EFFECT OF A DARK MATTER HALO ON THE DETERMINATION OF BLACK HOLE MASSES

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ABSTRACT

Stellar dynamical modeling is a powerful method to determine the mass of black holes in quiescent galaxies. However, in previous work the presence of a dark matter halo has been ignored in the modeling. Gebhardt & Thomas in 2009 showed that accounting for a dark matter halo increased the black hole mass of the massive galaxy M87 by a factor of two. We used a sample of 12 galaxies to investigate the effect of accounting for a dark matter halo in the dynamical modeling in more detail, and also updated the masses using improved modeling. The sample of galaxies possesses $Hubble\ Space\ Telescope$ and ground-based observations of stellar kinematics. Their black hole masses have been presented before, but without including a dark matter halo in the models. Without a dark halo, we find a mean increase in the estimated mass of 1.5 for the whole sample compared to previous results. We attribute this change to using a more complete orbit library. When we include a dark matter halo, along with the updated models, we find an additional increase in black hole mass by a factor of 1.2 in the mean, much less than for M87. We attribute the smaller discrepancy in black hole mass to using data that better resolve the black hole's sphere of influence. We redetermined the M_{\bullet} - σ_{*} and M_{\bullet} - L_{V} relationships using our updated black hole masses and found a slight increase in both normalization and intrinsic scatter.

Key words: black hole physics – galaxies: general – galaxies: kinematics and dynamics – galaxies: nuclei *Online-only material:* color figures

1. INTRODUCTION

It is now well established that almost every massive galaxy harbors a supermassive black hole in its center. Furthermore, close relations between the mass of this supermassive black hole and the properties of the galaxy's spheroid component have been found, namely with the mass (Magorrian et al. 1998; Häring & Rix 2004), luminosity (Kormendy & Richstone 1995; Kormendy & Gebhardt 2001; Marconi & Hunt 2003; Gültekin et al. 2009b), and with the velocity dispersion (Gebhardt et al. 2000a; Ferrarese & Merritt 2000; Tremaine et al. 2002; Gültekin et al. 2009b). These relations imply a link between the growth of black holes and galaxy evolution, usually attributed to active galactic nucleus (AGN) feedback (e.g., Silk & Rees 1998; Di Matteo et al. 2005; Springel et al. 2005; Ciotti & Ostriker 2007), but at least to some degree they are a natural result within a merger-driven galaxy evolution framework (Peng 2007; Hirschmann et al. 2010; Jahnke & Maccio 2010). In general, the black hole-bulge relations and especially their evolution with cosmic time are able to provide deep insight into galaxy formation and black hole growth. Therefore, it is essential to properly establish the local relationships as precisely as possible.

The black hole-bulge relations are based on a sample of \sim 50 quiescent black holes, whose masses have been determined based on maser emission (e.g., Greenhill et al. 2003; Herrnstein et al. 2005; Kuo et al. 2010), gas kinematics (e.g., Ferrarese et al. 1996; Marconi et al. 2001; Dalla Bontà et al. 2009), and stellar kinematics (e.g., van der Marel et al. 1998; Gebhardt et al. 2000b; Shapiro et al. 2006; Gebhardt et al. 2007; Gültekin et al. 2009a). In particular, stellar dynamical modeling using orbit superposition is a powerful method to estimate black hole masses in quiescent galaxies, and also recovers the orbital structure within the galaxy. Usually, axisymmetry is assumed in these models. However, there are still uncertainties and possibly systematic biases within these methods. Uncertainties may arise

from the deprojection of the observables onto three dimensions as the true inclination of the galaxy often is not well known, the presence of dust, some triaxiality that cannot be modeled properly with axisymmetric models (van den Bosch & de Zeeuw 2010), or the presence of an AGN at the center. So far, in most models the contribution of the galaxy's dark matter (DM) halo has been neglected. Gebhardt & Thomas (2009) recently showed that the black hole mass can be underestimated in this case. For the massive galaxy M87 they found an increase of more than a factor of two in the measured black hole mass, just by including a DM halo in the modeling. The reason is that without a DM halo the mass-to-light ratio is overestimated in order to account for the mass in the outer parts of the galaxy. Under the usually applied assumption of a constant mass-to-light ratio for the whole galaxy, this will propagate inward and lead to an underestimation of the black hole mass at the center due to overestimation of the stellar contribution.

A similar result has been obtained by McConnell et al. (2010). They measured the black hole mass in the brightest cluster galaxy NGC 6086. They report a factor of six difference between the black hole mass obtained from models without a DM halo and their most massive DM halo models. However, the black hole's sphere of influence is barely resolved in their work.

Shen & Gebhardt (2010) found for NGC 4649, also a massive galaxy, no change in the black hole mass by including a DM halo. In this case the sphere of influence is well resolved by the data. A larger sample, especially spanning a larger range in mass, is clearly required.

Gebhardt et al. (2003; hereafter G03) studied a sample of 12 galaxies with kinematics derived from *Hubble Space Telescope* (*HST*) and ground-based observations, using axisymmetric orbit superposition models. They do not include a DM halo in their modeling. Since then the orbit superposition code used by our group has been improved (Thomas et al. 2004, 2005; Siopis et al. 2009) by including a more complete orbit sampling.

The aim of this paper is to reanalyze the data set presented by G03, using the most up-to-date dynamical modeling code and investigating the effect of accounting for the DM contribution on the derived black hole masses. One of the galaxies in the G03 sample, NGC 4649, was recently analyzed by Shen & Gebhardt (2010), including a DM halo. We have reanalyzed this galaxy for consistency with the remaining sample, but find consistent results with this previous investigation.

2. DATA

The data set used in this work is identical to those used in the work of G03. Thus, we will only give a brief summary and refer to G03 for more detail. The data consist of three sets of observations for each galaxy: imaging, *HST* stellar kinematics, and ground-based stellar kinematics.

High-resolution imaging is required to obtain the stellar surface brightness profile for each galaxy. This imaging has been obtained in the V band with the HST WFPC2 (Lauer et al. 2005), except for NGC 4697, which was observed with the HST WFPC1 (Lauer et al. 1995). Surface brightness profiles were measured from the point-spread function deconvolved images and were augmented with ground-based imaging at the outer parts, not covered by HST. For the deprojection of the surface brightness profile to a luminosity density profile, we assume axisymmetry, an inclination angle of 90° , which we refer to as edge-on, and used the technique outlined in Gebhardt et al. (1996).

The *HST* observations and kinematics are presented by Pinkney et al. (2003) and G03. They consist of Space Telescope Imaging Spectrograph (STIS) long-slit spectra along the major axes, except for NGC 3377 and NGC 5845, which have Faint Object Spectrograph (FOS) aperture spectra. The spectra cover the Ca II triplet around 8500 Å. For the dynamical modeling, the line-of-sight velocity distributions (LOSVDs), extracted from the spectra, are used. The LOSVDs are given in a non-parametric form, binned into 15 equidistant bins, compared to 13 bins in G03.

The ground-based kinematics are presented by Pinkney et al. (2003) and G03 as well. They consist of long-slit spectra along several position angles, mainly obtained at the MDM observatory. They also cover the Ca II triplet, or alternatively the Mgb absorption at 5175 Å. The individual LOSVDs are binned into 15 points as well.

