq. (5).

Finally, requiring a narrow width $\Gamma\left(h_{2}\right) / m_{2}<5 \%$, where $\Gamma\left(h_{2}\right)$ is the total $h_{2}$ width, further constrains the allowed regions of $\sin \theta$. For $m_{2}=600$ and 750 GeV the limit is $|\sin \theta| \lesssim 0.4$. For $m_{2}=400 \mathrm{GeV}$, the effect of the narrow width restriction is to eliminate the large $\sin \theta \sim 1$ region. The remaining parameter region is $-0.4 \lesssim \sin \theta \lesssim 0.7$.


FIG. 6. $95 \%$ confidence level allowed regions obtained by varying $c_{g g}, c_{W W}, c_{B B}, \cos \theta$, along with $b_{1}, b_{3}$ and $a_{2}$, allowed by the 8 TeV and 13 TeV resonance searches of Tables I and II.


FIG. 7. Allowed regions combining $h_{1}$ and $h_{2}$ data and a narrow width $\Gamma\left(h_{2}\right) / m_{2}<0.05$ restriction. The new physics scale is set $\Lambda=2 \mathrm{TeV}$, and $c_{W W}, c_{B B}$ are scanned over.

## V. CONCLUSIONS

We examined the effects on Higgs physics of a gauge singlet scalar which mixes with the SM-like 125 GeV Higgs boson when the theory is augmented by EFT operators coupling the singlet scalar to SM gauge bosons. The new feature of our analysis is a study of the properties of both the 125 GeV and heavy scalar resonance, and the demonstration that significant cancellations are possible between effects in the two sectors. We fit our model parameters to the 7 and 8 TeV combined ATLAS and CMS precision Higgs measurements [15] and applied constraints from scalar resonance searches at the 8 and 13 TeV LHC.

We find that the inclusion of the operators greatly changes the allowed values of the scalar mixing angle. In the renormalizable model, the strongest bound from Higgs precision is $|\sin \theta| \leq 0.35$ [14]. Including the EFT
operators between the singlet scalar and SM gauge bosons, we find Higgs precision measurements and scalar resonance searches give $\sin \theta \gtrsim-0.4$ for a heavy scalar mass of 400 GeV and $|\sin \theta| \lesssim 0.6$ for masses of 600 and 750 GeV . If the additional requirement of a narrow width $\Gamma\left(h_{2}\right) / m_{2}<0.05$ is included, the limits are $-0.4 \lesssim \sin \theta \lesssim$ 0.7 for a heavy scalar mass of 400 GeV and $|\sin \theta| \lesssim 0.4$ for masses of 600 and 750 GeV . In all cases, these restrictions are less than those in the renormalizable theory.

Digital data related to our results can be found at [41].

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[^0]:    ${ }^{1}$ This freedom to set $x=0$ does not occur in the $Z_{2}$ symmetric case.

[^1]:    ${ }^{2}$ For example, all points within the shaded regions are allowed by the minimization of the potential.

