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ABSTRACT

Full control over the density and emission properties of GaN quantum dots (QDs) should be feasible, provided that the growth proceeds in the Stranski-Krastanov (SK) growth mode. In this work, we derive the phase diagram for GaN QD formation on AlN by NH_3 -molecular beam epitaxy and analyze the corresponding optical signature by micro-photoluminescence (μ -PL). Interestingly, the growth window for SK-GaN QDs is very narrow due to the relatively small lattice mismatch of the GaN/AlN system (2.5%), constituting a fundamental challenge for QD growth control. By relying on bulk AlN single crystal substrates, we demonstrate QD density control over three orders of magnitude, from 10⁸ to 10¹¹ cm⁻² by changing the growth rate. In contrast, the QD density is pinned to 2×10^{10} cm⁻² when growing on AlN/sapphire templates, which exhibit dislocation densities on the order of 10^{10} cm⁻². Thanks to QD densities as low as 10^8 cm⁻² on bulk AlN, we can probe the emission of spatially isolated single GaN QDs by μ -PL on unprocessed samples.

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The progress in the field of integrated quantum optics has been fueled by potential applications in, e.g., quantumcomputing and secure data transmission. 1,2 First, lab-on-a-chip experiments using the mature III-V quantum dot (QD) arsenide material system were realized to address, e.g., single photon emission characteristics, two-photon interference, and polarization entanglement.4 Nowadays, all building blocks from the quantum light source, over waveguides and beamsplitters, 6,7 to single photon detectors⁸ are at hand. Epitaxial QDs have proven as promising quantum light emitters based on their scalability and integrability.2 However, the operation of such sources is often limited to cryogenic temperatures.9

In contrast, future non-cryogenic on-chip quantum optics would need to build on nanostructures or suitable point-defects based on wide-bandgap materials such as SiC, 10 diamond, 11 II/ III-oxides, 12 or III-nitrides. For instance, GaN QDs embedded in AlN can exhibit large exciton binding energies in excess of 150 meV, rendering them ideal candidates for single photon emission at room temperature and beyond. 13 Recently, coherent control of excitonic qubits, 14 two-photon emission at 50 K based on the biexciton cascade, 15 and room-temperature single photon emission¹⁶ were reported for GaN QDs embedded in

Al(Ga)N. Single photon emission up to 350 K was reported by Holmes et al.¹⁷ from a GaN QD embedded in a nano-pillar. Despite such recent achievements, future on-chip integration of three-dimensional (3D)-structures that boost the light outcoupling efficiency shall prove to be extremely challenging. The aforementioned complex arsenide structures are commonly based on planar, strain-induced Stranski-Krastanov (SK) QDs which can, e.g., straightforwardly be embedded into photonic crystals.² In the prototypical InAs/GaAs system, SK growth manifests itself by a spontaneous morphological transition from a smooth 2D surface to 3D islanding during growth after a certain thickness of InAs. 18,19 In this material system, the QD size and the density are tunable over a large range of values,²⁰ inpart due to the large lattice mismatch of 7.2% between InAs and GaAs and the high surface kinetics, which favor islanding.

The lattice mismatch between GaN and AlN is only 2.5%, which may hinder the SK growth mode transition. Nonetheless, GaN/AlN QDs have been realized by using plasma assisted molecular beam epitaxy (PA-MBE), 21-24 ammonia molecular beam epitaxy (NH₃-MBE), ²⁵⁻²⁹ and metalorganic vapor phase epitaxy (MOVPE).^{30–32} Based on these techniques, several growth methods for achieving QDs have been developed. For

instance, droplet epitaxy,^{33,34} SK,^{22,24} and modified-SK^{34,35} growth were reported for PA-MBE. In the case of NH₃-MBE, a transition from a 2D to a 3D growth mode was found for the growth of AlGaN when finely tuning the growth conditions;³⁶ however, for the growth of GaN, most QD growths were achieved by a modified-SK method. A 2D-3D transition is achieved after a growth interruption and cutting off of the NH₃ flow.^{25–27,29,37} Notice that all these different approaches share one common disadvantage: the QD density commonly appears to be pinned at about 10¹⁰ cm⁻², representing the lack of growth control necessary for further progress towards integrated quantum optic devices.

