THE BOLOCAM GALACTIC PLANE SURVEY. V. HCO⁺ AND N₂H⁺ SPECTROSCOPY OF 1.1 mm DUST CONTINUUM SOURCES

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ABSTRACT

We present the results of observations of 1882 sources in the Bolocam Galactic Plane Survey (BGPS) at 1.1 mm with the 10 m Henrich Hertz Telescope simultaneously in HCO⁺ J = 3-2 and N₂H⁺ J = 3-2. We detect 77% of these sources in HCO⁺ and 51% in N₂H⁺ at greater than 3σ . We find a strong correlation between the integrated intensity of both dense gas tracers and the 1.1 mm dust emission of BGPS sources. We determine kinematic distances for 529 sources (440 in the first quadrant breaking the distance ambiguity and 89 in the second quadrant). We derive the size, mass, and average density for this subset of clumps. The median size of BGPS clumps is 0.75 pc with a median mass of 330 M_{\odot} (assuming $T_{\rm Dust} = 20$ K). The median HCO⁺ linewidth is 2.9 km s⁻¹ indicating that BGPS clumps are dominated by supersonic turbulence or unresolved kinematic motions. We find no evidence for a size-linewidth relationship for BGPS clumps. We analyze the effects of the assumed dust temperature on the derived clump properties with a Monte Carlo simulation and find that changing the temperature distribution will change the median source properties (mass, volume-averaged number density, surface density) by factors of a few. The observed differential mass distribution has a power-law slope that is intermediate between that observed for diffuse CO clouds and the stellar initial mass function. BGPS clumps represent a wide range of objects (from dense cores to more diffuse clumps) and are typically characterized by larger sizes and lower densities than previously published surveys of high-mass star-forming regions. This collection of objects is a less-biased sample of star-forming regions in the Milky Way that likely span a wide range of evolutionary states.

Key words: Galaxy: kinematics and dynamics – Galaxy: structure – ISM: clouds – ISM: kinematics and dynamics – stars: formation – submillimeter: ISM – surveys

Online-only material: color figures, machine-readable tables

1. INTRODUCTION

Stars form out of clouds of dense molecular gas and dust. From detailed studies of nearby molecular clouds, we have developed a picture of how stars with masses typically close to our Sun's form and evolve onto the main sequence (e.g., Shu et al. 1987). A corresponding picture does not exist for the highest mass end of the stellar-mass spectrum. This is in part due to high-mass star-forming regions in our Galaxy being at greater distances, and thus being observed at lower spatial resolution, than low-mass regions. High-mass stars also form in highly clustered environments, whereas the well-studied nearby low-mass stars are typically more isolated (e.g., Taurus). Not even the basic formation mechanism of massive star formation (scaled-up version of monolithic core collapse versus competitive accretion formation; Shu et al. 1987; Bonnell & Bate 2006; McKee & Ostriker 2007) is yet well agreed upon, especially for the formation of the highest mass stars. It is possible that both processes are important in different regimes of the stellar mass spectrum. For low-mass stars, there are observational indicators of the evolutionary state of the protostar (e.g., T_{bol} —temperature of a blackbody with a peak at the fluxweighted mean frequency of the spectral energy distribution

and α_{IR} —IR spectral index, defining the Class 0, I, II, III system; Lada 1987; Evans et al. 2009); a universal evolutionary sequence for high-mass stars is still being developed and that exact ordering of the possible observational indicators (e.g., the presence of a H_2O maser or a CH_3OH Class I or Class II maser, e.g., Plume et al. 1997; Shirley et al. 2003; De Buizer et al. 2005; Minier et al. 2005; Ellingsen et al. 2007; Longmore et al. 2007; Purcell et al. 2009; Breen et al. 2010) is still debated.

