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# A comprehensive lattice study of SU(3) glueballs

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We present a study of the SU(3) glueball spectrum for all  $J^{PC}$  values at lattice spacings down to  $a^{-1} = 3.73(6)$  GeV ( $\beta = 6.4$ ) using lattices of size up to  $32^4$ . We extend previous studies and show that the continuum limit has effectively been reached. The number of clearly identified  $J^{PC}$  states has been substantially increased. There are no clear signals for spin-exotic glueballs below 3 GeV. A comparison with current experimental glueball candidates is made.

# 1. Introduction

The extraction of reliable predictions for the glueball spectrum of QCD remains an important challenge for lattice gauge theory. As part of a recent programme to study non-perturbative pure SU(3) gauge theory closer to the continuum limit, we have obtained new data for glueball masses which confirm that results of relevance to continuum physics are indeed being achieved with currently accessible lattices. The lowlying spectrum for pure glue states below 3 GeV or so has become well established now and awaits progress with understanding the effects of light-quark mixing.

Glueballs are not particularly light – they start around 1500 MeV – and have no non-trivial flavour content. The extraction of a signal in the presence of vacuum fluctuations is therefore more difficult than for many other hadrons or for potentials. In this situation it is highly desirable to perform coherent measurements over a suitable  $\beta$ -range, in order not to be lost in possible systematic effects. In this spirit we apply here the techniques used by and, in some cases, pioneered by Michael and Teper (MT) [1–3] and extend their analysis. They used lattices ranging from 10<sup>4</sup> to 20<sup>4</sup>, at  $\beta$  values up to 6.2. In the meantime, there has been progress both in the available computing power and in the efficiency of updating algorithms. In this work we have used a hybrid [4,5] of heat-bath and over-relaxation. The code was specifically developed for the Connection Machine and was run on an 8K machine at Wuppertal and a 16K machine at Edinburgh. The key parts of the code, including the group theory, were thus independent of previous work. We have concentrated on  $\beta = 6.4$  on  $32^4$  – slightly larger in physical size than the largest size used by MT, but have also taken data at  $\beta = 6.0$ and 6.2 where a direct comparison could be made.

# 2. Measurement procedures

The  $\beta = 6.4$  results presented in this letter were based on the measurement of 3220 configurations, each separated by ten sweeps. Every fifth sweep was a heat-bath step, the remainder being Creutz overrelaxation. The data was obtained in two parts, from hot and cold starts with at least 2000 sweeps used to equilibrate in each case. During the subsequent analysis, described below, a careful check was made that no residual equilibration effects were present, that both samples were consistent, and the measurement sampling rate was reasonable compared with the autocorrelation times. A direct measurement of the auto correlation time gave  $\tau \leq 20$  sweeps for the correlators of interest. In order to allow greater flexibility in analysis and to allow further cross-checking, the in-line measurements were done in a rather general way. They were made on the  $(L/2)^{3}L$  lattice configuration obtained from an  $L^4$  configuration by Teper fuzzing [6] with the link/staple mixing parameter  $\alpha = 1.0$ . On each time slice, operator momentum transforms for a variety of oriented "shapes" and for all cubic orientations were stored for this level of fuzzing, and for each subsequent level up to the maximum physically reasonable. The shapes were as noted in table 1 (see ref. [3] for details and a diagram). Non-zero momentum operators were used only for the plaquette shape for which we considered  $k_{\mu} = 0, \pm 1$ where  $p_{\mu} = (2\pi/L)k_{\mu}$ . Because of the initial fuzzing step before measurement, the space points summed over were spaced by 2 units so that the momentum eigenvalues  $k_{\mu}$  were unique only up to modulo L/2. For small momenta the contamination is expected to decay very fast in Euclidean time. By studying similar sized lattices in SU(2) we did confirm this effect but found that the t = 0 correlations, and hence 1/0 ratios showed significant contamination from the high momentum piece. Because of the variational nature of the calculation (see below) this did not affect our spectrum results at all. The total time used to update the gauge configuration and make these primary measurements was of order 300 h (16K CM-200 equivalent). The gauge update time was 3.8  $\mu$ s per link.

