Copyright by Wentao Fu

2014

The Dissertation Committee for Wentao Fu Certifies that this is the approved version of the following dissertation:

A CONCURRENT APPROACH TO AUTOMATED MANUFACTURING PROCESS PLANNING

Committee:

Richard H. Crawford, Supervisor

Matthew I. Campbell, Co-Supervisor

Wei Li

Benito R. Fernandez

Tolga Kurtoglu

A CONCURRENT APPROACH TO AUTOMATED MANUFACTURING PROCESS PLANNING

by

Wentao Fu, B.E., M.S.E.

Dissertation

Presented to the Faculty of the Graduate School of

The University of Texas at Austin

in Partial Fulfillment

of the Requirements

for the Degree of

Doctor of Philosophy

The University of Texas at Austin May 2014

Dedication

To my parents, Andao Fu and Jieying Li.

Acknowledgements

I would like to thank Dr. Matthew Campbell for his constant guidance, support and encouragement during the progress of this dissertation and my graduate study abroad. It was his excellent research that ignited my enthusiasm in the research direction I am pursuing. His vision, pursuit of high standard and kindness will continue benefiting my future development. Also I would like to thank Dr. Richard Crawford for serving as my supervisor after Dr. Campbell moved to another university. In particular, I am grateful for his help on finding financial support for me during my last year, without which it would not have been so smooth for me to finish my research. I wish to thank my committee members, Dr. Wei Li and Dr. Benito Fernandez, for their valuable input ever since my qualifying exam all the way to my final defense.

This work is based on a collaborative research project that was led by Palo Alto Research Center. I would like to thank all my research partners and colleagues, especially Dr. Ata Eftekharian and Dr. Tolga Kurtoglu, for their excellent work and leadership that helped make this dissertation possible. Dr. Kurtoglu is also my external committee member, and I would like to thank him for his service.

I want to thank my family: my sister, my brother, and particularly my father and mother, Andao and Jieying. They have witnessed me going through all the important stages through my life and they have always been there to support me, to comfort me, and to be proud of me.

At the end, I thank my friends in Austin, without whom my life here would not have been this meaningful. I want to extend special thanks to my girlfriend Suirong, for not breaking up with me when we were staying apart, for preparing countless tasteful dishes that have been engraved in my memory, and for travelling with me to every meaningful place in my life.

A CONCURRENT APPROACH TO AUTOMATED MANUFACTURING PROCESS PLANNING

Wentao Fu, Ph.D.

The University of Texas at Austin, 2014

Supervisors: Matthew I. Campbell, Richard H. Crawford

With the increasing demand of fast-paced and hybrid manufacturing processes in modern industry, it is desirable to expedite the iterations between design and manufacturing through intelligent computational techniques. In this research, we propose a concurrent approach of this kind to streamline the design and manufacturing processes. With this approach, a CAD design is automatically analyzed in terms of its manufacturability in the early design stage. If the part is manufacturable, a set of process plans optimized in time, cost, fixture quality and tolerance satisfaction are reported in real time. If the part is not manufacturable, the potential design changes are provided for better manufacturing.

In the approach, the geometric information of 3D models and the empirical knowledge in manufacturing processes, fixtures, and tolerances are combined and encapsulated into a graph-grammar based reasoning. The reasoning systematically extracts meaningful manufacturing details that later constitute complete process plans for any given solid model. The plans are then evaluated and optimized using a specially designed multi-objective best first search technique. The complete approach enables a concurrent and efficient manufacturability analysis tool that closely resembles real manufacturing planning practice.

Numerous case studies with real engineering parts are presented to characterize the novelty and contributions of this approach. The optimality of the suggested plans is verified through computational comparisons, and the practicality of the plans is validated with hands-on implementations on the shop floor.

Table of Contents

Table of Contents	ix
List of Tables	xii
List of Figures	xiii
Chapter 1: Introduction	1
1.1. Motivation	3
1.2. Technologies and Approaches Involved	4
1.3. Dissertation Statement	5
1.4. Organization	5
Chapter 2: Literature Review	8
2.1. Computer-aided Manufacturing Process Planning	8
2.2. Computer-aided Fixture Design	11
2.3. Automated Turning Process Planning	13
PART I: AUTOMATED MANUFACTURABILITY FEEDBACK ANALYSIS	15
Chapter 3: Geometric Reasoning	19
Chapter 4: Graph Grammar Based Reasoning	23
4.1. Seed Lexicon	23
4.2. Rule Development	30
Chapter 5: Fixture Design and Plan Evaluation	40
5.1. Defining Fixture Candidates with Graph Grammar	41
5.1. Defining Fixture Candidates with Graph Grammar5.2. Evaluating Fixture Candidates	41 44
5.1. Defining Fixture Candidates with Graph Grammar5.2. Evaluating Fixture Candidates5.3. Plan Consolidation	41 44 49
 5.1. Defining Fixture Candidates with Graph Grammar 5.2. Evaluating Fixture Candidates 5.3. Plan Consolidation Chapter 6: Multi-objective Hierarchical Sorting based Best First Search 	41 44 49 51
 5.1. Defining Fixture Candidates with Graph Grammar 5.2. Evaluating Fixture Candidates 5.3. Plan Consolidation Chapter 6: Multi-objective Hierarchical Sorting based Best First Search 6.1. Introduction 	41 44 49 51 51
 5.1. Defining Fixture Candidates with Graph Grammar 5.2. Evaluating Fixture Candidates 5.3. Plan Consolidation Chapter 6: Multi-objective Hierarchical Sorting based Best First Search 6.1. Introduction	41 44 51 51 54
 5.1. Defining Fixture Candidates with Graph Grammar 5.2. Evaluating Fixture Candidates 5.3. Plan Consolidation Chapter 6: Multi-objective Hierarchical Sorting based Best First Search 6.1. Introduction	41 44 51 51 54 57

6.5. Summary
Chapter 7: Case Studies and Discussions
7.1. Radiobox: Dynamic Allocation of Faces For Optimal Fixture Design .67
7.2. Part II: Dependency Between Fixture Design and Manufacturing Process Planning
7.3. Stabilizer: Synthesized Reasoning Applied in Manufacturing Complicated Features
7.4. Non-manufacturability Analysis79
7.5. Characteristics of Implementation and Deployment
Chapter 8: Part I Summary
PART II: AUTOMATED REASONING FOR DEFINING TURNING OPERATIONS FOR MILL-TURN PARTS 85
Chapter 9: Geometric Reasoning
9.1. Detecting the Dominant Rotational Axis
9.2. Defining the Cutting Planes91
9.3. Recovering the Revolving Facet92
9.4. Extracting Turnable and Non-turnable Features
9.5. Efficiency and Effectiveness
Chapter 10: Setup Design Based On Tolerance Analysis
Chapter 11: Graph Grammar Based Reasoning
Chapter 12: Detailed Example
Chapter 13: Plan Validation
Chapter 14: Part II Summary
Chapter 15: Conclusion
15.1. Summary120
15.2. Contributions and Novelty121
15.3. Future Work
15.4. Closing Remarks127

Bibliography	
Vita	

List of Tables

Table 1:	Labels and their definitions in AMFA grammar reasoning2	8
Table 2:	Description of rule sets and their tasks	1
Table 3:	Fixture design guidelines and evaluation metrics	5
Table 4:	Extreme cases that are penalized in fixture quality measurement	6
Table 5:	All computations needed to form the fixture quality	8
Table 6:	Comparison between hierarchical search and A* search for example 16	0
Table 7:	Comparison between hierarchical search and A* search for example 2 6	3
Table 8:	An optimal manufacturing plan with fixtures for Radio box	9
Table 9:	An optimal manufacturing plan with fixtures for part II	2
Table 10:	Comparison between the manufacturing parameters suggested by the	
	reasoning and the actual choices in the machine shop for part II	4
Table 11:	An optimal manufacturing plan with fixtures for the stabilizer7	6
Table 12:	Comparison between the manufacturing parameters suggested by the	
	reasoning and the actual choices in the machine shop for the stabilizer 7	8
Table 13:	The analysis results of the two plans from the tolerance analysis	
	module	6

List of Figures

Figure 1:	Overview of the work presented in the dissertation	2
Figure 2:	Flowchart of AMFA reasoning	16
Figure 3:	Volume decomposition tree.	21
Figure 4:	Part A in Figure 2 as a seed graph.	24
Figure 5:	A sample face representation in the seed lexicon.	25
Figure 6:	An example of infeasible tool entry face	33
Figure 7:	Another case of infeasible tool entry face	34
Figure 8:	(a) Drilling rule 1 for type 1 hole, (b) drilling rule 2 for type 2 hole	36
Figure 9:	Grammar reasoning flowchart in AMFA	38
Figure 10:	Downward clamping and side clamping as applied on a work-piece	42
Figure 11:	Screenshot of a rule in rule set 5	43
Figure 12:	Screenshot of another rule in rule set 5	44
Figure 13:	A case where the inaccessibility penalty is assigned	47
Figure 14:	Comparison of two plans with and without consolidation	50
Figure 15:	A tree structure of the search space in process planning	52
Figure 16:	An illustrative part.	55
Figure 17:	Flowchart of the search algorithm with hierarchical sorting	57
Figure 18:	Example part 1	60
Figure 19:	Comparison of two plans for example 1	62
Figure 20:	Example part 2.	63
Figure 21:	The optimal plan generated by hierarchical search for example 2	64
Figure 22:	The plot of computational time versus part complexity.	65
Figure 23:	Summary of the exhaustive search for the part in Figure 16	66
Figure 24:	CAD model of the "Radio box"	67
Figure 25:	CAD model of part 2	71
Figure 26:	CAD model of the stabilizer.	75

Figure 27:	(a) A non-manufacturable part due to design flaws, (b) the machine	d part	
	simulated in FeatureCAM, and (c) the manufacturability anal		
	generated in AMFA.	80	
Figure 28:	A sample manufacturing plan generated in FeatureCAM.	80	
Figure 29:	A sample AMFA GUI	81	
Figure 30:	A sample part with non-turnable features	88	
Figure 31:	(a) The identified curved edges and (b) their axial normal vectors for	or the	
	part in Figure 30	91	
Figure 32:	A unit circle with non-uniform radial vectors	92	
Figure 33:	(a) The sampled cross sections of the part in Figure 30; (b) the union	n of all	
	the cross sections	93	
Figure 34:	(a) The revolving face and the rotational axis; (b) the as-lathed mod	lel 93	
Figure 35:	(a) The decomposed turnable features; (b) the non-turnable features	94	
Figure 36:	A summary of the tests on more complex parts	95	
Figure 37:	Grammar reasoning flowchart for turning process planning	100	
Figure 38:	The CAD drawing of the part shown in Figure 34b.	100	
Figure 39:	The tolerance graph generated from the 2D drawing in Figure 38	101	
Figure 40:	The generalized angle α of the parallelism tolerance	102	
Figure 41:	The screenshot of (a) rule 1, (b) rule 2 and (c) rule 3.	105	
Figure 42:	The screenshot of the setup graph	106	
Figure 43:	The suggested turning sequence for the part shown in Figure 34b	108	
Figure 44:	A complex part with interacting features	109	
Figure 45:	The CAD drawing of the as-lathed model in Figure 44a	110	
Figure 46:	The tolerance graph for the part shown in Figure 44a	110	
Figure 47:	The updated tolerance graph for the part shown in Figure 44a	111	
Figure 48:	The setup graph for the part in Figure 44a	112	
Figure 49:	The suggested turning sequence for the part shown in Figure 44a	112	
Figure 50:	A traditional turning sequence for the part shown in Figure 34b	115	
Figure 51:	2D contour tool path.	124	

Chapter 1: Introduction

Computer-aided manufacturing process planning (CAMPP, also known as CAPP) is a broad research topic as it sees applications in disassembly [1], assembly [2], and machining [3], [4]. In this work, we present systematic approaches to solving the manufacturing process planning problems. As shown in Figure 1, we start with an input CAD model. Then the geometric reasoning that was developed by Eftekharian et al. [5], [6] analyzes the part in order to identify the turnable and non-turnable features that need to be created. For non-turnable features that require milling, drilling and other nonturning material-removal processes (also referred to as subtractive manufacturing processes), a tool known as Automated Manufacturability Feedback Analysis (AMFA) [3], [7], [8] has been developed to automatically generate process plans that are optimized in manufacturing time, cost and fixture quality. Each optimal plan is detailed with suggested tools, feed directions, machines, and fixtures in order to complete the machining of the part. For turnable features, a tolerance based algorithm presented in [6], [9] is used to propose feasible turning process plans that best comply with the design tolerance specifications. Both process planning algorithms are developed based on the graph grammar, and are referred to as Grammar Reasoning in the flowchart. This dissertation focuses on the grammar reasoning as it is the major contribution of the author. In addition, since the geometric reasoning serves as an important module to this work, we will give moderate explanation when necessary.

As indicated in Figure 1, the research is split into two parts depending on the types of feature identified from the input CAD model. For the non-turnable features, the relevant geometric reasoning and grammar reasoning have been integrated into AMFA, which is part I of this dissertation. The geometric reasoning and grammar reasoning

relevant to the turning process planning are introduced together in part II of this dissertation.



Figure 1: Overview of the work presented in the dissertation.

1.1. MOTIVATION

Modern manufacturing industry is motivated to reduce time and cost in order to keep competitiveness. The main hurdle is the unnecessary back-and-forth between the design and manufacturing due to a lack of thorough understanding of a product in terms of its manufacturability in the early design phase, which often leads to additional time and cost for design iterations and manufacturing process improvements. The computational approach proposed in this research is aimed at alleviating this problem. In this technique, the manufacturability analysis is customizable based on a specific foundry capability, and a CAD design is assessed automatically and efficiently in terms of every detail of the manufacturing processes. The automated reasoning expedites the communication between design and manufacturing, and facilitates the designer to make judicious decisions in how to improve the design for better manufacturing and to get a sense of how to manufacture the part for lowest time and cost during the product development.

To reduce the manufacturing time and cost, the traditional process planning relies heavily on the shop-floor experience, which is very difficult to interpret computationally. Existing commercial CAD/CAM packages such as FeatureCAM [10] require numerous pre-decisions made by the user (e.g. the orientation of the raw-stock, the available tools and machines) before a process plan can be generated. The reported plan is therefore subject to change with the user customization and the optimality is not guaranteed. The dissertation aims to break through such limitations in current manufacturing practice by introducing the notion of a design space in which all possible process plans are generated for a given solid model. The integrated search technique constantly traverses the space in order to find the best plans that are guaranteed to be optimal in terms of the user-specified objectives. The concurrency of the proposed approach stems from the fact that manufacturing process planning overlaps with the knowledge of several disciplines. The interaction between one aspect and another (e.g. the effect of fixture design on the time and cost estimation of a process plan, and the interaction between the sequence of machining operations and the corresponding fixture designs) needs to be carefully assessed before a conclusion of the optimality of a process plan can be made. In our algorithm, the multi-disciplinary knowledge relevant to the process planning is considered "on the fly" so that the reasoning is constantly informed of the direction towards defining the empirical and optimal process plans.

1.2. TECHNOLOGIES AND APPROACHES INVOLVED

The graph grammar based approaches perform the process planning for turnable and non-turnable features on a graph grammar platform known as GraphSynth [11] that was developed by Campbell. It provides a library of graph elements and data structures that the author uses to design graphs and grammar rules in order to store and capture relevant geometric and manufacturing knowledge in the reasoning.

For the fixture design in AMFA [8], we use the knowledge gathered from the shop floor and the engineering handbooks to directly inform the reasoning of optimal fixture mechanisms for a given tooling operation. In this way, the complicated multi-objective optimization problem in the fixture design phase is avoided. The resulting fixture mechanisms are proven to be optimal and implementable.

The planning search technique developed in AMFA is a multi-objective hierarchical sorting based best first search [8]. It incorporates the manufacturing knowledge in the otherwise naïve search process and is able to converge to optimal process plans in manufacturing time, cost and fixture quality in near-linear time. As compared to the traditional A* search, this technique generates more practical process plans in a much shorter computation time.

A novel tolerance based technique [6], [9] is proposed to define the turning process plans that better satisfy the tolerance specifications. The idea is to identify the design knowledge conveyed by the tolerances and encapsulate it into the grammar reasoning such that the tolerances can be directly and effectively used to guide the generation of optimal turning sequences.

A tolerance analysis module for validating manufacturing process plans that was developed by the author and colleagues from Palo Alto Research Center [12] is employed to compare the suggested turning sequences with manually proposed plans. The result is used to validate the optimality of our plan in satisfying the prescribed tolerances.

1.3. DISSERTATION STATEMENT

A concurrent approach encapsulating the knowledge of manufacturing, fixture, tolerance analysis, graph grammars, and tree search optimization automatically defines optimal manufacturing process plans in terms of manufacturing time, cost, fixture quality and tolerance satisfaction for any solid model.

1.4. ORGANIZATION

The dissertation is organized as follows. Chapter 2 explores the existing research in the three major topics of this dissertation: the computer-aided manufacturing process planning, the computer-aided fixture design and the automated turning process planning. After this, the dissertation is separated into two parts. The first part is the automated reasoning for non-turning operations, which includes chapter 3 through chapter 8. In this part, we explain in detail the automated process planning algorithm, the fixture design and the search optimization. Chapters 9 to 14 constitute the second part of this dissertation, in which the automated reasoning for defining turning operations is presented. More specifically:

Part I:

Chapter 3 briefly introduces the geometric reasoning in AMFA done by Eftekharian et al. As it is not the author's work, only a high-level description of the algorithm is provided to ease the understanding of the following chapters.

Chapter 4 describes the graph representation of the solid model and the grammar rule based reasoning for generating process plans.

Chapter 5 explains how the candidate fixtures for a machining operation are generated using grammar rules and how the complete plans are evaluated against specially designed metrics.

Chapter 6 presents a hierarchical sorting based best first search that is developed to solve the multi-objective optimization problem during the process planning.

Chapter 7 provides three case studies to validate the novelty, effectiveness and efficiency of our approach. The practicality of the proposed plans is validated through real implementations in the machine shop.

Chapter 8 summarizes the work in the first part.

Part II:

Chapter 9 provides the geometric reasoning developed by Eftekharian that is used to identify the turnable features from a mill-turn part. The features are converted to a graph representation for the later grammar reasoning to work on.

Chapter 10 explains the fundamentals of the turning setup design based on tolerance analysis.

Chapter 11 describes the graph grammar based implementation of the setup design algorithm through an illustrative case study.

Chapter 12 provides a more complex and detailed example to further explain the grammar reasoning.

Chapter 13 introduces briefly a tolerance analysis module that the author developed with Palo Alto Research Center and uses this algorithm to validate the suggested turning sequences in satisfying prescribed tolerances.

Chapter 14 summarizes the research in part II.

The dissertation closes with chapter 15, which highlights the contributions of this dissertation. It also outlines the future directions along which the work can be further improved.

Chapter 2: Literature Review

Our research contributes to three major areas: the computer-aided manufacturing process planning, the computer-aided fixture design, and the automated turning process planning. Previous work in the three areas is explored in this chapter. For the search technique and the evaluation of process plans in part I and the tolerance analysis in the turning process planning, the relevant work is embedded into corresponding chapters for a better elaboration.

2.1. COMPUTER-AIDED MANUFACTURING PROCESS PLANNING

Computer-aided manufacturing process planning (CAMPP, or CAPP) was first proposed by Russell [13] in 1967. Due to the fast development since the 1980s, this topic continues to receive considerable attention both from researchers and engineers. At this time, many knowledge based approaches [14]–[16] were developed to capture the basics behind process planning. Marri et al. [17] provided a comprehensive review of these CAPP systems. They concluded that more attention should be paid to the architecture and constraints behind machining operations while developing a comprehensive CAPP system. More recently, Sharma and Gao [18] proposed a process planning system that employs the up-to-date tools and technologies consistent with the international standard for exchange of product data (i.e. the .STEP format¹). However this system is only intended for simple prismatic models and the feedback cannot be automatically imported into CAD systems for detailed re-design. Allen et al. [19] developed an agent-based approach that provides a number of generic solutions while maintaining the ability for manual intervention in order to establish local working preferences. However, the efficiency of this algorithm is restricted by its parametric optimization structure.

¹ (.STEP) is used as the standard format for the exchange and conversion of solid models.

