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Determination and optimization of material parameters of particle-based LaTiO₂N photoelectrodes

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15 Abstract

16 We developed a validated numerical model capable of predicting the photocurrent-voltage

17 characteristics of oxide and 18 oxynitride particle-based 19 photoelectrodes and identifying 20 the critical parameters affecting 21 performance of the those 22 photoelectrodes. We used 23 particle-based LaTiO₂N 24 photoelectrodes as the model 25 system. Two different types of 26 electrodes were studied: 27 LaTiO₂N photoelectrodes with 28 TiO₂ inter-particle connections 29 and the same photoelectrodes



30 with $NiO_x/CoO_x/Co(OH)_2$ co-catalysts and a Ta₂O₅ passivation layer. The necessary material parameters, namely complex refractive index, permittivity, density of states of the conduction and 31 valence bands, charge mobilities, flatband potential, doping concentration, recombination 32 lifetimes, and interfacial hole transfer velocity, were derived by density functional theory 33 calculations, dedicated experiments, and fitting of the numerically determined photocurrent-34 35 voltage curves to the measured ones under back-side illumination. The model was validated by 36 comparing its prediction to front-side illumination photocurrent-voltage measurements. A parametric study was then carried out to provide an extensive set of material design guidelines and 37 38 key parameters for high-performing particle-based LaTiO₂N photoelectrodes. The interfacial hole 39 transfer velocity was identified as the most significant parameter for the performance of LaTiO₂N 40 photoelectrodes.

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42 **1. Introduction**

The direct conversion of solar energy into chemical fuels via photoelectrochemical (PEC) water splitting is a viable route for the production of solar hydrogen^{1,2}. Scaled production of solar

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hydrogen must be cost competitive with non-renewable hydrogen production (mostly steam 1 2 reforming of natural gas), which requires scalable PEC approaches that produce hydrogen with 3 high efficiency but at low cost. PEC approaches using particle-based photoelectrodes (PEs), which 4 can be fabricated with simple dip or slurry coating procedures that are already scaled in industrial 5 battery production, can be a route to efficient and economic solar hydrogen. LaTiO₂N (LTON) is 6 a promising PEC material with a suitable bandgap of $2.1 \text{eV}^{3,4}$ which enables the absorption of visible light up to 590nm. Indeed, highly preforming particle-based LTON PEs with a photocurrent 7 density up to 8.9mA/cm² at 1.23V vs RHE were recently reported⁵. However, the various material 8 9 parameters of particle-based LTON PEs must be determined, and the impact of each parameter on 10 the photocurrent and their underlying multi-physical phenomena must be investigated and understood to further improve the performance of particle-based LTON PEs. 11

12 Numerical modelling can help in identifying crucial material, processing, and design challenges 13 for PEs, not accessible and identifiable by experimental investigations. Berger et al. introduced the 14 first 1-dimensional (1D) PEC electrode model for investigating the light absorber's role on the 15 device performance by accounting for the charge transport in the electrolyte and in the semiconductor⁶. This model was developed for homogeneous, thin-film photoabsorber materials 16 17 and metallic catalysts and was compared to a crystalline-Si PEC cell with Pt as a hydrogen 18 evolution reaction catalyst, two materials with well-known material parameters. These parameters 19 were either taken from literature or assumed (for example, the charge transfer rate constant from the semiconductor to the electrode). Cendula et al.⁷ introduced a 1D model capable of describing 20 21 photocurrent-voltage (I-V) curves and energy band dynamics of photoabsorbers in direct contact 22 with an electrolyte. Their work was based on n-type hematite and p-type cuprous oxide, two known 23 semiconductor materials. However, some material parameters such as the densities of states of the 24 conduction and valence band and the relative permittivity of cuprous oxide were assumed. The 1D 25 numerical model of charge transfer at the semiconductor-catalyst-electrolyte interface by Mills et 26 al. provided the flexibility to account for different types of catalysts (metallic, adaptive, and 27 molecular), and has provided insights into the I-V characteristics of semiconductor-catalyst-28 solution sytems⁸. Their model was based on semi-classical macroscopic semiconductor physics, 29 similarly to what we use here. They assumed numerous parameters (for example, the hole/electron 30 transfer rate constants) and compared their results to experiments with a n-TiO₂ photoabsorber and 31 IrOx, hydrous Ni(OH)₂/NiOOH, and NiOx catalysts. Our previous work with a 1D validated 32 numerical model, accounting for electromagnetic wave propagation (EMW) within the electrolyte 33 and semiconductor and for charge carrier transport and conservation within the semiconductor and 34 at the semiconductor-electrolyte interface, has shown the significant impact of surface lifetimes on 35 the photocurrent for a thin-film GaN photoanode, a well-defined material with known material 36 parameters⁹. It becomes obvious from these early modelling works that the knowledge of the 37 material parameters is key for model accuracy. However, determining the material parameters of 38 many well-known, well-defined materials and films is already a challenge. For this reason, successful models have been mostly limited to classical semiconductor materials such as Si, GaAs, 39 GaInP, TiO₂ or GaN^{6,9-12}, in monocrystalline and almost defect free thin films. Detailed 40 experimental characterization of these materials has been done for decades, and essential material 41 parameters (e.g. electrical transport properties or electron and hole recombination lifetimes) are 42 well documented in literature^{13–16} or in well referenced electronic archives¹⁷. However, many of 43 the recent materials (e.g. BiVO4^{18,19}, SrTiO3^{20,21} and LTON) used in high performing PEs are 44 complex oxides or oxynitrides. The parameters of these materials are less investigated and also less 45 straight forward to determine since variations in the synthesis procedure induce significant 46 47 differences in terms of defect density and morphology for the same compound. Transport properties

are especially difficult to assess since the preparation of comparable thin films is not yet possible 1 2 for some complex oxides and oxynitrides like LTON²². This is one of the significant challenges in 3 building a realistic numerical model of particle-based PEs of oxides and oxynitrides.

The second challenge is related to the multi-physical nature of PEs^{23,24}. Most of the material 4 5 parameters are difficult to determine since they depend on multi-physical interactions. It is often 6 not possible to determine them with one dedicated experiment or numerical model. Instead, a 7 combination of experiments and numerical modeling must be used to isolate each physical process 8 with its related parameters. Numerous experiments, such as spectrophotometry, electrochemical 9 impedance spectroscopy (EIS), and conduction measurements, are required and need to be 10 carefully combined with molecular and macroscopic numerical models in order to build a complete 11 model capable of describing the I-V characteristics of oxide and oxynitride PEs.

12 The third challenge is related to the morphological complexity of particle-based PEs for which a 13 traditional 1D model is not appropriate and a 3D discrete model is not vet practical. In such a 14 complex PE, each photocatalytic particle is almost fully surrounded by an electrolyte enabling the 15 oxygen evolution reaction (OER). The use of a 1D model would reduce this continuous interface to a single one at the model's boundary. Therefore, a 1D model requires to determine an average 16 17 path for charge transport and conservation which can only be found once all other material 18 parameters are known. In contrast, a 3D-scale model based on the exact morphology can fully 19 capture the physical behavior of particle-based PEs, but the morphological complexity of LTON 20 particles, including nanopores inside and at the surface of particles, introduce considerable 21 computational efforts and require nano-scale transport modeling. Additionally, inter-particle 22 charge transfer mechanism have not been investigated for our PEs. Therefore, it is challenging to 23 develop a model with a simplified morphology that can still capture the physical behavior of LTON 24 particle-based PEs and allows for understanding the interplay of multi-physics processes and 25 identifying key factors in the performance of LTON PEs.