The operator sums for each time-slice were analysed off-line. We studied Euclidean time correlators for all representations of  $O_h$ :  $A_1$ ,  $A_2$ , E,  $T_1$  and  $T_2$  for both values of parity and C-parity [7]. The relevant projection table is given, for example, in ref. [8]. In addition, we studied Polyakov line correlators (the torelon) as a cross check on the string tension. Further data acquired for smeared Wilson loops and for the topological susceptibility will be presented elsewhere [9]. In the off-line analysis of correlations, a variational approach was used [3] in which a matrix of correlators is formed using, as basis, the different relevant operator shapes and fuzzing levels. By diagonalising the transfer matrix and studying ratios of eigenvalues at consecutive Euclidean times, one ob-

Table 1		
Glueball operators used. S	See ref. [3]	for a diagram.

Links	Shapes	Orientations	Fuzz levels	
4	plaquette	3	1,2,3,4	
6	rectangle	6	1,2,3	
6	chair	12	1,2,3,4	
8	hand	48	1,2,3	
8	butterfly	24	1,2,3	

tains upper bounds on the effective mass (or energy for non-zero momentum) of the ground state in each channel. In principle, estimates of excited states can also be made.

There are two cross-checks on the reliability of the mass values so obtained. First, the overlaps for the various operators are obtained. For a stable determination, one would prefer large "wave-function" components carrying the same sign rather than a delicate cancellation (as a result of a poor choice of basis). Indeed, we have checked the stability of our results to using smaller and differing samples of basis operators. The  $A_1^{++}$  receives contributions from a broad range of shapes and fuzzing levels, while the remaining states receive dominant contributions from the maximum fuzzing level, mostly from the "hand" shaped loops (see table 1). Second, one expects the ground state in each channel to dominate at large Euclidean time. We have monitored the difference between successive effective masses to find at which t value this becomes statistically insignificant. For the determination of errors, we have always used the bootstrap sampling procedure where the data are organised in bins large compared with the measured autocorrelation length #1. For the majority of states, the effective mass "plateau" identified in this way starts at time ratio 2/3.

## 3. Results

Table 2 contains the measured effective masses of all ground state glueballs which can be studied on a hy-

#1 In fact, for test observables, we have used the bin size dependence of the measured variance to cross-check the direct measurements of the autocorrelation time quoted above. Table 2

Glueball effective masses at  $\beta = 6.4$ , in lattice units. The last column shows the ratio to the string tension where the quoted errors arise only from the glueball statistical errors. The  $J^{PC}$  value displayed labels the lowest continuum representation that can contribute. Exotic  $J^{PC}$  content is indicated by (\*).

