

# Imaging the topside ionosphere and plasmasphere using Swarm GPS observations

## RECONSTRUCTION METHOD

### Observables

Only **phase measurements** were considered and the data was **screened for cycle slips**. We are using the geometry free linear combination of the two phase observables  $L_1$  and  $L_2$ ,

$$L_{gf} = L_1 - L_2 \approx \left( \frac{1}{f_1^2} - \frac{1}{f_2^2} \right) \cdot 40.3 \int_{LEO}^{GPS} N_e dl + C_{ARC} \quad [1]$$

The **linear combination**  $L_{gf}$  is in first order proportional to

the integrated **electron density**  $N_e$  along the line of sight from the LEO-receiver to the GPS-satellite

plus an **unknown offset**, which contains the ambiguities and unknown biases. This offset is assumed to be constant as long as there is no loss of lock.

### Reconstruction Technique

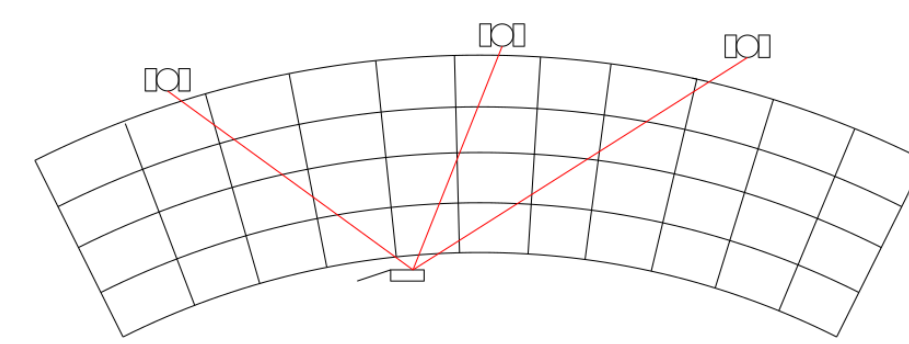
The reconstruction relies on **discretization**. We divide the two-dimensional plane into  $N$  grid cells.

$$L_{gf} \approx \left( \frac{1}{f_1^2} - \frac{1}{f_2^2} \right) \cdot 40.3 \sum_{i=0}^N l_i(N_e)_i + C_{ARC} \quad [2]$$

After computing the length of the **line of sight**  $L_i$  in each cell, we can approximate integral [1].

In each cell we assume the plasma density  $(N_e)_i$  to be constant.

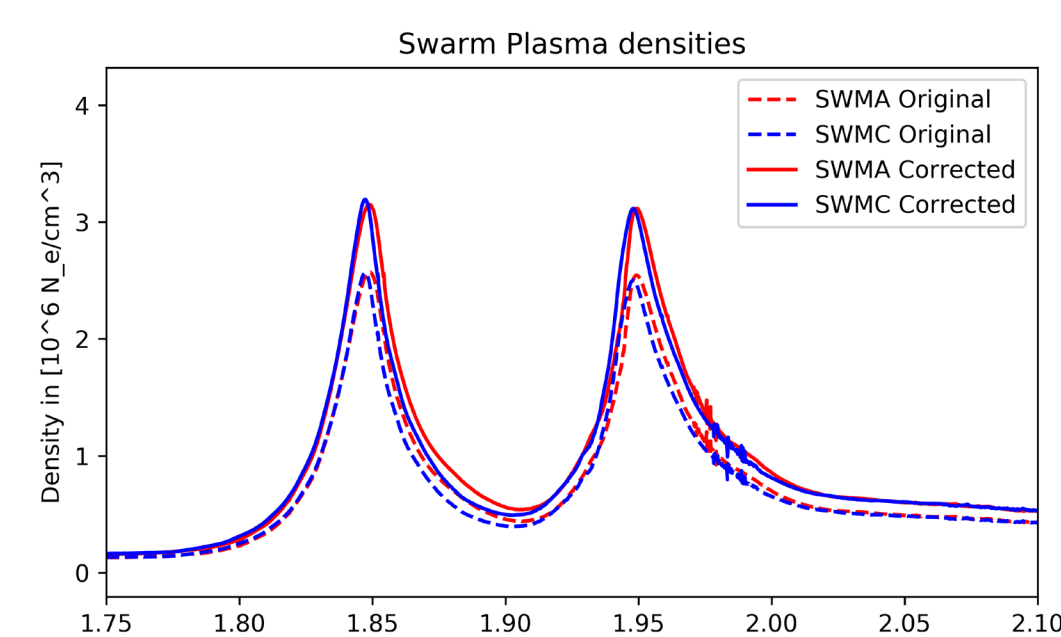
- We selected the settings:
- 0.5° resolution in latitude
  - 180 boxes in altitude from LEO altitude to GPS altitude
  - altitudinal bins exponentially increasing (20km - 700km)
  - rays were mapped in the 2D-plane, length were computed 3D
  - offsets estimated in least square solution