In contrast, the graph grammar based approach to automated manufacturing planning, in principle, can support a larger variety of topologies and is not necessarily restricted by any optimization process. It utilizes a technique of creating new graphs from an original graph (host) by applying prescribed rules onto the host [20]. The rules are of the form (L-to-R) where the left hand side (LHS) includes elements and conditions to be recognized and satisfied in the host graph and the right hand side (RHS) indicates the transformations of those elements.

A well-known grammar based approach in automated manufacturing planning uses Form-Feature Recognition (FFR) technique [21]. FFR is primarily important because it can extract or generate higher level and meaningful geometric primitives [22] (for example, lines, polygons, triangular facets, et al.) that are not easily inferable from the 3D geometry. These geometric features serve as a bridge between the geometry on one hand and manufacturing reasoning on the other hand [23]. Thorough surveys of various techniques in form-feature recognition can be found in the work by Han et al. [24], Shah [25], [26], Subrahmanyam [27] and Babic et al. [28]. According to these surveys, three dominant techniques – graph based, rule based and hint based approaches - are mostly used in modern FFR algorithms. Graph based techniques, although proven to be reliable in recognizing isolated features, mainly suffer from the complexity of geometries and the fact that features may have interactions with each other [29], [30]. Some researchers [31] have tried to tackle the problem by introducing various types of heuristics to the algorithm and have gained considerable achievements, but still the problem remains unsolved for complex geometries. Others [29], [32] have tried to add missing elements that correspond to interacting features into the graph, but despite the added complexity they do not completely solve the problem. In addition, many contemporary recognition systems deal only with orthogonal features [33]–[36], but little attention has been paid to non-orthogonal and arbitrary features [37].

Volumetric decomposition methods stand apart from the others, both in the algorithm employed and the results. Researchers have continued to extend and refine this approach to solve numerous shortcomings, such as non-convergence and geometricdomain restrictions. The volumetric decomposition method can handle interactions and provide additional information such as geometry-based precedence relations [38]. Methods that are most related to our approach use the concept of convex-hull and setdifference operations to generate meaningful features suitable for machining processes. The idea is raised from the complicated concept of B-rep to CSG (Constructive Solid Geometry) conversion discussed in a number of early CAD research works [39]-[41]. Woo [42] proposed a method based on this idea known as Alternating Sum of Volumes (ASV). One problem in his decomposition approach is the possibility of nonconvergence, which means that the decomposition will never stop unless terminated by the user for certain geometries. It significantly limits the applicability of this approach. Kim [43], [44] proposed a technique to overcome this limitation by using a new partitioning strategy and combining that with the ASV idea mentioned above. The new method – referred to as ASVP –shows better convergence than ASV but cannot guarantee the optimality of generated machining features. Another similar approach to this work was provided by Ertelt and Shea [45]. In this method a vocabulary of removal volume shapes (or the so-called shape grammars) is used to encode the knowledge of fundamental machine capabilities. Shape grammars may include available tool dataset, machines, tool motion information, etc. Since this approach uses topological reasoning and parametric evaluation concurrently, its scalability to handle parts with increasing complexity and non-traditional machining processes is questionable.

2.2. COMPUTER-AIDED FIXTURE DESIGN

Computer-aided fixture design (CAFD) has been a challenging task for several reasons. First, a fixture is proposed based on the assessment on factors across different fields. For example, it relies on the available type of fixtures (either modular or dedicated fixture) and is specific to particular manufacturing processes [46]. Also a proper fixture has to provide enough constraints to secure the part under unknown cutting forces. Additionally, it should not block any potential feed directions or tool paths that are determined by the geometry of the part as well as the manufacturing procedures. While a human being with experience thinks of this multi-objective problem naturally, the computational approaches nowadays still lack the ability to consider these factors as a whole [47].

Numerous articles can be found in CAFD with each based on a particular topic. Sermsuti-anuwat [48] proposed a tolerance based approach for milling fixture design, and Kang et al. [49] generalized the tolerance analysis technique to any type of fixture design. Pang and Trinkle [50] and Kang et al. [51] approached the fixture design problem by characterizing the stability of the work-piece. Fan et al. [52] attempted to establish a service-oriented architecture (SOA) in fixture design in order to facilitate the communication between various assemblies. Another popular approach is based on the form closure theory [53], [54], which has been introduced and developed since 1980s. The idea is that for any given shape in 3D space, there exist 7 frictionless points of contact that are necessary and sufficient to hold and secure the object under whatever external forces. With this theory, the problem of fixture design reduces to the selection of 7 points on the part surfaces. Researchers have been actively investigating algorithms to define the point configurations in [55]–[57]. Meanwhile, different techniques have been developed for fixture designs in distinct applications. The modular fixture provides reconfigurable setups that can be used for various purposes (e.g. parts of different sizes and shapes). One popular modular fixture is the reconfigurable pin-array fixture technology [58]. The modular fixture design has also been studied with intelligent algorithms [59] and sees successful applications in various environments [60], [61]. In contrast, more complicated or precise manufacturing processes require dedicated fixtures, for which case-based reasoning (CBR) [62] techniques have been applied to automate the fixture design process.

Reviews of the aforementioned techniques as well as existing computerized tools are given in [46], [63]–[65]. In light of the variety of research, Rong et al. [66] proposed a basic framework for fixture design in order to better streamline the CAFD processes, where the existing techniques were benchmarked against four main stages: setup planning, fixture planning, fixture unit design and verification. According to their investigation, most of the existing work is not able to perform the fixture verification. One reason is that the fixture analysis has not been thoroughly studied in the context of manufacturing process planning. This is critical considering that the fixture for a given operation may need adjustments based on how the operation is sequenced in a manufacturing plan. It is possible that for a certain operation we want a "sub-optimal" fixture (e.g. less convenient, relatively harder to set up) in order to ease the operations that follow.

The fixture design technique proposed in this work is derived from the manufacturing perspective and is fully embedded into our manufacturability analysis tool. As to be presented, the reasoning is seamlessly synthesized with the other modules in grammar reasoning and therefore the optimal and more empirical plans can be found while the efficiency is preserved.

2.3. Automated Turning Process Planning

In the geometric reasoning of the turning process, Tseng and Joshi [67] developed a method to extract rotational and prismatic features from mill-turn parts. According to this work, cylindrical features are extracted by using a sweep-type process where a 2D profile is first established and then swept around an axis of rotation. One drawback is that this method requires the axis of rotation to be known therefore is not very suitable for automatic feature extraction. Kim et al. [68] developed a feature recognition system that used convex decomposition to decompose the mill-turn parts into a series of negative machining volumes. They also utilized this method to determine precedence relationships for machining features. However, their method requires a positive stock volume to be known a priori.

In automatic generation of machining plans, a small body of literature has been devoted to turning operations in contrast to milling and CNC machining. In general, reasoning about turning operations mainly includes two approaches: parametric based and feature based. Berra and Barash [69] proposed an automatic reasoning scheme for process planning and optimization of a turning operation. In this work, various turning parameters were tuned in order to achieve the minimum time and cost associated with manufacturing. In terms of generating accurate plans (while considering time and cost) this work lacks incorporating tolerance relationships of various features. Lai-Yuen and Lee [70], Zhang et al. [71], and Huang et al. [72] have implemented a more comprehensive algorithm by using various approaches including an activity-based approach, a surface-roughness approach and an engineering knowledge approach to model and analyze the turning process. Although they have achieved considerable improvements, the completeness and accuracy of their methods are still controversial, as none have studied the tolerance specifications and its effect on the setup design.

Feature-based techniques in turning operations have shown to be more accurate in generating optimal manufacturing plans. Culler [73] developed a feature based intelligent process planner known as Turning Assistant (TA), which perceives the precedent knowledge built into the rules and prescribes necessary operations accordingly for each feature that requires NC lathe work. Similarly, Liu [74] presented a method for the feature extraction and classification of rotational parts. But according to these papers, not all forms of the features can be recognized by these approaches. In a different technique, Suliman and Awan [75] developed a turning feature recognition technique directly from 2D drawings. Although this is an important technique, the validity and applicability in various models are still to be verified, as the 2D feature recognition is trivial and not generic enough for use in non-prismatic 3D geometries.

Additionally, it is revealed from the past literature that the feature-based techniques generally suffer from the feature interactions and the fact that turnable and non-turnable features may have interference with each other. To solve this problem, Li and Shah [76] attempted to automatically separate the coupled portions and detect the form features as well as user-defined features via a graph and rule based recognition algorithm. But the approach imposes constraints on the shapes that can be processed due to the missing of certain graph elements. In contrast, this work proposes a new technique to effectively de-couple features in complex mill-turn parts and generate manufacturing plans based on tolerance considerations, which is lacking in previous literatures.

PART I: AUTOMATED MANUFACTURABILITY FEEDBACK ANALYSIS

In order to better streamline the interaction between computer-aided design and manufacturing, an approach is provided which automatically reasons about a CAD model to define detailed and optimal manufacturing plans. The larger system is known as Automated Manufacturing Feedback Analysis (AMFA), and this part presents the graph grammar based reasoning that serves at the system's foundation. Starting from a seed graph that represents a CAD model, the grammar reasoning performs the analysis of manufacturability by referencing the data provided for the manufacturing facility that will build the part in question. The outputs of AMFA are optimal manufacturing plans, their associated times and costs, and, in certain cases, recommendations to the designer on how to change the part for better manufacturing.

To generate the outputs, two distinct efforts are involved, which are referred to as Geometric Reasoning and Grammar Reasoning as shown in Figure 2. In geometric reasoning, first a CAD model in the STEP format (Part A in Figure 2) provided by designers is loaded. Then the geometry – comprised of vertices, edges, and faces – is translated into a label-rich graph which serves as the basis for the grammar reasoning (the lower portion in Figure 2). During the translation, a bounding box (Part B in Figure 2) is extrapolated from the original part A since one would likely start the actual manufacturing from a bounding raw stock. Then the original part A is subtracted from the bounding box B to create the negative volume (Part C in Figure 2) that is to be removed. The removal volume then undergoes further decomposition in order to generate compact sub-volumes where each is assumed to be machined in one operation or to be tagged as non-manufacturable. Finally the decomposed removal volume (negative solid) is converted to a graph, which is used as the initial seed in the grammar reasoning.



Figure 2: Flowchart of AMFA reasoning.

In the grammar reasoning, eight sets of grammar rules are invoked in a prescribed sequence in order to map specific elements that are detected in the seed graph to certain manufacturing details. This process continues recursively until all feasible manufacturing operations for the part are defined. The grammar rules reason about the manufacturability under certain foundry capabilities. First, all available manufacturing processes within a production facility are translated into grammar rules. The rules are then organized to

reason about the seed graph in order to determine its machining details. A search tree is drawn in Figure 2 to describe the reasoning. Steps in the tree represent alternative manufacturing operations for different sub-volumes. These operations are determined through the rules which detect prescribed graph elements in the seed and relate them to particular manufacturing processes. Each operation consists of the tool entry face, the feed direction, the tool type, the machine choice, and the proper fixture to machine one sub-volume. As the tree grows, more and more sub-volumes are effectively removed. This procedure continues recursively until there are no more sub-volumes available for machining, and a complete search space that includes all alternative manufacturing plans for the given part is derived. In addition, by translating the given foundry capability into graph grammar rules, a precise conclusion of non-manufacturability of a part can be made if the rules fail to find a feasible plan for this part. It signals that the manufacturing process is beyond the foundry capability and this part needs to be redesigned.

The geometric and grammar reasoning in AMFA is based on the following assumptions:

1) After decomposition of the negative solid, each of the resulting sub-volumes is assumed to be machined in one operation or to be non-machinable. Since the decomposition cuts the negative solid into a collection of convex sub-volumes, each subvolume represents a simple geometric shape (i.e. a cuboid, a cylinder, or a trapezoidal shape), which can be mapped directly to a tooling operation. For instance, a negative cylinder is a hole that can be created in a drilling operation, and a negative cuboid can refer to a pocket that is machined in one milling operation.

2) Tolerance is not considered in this reasoning of non-turning operations (i.e. milling, drilling, sheet-metal cutting, etc.). The high-level manufacturing plan generated from the reasoning provides a quick insight into how the profile of the input model can be

roughly created. It does not cover the final finishing processes, in which the tolerance information starts to be critical in deciding the tooling sequence in order to precisely create the final shape.

3) If a part is not manufacturable because of inaccessible regions (e.g. inner sharp edges) or unrecognized or invalid geometric elements (e.g. an edge with more than two vertices), then this part would always be tagged as non-manufacturable in the reasoning until the required redesign modifications are made by the users.

The following chapters in this part explain the geometric reasoning, the grammar reasoning, the fixture design, the plan evaluation, and the search optimization of the non-turning process planning algorithm. Case studies are incorporated into the description for better understanding. A summary of the characteristics and contributions of the work in this part is provided at the end.

Chapter 3: Geometric Reasoning

This chapter briefly describes the geometric reasoning that was developed by Eftekharian et al. [5]. As an upstream module of the overall system, the geometric reasoning in AMFA is customized by the grammar reasoning such that all necessary information required by the grammar reasoning is extracted from the CAD model and is passed to the grammar reasoning. While the author was not involved in the development of this module, a moderate introduction here will facilitate the explanation and understanding of the grammar reasoning.

In the context of CAPP, the volume decomposition is important and useful for generating simple removal volumes from the initial work-piece. These sub-volumes are commonly referred to as machining features in literature. In theory, a decomposed solid can be represented as the sum of sub-volumes in a hierarchical order that forms a complete object obtained from its boundary representation (B-rep). In this work we extend the idea of volumetric decomposition for 3D solid models by adding a level of reasoning to the algorithm. Our decomposition algorithm uses a ranking strategy to prioritize concave-edges, in which three heuristics are defined to evaluate the direction of cut for each division. As shown in Figure 3, the process of volume decomposition can be represented as an AND/OR tree [77] structure with branching factor equal or greater than 2 (2 is the case when there are exactly two solids generated after each cut) and the depth of the tree equal to the total number of concave edges in the solid. Each node represents a volume that needs to be cut and each branch represents a left (L) or right (R) cut in the tree. Nodes can refer to simple shapes (contain no concave edges) that are represented as (S) in the tree or complex shapes (contain one or more concave edges) that are represented as (C) in Figure 3. It is important to note that the "left" and "right" are

arbitrary names for the two faces that meet at each edge and they provide the reference cutting directions for decomposing the larger solid. Both options for slicing are evaluated to determine which direction (left or right) yields a better decomposition. The evaluation is based upon three heuristics as summarized below.

Heuristic 1: For both cuts (L versus R), if there are equal concavities in the resulting sub-volumes, prefer the one that leads to less volume difference. This method is responsible for cutting the solid in a direction that leads to more equally sized sub-volumes.

Heuristic 2: For both cuts, if the resulting volumes are non-convex, prefer the one (L versus R) that leads to fewer overall concave edges within the resulting sub-volumes.

Heuristic 3: For cuts that produce blind faces that an external tool cannot reach, the Visibility Test Analysis (VTA) is implemented. This heuristic prefers the cut (L versus R) that creates fewer (ideally zero) faces that are invisible from outside.



Figure 3: Volume decomposition tree.

For a given solid model shown on the top of Figure 3, consider a case where the left branch is always chosen as the preferred cut, and the results after the first cut could be one complex (C) and one simple (S) volume (as in Figure 3). The simple volume does not need any further cutting operations so the branch after this node is terminated: this is indicated as a red node in the tree. For each complex volume (C) the branch propagates further to lower levels until it is terminated at simple volumes (S). In order to find an optimal decomposed solid for use in the grammar reasoning, one can generate all the possible options in the tree and evaluate each individual option. This, however, is not
realistic since the Boolean operations are computationally expensive. Furthermore, the evaluation conceptually requires a human to inspect the result and decide if it is a good decomposition (computationally evaluating the quality may be possible, but it is out of the scope of the work). The alternative solution is to expand a single but promising branch. At each level of the tree the algorithm evaluates the options and decides the preferred direction to the next level. This continues until no more complex volumes are detected. It is important to note that a desired solution is described as a decomposed volume that contains sub-volumes which are suitable for manufacturing. In other words, each sub-volume should possess the following properties: 1) it should be of a compact shape with no or few concavities, 2) it should have a prismatic or close to prismatic geometry and 3) it should be machinable in one machining operation. Due to the lack of space, details about the algorithm are omitted here and we refer the interested reader to [5]. Based on the aforementioned heuristics, only desirable branches will survive and continue to grow until no further concave edges are recognized. The final decomposed shape is a combination of all remaining S-type volumes in the decomposition tree. The decomposed solid at the bottom of Figure 3 is a sample result after the heuristic-guided volume decomposition of the input solid model.

Chapter 4: Graph Grammar Based Reasoning

In this chapter, we explain in detail how the input 3D geometry and the nonturning operations are represented with graph grammar using GraphSynth. Section 4.1 presents the seed lexicon that uses the graphical elements (e.g. nodes, arcs, and hyperarcs) to capture all geometric information of the input model that is relevant to manufacturing process planning. The machining operations are translated into specially designed grammar rules, which then perform process planning reasoning as illustrated in section 4.2.

4.1. SEED LEXICON

After the removal volume (negative solid) of a given solid model is decomposed, the compound solid comprised of different sub-volumes has to be translated into a seed graph such that the grammar reasoning can reason on it. Rather than using existing graph techniques to represent a solid model, a new lexicon is proposed in this work. Figure 4 gives an example showing how part A in Figure 2 is represented as a label-rich graph.

This is a simple shape with a pocket in front and a through hole on the back. In the seed graph, geometric elements are described by nodes, arcs, and hyperarcs. Nodes are used to represent vertices and faces. Arcs are used to represent edges as well as to indicate relative positioning information (i.e. parallelism, perpendicularity, etc.) between any two faces. A hyperarc is a special graph element in GraphSynth. While an arc can only connect two nodes, a hyperarc can connect as many nodes as needed. In the seed lexicon, it is used to connect all vertices belonging to a face to their face node. Figure 5 gives an example of a graph representation for a face with four vertices. The node 0 (indicated as n0) with label "*face*" and "*accessible*" represents a face that is exposed for the tool to enter. The other four nodes (n1, n2, n3, and n4) represent all the vertices of

this face. They are connected by hyperarc 0 (*ha0*), which also has label "*face*" and "*accessible*". The labels are used to distinguish a hyperarc that defines a face from the one that defines a volume (described below) in the lexicon.



Figure 4: Part A in Figure 2 as a seed graph.



Figure 5: A sample face representation in the seed lexicon.

Another type of hyperarc is defined to encompass a sub-volume by connecting all the nodes in a sub-volume together. The nodes can be the face nodes as well as the nodes denoting vertices. For example, in Figure 4, the hole and the bottom cuboid are separated by two hyperarcs. By using nodes, arcs, and hyperarcs in the seed graph, all geometric information about vertices, edges and faces for a solid model is stored and mapped to the graph. The face nodes are used in the seed and rules to refer to machining features, like holes, pockets and slots, if applicable. Mapping edges and vertices to graph elements provide more detailed information about shapes and geometries, which is essential for the rules to be able to reason about manufacturing operations more precisely.

It is also important to note that a variety of labels in the graph that are assigned in the geometric reasoning are used to store topological, rather than parametric, information. By reasoning about the labels selectively, the grammar reasoning can extract enough information for the manufacturability analysis for a given geometry. As a result, the geometric computations can be avoided in the grammar reasoning.

For example, a face node may have a label "bb", which indicates that this face is a bounding box face. When a face node represents a face that belongs to the removal volume, it is assigned the label "neg". For instance, in Figure 4, the face node 1 (n1) (not explicitly shown, but overlaps with its face hyperarc ha1) representing the bottom face of the cuboid has a label "neg", while face n12 has a label "bb". Besides, the face adjacency property – "convexity" or "concavity" – between any two adjacent faces is also stored in the label of their common edge. These labels are essential to inform the search of feasible machining operations for a given sub-volume.