$O_h$ representation	$J^{PC}$	0/1	1/2	2/3	3/4	4/5	m/√σ
<i>A</i> <sup>++</sup>	0++	0.604(7)	0.435(8)	0.415(14)	0.402(20)	0.38(3)	3.52(12)
$A_{2}^{1++}$	3++	1.552(15)	1.06(4)	1.05(13)	1.0(3)	_	8.9(11)
$E^{2++}$	2++	0.911(5)	0.653(11)	0.620(17)	0.61(3)	0.56(6)	5.25(25)
$T_{2}^{++}$	2++	0.914(5)	0.638(9)	0.598(14)	0.55(2)	0.52(4)	5.07(17)
$T_{1}^{2++}$	1++	1.657(10)	1.10(3)	1.06(8)	1.0(2)	0.8(6)	9.0(7)
$A_{1}^{-+}$	0-+	1.155(9)	0.751(18)	0.63(4)	0.69(7)	0.68(14)	5.3(6)
$A_{2}^{1++}$	3-+*	2.34(3)	1.56(18)	2.6(24)	-		
$E^{2} +$	2-+	1.265(8)	0.853(16)	0.83(4)	0.77(8)	0.9(2)	7.0(3)
$T_{2}^{-+}$	2-+	1.284(7)	0.851(12)	0.79(3)	0.80(6)	0.95(19)	6.7(5)
$A_{1}^{++} \\ A_{2}^{++} \\ E^{++} \\ E^{++} \\ T_{1}^{++} \\ T_{1}^{++} \\ A_{1}^{-+} \\ A_{2}^{-+} \\ E^{-+} \\ T_{2}^{-+} \\ T_{1}^{-+} \\ T_{1}^{-+} \\ H_{1}^{-+} \\ H_{2}^{-+} \\ H_{1}^{-+} \\ H_{2}^{-+} \\ H_{1}^{-+} \\ H_{2}^{-+} \\ H_{2}^{-+} \\ H_{1}^{-+} \\ H_{2}^{-+} \\ H_{1}^{-+} \\ H_{2}^{-+} \\ H_{2}^{-+} \\ H_{1}^{-+} \\ H_{2}^{-+} \\ H_{2}^{-+} \\ H_{1}^{-+} \\ H_{2}^{-+} \\ H_$	1-+*	1.824(10)	1.22(3)	0.99(11)	1.2(5)	-	
$A_1^{+-}$ $A_2^{+-}$ $E^{+-}$ $T_2^{+-}$ $T_1^{+-}$	0+-*	2.24(2)	1.31(9)	0.8(2)	0.9(6)	-	
$A_{2}^{1+-}$	3+-	2.68(3)	1.6(2)	0.9(5)	-		
E <sup>2</sup> +-	2+-*	2.090(18)	1.23(5)	1.2(2)	0.5(4)	-	10(2)
$T_{2}^{+-}$	2+-*	1.461(12)	0.97(2)	<b>0.91</b> (5)	0.93(12)	1.0(4)	7.7(10)
$T_{1}^{2+-}$	1+-	1.188(5)	0.837(13)	0.78(3)	0.82(7)	0.92(14)	6.6(6)
$\begin{array}{c} A_{1}^{} \\ A_{2}^{} \\ E^{} \\ T_{2}^{} \\ T_{1}^{} \end{array}$	0*	2.24(3)	1.55(14)	1.4(6)	-		
$A_{2}^{1}$	3	2.70(3)	1.5(2)	-	-		
E <sup></sup>	2	1.715(13)	1.07(3)	1.03(9)	1.7(6)	-	8.7(8)
$T_{2}^{}$	2	1.804(9)	1.13(3)	1.08(9)	0.9(3)	-	9.2(8)
$T_{1}^{2}$	1	1.845(11)	1.17(4)	1.22(13)	0.8(3)	1.2(10)	9.9(11)

percubic lattice. Where a significant signal was found, the chosen plateau value and its associated error estimate is indicated by bold face. Where larger time ratios gave higher masses or where the plateau was not particularly well established, the error was conservatively estimated from the next larger time ratio. In the final column of the table, the glueball masses m are given in units of the string tension from Wilson loops. We find that the spectrum proposed by MT from the average of their large volume data at  $\beta = 5.9, 6.0$ and 6.2 ([3], table 7) is in agreement with our  $\beta =$ 6.4 mass ratios. Our data at 6.0 (on  $16^3 \times 32$ ) and at 6.2 (on  $32^4$ ) are themselves consistent with the corresponding results of [3]. Overall, we conclude that the new lattice measurements of the low-lying spectrum at  $\beta = 6.4$  do indeed represent useful information about continuum physics.

The restoration of symmetry provides an additional and more stringent test for continuum physics. The expected continuum  $J^{PC}$  content of the  $O_h$  representations can be found, for example, in ref. [7]. In table 2, we indicate only the lowest possible  $J^{PC}$ . We confirm that the E and  $T_2$  ground states (that both contribute to J = 2 in the continuum O(3) symmetry group) exhibit the expected degeneracy for all PC combinations. For PC = ++ this has been found previously in ref. [3] for  $\beta \ge 6.0$ . A related requirement is the restoration of the continuum dispersion relation i.e. Lorentz symmetry. We have been able to test this for the momenta  $k^2 = 0, 1, 2, 3$ . A one parameter fit  $\#^2$  of  $E_k$  to

$$E_{\mathbf{k}}a = \sqrt{m_0^2 a^2 + \left(\frac{2\pi |\mathbf{k}|}{L}\right)^2} \tag{1}$$

yields for the  $A_1^{++}$  data  $m_0 a = 0.425(12)$  with  $\chi^2/\text{DOF} = 0.55$ . The non-zero momentum results for the mass, though slightly higher than the zero momentum value given in table 2, agree well within errors. These two features give strong support to our