One observational aspect that has limited our complete understanding of star formation is that we lack a complete census of the star-forming regions in our own Galaxy and, therefore, a census of their basic properties (size, mass, luminosity). Previous surveys of star-forming regions have been heavily biased. For instance, the earliest studies of dense molecular gas focused on known (optical or radio) H II regions where an O or B spectral type star had already formed. The discovery and cataloging of UCH II regions (e.g., Wood & Churchwell 1989) extended studies to an earlier embedded phase, but still required the presence of a forming high-mass star. Infrared Dark Clouds (IRDCs), clouds of dust and gas that are opaque at midinfrared wavelengths (i.e., $8 \mu m$), permitted less-biased studies of star-forming regions through the earliest (prestellar) phases and across the stellar mass spectrum (Carey et al. 2009; Peretto & Fuller 2009); however, they were limited to clouds at near kinematic distances and typically observable only in the inner

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Galaxy ($-60 \deg < \ell < 60 \deg$). Dust continuum observations at far-infrared through millimeter wavelengths provide the least-biased means to survey star-forming regions at all embedded evolutionary phases and a wide range of the stellar mass spectrum across the Milky Way since the emission is optically thin, always present, and can trace small amounts of mass.

In the past decade, new surveys of the Milky Way Galaxy have been made from mid-infrared through millimeter wavelengths. Several Galactic plane surveys are published or are currently being observed, including the Bolocam Galactic Plane Survey (BGPS; Aguirre et al. 2011), the APEX Telescope Large Area Survey of the Galaxy (ATLASGAL; Schuller et al. 2009), and the *Herschel* infrared Galactic Plane Survey (Hi-GAL; Molinari et al. 2010). The goals of these surveys are to look for the precursors to massive star formation in the Galaxy as a whole, without targeting individual regions known to contain forming stars. They are an integral part of completing a full census of star-forming cores and clumps in the Milky Way as they are sensitive to star formation at all stages.

The BGPS is a 1.1 mm continuum survey of the Galactic plane (Aguirre et al. 2011). Covering $220 \, \text{deg}^2$ at 33'' resolution, the BGPS is one of the first large-area, systematic continuum surveys of the Galactic plane in the millimeter regime. The BGPS spans the entire first quadrant of the Galaxy with a latitude range of |b| < 0.5 deg from the Galactic plane and portions of the second quadrant (Aguirre et al. 2011). The survey has detected and cataloged approximately 8400 clumps of dusty interstellar material (Rosolowsky et al. 2010). The BGPS is beam-matched to the spectroscopic data we are taking in this paper. This allows us to easily compare the gas and dust in the same phase of star formation. The BGPS data are available in full from the IPAC Web site.

The vast majority of sources detected in the BGPS represents a new population of dense, potentially star-forming clumps in the Milky Way. The basic properties of these objects such as size, mass, and luminosity depend on the distance to the objects. However, since the BGPS observations are continuum observations, they contain no kinematic information. In this paper, we use the line-of-sight velocity ($v_{\rm LSR}$) from a molecular line detection and a model of the Galaxy to determine the kinematic distance. Not only is $v_{\rm LSR}$ useful, but the line properties themselves can elucidate a number of properties of the dense gas in the clumps (e.g., virial mass, infalling gas, outflows, etc.).

Most kinematic surveys of the Milky Way have been performed using low gas density tracers (e.g., HII: Giovanelli et al. 2005; ¹²CO: Dame et al. 2001; GRS(¹³CO): Jackson et al. 2006). With these low density tracers, most lines of sight in the Galaxy have multiple velocity components. To mitigate this, we choose dense gas tracers that will be excited exclusively in the BGPS clumps. Surveying dense gas has been done before using CS J = 2-1 toward IRDCs (see Jackson et al. 2008). In this survey, we simultaneously observe two dense gas tracers HCO+ J = 3-2 and N₂H⁺ J = 3-2 using the 1 mm ALMA prototype receiver on the Heinrich Hertz Submillimeter Telescope (HHT). The HHT resolution of $\sim 30''$ at 1.1 mm is nearly beam-matched to the original BGPS survey, allowing a one-to-one comparison between these dense gas tracers and peak 1.1 mm continuum emission positions. These two molecular tracers have very similar effective excitation densities, $n_{\rm eff} \sim 10^4 \, {\rm cm}^{-3}$, that are well matched to the average density derived from the continuumemitting dust (see Dunham et al. 2010). The effective excitation density for a molecular tracer is defined in Evans (1999) as the density at a given kinetic temperature required to excite a 1 K line for a column density of $\log_{10} N/\Delta v = 13.5$. To determine the effective density, we use RADEX, which is a Monte Carlo radiative transfer code (Van der Tak et al. 2007), assuming $\log_{10} N = 13.5~\text{cm}^{-2}$ and $\Delta v = 1~\text{km s}^{-1}$. The chemistry of HCO+ and $N_2 \text{H}^+$ is useful, as these two