### Lower boundary condition

We use relative measurements, which makes it necessary to specify **reference values**. Swarm satellites are equipped with **Langmuir probes**, which allow an in-situ measurement of the ambient plasma density.

We calibrated the Langmuir probe measurements using values given by Lomidze et. al (2018) and assigned the **average value** in each latitudinal bin to lower boundary.



### Regularisation

The ray geometry is very weak. In order to obtain **stable solutions**, regularization is important.

We use a **Tikhonov regularization**:

$$\|Ax - y\| + \lambda \|Bx\| \rightarrow \min. \quad [3]$$

least square solution following (2)

regularization term

$$(Bx)_i = \sum_j^N ((N_e)_i - (N_e)_j) \cdot l_{ij}, \quad [4]$$

$l_{ij}$  is the length of the edge between boxes  $i$  and  $j$ .

The regularization matrix  $B$  is defined: the regularization term **vanishes**, if the **value** in one box **matches weighted average** of the surrounding ones:

The physical interpretation implies, that the **inflow should match the outflow** and that the solution should be **locally divergence free**. This can be justified by the conductivity along the magnetic field lines.

## IN A NUTSHELL

### GPS for Ionosphere:

The benefit of dual frequency GPS to gather ionospheric information is well understood and used for TEC Maps or ROTI products. There exist applications on ionospheric tomography too<sup>1</sup>. The major difficulty is that it is an **ill posed inverse problem** due to ray geometry. To overcome these difficulties most of the present models heavily constrain to background models, use long time averaging or big arrays of ground receivers - Minkwitz et al. (2015), Norberg et al. (2015).

### Problematic Swarm Data:

Commonly the Swarm GPS receivers had **schematic errors** in the data **during high ionospheric activity**. This is clearly visible in the gravity field solutions, even though for the precise orbit determination the ionosphere-free linear combination was used<sup>2</sup>.

**Weighting and screening strategies** were developed by TU Graz and AIUB to remove those errors. Since Mai 2015 Swarm tracking loops were updated, which again improved the data quality.

### Our Approach

It relies on a **single spaceborne GPS receiver** onboard a Swarm Satellite, uses only **20 min. of GPS carrier phase observations**, and is **independent of model assumptions** (like IRI, PIM or IGRF Models). It produces a **two dimensional slice** showing the Plasma density distribution in latitude and altitude. We investigate the stability of the reconstruction by applying different weighting strategies and perform validation by comparing the results from Swarm A to nearby satellite Swarm C.

## SWARM SPECIFIC ISSUES

### Weighting

To **overcome possible data problems**, different weightings have been developed for precise orbit determination and subsequent gravity field recovery. We use these weightings to derive a covariance matrix  $P$  which we apply on [3] s.t.

$$\|P(Ax - y)\| + \lambda \|Bx\| \rightarrow \min. \quad [5]$$

### ROTI (Rate of TEC index)

ROTI is defined via the **quadratic variance of the slant TEC** and computed from the RINEX observation file:

$$ROTI = \sqrt{\frac{\langle \Delta TEC^2 \rangle - \langle \Delta TEC \rangle^2}{\Delta t^2}} \quad [6]$$

As in Zehentner et al. (2015) ROTI was applied in a 31s sliding window manner and scaled.