<sup>&</sup>lt;sup>#2</sup> For technical reasons, we have not attempted a full correlated error analysis.

statement that, for the low-lying states, our  $\beta = 6.4$  results are effectively measurements of the continuum glueball spectrum.

Different continuum  $J^{PC}$  states can contribute to a given  $O_h$  representation. A priori their level ordering is not obvious. In fact we observe that the 1<sup>++</sup> mass is definitely larger than the 2<sup>++</sup> mass. By assigning the 1<sup>++</sup> quantum number to the  $T_1^{++}$  lattice state we have assumed the "natural" ordering  $m_{1++} < m_{3++}$ . However, the data at  $\beta = 6.4$  show the  $A_2^{++}$  and  $T_1^{++}$ to be approximately degenerate. This is not the naïve expectation since the lowest contributing  $J^{PC}$  values in each case are 3<sup>++</sup>, 6<sup>++</sup> and 1<sup>++</sup>, 3<sup>++</sup>, 4<sup>++</sup>, respectively. One possibility is that the  $3^{++}$  state is in fact lower than the  $1^{++}$  and so gives a common lightest contribution to both lattice states. These higher mass states are difficult to observe cleanly at lower  $\beta$  where ma is unhelpfully large. Indeed this possible degeneracy was not seen by MT at 6.2 or 6.0. Our estimate of  $m_{A^{++}}/\sqrt{\sigma}$  at 6.4 is consistent with the data of ref. [3] at 6.2, and with both our 6.2 and 6.0 data. For the

 $T_1^{++}$  also, we have a reasonable signal at 6.4 unlike at 6.2 where an upper limit only was obtained [3].

According to table 2 we observe reasonably good signals for 10 states of different continuum  $J^{PC}$  contents. These are included as the solid circles in fig. 1. Moreover, we determine upper limits for the masses of the remaining 6 states with J < 4. These are also shown in the figure. With our lattice resolution  $(a^{-1} \approx$ 3.7 GeV) and statistics we are in a position to trace the signals over larger time separations and achieve more stringent upper bounds on masses than previously possible. This improves our capability to separate low lying glueball states and establish the spectrum order. The 2<sup>++</sup> is separated by some 6 standard deviations from the lightest  $(0^{++})$  glueball. Moreover, the  $2^{-+}$  glueball is found to be significantly heavier than the  $0^{-+}$ . Above the  $2^{-+}$ , five further states have been identified but their ordering cannot vet be determined.

Before proceeding with further interpretation of our results, it is useful to convert the continuum predic-

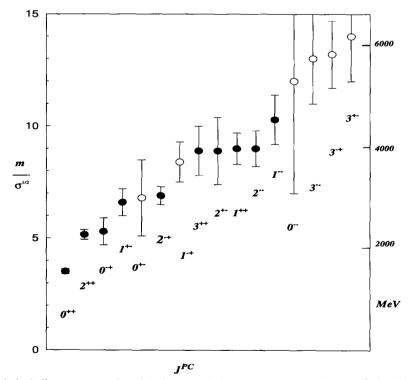


Fig. 1. The measured glueball spectrum at  $\beta = 6.4$ . Open symbols represent measured upper limits. The origin of the MeV scale is described in the text.