The chemistry of HCO^+ and N_2H^+ is useful, as these two molecules have opposite chemistries with respect to the CO molecule (Jørgensen et al. 2004). HCO^+ is created by CO and N_2H^+ is destroyed by CO. The formation routes of HCO^+ and N_2H^+ are dominated by the following reactions:

$$H_3^+ + CO \rightarrow HCO^+ + H_2$$
 (1)

$$H_3^+ + N_2 \rightarrow N_2 H^+ + H_2$$
 (2)

$$N_2H^+ + CO \rightarrow N_2 + HCO^+.$$
 (3)

For N_2H^+ to exist in large quantities, the gas must be cold where CO has frozen out onto dust grains. The ratio of N_2H^+/HCO^+ emission can be a chemical indicator of the amount of dense, cold gas in BGPS clumps. Even with the modest upper energy levels, E_u/k (HCO⁺ J=3-2) = 25.67 K and E_u/k (N_2H^+ J=3-2) = 26.81 K, these transitions can still be excited at low temperatures if the density of the gas is high enough. This brings up an interesting conflict for N_2H^+ : chemically, it favors a low kinetic temperature where CO is depleted but higher $T_{\rm kin}$ or higher gas density leads to a stronger excitation of the J=3-2 line.

In this paper, we present the results for spectroscopic observations of 1882 BGPS clumps. In Section 2, we discuss source selection and observing, calibration, and reduction procedures. In Section 3, the detection statistics, line intensities, velocities, and linewidths are analyzed. In Section 4, we calculate the kinematic distance to each detected source and determine our size–linewidth relations, clump mass spectra, and present a face-on view of the Milky Way Galaxy based on kinematic distances determined from our sample.

2. OBSERVATIONS, CALIBRATIONS, AND REDUCTION

2.1. Facility and Setup

Observations were conducted with HHT on Mount Graham, Arizona. The data were taken over the course of 44 nights beginning in 2009 February and ending in 2009 June. We utilized the ALMA Band-6 dual-polarization sidebandseparating prototype receiver in a 4-IF setup (Lauria et al. 2006, ALMA memo 553). With this setup we simultaneously and separately observe both the upper and lower sidebands (USB and LSB, respectively) in horizontal polarization (H_{pol}) and vertical polarization (V_{pol}) using two different linearly polarized feeds on the receiver. The receiver was tuned to place the HCO⁺ J = 3-2 (267.5576259 GHz) line in the center of the LSB. The IF was set to 6 GHz, which offsets the N₂H⁺ J = 3-2 line (279.5118379 GHz) in the USB by +47.47 km s⁻¹. The signals were recorded by the 1 GHz Filterbanks (1 MHz per channel, 512 MHz bandwidth in 4-IF mode; LSB velocity resolution $\Delta v_{\rm ch} = 1.12 \ {\rm km \ s^{-1}}$ and USB velocity resolution $\Delta v_{\rm ch} = 1.07 \ {\rm km \ s^{-1}})$ in each polarization and sideband pair $(V_{\text{pol}} \text{ LSB}, V_{\text{pol}} \text{ USB}, H_{\text{pol}} \text{ LSB}, H_{\text{pol}} \text{ USB}).$