26 Here, we describe the development of a 2D model which is able to predict the performance of 27 particle-based PEs made of oxynitrides, specifically LTON particles. LTON particle-based PEs 28 were chosen as the model system because of the monocrystallinity of the particles²⁵, reproducibility by simple dipping procedures⁴, and potential for high performance⁵. The 2D PE model accounts 29 30 for the EMW propagation, charge generation and transport, and semiconductor-electrolyte 31 interface charge transfer. Bulk material parameters, namely the density of states of the valence and 32 conduction bands and the relative permittivity, were calculated by density functional theory (DFT). 33 Consequently, our approach provides a link between the macroscopic and molecular simulation approaches in PEC materials and devices. Additional material parameters, such as spectrally-34 35 resolved complex refractive index, charge mobilities, flatband potential and doping concentration, 36 are extracted from dedicated experiments. The numerical model is used in combination with back-37 side illumination experiments to inversely determine missing material parameters, such as 38 recombination lifetimes and interfacial hole transfer velocity, parameters not accessible 39 experimentally. By doing so, we identify simultaneously the critical parameters affecting the 40 performance of LTON particle-based PEs while showing the predictive character of the model 41 (specifically predicting the I-V curve under front-side illumination). Finally, we provide pathways 42 for the improvement of LTON PEs by identifying the key parameters contributing to performance 43 enhancement.

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1 2. Numerical I-V curve model

The numerical model to predict the I-V characteristics accounts for EMW propagation, charge transport and conservation, and semiconductor-electrolyte interface charge transfer. All equations are presented in detail in our previous work⁹. Here, we only review the equations relevant to key material parameters for the performance of the LTON particle-based PEs.

6 Model domain and general assumptions - The complex morphology of LTON PEs is simplified 7 by an equivalent homogeneous domain (Fig. 1) relying on two approximations. First, the light 8 absorption model considers the particle-based PEs as a thin film (Fig. 1.b) of the same thickness as 9 the particle-based PEs with a weighting according to the solid-phase density profile along the 10 thickness. Second, the domain for the semiconductor physics was reduced to the dimensions of an average-sized single particle, approximated by a rectangular domain with two semiconductor-11 12 electrolyte interfaces, one ohmic contact between LTON and the fluorine-doped tin oxide (FTO) 13 and one insulation interface to account for contacts with upper particles (Fig. 1.c). Only a single 14 particle in direct contact with the FTO is assumed to significantly contribute to the photocurrent. 15 This approximation can be justified by considering that the inter-particle contact introduces a resistance due to the formation of a double Schottky barrier^{26,27}, reducing the space charge layer 16 (SCL) potential, V_{SCL} , at the semiconductor-electrolyte ²⁸ as given by $V_{SCL} = V_a - \sum_{i}^{n} V_{IPC,i}$, with 17 $V_{\rm a}$ the applied potential, $V_{\rm IPC}$ the potential drop at the inter-particle contact, and *n* the number of 18 inter-particle contacts the electron goes through. Additionally, the inter-particle contact reduces the 19 20 effective electron mobility $(1/\mu_{eff,n} = 1/\mu_b + \sum_{i=1}^{n} 1/\mu_{IPC,i})$ as observed for polycrystalline silicon^{29,30} or mesoporous TiO₂. In the latter case, it was observed that the electron diffusion 21 coefficient in the mesoporous TiO₂ dropped when the particles were not well sintered leading to 22 poor performance of dye sensitized solar cells³¹. Generally, photoelectrodes containing only one 23 24 layer of LTON particles have shown equal or even better performance than multilayer particle-25 based photoelectrodes, pointing to the vital role of the first particle layer for the performance of the $PE^{4,5}$. 26

27 The dimensions of the approximated particle size, namely $1.42 \,\mu m$ thickness and $0.6 \,\mu m$ width, are 28 based on the average dimensions and orientations of particles calculated by a detailed quantitative 29 structural analysis of LTON particle-based PEs utilizing 3D nano-tomography data of the actual 30 electrodes³². A particle identification algorithm based on fitting ellipsoids inside LTON particles 31 was applied to focused ion beam scanning electron microscopy (SEM) data. Particle characterization such as nominal sizes of particles were then determined by fitting a log-normal 32 33 distribution of particle size in x, y, and z directions. The average orientation of particles in all 34 directions was also determined. The length of the model domain is $1.42 \mu m$, corresponding to the 35 average particle size of the longest axis of 1.79µm (Fig. S1) and the average orientation angle of 36 37.4° (Fig. S2), i.e. the angle between the normal of the FTO plan and the direction of the particle 37 in the longest direction. The width of the model domain is 0.6µm, corresponding to the average 38 particle size of the medium and shortest direction.

39

40 **Radiation absorption** - The electron-hole pair generation rate was calculated considering a 2D 41 EMW propagation model with irradiation wavelengths from 400nm to 590nm, corresponding to 42 the spectrum of the solar simulator, up to the bandgap of LTON (2.1eV=590nm). The irradiation 43 was considered as transverse electric field, and therefore, only the out-of-plane electric field was 44 calculated. Bloch-Floquet theory was assumed for the periodicity on both lateral sides of the 45 computational domain with a width of 5µm, ensuring convergence of the model^{33,34}. Fig. 1.b 46 depicts the computational domain, the dimensions, and the boundary conditions of the model. The location-dependent charge carrier generation rate in LTON particle-based PEs was calculated by solving the Maxwell's curl equation³⁵ for each spectral band of the irradiation for the given spectrally-resolved complex refractive index and the particle density profile. A spectral band of $\Delta\lambda$ = 4nm was carefully chosen to reduce calculation time without losing accuracy of the calculated generation rate. For non-chromatic sources of light, the total generation rate is the spectral integration of the fraction of the absorbed optical power and the energy of the corresponding photon.

8 EMW propagation was calculated considering the electrolyte (assumed to have the optical 9 properties of water), the FTO glass, and LTON, with the spectral irradiance of the solar simulator 10 Verasol-2 from Oriel and an incident angle of 0° (Fig. S4). The reflection losses at the semiconductor-electrolyte interface can greatly influence the photogeneration efficiency and were 11 12 accounted for by adding a 2mm-thin layer of water at the back- and the front-side of the PE. The 13 absorption losses due to the electrolyte are negligible since the water extinction coefficient is below $4 \cdot 10^{-6}$ in the visible range^{36,37}. Indeed, the same photogenerated current density was calculated 14 15 using a smaller thickness of the water layer. The spectral complex refractive index, \tilde{n} , of LTON is 16 a material parameter required for the numerical model based on EMW propagation and was 17 extracted from spectrophotometry measurements (see section 3). 18



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Fig. 1. a) Scanning electron microscopy picture of a LTON particle-based PE and indication of the domain sizes used for the numerical model (yellow for the EMW simulations, blue for the semiconductor physics simulations), b) EMW propagation model domain and boundary conditions, and c) semiconductor physics model domain and boundary conditions. The generation rate calculated with model b) is used as an input in

24 model c).