tions in the last column of table 2 to an MeV scale. The extra scale displayed in fig. 1 was obtained by multiplying the latter numbers by a string tension value of 440 MeV. Direct comparison with experiment is valid only within the following two assumptions: (a) that the glueball masses are, for some reason, insensitive to light quark mixing where this takes place and (b) that the physical string tension estimate  $(440 \text{MeV})^2$ based on a model for Regge trajectories is reliable for the pure glue sector. Some encouragement for this latter belief is provided by the fact that the scale for light hadron masses set in this way is very reasonable. A recent large scale quenched lattice study of the light meson and baryon spectrum at similar lattice spacings [10] shows excellent agreement with experiment. provided sufficiently small valence quark masses are used for extrapolations. Using the  $\rho$  mass to set the scale at  $\beta = 6.17$  yields  $a^{-1} = 2.63(4)$  GeV which is quite consistent with 2.78(5) GeV [11,12] and

2.72(3) GeV [4] at  $\beta = 6.2$  as obtained from the string tension. Furthermore, values of  $\Lambda_{\overline{MS}}$  deduced from independent studies of the SU(3) heavy quark potential (256±20 MeV [12] and 244±8 MeV [5]) are compatible with the (unquenched) values found in experiment [13].

To set the scale in what follows, we have used string tension values  $\sigma a^2$  extracted from Wilson loops measured on sufficiently large lattices: 0.168(11) at  $\beta = 5.7$  [14], 0.073(1) at  $\beta = 5.9$  [14], 0.0476(7) at  $\beta = 6.0$  [15], 0.0251(8) at  $\beta = 6.2$  [12] and 0.0138(4) at  $\beta = 6.4$  [9]. It is interesting to note that the latter value is in good agreement with the effective string tension deduced from our Polyakov–Wilson line correlator (torelon),

 $\sigma_{\rm eff}a^2 = am_{\rm tor}/L = 0.440(20)/32 = 0.0138(6).(2)$ 

One should remember that the latter is subject to a finite size correction of order  $\pi/3L^2$  [16] which on

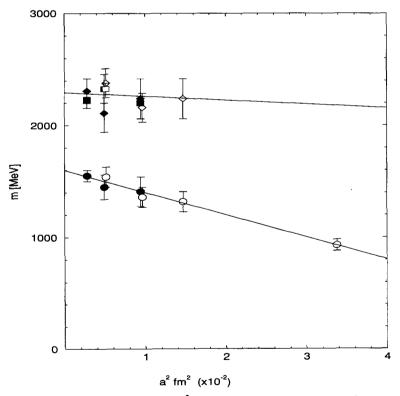


Fig. 2. Scalar and tensor glueball masses as a function of  $a^2$ . Full symbols refer to our data. Open symbols are taken from refs. [3,17]. Circles are  $A_1^{++}$ , diamonds  $E^{++}$ , and squares  $T_2^{++}$ . For clarity data points at the same  $\beta$  values have been separated slightly.

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our size of lattice is small (+0.0010).

In fig. 2, we show a new compilation of scalar and tensor glueball masses, measured at various couplings. Since the lattice corrections to  $ma/\sqrt{\sigma a}$  are expected to be of order  $a^2$ , we display the physical masses as a function of  $a^2$  where physical units on both axes have been set as described above. The present data is displayed with full symbols and previous data with open symbols ( $\beta = 6.2, 6.0, 5.9$  [3],  $\beta = 5.7$  [17]). We are aware that the string tension results have been obtained by slightly different methods but, for present purposes, the ensuing uncertainties are small compared to the statistical errors from the glueball masses. It is clear that, at least for the scalar glueball, there appears to be little room for uncertainty in any reasonable extrapolation to  $a^2 = 0$ . A linear fit is shown as an example. The fitted slope to the scalar glueball data suggests a systematic error of less than 5% in extrapolation from  $\beta = 6.4$ , which would be of the same order as the statistical error. Because of this, we henceforth use the results at  $\beta = 6.4$  as an adequate approximation to the continuum spectrum.