http://irsa.ipac.caltech.edu/data/BOLOCAM_GPS/

Table 1 $\eta_{\rm mb}$ for Each Polarization and Sideband

Calibration Data	V_{pol} LSB HCO ⁺ $J = 3-2$	V_{pol} USB N ₂ H ⁺ $J = 3-2$	H_{pol} LSB HCO ⁺ $J = 3-2$	$H_{\text{pol USB}}$ $N_2H^+ J = 3-2$
$ \eta_{\rm mb} $ – Average $ \eta_{\rm mb} $ – MJD 918 – 920	0.81(0.04)	0.81(0.03)	0.70(0.03)	0.70(0.04)
	0.64(0.01)	0.64(0.02)	0.64(0.01)	0.64(0.02)

Note. The errors are the standard deviations of all main beam efficiencies for the dates specified.

2.2. Calibration and Sideband Rejections

Every observing session utilized three types of observations to calibrate the velocity offset, temperature scale, and rejection of the sideband separating receiver. The antenna temperature scale T_A^* is used at HHT and is set by the chopper wheel calibration method (Penzias & Burrus 1973). This temperature scale was then converted to $T_{\rm mb} = T_A^*/\eta_{\rm mb}$ by observing Jupiter and calculating the main beam efficiency ($\eta_{\rm mb}$; Mangum 1993)

$$\eta_{\text{mb}} = \frac{f_{\text{rej}} \cdot T_A^*(\text{Jupiter})}{J(\nu_s, T_{\text{Jupiter}}) - J(\nu_s, T_{\text{CMB}})} \cdot \left[1 - \exp\left(-\ln 2 \cdot \frac{\theta_{eq}\theta_{\text{pol}}}{\theta_{\text{mb}}^2}\right)\right]^{-1}, \tag{4}$$

where $J(\nu, T_B) = \frac{h\nu/k}{\exp(h\nu/kT_B)-1}$ is the Planck function in temperature units evaluated at the observed frequency ν and brightness temperature T_B , T_A^* is the average observed temperature of Jupiter in the bandpass, $T_{\rm Jupiter} = 170 \pm 5$ K, $T_{\rm CMB} = 2.73$ K, $\theta_{\rm eq}$, and $\theta_{\rm pol}$ are the daily equatorial and poloidal angular diameters of Jupiter, $\theta_{\rm mb}$ is the HHT FWHM (equal to 28%2 LSB and 26%9 USB). The sideband rejection correction factor is given by

$$f_{\text{rej}} = \left(1 + \frac{I(T_A^* \text{USB})}{I(T_A^* \text{LSB})}\right)^{-1}.$$
 (5)

We calculate $f_{\rm rej}$, by measuring the integrated intensity of the flux that bleeds over from the LSB into the USB by observing S140, a source with very strong HCO⁺ J=3–2 emission ($T_{\rm mb}=18~{\rm K}$). The average rejection was $-13.8~{\rm dB}$ in $V_{\rm pol}$ and $-15.2~{\rm dB}$ in $H_{\rm pol}$. We ignore the difference in atmospheric opacities between 267 GHz and 279 GHz since it is small.

We report the computed η_{mb} for each observing session in Table 1 (see Figure 1). Each data point for η_{mb} in Figure 1 consists of the average of five or more observations of Jupiter each night. There are no apparent trends in η_{mb} versus time except on MJD 918–920, when η_{mb} for V_{pol} is significantly lower than for the rest of the observing sessions. For these dates we choose to use the average η_{mb} and treat them independently from the rest of the calibration. A drop in the integrated intensity, $I(T_A^*)$, is also seen in the data taken from the two spectral line calibration sources, S140 and W75(OH) (Figure 1), supporting the decision to treat these days separately.