1 Charge transport and conservation - The charge transport and conservation were calculated 2 considering a 2D continuum model within the calculation domain. The 2D model, representing an 3 average LTON particle, ensures that the OER can occur along a typical particle surface. The 4 numerical model fully couples the static and the dynamic behavior of charge carriers in the semiconductor. The static behavior was calculated by solving the Poisson's equation¹⁵ with the 5 6 permittivity and the doping concentration as relevant material parameters. The dynamic behavior 7 of the carriers was calculated by solving the drift-diffusion equation with the electron and hole 8 mobilities as relevant material parameters. The charge carrier density in the semiconductor was 9 determined by the product of the Fermi-Dirac distribution and the density of states of the 10 conduction and valence bands as material parameters. The governing equations were solved at steady-state with a uniform isothermal device temperature of 20°C. The steady-state charge 11 conservation is given by the sum of all recombination and the generation rate, the latter being 12 13 calculated through the EMW model. Only Shockley-Read-Hall (SRH) recombination was 14 considered and modeled using effective electron and hole lifetimes, given by

15

 $R_n^{\text{SRH}} = R_p^{\text{SRH}} = \frac{np - n_i^2}{\tau_{\text{eff},p}(n+n_1) + \tau_{\text{eff},n}(p+p_1)},$ (1)

16

where $n_i = \sqrt{N_c N_v} e^{-E_{gap}/(2k_BT)}$ is the intrinsic carrier density, and N_c and N_v are the conduction 17 and valence band densities of states, respectively. n_1 and p_1 are the electron and hole trap state 18 densities, respectively. The effective electron and hole lifetimes, $\tau_{\text{eff},n/p}$, is a combination of the 19 bulk lifetimes, $\tau_{n/p}$, and the surface lifetimes, $\tau_{s,n/p}$, given by 20

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22

$$\frac{1}{\tau_{\text{eff},n/p}} = \frac{1}{\tau_{n/p}} + \frac{1}{\tau_{\text{s},n/p}}.$$
(2)

23

24 We used effective lifetimes to account for both the bulk and the surface recombination, which is in accordance with the general practice of modeling surface recombination^{38,39}. This approximation 25 26 still accurately predicts the I-V characteristics of water-splitting photoelectrodes, as shown in our 27 previous work⁹. The charge transport at the particle-FTO interface was modeled as an ideal ohmic contact. The 28

29 current density at the semiconductor-electrolyte interface along the side of the particle was 30 determined by using a Schottky contact with the interfacial hole transfer velocity and the flatband 31 potential as relevant material surface parameters. The interfacial hole transfer velocity dictates the kinetics of the oxygen evolution reaction at the semiconductor-electrolyte interface. The hole 32 current, i_p , in a Schottky contact (the photocurrent in an n-type semiconductor) is given by 33

34

$$\boldsymbol{i}_{p} \cdot \boldsymbol{n} = q \boldsymbol{v}_{s,p} (p - p_{\text{eq}}), \tag{3}$$

35

$$\boldsymbol{u}_p \cdot \boldsymbol{n} = q \, \boldsymbol{v}_{s,p} (p - p_{\text{eq}}), \tag{3}$$

36 where n is the surface normal, p is the hole concentration at the semiconductor-electrolyte interface, and p_{eq} is the hole concentration at equilibrium. The use of a Schottky contact to describe 37 the charge transfer mechanism at the semiconductor-electrolyte interface simplifies the actual 38 39 charge transfer mechanisms involved in a photoelectrode with co-catalyst and surface states (SS). 40 A charge carrier can be transferred across different interfaces and paths, such as a direct transfer from the LTON bulk states to the electrolyte, through SS, and/or through co-catalysts. Each path, 41

1 with its own kinetic characteristics, is competing with the others. Moreover, SS or co-catalyst might

- 2 lead to Fermi level pinning, inducing a potential drop not only in the SCL but also in the
- electrolyte⁴⁰. However, if the band bending due to the semiconductor-electrolyte interface is fully
 developed and if there is no mass transport limitation from the electrolyte side, the use of a Schottky
- 5 contact has shown to fit experimental I-V curves well (for example for GaN⁹). We confirmed that
- 6 an electric field was present at the semiconductor-electrolyte interface by conducting open-circuit
- 7 voltage measurements for the LTON particle-based PEs (Fig. S5). We also used a highly alkaline
- 8 solution to ensure that mass transport limits were not present. Furthermore, the Helmholtz layer
- 9 (HL) capacitance is usually much larger than the SCL capacitance, thus ensuring that the applied
- 10 potential drops only in the SCL and not in the $HL^{41,42}$. Therefore, the Schottky contact 11 approximation was justified in the present study. Further details and equations related to the 12 Schottky contact mechanism can be found in our previous work⁹.

13 Flatband potential, doping concentration, densities of states, permittivity, charge mobilities,

- effective lifetimes, and interfacial hole transfer velocity are required material parameters for the charge transport and conservation numerical model and were extracted from molecular numerical
- model, various experimental measurements, and the inverse analysis (see section 3).

18 **3. Determination of material parameters**

19 *Complex refractive index* - The complex refractive index, $\tilde{n}=n-ik$, of LTON was extracted from 20 spectrophotometry measurements. Spectral reflectance and transmittance were acquired in an air 21 environment with a UV-3600 Shimadzu UV-VIS-NIR spectrophotometer using an integrating 22 sphere to account for diffuse reflectance and transmittance.

The real part of the complex refractive index, the refractive index, *n*, of LTON particle-based PEs was determined by using the total reflectance, ρ_m , measured under front-side illumination and using the Fresnel's equations⁴³ under normal incident, unpolarized light with $n \gg k$, given by

26

$$n = \frac{n_{\rm air}(\rho_{\rm m} + 2\sqrt{\rho_{\rm m}} + 1)}{1 - \rho_{\rm m}} \cong \frac{\sqrt{\rho_{\rm m}} + 1}{1 - \sqrt{\rho_{\rm m}}} \text{ with } n_{\rm air} \cong 1.$$
⁽⁴⁾

27

The imaginary part of the complex refractive index, the extinction coefficient, *k*, was determined by using the total transmittance, $\tau_{\rm m}$, and reflectance, $\rho_{\rm m}$, measured under back-side illumination. The reflectance measurement was corrected for the absorbance of the FTO glass by $\rho_{\rm c} = \rho_{\rm m} + \alpha_{\rm FTO}$. The absorbance of the FTO glass was determined by transmittance and reflectance measurements using $\alpha_{\rm FTO}=1-\rho_{\rm FTO}-\tau_{\rm FTO}$. Following the multiple internal reflections for a single partially transmitting layer with a film thickness much larger than the irradiation wavelength, $D > \lambda$, the reflectance and transmittance are given by⁴³

$$\rho_{\rm c} = \rho_{\rm m} + \alpha_{\rm FTO} = \rho \left[1 + \frac{(1-\rho)^2 \sigma^2}{1-\rho^2 \sigma^2} \right]$$
(5)

and
$$\tau_{\rm m} = \frac{\sigma (1-\rho)^2}{1-\rho^2 \sigma^2}$$
. (6)

36

37 where ρ is the light intensity amount reflected, and 1- ρ is the amount refracted. σ is the transmitted 38 amount given by $\sigma = e^{-\tau/\cos\theta_i}$ with τ the optical thickness and θ_i the incident angle. The 39 absorption coefficient was assumed to depend on the particle density distribution, $\rho(z)$, along the 40 height, $\alpha(z) = \alpha^* \rho(z)$. The particle density distribution was calculated by a detailed quantitative structural analysis of LTON particle-based PEs utilizing 3D nano-tomography data of the actual electrodes³² (Fig. S3). The effective depth, D^* , of particle-based photoelectrode using the particle density distribution is given by

4

$$\tau = \alpha^* \int_0^D \rho(z) dz = \alpha^* \cdot D^*.$$
⁽⁷⁾

5 By rearranging eqs. (5) to (7) and considering an incident angle of $\theta_i = 0^\circ$, the absorption coefficient, 7 α^* , can be expressed in function of the measured transmittance and the corrected reflectance, given 8 by 9

$$\alpha^* = -\frac{1}{D^*} \ln\left(\frac{\sqrt{(-\rho_c^2 + 2\rho_c + \tau_m^2 - 1)^2 + 4\tau_m^2} - \rho_c^2 + 2\rho_c + \tau_m^2 - 1}{2\tau_m}\right).$$
(8)

10

11 Finally, the extinction coefficient depending on the PE's thickness is given by $k(z) = k^* \rho(z)$, where 12 $k^* = \alpha^* \lambda / 4 / \pi$.