3. DYNAMICAL MODELS

The dynamical modeling uses the orbit superposition method, first proposed by Schwarzschild (1979). This general method has been widely used by various groups (Rix et al. 1997; van der Marel et al. 1998; Cretton et al. 1999; Valluri et al. 2004). Our technique is described in detail in G03, Thomas et al. (2004, 2005), and Siopis et al. (2009). We will give a brief summary here and especially point out the differences compared to the work of G03. The basic approach consists of the following steps: (1) deprojection of the surface brightness profile to a three-dimensional luminosity distribution, (2) computation of the specified gravitational potential, (3) generation of a representative orbit library in this potential, (4) fitting the orbit library to the observed light distribution and kinematics, and (5) modifying the input potential to find the best match to the data, based on a χ^2 analysis.

As described in Section 2, we deproject the surface brightness profile following Gebhardt et al. (1996) and assume an edge-on

configuration, as used by G03. The only exception is NCG 4473, where we assume an inclination of 72° , as has been done in G03. To determine the potential, we assume a constant mass-to-light ratio throughout the galaxy, a specific black hole mass and optionally also include a DM halo. The mass distribution is then given by

$$\rho(r,\theta) = M_{\bullet}\delta(r) + \Upsilon \nu(r,\theta) + \rho_{\rm DM}(r), \tag{1}$$

where M_{\bullet} is the black hole mass, Υ is the mass-to-light ratio, ν is the stellar luminosity distribution, and $\rho_{\rm DM}$ is the DM density profile. The potential $\Phi(r,\theta)$ is derived by integrating Poisson's equation.

In this potential, a representative orbit library is constructed that samples the phase space systematically. The generation of the orbit library is described in detail in Thomas et al. (2004) and Siopis et al. (2009). For comparison with the data, we use a spatial grid of $N_r = 20$ radial bins and $N_\theta = 5$ angular bins and use $N_v = 15$ velocity bins for the LOSVD at each spatial gridpoint. The galaxy potential and the forces are evaluated on a grid with 16 times finer resolution. For our axisymmetric code, there are three integrals of motion that sample the phase space accordingly: the energy E, the angular momentum L_z , and a non-classical third integral I_3 . The (E, L_z) -plane is sampled based on the spatial binning (Richstone & Tremaine 1988). We choose E and L_z such that the respective orbits have their pericenter and apocenter in every pair of the radial grid bins. The third integral I_3 is sampled as outlined by Thomas et al. (2004). First, orbits are dropped from the zero-velocity curve (defined by $E = L_z^2/(2r^2\cos^2\theta) + \Phi(r,\theta)$), as in G03. This is done by using the intersections of the angular rays of the spatial grid with the zero-velocity curve as starting points for the integration of the orbit's motion. However, this does not ensure a representative sampling of orbits. Such a sampling is indicated by a homogeneous coverage of the surface of section, i.e., the position of radii and radial velocities of orbits during their upward crossing of the equatorial plane. Therefore, additional orbits are launched to give such a homogeneous coverage. This method provides a complete sampling of the surface of section for given E and L_z and thus a proper coverage of phase space. We typically have 13,000–16,000 orbits in our library. The allocation of the individual orbits to the spatial grid points is based on the time they spend there.

Given this orbit library, the orbit weights are chosen by matching the orbit superposition to the observed light distribution and the LOSVDs of the galaxy on the spatial grid. To fit the orbit library to the data, we use the maximum entropy technique of Richstone & Tremaine (1988). This method maximizes the function

$$\hat{S} = S - \alpha \chi^2,\tag{2}$$

where χ^2 is the sum of the squared residuals over all spatial and velocity bins, e.g.,

$$\chi^2 = \sum_{k=1}^{N_d} \frac{(l_{\text{mod},k} - l_{\text{dat},k})^2}{\sigma_k^2},\tag{3}$$

where l_k is the light in the kth bin, with the bins composed of the spatial position on the sky and the line-of-sight velocity, thus the bin in the LOSVD, at that position. Hence, k is varying from 1 to $N_d = N_r N_\theta N_v$. While $l_{\text{dat},k}$ refers to the measured light at that position, $l_{\text{mod},k}$ is given by the weighted sum of the contribution of all orbits to the kth bin.

Table 1
Results for the Galaxy Sample

Galaxy (1)	D (Mpc) (2)	$M_{\bullet, \text{G03}}(M_{\odot})$ (3)	M/L_{G03} (4)	$M_{\bullet, \text{noDM}}(M_{\odot})$ (5)	M/L_{noDM} (6)	$M_{\bullet,\mathrm{DM}}(M_{\odot})$ (7)	$M/L_{\rm DM}$ (8)	$V_c (\text{km s}^{-1})$ (9)	r _c (kpc) (10)	R _{inf} (") (11)
NGC 821	25.5	$9.9 \pm 4.1 \times 10^7$	6.8	$1.1 \pm 0.4 \times 10^8$	7.7 ± 0.5	$1.8 \pm 0.8 \times 10^8$	6.2 ± 0.7	450	14.0	0.14
NGC 2778	24.2	$1.6 \pm 1.0 \times 10^7$	7.2	$1.4 \pm 1.1 \times 10^7$	11.9 ± 1.1	$1.5 \pm 1.5 \times 10^7$	11.8 ± 1.2	300	5.0	0.02
NGC 3377	11.7	$1.1 \pm 0.6 \times 10^8$	2.7	$1.6 \pm 1.0 \times 10^{8}$	2.6 ± 0.5	$1.9 \pm 1.0 \times 10^{8}$	2.3 ± 0.4	350	6.0	0.69
NGC 3384	11.7	$1.8 \pm 0.2 \times 10^7$	2.5	$8.0 \pm 4.2 \times 10^6$	2.4 ± 0.1	$1.1 \pm 0.5 \times 10^7$	2.2 ± 0.1	400	8.0	0.04
NGC 3608	23.0	$1.9 \pm 0.9 \times 10^{8}$	3.7	$4.6 \pm 0.9 \times 10^{8}$	3.5 ± 0.3	$4.7 \pm 1.0 \times 10^{8}$	3.3 ± 0.3	400	10.0	0.55
NGC 4291	25.0	$3.2 \pm 1.6 \times 10^8$	6.0	$9.7 \pm 2.0 \times 10^{8}$	6.0 ± 0.5	$9.2 \pm 2.9 \times 10^8$	6.0 ± 0.8	400	8.5	0.56
NGC 4473	17.0	$1.3 \pm 0.7 \times 10^8$	5.1	$5.9 \pm 5.0 \times 10^7$	7.4 ± 0.2	$1.0 \pm 0.5 \times 10^8$	6.8 ± 0.3	400	10.0	0.15
NGC 4564	17.0	$6.9 \pm 0.7 \times 10^7$	1.6	$9.8 \pm 2.3 \times 10^7$	1.6 ± 0.1	$9.4 \pm 2.6 \times 10^7$	1.5 ± 0.1	350	7.0	0.19
NGC 4649	16.5	$2.1 \pm 0.6 \times 10^9$	8.8	$3.9 \pm 1.0 \times 10^9$	8.6 ± 0.6	$4.2 \pm 1.0 \times 10^9$	8.0 ± 0.7	500	20.0	1.51
NGC 4697	12.4	$2.0 \pm 0.2 \times 10^8$	4.2	$2.2 \pm 0.3 \times 10^8$	4.5 ± 0.3	$2.0 \pm 0.5 \times 10^8$	4.3 ± 0.3	450	12.0	0.45
NGC 5845	28.7	$2.9 \pm 1.1 \times 10^8$	4.5	$4.5 \pm 1.2 \times 10^8$	5.4 ± 0.2	$5.4 \pm 1.7 \times 10^8$	5.1 ± 0.2	300	5.0	0.30
NGC 7457	14.0	$4.1\pm1.4\times10^6$	2.8	$7.4 \pm 4.2 \times 10^6$	2.7 ± 0.5	$1.0\pm0.6\times10^7$	2.6 ± 0.5	300	5.0	0.14

Notes. Column 1: name. Column 2: distance. Columns 3–4: black hole mass and mass-to-light ratio from study of Gebhardt et al. (2003). Columns 5–6: black hole mass and mass-to-light ratio using updated code but without including a DM halo in the dynamical modeling. Columns 7–8: black hole mass and mass-to-light ratio when a DM halo is included. Columns 9–10: parameters of the circular velocity and the core radius for the logarithmic DM density profile used. Column 11: radius of the black hole's sphere of influence, based on the black hole mass including the contribution of DM.