Another important function of labels is to guide the sequencing of machining operations for different sub-volumes. The following labels are designed to support this functionality. First, a hyperarc that denotes a face will have a label "accessible" if the face is reachable by the tool. Such face is a candidate for the tool to enter. Examples can be found in hyperarcs *ha1* and *ha9* in Figure 4 and hyperarc *ha0* in Figure 5. Second, for a given face, if its entire area is shared by more than one sub-volume, the face hyperarc that represents this face will be given a label "common". When it comes to the case where only a partial area of this face is common with other sub-volumes, the specific portion, which is represented by a new hyperarc, will have the "common" label. An example can be found in the hyperarc *ha7* in Figure 4, where it represents the internal circular face of the hole that is shared by the bigger face of the cuboid that the hole sits on. The idea of the sub-volume removal sequencing is that: 1) a sub-volume is manufacturable from only its accessible faces; 2) after one sub-volume is machined, all the remaining "common" faces that are attached to this sub-volume become "accessible"; 3) the newly-generated accessible faces can serve as the tool entry faces for

the adjacent sub-volumes that are to be machined next. Following these three steps, the feasibility of volume removing sequences is guaranteed.

A list of all labels defined in the grammar reasoning is given in Table 1. With these labels, the grammar rules are able to perform precise reasoning about the graph elements in order to define complete and feasible manufacturing plans. Detailed explanation of the rule based reasoning is presented in next section.

Geometrical				
element in	Description	Related Labels	Explanation	
the seed				
	Represent a face	machining_sta rt	This face is chosen as a tool entry face	
		common	This face is shared by two or more sub- volumes	
		face	Indicate this node represents a face	
		bb	This face is a bounding box face	
Face node		neg	This face is a surface of the negative solid	
		planar	This face is a planar face	
		non_planar	This face is not a planar face	
		fillet	This face is a fillet face	
		cylindrical	This face is a cylindrical face	
		machined	This face is machined	
		fixed	This face is fixed	
Easo are	Connect two	parallel	Two faces are parallel	
race are	faces	perpendicular	Two faces are perpendicular	
Connect Face together all		original	Indicate the face this hyperarc represents is accessible	
hyperarc	elements of a	face	Indicate the geometric element this hyperarc	
	face	lace	represents is of type face	
Edge arc	Represent an edge	tangential	Indicate the two adjacent faces this edge	
			belongs to are tangential to each other	
Luge ale		convex	The two adjacent faces this edge belongs to	
			are convex to each other	

Table 1:Labels and their definitions in AMFA grammar reasoning.

Geometrical			
element in	Description	Related Labels	Explanation
the seed			
		concave	The two adjacent faces this edge belongs to are concave to each other
		common	This edge is shared by two or more sub- volumes
		accessible	This edge is accessible to the tool
		curved	This edge is not a linear edge
		onedge	This vertex is on an edge of bounding box
Vertex node	Representing a	neg_vertex	This vertex is a vertex of the negative solid
	vertex	boundingbox_ vertex	This vertex is a vertex of the bounding box
	Representing a	convex shape	Indicate that this hyperarc refers to a sub-
	sub-volume by	convex_snape	volume
Sub-volume	connecting all		Indicate that the sub-volume this hyperarc
hyperarc	elements of a	current_shape	represents is the current sub-volume that is
	sub-volume		being machined
	together	machined	Indicate this sub-volume has been machined

Table 1 (continued): Labels and their definitions in AMFA grammar reasoning.

4.2. RULE DEVELOPMENT

In this section, eight sets of grammar rules are designed to simulate a virtual machining process; that is, removing sub-volumes of the compound solid in a hierarchical order. This material removal process stops when the volume of the compound solid goes to zero. These rule sets are arranged in a specific order such that they collectively perform the required reasoning as a whole. The tasks of each rule set are summarized in Table 2, and we explain some of them in detail as follows.

Rule set index, name,		Task
(number of rules contained)		
		Prepare the seed graph before grammar reasoning starts
0.	$\mathbf{Preprocessing}(5)$	(check the seed graph, fix wrong labels, delete dangling
	r reprocessing (5)	arcs, identify and isolate non-material-removal
		operations, etc.).
1	Choose sub volume	Choose an accessible region as current sub-volume to
1.		start the machining; if no sub-volume is found, go to rule
	(1)	set 7.
2.	Choose tool entry	For current sub-volume, define a face for the tool to
	face (1)	enter. The tool feed direction is also identified based on
3.	Validate tool entry	the tool entry face normal and the sub-volume accessible
	face (4)	directions.
		Choose an available tool that can perform the machining
	Choose tool type (8)	of current sub-volume. The rules identify necessary
		geometric information from the sub-volume and match it
4.		to available tool types that are defined by each rule (e.g. a
		cylindrical feature is mapped to a drill bit or an end mill
		tool).
		Based on the tool feed direction, the tool type and the
5.	Choose machine and	sub-volume, the rule set identifies all possible machines
	fixture type (6)	and fixtures that are capable of conducting the tooling
		operation defined in rule set 4.
		Perform clean-ups and updates of the seed graph (e.g.
		label the sub-volume as machined, delete graphical
6.	Postprocessing (5)	elements that are unique to the removed sub-volume, etc.)
	B (1)	in order to complete the virtual manufacturing process of
		current sub-volume.
		If this rule set is invoked, all the sub-volumes of the seed
7.	Goal check (1)	graph have been removed. The rule set informs the search
		that a candidate manufacturing plan is found
		mai a candidate manufacturing plan is found.

Table 2: Description of rule sets and their tasks.

The first rule set (rule set 0) aims to recognize typical sub-volumes (counter-sink, round-edges, etc.) as well as non-traditional machining operations (bending, etc.) and tag them for later use. These features are usually machined in the final finishing processes

using specific tools. By recognizing and isolating these special cases at the initial stage, more realistic manufacturing plans, which separate roughing and finishing passes, can be generated. Unlike other machining operations, bending operations do not remove any material but rather change the initial part geometry and hence change the seed graph. It affects the generation of a correct bounding box for a given part. In such situation, the rules in this rule-set operate in conjunction with the geometric reasoning to pre-define these non-material-removal operations on the part such that a correct bounding box can be generated.

The third and fourth rule sets (rule set 2 and 3) are used to identify a feasible tool entry face from which the current sub-volume selected by rule set 1 is machined. In rule set 2, a single rule is designed to capture any face accessible to the tool. If such a face is found, it is labeled as a *"machining_start"* face. If no faces are found at this stage, the process terminates – there are no sub-volumes that are left to machine or are accessible. Rule set 3 consists of 4 rules, representing several special cases where a tool entry face previously selected in rule set 2 needs to be re-checked. The idea is that an accessible face is not allowed to be chosen as a tool entry face if the corresponding sub-volume cannot be fully removed from it. For example, an infeasible tool entry face is shown in Figure 6. If the hole is first removed, the internal circular face of the hole that is shared by the front pocket becomes accessible. However this face is not a valid tool entry face is considered as a valid face to begin the machining in rule set 2, it is invalidated in rule set 3.



Figure 6: An example of infeasible tool entry face.

A second example is provided in Figure 7 to illustrate another scenario where a tool entry face is not a valid option. The original solid in Figure 7a was provided by research partners in Arizona State University. The compound negative solid comprised of all decomposed sub-volumes is shown in Figure 7b. There is a beam-shaped sub-volume (the green shape) lying on top and across the entire length of the negative solid. If the tool enters from the top and feeds downward (indicated as the black arrow), then all the transverse sub-volumes that this beam sits on (from left to right: the dark yellow, gray, dark blue, and dark pink sub-volumes) are not fully removable since the tool cannot access the material underneath the beam. Therefore any accessible face on top cannot be chosen as a feasible tool entry face.



Figure 7: Another case of infeasible tool entry face.

After rule set 2 and 3, a feasible tool entry face is identified and the reasoning moves to rule set 4, which is responsible for the tool type selection. Rule set 4 is a cluster of available non-turning operations, including drilling, milling (end-milling and ball milling), sheet metal cutting (i.e. water jetting), counter-sinking, etc. Each operation corresponds to one or more rules in this rule set. These rules are specially designed based on physics of each tooling operation.

For example, in this rule set there are two drilling rules as shown in Figure 8. The reason for creating two rules is that there are two different representations for holes in the STEP files. The planar circular face of a hole can be represented with either two vertices and two semi-circular edges (type 1) or one vertex and one full circular edge with 360° angle (type 2). Figure 8a captures the first type hole: the left hand side (LHS) of this rule attempts to find a hole by capturing its cylindrical face (a hyperarc labeled with *"cylinder"*) and one of its planar faces, which is accessible by the tool and is denoted as another hyperarc labeled with *"machining_start"*. Additionally, since this hole is a subvolume to be machined, its sub-volume hyperarc (a hyperarc with label *"convex shape"*)

is also captured. If such a hole is found, a drilling operation is invoked on the corresponding sub-volume. This is realized by a virtual transformation from LHS to RHS of the rule. After that, the hyperarcs of "*machining_start*" face and "*convex_shape*" sub-volume are tagged as "*machined*". Figure 8b is the drilling rule for the second type hole. Similar reasoning is encapsulated in the rules for the remaining tool types where the complete left hand sides have been developed to capture the intricacies of the geometric constraints.



Figure 8: (a) Drilling rule 1 for type 1 hole, (b) drilling rule 2 for type 2 hole.

After a tool is selected for a sub-volume, this sub-volume is marked as *"machined"*. Then the reasoning moves to rule set 5, in which the corresponding machine and fixture (used to conduct current tooling operation) are selected. These decisions are made in one single rule by considering which face to locate and which faces to clamp from the geometry. Details of the machine selection and the fixture design are given in next chapter.

After the fixture design and machine selection, rule sets 6 is designed to perform post-processing and clean-up tasks, like adding new "*accessible*" labels to those faces that become exposed to the tool after certain sub-volumes have been removed, in order to facilitate further reasoning.

After rule sets 6, one complete step in a manufacturing plan is defined to remove one sub-volume. Next, the algorithm iterates to rule set 1 to start another loop for a different sub-volume. The complete reasoning is shown in Figure 9. If all the subvolumes for a given part are machinable, the similar loop for each sub-volume is performed until all are machined. At that time, since there are no more sub-volumes to be recognized by rule set 1, the reasoning will terminate at rule set 7 by returning a complete manufacturing plan.



Figure 9: Grammar reasoning flowchart in AMFA.

Conversely, as seen in Figure 9, instead of finding a complete plan, the reasoning may be terminated at different stop-points defined by different rule sets. Depending on the functionality of each rule set, the reasoning can end when there are no rules applied in a particular rule set (i.e. rule sets 2, 4 and 5), or when a particular termination rule is triggered (i.e. rule set 3). For the first scenario, for example, the loop may stop if there is no tooling operation identified in rule set 4 for a particular sub-volume. This situation provides an insight to the user that the current sub-volume being machined is actually not manufacturable with current available tools (defined in rule set 4). Since a foundry capability is always mapped into different tooling rules, it is reasonable to conclude that manufacturing this part is beyond the existing foundry capability. In this case, one has to re-design the part to make it manufacturable (i.e. add or remove certain round edges), or the complementary machines and tools need to be added to the foundry in order to cover

required operations. For the second scenario, for instance, the rules in rule set 3 define several infeasible cases for tool entry face selection. If any of these rules is invoked, the tool entry face selected in rule set 2 will be invalidated, and the search will be terminated after this rule is triggered.

Therefore, depending on the geometry of the given part and the knowledge of the manufacturability analysis built in the rules, a complete process described in Figure 9 will either succeed with a feasible manufacturing plan, or find no plan. One should also be aware that a complete loop from rule set 0 to 7 represents only one branch of the search tree in Figure 2. The whole search process represented by the tree actually contains numerous branches and therefore the search space grows exponentially with the complexity of the geometry. Chapter 6 elaborates in detail how the size of the search space is managed while the search effectiveness and efficiency are achieved.

Chapter 5: Fixture Design and Plan Evaluation

In manufacturing process planning, it is critical to ensure that the manufacturing dependency between process planning and fixture design is assessed before a conclusion regarding the optimality of a plan or the quality of a proposed fixture can be made. In this chapter, we propose a concurrent reasoning for generating optimal fixture designs for a manufacturing process plan [8]. It consists of two efforts. First, several grammar rules are developed to encapsulate the knowledge that is critical to generate feasible fixture mechanisms for a particular operation. A fixture mechanism provides a locating face and one or two clamping faces depending on which clamping mechanism the fixture uses to secure the work-piece in order to conduct current operation. The rules are included in rule set 5 so that the reasoning is seamlessly synthesized with the other rules to perform concurrent reasoning about the manufacturability of an input model.

In the second effort, the candidate operations with fixtures being generated in the grammar reasoning are sent to an evaluation module, where each operation is measured with respect to the manufacturing time, cost and fixture quality. For a given operation, the time and cost needed can be estimated using both empirical and theoretical models that are available in many engineering handbooks [78]–[80] and this implementation has been reported separately in Van Blarigan's work [81]. The fixture quality, however, is uniquely defined in this work in order to provide a consistent and complete assessment of a given fixture for an operation. The assessment is based on a collection of fixture design guidelines that the author gathered from existing fixture design manuals [82]–[84]. As confirmed from the experience in machine shop, these guidelines address common concerns during the manufacturing processes (e.g.: stability, stress distribution, accessibility, ease of implementation, etc.). The idea behind this is that by translating the

empirical and widely-followed fixture design guidelines to quantitative metrics, the candidate fixture mechanisms defined in the grammar reasoning can be thoroughly evaluated in a way closely resembling the actual manufacturing practice.

The work in this chapter sees major contributions in the following aspects:

1) We demonstrate an efficient and effective rule-based fixture design algorithm as applied in the automated manufacturing process planning. For small one-off machine shops, the plans are readily implementable; for modular and dedicated fixture unit designs, the proposed fixture mechanisms provide optimal regions for setting up the locating and clamping;

2) We identify the dependency between the fixture design and the manufacturing process planning, and show via examples that the dependency is critical in defining optimal and practical process plans;

3) We use manufacturing knowledge and experience to guide the generation of optimal and practical fixture designs and process plans. This way, the multi-disciplinary problems in the early fixture design phase are avoided.

5.1. DEFINING FIXTURE CANDIDATES WITH GRAPH GRAMMAR

A fixture design includes the selection of a locating face and one or several clamping faces. The locating face refers to a face of the work-piece to be seated on machine table, and the clamping faces are used to hold the work-piece firmly engaged with the locating face during the machining. The fixture configurations considered in this work are categorized into downward clamping (Figure 10a) and side clamping (Figure 10b) as suggested in [82]. The downward holding mechanism needs one clamping face and the side clamping requires two faces for clamping.



Figure 10: Downward clamping and side clamping as applied on a work-piece.

Multiple rules are designed in rule set 5 with each defining a particular fixture mechanism. Figure 11 is a screenshot of one rule that defines a downward clamping mechanism in a vertical machining center (VMC). The rule is of the form L-to-R while the left side of the rule specifies all the elements and conditions that need to be found and satisfied in the seed graph in order to invoke the rule. The right side of the rule defines necessary transformations on these elements that will be imposed by the rule. As shown on the left, the rule needs to find three faces (denoted as "n0", "n1", "n2") in the seed graph that are parallel with each other (parallelism is imposed by arc "a0" and "a1" with label "parallel"). One face (denoted as "n1") must have a label "tool entry", which indicates that this face has been chosen by rule set 3 as the tool entry face for current subvolume. The other two faces (denoted as "n0" and "n2") do not have any label constraints; therefore the rule will identify all pairs of accessible faces in the seed graph that are parallel to the tool entry face. On the right side of the rule, one of the two faces (in this case "n2") is assigned a label "*fixed*", meaning this face will be used as the locating datum; and the other face "n0" is assigned labels "downward" and "clamp", saying that this face will be used as the downward clamping face. Meanwhile, a global label "VMC" (on top of the right side of the rule) is assigned to the seed graph, informing the later reasoning that a vertical machining center has been chosen for the current operation. Note that the parallelism between the tool entry face "n1" and the locating face "n2" ensures a VMC is invoked, and the parallelism between the clamping face "n0" and the locating face "n2" specifies a downward clamping mechanism. As the rule is applied on the seed graph, all possible downward-clamping fixture mechanisms in a VMC are invoked for current operation.



Figure 11: Screenshot of a rule in rule set 5. This rule defines a downward clamping fixture in a vertical machining center.

Similarly, Figure 12 shows a rule that defines all possible side-clamping fixtures in a VMC. There are additional rules in this rule set that define the two types of fixtures in a HMC (horizontal machining center) and higher-axis machines, respectively. For higher-axis machines, the faces for fixture are not necessarily parallel or orthogonal with each other. In this case, the precise orientation of each fixture face is computed as well by the rules. All knowledge and information captured in this rule set will be passed "on the fly" to following rule sets in order to enable and facilitate further reasoning.



Figure 12: Screenshot of another rule in rule set 5. This rule defines a side-clamping fixture in a vertical machining center.

5.2. EVALUATING FIXTURE CANDIDATES

After the candidate fixtures are generated, next task is to measure the quality of each candidate against a set of consistent and meaningful metrics. According to Joshi [82], a proper fixture design needs to be validated against several criteria. For locating, it has to comply with the part's dimensional requirements, and therefore machined faces are preferred to set up the locating frame due to their relatively higher precision. Second, the fixture needs to impose necessary constraints on the work-piece to ensure the part stability during machining. Third, several common engineering concerns (strength, part deflection and distortion, stress distribution, etc.) need to be addressed before a fixture mechanism is actually mounted in a machine. As the fixture analysis overlaps with many disciplines, it is hard to incorporate all issues in one fixture analysis module.

To tackle the problem, we view the fixture analysis directly from manufacturing perspective. Despite the numerous issues in the early fixture design phase, a list of

guidelines that are used in the machine shop to facilitate the quick assessment of fixture mechanisms have been generalized. As shown in Table 3, each guideline takes into account several design criteria and is converted to a metric against which a candidate fixture can be evaluated. Note that more design guidelines can be added to cover more aspects of the fixture design.

Guidelines summarized from	Design criteria	Evaluation metrics
[82]–[84]	Design enterna	(optimization strategy)
Available area for fixture faces (locating face, clamping faces, and tool entry face): larger is better	Stress concentration, clamping distortion, stability, etc.	Face area (maximize)
Overlapping area between two parallel fixture faces (e.g. locating face and tool entry face, two clamping faces, etc.): larger is better	Clamping torque, stability, cutting torque, clamping distortion, work-piece deflection, etc.	Overlapping area between two faces (maximize)
Distance between two parallel fixture faces (e.g. locating face and tool entry face, two clamping faces, etc.): larger is better	Stability, resultant torque due to cutting forces, etc.	Distance between two faces (maximize)
Spindle angle: smaller is better	Tool deflection, ease of fixture, etc.	Spindle angle (minimize)
Face type: primitive features (planar, cylindrical, etc.) are better	Ease of fixture, stress distribution, etc.	Face type (if not a primitive feature, assign penalty)

 Table 3:
 Fixture design guidelines and evaluation metrics.

Next, a set of penalties are set up in Table 4, which represents extreme cases of fixture design that need to be avoided. For example, Figure 13 gives a case where the inaccessible penalty is assigned. Most penalties can be viewed as the consequences when the metrics in Table 3 approach their extremes or singularities (i.e. the distance between two faces is 0; the overlapping area of two faces reduces to 0; etc.). In addition, the Not-primitive-penalty is assigned when the fixture face is not a primitive feature (i.e. planar face, cylindrical face, circular face, etc.).

Cases to penalize	Instances	Assigned penalty
Invalid operations or fixture	Inaccessibility Penalty	10000
Need substantial change in	Coplanar penalty	1000
fixture mechanism	Tiny face penalty	1000
Require additional auxiliary	Not primitive penalty	100
jigs	Bad orientation penalty	100
Potential static or dynamic	No overlapping area	10
mechanics problem	penalty	-

 Table 4:
 Extreme cases that are penalized in fixture quality measurement.



Figure 13: A case where the inaccessibility penalty is assigned.If we are to remove the pocket from top down, we do not want to use the top shadowed face as the locating face as it will block the tool entry direction.This case happens when the distance between the tool entry face and the locating face reduces to 0 (i.e. they are coplanar).

The penalty assigned to each case has been carefully tuned based on the tests on real parts to reflect the extent of infeasibility. The measurement is based on the complexity and possibility of setting up a given fixture design. Cases with lower penalty are easy to implement, but there may be some minor engineering concerns associated with them. Cases with higher penalty are typically very hard, if not impossible, to set up. The penalty levels are scaled by a factor of 10 such that each extreme case holds a separate digit position. A side benefit is that by looking at the accumulated result after evaluation, one can directly tell how many critical constraints the current design violates and need to be resolved.