In the present work, we demonstrate GaN/AlN QD density control from 10⁸ to 10¹¹ cm⁻² by using a SK growth mode on bulk AlN substrates. By comparing GaN QDs grown on bulk AlN and on AlN on sapphire templates, we demonstrate that the presence of threading dislocations fixes the minimum QD density which can be achieved on the latter. In contrast, growth on AlN single crystal substrates allows us to tune the QD density over three orders of magnitude, while keeping the same equivalent GaN coverage. Finally, we report the photoluminescence (PL) properties of low density QDs grown on the AlN single crystal substrate.

Growth was performed on AlN on c-plane sapphire with typical threading dislocation densities (TDDs) on the order of $10^{10}\,\mathrm{cm^{-2}}$ and on a bulk AlN single crystal with TDD of $10^3\,\mathrm{cm^{-2}}$ substrates in a Riber C-21 MBE. Prior to QD growth, $100\,\mathrm{nm}$ of AlN were grown at high temperatures ($1050-1150\,^{\circ}\mathrm{C}$) under N-rich conditions (V/III \sim 200) to ensure a single monolayer (ML) height step flow morphology. 38,39 We define the following as the standard growth conditions for GaN QDs on AlN: a substrate temperature ($1000\,\mathrm{cm}$) of $1000\,\mathrm{cm}$ of $1000\,\mathrm{cm}$ 0 of $10000\,\mathrm{cm}$ 0 of $1000\,\mathrm{cm}$ 0 of 10000

The film's free energy describing the formation of self-assembled 3D islands of GaN deposited on AlN can be expressed in terms of the energy of a pseudomorphic 2D surface and of the energy of coherently strained 3D islands. According to Mariette, 40 one obtains

$$E_{2D}(h) = M\epsilon_{GaN}^2 h + \gamma, \tag{1}$$

and

$$E_{3D}(h) = (1 - \alpha)M\epsilon_{GaN}^2 h + \gamma + \Delta\gamma, \tag{2}$$

where $E_{2D}(h)$ is the energy of the pseudomorphic 2D surface, M is the film's biaxial modulus, ϵ_{GaN} is the strain, $M\epsilon_{GaN}^2h$ is the elastic energy for a given GaN equivalent thickness (h), and γ is the surface energy for the (0001) surface. $E_{3D}(h)$ is the energy of the layer when a fraction α of the surface is covered by 3D islands, and $\Delta\gamma$ is the surface energy cost to form the 3D islands. For a given GaN thickness h, the layer will rearrange in 3D islands if $E_{3D}(h) < E_{2D}(h)$ and the minimal thickness for which this inequality holds will be the critical thickness for the 2D-3D transition (h_{2D-3D}). Furthermore, islanding supposes a sufficient diffusion length. The latter depends mainly on T_S and V_{GaN} . Hence, the formation of 3D islands is kinetically limited and higher T_S leads

to faster 3D islanding as shown by Damilano et al.²⁶ From this simplified model, it is already clear that $\Delta \gamma$ plays a paramount role in determining whether the layer will undergo a 2D to 3D transition. For instance, using standard growth conditions in NH₃-MBE, Damilano et al.²⁵ observed a 2D growth regime and plastic relaxation. This behavior occurs for a wide range of substrate temperatures and is independent of the initial density of dislocations. 41 A 2D-3D transition was only possible after a growth interruption without NH3 flow-the basis for the modified SK-growth method. It was concluded that $\Delta \gamma$ is reduced under vacuum; alternatively, this can be understood as $\Delta \gamma$ being proportional to the NH3 pressure. One could be tempted to increase T_S to provide the energy to promote island formation and overcome the barrier set by the surface energy. However, GaN decomposes under vacuum at a significant rate for temperatures above 750 °C, a process that can be prevented by supplying NH₃. ⁴² In summary, we can establish the following guidelines for the spontaneous formation of self-assembled GaN 3D islands by a SK growth mode:

- 1. T_S should be increased to maximize the diffusion length but should be kept at reasonable values to prevent high evaporation rates ($V_{\rm evaporation}$).
- 2. The NH_3 flow should be minimized because $\Delta\gamma$ depends strongly on the NH_3 pressure. Indeed, high NH_3 flows completely hinder the formation of 3D islands.²⁵
- 3. The growth rate V_{GaN} should be low enough to allow the necessary formation time²⁶ for a given $\Delta\gamma$ and T_S . V_{GaN} should also be lowered in order to remain under N-rich conditions, even when using low NH₃ flows.

With these considerations in mind, we selected a growth temperature of 750°C and decreased both the growth rate (0.025 ML/s) and the NH₃-BEP (3.3×10^{-7} Torr), matching the standard growth conditions. The 2D-3D morphological transition was monitored by reflection high energy electron diffraction (RHEED). In Fig. 1(a), the typical RHEED intensity curves during the growth of GaN on AlN for growth conditions promoting 3D island formation are displayed. RHEED intensity oscillations, signature of a layer by layer growth mode, are observed for the specular beam for a thickness up to 3 MLs; afterwards, the oscillations stop and the intensity decreases. After the completion of 3 MLs, a drastic increase in intensity is observed at Bragg diffraction positions, indicating the formation of the 3D islands. The critical thickness for the morphological transition was further confirmed by atomic force microscopy (AFM). As shown in Figs. 1(b) and 1(c), a 2D-3D transition occurs at 3 MLs. Very small, low density $(3 \times 10^9 \,\mathrm{cm}^{-2})$ QDs are obtained. The inset of Fig. 1(c) displays a height profile over an exemplary island.

Note that this transition occurs without growth and NH_3 interruption. Thus, our results indicate that a conventional SK growth can be achieved by NH_3 -MBE. Hence, the versatile growth control found in arsenides should become applicable for GaN/AlN QDs.

We report in Fig. 2 a phase diagram of the growth conditions that lead either to the spontaneous formation of 3D islands (red dots) or to a 2D surface (black crosses) on AlN/sapphire templates. Under high NH_3 BEP and low T_S , the RHEED shows

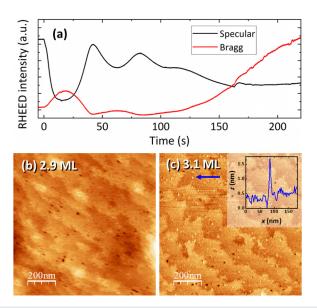


FIG. 1. (a) RHEED intensity at the specular and Bragg positions for standard growth conditions. (b) and (c) $1 \times 1 \mu m^2$ AFM scans of GaN on AlN/sapphire templates, showcasing a value of 3 MLs for the critical thickness of the 2D-3D transition (h_{2D-3D}) . Inset: Height profile over a 3D island.

the common streaky pattern, which is typical for the 2D surface. The high $\rm NH_3$ pressure leads to high $\Delta\gamma$ values that prevent islanding, and GaN relaxes plastically. In Fig. 2, this growth regime is indicated by blue color shading. At low $\rm NH_3$ BEP and high $\rm T_S, V_{evaporation}$ is non-negligible and can compete with $\rm V_{GaN}$ (green shaded regime of Fig. 2). Thus, only a sharp growth window enables 3D islands. Further details are discussed in the supplementary material.

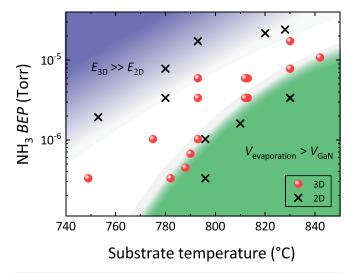


FIG. 2. Phase diagram of the surface morphology measured by RHEED in terms of NH_3 beam equivalent pressure (*BEP*) and substrate temperature at a growth rate of 0.025 ML/s.