13

14 Density of states of the valence and conduction bands, and relative permittivity - Assuming 15 parabolic bands in the electronic band structure, the density of states of the valence and conduction 16 bands are given by⁴⁴

17

 $N_{\rm V/C} = 2 \left(\frac{2\pi m_{\rm h/e}^* k_B T}{h^2}\right)^{3/2}.$ (9)

The electron and hole effective masses, $m^*_{\rm h/e}$, of LTON were computed using DFT calculations 19 with the Quantum ESPRESSO⁴⁵ package using the PBE⁴⁶ exchange-correlation functional with a 20 Hubbard U correction⁴⁷ of 3.0 eV applied to the Ti 3d states and using the virtual crystal 21 approximation to describe a $\frac{1}{3}$ N $\frac{2}{3}$ O disorder on the anion sublattice (for additional 22 23 computational details, see the supporting information). Based on band structure calculations, we 24 determined the electron and hole effective mass tensors using finite differences with a stencil grid 25 of step size 0.01Bohr⁻¹ by means of the EMC utility⁴⁸. For our orthorhombic cell (b is the long 26 axis), we converted the effective masses in all direction into conduction effective masses via 27

$$m_{\text{cond}}^* = 3\left(\frac{1}{m_a} + \frac{1}{m_b} + \frac{1}{m_c}\right)^{-1}.$$
 (10)

The permittivity of LTON was computed using functional perturbation theory, considering bothelectronic and ionic contributions.

30

31 Flatband potential and doping concentration - The flatband potential and the doping 32 concentration were determined by EIS and Mott-Schottky analysis of LTON PEs. The Mott-33 Schottky plot of LTON PEs using only a capacitance showed a high frequency dispersion (Fig. 34 S6). This frequency dispersion is commonly found in practical electrodes and is attributed to various physico-chemical phenomena, such as surface roughness, surface defects, local charge 35 inhomogeneity, absorbed species, different phase region, variations in composition and 36 37 stoichiometry, doping inhomogeneity, dielectric relaxation, electric double layer, and deep donor levels 49-51. 38

Frequency-independent Mott-Schottky plots using Mott-Schottky theory^{44,50} can be obtained by using a constant phase element (CPE) combined with the appropriate EIS model. Zoltowski suggested using the following admittance of the CPE⁵²:

4

$$Y_{\rm CPE} = Y_0(i\omega)^{\alpha}.$$
 (11)

5 6 where $Y_0(\text{F} \cdot \text{s}^{\alpha-1})$ and α are the frequency independent parameters of the CPE ($0 \le \alpha \le 1$), and ω the 7 angular frequency. Y_0 cannot be approximated as a capacitance since a small deviation of α from 1 8 would lead to large error in the capacitance⁵¹, and Y_0 does not have the unit of a capacitance as 9 mentioned by Zoltowski⁵². The capacitance without any frequency dispersion is obtained from Y_0 10 and the related resistance, $R^{49,53}$, given by

11

$$C = \frac{(R \cdot Y_0)^{1/\alpha}}{R}.$$
(12)

12

13 The model for EIS fitting and for determining the flatband potentials and doping concentrations of 14 the best-LTON PEs is depicted in Fig. 4. LTON PEs with co-catalysts were used for the impedance 15 analysis instead of LTON without co-catalysts due to better performance and more reliable results. $R_{\rm s}$ in the equivalent circuit model denotes a series resistance of the electrolyte and the 16 semiconductor. R_{sc} and CPE_{sc} denote the resistance and the CPE in the SCL. R_{ss} and CPE_{ss} denote 17 18 the resistance and the CPE caused by SS at the semiconductor-electrolyte interface. This equivalent circuit is usually used for a semiconductor-electrolyte interface with species adsorption at the 19 20 interface⁵⁰ and was previously used for n-type GaN⁵⁴.

The model was fitted to a frequency range of 2-16kHz to 50Hz to avoid the slow diffusion 21 component, which is not related to the SCL capacitance⁵⁴. The varying upper frequency limit is 22 23 due to an abrupt change in the impedance spectra of the best-LTON PEs appearing in all our 24 electrodes at a frequency of 10kHz at 0.12V vs reversible hydrogen electrode (RHE) (Fig. S7). The 25 flatband potential is often determined using the Mott-Schottky equation, which requires that the 26 HL capacitance is much larger that the SCL capacitance. Since the HL capacitance is unknown, 27 the flatband potential is reported without considering any potential shift due to the HL capacitance, 28 in accordance with the general practice⁴⁹.

29

30 *Electron and hole mobilities* - The conductivity of LTON particle-based PE was measured by 4-31 point probes with a sourcemeter (Keithley 2450). The mobilities of electron and holes are estimated 32 by conductivity measurements and using the DFT-calculated effective mass of electrons and holes. 33 The conductivity, σ , of a semiconductor material is given by

34

35

$$\sigma = q(n\mu_n + p\mu_p), \tag{13}$$

36 where *n* and *p* are the electron and hole densities. μ_n and μ_p are the electron and hole mobilities. 37 Since LTON is naturally a n-type semiconductor material, the hole density in the material is 38 negligible compared to the electron density. Consequently, the hole density term in the conductivity 39 equation (as (12)) was neglected. The abave density in the hole was

equation (eq. (13)) was neglected. The charge density in the bulk of the semiconductor was assumed to be zero, hence $n \approx N_{\rm D}^+$, and the electron mobility is given as $\mu_n = \sigma/(qN_{\rm D}^+)$. By

41 assuming that the average scattering time of electrons and holes is equal, the hole mobility is

42 calculated by

Electron and hole effective lifetimes and interfacial hole transfer velocity - The interfacial hole 3 4 transfer velocity and effective lifetimes (combination of surface lifetimes at the semiconductorelectrolyte interface, inter-particle contact, and bulk lifetimes) are difficult to access 5 6 experimentally. Here, we used an inverse analysis for their determination. First, we measured I-V 7 curves under back- and front-side illumination and provided experimental error bars. Then, we 8 applied our inverse analysis which consisted in varying these parameters until the numerical I-V 9 curves fitted the experimental I-V curves under back-side illumination within the error bars. Once, 10 a parameter had been determined under back-side illumination, the numerical photocurrent under 11 front-side illumination was calculated and compared with the corresponding measurement. If the 12 numerical photocurrent under front-side illumination followed the experimental one, the 13 determined parameter was approved, and the model was considered validated and of predictive 14 character. Finally, the exact value of the parameter was determined by minimizing the R-square 15 value of the numerical fitting to the averaged experimental I-V curve above 1V vs RHE under 16 front-side illumination.

 $\mu_p = \mu_n \frac{m_e^*}{m_h^*}.$

17

18 **4. Experimental section**

19 Photoelectrode preparation and characterization - Two types of LTON PEs were prepared following the procedure of Landsmann et al.⁴: best-LTON with multiple coating processes and 20 21 bare-LTON with a single dipping procedure. In both configurations, the LTON PEs were fabricated 22 using LTON suspended particles deposited on a FTO glass substrate by electrophoretic deposition. 23 Subsequently, the LTON PEs were dipped in an ethanol solution of Ti(OEt)₄ and then annealed 24 under a NH₃ flow. This last process ensures ohmic contact between the LTON particles and the 25 FTO glass substrate. These electrodes were called bare-LTON PEs. Best-LTON PEs were obtained 26 by additional dipping of the electrodes firstly in an ethanol solution of Ta(OEt)₄ followed by 27 annealing under NH₃ flow to form a passivation layer of Ta₂O₅. NiO_x co-catalysts were then 28 deposited by dipping the electrode in an ethanol solution of Ni(NO₃)₂ and subsequently annealed 29 in normal air environment. A similar procedure was used to deposit the CoO_x co-catalyst. Finally, 30 the Co(OH)₂ co-catalyst was also deposited by a dipping procedure. SEM images of the electrodes 31 were acquired with a FEI NovaNanoSEM using a through-the lens detector at 5 kV acceleration 32 voltage. 33 The thickness of the PEs were determined by taking the average thickness along 1µm of the PEs,