We also compared η_{mb} for the two polarizations and sidebands against each other (Figure 2). The two upper panels compare the USB and LSB of each polarizations against each other. These are highly correlated with Spearman's rank coefficients of $\rho \sim 1$, which is expected, as each linear polarization has its own feed. The Spearman's rank coefficient is a measure of the monotonic dependence between two variables. The lower panels compare the two polarization feeds of the LSB and two polarization feeds of the USB against each other. These are less well correlated with Spearman's rank coefficients of $\rho \sim 0.5$ and show that the

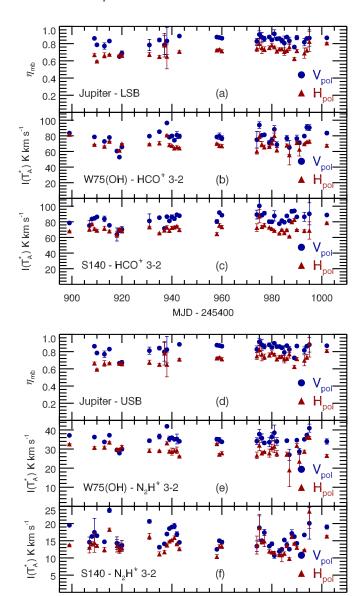


Figure 1. Calibrations of Jupiter, S140, and W75(OH) vs. MJD for the USB and LSB. For almost all observing sessions, $\eta_{\rm mb}$ and $I(T_A^*)$ are well behaved and consistent from day to day. At MJD - 245400 = 920–922, there were three days where $\eta_{\rm mb}$ in $V_{\rm pol}$ was significantly lower than the rest of the observations; this is also seen in the two line calibration sources in both sidebands. These days were taken to be independent and calibrated with the average values of $\eta_{\rm mb}$ for those three days as shown in Table 1.

940

960

MJD - 245400

980

1000

920

900

(A color version of this figure is available in the online journal.)

variation we see in η_{mb} does not come from a systematic effect that affects both polarizations at the same time.

We observed each source in the catalog described in Section 2.3 for 2 minutes total integration time. We position

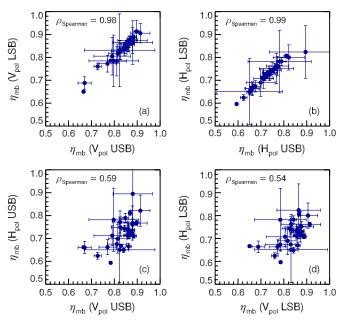


Figure 2. Two upper panels, (a) and (b), plot η_{mb} determined from the USB and LSB for each polarization. The two lower panels, (c) and (d), compare the two polarization feeds against each sideband. The Spearman's rank coefficients are printed in the upper left corner of each plot.

switched between a common OFF position for each 0.5 deg in Galactic longitude (ℓ). Each of these OFF positions was observed for 6 minutes to check if the OFF position had any detectable line emission. For a subset of sources near the end of our observations, starting on MJD - 245400 = 986, the integration time was increased to 4 or 10 minutes to compensate for deteriorating weather. Our goal was to keep the baseline rms less than 100 mK ($\Delta v_{ch} \sim 1 \text{ km s}^{-1}$) for as many sources as possible. S140 was also used to calculate the Allan Variance of the ALMA prototype receiver (Schieder & Kramer 2001). Accounting for the Allan Variance, we determined that \sim 20 s was the optimal switching time between ON and OFF positions for position switching with the 1 mm ALMA prototype receiver.

2.3. Source Selection

We selected sources out of a preliminary version of the BGPS source catalog (BOLOCAT: Rosolowsky et al. 2010). We used the BOLOCAT version 0.7 to divide sources into logarithmic flux bins with equal numbers using the 40" aperture flux. We point at peak 1.1 mm continuum positions as listed in the BOLOCAT and we restricted the range of Galactic longitudes to fall between $10^{\circ} \le \ell \le 100^{\circ}$. The entire BOLOCAT in this longitude range was divided into logarithmically spaced flux bins from $S_{1.1\text{mm}} = 0.1 \text{ Jy to } S_{1.1\text{mm}} \sim 0.4 \text{ Jy in intervals of}$ $\log_{10}(S_{1.1\text{mm}}) = 0.1$. All sources greater than $S_{1.1\text{mm}} \sim 0.4 \, \text{Jy}$ were included for observation (N = 689). Below this flux, 100 sources per bin were selected at random to comprise a flux-selected set of N = 1289 sources from the BOLOCAT v0.7. In addition, we observed all BOLOCAT v0.7 sources in ℓ ranges of 10° – 11° 5, 15° – 21° , and 80° – 85° 5. These ranges were chosen due to a combination of overlap with other surveys and observing availability. Sources with $\ell > 100^{\circ}$ were taken from the BOLOCAT v1.0 and were only restricted by observability.