S is the Boltzmann entropy

$$S = \sum_{i=1}^{N_{\text{orb}}} w_i \log \left(\frac{w_i}{V_i} \right), \tag{4}$$

where w_i is the weight of the individual orbit and V_i is the phase space volume of this orbit, i.e., the volume of the region in phase space that is represented by this orbit i, given by

$$V = \Delta E \Delta L_z \int T(r, v_r) dr dv_r , \qquad (5)$$

where $T(r, v_r)$ is the time between two successive crossings of the equatorial plane, and ΔE and ΔL_z are the ranges in energies and angular momenta of the respective orbits (Binney et al. 1985; Thomas et al. 2004).

The parameter α in Equation (2) controls the relative weight of entropy and χ^2 for the maximization. We start with a small α , being dominated by the entropy maximization in the fit, and then iteratively increase it until there is no longer an improvement in the χ^2 .

This procedure provides a value for the χ^2 for one combination of M_{\bullet} , Υ , and DM halo. The best fit is found by the global minimum of χ^2 for the variation of these parameters. For the estimation of the parameter uncertainties, we adopt the usual $\Delta\chi^2=1$ criterion (Press et al. 1992) to obtain the 68% confidence intervals for one degree of freedom, thus when marginalizing over the other free parameters.

4. RESULTS

4.1. Models without a Dark Matter Halo

We first ran a set of models without including the contribution of a DM halo; thus, we set $\rho_{DM}=0$ in Equation (1). This assumption is consistent with most previous studies on black hole masses using dynamical models as well as with G03. As we are using the same data as those of G03, the main difference is the improved modeling code. Thus, we would expect to recover similar black hole masses as in G03. We also use slightly different distances to the galaxies, as given by Gültekin et al. (2009b).

For each galaxy we ran models on a fine grid in M_{\bullet} and mass-to-light ratio (M/L). Each model gives a best-fitting orbit superposition, and thus orbital structure for the galaxy, with a corresponding value of χ^2 . The best fits M_{\bullet} and M/L are determined by the global minimum of the χ^2 distribution.

The χ^2 distribution as a function of M_{\bullet} (marginalized over M/L) is shown as the blue line in Figure 1. We determined our stated best fits M_{\bullet} and M/L from their marginalized χ^2 distributions, using the mid-point of the $\Delta\chi^2=1$ interval, which corresponds to a 1σ uncertainty. The results are presented in Table 1.

4.2. Models with a Dark Matter Halo

It has been shown that dynamical models are clearly able to detect and constrain the presence of a DM halo, if the data range sufficiently far in radius (Rix et al. 1997; Kronawitter et al. 2000; Thomas et al. 2007; Weijmans et al. 2009; Forestell & Gebhardt 2010). Due to the faintness of the stellar component at large radii, other kinematic tracers such as globular clusters (Zepf et al. 2000; Pierce et al. 2006; Bridges et al. 2006) or planetary nebulae (Méndez et al. 2001; Romanowsky et al. 2003; Coccato et al. 2009) have to be used. Furthermore, if dynamical coverage of both the central and the outer regions of the galaxy is present, it is possible to constrain M_{\bullet} , M/L, and the dark halo parameters by dynamical modeling (Gebhardt & Thomas 2009; Shen & Gebhardt 2010).

Two common parameterizations for the DM halo are a Navarro–Frenk–White (NFW) profile (Navarro et al. 1996) and a DM distribution based on a cored logarithmic potential (Binney & Tremaine 1987; Thomas et al. 2005). For a sample of 17 early-type galaxies, Thomas et al. (2007) found both profiles to give consistent results, with tentative evidence to favor a logarithmic dark halo. Gebhardt & Thomas (2009) confirmed this result for M87, and McConnell et al. (2010) found consistent results for M_{\bullet} using either a logarithmic dark halo or an NFW profile. In the following, we will use a dark matter halo with a cored logarithmic potential, whose density profile is given by

$$\rho_{\rm DM}(r) = \frac{V_c^2}{4\pi G} \frac{3r_c^2 + r^2}{\left(r_c^2 + r^2\right)^2},$$
 (6)

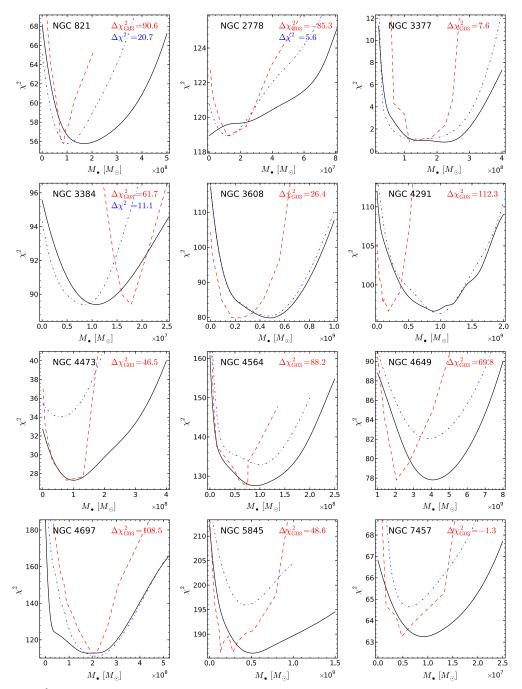


Figure 1. Comparison of the χ^2 distributions as a function of M_{\bullet} (marginalized over M/L). The black solid line shows the models including a DM halo. Their χ^2 values always show the actual modeling result. The χ^2 distribution for the models without a DM halo is shown as the blue dashed-dotted line. The zero point has been shifted for NGC 2778 and NGC 3384 by an offset given in the figure as $\Delta\chi^2$ (in blue). The χ^2 distribution of G03 is shown as the red dashed line, offset by the value given as $\Delta\chi^2_{G03}$ (in red). The distributions have been scaled in M_{\bullet} , to account for the difference in the assumed distance. (A color version of this figure is available in the online journal.)

where V_c is the asymptotically constant circular velocity and r_c is the core radius, within which the DM density is approximately constant.

Our data in general do not constrain the DM profile, as we are lacking kinematic information at large radii. While for a few galaxies in our sample large radii kinematic information for the stars, globular clusters, or planetary nebulae exist in the literature, we do not include them in this analysis. In this work, we are not aiming at constraining the DM halo itself, but we are mainly interested in the effect of including such a halo for the recovered black hole mass. We leave a more

detailed investigation of the combined DM halo and black hole properties for these individual galaxies to future work. This also allows better direct comparison to the work of G03 and the models without a DM halo, presented in the previous section.