For each candidate fixture, a *"fixture quality"* synthesized from the evaluation metrics is assigned. Since the quantity is treated as an objective to optimize in the search, it needs to be monotonic [85]. That is, it should be monotonically increasing with a lower value indicating a better fixture design. In order to achieve this, we take the reciprocals of the metrics that are to be maximized and aggregate them with metrics to be minimized. To compute the fixture quality, first it is initialized to zero. Then for every fixture design,

Table 5 is traversed to identify which cells are applicable and need to be computed. All the results will accumulate to form the final value of fixture quality. Note every cell in the table is bounded by a corresponding penalty, which is used to capture the extreme case.

Table 5:All computations needed to form the fixture quality.Note that θ_{ref} , A_{ref} and L_{ref} in the table are the reference spindle angle,reference face area and reference length, which are used to normalize eachevaluation result to a unitless quantity.

Metric		Evaluation				
		Entry face	Locating face	Clamping face 1	Clamping face 2	
Overl- apping area	Locating face	A_{ref} /overlapArea \leq No Overlapping Penalty				
	Clamping face 1	A_{ref} /overlapArea \leq No Overlapping Penalty	A_{ref} /overlapArea \leq No Overlapping Penalty			
	Clamping face 2			A_{ref} /overlapArea \leq No Overlapping Penalty		
Dista- nce	Locating face	L_{ref} /dist \leq Inaccessibility Penalty				
	Clamping face 1		<i>L_{ref}</i> /dist ≤ Coplanar Penalty			
	Clamping face 2			L_{ref} /dist \leq Coplanar Penalty		
Face area		A_{ref} /faceArea \leq Tiny Face Penalty	A_{ref} /faceArea \leq Tiny Face Penalty	A_{ref} /faceArea \leq Tiny Face Penalty	<i>A_{ref}</i> /faceArea ≤ Tiny Face Penalty	
Face type		If not primitive: Not primitive penalty	If not primitive: Not primitive penalty	If not primitive: Not primitive penalty	If not primitive: Not primitive penalty	
Spindle angle θ		$\theta/\theta_{ref} \leq$ Bad orientation penalty				

5.3. PLAN CONSOLIDATION

One assumption made in the reasoning is that each sub-volume can either be machined in one operation or be non-machinable. However, a more realistic process plan relies heavily on the type of operations and tools selected rather than the geometric features, which are represented as sub-volumes in our case. In general, an actual manufacturing process always starts with a roughing process in which the removal volume is machined as much as possible. Such manufacturing knowledge is modeled in our reasoning by consolidating the generated manufacturing plans into fewer steps that resemble the roughing passes of realistic plans.

The idea is to integrate similar manufacturing operations in a plan into one unified roughing pass. Given the current setup and tool, the reasoning detects all manufacturing operations in the plan that can be implemented at one time and integrates them as one step. To collapse the list of machining operations to only the number of unique part setups in the process plan, we introduce a rule that operations requiring a re-fixture of the part represent new setups, and cannot be combined with the previous operations. This is a simple check to perform since in our algorithm the machine operations hold a Boolean (i.e., true or false) for re-fixturing. Re-fixturing is set to true if any of the tool, the machine and the fixture has changed, as doing such requires the re-orientation, realigning and re-fixturing of the part. Therefore, re-fixturing will only ever be false if the operation is in the same tool, the same machine and the same fixture as the previous operation. If this is the case, the two operations can be combined.

An example of two operations that can be combined is shown in Figure 14. As compared with plan I that requires two steps, the condensed plan II suggests only one step to machine the pocket and the hole, which is more realistic from the human perspective. It is also beneficial as it saves time and cost in manufacturing since we do not need to re-fix the part when we continue machining the hole after the pocket.

Initial raw stock (left) Final shape after machining (right)







Plan I - Step 2: mill out the front pocket from left





Plan II - Step 1: mill out the pocket and hole from top



Figure 14: Comparison of two plans with and without consolidation.

Chapter 6: Multi-objective Hierarchical Sorting based Best First Search

This chapter elaborates the search technique [8] that was developed to efficiently find the near-optimal and empirical process plans among a huge space of solutions defined by the grammar reasoning.

6.1. INTRODUCTION

CAMPP is a challenging task since it involves a large search space that contains all possible process plans for an input part. One way to represent the space of plans is with a tree structure (as depicted in Figure 15). The top of the tree is the initial state from which the search process starts. The state can imply an input CAD model for machining process planning, or a product assembly for assembly and disassembly planning. Every level of the tree represents a step that specifies a particular manufacturing detail that will later constitute a complete process plan. Multiple branches at each level represent alternative options that are identified for a particular manufacturing detail. For example, in machining process planning, one level can be designated to define an accessible region in the solid model for the machining to start and every possible region in the CAD file has its own branch at that level.



Figure 15: A tree structure of the search space in process planning.

The task is to find the complete and optimal process plans among the huge search space. A complete process plan is essentially a path from the top of the tree to the bottom. While uninformed search (such as Depth-first search) can be used to enumerate all possible plans, an informed search (e.g. A*) can be used to more quickly find the optimal plan.

To characterize the optimality of a plan, manufacturing time and cost are usually used as evaluation metrics. Additional metrics may be added depending on which problem domain within CAMPP one is solving. For assembly planning, the work load imposed on labors needs to be carefully assessed. For the machining process planning that the authors are studying [3], two more metrics are introduced: a unitless *"fixture quality"* which evaluates the quality of fixture designs for a process plan against manufacturing constraints, and a *"remaining volume of material"* factor which measures how much material left to remove after every operation. With these criteria, the informed search is a multi-objective optimization problem, where the preference over each criterion needs to be articulated. Different optimization algorithms were summarized in [86], among which the weighted sum method is widely-used and effective to consolidate multiple objectives into one:

$$U = \sum_{i=1}^{k} w_i F_i(x)$$

where $F_i(x)$ is the *i-th* objective and w_i is the weight associated with the objective. As long as w_i 's are positive, minimizing U will give pareto-optimal solutions [87]. The problem in CAMPP domain – as in many real-world applications – is that the objectives are in different units, and some normalization technique has to be used in order to consolidate these objectives. Second, there is usually no clear preferences over the objectives from manufacturing that could tell the research how to set up the weights. As the manufacturing knowledge is not well captured in the subjective setting of weights, the optimal process plans found using a best first search technique are often not consistent with the manufacturing practice, and are not readily implementable in a machine shop.

In this chapter, a hierarchical ordering based best first search algorithm is proposed to solve the multi-objective CAMPP problems. The hierarchical method in solving optimization problems defines a hierarchical order of the criteria, and the criteria on top have the authority to strongly affect the performance of other criteria [88]. Based on the hierarchy, the objectives are solved one at a time:

$min F_i(x)$

where *i* represents the position of corresponding objective in the preference list. As an extension of Stackelberg strategy [89], the hierarchical optimization has been widely studied in various areas [90], [91], and the assessment of its performance is available in [92]–[94].

In this work, we establish the hierarchy of the evaluation criteria, and the promising branch of the tree that the search algorithm chooses is defined by the criteria hierarchically. We will compare the performance of the hierarchical search in manufacturing planning with A* search through examples. The observation from this work is that by incorporating the manufacturing knowledge and practice into the hierarchy of the objectives, the new search is able to find optimal yet practical solutions in near-linear time.

Three major contributions are summarized from this work:

1) We demonstrate an effective and efficient hierarchical ordering based best first search algorithm as applied in the automated manufacturing process planning.

2) We show via examples that the search effectiveness can be greatly improved by customizing the search with particular engineering knowledge.

3) We demonstrate that the multi-objective optimization problem can be effectively solved with hierarchical ordering of evaluation metrics. The dependency of the optimality of solutions on the weight associated with each metric is removed.

The chapter is organized as follows. Next section talks about the hierarchy of four evaluation metrics and the sorting strategy used in the search. Then the search efficiency and practicality are discussed in detail. The characteristics of the search are validated through two case studies and observations from the results. The chapter ends with a summary of the algorithm.

6.2. SEARCH HIERARCHY AND SORTING STRATEGY

Four metrics are set up to evaluate the optimality of a manufacturing process plan: the manufacturing time, the manufacturing cost, the fixture quality and the remaining volume under current operation. While the search is traversing down the tree, we want the accumulating plan to consume as little time and cost as possible. For the fixture penalty, it is converted from a set of fixture design guidelines collected from engineering handbook and machine shop experience. It gives a comprehensive assessment of the fixture designs proposed by our manufacturing process planning tool.

The remaining volume under current operation is treated as a heuristic that leads the search quickly to the optimal solution. One goal during the search is to reduce the remaining volume as much as possible after every step. It is a reflection of the real machining practice in which we want to remove as much material as possible before we have to change the setup to initiate next operation. For example, to start the machining of the part in Figure 16, two alternative plans are defined in the search space as shown in Figure 14. Given the raw stock, plan I suggests drilling the holes from right as the first step and then milling the pocket from left as a second step. Plan II suggests creating the pocket and the hole from top in one step. While both options are implementable, plan II is better as it saves time and cost by removing more material within the initial setup. This option also puts the plan closer to the final solution as less material (in this case no material) is left to remove as compared to plan I.



Figure 16: An illustrative part.

Figure 17 shows the search queue structure and the evaluation strategy based on the hierarchical sorting of metrics. The hierarchy of the metrics is set up as follows: the options in the search space are sorted by the remaining volume, and then by the fixture quality, followed by the machining time, and last by the machining cost. Sorting on remaining volume first guarantees a quick convergence of the search to complete machining process plans. For candidates with the same remaining volume, they are next ordered by fixture quality – thus putting a priority on fixturing, which is a significant chore in machining. One does not want to generate any plan that later is shown impractical because the fixtures are too complicated – if not impossible – to create within machine shops. After this, the time and cost are evaluated. The time goes first because – given a machine shop – the facilities, labor, and overhead are based on this. Shorter machining time directly lowers the cost. While there are often negotiations over the cost with clients, the time is a more sensitive factor to manufacturing engineers. With the manufacturing background knowledge embedded into the hierarchy of the metrics and sorting strategy, the purpose is that the search is better informed to find optimal yet practical plans.





6.3. SEARCH EFFICIENCY AND PRACTICALITY

As a general concern, the tree search algorithms usually encounter an exponentially increasing search space. As in manufacturing process planning, with the increase of the input part complexity, more and more steps are needed to create the final shape, which means more levels of the search tree in Figure 15. Therefore the branches that the search needs to traverse grow exponentially. In this case, how to find the best solutions faster than the propagation of the search space is a challenging problem. In this work, two concepts are introduced into the hierarchical search for the purpose of improving the search efficiency in find near-optimal process plans. While finding the true optimal solution would be best, any effective and sensical plan will often differ only slightly from the optimal.
6.3.1. List Reordering Based on Limits on Objectives

A limit is used to deter the search from considering states that have one of the four objectives above a specific cutoff value. This introduces practical engineering heuristic into the otherwise naïve search algorithm. For example, a limit is set for the fixture quality. Referring to the additional fixture quality check in Figure 17, if the fixture quality is larger than the cutoff value, the search will immediately move the candidate to the bottom of the search queue regardless of where the hierarchical sorting places the candidate (which would be with others that have identical remaining volume). This makes the process more efficient and leads to more practical results since these highly unlikely plans are not expanded in the tree search at the time of others with like volume. This fixture cutoff is prescribed to a value corresponding to a likely infeasible fixture.

The computational resources saved by the cutoff are thus relocated to expanding other branches in the search space. The concept is also extended to the third and fourth heuristics: time and cost, but there appears to be little impact on the results or speed. Naturally, it does not make sense to apply such a strategy on the first heuristic (remaining volume) since solutions of high value are already at the bottom of the search queue. This approach should be considered in any hierarchical search in order to ensure that time is not wasted on candidates that – while having good values for their first objective – have very poor values for the other objectives.

6.3.2. Search Queue Truncation

Another modification is to place a limit on the maximum length of the search queue. As shown in Figure 17, any candidates that are outside of the maximum queue are discarded. This has the obvious effect of making the search more efficient while preventing problems with handling more solutions than is budgeted. For this particular problem, we show via examples that the optimality of the solutions is not affected by the imposed incompleteness of the search space for two reasons.

First, in hierarchical search, the candidates at the bottom of the queue are those with more remaining volume, larger fixture quality, longer machining time, and more cost as well as those exceeding aforementioned cutoffs. These non-optimal states do not contribute to the generation of optimal or best plans as measured by the metrics.

Second, in CAMPP problem, a complete process plan involves a diverse set of decisions, such as accessible regions to start an operation, feasible feed directions for the tool, available machines to use, available tools to use on each machine, and the fixtures to secure the part during the operation. So, it requires at least 5 levels of the search tree to fully specify a given operation with each decision having a branching factor, b, that is adequately large (b > 5). Therefore, the first complete operation may have over 3000 options (3125 = 5^5). As such, truncating seemingly poor partial states is a necessary process. It is theorized that for the problem at hand, there is a strong consistency between local decisions and their impact on complete plans. There does not appear to be the situation in manufacturing planning that sometimes inflicts other path-planning problems, such as in traversing a maze where "going south first" may be the best way to "go north in the end".

6.4. CASE STUDIES

The hierarchical search algorithm is characterized in terms of optimality, practicality and efficiency through two case studies and observations.

6.4.1. Example 1

Consider the part shown in Figure 18. The optimal process plans found by hierarchical search is compared with the results from an A* search algorithm using weighted sum method to consolidate the evaluation metrics. To limit the memory use and maintain the efficiency, the search queue length is limited to 600.



Figure 18: Example part 1.

Table 6:	Comparison between hierarchical search and A* search for example 1.
	Maximal queue size is set to 600.

Experiment		Total solutions	Quality of optimal plan			
		found	Mfg. time (min)	Mfg. cost (\$)	Fixture quality	
1	Hierarchical search	300	35.86	23.79	0.2763	
2	A*	300	71.42	46.32	7149.93	
3	A*	1000	74.63	48.68	5200.35	

In Table 6, the optimal plans are assessed in terms of time, cost and fixture quality. We can see among the first 300 plans found by the two algorithms, the hierarchical search has a much better optimal solution. In fact, in the third experiment, we

waited for the A* search to find 1000 solutions before an optimal plan was filtered. In this experiment, A* reported a plan with smaller fixture quality but slightly worse time and cost as compared to the last experiment. Due to the weights of the metrics, this plan was considered better than the other one from A*. However, it is still far behind the first plan from hierarchical search. These comparisons indicate that in solving CAMPP problems, the hierarchical search converges much faster to the optimal plans than the weighted-sum A* search. Initial raw stock (left) Fixture mechanism Final shape after (middle) machining (right)

Plan I - Step 1: mill out pockets and slots from top



Plan II - Step 1: flip part over, drill holes from bottom



Plan II - Step 2: flip part over, mill side slot from top



Plan II - Step 3: mill middle pockets and slots from side



Figure 19: Comparison of two plans for example 1.Plan I from hierarchical search and Plan II from A* with 1000 solutions.The arrow indicates the feed direction. For the fixture mechanism, the bottom face is the face for locating the part on the machine table, and the side two faces are the faces for clamping.

Figure 19 shows the plans from hierarchical search and A* with 1000 solutions,

respectively. The second one is not optimal as it requires unnecessary setup changes (step 2 and 3) and an uncomfortable feed direction (step 3), which lead to more time and cost and penalized fixture quality.

6.4.2. Example 2

For the second example show in Figure 20, experiments with the same settings as in example 1 were conducted and the results are given in Table 7. Again the hierarchical search is able to find a much better plan. Figure 21 shows the plan details step by step.



Figure 20: Example part 2.

Table 7:Comparison between hierarchical search and A* search for example 2.Maximal queue size is set to 600.

Experiment		Total solutions	Quality of optimal plan			
		found	Mfg. time (min)	Mfg. cost (\$)	Fixture quality	
1	Hierarchical search	300	67.89	45.13	10.96	
2	A*	300	123.75	82.05	24285.78	
3	A*	1000	139.75	92.72	22275.77	

Initial raw stockFixture mechanismFinal shape after(left)(middle)machining (right)

Step 1: mill out features from top



Step 2: flip part over, mill out features from bottom



Step 3: remove left fillet





Figure 21: The optimal plan generated by hierarchical search for example 2.

6.4.3. Discussion

More experiments were implemented to validate our algorithm. Due to the space limitation, the results are not presented. This section mainly characterizes the search efficiency based on the analysis of the test results.

Figure 22 shows a plot of the computation time to find the first optimal solution against the complexity of the input solid model based on the results of the experiments. The complexity is measured by the number of sub-volumes that need to be removed from a bounding box in order to create the final shape.

An interesting observation is that as opposed to the exponentially increasing search space, the hierarchical search is able to find the first optimal and practical solution in near-linear time. The reason is that the hierarchical search always specifies a "promising" direction at every level of the tree for the best first search to go. The computation time is only dictated by the length of the complete process plan from the top to the bottom of the tree, which is proportional to the number of sub-volumes to remove. Therefore the computation time is linear rather than exponential.



Figure 22: The plot of computational time versus part complexity. It shows the linear trend of the computation time for hierarchical search to find the first optimal solution with the complexity of the part.

For the part shown in Figure 16, an exhaustive search was performed to generate the complete search space. Figure 23 summarizes the exhaustive search process. Within a very short computation time all 96 solutions were generated for this simple part. All the solutions were manually verified in order to ensure the completeness of the search space. Among all the solutions, the exhaustive search gave the same best plan shown as Plan II in Figure 14 that was previously found by our hierarchical sorting based search. As opposed to 127 solutions (shown in Figure 23) that had been tested before the best one was reported in the exhaustive search, our new algorithm is more efficient since the first solution it converged to was the best one.

Number of Total Solutions: 96 Nodes: 869 Total CPU Time: 00:00:01.341 Sec Nodes/Sec: 647.72 Goal Tests: 127



Figure 23: Summary of the exhaustive search for the part in Figure 16.

6.5. SUMMARY

In this chapter we present a multi-objective hierarchical sorting based best first search technique and successfully apply it in solving manufacturing process planning problems. The hierarchy of the objectives is set up in accordance with the manufacturing knowledge and preferences. The cutoffs for fixture, time and cost are used to adjust the search queue in order to capture the impractical manufacturing decisions. The search is educated by the manufacturing knowledge such that it is able to find the optimal and implementable process plans in near-linear time.

To extend the technique to other areas of CAMPP (like assembly and disassembly process planning), similar strategies as mentioned in the chapter can be used. It is suggested that an initial detailed study of the problem domain would be beneficial in encapsulating the underlying knowledge. Such domain-specific knowledge should not only be used to define evaluation metrics but also used to tailor the sorting strategy – even if such a strategy is as aggressive as the hierarchical sorting shown here – in order to yield practical results.

Chapter 7: Case Studies and Discussions

Several examples are provided in this chapter to validate our algorithm in manufacturability analysis. Each of the examples showcases different aspect of our work. The next three sections are tilted with the part name followed by the aspect that we are highlighting. Section 7.4 discusses the non-manufacturability reasoning in our approach and section 7.5 itemizes the characteristics of the computerized tools built on our approach.

7.1. RADIOBOX: DYNAMIC ALLOCATION OF FACES FOR OPTIMAL FIXTURE DESIGN

The first part presented – refer to as the "Radio box" – is a vehicle component design from our research partner (Figure 24). It is interesting in its complex profile and intersecting features. In this case, the actual manufacturing sequence dictates the fixture design for each operation since most planar faces that are preferred for fixture are actually created by intermediate steps and are subject to subsequent tooling as well.



Figure 24: CAD model of the "Radio box".

Table 8 shows an optimal plan with fixtures for each step generated using our approach. The first column describes each step briefly, and the second column is the initial work-piece that each step starts to machine. The third column shows the faces that

are used to set up the fixture mechanism at each step and the fourth column is the part created after every step.

In this plan, step 2 requires an intermediate face, which is created in step 1, as the locating datum to set up the work-piece. Step 4 is necessary to machine the bottom left chamfer and the left side wall as these features are partially used for clamping in step 3 and therefore are not available for the tool to enter at that step. The dynamic allocation of faces that are either preserved in the final part or are created but removed during intermediate steps for optimal fixture design is a unique feature of our algorithm.