- measured by profilometry using a Bruker DektakX with a 60° tip and an applied contact weight of 1mg. The best-LTON PEs have an average thickness of 8.43µm, and the bare-LTON PEs have an
- 36 average thickness of 5.51 μ m. All LTON PEs in this work have an illuminated surface area of
- 37 1 ± 0.3 cm².
- 38 Photoelectrochemical measurements Photoelectrochemical experiments were conducted in a 39 three-electrode setup to refer the potential of our measurements to the RHE. The electrodes were
- 40 connected to a potentiostat (Bio-Logic VSP-300 controlled by the EC-lab software) for I-V curve
- 41 measurements and EIS measurements. The reference electrode was Ag/AgCl (sat. KCl), and the
- 42 counter electrode was Pt. The aqueous electrolyte solutions used were 0.1M Na₂SO₄ and NaOH at
- 43 pH=13.2±0.2. The sample was illuminated by the solar simulator VeraSol-2 from Oriel
- 44 corresponding to AM1.5G in the visible and near-infrared region (400-1100nm) with a light

(14)

irradiance of 76±3 mW/cm² (Fig. S4). The PEs were measured under front-side illumination with 1 2 the irradiance transmitted through the electrolyte and absorbed by the LTON and under back-side 3 illumination with the irradiance transmitted through the electrolyte and the FTO glass substrate 4 before being absorbed by the LTON (Fig. 1). I-V curves were measured with a potential sweep of 10mV/s in the potential range of 0.5 to 1.5V vs RHE. A small hysteresis could be observed between 5 6 forward and backward swept voltage even at this low voltage sweep rate. Therefore, the current 7 density was averaged between forward and backward swept voltage. The final I-V curves depicted 8 in this work for best-LTON and bare-LTON under back- and front-side illumination are the 9 measurement averages of eight fresh PEs each to ensure representative results and stable current 10 conditions (LTON corroded in the electrolyte after a few minutes under illumination). The error 11 bars of the experimental I-V curves are the minimum and maximum photocurrent densities 12 measured for the eight PEs. EIS was done under dark conditions at potentials varying from 0 to 13 0.6V vs RHE and covering a frequency range of 50Hz to 20kHz.

14

15 **5. Results and discussion**

16 **5.1. Determination of material parameters**

17 **5.1.1. Optical parameters and photoabsorption**

18 *Complex refractive index* - The complex refractive index of bulk LTON calculated with eqs. (4) 19 and (8) from transmittance and reflectance measurements are depicted in Fig. 2. The Tauc plot of LTON is given in the supporting information (Fig. S8). The refractive index based on the total 20 21 reflectance using eq. (4) has a drop below 600nm. This drop can be interpreted as the bandgap 22 value of LTON (600nm \approx 2.1eV) using the Kubelka-Munk (K-M) transform based on the total 23 reflectance (Fig. S9). It is therefore often used to determine the bandgap of semiconductors, for 24 which transmittance cannot be measured. The complex refractive of the glass substrate and the 25 FTO layer can be found in the supporting information (Figs. S10 and S11). For validation purposes, the transmittance was numerically simulated using the obtained optical 26 27 parameters and compared to the experimental one (Fig. S12). The transmittance was also calculated

by utilizing Beer-Lambert's law and additionally accounting for reflectance and absorptance of the
FTO glass substrate (Fig. S13). The calculated transmittance for both methods was below 2% error
compared to the measured transmittance in a spectral range of 400nm to 590nm. This gave us

31 confidence in the accuracy of the extracted complex refractive index of LTON PEs. The model

32 based on Beer-Lambert's law is very efficient and simple compared to EMW propagation model

but should be used with care in the UV region where over 3% error in the transmittance under backaida illumination was absorbed (relative error of 100% at 240 pm Fig. S12 c)

34 side illumination was observed (relative error of 100% at 340nm, Fig. S13.a).

35



1 Wavelength (nm) 2 Fig. 2. Complex refractive index of LTON particle-based PE using reflectance and transmittance measurements 3 with an integrating sphere. The refractive index (left y-axis) is calculated using Fresnel's equation (eq. (4)) in 4 conjunction with total reflectance measurements. The extinction coefficient (right y-axis) is determined using 5 reflectance and transmittance measurements in conjunction with eq. (8) derived by considering multiple 6 internal reflections in a single, partially transmitting thick layer ($D > \lambda$).

8 Generation rate - The calculated generation rate and photogenerated current density under back-9 and front-side illumination of the solar simulator is depicted in Fig. 3. Under back-side 10 illumination, the generation rate follows an exponential decay given by the constant extinction coefficient, resulting from a constant density of particles within the first 1.5µm (Fig. S3). The ratio 11 12 between the front- and back-side illumination photogenerated current density reproduces the 13 experimental front- and back-side photocurrent ratio. The numerical model, considering only the first layer of particles in direct contact with the FTO, is already partially validated, based only on 14 light absorption. As depicted in Fig. 3, the front-side illumination's photogenerated current is more 15 affected by the use of only the first layer of particles. The photogenerated current densities of the 16 front- and back-side illuminations are 0.8mA/cm² and 4.4mA/cm² respectively. 17

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 19
 Thickness(μm)

 20
 Fig. 3. Generation rate of LTON particle-based PEs under back- and front-side illumination with the AM1.5G

- 21 solar simulator's spectral irradiance. The integrated photogenerated current density is indicated for PEs of 22 this large 1 42 mm (dashed king) and 8 42 mm
- 22 thickness 1.42µm (dashed line) and 8.43µm.

1 **5.1.2 Electronic parameters**

2 Density of states of the valence and conduction bands - For our orthorhombic cell (b is the long 3 axis), the electron effective masses are 0.788, 4.553 and $0.390m_{\rm e}$ along the a, b and c axes, 4 respectively, whereas the hole effective masses are 0.714, 0.956 and $0.341m_{\rm e}$, respectively, $m_{\rm e}$ 5 being the electron mass at rest. We converted these into conduction effective masses via eq. (10), 6 resulting in $0.740m_{\rm e}$ for the electrons and $0.558m_{\rm e}$ for the holes. These values agree well with 7 $0.750m_{\rm e}$ and $0.517m_{\rm e}$ obtained by averaging over conduction effective masses for explicit disorder 8 models⁵⁵. The light holes in oxynitrides can be explained from their electronic structure. While the 9 top of the valence band is N 2p dominated, the Ti 3d dominated bottom of the conduction band is 10 hybridized more with O 2p than N 2p orbitals. Given the stronger covalent Ti-N bond compared to 11 Ti-O, a stronger band dispersion for the N-derived states at the top of the valence band compared 12 to the bottom of the conduction band is expected. Therefore, we observe a lighter mass of the holes 13 compared to the electrons. In pure oxides or nitrides, such an effect would be absent, but we see similar trends for layered Ruddlesden-Popper oxynitrides⁵⁶. The density of states of the valence 14 and conduction bands using eq. (9) are 1.01 10¹⁹ cm⁻³ and 1.54 10¹⁹ cm⁻³, respectively, at a 15 temperature of 20°C. The electronic band structure of orthorhombic LTON can be found in the 16 17 supporting information (Fig. S14).

18

19 **Relative permittivity** - The full tensor of the relative permittivity of LTON is given in the supporting 20 information. We converted it to a single value via an effective medium theory⁵⁷ and obtained a 21 value of 14.94 without the second order correction and 15.19 with second order corrections. For 22 the macroscopic model, we assumed an approximate relative permittivity of ε_r =15.