Therefore, we assume a fixed DM halo, with fixed parameters V_c and r_c . These are taken from the scaling relations presented by Thomas et al. (2009), based on the galaxy luminosity:

$$\log r_c = 1.54 + 0.63(\log(L_B/L_{\odot}) - 11) \tag{7}$$

$$\log V_c = 2.78 + 0.21(\log(L_B/L_\odot) - 11), \tag{8}$$

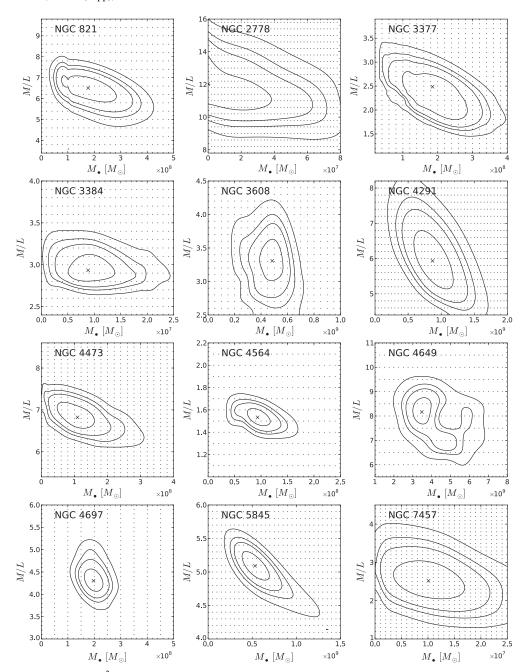


Figure 2. Two-dimensional contour plot of χ^2 as a function of M_{\bullet} and M/L for each galaxy. Here, the models with a DM halo included are shown. The contour lines show $\Delta\chi^2$ values of 1.0, 2.71, 4.0, and 6.63 (corresponding to 68%, 90%, 95%, and 99% confidence for one degree of freedom). The points indicate the individual models we ran. The contours are derived from a smoothing spline to these models. The cross represents the best fit.

and given in Table 1. These scaling relations have been established based on a sample of 12 early-type galaxies in the Coma cluster with old stellar populations. While our sample does not have to follow these scaling relationships exactly, they at least provide well-motivated parameters for the DM halo. Younger early-type galaxies and disk galaxies have been found to have on average a less massive halo; thus, our approach tends to maximize the DM contribution. We investigate the effect of changing the assumed DM halo on the central black hole mass further below.

Thus, for each galaxy, we ran a grid of models for varying M_{\bullet} and M/L with fixed DM halo. We show the two-dimensional distribution of χ^2 as a function of M_{\bullet} and M/L in Figure 2. The contours are based on the χ^2 values of the underlying grid points, applying a two-dimensional smoothing spline (Dierckx 1993).

The marginalized χ^2 distribution as a function of M_{\bullet} is shown as the black line in Figure 1. We again determined the best-fit values for M_{\bullet} and M/L from the marginalized distribution and have given them in Table 1.

5. COMPARISON OF BLACK HOLE MASSES

5.1. Comparison with Gebhardt et al. (2003)

As we are using the same data as those in G03, the only difference between the work presented in Section 4.1 and in G03 is the improved modeling code. Thus, we would expect to recover the same black hole masses as in G03.

For a comparison with G03, their masses are first increased by a factor of 1.09, due to a unit conversion error (Siopis et al. 2009), and then are rescaled, according to the difference in

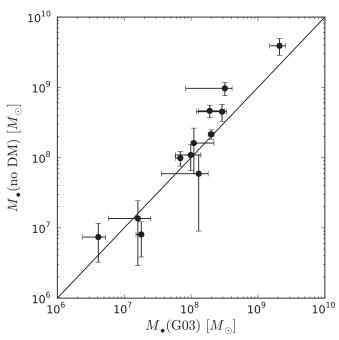


Figure 3. Black hole masses given by Gebhardt et al. (2003) vs. the black hole masses determined in this work (without a dark halo). The solid line shows a one-to-one correspondence.

the adopted distance, assuming $M_{\bullet} \propto d$. These masses are listed in Gültekin et al. (2009b), apart from NGC 821. This galaxy has an erroneous black hole mass in G03, corrected in Richstone et al. (2004). After accounting for the factor of 1.09 and the distance difference, the black hole mass for NGC 821 is $M_{\bullet} = 9.9 \times 10^7 \, M_{\odot}$.

In Figure 3, we compare the black hole masses, determined without including a DM halo, with the black hole masses given in G03. In Figure 4, we show as blue squares the ratio between both mass determinations as a function of the G03 mass. The marginalized χ^2 distributions for the individual objects are shown in Figure 1, as blue dashed-dotted lines for the current work masses and as red dashed lines for the G03 distributions. Note that the G03 distributions are offset in χ^2 , such that the minimum corresponds to the minimum of the χ^2 distribution including a dark halo, shown in black. The reason for the offset in χ^2 is mainly due to the larger number of orbits used in the current modeling, compared to G03.

For three objects (NGC 821, NGC 2778, and NGC 4697) the difference in M_{\bullet} is less than 20%, thus consistent with our previous work. The internal structures of the dynamical models (as discussed below) are similar for these three galaxies in the old and new models, which explains the reason for the lack of change. The small difference is probably due to the presence of numerical noise in the models. This noise is mainly caused by the use of a finite number of individual orbits instead of a smooth orbit distribution function. The comparison of the χ^2 distribution for the three objects shows that they are basically consistent, while the distribution may widen, possibly due to a more complete orbit library. Also, for NGC 3377 and NGC 4564, the difference in M_{\bullet} is within the stated uncertainties.

However, for the rest of the objects the new M_{\bullet} is significantly offset from the previous estimate, and not simply explained by numerical noise. For two objects, NGC 3384 and NGC 4473, M_{\bullet} decreases; for the rest there is an increase in M_{\bullet} , by up to a factor of three. The mean increase for this sample is a factor of 1.46

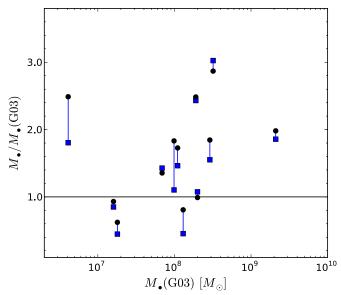


Figure 4. Ratio between the M_{\bullet} determined in this work and the M_{\bullet} given in Gebhardt et al. (2003), as a function of the G03 M_{\bullet} . The blue squares are for the models without a dark halo, while the black circles correspond to the result, when a dark halo is included in the models. The solid line is a one-to-one correspondence to the G03 values.

(A color version of this figure is available in the online journal.)

with the standard deviation of 0.73. This result is in line with the findings of Shen & Gebhardt (2010), who found an increase in the mass by a factor of two for NGC 4649. This object is included in Figures 3 and 4 as the highest mass point. Shen & Gebhardt (2010) attribute the mass difference to the better orbit sampling in the new models. In particular, they argue that the old orbit sampling lacks high energy, nearly circular orbits, which lead to an underestimate of M_{\bullet} . NGC 4649 is a core galaxy, and it is important to note that all galaxies with an increase in mass by more than a factor of two are core galaxies as well. This seems to indicate that the previous orbit sampling was not able to properly model core galaxies.