Table 8:An optimal manufacturing plan with fixtures for Radio box.
The cutoff value for fixture quality is set to 1000. Cutoff value for the
number of optimal solutions is set to 600. Maximal queue size is set to 300.
Total run time is 313.936s.

Step description	Initial work-piece ²	Fixture mechanism ³	Final work-piece
1: side clamping in Vertical milling center, use End mill, feed along –z direction	z x y	Clamping faces	Intermediate face created for clamping in step 2
2. side clamping in Vertical milling center, use End mill, feed along x direction	z y y x	Intermediate face created in step 1 for clamping in step 2	
3. side clamping in Vertical milling center, use End mill, feed along –z direction			Side wall Bottom left fillet Both features used for fixture so not accessible at step 3

 $^{^2}$ For all the cases, the initial work-piece at step 1 is the bounding box, and after that the final work-piece at a previous step is served as the initial work-piece of the next step.

³ Refer to Figure 10 for the definition of the face configurations. For side clamping, the bottom face is the locating face and the two side faces are the clamping faces. The faces shown here are only used to indicate the orientations of the actual fixturing faces on the work-piece. While the exact fixturing areas projected on each face are identified automatically in the reasoning, not all are explicitly shown due to the tedious visualization process.

Table 8 (continued):An optimal manufacturing plan with fixtures for Radio box.
The cutoff value for fixture quality is set to 1000. Cutoff value for
the number of optimal solutions is set to 600. Maximal queue size
is set to 300. Total run time is 313.936s.

Step description	Initial work-piece	Fixture mechanism	Final work-piece
4. side clamping in Vertical milling center, use End mill, feed along -x direction			

Although Table 8 shows only one optimal plan, our reasoning actually suggests multiple pareto-optimal plans with each varying slightly in terms of time, cost and fixture quality. The runtime to generate 600 optimal plans is about 5 minutes⁴. The total manufacturing time is estimated to 41.68 min.

7.2. PART II: DEPENDENCY BETWEEN FIXTURE DESIGN AND MANUFACTURING PROCESS PLANNING

The part in Figure 25 is a benchmarking problem found in the feature-recognition research community. It is of a simple prismatic shape, but is not that intuitive to manufacture. The slots on top are intersecting and the islands at four corners are of different sizes, which require tool changes during the process planning.

⁴ All experiments were implemented on a desktop computer with Intel 3.4 GHz processor and 16 GB of memory.



Figure 25: CAD model of part 2.

An optimal plan from the reasoning as shown in Table 9 suggests that the initial stock needs to be set up with bottom slot facing upward such that the slot is created first. Next, the work-piece is flipped over so that the tools can create the features on top. Note that if the fixture design is not considered, the bottom slot is an isolated feature that can be created at any step of a manufacturing plan. Nevertheless, if we incorporate fixture design into the reasoning, it is better to machine the slot first. Considering that all other features reside on top, it is more reasonable to first locate the bottom slot using the unmachined top face as it gives larger locating area as well as preventing the top features from being contaminated by fixtures that may be required for machining the slot in later steps.

An implementation of the proposed plan in a machine shop is also shown in Table 9. The experiment justifies the practicality of the proposed plan in one-off machine shops. Table 9:An optimal manufacturing plan with fixtures for part II.The cutoff value for fixture quality is set to 1000. Cutoff value for the
number of optimal solutions is set to 200. Maximal queue size is set to 300.
Total run time is 447.864s.

Step description	Initial work-piece	Fixture mechanism	Final work-piece		
	Results from AMFA				
1: side clamping in	y				
Vertical	Implementation in machine shop: side clamping setup in VMC				
milling center, use End mill, feed along z direction	z	y z	xyy		

Table 9 (continued):An optimal manufacturing plan with fixtures for part II.
The cutoff value for fixture quality is set to 1000. Cutoff value
for the number of optimal solutions is set to 200. Maximal
queue size is set to 300. Total run time is 447.864s.



Table 10 gives a comparison between the AMFA-suggested tooling parameters and the actual parameters used at each step during the real implementation. Note the actual parameters are less than – if not equal to – the suggested values. The reason is that the machine shop does not have a complete tool library as assumed in AMFA. In addition, due to the limitation of the manually operated machines, it is always safer to choose a relatively smaller tool to do the required machining.

No	Operation	Tooling	Suggested from	Actual choice in
110.	Operation	parameter	AMFA	machine shop
		Tool diameter	1	3/4 = 0.75
1	Create bottom slot	Depth of cut	0.15	0.15
		Feed rate	0.086	0.05
		Tool diameter	0.75	3/4 = 0.75
	Create left slot	Depth of cut	0.55	0.55
		Feed rate	0.086	0.05
		Tool diameter	0.75	3/4 = 0.75
	Create top slot	Depth of cut	0.15	0.15
		Feed rate	0.086	0.05
	Create intersecting	Tool diameter	0.4	25/64 = 0.390625
		Depth of cut	0.3	0.3
2	noies	Feed rate	0.051	0.03
2	Create secondary	Tool diameter	0.32	5/16 = 0.3125
	slot	Depth of cut	0.15	0.15
	5101	Feed rate	0.036	0.03
	Create up-right and	Tool diameter	0.375	3/8 = 0.375
	bottom-right pocket	Depth of cut	0.3	0.3
	bottom-right pocket	Feed rate	0.036	0.03
	Create up-left and	Tool diameter	0.24	7/32 = 0.21875
	bottom-left holes	Depth of cut	0.2	0.2
		Feed rate	0.03	0.03

Table 10:Comparison between the manufacturing parameters suggested by the
reasoning and the actual choices in the machine shop for part II⁵.

⁵ All length parameters are in inch, and the feed rate is in inch per second.

7.3. STABILIZER: SYNTHESIZED REASONING APPLIED IN MANUFACTURING COMPLICATED FEATURES

The third part is a simplified vehicle stabilizer design from our research partner. As shown in Figure 26, the part has a contour groove around a center rib, which is not that intuitive to machine. In fact, the groove needs several steps to finish, and the complexity of the fixture design at each step depends highly on how the operations are sequenced. Further, as the feed direction for the left hole and right through pocket does not coincide with any of the feasible feed directions for the groove, how to arrange the operations for minimal time and cost is challenging. Because of these problems, a synthesized manufacturability analysis as implemented in our reasoning is necessary.



Figure 26: CAD model of the stabilizer.

For this part, the reasoning successfully generated several optimal plans in about 5.5 minutes. One of them is given in Table 11.

Table 11:An optimal manufacturing plan with fixtures for the stabilizer.
The cutoff value for fixture quality is set to 1000. Maximal queue size is set
to 300. Total run time is 325.674 s.

Step description	Initial work-piece	Fixture mechanism	Final work-piece
1: side clamping in Vertical milling center, use End mill, feed along -y direction	Results from AMFA		
	z	z	1 VMC
2. side clamping in Vertical milling center, use End mill, feed along y direction	Results from AMFA	ne shop: side clamping ir	A VMC

Table 11(continued):An optimal manufacturing plan with fixtures for the stabilizer.
The cutoff value for fixture quality is set to 1000. Maximal
queue size is set to 300. Total run time is 325.674 s.



Following the suggested plans, we were able to replicate the stabilizer in three steps in the machine shop rather than the high-tech manufacturing facility in the automobile industry where the part is usually created. Table 12 compares the suggested tooling parameters with the actual choices, where most of the parameters are the same. For step 3, the difference in machining the pocket is due to the slight inconsistency of tool libraries used in the two environments. For the drilling in step 3, we intentionally used a smaller tool in the consideration of a future reaming operation.

No	Operation	Tooling	Suggested from	Actual choice in
110.	Operation	parameter	AMFA	machine shop
		Tool diameter	0.5	0.5
1	Create top slot	Depth of cut	0.375	0.375
		Feed rate	0.051	0.03
	Create bottom	Tool diameter	0.5	0.5
	slot	Depth of cut	0.375	0.375
	5101	Feed rate	0.051	0.03
		Tool diameter	0.5	0.5
2	Create left slot	Depth of cut	0.25	0.25
		Feed rate	0.051	0.03
	Create right slot	Tool diameter	0.5	0.5
		Depth of cut	0.25	0.25
		Feed rate	0.051	0.03
	Create left	Tool diameter	0.45	7/16 = 0.4375
	pocket	Depth of cut	1	1
3	poenet	Feed rate	0.051	0.03
5	Create right	Tool diameter	0.5	7/16 = 0.4375
	hole	Depth of cut	0.25	0.25
		Feed rate	0.051	0.03

Table 12:Comparison between the manufacturing parameters suggested by the
reasoning and the actual choices in the machine shop for the stabilizer.

7.4. NON-MANUFACTURABILITY ANALYSIS

The non-manufacturability of a given part is due to two constraints. One is the production facility limitation and the other is the design flaw of the CAD model. The non-manufacturability analysis in the grammar reasoning is implemented by topological, rather than parametric reasoning through the recognition and application of rules. At this stage, we intentionally relax the parametric constraints imposed by the foundry capability. One reason is that these constraints, such as the lack of appropriate tool sizes, can always be solved by importing required tools into the foundry. Thus, no redesign feedback for the designers is needed. However, the design flaws detected by the reasoning usually relate to the topological defects in the given part. The underlying logic behind this reasoning is that if a part is topologically not manufacturable because of 1) inaccessible regions (for example, the inner sharp corners of the part in Figure 27a) or 2) unrecognized or invalid geometric elements (for example, an edge with more than two vertices), then this part would always be recognized as non-manufacturable unless the required redesign modifications are made by the users.

Consider the part in Figure 27a. It is not manufacturable due to an inaccessible sharp edge from any tool feed direction. From the analysis report shown in Figure 27c we see that the reasoning asserts that no manufacturing plan can be found for this part. Additionally, the user is informed that all the inner sharp edges should be removed before any machining operation can start. This example shows how our reasoning communicates with the user in terms of design improvements.



Figure 27: (a) A non-manufacturable part due to design flaws, (b) the machined part simulated in FeatureCAM, and (c) the manufacturability analysis result generated in AMFA.

For comparison, this part was also processed in FeatureCAM [10] and the proposed manufacturing plan is shown in Figure 28. In this plan, several stages of roughing and finishing passes are used to remove the negative cuboid. However, considering the manufacturing precision that the tools can achieve, the sharp edges would never be created exactly as designed. Figure 27b shows the amount of residual material that is left over after the plan is implemented. These areas are exactly where the non-manufacturable sharp edges locate. Rather than attempting to tackle the bad geometries by the ineffective employment of foundry capability, our approach is able to return redesign suggestions directly to the end-user in a much earlier phase, which is critical to ensure the efficiency and effectiveness of modern product design.

Candidate Manufacturing Plan in FeatureCAM

0	Automatic Order	ing)				암 🛯 🐿	*
R	Operation	Feature	Tool	Feed	Speed	Depth	
	finish	face1	facemillM3200	2971.8 MMPM	5200 RPM		
	rough pass 1	side1	endmillM2500:reg	1261.3 MMPM	2523 RPM	35.000 mm	
	finish	side1	endmillM2500:reg	1164.3 MMPM	3881 RPM	35.000 mm	
	rough pass 1	side2	endmillM2500:reg	1261.3 MMPM	2523 RPM	35.000 mm	
	finish	side2	endmillM2500:reg	1164.3 MMPM	3881 RPM	35.000 mm	
	Results						

Figure 28: A sample manufacturing plan generated in FeatureCAM.

7.5. CHARACTERISTICS OF IMPLEMENTATION AND DEPLOYMENT

The geometric and grammar reasoning demonstrated in Part I serve as the foundation based on which multiple computerized tools can be developed. Figure 29 shows one web-based GUI that was developed to visualize the functionalities of AMFA.



Figure 29: A sample AMFA GUI.

The key characteristics of the tool are summarized as follows:

- The tool is customizable based on available resources of a particular foundry. The manufacturing capability can be extended from the widely used traditional operations to the non-traditional and new-born manufacturing techniques. We have demonstrated the aptitude of the tool for reasoning about various machine libraries provided by our research partners.
- The tool is capable of analyzing complex geometries, including feature interactions. The complex regions are decomposed into simple and prismatic machining features (sub-volumes) for the rules to reason about.

• The tool allows the user to step through individual steps of a proposed plan and see the staging models, i.e., the geometry that is created after every step of the plan. Since each step removes one sub-volume in the compound negative solid, the remaining negative solid constitutes the staging model. This feature allows the easy validation of every plan, and provides a concrete means for designers to communicate with manufacturing engineers about the feasibility of the suggested plans.

Chapter 8: Part I Summary

In this part, an efficient and effective approach to automated manufacturing process planning is demonstrated for any solid model that requires non-turning operations. The approach is split into the geometric reasoning and the grammar reasoning. The geometric reasoning is a separate work from the dissertation and is developed to decompose the solid model into machinable sub-volumes and to convert the resulting sub-volumes to a graph representation. The grammar reasoning is realized using the specially designed seed lexicon and graph grammar based rules. The seed lexicon stores all geometric elements and their topological relations of a solid model through nodes, arcs, hyperarcs and labels. The grammar rules are deployed in a particular sequence to invoke all feasible sequences of machining operations that are necessary to create the input CAD model. Each operation is detailed with the amount of material to remove, the tool and machine specs, the tooling parameters, and the fixture mechanism. After the candidate manufacturing plans are generated by the grammar rules, they are evaluated in terms of time, cost and fixture quality, and a hierarchical sorting based search algorithm is developed to find the optimal and practical plans efficiently.

This work highlights the important interaction and dependency between the fixture design and the manufacturing process planning. Depending on how the part is machined, the fixture needs to be designed in accordance with the operation at each step in order to achieve the optimality as well as the practicality of a proposed plan.

For the fixture design, instead of considering it from a pure design perspective where specific subjects are investigating and their influences on the fixture design are assessed, this work first invokes all feasible fixtures with several simple rules. Then the knowledge gathered from manufacturing practice is used to dictates the selection of optimal fixtures. Through multiple case studies, we see that the strategy enables an concurrent and effective fixture design algorithm in the context of manufacturing planning.

A hierarchical sorting based best-first search algorithm is also introduced in this work. While the motive is to incorporate intuitive manufacturing background knowledge to the otherwise naïve search algorithm, the same idea can be applied in other research areas. For example, in assembly planning or robot path planning where the space of solutions expands with the complexity of the problem, the a priori knowledge can be used to better inform the search in order to achieve a much quicker convergence to optimal and practical solutions.

PART II: AUTOMATED REASONING FOR DEFINING TURNING OPERATIONS FOR MILL-TURN PARTS

To automate the manufacturing planning for the hybrid machining processes (e.g. mill-turn machining), a smart system is developed which defines the detailed manufacturing plans that are optimized in time, cost, fixture quality and tolerance satisfaction for any input CAD model. The system includes two parts. The first is a tool known as AMFA (Automated Manufacturability Feedback Analysis), which is introduced in Part I of this dissertation and is capable of reasoning about the non-turning manufacturing processes and generating user-preferred plans based on these operations. This software has been tested thoroughly and results along with the detailed description are reported in [3], [7], [8], [95]. One limitation of AMFA is that it cannot handle complex parts which require hybrid manufacturing processes. For example, consider a part with both turnable and non-turnable features. While the non-turnable features are, in principle, manufacturable in a milling center, the turnable features are more complicated to be machined via milling and require extra turning operations. In this case, how to arrange the manufacturing sequence as a whole for achieving the lowest time and cost becomes a question. Moreover, the fact that the turnable and non-turnable features are in most cases interacting makes the reasoning more challenging.

To resolve this issue, the research in the second phase [6], [9] is presented in this part, which aims to automate the reasoning for defining the lathe operations for complex geometries. It has a similar two-phase structure as AMFA: the geometric reasoning and the grammar reasoning. The geometric reasoning is a separate work done by Eftekharian, and is introduced in chapter 9. From a given CAD model, we extract both its bounding cylinder and the as-lathed axisymmetric model. Since the as-lathed model serves as the intermediate work-piece after all turning operations, the turnable volume can be

generated by subtracting the as-lathed model from the bounding cylinder. Meanwhile, the non-turnable volume can be extracted by subtracting the final part from the as-lathed model. After that, the turnable and non-turnable volumes are sent to a volume decomposition algorithm [5] to generate the isolated machining features. Features generated from the non-turnable volume are fed into AMFA to generate the optimal manufacturing plans in terms of time, cost and fixture quality.

To automate the process planning for the turnable features, first these features along with their tolerance specifications are represented by a tolerance graph. This graph then serves as the seed on which the grammar reasoning performs analysis in order to study feasible turning sequences against the tolerance specifications. The reasoning is based on the direct analysis of the knowledge conveyed by the design tolerances. The output from the grammar reasoning is the feasible turning plan for creating all turnable features. This plan is validated using a separate tolerance analysis module to show its effectiveness in satisfying the tolerance requirements.

By integrating both parts of the research, the final goal of this work is to propose a novel manufacturability analysis tool that is able to quickly inform the users (e.g. designers or manufacturing engineers) of the optimal plans in terms of time, cost, fixture quality and tolerance satisfaction for a given solid model that requires hybrid manufacturing processes.

This part is organized as follows. In chapter 9 the algorithm developed by Eftekharian to automatically separate the turnable and non-turnable features is introduced. It also converts the turnable features to a graph representation for the grammar reasoning to work on. Chapter 10 illustrates how the tolerance specifications dictate the setup design for turning operations. Beyond that, chapter 11 presents the grammar rule based reasoning to generate turning plans for the turnable features via an

illustrative case study. Another example and discussions are provided in chapter 12, which is followed by the validation of the suggested turning sequences (chapter 13) and the conclusion (chapter 14).

Chapter 9: Geometric Reasoning

This chapter explains the geometric reasoning work done by Eftekharian, which extracts the turnable features from a mill-turn part and converts them to a graph representation for the grammar reasoning to work on. While the author of this dissertation did not develop the algorithm, the author led the integration of this part with the grammar reasoning and the combined work has been published in [6], [9]. It is incorporated in the dissertation for a better understanding of the major work that follows.

The features in a mill-turn part can be categorized into two classes, turnable and non-turnable. One challenge in reasoning about the manufacturing is to correctly identify and successfully isolate the two types of features in order to assign feasible machining operations to each. Figure 30 shows a sample model with some non-turnable features that are not machinable in a typical turning operation.



Figure 30: A sample part with non-turnable features.

To isolate these features, the reasoning starts by generating the accurate as-lathed model. The as-lathed model is the intermediate work-piece that is created after all the turning operations on the bounding cylinder or the initial raw stock. The as-lathed model can be viewed as the result of revolving a two-dimensional axisymmetric silhouette around the rotational axis. Therefore, the problem of defining the as-lathed model can be formulated as finding the rotational axis of a mill-turn part and then generating the defeatured silhouette.

One approach to generate the as-lathed model that is largely used in the past literature is to revolve the original solid around a rotational axis defined by the designer in order to fill in all the non-turnable features. This is not desirable in computational geometry as the general sweeping operations (in which revolving is a special case) are computationally expensive for 3D shapes in almost all solid modeling kernels. As a result, this procedure is particularly slow and potentially inaccurate for complex parts with blended features.

In this chapter, a simpler and efficient method is proposed. It starts by automatically finding the dominant rotational axis from the CAD model. Next, it samples a set of non-uniform longitudinal cross sections of the original solid passing through the dominant rotational axis. In order to perform each sampling, a planar cutting face is needed. This plane can be created by a point and a normal vector, where the point can be any point along the rotational axis, and the normal is a unit vector perpendicular to the rotational axis. These planes are used to cut the model to generate many cross sections of the geometry. The revolving silhouette is then created by uniting all these cross sections, and the as-lathed model is formed by sweeping the silhouette for a full circle. The complete process is explained in detail in the following sections.

9.1. DETECTING THE DOMINANT ROTATIONAL AXIS

In order to identify the dominant rotational axis, the algorithm first recognizes all the curved edges in the boundary representation of the original part by collecting their center points, radii and axial normal vectors (Figure 31). A curved edge refers to any edge with a constant radius, such as a full-circular edge, a semi-circular edge, or a fillet edge. For every curved edge, two parameters are defined. The first is the number of the other curved edges N that are co-axial with the current edge. The other is the radius of the edge, R. The dominant rotational axis of the part is defined as the axis of the edge with the maximum product of the two parameters ($N \times R$).