23

24 Flatband potential and doping concentration - Fig. 4 shows the Mott-Schottky plot for best-25 LTON PEs in the dark with a resulting flatband potential of 0.1 V vs RHE (in accordance with the work of Feng et al.⁵⁸) and a doping concentration of 7.43·10¹⁷ cm⁻³. The flatband potential of 0.1 V 26 vs RHE is also in accordance with the I-V curve found in a previous paper⁵⁸. A flatband potential 27 28 of 0.1V vs RHE and a doping concentration of 7.4.10¹⁷ cm⁻³ result in a conduction band situated at 29 0.02V vs RHE, below the hydrogen evolution reaction (HER) potential. However, hydrogen 30 production with LTON particles has been reported by Kasahara et al.³. We think that the HER can still occur with the conduction band below the HER potential because these redox systems have a 31 continuous distribution of energy states and not a single discrete state⁵⁹. Nevertheless, this situation 32 33 will lead to very poor hydrogen production as reported by Kasahara et al. (one order of magnitude 34 lower production of hydrogen than oxygen). The same situation is observed with BiVO₄ with a flatband potential of 0.1V vs RHE⁶⁰ and the ability to produce hydrogen⁶¹ or La₅Ti₂CuS₅O₇ with a 35 valence band above the OER potential⁶² and the ability to produce oxygen⁶³. The normal surface 36 of the electrode used to calculate the doping concentration with the Mott-Schottky equation^{50,64} 37 was 0.79 cm². The active area, A_{active} , was 14.39 cm², utilizing a surface roughness factor of 18.2, 38 obtained from the structural analysis³² (Table 1). The flatband potential obtained with the best-39 LTON PEs gives the same result as the one obtained from a Mott-Schottky plot with frequency 40 41 dispersion (Fig. S6). We can expect to see the effect of SS recombination on the photocurrent up 42 to a potential of 0.6V vs RHE (Fig. 4) and higher, since the onset potential is at 0.9 V vs RHE (Fig. 5). Similar distributions of $1/C_{ss}^2$ have been shown for other semiconductor materials such as TiO₂ 43 in aqueous electrolyte⁶⁵. 44

45 We obtained a doping concentration variation of $\pm 5 \cdot 10^{17}$ cm⁻³ based on two measurements with

46 newly prepared best-LTON PEs.



Fig. 4. Frequency-independent Mott-Schottky plots for best-LTON photoelectrodes with the determined doping concentration. The equivalent circuit for the electrochemical impedance analysis is also indicated.

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Hole and electron mobilities - The electron mobility of the LTON particle-based PEs is 46 $\text{cm}^2\text{V}^{-1}\text{s}^{-1}$ with a doping concentration of $7.43 \cdot 10^{17} \text{ cm}^{-3}$ and with a measured conductivity of 5.51 S/cm (eq. (13)). By using the effective masses determined by DFT calculations and using eq. (14), the hole mobility of LTON is 61 cm²V⁻¹s⁻¹.

11 Effective electron lifetimes - The numerical I-V curves for varying effective electron lifetimes 12 under back- and front-side illumination are presented in Fig. 5, together with the experimentally 13 measured ones. The experimental relative error of the photocurrent is $\pm 17\%$ at 1.23V vs RHE for 14 the best-LTON PEs under back-side illumination and ±30% under front-side illumination. A 15 numerical photocurrent density within the experimental variations above 1V vs RHE under both illuminations' sides is obtained for an electron lifetime of 510⁻¹⁰s. We can conclude that our 16 numerical model can reproduce the experimental I-V curves well and is predictive by reproducing 17 18 the front-side illumination I-V curve. The photocurrent density below 1V vs RHE was not 19 considered for the fitting of the experimental I-V curves since the modeling of the photocurrent in 20 the potential region below 1V vs RHE is highly complex. Indeed, surface recombination is present 21 at low applied potential and any attempt to simulate the photocurrent in this region requires precise 22 knowledge of the surface recombination phenomena with all the related parameters. Thus, this work, in conjunction with state-of-the-art modeling work^{7,8}, does not address this issue nor 23 reproduces well the I-V curves in the regions where surface recombination occurs (potential below 24 25 1V vs. RHE). An in-depth understanding and modeling of surface recombination phenomena at the 26 semiconductor-electrolyte interface would greatly help the community to improve the performance 27 of photoelectrodes but is still missing. The numerical model was also compared to experimental I-28 V curves under back illumination for different light intensities: 1 sun, 0.1 sun and 0.01 sun. 29 Although some discrepancies between the numerical and the experimental I-V curves occur at a 30 potential between 0.9V to 1.3V vs RHE—most probably due to the surface recombination—the 31 numerical model is able to follow the experimental I-V curves for different light intensities (Fig. 32 33 S15).



Fig. 5. Numerical and experimental photocurrent-voltage curves of best-LTON under a) back- and b) frontkide illumination for varying effective electron lifetimes. The photocurrent density was reduced from 1.18mA/cm² to 0.63mA/cm² at 1.23V vs RHE when reducing the effective electron lifetime by four orders of magnitude under back-side illumination (from 10ns to 1ps). Under front-side illumination, the photocurrent density was reduced from 0.55 mA/cm² to 0.34mA/cm² at 1.23V when reducing the effective electron lifetime by four orders of magnitude.

8 The back-side illumination photocurrent of best-LTON PEs is around 2.5 times higher than the 9 front-side illumination photocurrent at 1.23V vs RHE, although part of the light is absorbed by the 10 FTO glass under back-side illumination and not under front-side illumination. Since electrons are 11 collected at the FTO substrate, electrons generated closer to it have a higher chance to be collected 12 before recombining, leading to a higher photocurrent under back-side illumination. As previously 13 mentioned, we assumed for the modeling that only the first layer of particles in direct contact with 14 the FTO substrate is significantly contributing to the photocurrent. This approximation is supported 15 by the experimental I-V curves (Fig. 5) since the upper particles (not contributing to the photocurrent) are parasitically reducing the light under front-side illumination. This unexpected 16 behavior was attributed in previous work to electron transport limitations due to poor inter-particle 17 18 conductivity^{4,66–68}. The numerical photocurrent reaches saturation already at 1.3V vs RHE while 19 the experimental photocurrent does not show saturation below 1.5V vs RHE (Fig. 5.b). We 20 hypothesize that this discrepancy is caused by the upper particles of the PE starting to contribute 21 to the photocurrent under large applied potential (above 1.3V vs RHE). Such a large applied 22 potential might help to overcome the potential losses appearing at the inter-particle contacts of the 23 upper particles. In the case where there is no potential loss for the upper particles and, thus, the 24 entire thickness of the photoelectrode becomes active, the front-side illumination photocurrent 25 would be larger than the back-side illumination (Fig. S16). This is not observed for our particle-26 based LTON photoelectrodes. We recognize that in reality a smoother potential drop for the top 27 particles might be experienced, instead of our assumed complete loss of the applied potential above 28 the first layer of particle. Future work will be devoted to investigate this assumption and variations 29 thereof.

30

31 *Effective hole lifetimes* - The impact of effective hole lifetime under back- and front-side 32 illumination on the calculated photocurrents is depicted in Fig. 6, together with the experimentally

33 measured ones. The effective hole lifetime affects both the photocurrent and the onset potential. A

 $\frac{1}{2}$

hole lifetime of $5 \cdot 10^{-10}$ s gave a photocurrent density within the experimental variation for both illuminations' sides above 1V vs RHE.

)



Fig. 6. Numerical and experimental photocurrent-voltage curves of best-LTON under a) back- and b) frontside illumination for varying effective hole lifetimes. The photocurrent density was reduced from 1.01mA/cm² to 0.37mA/cm² at 1.23V vs RHE when reducing the effective hole lifetime by four orders of magnitude under back-side illumination (from 10ns to 1ps). Under front-side illumination, the photocurrent density was reduced from 0.68 mA/cm² to 0.11mA/cm² at 1.23V when reducing the effective hole lifetime by four orders of magnitude.

10

11 *Interfacial hole transfer velocity* – The numerical I-V curves for varying interfacial hole transfer 12 velocities under back- and front-side illumination are presented in Fig. 7, together with the 13 experimentally measured ones. The interfacial hole transfer velocity significantly affected the 14 photocurrent under back- and front-side illumination. A hole transfer velocity of $v_{s,p} = 3.5 \cdot 10^{-6}$ cm/s 15 provided a numerical photocurrent within the experimental variation under back-side illumination 16 above 1V vs RHE. The same hole transfer velocity was within the experimental error under front-17 side illumination.