To investigate this issue further for our whole sample, we inspect the internal orbit structure, looking for any clear difference between the models. To do so, we examine the shape of the velocity dispersion tensor, represented by the ratio of radial to tangential dispersion σ_r/σ_t . The tangential dispersion includes contributions from random as well as from ordered motion; thus, it is given by $\sigma_t^2 = \sigma_\theta^2 + \sigma_\phi^2 + V_\phi^2$. In Figure 5, we compare the internal dispersion ratio σ_r/σ_t for the best-fit models presented here, with and without a DM halo (as blue solid and black dashed-dotted lines, respectively), with the ratio for the models in G03, shown as red dashed lines. We also indicate the black hole sphere of influence $R_{\text{inf}} = GM_{\bullet}\sigma^{-2}$, assuming the new M_{\bullet} (without a DM halo). The galaxies with consistent black hole masses, such as NGC 3377 and NGC 4697, also exhibit consistent internal structure. On the other hand, the galaxies with the largest mass increase, especially the core galaxies such as NGC 4291 and NGC 3608 show a clear difference in the internal structure. First, there is a strong radial bias at large radii for these galaxies, especially compared to the previous dispersion ratio. However, this radial bias is mainly outside the range for which kinematic data are available and is therefore driven by the maximization of the entropy. We do not expect these orbits to have an influence on the black hole mass determination. Second, there is a stronger tangential bias inside

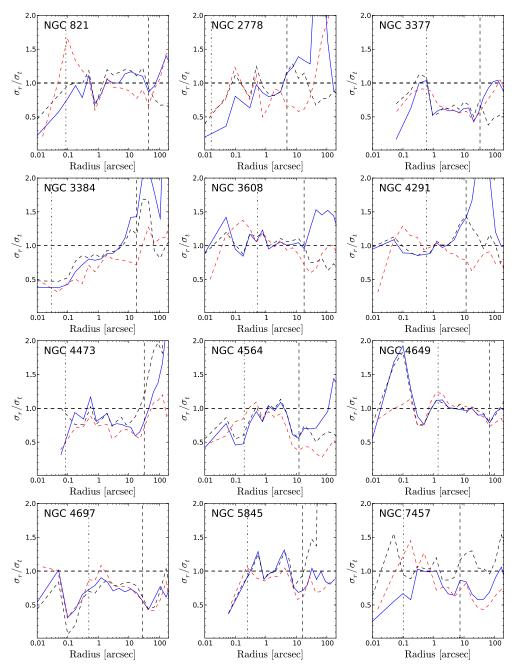


Figure 5. Ratio of the internal velocity dispersions as a function of radius for the best model of each galaxy. Shown is the ratio σ_r/σ_t along the major axis. The result with a DM halo, without a DM halo, and the result of Gebhardt et al. (2003; without a dark halo) are shown as the black dashed, blue solid, and red dashed lines, respectively. The horizontal dashed line corresponds to a non-rotating isotropic model. The vertical dashed-dotted line indicates the black hole's sphere of influence, assuming the black hole mass, determined without including a DM halo. The vertical dashed lines show the radial extent of the ground-based data. (A color version of this figure is available in the online journal.)

the black hole sphere of influence. In particular, the previous models exhibit a radial bias within $R_{\rm inf}$ for the largest outliers. G03 only sampled the zero-velocity curve, instead of the whole phase space, and due to the coarse sampling of drop points, they missed the orbits near the pole that are nearly circular. This sampling then causes a radial orbital bias. This radial bias is removed in the models presented here, using a better orbit sampling. An increase in tangential orbits will reduce the projected line-of-sight velocity dispersion, and therefore a more massive black hole is required to match the observed velocity dispersion profile. On the other hand, NGC 4473, which shows a decrease in the determined black hole mass, exhibits a stronger

radial bias in the new modeling compared to G03. This radial bias is probably caused by the presence of a nuclear disk in this galaxy.

Thus, we find that the main reason for the change in black hole mass is the different orbit sampling used, as already found by Shen & Gebhardt (2010) for NGC 4649. We now cover the phase space more completely and therefore also include orbits missed by the previous sampling. This issue is of special importance for core galaxies, as they often show a significant tangential orbital bias in their center, i.e., they usually have the largest σ_t (G03).

To illustrate this point, we computed the difference of the dispersion ratio between G03 and this new model in a shell

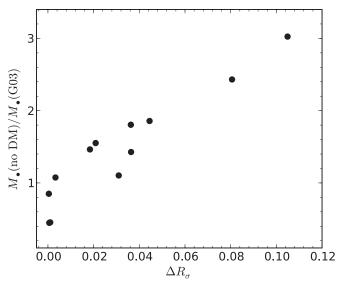


Figure 6. Ratio between the M_{\bullet} determined in this work and the M_{\bullet} given in Gebhardt et al. (2003), as a function of the excess in radial motion in the internal structure of the models of Gebhardt et al. (2003), as defined by Equation (9). A correlation between both quantities is apparent.

inside the black hole sphere of influence:

$$\Delta R_{\sigma} = \int_{r_{\text{min}}}^{r_{\text{max}}} \left[(\sigma_r / \sigma_t)_{\text{G03}} - (\sigma_r / \sigma_t) \right] dr, \tag{9}$$

with $r_{\rm min}=0.1R_{\rm inf}$ and $r_{\rm max}=R_{\rm inf}$. This quantity is just a simple and quick way of quantifying the change in the orbital structure and is just meant to highlight the relation between the change in orbital structure and the change in black hole mass. In Figure 6 we plot it against the ratio of the black hole masses $M_{\bullet}/M_{\bullet,G03}$. There is a clear correlation between the quantities, confirming our previous argument. We have also tested the effect of decreasing the number of orbits in the modeling, but saw no clear influence on the best-fit black hole mass. Thus, we confirm our previous results in finding that the recovered black hole mass is not affected by the number of orbits (Gebhardt 2004; Richstone et al. 2004; Shen & Gebhardt 2010).

This investigation emphasizes the need for a complete orbital sampling of phase space for dynamical modeling of galaxies, especially of core galaxies.

5.2. Effect of a Dark Matter Halo on the Determined Black Hole Mass

The main motivation of this paper is to investigate the effect of the inclusion of a DM halo in the dynamical modeling on the determined black hole mass. In Figure 7, we show the difference in black hole masses between the models with and without the inclusion of a DM halo as a function of the resolution of the black hole sphere of influence divided by the spatial resolution of the kinematic observation ($R_{\rm inf}/d_{\rm res}$). For the computation of $R_{\rm inf}$, we used the black hole mass including a DM halo (given in Table 1). The spatial resolution is given by the seeing and the aperture of the *HST* kinematic observations; thus, $d_{\rm res}=0.08$ for the STIS data and $d_{\rm res}=0.15$ for the FOS data.

As expected, there is a general trend of an increase in M_{\bullet} when a DM halo is included. For five objects, we find almost no change in M_{\bullet} , while for one object—NGC 2778—the significance of the black hole detection even vanishes, with the minimum χ^2

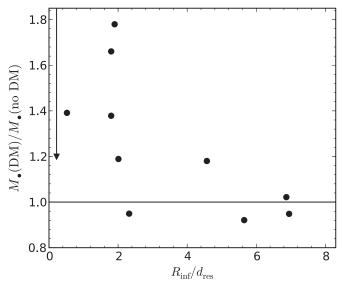


Figure 7. Ratio between the M_{\bullet} without accounting for the DM halo and the M_{\bullet} including a DM halo in the model, as a function of the ratio of black hole sphere of influence over the spatial resolution. The arrow indicates the upper limit for the mass of NGC 2778 when DM is included. The solid line shows a one-to-one correspondence between both masses.

for no black hole. The other six galaxies show an increase in the measured M_{\bullet} between 20% and 80% when a DM halo is included. The most extreme case is NGC 4473, probably due to the presence of a nuclear disk, with an increase of a factor of 1.8 when a DM halo is included. For the whole sample we find a mean increase of a factor of 1.22 with standard variation of 0.27. This increase is much less than the factor of more than two found for M87. In contrast to M87, our data set contains no stellar kinematic information at large radii but includes HST data at small radii. Thus, we are better able to probe the region affected by the presence of the black hole at the center.