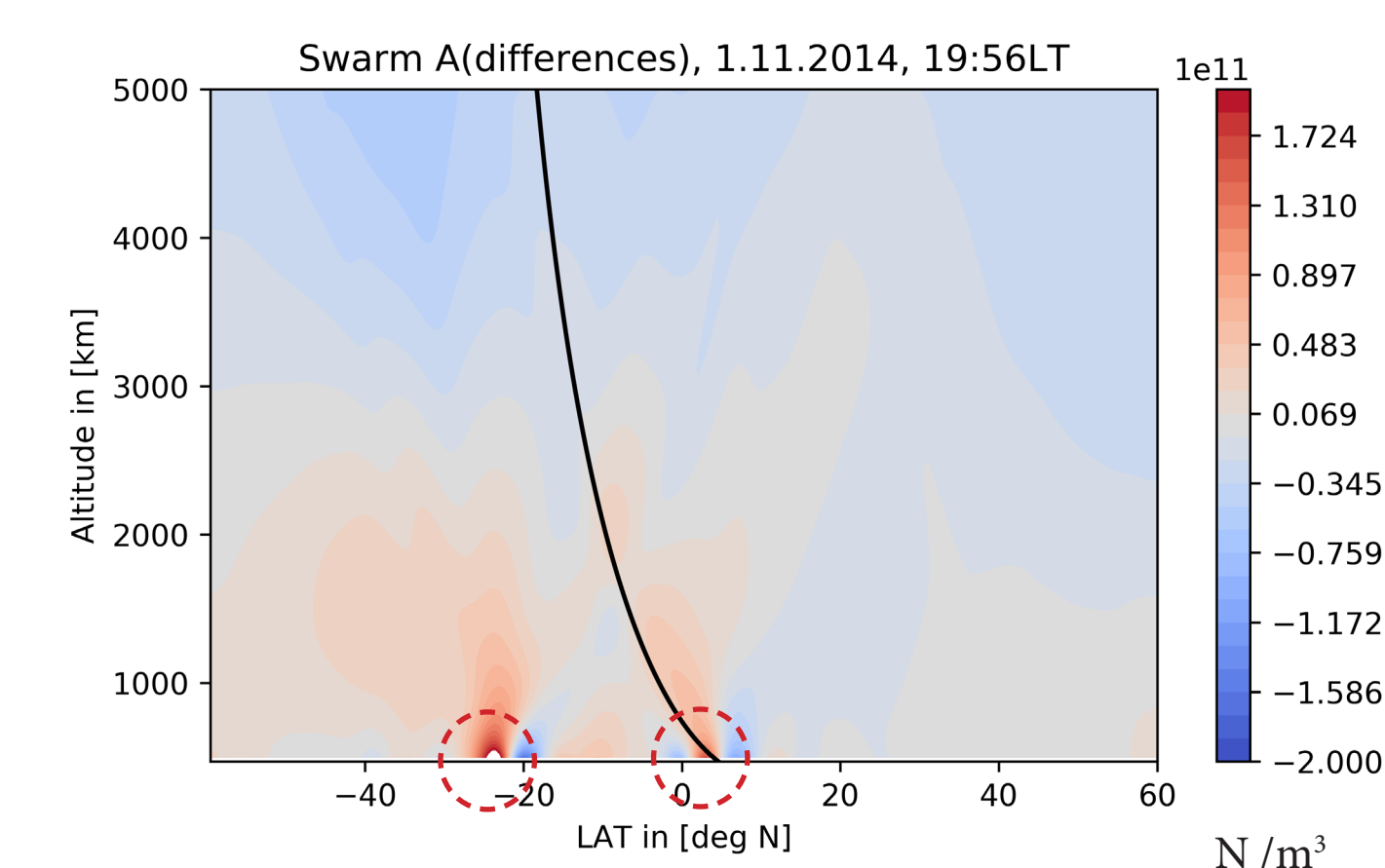
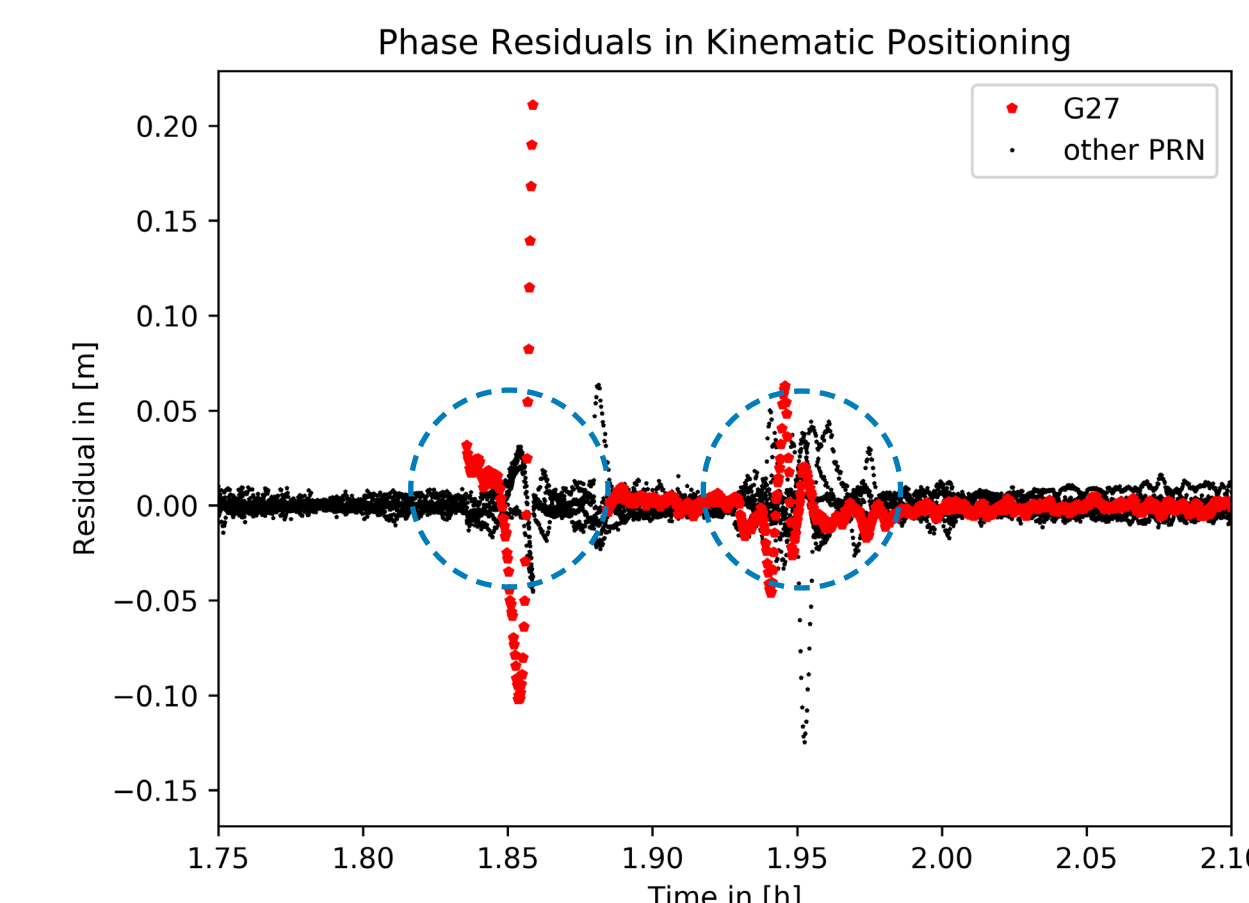
- TU-Graz:  $\sigma = \exp(20 \cdot ROTI)$
- AIUB:  $\sigma = \max(1, 60 \cdot ROTI)$