Near the end of our spectroscopic survey, the BGPS version 1.0 maps and the BOLOCAT v1.0 were released. We recomputed the photometry of our sources at the observed v0.7 posi-

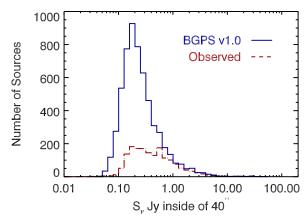


Figure 3. 40'' aperture fluxes for all of the BOLOCAT v1.0, solid blue line, and 40'' aperture fluxes for the BOLOCAT v0.7 positions that were observed with HHT as determined from the v1.0 maps, dotted red line.

(A color version of this figure is available in the online journal.)

tions on the v1.0 maps using the HHT beam size, this is the data presented in Section 3. A correction factor of 1.5 was multiplied to all of the 1.1 mm fluxes (see Aguirre et al. 2011). This calibration factor was determined by the BGPS team to account, in part, for the spatial filtering present in the BGPS v1.0 maps and possible calibration differences between the BGPS and other surveys. This factor brings the BGPS fluxes inline with those of other surveys (e.g., Motte et al. 2007).

Between versions of the catalogs the algorithms for processing the images were improved and thus source peak continuum positions may have moved or sources may even be removed from the catalog. The differences between the BOLOCAT v1.0 and our observed v0.7 sources are shown in Figure 3. In Section 4, we compare physical properties of the sources and need to know the overall source properties, and not just the photometry of the locations we observed. We take the nearest source from the v1.0 catalog to the position we observed. The median offset between observed v0.7 positions and v1.0 positions is 6".4. The vast majority (83%) of v0.7 observed positions lie within 15" (1/2 the beamwidth) of the nearest v1.0 position. Since the median angular size of our observed sources is \sim 60", the small positional differences between v0.7 and v1.0 do not significantly affect the physical properties derived from the 1.1 mm emission (e.g., size, mass). No source for which we have resolved the distance ambiguity and derived physical properties for in Section 4 (Known Distance Sample) has an offset between the catalogs greater than 30" (one beamwidth) when determining physical properties.

In the following analysis, we refer to the "Full Sample" of 1882 observed sources and the "Deep Sample" of 707 sources where the entire BOLOCAT was observed within the longitude ranges described above. Figure 4 shows the location of the sources we observed in the Full Sample and the sources in the Deep Sample.

2.4. Data Reduction

The spectra were reduced using scripts we developed for the CLASS software package. In 4-IF mode, there are four filterbank spectra for each source. The HCO⁺ J=3-2 spectrum was used to determine the baseline window, typically $\pm 50-75$ km s⁻¹ from the line center, and to determine the line window, typically $\pm 10-15$ km s⁻¹ from line center. The two

⁸ http://www.iram.fr/IRAMFR/GILDAS/

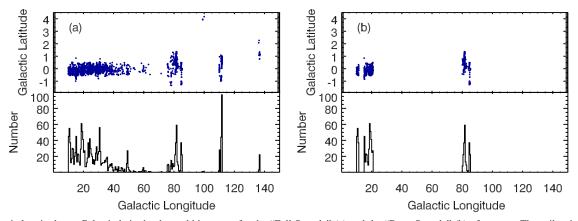


Figure 4. Galactic longitude vs. Galactic latitude plot and histogram for the "Full Sample" (a) and the "Deep Sample" (b) of sources. The spikes in the histogram around $\ell = +10, +20$, and +80 deg are due to the deep survey that was done after the initial survey was completed. The peaks at $\ell = +25, +30$, and +50 deg are due to the intrinsic number of sources in those areas. For $\ell > +90$ deg, these sources represent star formation complexes in the outer galaxy regions observed by the BGPS. (A color version of this figure is available in the online journal.)