In Figure 7, there appears to be a trend of a larger bias for objects where $R_{\rm inf}$ is less well resolved, as would be expected. However, due to the black hole mass uncertainties there is no statistically significant relation. The most massive galaxy in our sample, NGC 4649, is not shown in the figure, as it would appear at $R_{\rm inf}/d_{\rm res}\approx 20$ with no significant change in black hole mass. M87 would lie at $R_{\rm inf}/d_{\rm res}\approx 1.5$ and $M_{\bullet,{\rm DM}}/M_{\bullet,{\rm no\,DM}}\approx 2.8$. In contrast to M87, the galaxies in our sample with a less well resolved sphere of influence exhibiting a smaller change in the determined M_{\bullet} are less massive and probably reside in less massive DM halos. This indicates that especially for massive galaxies properly resolving $R_{\rm inf}$ is important to determine M_{\bullet} under the consideration of DM.

In Figure 1, the marginalized χ^2 distributions for the individual objects with (solid black line) and without (dotted-dashed blue line) a DM halo are shown. For the five objects with almost no change in M_{\bullet} (NGC 3377, NGC 3608, NGC 4291, NGC 4649, and NGC 4697), there is also no change in the χ^2 (apart from NGC 4649). For the other galaxies, including a reasonable DM halo improves the fit in terms of χ^2 . The most convincing cases are NGC 821 and NGC 3384, where the model without a DM halo is excluded at more than 3σ significance. Thus, while we are not able to constrain the shape of the DM halo, at least for some galaxies the presence of such a halo is supported. In total, for six galaxies (NGC 821, NGC 2778, NGC 3384, NGC 4473, NGC 4564, and NGC 5845), the model without a DM halo is excluded with at least 2σ significance.

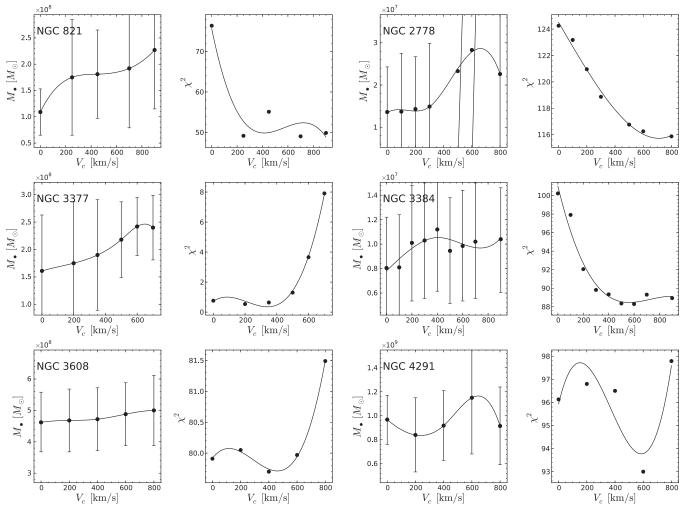


Figure 8. Variation of the black hole mass and the minimal χ^2 as a function of the assumed DM halo for each galaxy. In the left columns of the subpanels the change in M_{\bullet} for various values of $V_{\rm DM}$ is shown. The error bars correspond to 1σ (i.e., $\Delta\chi^2=1$). In the right columns the corresponding value of χ^2 is shown. A spline interpolation is shown as the solid line.

The mean increase of the black hole mass goes along with a decrease of the mass-to-light ratio, as expected. This indicates the degeneracy present between the stellar mass-to-light ratio and the DM contribution in dynamical models. For the whole sample we find a decrease in M/L of 6% with a scatter of 5%.

Even if our choice of DM halo is well motivated by the scaling relations of Thomas et al. (2009), it is basically an ad hoc assumption we had to make as we do not have the data to robustly constrain the DM halo profile. To at least test the effect of changing the assumed DM halo on the black hole mass, we ran a set of models, changing V_c in the logarithmic DM potential. We restrict ourselves to changing only this one parameter, as we want to avoid sampling the whole four-dimensional parameter space. It has also been found that V_c and r_c are degenerate, especially if the large radii coverage is poor (Shen & Gebhardt 2010; Forestell 2009). For each galaxy, we assume a twice as massive DM halo and a DM halo about half as massive, as well as some additional values. The results are shown in Figure 8 and 9. We confirm the basic trends of an improved χ^2 for a reasonable massive halo and an increase in M_{\bullet} for a more massive halo. The range of given M_{\bullet} approximately covers the range consistent with the current data, as long as the DM halo is not constrained for these galaxies.

5.3. Notes on Individual Galaxies

In the following, we provide more detailed information on the black holes for some individual galaxies.

NGC 821. There are two recent studies on the DM halo of this galaxy, providing large radii data. Weijmans et al. (2009) used SAURON data to measure LOSVDs out to ~4 effective radii. Their assumed DM halo gives $M_{\rm DM} = 9 \times 10^9 \, M_{\odot}$ within the effective radius (assuming $R_e = 5.1$ kpc), using an NFW profile. Forestell & Gebhardt (2010) used long-slit data from the Hobby-Eberly Telescope to measure the LOSVD out to $\sim 2R_e$. Assuming their power law fit to the DM halo, we find $M_{\rm DM} = 8 \times 10^9 \, M_{\odot}$ within R_e . Our assumed DM halo is more than twice as massive. Thus, M_{\bullet} for the true DM halo should be contained within the range spanned by our no DM and DM solution. Including these large radii data into the dynamical models is beyond the scope of this paper. The nuclear supermassive black hole in NGC 821 has been detected as a weak X-ray source, implying a very weak level of activity $(L_{\rm X}/L_{\rm Edd}\sim 10^{-8}; {\rm Pellegrini}\,{\rm et}\,{\rm al.}\,2007)$. There is also evidence for the presence of a jet (Fabbiano et al. 2004; Pellegrini et al. 2007).

NGC 2778. This galaxy already had the least confident black hole detection in G03. Assuming the value for M_{\bullet} of our no

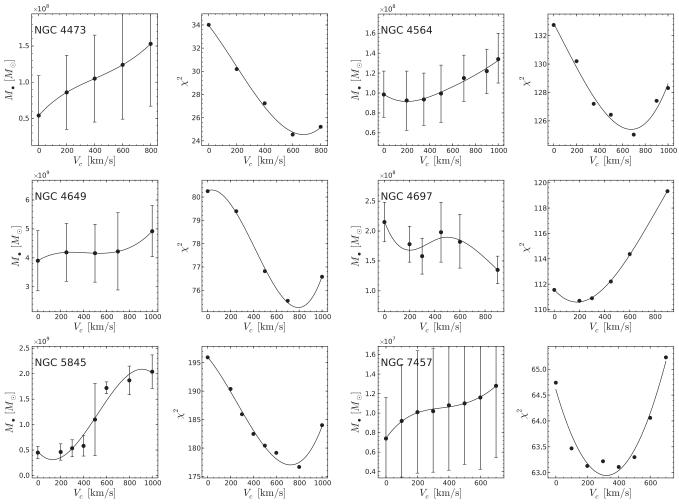


Figure 9. Same as Figure 8 for the second half of the galaxy sample.