This sorting method guarantees that the dominant rotational axis is shared by the most curved edges. This is consistent with the real turning practice: when a raw cylindrical stock is initially set up in a turning machine, it is desirable to turn as many features as possible under the initial setup. If certain features are off center from the current rotational axis, they are either left to a milling process after turning, or created with special setups in the lathe. In such cases, since no other edges are co-axial with these acentric features, the value of N for these features is zero, which negates these features from being selected for defining the rotational axis. Secondly, the factor R is critical to ensure that the rotational axis comes from a larger circular edge if there happen to be multiple co-axial edges. Again, this coincides with the practice in the machine shop. The raw stock always undergoes an initial turning to generate a smooth profile with a known radius. This profile provides the outer shape of the final part and all the following features are turned from it. Therefore, this outer profile with the largest radius R provides the best candidate edge for defining the dominant rotational axis.



Figure 31: (a) The identified curved edges and (b) their axial normal vectors for the part in Figure 30.

9.2. DEFINING THE CUTTING PLANES

To generate the cross sections of the model, a cutting plane needs to be constructed first. As mentioned, each plane needs a point and a unit normal vector. In order to generate a set of unit normal vectors, a number of points are enumerated along a unit circle circumference. As the circumference is a parametric curve, it can be enumerated by using the following equation:

$$p_i = (i + r + 1) \times \delta$$

where p_i is point *i* on the circular curve; δ is the increment and *r* is a randomly generated number between 0 and 1. The use of a random number is to ensure the non-uniformity of the curve parameters. Having this equation, some non-uniform points along the curve are generated. A unit vector is formed by connecting the circle center to each point, and it serves as the normal of a cutting plane. An example of the unit vectors is

given in Figure 32. Note that the angle α of each vector with respect to the global axis is a random value due to the non-uniformity in the equation. Given the unit vectors and the dominant rotational axis, the cutting planes can be constructed such that every plane passes through the rotational axis and has a unit vector as its normal. Once we have all the cutting planes, the solid model is sectioned with each to generate a set of cross sectional faces as shown in Figure 33a.



Figure 32: A unit circle with non-uniform radial vectors.

9.3. RECOVERING THE REVOLVING FACET

In order to find the as-lathed model a de-featured silhouette needs to be revolved around the rotational axis. This face is formed by uniting the cross sections of the model previously generated. Instead of performing the Boolean operation directly in 3D space, first all the cross-sections are re-oriented and projected onto a 2D plane defined by a global coordinate system (Figure 33b). The projected cross-sections are then united to create the de-featured revolving facet (Figure 34a). All Sampled Cross-sectional Faces



Figure 33: (a) The sampled cross sections of the part in Figure 30; (b) the union of all the cross sections.



Figure 34: (a) The revolving face and the rotational axis; (b) the as-lathed model.

9.4. EXTRACTING TURNABLE AND NON-TURNABLE FEATURES

Figure 34 shows how the as-lathed model is formed by sweeping the revolving facet around the rotational axis. The non-turnable volume is obtained by subtracting the as-lathed model from the original CAD model. To create non-turnable machining features, this negative volume is fed into the volume decomposition algorithm in [5], and
the outputs are the isolated features for machining, which are shown in Figure 35b. For these features, AMFA is used to generate the separate machining plans.

To extract the turnable features, first the as-lathed model (Figure 34b) is subtracted from the raw work-piece (typically a bounding cylinder) to get the turnable removal volume. The volume is then fed into a volume decomposition module similar to [5] to generate isolated features for turning (Figure 35a). These features are then translated into a seed graph representation. In the following chapters, a graph grammar based approach is introduced to automate the reasoning on the graph in order to define the turning operations for these features.



Figure 35: (a) The decomposed turnable features; (b) the non-turnable features.

9.5. EFFICIENCY AND EFFECTIVENESS

To ensure that the non-uniformly sampled cutting planes effectively capture all the features from the original geometry, a series of tests have been conducted on complex real parts that have several acentric features (Figure 36). Based on the results, a set of heuristics have been set up in the reasoning to guide the selection of the number of nonuniform samples that are needed based on the part complexity. As compared to the uniform-sampling based approach in which the increment needs to be small enough to detect the minimal circumferential feature, the non-uniform approach is able to set the sample cuts adaptively such that the initial cuts with small increments are always initiated at regions with dense features while the cuts with large increments are used to capture uniformly distributed features as well as regions with no feature at all.

In addition, the rotational axis is identified automatically and without using any Boolean operations. The revolving facet is recovered using a 2D union operation as opposed to a 3D operation. In light of the computationally expensive Boolean operations that are associated with the existing techniques, our novel simplifications guarantee the efficiency and effectiveness of the algorithm.



Figure 36: A summary of the tests on more complex parts.

Chapter 10: Setup Design Based On Tolerance Analysis

In manufacturing process planning, tolerance analysis is of particular importance in that a part created by any process plan must comply with all tolerances specified by the designer in order to meet certain engineering constraints. Over the past several decades, researchers have been exploring numerous tolerance analysis techniques, including tolerance chain [96], kinematic analogies based approach [97], [98], Vectorial representation [99], T-map and M-map [100], [101], Monte Carlo simulation based approach [102], [103], statistical approach [104], [105], and more [106]–[109]. However, in general those approaches either involve complicated geometric manipulations (e.g. Minkowski sum) in both Euclidean space and specific pre-defined configuration space, or require a large amount of computational resources (e.g. sampling) for reliable results. Due to these limitations, the approaches have yet to be embedded into automated manufacturability reasoning tools such that the results can be directly used as heuristics to guide the generation of optimal manufacturing plans.

In this work, the tolerance analysis is envisioned from a prognostic perspective. As the designer interprets the design intentions as the tolerance specifications, the knowledge that is otherwise hidden in the tolerance specs is extracted and encapsulated into the turning sequencing reasoning such that the tolerances themselves can be effectively used to guide the generation of optimal plans in terms of satisfying the tolerances. The tolerance analysis based setup design proposed in this work is based on a tolerance graph approach proposed in [110], and it involves two phases of effort:

1. Selection of setups

A setup refers to the act of positioning and clamping a part with respect to one or a set of manufacturing datums such that the turning operation can be conducted. For the setup design, we need to consider two types of errors that are introduced during the turning process. The first is the setup error, which includes the locating errors, the clamping distortion, and the geometrical and dimensional inaccuracy of the fixture. The second error is the machine motion error, which is generally caused by the deviation of the tool under cutting forces. Additionally, each tolerance is designed with respect to one or more specific design datums, which will be used to inspect the tolerance. However in manufacturing, these design datums are not always available as manufacturing datums due to numerous constraints (space limitation, tool-part collision, surface accessibility, etc.). The inconsistency between the design datums and manufacturing datums leads to the stack-up of the two types of errors, which make the tolerances difficult to satisfy.

The objective in setup selection is to minimize the total number of setups that are required to turn a part in order to avoid potential error stack-ups. For that, we prefer to turn as many faces as possible in a single setup. As long as the setup is not changed, the setup error remains constant, and it does not lead to the stack-up with the machine motion error. Therefore the turning precision is best guaranteed.

2. Selection of manufacturing datums for each setup

In this phase, we perform the selection of two datums (one cylindrical and one planar) in order to fully secure the part in a lathe. The cylindrical face is used to define the orientation, and the size of the feature is considered in the tolerance specifications so that only large cylindrical faces are specified as design datums. The planar face is only used to confine the axial translation, in which case the size factor is not important. It is proposed that the faces with tighter tolerances should be preferred over faces with looser tolerances when selecting manufacturing datums in order to achieve a better precision. While this datum selection strategy may violate the intention of the standardized tolerances in the sense that the design datum for a particular tolerance is not necessarily

considered as the manufacturing datum, it is shown in later chapters that this strategy can effectively improve the overall satisfaction for all tolerances, especially in cases where multiple tolerances are specified for a part and the inconsistency of manufacturing datums and design datums is often inevitable during machining. Since features with tighter tolerances are intended to have higher precision, they introduce less setup error when used as manufacturing datums during machining processes as compared to other faces. In addition, our strategy can effectively eliminate the influence of the error stack-up on the tighter tolerances, which are generally more vulnerable to the errors.

Chapter 11: Graph Grammar Based Reasoning

To automate the aforementioned setup design strategy, a novel graph grammar based approach is presented in this chapter. The grammar reasoning is implemented using a graph grammar software (GraphSynth) that was previously developed by Campbell [11]. As shown in the flowchart in Figure 37, three rules are manually designed to encapsulate all the required reasoning. When an as-lathed model is fed into the module, the reasoning performed by the rules as shown in Figure 37 is triggered automatically on the platform of GraphSynth and the output is the recommended turning sequence.

The input of the reasoning is the 2D drawing or the 3D CAD model of an aslathed model with geometric dimensioning and tolerancing included. First, the geometric reasoning automatically converts the as-lathed model to a tolerance graph (see the left section of Figure 37), which serves as the seed of phase 1. In the first phase, rule 1 is called recursively to convert the tolerance graph to a setup graph (refer to the center section of Figure 37). During the reasoning, the minimal setups are identified from the tolerance graph and are stored in the setup graph. Phase 2 takes the setup graph as an input, and performs the reasoning prescribed by rule 3 (refer to the right section of Figure 37). The reasoning first identifies the manufacturing datums from the graph for each setup with the goal of prioritizing faces with tighter tolerances. Then the selected datums are attached to the setups that are sequenced in an order defined by the knowledge in the rule. After phase 2, a complete turning sequence is generated. For both phases, rule 2 is used to update the tolerance graph and setup graph if applicable in order to facilitate the reasoning (see the center and right sections of Figure 37). In the first example that follows, rule 2 is inactive, and its meaning is explained in the second example in chapter 12.



Figure 37: Grammar reasoning flowchart for turning process planning.

Consider the as-lathed model shown in Figure 34b as an example. A 2D engineering drawing of the part is given in Figure 38 with the user-defined tolerances carefully labeled. For example, face 4 has a coaxiality tolerance of *0.02mm* with face 7, and face 10 has a perpendicularity tolerance of *0.01mm* with face 1.



Figure 38: The CAD drawing of the part shown in Figure 34b.

First, the 3D model (with associated GD&T data) or the 2D drawing is converted to a tolerance graph (Figure 39) for the grammar reasoning to use. In the tolerance graph, the geometric elements are represented by nodes, arcs and hyper-arcs. Nodes are used to represent faces. For example, the cylindrical face 7 is represented by the node with name "n7" and a label "*cylindrical*". The label is a string stored in the data structure of the node and is used to indicate the face type. If two nodes have a tolerance relationship assigned to them, an arc will connect them with the normalized tolerance labeled on it.



Figure 39: The tolerance graph generated from the 2D drawing in Figure 38.

As discussed in [111], the tolerance normalization stems from the fact that every tolerance essentially defines a minimal zone within which a feature in question must locate. Therefore, a generalized angle can be determined from the tolerance zone such that the feature will always remain inside the minimal zone as long as the deviation of the feature from its ideal position (i.e. the center of the minimal zone) is less than this angle. Figure 40 shows the generalized angle for the parallelism tolerance. As the tolerance zone for parallelism resembles a 2D region, the angle is relatively easy to identify. However, for 3D tolerance zones (e.g. position tolerances), the derivation is more complicated and we refer interested readers to [111]. Considering that all generalized angles are in radians, the rules can assign relative tightness between two tolerances by simply comparing their angles. In Figure 39, the generalized angle in radians for each arc (indicating each tolerance relationship) is labeled in the parenthesis following the arc's name. For instance, the *0.02mm* perpendicularity tolerance between face 4 and face 7 is normalized to *0.0095 radians*.



Figure 40: The generalized angle α of the parallelism tolerance. The figure shows the front view of a cuboid with its top face milled out

The normalization has been strictly defined for datum-dependent tolerances, including orientation tolerances (parallelism, perpendicularity, angularity, etc.), location tolerances (position tolerance, symmetry, concentricity, etc.) and profile tolerances for primitive features (line, planar surface, cylinder, polygons, etc.). But for datum-independent tolerances like form tolerances (flatness, cylindricity, etc.), the definition needs to be modified to include the form variations. In the current work we assume perfect form of feature. For the orientation and position tolerances in Figure 39, they are directly comparable after converted to the generalized angle representations.

Figure 39 also includes several hyper-arcs, which are special graph elements for the designer to use in GraphSynth and are represented as polygons encompassing the connected nodes. While an arc can only connect two nodes, a hyper-arc can connect as many nodes as needed. In the tolerance graph, three hyper-arcs (named as "ha0 (Sr)" – name ha0 followed by the label Sr in the parentheses, "ha1 (Sl)" and "ha2 (Sb)") are used to categorize the face nodes into three groups: Sb, Sl and Sr. Group Sl contains all faces that are better turned from the positive X (+X) direction. For example, since face 11 is in Sl – referring back to Figure 38 – (+X) direction is a better choice for turning this face. Similarly, group Sr contains all faces that are better turned from both (-X) and (+X) directions are grouped into Sb. After the tolerance graph is generated, a set of rules are called to reason on the graph in order to study the turning sequences against the tolerance specifications.

Phase 1: selection of setups

The first grammar rule as shown in Figure 41a is designed to perform the setup selection. The rule is of the form $(L \rightarrow R)$ where the left hand side (L) includes elements and conditions to be recognized and satisfied in the host graph (tolerance graph) while the right hand side (R) indicates the transformations of those elements that have been recognized in the host graph.

Since our objective is to minimize the total number of setups, we are interested in the faces in *Sb* group as they can be turned from either (+X) or (-X) direction and therefore can be merged into either *Sr* or *Sl* group. The tightest tolerance associated with a face dictates which group the face is moved into. The L of the rule begins the reasoning by first detecting a set of arcs in the tolerance graph that have one end in the *Sb* group. Within this set, the arc with the tightest tolerance (represented as arc a0 in the L of the rule) is recognized. The arc in the tolerance graph (Figure 39) that meets the two conditions is arc a1. Since a1 connects face nodes n7 and n9, and it is already known that n9 can only be turned from the (+X) direction, we move n7 from group *Sb* into group *Sl*, meaning n7 will be turned in the same setup as n9. The manipulation of n7 is realized automatically through a virtual transformation from L to R of rule 1. In the R of the rule, arc a0 (mapped to a1 in the tolerance graph) that was previously captured in the L is deleted and face n0 (mapped to n7 in the tolerance graph) becomes encompassed by hyperarc ha1 (representing *SI* group) instead of ha0 (representing *Sb* group). Since in this tolerance graph there is only one face in *Sb* group, the rule is called only once. After this transition, *Sb* becomes empty and is deleted by the rule (as seen in the R of the rule, ha0no longer exists). As a result, the tolerance graph evolves into a setup graph as shown in Figure 42.



Figure 41: The screenshot of (a) rule 1, (b) rule 2 and (c) rule 3.



Figure 42: The screenshot of the setup graph.

In the setup graph, since the faces in Sl and Sr do not share common turning directions, they have to be turned in two distinct setups. Therefore, we end up with two minimal setups (Sl and Sr) after the setup selection. Next, we will select the manufacturing datums for the two setups.

Phase 2: selection of manufacturing datums

The algorithm to select manufacturing datums is encoded into the third rule shown in Figure 41c. Since each setup has multiple tolerances to satisfy, the inconsistency of design and manufacturing datums is inevitable. For achieving a better overall satisfaction for all tolerances, we prefer the faces with tighter tolerances as the locating datums of each setup. Among all the remaining arcs in the setup graph (Figure 42: arcs a2, a3, a4, and a5), a4 is recognized as it represents the tightest tolerance. Therefore face n1 and face n10 connected by a4 are intended to have the highest precision. We can use face n1 as the locating datum of setup SI, and face n10 as the locating datum of setup Sr. Both faces will introduce less setup errors as compared to other faces. Consider setup Sr first, the cylindrical datum n10 defines the orientation of the part on the lathe. We still need a planar datum from the same group of n10 (SI) in

order to constrain the translation of the part along X axis. While both face n9 and n11 are available in *SI*, n11 is selected as the second datum since it has a tighter tolerance compared to n9. As a result, face n10 and n11 are chosen as the locating datums for setup *Sr*.

Similarly, for setup SI, the cylindrical face n4 is chosen with planar face n1 as the locating datums. Note that n4 has a tighter tolerance compared to other cylindrical faces in the same group. As represented in the third rule (Figure 41c), the two datum faces are first recognized in the L as nodes n1 and n2. After the transformation from the L to the R, the two nodes are assigned a new label "*datum*", which indicates that the two datum faces have been determined.

The last step of reasoning in phase 2 is to decide the setup sequence, or which group (*SI* or *Sr*) of faces to create first. This involves a concept of *the Number of Tolerances (NoT)* associated with a face node, which is equivalent to the total number of arcs incident on the node. The algorithm suggests that the group in which the face with the highest *NoT* resides should be machined first. For this part, since face *n1* has the highest *NoT (NoT = 2)*, *Sr* group should be turned fist. This is to guarantee more faces are created in the early setups. The final setup sequence is shown in Figure 43, which is effectively defined by the order in which the three grammar rules are called.



Figure 43: The suggested turning sequence for the part shown in Figure 34b.

Chapter 12: Detailed Example

As a more complex example, the part shown in Figure 44b is presented to further explain our reasoning. Although there are interacting non-turnable features in the part, the geometric reasoning is capable of recovering the as-lathed model (Figure 44a) for the grammar reasoning to use. This conversion takes place within 0.135 seconds⁶ using C++ code and Parasolid kernel [112]. Then, the non-turnable volume (Figure 44c) is decomposed into non-turnable features (Figure 44d) automatically within 0.19 seconds. Due to space limitations, only the reasoning about the as-lathed model is described below.



Figure 44: A complex part with interacting features.

The 2D drawing for the as-lathed model is shown in Figure 45 and the corresponding tolerance graph is given in Figure 46. Note that, there are two arcs (a2 and a4) located entirely inside *SI* and *Sr* respectively. In our methodology, faces in the same group are always turned in one setup for achieving the highest precision. Therefore, it is assumed that the tolerances represented by these internal arcs are automatically satisfied within their setup and there is no need to consider them in the later reasoning. The second

⁶ With no further specifications, all experiments in this part were implemented on a desktop computer with AMD 3.2 GHz processor and 6 GB of memory.

rule in Figure 41b is specially designed to delete arcs of this kind before other rules start the reasoning. If a tolerance graph does not have internal arcs (as in the first example), then rule 2 will not be invoked.



Figure 45: The CAD drawing of the as-lathed model in Figure 44a.



Figure 46: The tolerance graph for the part shown in Figure 44a.



Figure 47: The updated tolerance graph for the part shown in Figure 44a. The internal arcs a^2 and a^4 are deleted.

After the update, the new tolerance graph is shown in Figure 47. Starting from the new graph, similar reasoning is implemented to design the setups. First, rule 1 (Figure 41a) is called to evolve the tolerance graph into a setup graph, during which face n6 in **Sb** is moved to **Sr**. This step is to minimize the number of setups such that the potential error stack-ups can be avoided to the maximal extent. The resulted setup graph is shown in Figure 48. Note that, after face n6 is moved to **Sr** group, arc a5 and a6 become internal arcs and therefore are deleted by the second rule (Figure 41b). Next, rule 3 (Figure 41c) is called to select the locating datums for the two remaining setups. The objective in this phase is to prioritize the tightest tolerance a3 among the three remaining tolerances (Figure 48: a0, a1, and a3). Therefore face n11 is preferred as the planar datum for **Sl**. Meanwhile cylindrical face n6 that has the highest precision is chosen as the second datum to fully secure the work-piece. For setup **Sl**, the pair of datums with highest precision are face n3 and face n4. After the datum selection, the setup sequencing is also

performed during the call of rule 3. In this case, face *n6* has the highest *NoT* (*NoT* = 2), therefore the faces in *Sr* are turned first.



Figure 48: The setup graph for the part in Figure 44a. The internal arcs *a5* and *a6* are deleted.

The complete grammar reasoning takes 0.18 seconds and the suggested turning

sequence is shown in Figure 49.



Figure 49: The suggested turning sequence for the part shown in Figure 44a.