Table 2 Line Flags

Flag Number	Flag Description
0	No detection: there is no visible line
1	Single detection: one line visible with no visible structure
2	Multiple detections: more than one line is visible in the spectrum
4	Obvious line wings: one line that shows a possible line wing(s)
5	Self-absorbed profile: one line that shows a possible self-absorbed profile
9	Unusable data: both polarizations have defects that make the spectrum unusable

polarizations of HCO⁺ J = 3-2 data were then baselined, and averaged together. This averaged spectrum is used to determine the line flag of the observed source and the line flag is determined from the approximate line shape (see Table 2). A flag of 0 means there is no apparent line in the spectrum at any velocity. A flag of 1 indicates a single line in the spectrum and the line exhibits no apparent structure from a line wing or self-absorbed profile. A flag of 2 means there was confusion along the line of sight and multiple velocity components are observed. In this case there is no way of determining which source is associated with the 1.1 mm map without mapping the molecular emission. A flag of 4 means there was a possible line wing. A Gaussian fit is plotted over the data to emphasize any deviations from a Gaussian shape; this helped to accentuate any sources with line profiles with a red or blue line wing, or possibly both. A flag of 5 means the line profile was possibly self-absorbed. Examples of spectra for the various flags are shown in Figure 5.

The N_2H^+ J=3-2 line is offset +47.47 km s⁻¹ from the center of the USB; therefore, each of the HCO⁺ baseline windows is shifted by that offset in order to baseline the N_2H^+ data. The N_2H^+ spectra are baselined and averaged in the same manner as above and the line is flagged for its quality and structure.

After each spectrum is flagged, it is converted to the $T_{\rm mb}$ scale and the two polarizations are averaged together. Each spectrum is corrected with the corresponding $\eta_{\rm mb}$ given by the date it was observed and its polarization, as explained in Section 2.2. The spectra are weighted by their baseline rms values, averaged, and baselined. The resulting combined spectra are used in our analysis.

2.5. Analysis Pipeline

Once the spectrum for each source has been calibrated and averaged, the next step is to measure the line properties. The analysis of all the spectra is performed in IDL using custom and ASTROLIB routines, and all CLASS spectra are exported to an ASCII file containing the final spectrum. The peak temperature is given by the maximum temperature within the defined line window and the error is the rms of the data outside of that window. Histograms of the baseline rms for all 1882 sources in HCO^+ and N_2H^+ are shown in Figure 6. The integrated intensity, central velocity, and line width are computed using both an analysis of the 0th, 1st, and 2nd moments and by fitting a Gaussian model to the spectral line.

2.5.1. Moment Analysis

The moments of a spectral line are calculated using

$$M_n = \sum_{i=v_l}^{v_u} T_i v_i^n \Delta v_{\rm ch}, \tag{6}$$

where n is the moment and i represents each channel between the v_l and v_u , defining the line window. These moments are then used to compute the integrated intensity, central velocity, and FWHM using

$$I(T_{\rm mb}) = M_0 \tag{7}$$

$$v_{\rm cen} = \frac{M_1}{M_0} \tag{8}$$

$$v_{\text{FWHM}} = \sqrt{8 \ln 2} \cdot \left(\frac{M_2}{M_0} - v_{\text{cen}}^2\right)^{1/2}.$$
 (9)

Moment calculations are sensitive to the rms of the baseline and our generously large line windows. For lower signal-tonoise lines, a small noise feature in the spectrum can drastically change the first moment when using all of the data points in the