DM halo model, we do not resolve the black hole's sphere of influence ($R_{\rm inf}/d_{\rm res}=0.2$). Including a DM halo in the model improves the fit significantly, but the significance of the black hole detection disappears. However, the previous M_{\bullet} estimate is still fully consistent with the 1σ upper limit of $M_{\bullet,\rm up}=2.99\times10^7\,M_{\odot}$ that we derive for NGC 2778 under the presence of a DM halo. This behavior might indicate the need to properly resolve $R_{\rm inf}$ when a DM halo is included to properly determine M_{\bullet} .

NGC 3377. The black hole mass for this galaxy increased by \sim 70%, compared to G03, mainly caused by the stronger widening of the confidence contours at the high-mass end than at the low-mass end. The previous value is still fully consistent within 1σ . Copin et al. (2004) reported a black hole mass of $M_{\bullet} = 8.3 \times 10^7 \, M_{\odot}$ (for our assumed distance) based on integral field unit observations with SAURON and OASIS, also still consistent with our results within 1σ . The first detection of a black hole in NGC 3377 has been reported by Kormendy et al. (1998), based on ground-based observations. Using an isotropic model, they found $M_{\bullet} = 2.1 \times 10^8 M_{\odot}$ and $M/L_V = 2.0$ (for our assumed distance), in good agreement with our results. NGC 3377 is a rapid rotator and close to isotropy, justifying the isotropic assumption for this galaxy. NGC 3377 exhibits a nuclear X-ray source, showing a jet-like feature (Soria et al. 2006).

NGC 3384. Besides NGC 2778, this is the only other galaxy for which the sphere of influence is not resolved. While for

NGC 2778 the new code does not lead to a change of the χ^2 distribution, for NGC 3384, M_{\bullet} decreases. This might indicate a larger uncertainty in the determination of M_{\bullet} using different modeling codes when $R_{\rm inf}$ is not resolved. NGC 3384 is the galaxy with the strongest constraints on the presence of a DM halo. For this galaxy, we ran a grid of models changing r_c as well as V_c , but we found no change in χ^2 for different values of r_c . However, we are able to set a lower limit on V_c with $V_c > 350 \text{ km s}^{-1}$ at 1σ confidence. The no DM halo model is excluded at more than 3σ confidence (see Figure 8).

NGC 4473. NGC 4473 shows evidence for a central stellar disk both in the imaging and the kinematics, as discussed by G03. We followed G03 and include a central exponential disk and also assumed a galaxy inclination of 71°, as found for the disk component. Thus, this galaxy is the only case in our sample not modeled with an edge-on inclination. The presence of the disk has a distinct influence on the measured black hole mass causing a relatively large difference between the models with and without a DM halo.

NGC 4564. This galaxy is known to have a nuclear X-ray source (Soria et al. 2006), indicating the presence of an extremely sub-Eddington accreting AGN.

NGC 4649. This object has recently been studied by Shen & Gebhardt (2010) including a DM halo in the models. In addition to the stellar kinematics used in this work, they included globular cluster velocities from Hwang et al. (2008). Thus, our results are not directly comparable. They report values of

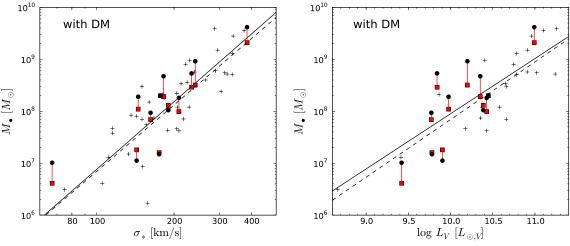


Figure 10. Left panel: M_{\bullet} – σ_* relationship. The red squares show our sample with the M_{\bullet} values given by Gebhardt et al. (2003), the black circles give the M_{\bullet} determined in this work with the inclusion of a DM halo. The black solid line shows our updated result for the M_{\bullet} – σ_* relation, while the dashed line shows the relation by Gültekin et al. (2009b). The crosses show the rest of their sample. Right panel: M_{\bullet} – L_V relationship. The symbols are the same as in the left panel. The solid line is our best fit when including a DM halo for our 12 galaxies. The dashed line and crosses are again from Gültekin et al. (2009b). (A color version of this figure is available in the online journal.)

 $M_{\bullet} = (4.5 \pm 1.0) \times 10^9$ when including a DM halo in the models and $M_{\bullet} = (4.3 \pm 0.7) \times 10^9$ without a DM halo. Our results for M_{\bullet} are consistent with their work.

NGC 4697. The black hole mass for this galaxy is basically unchanged using the modified code and including a DM halo. This result is consistent with Forestell (2009). She used the same data and model code as we did, but augmented by kinematics of planetary nebulae at large radii (Méndez et al. 2001, 2008, 2009), constraining M_{\bullet} and the DM halo at the same time. Her best-fit model has $M_{\bullet}=2.1\times10^8\,M_{\odot},\,M/L=4.35,\,V_c=388~{\rm km~s^{-1}},\,{\rm and}\,r_c=9~{\rm kpc},\,{\rm assuming}$ a logarithmic halo. We find identical values for M_{\bullet} and M/L, using slightly different DM halo parameters. NGC 4697 has a nuclear point source detected in X-rays (Soria et al. 2006), showing that its black hole is active at a low rate.

NGC 5845. While there is a moderate increase in M_{\bullet} when a DM halo is included in the model, the χ^2 distribution flattens at the high-mass end, due to an increased degeneracy between M_{\bullet} and M/L. Increasing the mass of the DM halo strongly enhances this degeneracy, leading to an almost unconstrained M_{\bullet} over a wide mass range, until for $V_c \approx 600 \text{ km s}^{-1}$ the minimum switches to $M_{\bullet} \approx 1.7 \times 10^9 \, M_{\odot}$, still with strong degeneracy between M_{\bullet} and M/L. Kinematic data at large radii, to better constrain the DM halo and M/L, would be desirable for this galaxy. The model without a DM halo is excluded with more than 3σ significance for NGC 5845. There is a nuclear X-ray source here as well (Soria et al. 2006). There is evidence for obscuration of the black hole by a dusty disk, with the X-ray emission originating from scattering of the AGN continuum emission on the surrounding plasma.

6. THE BLACK HOLE-BULGE RELATIONS

As our sample constitutes a significant fraction of the galaxy sample for which dynamical black hole masses are available, it is worth looking at the effect of these new black hole mass measurements on the black hole–spheroid relations, namely the M_{\bullet} – σ_* and M_{\bullet} – L_V relationships. We used the sample of Gültekin et al. (2009b) as the reference sample, containing 49 M_{\bullet} measurements and 18 upper limits, including our 12 objects.