Chapter 13: Plan Validation

After a turning sequence is generated, it is critical to verify if the plan achieves a better performance in satisfying all the design tolerances. The author was working with colleagues in Palo Alto Research Center to develop a real-time tolerance analysis module for use in the automated manufacturing process planning tools [12]. The module takes in a complete manufacturing plan as well as the part with all its tolerance specs. Then the tolerance analysis technique performs a sampling based reasoning on the inputs. The outputs from the reasoning are the acceptance rates for all design tolerances. An acceptance rate is a stochastic estimation of the quality of a plan in terms of satisfying a specific tolerance.

Two types of errors are discerned in simulating the manufacturing processes. The first is the local manufacturing error that comes from the actual machining of a feature in question. For example, the positioning inaccuracy of a machine and the spinning deflection of a tool are common sources for this error. The second is the stack-up error, which is due to the inconsistency between the manufacturing datums used to machine a feature and the design datums used when inspecting the tolerance of the feature. When machining the feature, design datums are not always available for use as manufacturing datums due to numerous constraints (space limitation, tool-part collision, surface accessibility, etc.). If the feature is machined with respect to other manufacturing datums, variations from these datums will stack up with the variations of design datums during the tolerance inspection, which makes the tolerance difficult to satisfy.

The tolerance analysis technique in [12] systematically analyzes the local manufacturing error and the stack-up error. First, a set of points are sampled on a feature to be analyzed. For each point, we then sample from error distributions that model the

local manufacturing error. By accumulating sampled errors onto the ideal location of each point, we are able to get a stochastic estimation of the discretized feature after machining. For a datum-independent tolerance, the estimated locations are evaluated through membership tests against the Design Tolerance Zone (DTZ) that is explicitly specified by the tolerance and the tolerance satisfaction can be assessed.

For the stack-up error, the idea is that every datum (design or manufacturing datum) applies a homogeneous transformation onto the feature when it is used to locate the feature. If the datum has a perfect form, this transformation is essentially an identity transformation – meaning that the position and orientation of the feature are not changed during alignment. Variation of a datum is caused by its local manufacturing error, and may be bounded by a Manufacturing Tolerance Zone (MTZ) that is determined by the manufacturing precision when creating the datum. Following a process plan, we can extract a chain of datums that have been involved in the machining and inspection of the feature in question. For each datum, a transformation is sampled in six Degrees of Freedom (DOF) within its MTZ to describe the variation. Then the stack-up of the variations in DTZs and MTZs can be implicitly represented by the composition and intersection of all the relevant transformations in a sequence decided by the manufacturing plan.

For a datum-dependent tolerance, the stack-up error represented by transformations is accumulated with the local manufacturing error. The results are compared with the explicitly specified DTZ in order to compute the tolerance satisfaction rate.

For the purpose of evaluating the quality of our plans, we conduct a comparative study using the tolerance analysis module. We take the part in Figure 34b as a case to study. The plan generated by our reasoning in Figure 43 is used as the first sample. To

make our experiment general, we propose a traditional turning plan as shown in Figure 50 for comparison. As compared to the suggested plan, this plan creates face 7 in setup 1 and uses different locating datums in setup 2. It is an obvious plan that one may bring up without considering any tolerances.

Setup 0:				
 Roughing pass: Create surface n10 and n11 as initial locating datums 				
Setup 1:				
- Use surface n10 and n11 as the locating datums to setup the work piece				
- Perform Turning Operations on surfaces:				
n1→n2→n3→n4→n5→n6→n7				
Setup 2:				
- Use surface n1 and n2 as the locating datums to setup the work piece.				
- Perform Turning Operations on surfaces:				
n11→n10→n9→n8				

Figure 50: A traditional turning sequence for the part shown in Figure 34b.

The tolerance analysis module is used to analyze both plans. To make the comparative results more prominent, we set the maximum variations of all error sources (machine error, tool error, locating error, etc.) to be 0.02 mm with a 95% confidence interval, which are of the same scale as the tolerance specs. The results are summarized in Table 13.

Relative		Acceptance rate		Performance
tightnass	Tolerances	Our plan	The traditional	change w.r.t the
ugniness			plan	traditional plan
From tightest to loosest	Face 7:	33.67%	29.83%	+12.87%
	perpendicularity			
	Face 10:	54.5%	53.25%	+2.35%
	perpendicularity			
	Face 1	62.58%	51.58%	+21.33%
	parallelism			
	Face 4:	48.25%	30.58%	+57.78%
	coaxiality			
	Face 10:	91 92%	91.5%	+0.46%
	coaxiality	1.7270	71.570	10.4070
	Face 9:	8/1 50%	01%	7 1/0/
	parallelism	04.370	J170	-7.1470
Chance of satisfying all the		4 3%	2 09%	+105 74%
tolerances				100.7170

 Table 13:
 The analysis results of the two plans from the tolerance analysis module.

The results reveal that the plan generated from our automated reasoning has a better overall quality in terms of satisfying all the tolerances, especially the tighter tolerances. While the acceptance rate for the loosest tolerance is reduced, all the tighter tolerances are better satisfied. As compared to the traditional plan, the automated plan can be viewed as a better allocation of the turning setups such that the reduced precision on those loose tolerances are used to compensate for the acceptance rates of the tighter tolerances. The results agree with the design intent to prioritize the tighter tolerances as they are more vulnerable to manufacturing errors. Additionally, the overall acceptance rate, which is interpreted as the chance of satisfying all the tolerances, is doubled in our new plan (4.3% compared to 2.1%). Two insights can be drawn from the final percentages: 1) By leveraging the performance on tighter tolerances, our algorithm is able to improve the overall plan quality significantly; 2) Despite the doubled acceptance rate, the manufacturing is poorly able to meet all these tolerance requirements. It signifies that the designer ought to rethink of the tight tolerance specifications in light of the existing manufacturing capabilities.

Chapter 14: Part II Summary

A novel approach for automating the turning process planning for mill-turn parts is presented in this part. The algorithm starts by identifying the dominant rotational axis from a mill-turn part and performing several non-uniform longitudinal cross-sectional cuts to quickly generate the as-lathed model. Then several simple Boolean operations are implemented to successfully generate both the turnable and non-turnable features. For the non-turnable features, AMFA is employed to automatically generate the optimal process plans in terms of manufacturing time, cost and fixture quality.

For the turnable features, the turning sequences are designed based on the analysis of the knowledge that is conveyed in the tolerances specified by the designer. Given a set of turnable features with multiple tolerances attached, the inconsistency between design datums and manufacturing datums is often inevitable. It is therefore hard to decide which faces to use as manufacturing datums when turning the features in order to achieve the best tolerance satisfaction. The tolerance based reasoning streamlines the turning setup design with a two-phase strategy: 1) selection of setups and 2) selection of manufacturing datums for each setup. In phase 1, we design the setups in a way that every setup creates as many features as possible. As a result, the number of setups required is minimized and the potential error stack-up is avoided to the maximum extent. In phase 2, two faces (a cylindrical face and a planar face) are selected to fully secure the work-piece for each setup. During the selection, we prioritize faces with tighter tolerances as manufacturing datums because they are intended to have higher precisions and therefore lead to less setup errors as compared to other faces.

A rule-based grammar reasoning scheme has been developed to automatically implement such reasoning and generate turning sequences that satisfy the tolerance requirements. The reasoning differs from the existing turning process planning techniques in that it extracts knowledge directly from the design tolerances and uses the knowledge to dictate the generation of optimal turning sequences. We have demonstrated that the information conveyed in the tolerances is critical to ensure that the suggested process plans are able to significantly improve the turning precision.

As compared to the existing tolerance analysis techniques, our approach is prognostic rather than diagnostic in the sense that the tolerances are used as heuristics to guide the generation of optimal plans instead of being used to validate an existing plan. In addition, since it reasons directly on the tolerances, much less computation is required as the large-scale sampling of the manufacturing processes that is often performed in traditional tolerance analysis is no longer necessary. As a result, the efficiency of our reasoning is preserved.

Chapter 15: Conclusion

This chapter summarizes the work in the dissertation and highlights the contributions and novelty. The potential directions of further study are also discussed. The chapter ends with closing remarks.

15.1. SUMMARY

A complete and systematic approach to reasoning about the manufacturability of any solid model is demonstrated in this dissertation. It consists of two modules: the Automated Manufacturability Feedback Analysis (AMFA) that is developed to propose optimal process plans in time, cost and fixture quality for non-turning operations, and the turning process planning module that generates feasible turning sequences for achieving the best tolerance satisfaction. For complex mill-turn parts, the approach is able to automatically separate the turnable features for turning process planning and the nonturnable features for AMFA. The process plans for non-turnable features are detailed with the amount of material to remove, the suggested tools and machines, the precise feed directions, the optimal fixture mechanisms to secure the work-piece and the estimated time and cost for machining. Numerous real parts provided by our industrial and research partners are used to validate the optimality and practicality the suggested plans. The real implementations of two suggested plans in the machine shop are also provided. The results show the consistency between the suggested plans and tooling parameters from AMFA and the actual choices on the shop floor.

For the turnable features, the suggested turning sequences articulate the required setups and the features to be created at each setup in order to best satisfy the prescribed tolerances. Each setup includes a cylindrical face that is used to define the orientation of the work-piece and a planar face that is used to constrain the axial translation of the work-piece in the lathe. The preferred sequence and feed directions for turning the features in each setup are also provided. Two mill-turn parts are used to demonstrate the validity of our algorithm. One of the suggested turning sequences is compared with a manually proposed plan from expert machinist using a separate tolerance analysis module in which the tolerance satisfactions for both plans are assessed. The results show the effectiveness and optimality of our plans in satisfying all the prescribed tolerances.

15.2. CONTRIBUTIONS AND NOVELTY

Three major engineering problems are addressed in this dissertation: the computer-aided manufacturing process planning (CAPP), the computer-aided fixture design (CAFD), and the automated turning process planning.

- 1. For CAPP, we demonstrate a graph grammar based approach to automatically define detailed manufacturing process plans for complex solid models. The graph lexicon preserves all necessary geometric and topological information of the solid model that is relevant to the manufacturability analysis and enables an accurate reasoning of the manufacturing process planning for complex geometries. The approach is very efficient as it is structured in a way that the computationally intensive geometric reasoning is separated from the grammar based manufacturability analysis, which has not been seen in the existing research.
- 2. The CAFD solution proposed here is seamlessly integrated into AMFA and it allows us to identify the dependency between the fixture design and the manufacturing process planning, which has not been well explored in existing literatures. Through a set of case studies, the necessity of thoroughly

assessing the manufacturing dependency is shown for defining optimal process plans and fixture designs.

- 3. The CAFD algorithm uses the manufacturing knowledge and experience instead of the conventional multi-disciplinary design optimization techniques to define the optimality of a fixture design. The algorithm is particularly efficient as it avoids the complicated and inefficient computations in the early stage of fixture design. In addition, the practicality of the suggested fixtures is guaranteed by the empirical knowledge used to guide the generation of optimal solutions.
- 4. The automated turning process planning algorithm in the dissertation shifts the view of the tolerance analysis from a diagnostic perspective to a prognostic aspect. We extract the knowledge that is otherwise hidden in the tolerances and use it directly to decide the optimal sequences of turning operations. The approach is effective as it takes tolerances into consideration at every stage of the reasoning, which closely matches the design intentions. Compared to the existing tolerance analysis techniques that are typically used to validate a given process plan, our approach is able to generate plans that are proven to be optimal in satisfying all the tolerances. This way, the tolerance analysis after machining becomes easier and the manufacturing efficiency is improved.
- 5. In this work we also develop a hierarchical sorting based best first search technique and demonstrate its efficiency and effectiveness in solving multiobjective optimization problems in manufacturing domains (e.g. machining process planning, and assembly/disassembly process planning). We have validated the linear-time convergence of the search technique to optimal 122

solutions. The rationale behind the new search is that the domain-specific knowledge can not only be used to define evaluation metrics in the optimization but also used to tailor the sorting strategy in order to yield practical results.

15.3. FUTURE WORK

15.3.1. Tool path generation

The current process planning algorithms specifies the optimal sequences of operations that are required to create the final shape of a CAD model. For the plans to be readily implementable on the shop floor, especially in a CNC machining environment, the precise tool path for each operation is required. A complete tool path for a given operation includes air cut and non-air cut. During the non-air cut, the tool is engaged with the removal material and the tool motion is directly used to cut off required material from the work-piece. Given a region of material to remove, the tool path for the non-air cut is closely related to the geometry of the removal material and the tooling parameters. Two types of non-air cut tool paths that are widely used in the foundry are the contour tool path (Figure 51) and the zigzag tool path (Figure 52). Further efforts are needed to encode the tool paths in the context of prescribed tooling environment.



Figure 51: 2D contour tool path⁷.



Figure 52: The zig-zag tool path projected onto a milling surface⁸.

The air-cut is also critical as it provides the tool proper lead-in and lead-out directions before and after an operation, which is critical to keep the tool from sudden changes of cutting forces. It also defines the motion of the tool between regions of removal material that are not inter-connected. The motion needs to be carefully planned in order to save the air-cut time and to avoid the collision of the tool with environmental obstacles (e.g. fixtures, jigs, machine table and spindle, etc.). Given the sizes of the tool

⁷ Excerpted from http://www.hsmworks.com/docs/cncbook/en/#Ch07_2DContour.

⁸ Excerpted from

 $http://www.ezcam.com/web/products/help/ezmill/machining_mill_2d/projection_\&_zig_zag_graphic.htm.$

and the obstacles, the automated tool path planning is often a very complicated optimization problem that involves Boolean operations of rigid bodies in 3D space. In addition, for the continuous tool movements between any two consecutive operations, each individual tool path planning problem needs to be considered collectively. Extensive research is required to address all the concerns before a complete and optimal tool path for a given process plan can be generated.

15.3.2. Fixture unit design

In this dissertation we limit the fixture mechanisms to the downward clamping and the side clamping, and only consider the fixture faces used for each mechanism. In high-production foundry where the modular fixtures are often desired, the actual locations on each fixture face that are used to engage with the modular fixtures (e.g. pinarray fixture) need to be computed. Since in our reasoning we already identify feasible regions within every fixture face for clamping and locating, the fixture unit design problem is greatly simplified as there is no need to blindly search every face of the geometry in order to find the best ones. However, the selection of contacting points on our suggested face regions still requires specific algorithm (for example, a typical technology used is the Ray-tracing algorithm) to be employed, in which the force and stress distribution, the spatial interference, and the clamping and locating strategies need to be considered collectively.

15.3.3. Tolerance analysis in non-turning process planning

Currently tolerance analysis is only used in the automated turning process planning in the dissertation. In non-turning process planning, the tolerances are of equal importance to ensure that the part created meets all engineering constraints. The idea of analyzing the prescribed tolerances in order to guide the generation of optimal process plans can be extended to AMFA as well. The knowledge conveyed by the tolerances can be used as another heuristic in the hierarchical sorting based best first search such that the suggested plan is also assessed in terms of tolerance satisfaction. The only problem with this strategy is the need of a new hierarchy for the extended set of metrics. It is expected that a second study of the problem will avail the setup of the hierarchy in order to yield practical and optimal solutions.

15.3.4. System integration

Above the aforementioned directions, the ultimate task is to integrate the separate reasoning for turning and non-turning operations into a synthesized approach. Currently, the differentiation of the turning process and the non-turning process may prevent some optimal plans from being generated. For instance, in a machining center it is possible for a milling tool to machine certain turnable features as well. In the integrated system the turning and milling processes will be alternative options for the turnable features (for non-turnable features, turning operations will never be invoked simply because it is highly unlikely that these features can be machined in turning process). This way, the automated reasoning can be performed on complex mill-turn parts that require solely milling processes.

With the system integration, we will be able to develop a complete graph grammar based system that is able to reason about all subtractive manufacturing processes and geometries of different complexity and generate optimal manufacturing plans in terms of any user-specified objectives.

15.4. CLOSING REMARKS

The computational approach presented here streamlines the design and digital manufacturing by synthesizing the multi-disciplinary knowledge across geometry, manufacturing, fixture, tolerance analysis and generative search while providing automated feedback for optimal design and manufacturing. The resulting tool can help industries in improving manufacturing efficiency, precision, and cost and catalyzing product designs with better manufacturability.

Bibliography

- T. Dong, L. Zhang, R. Tong, and J. Dong, "A hierarchical approach to disassembly sequence planning for mechanical product," *Int. J. Adv. Manuf. Technol.*, vol. 30, no. 5–6, pp. 507–520, Dec. 2005.
- [2] Q. Guan, J. H. Liu, and Y. F. Zhong, "A concurrent hierarchical evolution approach to assembly process planning," *Int. J. Prod. Res.*, vol. 40, no. 14, pp. 3357–3374, Jan. 2002.
- [3] W. Fu, A. A. Eftekharian, and M. I. Campbell, "AUTOMATED MANUFACTURING PLANNING APPROACH BASED ON VOLUME DECOMPOSITION AND GRAPH-GRAMMARS," J. Comput. Inf. Sci. Eng., vol. 13, no. 2, 2013.
- [4] A. Nagpal, "A hierarchical approach to process planning," University of Windsor, 1989.
- [5] A. Eftekharian and M. I. Campbell, "Convex Decomposition of 3D Solid Models for Automated Manufacturing Process Planning Applications," in ASME 2012 International Design Engineering Technical Conferences & Computers and Information in Engineering Conference (IDETC/CIE), 2012.
- [6] A. A. Eftekharian, W. Fu, C. Manion, and M. I. Campbell, "Automatic Reasoning for Defining Lathe Operations for Mill-Turn Parts," in *Proceedings of the ASME* 2013 International Design Engineering Technical Conference & Computers and Information in Engineering Conference IDETC/CIE 2013, 2013, no. 512, pp. 1–11.
- [7] W. Fu, A. Eftekharian, P. Radhakrishnan, M. Campbell, and C. Fritz, "A GRAPH GRAMMAR BASED APPROACH TO AUTOMATED MANUFACTURING PLANNING," in ASME 2012 International Design Engineering Technical Conferences & Computers and Information in Engineering Conference (IDETC/CIE), 2012, no. 512.
- [8] W. Fu and M. I. Campbell, "Concurrent Fixture Design for Automated Manufacturing Process Planning," Int. J. Adv. Manuf. Technol., pp. 1–22, 2014.
- [9] W. Fu, A. A. Eftekharian, M. I. Campbell, and T. Kurtoglu, "Automatic Reasoning for Defining Lathe Operations For Mill-Turn Parts: A Tolerance Based Approach," *J. Mech. Des.*, 2013.
- [10] Delcam Advanced Manufacturing Solutions, "FeatureCAM." [Online]. Available: http://www.featurecam.com/.