Fig. 7. Numerical and experimental photocurrent-voltage curves of best-LTON PEs under a) back- and b) frontside illumination for varying interfacial hole transfer velocities. The hole transfer velocity was significantly affecting the photocurrent under back-side illumination: a photocurrent of 3.48mA/cm² at 1.23V vs RHE with $v_{s,p}$ =1·10⁻⁴cm·s⁻¹ and of 1.01mA/cm² with $v_{s,p}$ =3.5·10⁻⁶cm·s⁻¹. Under front-side illumination, the hole transfer velocity was less affecting the photocurrent since the photocurrent reached almost saturation at 1.23V vs RHE

- 1 with $v_{s,p}=3.5\cdot10^{-6}$ cm·s⁻¹, a photocurrent density of 0.61mA/cm² at 1.23V vs RHE with $v_{s,p}=1\cdot10^{-4}$ cm·s⁻¹ and of
- 2 0.54mÅ/cm² for $v_{s,p}=3.5\cdot10^{-6}$ cm·s⁻¹.
- 3 All material parameters of LTON particle-based PE used in this work are summarized in Table 1.
 - 2.1eV^{3,4,66,69–72} Literature Band gap, E_{gap} $4.3 eV^{71}$ Electron affinity, γ Flatband potential, $V_{\rm FB}$ 0.1V vs RHE Mott-Schottky analysis $7.43 \cdot 10^{17} \text{ cm}^{-3}$ Donor concentration, $N_{\rm D}^+$ **DFT** calculation 15 Relative permittivity, ε_r 0.74 Effective mass of electron, m_e^* Effective mass of holes, $m_{\rm h}^*$ 0.558 $1.54 \cdot 10^{19} \, \mathrm{cm}^{-3}$ Density of states of the conduction band, $N_{\rm C}$ $1.01 \cdot 10^{19} \, \mathrm{cm}^{-3}$ Density of states of the valence band, $N_{\rm V}$ $46 \text{ cm}^2 \text{V}^{-1} \text{s}^{-1}$ Conductivity measurements + Electron mobility, μ_n $61 \text{ cm}^2 \text{V}^{-1} \text{s}^{-1}$ **DFT** calculation Hole mobility, μ_p **Inverse analysis Best-LTON** Electron effective lifetime, $\tau_{eff.n}$ $5 \cdot 10^{-10} \text{ s}$ $1 \cdot 10^{-11} \text{ s}$ Bare-LTON Electron effective lifetime, $\tau_{eff,n}$ $5 \cdot 10^{-10} \text{ s}$ Hole effective lifetime, $\tau_{\text{eff},p}$ **Best-LTON** Hole effective lifetime, $\tau_{\rm eff,p}$ $1 \cdot 10^{-11}$ s **Bare-LTON** $3.5 \cdot 10^{-8} \text{m} \cdot \text{s}^{-1}$ **Best-LTON** Interfacial hole transfer velocity, $v_{s,p}$ $8.2 \cdot 10^{-9} \text{m} \cdot \text{s}^{-1}$ **Bare-LTON** Interfacial hole transfer velocity, v_{sn} $1.42 \mu m^{32}$ **Quantitative structural analysis** Height of model domain, d Width of model domain, W $0.6\mu m^{32}$ Surface roughness factor, r18.232 Interfacial electron transfer velocity, $v_{s,n}$ $1 \cdot 10^{-12} \text{ m} \cdot \text{s}^{-1*}$ Assumption
- Table 1. Material parameters of LTON particle-based PE determined by dedicated experiments (Mott-Schottky
 analysis and conductivity measurements), DFT calculations, and inverse analysis.

- *An interfacial electron transfer velocity of 1 10⁻¹²m/s is assumed to avoid having the back reaction of oxygen reduction.
- 6 7

8 5.2 Identifying key material parameters

9 Interfacial hole transfer velocity - The interfacial hole transfer velocity is highly affecting the 10 performance of the particle-based LTON PEs, as depicted in Fig. 7.a. Indeed, we observed a potential photocurrent increase of 2.3mA/cm² at 1.23V vs RHE compared to our current 11 12 experimental results when increasing the interfacial hole transfer velocity under back-side 13 illumination by a factor of 10. Similar trends were observed for photocurrent densities under frontside illumination, although the improvement was limited to 0.07mA/cm² at 1.23V vs RHE (Fig. 14 15 7.b). The interfacial hole transfer velocity also reduces the onset potential since it reduces the recombination rate and, thus, the need of a higher band bending at the semiconductor-electrolyte 16 17 interface. Therefore, less applied potential is required to overcome the recombination present in the SCL. The shape of the photocurrent's curve also changes with varying interfacial hole transfer 18 velocity, i.e. decreasing the slope of the photocurrent curve with smaller velocities. The 19 photocurrent density increased from 2.5mA/cm² to 3.5mA/cm² at 1.23V vs RHE with $v_{s,p}$ 20 increasing from 10⁻⁵ to 10⁻⁴ cm/s, respectively. Above a value of $v_{s,p} = 1.10^{-4}$ cm/s, the photocurrent 21 density remained constant at 3.5mA/cm² at potentials above 1.23V vs RHE, only the onset potential 22 23 was improved. The interfacial hole transfer velocity is the parameter affecting most significantly 24 the performance of LTON particle-based PEs in terms of photocurrent and onset potential.

25

Hole and electron mobilities – Improving the hole mobility from $10 \text{ cm}^2 \text{V}^{-1} \text{s}^{-1}$ to $500 \text{ cm}^2 \text{V}^{-1} \text{s}^{-1}$ does not significantly affect the photocurrent density, i.e. it increased the photocurrent by 0.1mA/cm^2 at 1.23V vs RHE, 10% relative increase (Fig. 8). Under back-side illumination, the

impact of the hole mobility was higher, with an increase of 0.22mA/cm² at 1.23V vs RHE (37% 1 2 relative increase) for a hole mobility increase from 10 cm²V⁻¹s⁻¹ to 500 cm²V⁻¹s⁻¹. LTON particles 3 have a high hole mobility, $61 \text{ cm}^2 \text{V}^{-1} \text{s}^{-1}$, and this is confirmed by the numerical I-V curves within the experimental error bars (Fig. 8). Therefore, the hole mobility is not a limiting parameters for 4 the performance of the PEs and any further improvement of it by, for example, reducing the doping 5 6 concentration of the material⁷³ would not lead to any performance improvement of the LTON PEs. The photocurrent was insensitive to variations of the electron mobility (tested for 0.1 cm²V⁻¹s⁻¹ to 7 8 500 cm²V⁻¹s⁻¹) under both illuminations' sides (Fig. S17). The photocurrent is a hole current and 9 the electrons are only here to balance the hole current under steady-state, but are not the limiting 10 factor. Only if the electron mobility becomes too small would the electrons not be able to balance the hole current, resulting in the photocurrent abruptly dropping to zero. This was the case under 11 front-side illumination for an electron mobility of 0.1 cm²V⁻¹s⁻¹ and below. 12



Fig. 8. Numerical and experimental photocurrent-voltage curves of best-LTON under a) back- and b) frontside illumination for varying hole mobilities. The photocurrent density was reduced from 1.02mA/cm² to 0.37mA/cm² at 1.23V vs RHE when reducing the hole mobility from 500cm²V⁻¹s⁻¹ to 0.01 cm²V⁻¹s⁻¹. Under frontside illumination, the photocurrent density was reduced from 0.59 mA/cm² to 0.07mA/cm² at 1.23V when reducing the hole mobility from 500cm²V⁻¹s⁻¹.