The equivalent GaN thickness h is the most prominent variable affecting the size and the density of the QDs. An increase in h simultaneously increases the QDs' density and height and thus decreases the emission energy. AL23,25,30 While using standard growth conditions and h=4 MLs, the AFM evidences well-defined QDs with a density of $\sim 10^{10}$ cm⁻² and typical heights and diameters of 2.5–3 nm and 20–35 nm, respectively. At 6 MLs, the surface is completely covered with QDs and the QD density reaches 10^{11} cm⁻² (see supplementary material).

An even more insightful observation regarding the evolution of the QD density on AlN/sapphire templates can be made by using our standard SK growth conditions at varying growth rates $V_{\rm GaN}.$ In general, longer diffusion lengths can be achieved by either increasing $T_{\rm S}$ or by decreasing $V_{\rm GaN}.$ A longer diffusion length should increase the probability for an ad-atom to attach at an existing QD site instead of nucleating a new island, thus reducing the density by increasing the QD size. However, in contrast to these expectations, AFM demonstrates that the QD density is hardly altered upon varying $V_{\rm GaN}$ (black squares in Fig. 3). The QD density appears as pinned to $\simeq 2\times 10^{10}~\rm cm^{-2}$ when growing on AlN/sapphire templates in the investigated $V_{\rm GaN}$ interval (0.001–0.025 ML/s). Hence, even though the conventional SK growth mode is applied, QD density control is still not possible.

Interestingly, switching from AlN/sapphire templates to bulk AlN single crystal substrates provides further insight into the apparent growth limitations. In contrast to our previous observation, a strong dependence of the QD density on $V_{\rm GaN}$ is present when growing on AlN single crystal substrates (see Fig. 3-blue dots). AFM images 1–3 from Fig. 3 highlight the achieved QD growth control by varying $V_{\rm GaN}$.

The dependence of the QD density on the substrate of choice can be understood by a detailed examination of AFM scan 4 from Fig. 4. Here, small dark spots can be observed next to most of the QDs. These pits are identified as edge dislocations. Such positioning of QDs next to edge dislocations was first

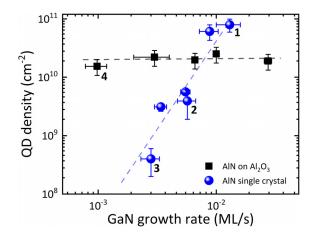


FIG. 3. QD density measured by AFM as a function of V_{GaN} on AIN/sapphire templates (black squares) and AIN single crystal substrates (blue dots). The dashed lines are guides to the eye. The numerical labels are related to the corresponding AFM images in Fig. 4.

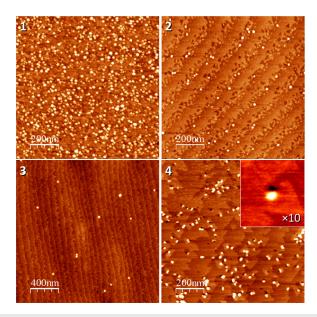


FIG. 4. AFM images of the labeled data points in Fig. 3. AFM images 1 to 3 originate from QD growth on AIN single crystal substrates, whereas image 4 originates from growth on an AIN/sapphire template. Inset: Magnification of a dot and a dislocation. Images 1, 2, and 4 show 1 \times 1 μm^2 areas, while AFM image 3 represents a 2 \times 2 μm^2 scan.

reported by Rouvière *et al.*⁴³ Edge dislocations create a strain dipole and thus provide a local minimum for strain release during the segregation of GaN.^{44,45} Any structural defects will lead to a non-perfect strain field and thus to preferential nucleation sites for the QDs at the strain minima. In contrast, the close-to featureless surface of the AlN grown on the AlN single crystal substrates (except the atomic terraces) provides a very smooth, strain-induced potential landscape. Hence, the growth of low density QDs becomes feasible, provided a sufficient diffusion length, is applied.