#### 4. Phenomenological considerations

With the above scale ( $\sqrt{\sigma} = 440$  MeV), the scalar glueball mass prediction from our  $\beta = 6.4$  data is

$$m_{0^{++}} = 1550 \pm 50 \,\mathrm{MeV}\,,\tag{3}$$

where the error here is purely statistical. This value is in agreement with previous lattice glueball calculations (e.g. refs. [7,1-3,18]). The status of the G(1560) [19] as a 0<sup>++</sup> glueball candidate has recently been considerably strengthened by its independent observation in  $\bar{p}p \rightarrow 6\gamma$  [20] where a strong coupling to the  $\eta\eta$ , but not to the  $\pi^0\pi^0$  channel, is found. The total width is  $245 \pm 50$  MeV. Clearly, the lattice calculation is guite consistent with this mass. However, the lattice state is not far from the broad  $q\bar{q}$  state  $f_0(1400)$  observed predominantly in  $\pi\pi$  but which also couples to  $\eta\eta$  (and  $\gamma\gamma$ ). Because of the influence of the  $f_0(975)$  and the  $K\bar{K}$  channel to which they both couple, the width (a few hundred MeV) and indeed the very nature of the  $f_0(1400)$  is difficult to establish. It seems not unlikely that this pure glue state will suffer mixing and be part of a

complex system involving the above states. Future lattice studies of light quark mixing will be very illuminating on this point. Pioneering attempts to study this [21,22] are hampered by the unphysically large quark masses currently accessible and the difficulty in acquiring sufficient statistics.

The above energy scale estimate puts the tensor glueball at

$$m_{2++} = 2270 \pm 100 \,\mathrm{MeV}\,.$$
 (4)

So far, only one experiment has provided evidence of a  $2^{++}$  glueball candidate in this mass range [23]. A series of three  $\phi\phi$  states in the range 2010 to 2340 MeV with widths of 150 to 300 MeV have been seen but not yet independently confirmed. The next predicted glueball state, a pseudoscalar at around the same mass (table 2), has no suitable experimental candidates currently. The search becomes increasingly difficult at high masses where many states overlap and many channels are competing.

As pointed out previously (e.g. ref. [3]), the prediction of low-lying exotic states (i.e. non  $q\bar{q}$  quark model states) would have interesting theoretical and phenomenological consequences. Michael [24] has recently reviewed the lattice and experimental evidence for glueball and hybrid states with these quantum numbers. Our results (table 2) confirm earlier predictions that no exotic glueball states are expected below about 3 GeV. On the lattice, each O<sub>h</sub> representation corresponding to an exotic  $J^{PC}$ : 0<sup>--</sup>, 0<sup>+-</sup>,  $1^{-+}$  etc. can also receive contributions from higher, but non-exotic,  $J^{PC}$  so identification is unlikely to be straightforward in the absence of very precise data. The strongest exotic signal we have observed is in the  $T_2^{+-}$  channel. There is also some evidence of a signal in the  $E^{+-}$  channel. These could correspond to a  $2^{+-}$ exotic glueball at around 3.9  $\pm$  0.7 GeV. However, the lowest non-exotic  $J^{PC}$  contributing to the  $T_2^{+-}$ would be  $3^{+-}$  ( $5^{+-}$  for the  $E^{+-}$ ) and so no strong conclusion may be drawn. The  $A_1^{+-}$  and  $T_1^{-+}$  channels also show some sort of signal. These do not satisfy the above criteria for plateau identification and so we only quote these as upper limits. Experimental confirmation of exotic states in the above mass range is likely to be very difficult.

In conclusion, we have demonstrated that at  $\beta = 6.4$  we are effectively at the continuum limit for the

quenched glueball spectrum below 3 GeV. To be specific, we observe clear signals for 10 different continuum states. Thus the ordering of the underlying spectrum is becoming established. Further improved studies of lattice glueballs are both practicable and desirable. In the near future, machines capable of sustaining 50 to 100 Gflops on QCD will allow a factor of  $\sqrt{50}$  or so reduction in statistical errors and hence greatly improved effective mass signals. The present work represents a reduction in lattice spacing by 25% and an increase in physical volume by 70% over previous studies. Our results show that there is no need to use larger lattices or smaller lattice spacings to probe the mass range which is likely to be of most experimental relevance i.e. below 3 GeV. However, higher mass states will require larger statistics and lattice spacings such that ma < 1. In order to estimate the possible influence of mixing effects due to light quarks it will be vital to have increased precision of meson and glueball masses in quenched QCD. This is almost within our grasp.

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