### Derivative based

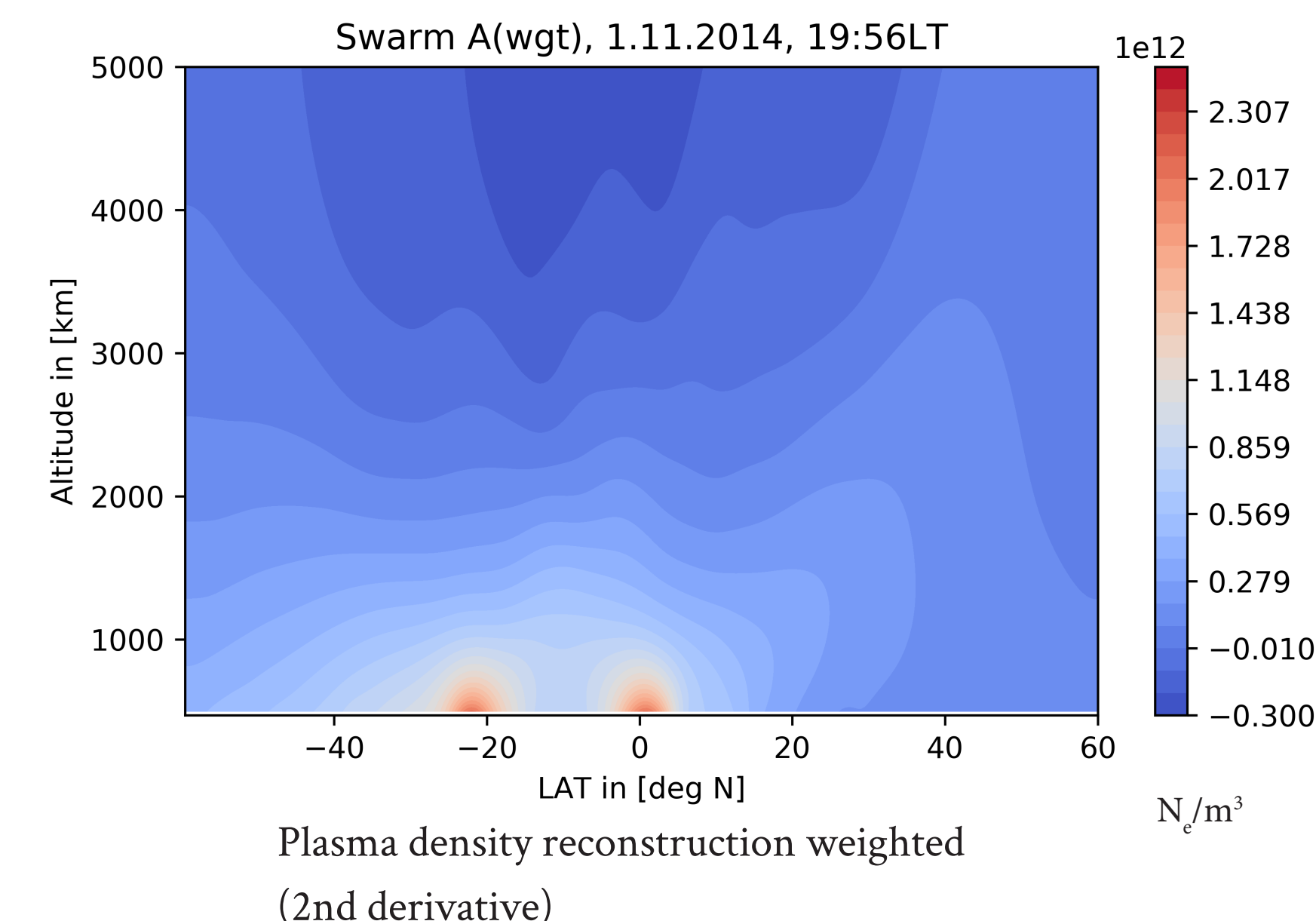
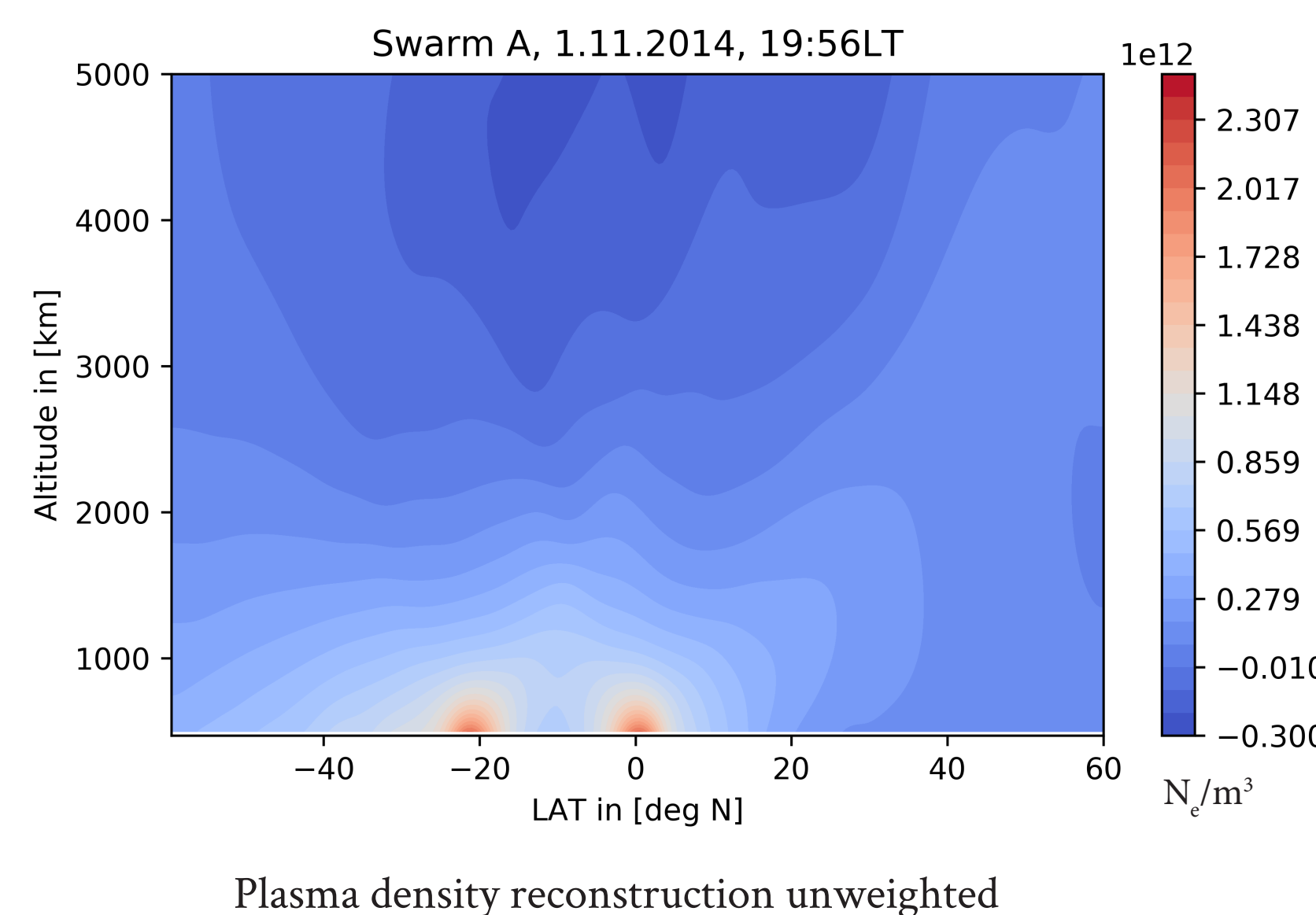
Values with a high second numerical derivative ( $> 0.025 \text{ cm/s}^2$ ) get a  $\sigma$  of 21, other observations stay unaffected ( $\sigma = 1$ ). This proved efficient in reducing equatorial artefacts in gravity field recovery<sup>3</sup>.