- [11] M. I. Campbell, "GraphSynth2: software for generative grammars and creative search," 2012. [Online]. Available: https://bitbucket.org/MattCampbell/graphsynth.
- [12] W. Fu, S. Nelaturi, A. Rangarajan, and T. Kurtoglu, "Tolerance Analysis for Validating Manufacturing Process Plans," in *Proceedings of the ASME 2014 International Design Engineering Technical Conferences & Computers and Information in Engineering Conference (IDETC/CIE)*, 2014.
- [13] E. L. Russell, *Automated Manufacturing Planning*. New York: American Management Association, 1967.
- [14] H. R. Berenji and B. Khoshnevis, "Use of artificial intelligence in automated process planning," *Comput. Mech. Eng.*, vol. 5, no. 2, pp. 47–55, 1986.
- [15] G. Chryssolouris, S. Chan, and N. P. Suh, "An Integrated Approach to Process Planning and Scheduling," *CIRP Ann. - Manuf. Technol.*, vol. 34, no. 1, pp. 413– 417, Jan. 1985.
- [16] P. Taylor, H. B. E. N. Wang, R. A. Wysk, and L. D. B. Hall, "A knowledge-based approach for automated process planning," *Int. J. Prod. Res.*, vol. 26, no. 6, 1988.
- [17] H. B. Marri, A. Gunasekaran, and R. J. Grieve, "Computer-Aided Process Planning: A State of Art," *Int. J. Adv. Manuf. Technol.*, vol. 14, pp. 261–268, 1998.
- [18] R. Sharma and J. X. Gao, "Implementation of step 224 in an automated manufacturing planning system," *Proc. Inst. Mech. Eng. Part B Eng. Manuf.*, vol. 216, no. 9, pp. 1277–1289, 2002.
- [19] R. D. Allen, J. A. Harding, and S. T. Newman, "The application of STEP-NC using agent-based process planning," *Int. J. Prod. Res.*, vol. 43, pp. 655–670, 2005.
- [20] H. Ehrig, G. Engels, H. J. Kreowski, and G. Rozenberg, *Handbook of Graph Grammars and Computing by Graph Transformations*. NJ: World Science Publication Co., 1999.
- [21] F. L. Krause, *Product Modeling: An Approach for Integrated Information Processing.* Springer Berlin Heidelberg, 1993, pp. 160–175.
- [22] A. P. Rockwood, "Geometric primitives," *ACM Comput. Surv.*, vol. 28, no. 1, pp. 149–151, Mar. 1996.
- [23] F. Krause, F. Kimura, T. Kjellberg, S. C. Lu, I. Suh, V. A. Tipnis, and M. I. Weck, "Product Modelling," vol. 42, no. 2, pp. 695–706, 1993.
- [24] J. Han, M. Pratt, and W. C. Regli, "Manufacturing feature recognition from solid models: a status report," *IEEE Trans. Robot. Autom.*, vol. 16, no. 6, pp. 782–796, 2000.
- [25] J. J. Shah, "Assessment of features technology," *Comput. Des.*, vol. 23, no. 5, pp. 331–343, Jun. 1991.
- [26] J. J. Shah, D. Anderson, Y. S. Kim, and S. Joshi, "A Discourse on Geometric Feature Recognition From CAD Models," J. Comput. Inf. Sci. Eng., vol. 1, no. 1, p. 41, 2001.
- [27] S. Subrahmanyam and M. Wozny, "An overview of automatic feature recognition techniques for computer-aided process planning," *Comput. Ind.*, vol. 26, no. 1, pp. 1–21, Apr. 1995.
- [28] B. Babic, N. Nesic, and Z. Miljkovic, "A review of automated feature recognition with rule-based pattern recognition," *Comput. Ind.*, vol. 59, no. 4, pp. 321–337, Apr. 2008.
- [29] M. Marefat and R. L. Kashyap, "Geometric reasoning for recognition of threedimensional object features," *IEEE Trans. Pattern Anal. Mach. Intell.*, vol. 12, no. 10, pp. 949–965, 1990.
- [30] T. Laakko and M. Miintylii, "Feature modeling by incremental feature recognition," *Comput. Des.*, vol. 25, no. 8, pp. 479–492, 1993.
- [31] S. Joshi and T. C. Chang, "Graph-based heuristics for recognition of machined features from a 3D solid model," *Comput. Des.*, vol. 20, no. 2, pp. 58–66, Mar. 1988.
- [32] S. N. Trika, S. Member, and R. L. Kashyap, "Geometric Reasoning for Extraction of Manufacturing Features in Iso-Oriented Polyhedrons," *IEEE Trans. Pattern Anal. Mach. Intell.*, vol. 16, no. 11, pp. 1087–1100, 1994.
- [33] B. V. S. Kumar and C. S. P. Rao, "Automatic Extraction of Three Dimensional Prismatic Machining Features from CAD Model," *Int. J. Comput. Sci. Commun. Networks*, vol. 1, no. 3, pp. 285–296.
- [34] M. Sadaiah, D. R. Yadav, P. V Mohanram, and P. Radhakrishnan, "A Generative Computer-Aided Process Planning System for," *Int. J. Adv. Manuf. Technol.*, vol. 20, pp. 709–719, 2002.

- [35] H. K. D. Bouzakis and G. Andreadis, "A feature-based algorithm for computer aided process planning for prismatic parts," *Int. J. Prod. Eng. Comput.*, vol. 3, no. 3, pp. 17–22, 2000.
- [36] M. Henderson and D. Anderson, "Computer Recognition and Extraction of Form Features : A CAD / CAM Link," *Comput. Ind.*, vol. 5, pp. 329–339, 1984.
- [37] V. B. Sunil and S. S. Pande, "Automatic recognition of features from freeform surface CAD models," *Comput. Des.*, vol. 40, no. 4, pp. 502–517, Apr. 2008.
- [38] Y. S. Kim, E. Wang, and H. M. H. M. Rho, "Geometry-based machining precedence reasoning for feature-based process planning," *Int. J. Prod. Res.*, vol. 39, no. 10, pp. 2077–2103, Jan. 2001.
- [39] V. SHAPIRO, "Well-formed set representations of solids," *Int. J. Comput. Geom. Appl.*, vol. 9, pp. 125–150, 1999.
- [40] S. B. Tor and A. E. Middleditch, "Convex Decomposition of Simple Polygons," *ACM Trans. Graph.*, vol. 3, no. 4, pp. 244–265, Oct. 1984.
- [41] D. Dobkin, L. Guibas, and J. Hershberger, "An Efficient Algorithm for Finding the CSG Representation of a Simple Polygon," ACM Trans. Graph., vol. 22, no. 4, pp. 31–40, 1988.
- [42] T. Woo, "Feature Extraction by Volume Decomposition," in *CAD/CAM Technology in Mechanical Engineering*, 1982.
- [43] Y. S. Kim and D. J. Wilde, "A Convex Decomposition Using Convex Hulls and Local Cause of Its Non-Convergence," J. Mech. Des., vol. 114, no. September 1992, 1992.
- [44] Y. S. Kim, "Recognition of form features using convex decomposition," *Comput. Des.*, vol. 24, no. 9, pp. 461–476, Sep. 1992.
- [45] C. Ertelt and K. Shea, "An application of shape grammars to planning for CNC machining," in the ASME 2009 International Design Engineering Technical Conferences & Computers and Information in Engineering Conference IDETC/CIE, 2009.
- [46] H. Wang, Y. (Kevin) Rong, H. Li, and P. Shaun, "Computer aided fixture design: Recent research and trends," *Comput. Des.*, vol. 42, no. 12, pp. 1085–1094, Dec. 2010.

- [47] D. Bourne, J. Corney, and S. K. Gupta, "Recent Advances and Future Challenges in Automated Manufacturing Planning," J. Comput. Inf. Sci. Eng., vol. 11, no. 2, pp. 021006–01, 2011.
- [48] Y. Sermsuti-anuwat, "Milling fixture design: a tolerance analysis approach," *Int. J. Mech. Eng. Educ.*, vol. 37, no. 2, pp. 111–118, 2009.
- [49] Y. Kang, Y. Rong, and J. C. Yang, "Computer-Aided Fixture Design Verification . Part 2 . Tolerance Analysis," *Int. J. Adv. Manuf. Technol.*, vol. 21, pp. 836–841, 2003.
- [50] J. S. Pang and J. C. Trinkle, "Stability characterizations of fixtured rigid bodies with Coulomb friction," Proc. 2000 ICRA. Millenn. Conf. IEEE Int. Conf. Robot. Autom. Symp. Proc. (Cat. No.00CH37065), vol. 1, pp. 361–368.
- [51] Y. Kang, Y. Rong, and J. C. Yang, "Computer-Aided Fixture Design Verification. Part 3. Stability Analysis," *Int. J. Adv. Manuf. Technol.*, vol. 21, pp. 842–849, 2003.
- [52] L. Fan, B. N. Jagdish, A. S. Kumar, S. Anbuselvan, and S. Bok, "Collaborative Fixture Design and Analysis Using Service Oriented Architecture," *IEEE Trans. Autom. Sci. Eng.*, vol. 7, no. 3, pp. 617–629, 2010.
- [53] B. Dizioglu and K. Lakshiminarayana, "Mechanics of Form Closure," *Acta Mech.*, vol. 118, pp. 107–118, 1984.
- [54] X. Markenscoff and C. H. Papadimitriou, "The Geometry of Grasping," *Int. J. Rob. Res.*, vol. 9, no. 1, pp. 61–74, Feb. 1990.
- [55] A. F. Van der Stappen, C. Wentink, and M. H. Overmars, "Computing formclosure configurations," *Proc. 1999 IEEE Int. Conf. Robot. Autom. (Cat. No.99CH36288C)*, vol. 3, no. May, pp. 1837–1842, 1999.
- [56] R. a. Marin and P. M. Ferreira, "Optimal Placement of Fixture Clamps: Maintaining Form Closure and Independent Regions of Form Closure," J. Manuf. Sci. Eng., vol. 124, no. 3, pp. 676–685, 2002.
- [57] Y. Zheng and C.-M. Chew, "Efficient Procedures for Form-Closure Grasp Planning and Fixture Layout Design," *J. Manuf. Sci. Eng.*, vol. 131, no. 4, pp. 041010–1, 2009.

- [58] C. Munro and D. Walczyk, "Reconfigurable Pin-Type Tooling: A Survey of Prior Art and Reduction to Practice," J. Manuf. Sci. Eng., vol. 129, no. 3, pp. 551–565, 2007.
- [59] X. Xiaowen, X. Wei, and Z. Beirong, "Modular Reconfigurable Fixture Design Based Intelligent Algorithm," 2009 Int. Conf. Inf. Technol. Comput. Sci., pp. 156– 159, Jul. 2009.
- [60] G. Wilson and J. P. Weaver, "Light fixture using modular accessories," 2013.
- [61] S. Zirmi, H. Paris, and I. Belaidi, "Analysis of modular fixtures design," *Mécanique Ind.*, vol. 8, pp. 1–6, 2007.
- [62] S. H. Sun and J. L. Chen, "A Fixture Design System using Case-based Reasoning," *Eng. Appl. Artif. Intell.*, vol. 9, no. 5, pp. 533–540, 1996.
- [63] J. Chang, "Methodology for automatic fixture design in a computer-integrated environment," Purdue University, 1989.
- [64] J. Cecil, "Computer-Aided Fixture Design A Review and Future Trends," *Int. J. Adv. Manuf. Technol.*, vol. 18, no. 11, pp. 790–793, Nov. 2001.
- [65] M. H. Yadav and S. S. Mohite, "Computer integrated fixture design system," *Proc. Int. Conf. Work. Emerg. Trends Technol. - ICWET '11*, no. Icwet, p. 775, 2011.
- [66] Y. Kang, Y. Rong, and J. C. Yang, "Computer-Aided Fixture Design Verification. Part 1. The Framework and Modelling," *Int. J. Adv. Manuf. Technol.*, vol. 21, no. 10–11, pp. 827–835, Jul. 2003.
- [67] Y.-J. Tseng and S. B. Joshi, "Recognition of interacting rotational and prismatic machining features from 3-D mill-turn parts," *Int. J. Prod. Res.*, vol. 36, no. 11, pp. 3147–3165, 1998.
- [68] D. L. Waco and Y. S. Kim, "Machining feature reasoning using convex decomposition," *Adv. Eng. Softw.*, vol. 20, pp. 107–119, 1994.
- [69] P. B. Berra and M. M. Barash, "Automatic process planning and optimization for a turning operation," *Int. J. Prod. Res.*, vol. 7, no. 2, pp. 93–103, 1968.
- [70] S. K. Lai-Yuen and Y.-S. Lee, "Turn-Mill Tool Path Planning and Manufacturing Cost Analysis for Complex Parts Machining," in *Industrial Engineering Research* (*IERC*) Conference, 2002.

- [71] X. Zhang, R. Liu, a. Nassehi, and S. T. Newman, "A STEP-compliant process planning system for CNC turning operations," *Robot. Comput. Integr. Manuf.*, vol. 27, no. 2, pp. 349–356, Apr. 2011.
- [72] S. Huang, D. Liu, and B. Wang, "Research on Lathe Automatic Design System," in 2009 International Conference on Management and Service Science, 2009.
- [73] D. E. Culler, "The Turning Assistant : Automated planning for numerical control lathe operations." ProQuest Dissertation and Theses (PQDT), 1994.
- [74] S. Liu, "FEATURE EXTRACTION AND CLASSIFICATION FOR ROTATIONAL PARTS TAKING 3D DATA FILES AS INPUT," J. Chinese Inst. Ind. Eng., vol. 21, no. 5, pp. 432–443, 2004.
- [75] S. Suliman and K. Awan, "Automatic Recognition of Turning Features Using 2-D Drawing Files.," *JSME Int. J. Ser. C*, vol. 44, no. 2, pp. 527–533, 2001.
- [76] S. Li and J. J. Shah, "Recognition of User-Defined Turning Features for Mill/Turn Parts," *J. Comput. Inf. Sci. Eng.*, vol. 7, no. 3, pp. 225–235, 2007.
- [77] R. Dechter and R. Mateescu, "AND/OR search spaces for graphical models," *Artif. Intell.*, vol. 171, no. 2–3, pp. 73–106, Feb. 2007.
- [78] R. A. Walsh and D. R. Cormier, *Machining and metalworking handbook*, 3rd ed. McGraw-Hill Companies, Inc., 2006.
- [79] G. Boothroyd and W. A. Knight, *Fundamentals of machining and machine tools*, 3rd ed. Boca Raton, FL : CRC/Taylor & Francis, 2006.
- [80] J. P. Davim, Ed., *Machining : fundamentals and recent advances*. London : Springer, 2008.
- [81] B. Van Blarigan, M. I. Campbell, A. Eftekharian, and T. Kurtoglu, "Automated Estimation of Time and Cost For Determining Optimal Machining Plans," in *ASME 2012 International Design Engineering Technical Conferences & Computers and Information in Engineering Conference (IDETC/CIE)*, 2012.
- [82] P. H. Joshi, *Jigs and Fixtures Design Manual*, 2nd ed. McGraw-Hill Companies, Inc., 2003.
- [83] Y. (Kevin) Rong and Y. (Stephens) Zhu, Computer-Aided Fixture Design, 1st ed. New York: Marcel Dekker, Inc., 1999.

- [84] Y. (Kevin) Rong, S. H. Huang, and Z. Hou, *Advanced Computer-Aided Fixture Design*, 1st ed. Elsevier Academic Press, 2005.
- [85] S. J. Russell, Artificial Intelligence: Modern Approach. pp. 73–110.
- [86] R. T. Marler and J. S. Arora, "Survey of multi-objective optimization methods for engineering," *Struct. Multidiscip. Optim.*, vol. 26, no. 6, pp. 369–395, Apr. 2004.
- [87] L. Zadeh, "Optimality and non-scalar-valued performance criteria," *IEEE Trans. Automat. Contr.*, vol. 8, no. 1, pp. 59–60, Jan. 1963.
- [88] G. Anandalingam and T. L. Friesz, "Hierarchical Optimization: An Introduction," *Ann. Oper. Res.*, vol. 34, pp. 1–11, 1992.
- [89] T. Basar and H. Selbuz, "Closed-Loop Stackelberg Strategies with Applications in the Optimal Control of Multilevel Systems," *IEEE Trans. Automat. Contr.*, vol. AC-24, no. 2, pp. 166–178, 1979.
- [90] M. Seder, P. Mostarac, and I. Petrovic, "Hierarchical path planning of mobile robots in complex indoor environments," *Trans. Inst. Meas. Control*, vol. 33, no. 3–4, pp. 332–358, Feb. 2010.
- [91] R. Rajagopalan, K. G. Mehrotra, C. K. Mohan, and P. K. Varshney, "Hierarchical Path Computation Approach for Large Graphs," *IEEE Trans. Aerosp. Electron. Syst.*, vol. 44, no. 2, 2008.
- [92] Y.-J. Lai, "Hierarchical optimization : A satisfactory solution," *Fuzzy Sets Syst.*, vol. 77, pp. 321–335, 1996.
- [93] A. Autere, "Estimating search depths in hierarchical path planning," in *Proceedings 1999 IEEE/RSJ International Conference on Intelligent Robots and Systems*, 1999, vol. 3, pp. 1304–1309.
- [94] W. Jia and Z. Sun, "On Computational Complexity of Hierarchical Optimization," *Int. J. Found. Comput. Sci.*, vol. 13, no. 5, pp. 667–670, 2002.
- [95] W. Fu and M. I. Campbell, "Multi-objective Hierarchical Sorting Based Best First Search : An Application in Manufacturing Process Planning," in *THE TWENTY-SIXTH ANNUAL CONFERENCE ON INNOVATIVE APPLICATIONS OF ARTIFICIAL INTELLIGENCE*, 2014.

- [96] Z. Shen, G. Ameta, J. J. Shah, and J. K. Davidson, "A Comparative Study Of Tolerance Analysis Methods," J. Comput. Inf. Sci. Eng., vol. 5, no. 3, pp. 247–256, 2005.
- [97] O. W. Salomons, H. J. J. Poerink, F. Van Slooten, F. J. A. M. Van Houten, and H. J. J. Kals, "A Computer Aided Tolerancing Tool based on Kinematic Analogies," in *CIRP seminar on computer aided tolerancing*, 1995.
- [98] J. Gao, K. W. Chase, and S. P. Magleby, "Generalized 3-D tolerance analysis of mechanical assemblies with small kinematic adjustments," *IIE Trans.*, vol. 30, no. 4, pp. 367–377, Apr. 1998.
- [99] C. Mickaël and A. Bernard, "3D ISO manufacturing specifications with vectorial representation of tolerance zones," *Int. J. Adv. Manuf. Technol.*, vol. 60, no. 5–8, pp. 577–588, Oct. 2011.
- [100] G. Ameta, J. K. Davidson, and J. J. Shah, "Tolerance-Maps Applied to a Point-Line Cluster of Features," J. Mech. Des., vol. 129, no. 8, pp. 782–792, 2007.
- [101] G. Ameta, J. K. Davidson, and J. J. Shah, "Using Tolerance-Maps to Generate Frequency Distributions of Clearance and Allocate Tolerances for Pin-Hole Assemblies," J. Comput. Inf. Sci. Eng., vol. 7, no. 4, pp. 347–359, 2007.
- [102] S. H. Huang, Q. Liu, and R. Musa, "Tolerance-based process plan evaluation using Monte Carlo simulation," *Int. J. Prod. Res.*, vol. 42, no. 23, pp. 4871–4891, Dec. 2004.
- [103] E. C. Anderson, "Monte Carlo Methods and Importance Sampling," 1999.
- [104] N. S. Khan, "Generalized Statistical Tolerance Analysis And Three Dimensional Model For Manufacturing Tolerance Transfer in Manufacturing Process Planning," Arizona State University, 2011.
- [105] S. Hamou, A. Cheikh, J. M. Linares, and A. C. Daho, "A stochastic concept for the optimization of manufacturing tolerances in computer aided process plan simulation," *Int. J. Comput. Integr. Manuf.*, vol. 19, no. 7, pp. 663–675, Oct. 2006.
- [106] T. M. Sobh, T. C. Henderson, and F. Zana, "Tolerance Representation and Analysis in Industrial Inspection," J. Intell. Robot. Syst., vol. 24, pp. 387–401, 1999.
- [107] A. Desrochers and A. Rivibret, "A Matrix Approach to the Representation of Tolerance Zone and Clearances," *Int. J. Adv. Manuf. Technol.*, pp. 630–636, 1997.

- [108] A. Mujezinović, J. K. Davidson, and J. J. Shah, "A New Mathematical Model for Geometric Tolerances as Applied to Polygonal Faces," J. Mech. Des., vol. 126, no. 3, pp. 504–518, 2004.
- [109] L. Carrino, G. Moroni, W. Polini, and Q. Semeraro, "Machining Planning for Tolerance Synthesis," *Mach. Sci. Technol.*, vol. 7, no. 3, pp. 333–347, Jan. 2003.
- [110] S. H. Huang, H. C. Zhang, and W. J. B. Oldham, "Tolerance analysis for setup planning: A graph theoretical approach," *Int. J. Prod. Res.*, vol. 35, no. 4, pp. 1107–1124, 1997.
- [111] Q. Liu and S. Huang, "Rigorous application of tolerance analysis in setup planning," *Int. J. Adv. Manuf. Technol.*, vol. 3, pp. 196–207, 2003.
- [112] "Parasolid," 2012. [Online]. Available: http://www.plm.automation.siemens.com/en_us/products/open/parasolid/.

Vita

Wentao Fu was born in Henan Province of China on June 12, 1989. He attended the pilot class in the school of mechanical engineering of Shanghai Jiao Tong University (SJTU) at 2006, where he was studying mechanical engineering and automation and got his Bachelor's degree in Mechanical Engineering in June 2010. He entered the Mechanical Engineering graduate program at The University of Texas at Austin in August 2010. His research focuses on digital manufacturing and design, CAD/CAM, computational design synthesis, design optimization and automation, and artificial intelligence.

Permanent email address: fwtay001@gmail.com This dissertation was typed by the author.