18

Electron and hole effective lifetimes - Both electron and hole lifetimes are affecting the 19 20 photocurrent and the onset potential (Fig. 5 and Fig. 6). The impact of effective hole lifetime on the photocurrent, however, was greater than for the effective electron lifetime, i.e. the photocurrent 21 22 increased by 0.5mA/cm² at 1.23V vs RHE for an increase of two orders of magnitude in hole lifetime compared to an increase of 0.3mA/cm² for an increase of two orders of magnitude in 23 electron lifetime. The impact of the effective hole lifetimes on the photocurrent was less significant 24 25 compared to the effect of the interfacial hole transfer velocity. The most pronounced effect of 26 increasing effective lifetimes was the downshift of the onset potential for both illumination sides. 27 The applied potential directly changed the band bending at the semiconductor-electrolyte interface, 28 and this bending was reduced with a higher effective electron lifetime.

29

30 Doping concentration - Modifying only the doping concentration without changing any other

- 31 parameters did not influence the performance of LTON PEs under back-side illumination (Fig.
- 32 S18.a). Under front-side illumination, the photocurrent was slightly increased, 0.1mA/cm² at 1.23V
- 33 vs RHE, by reducing the doping concentration from 10^{19} cm⁻³ to 10^{16} cm⁻³ (Fig. S18.b). Therefore,

the doping concentration must be varied together with other parameters to see an increase in the 1

- 2 performance.
- 3

4 **5.3 Pathways to improved performance**

5 Properties such as the effective lifetimes, the interfacial hole transfer velocity, and the doping 6 concentration can be modified experimentally to improve the photocurrent. The interfacial hole 7 transfer velocity for best-LTON PEs with CoO_x and CoOH as co-catalysts was still six orders of 8 magnitude smaller than the interfacial hole transfer for n-GaN $(5 \cdot 10^{-2} \text{ m/s})^9$ pointing to the need for co-catalyst improvement. Moreover, the hole transfer velocity of the bare-LTON PE was one 9 10 order of magnitude smaller than the best-LTON PE, i.e. 8.2·10⁻⁹cm/s for bare-LTON and 3.5·10⁻ ⁸ cm/s for best-LTON (Table 1 and Fig. S19). Thus, we conclude that either the role of the catalyst 11 12 is not a truly catalytic one or that the dipping deposition method is not providing a good contact between the catalyst and the photoabsorber. Recently, the deposition of CoOx co-catalyst on LTON 13 14 particle-based PEs with microwave annealing showed significantly higher photocurrent 15 (8.9mA/cm² at 1.23V vs RHE)⁵ than the PEs presented in this work. Therefore, different co-catalyst deposition should be investigated in the future to determine if the deposition method is truly the 16

17 key factor for the performance of LTON particle-based PEs.

18 The effective lifetimes include surface and bulk lifetimes. The effective lifetimes with a value of 19 0.5ns for the best-LTON PEs were high compared to other materials with high surface 20 recombination such as GaN⁹ (2-3 orders of magnitude higher) but low compared to well-known

21 and efficient material such as Si (effective lifetimes above 1µs⁷⁴). The effective lifetime of the best-

22 LTON PE was improved by one order of magnitude compared to the bare-LTON PEs (Table 1).

23 Thus, surface passivation treatments by the deposition of Ta₂O₅, or surface lifetime improvement

24 by deposition of NiO_x of our best-LTON PEs is confirmed to increase the photocurrent.

25 The key parameters on the performance of PEs are the effective lifetimes and interfacial hole transfer. These properties were optimized to improve photocurrent densities as depicted in Fig. 9. 26 27 Additionally, the doping concentration was adapted and optimized accordingly to the new 28 conditions. An internal quantum efficiency (IOE) of 46% (integrated from 400nm to 590nm) was 29 obtained at 1.23V vs RHE by improving the hole transfer velocity from 3.5 · 10⁻⁶ cm·s⁻¹ to 1 · 10⁻⁴ cm·s⁻¹ 30 ¹, increasing the hole and electron lifetimes from 5ns to 1ns, and reducing the doping concentration from 7.43·10¹⁷cm⁻³ to 1·10¹⁶cm⁻³. Indeed, the photocurrent was increased from 1.2mA/cm² to 31

4.33mA/cm² at 1.23V vs RHE, which corresponds to an incident photon-to-current efficiency 32

33 (IPCE) of 10% by considering the entire solar simulator's spectral irradiance (photon flux current

34 density of 41.56 mA/cm²). An effective lifetime of 1ns corresponds to a pure bulk lifetime with 35 complete removal of surface recombination if we assume a bulk lifetime of 1ns like for GaN⁹. The

36 onset can be reduced to 0.1V vs RHE with a strong photocurrent increase at 0.3V vs RHE by further

37 increasing the hole transfer velocity to 100cm/s. Nevertheless, such a high charge transfer velocity

38 is unlikely to be achieved even with highly performing co-catalysts.

39 By only increasing the surface properties of LTON particles, we reached an IQE of 40% at 1.23V

vs RHE which corresponds to a photocurrent increase of 2.56mA/cm², from 1.2mA/cm² to 40

3.76mA/cm². This photocurrent density corresponds to an IPCE of 9%, three times larger compared 41

42 to our current experimental value of 3%.

43 Although these improvements are important, they are greatly limited by the fact that only the first

layer of particles is contributing to the photocurrent. Much higher improvement could be achieved 44

45 if the entire film thickness of the LTON PEs would contribute to the photocurrent and will be

investigated in the future. 46



2

1

Fig. 9. Numerical and experimental photocurrent-voltage curves of best-LTON under back-side illumination for effective lifetime and interfacial hole transfer velocity optimization (blue line) and for additionally doping concentration optimization (red line). The current IPCE is 3% (black or green line) and is improved to 9% (blue line) by only improving the effective lifetimes of hole and electron from 0.5ns to 1ns and the interfacial hole transfer velocity from 3.5·10⁻⁶cm·s⁻¹ to 1.10⁻⁴cm·s⁻¹. The IPCE can be further improved to an IPCE of 10% by reducing the doping concentration from 7.43·10¹⁷cm⁻³ to 1.10¹⁶cm⁻³. The onset potential can be reduced to 0.1V vs RHE by increasing the interfacial hole transfer velocity to 100cm·s⁻¹ (red dashed line).

11 6. Conclusion

12 We presented an experimental-numerical approach for determining material parameters that are 13 not easily accessible otherwise. We successfully connected macro-scale and molecular-scale 14 modeling with optical, transport, and electrochemical experiments to provide—for the first time— 15 all necessary parameters to build a 2D numerical model capable of predicting the I-V curve of 16 particle-based LTON PEs. Furthermore, this numerical model provides a predictive tool for the 17 performance of morphologically complex, multi-component LTON PEs. It allowed us to identify 18 and to study the impact of key parameters on the photoelectrode's performance in order to deduce 19 material design guidelines for materials scientists and give recommendations for pathways to 20 photoelectrode performance engagements. We found that the interfacial hole transfer velocity was 21 the most important parameter, and its improvement should be prioritized. Indeed, photocurrent density was numerically improved by 2.3mA/cm² at 1.23V vs RHE (from 1.2mA/cm² to 22 23 3.5mA/cm²) by boosting only the interfacial hole transfer velocity. Further improvements up to a 24 photocurrent of 4.3mA/cm^2 (IPCE of 10%) were achieved by additionally reducing the doping 25 concentration and increasing the effective lifetime.

25 concentration and increasing the effective lifetime.

The numerical model developed in this work can be further used to study numerically the impact of particle size on the photocurrent, which can be modified using different synthesis routes⁴, and

28 on particle density, which can vary with the deposition method of particles. Thus, design guidelines

29 on the particle arrangement and size of particle-based PEs can be determined with this model.

30 Furthermore, a numerical model of the inter-particle charge transfer mechanism between LTON

31 particles can be added to the current model to provide additional understandings of particle-based

32 PEs and the role of inter-particle necking that is still not elucidated.

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- 6 appreciated.
- 7

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