### Combined

For gravity field determination a combined approach ( $\sigma = \max(\sigma_{ROTI}, \sigma_{deriv})$ ) turned out to be the **most efficient**

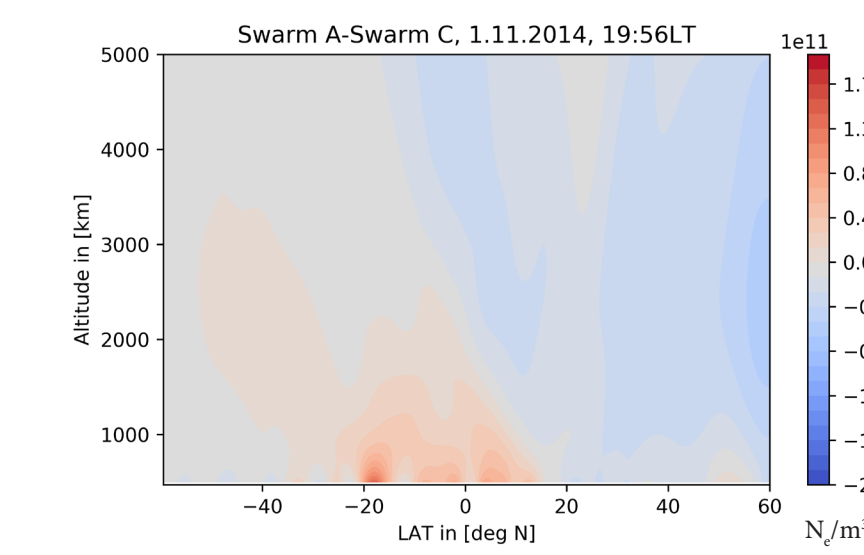


Data problems around the geomagnetic equator affect the reconstruction (black: line-of-sight Swarm A-G27)