In order to explore the optical properties of SK-GaN QDs grown on AlN single crystal substrates, we prepared a sample with parameters that lead to a very low QD density [h = 3.5 ML and $V_{\rm GaN} = 0.0015$ (± 0.0010) ML/s]. This sample was capped with a 50-nm thick AlN top barrier.

The sample was mapped using a 266 nm (4.66 eV) laser operating in continuous waves at a sample temperature of 5 K. A $50 \times 50~\mu\text{m}^2$ map was obtained by moving the laser excitation spot using a step size of $0.5~\mu\text{m}$ ($\simeq 0.5~\mu\text{m}$ laser excitation spot diameter). The polychromatic $\mu\text{-PL}$ map scan is displayed in Fig. 5(a). The map is plotted such that it highlights deviations from the background luminescence within the 3.7 to 4.5 eV range. It becomes clear that only a low density of specific locations shows QD-like luminescence as demonstrated in Fig. 5(b). Here, a selection of typical QD spectra is shown, exhibiting distinct sharp emission lines. Given the low excitation power density applied for the map scan, it seems plausible as a first approximation that each emission line corresponds to a single QD. 13,15 Clearly, a pronounced contribution of multi-excitonic features is only expected for higher excitation densities. Based on this

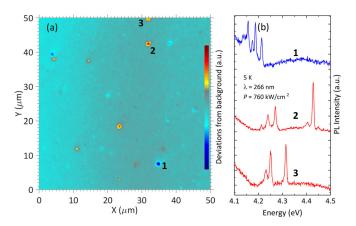


FIG. 5. (a) $50 \times 50~\mu\text{m}^2~\mu\text{-PL}$ map. We plot deviations from the substrate background luminescence. (b) Selected sites from the map displaying the typical QD emission (vertically shifted for clarity) found throughout the sample.

assumption, we derive a density of active QD emitters within the energy interval of 3.7 to 4.5 eV of $8\times10^6\,\mathrm{cm}^{-2}$. Clearly, this density only represents a lower boundary for the QD density, as particularly faint QD emitters could be masked by, e.g., the defect luminescence of the AlN substrate. Nevertheless, the present μ -PL results of Fig. 5(a) in combination with the applied growth parameters suggest that the QD density is significantly lower than for the sample shown in AFM image 3 in Fig. 4 $(4\times10^8\,\mathrm{cm}^{-2})$. The luminescence of the wetting layer is discussed in the supplementary material.

Currently, the defect luminescence of the bulk AlN substrate prevents any more sophisticated μ -PL spectroscopy on single GaN QDs as, e.g., $g^{(2)}$ -measurements in order to ensure single photon emission characteristics. PL excitation spectroscopy of Alden et al. has shown that the AlN defect luminescence exhibits a distinct excitation channel at 4.7 eV. 46 Collazo et al. reported a corresponding absorption coefficient ($\alpha_{4.7eV}$) above 1000 cm⁻¹ for the first generation of AlN substrates. 47 In contrast, the present study utilized the latest generation of AlN substrates exhibiting $\alpha_{4.7eV}$ < 100 cm⁻¹. Hence, the defect luminescence intensity drops by around one order of magnitude (not shown), rendering the emission of single QDs well comparable to the bulk defect luminescence bands, cf. Fig. 5(b). Future substrate development aiming for lower point defects is needed in order to enable more in-depth quantum-optical studies of SK GaN QD samples.

In conclusion, we demonstrated SK growth for GaN QDs on AlN using $\rm NH_3$ –MBE by carefully tuning the $\rm NH_3$ flow and the substrate temperature. As a result, QD density control was achieved similar to the seminal In(Ga)As/GaAs QD system. AFM images reveal a dot density variation from 10^8 to $10^{11}\,\rm cm^{-2}$. The use of low growth rates as well as of AlN single crystal substrates allowed us to optically address individual QDs. These results represent a promising advance towards the integration of single GaN QD operating at non-cryogenic temperatures into more complex photonic structures. 2

See supplementary material for additional information regarding experimental details, low temperature QD growth, QD ripening, and the luminescence of the wetting layer.

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