For the fitting, we used a generalized maximum likelihood method as described by Gültekin et al. (2009b; see also Woo et al. 2010). We minimize the likelihood function $S = -2 \ln \mathcal{L}$, with $\mathcal{L} = \prod_i l_i(\mu_i, s_i)$ being the product of the likelihoods for the individual measurements of black hole mass $\mu = \log M_{\bullet}$ and bulge property $s = \log \sigma_*$ or $s = \log L_V$. The likelihood for measuring the mass μ_i and bulge property s_i for given true mass μ and true bulge property s_i is

$$l_i(\mu_i, s_i) = \int Q_{\mu}(\mu_i \mid \mu) Q_s(s_i \mid s) P(\mu \mid s) d\mu ds.$$
 (10)

We assume Q_{μ} , Q_{s} , and P to have a log-normal form, with $\sigma_{Q_{\mu}}$ and $\sigma_{Q_{s}}$ corresponding to the measurement uncertainty in the black hole mass and bulge property, and $\sigma_{P}=\epsilon_{0}$ is the intrinsic scatter in the black hole mass–bulge property relation. Upper limits are incorporated in the fit, following Gültekin et al. (2009b). Thus, we minimize

$$S = \sum_{i=1}^{N} \left[\frac{(\mu_i - \alpha - \beta s_i)^2}{\epsilon_{\text{tot},i}^2} + 2 \ln \epsilon_{\text{tot},i} \right] + 2 \sum_{i=1}^{M} \ln l_{\text{ul},j}, \quad (11)$$

with α and β being the normalization and the slope of the black hole–bulge relations, $\epsilon_{\text{tot},i}^2 = \sigma_{Q_\mu,i}^2 + \sigma_{Q_s,i}^2 + \epsilon_0^2$, N is the number of black hole measurements, M is the number of upper limits, and $l_{\text{ul},j}$ is the likelihood of the upper limit as in Gültekin et al. (2009b).

We first fit the M_{\bullet} - σ_* and M_{\bullet} - L_V relationships using the sample of Gültekin et al. (2009b), finding identical results. We then updated their black hole masses with our new values for the 12 objects in our sample. We find

$$\log(M_{\bullet}/M_{\odot}) = (8.18 \pm 0.06) + (4.32 \pm 0.31) \log(\sigma_*/200 \,\mathrm{km \, s^{-1}})$$
 (12)

with intrinsic scatter $\epsilon_0 = 0.44 \pm 0.06$ and

$$\log(M_{\bullet}/M_{\odot}) = (9.01 \pm 0.10) + (1.06 \pm 0.15) \log(L_V/10^{11} L_{\odot,V})$$
 (13)

with intrinsic scatter $\epsilon_0 = 0.41 \pm 0.04$. They are shown in Figure 10.

Note that both relations are not based on exactly the same samples. As in Gültekin et al. (2009b), for the determination of the M_{\bullet} – L_V relationship we restricted the sample to elliptical and S0 galaxies with reliable bulge–disk decomposition. When using the same restricted subsample for the M_{\bullet} – σ_* relationship, we find a shallower slope ($\beta=3.80\pm0.33$) and a reduced intrinsic scatter ($\epsilon_0=0.34\pm0.05$), lower than for the M_{\bullet} – L_V relationship for the same sample. Restricting the sample in this manner is supported by observations that suggest that spiral galaxies do not follow the M_{\bullet} – σ_* relation of ellipticals (Greene et al. 2010).

We also used a generalized least-squares method to incorporate measurement uncertainties in both variables and intrinsic scatter as described in Tremaine et al. (2002), omitting the upper limits, which yields consistent results. Compared to Gültekin et al. (2009b), we find only a slight change for the best fit. While the slope of the relation is consistent, the normalization increased slightly as well as the intrinsic scatter in both relations. We also fitted the sample of Gültekin et al. (2009b) with our updated black hole masses, without accounting for a DM halo. Most of the change in the M_{\bullet} - σ_* and M_{\bullet} - L_V relationships is caused by the improved masses. The effect of the inclusion of a DM halo on these relationships is marginal.

However, this is not a full correction of the black hole—bulge relationships for the effect of a DM halo on the black hole masses, as it is restricted to our sample of 12 galaxies. The rest of the galaxies with stellar dynamical black hole mass measurements potentially suffer from the same systematic bias. Ideally, a correction would consist of a re-modeling of these galaxies including a DM halo, as performed in this work for the sample of G03. However, we can use Figure 7 as a guideline for an average correction. Figure 7 indicates that the correction factor depends on the resolution of the sphere of influence. For $R_{\rm inf}/d_{\rm res} \gtrsim 3$ including or ignoring a DM halo in the modeling gives consistent results, while for lower values there is on average a systematic bias with a mean $\langle M_{\bullet, {\rm DM}}/M_{\bullet, {\rm no}\,{\rm DM}}\rangle = 1.5$ for our sample.

To estimate the effect on the black hole–bulge relations, we increased all stellar dynamical black hole mass measurements in the sample of Gültekin et al. (2009b) with $R_{\rm inf}/d_{\rm res} < 3$ by this average factor and re-fitted the relations. To investigate the pure change due to the DM halo, we also fitted the black hole–bulge relations to the sample of Gültekin et al. (2009b), but with M_{\bullet} of the 12 galaxies of our work replaced by our results without a DM halo. Compared to the best fit to this sample, we found a slightly increased slope, a consistent intrinsic scatter, and an increase in normalization by 0.04 dex. We found a normalization, slope, and intrinsic scatter of (8.21,4.38,0.42) for the M_{\bullet} – σ_* and (9.05,1.07,0.41) for the M_{\bullet} – L_V relationship.

Additionally, we fitted only our sample with the values for M_{\bullet} with and without including a DM halo in the models. We recovered an increase in the normalization of ~ 0.07 dex, corresponding to the mean increase in M_{\bullet} in the sample, while the slope is consistent and the intrinsic scatter decreases.

7. CONCLUSIONS

We investigate the influence of accounting for the presence of a dark matter halo in the stellar dynamical modeling of galaxies on the measured black hole masses. We use a sample of 12 galaxies, already analyzed by Gebhardt et al. (2003), which have ground-based as well as high-resolution *HST* observations of the stellar kinematics to address this issue.

We model these galaxies without and with the presence of a dark matter halo. In the first case we found a significant difference of the measured black hole masses between our previous results for a large fraction of the sample. For most of the objects the mass increased compared to the values given by Gebhardt et al. (2003). We ascribe this difference to the improved code, exhibiting a better coverage of the phase space for the generated orbit library. This shows the importance of a dense coverage of phase space in the dynamical models.

Second, we include a reasonable dark matter halo into the models, using a scaling relationship based on the galaxy luminosity (Thomas et al. 2009). We find an increase of the measured black hole mass, but much less than what has been found for M87 and NGC 6086. For these two galaxies, kinematic information is available only at large radii, whereas for our sample we have high-resolution data covering the central parts of the galaxies. Thus, the black hole mass is better constrained by central kinematic observations and less affected by the presence of a dark matter halo in the models.

Using different massive dark matter halos for the same galaxy, we confirm the trend of an increase of the recovered black hole mass for a more massive halo as well as a decrease of the mass-to-light ratio. Based on a χ^2 analysis, the presence of a dark matter halo is implied for five of the 12 galaxies with at least 2σ significance, although we are not able to constrain the shape of the dark matter halo.

We study the consequence of our new black hole mass measurements on the M_{\bullet} – σ_* and M_{\bullet} – L_V relationships, updating the sample of Gültekin et al. (2009b) with our results. We found only a mild change in the best-fit values, still consistent with the previous estimate, with a slight increase in the normalization and the intrinsic scatter. We estimated the total effect of a black hole mass increase for galaxies studied by stellar dynamics by accounting for a dark matter halo which will lead to an increase in the normalization by \sim 0.04–0.07 dex.

Even if our sample shows only a mild influence of the dark matter halo on the black hole mass, a dark matter halo is clearly present. Thus, it is necessary to take it into account in the modeling of the galaxy to avoid a systematic bias.

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