## Validation

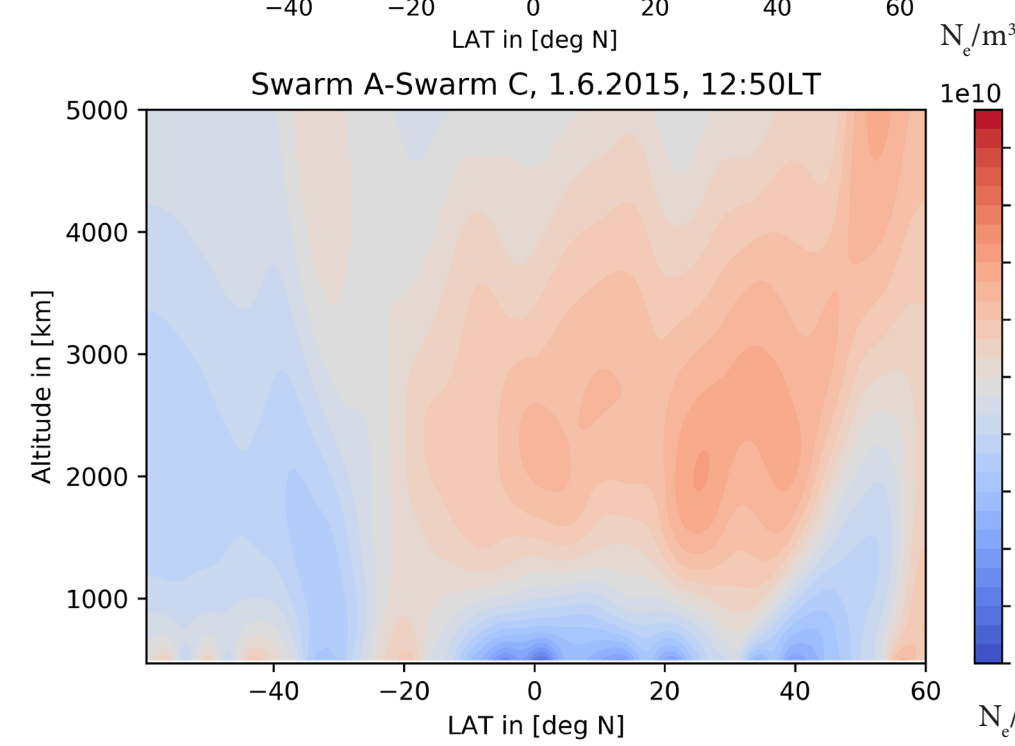
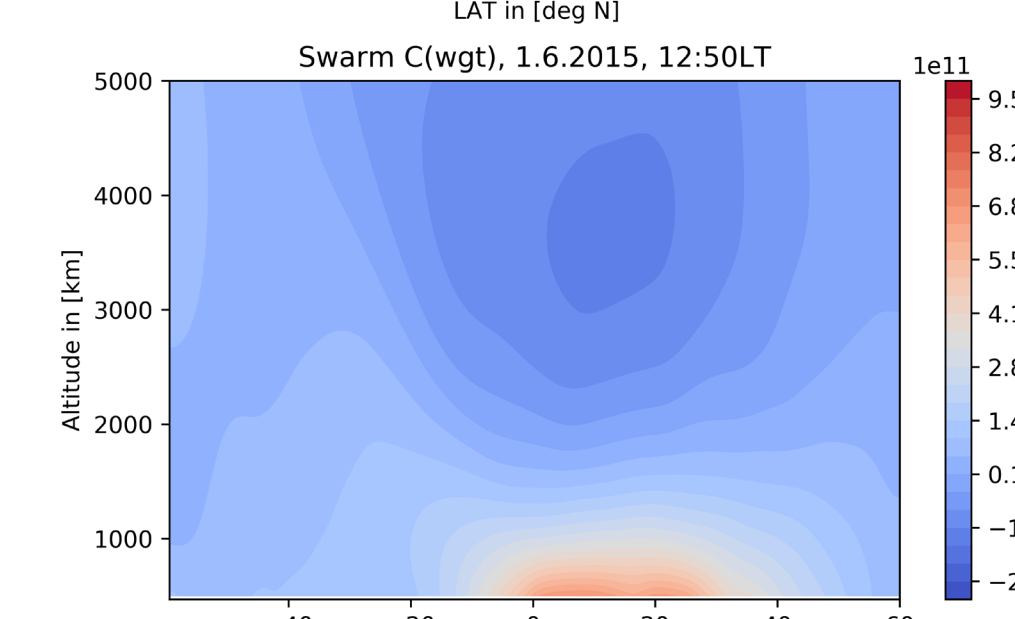
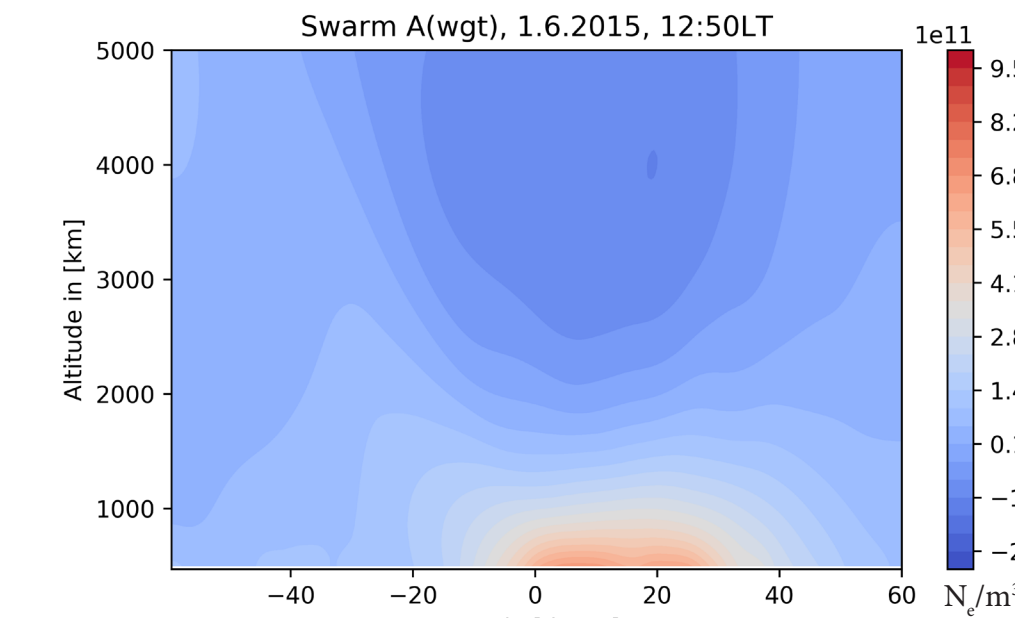
The Swarm mission offers an **unique option** to validate the reconstruction. Swarm A and C are **separated by only 6° in longitude** at equatorial regions. If the reconstruction algorithm is stable, results from A and C should be similar.



## Tracking Loop

For June the Tracking Loop settings of Swarm A and C had been **updated**. It allows to crosscheck the **impact** of the tracking loop update **on the reconstruction**.

The differences (as illustrated in the third image) are very small.



## CONCLUSIONS

- **Two dimensional reconstruction** is possible in short arcs with constraints
- Results are **sensitive to problematic GPS data** known from gravity field recovery
- problematic GPS data may be handled with **Covariance Matrix**
- **Swarm A and C show a good agreement** (Before/after tracking loop update)
- Reconstruction seems to **benefit from tracking loop update**

## References:

1: Schlüter, S., Stolle, C., Jakowski, N., Jacobi, C. (2003) Monitoring the 3-Dimensional Ionospheric Electron Distribution based on GPS Measurements. In: Reber, C., Lühr, H., Schweitzer, P. (eds) First CHAMP Mission Results for Gravity, Magnetic and Atmospheric Studies. Springer, Heidelberg.  
2: Dahlke, C., D. Arnold, A. Jäggi (2015) Impact of tracking loop settings of the Swarm GPS receiver on gravity field recovery. Advances in Space Research, 59(12), 2843-2854. doi:10.1016/j.asr.2015.04.003  
3: Jäggi, A. & Meyer, Ulrich & Schreiter, Lucas & Sterken, V. & Dabke, C. & Arnold, D. & Encarnação, João & Visser, Peter & van den IJssel, Joak & Mas, Xinyuan & Jerfida, Elisabetta & Bezdek, Ales & Sebera, Josef & Mayer-Gürr, T. & Zehentner, Norbert & Sham, C.K. & Lusk, C. & Rothrock, R. & Knebe, Jürgen & Zhang, Yu. (2018). Assessment of individual and combined gravity field solutions from Swarm GPS data and mitigation of systematic errors. Manuscr. Geodae., 18, 240, 5289, 1993.

## CONTACT / COPYRIGHT

Lucas Schreiter  
Astronomical Institute, University of Bern  
Sidlerstrasse 5  
3012 Bern (Switzerland)  
lucas.schreiter@aiub.unibe.ch