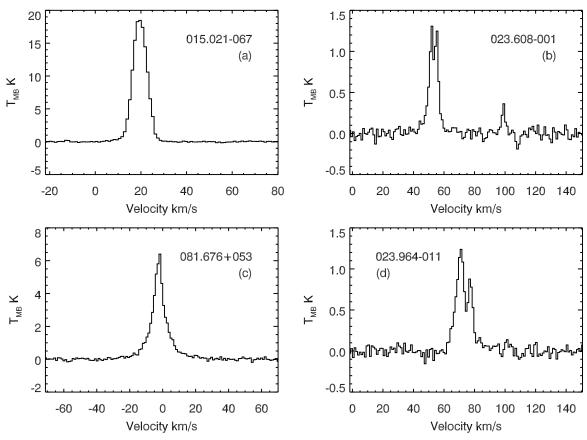


Figure 5. Sample HCO⁺ spectra of the four main flag types: (a) flag = 1—single detection, (b) flag = 2—multiple detections, (c) flag = 4—line wing(s), (d) flag = 5—self-absorbed spectrum.

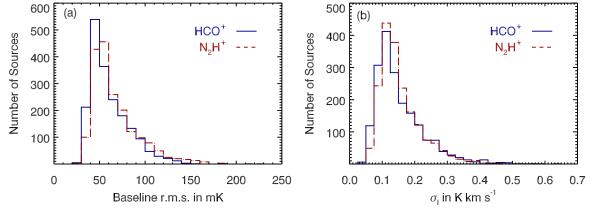


Figure 6. Histograms of the baseline rms (a) and σ_I (b) for all sources. Noise levels are lower than 100 mK rms in the baseline for the vast majority of sources (94% for HCO⁺ and 89% for N₂H⁺). The median baseline rms for HCO⁺ and N₂H⁺ are 53.8 mK and 58.6 mK, respectively. In σ_I , the median errors are 0.124 K km s⁻¹ and 0.138 K km s⁻¹ for HCO⁺ and N₂H⁺, respectively.

line window. To compensate for low signal-to-noise we estimate the line center using only data three times the baseline rms in the first moment calculation. This new method returns velocities and widths that more closely match those that are determined by eye than the method using all of the data within the line window. This only has significant effects for low signal-to-noise spectra.

2.5.2. Gaussian Fitting

Another method for determining the central velocity and FWHM for a spectral line is to fit a Gaussian model to the line profile. This method has its drawbacks as well, but the main

drawback is that it struggles with lines that deviate strongly from Gaussian shaped line profiles. Examples of such are lines with self-absorbed profiles or lines with very prominent line wings, (Figures 5(c) and (d)). The Gaussian fits are computed with the MPFITPEAK function (Markwardt 2009) and return a reduced χ^2 . The boundary conditions chosen are the following: (1) the baseline is defined to be 0, (2) the peak line temperature of the Gaussian is defined to be positive, (3) the central velocity of the line must be within the line window, and (4) the FWHM must be smaller than the line window. For the starting parameters of the fit, we use the results from the moment analysis.

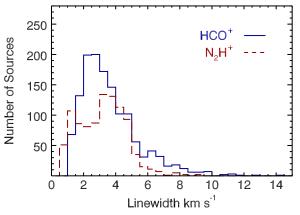


Figure 7. Histogram of HCO⁺ FWHM determined from the Gaussian fit to the spectrum. The Gaussian fits were computed using the MPFIT package also described in Section 2.5.2. The median of the distribution of FWHM is $2.9\,\mathrm{km\,s^{-1}}$. As a comparison, the median of the FWHM from the second moment calculation is $2.3\,\mathrm{km\,s^{-1}}$. The Gaussian linewidths for N_2H^+ are broadened due to hyperfine splitting and are not shown here. Fitting the hyperfine structure of N_2H^+ leads to a median FWHM of $3.5\,\mathrm{km\,s^{-1}}$ and are shown as the red curve. (A color version of this figure is available in the online journal.)

At this point we refine our method for computing the desired quantities for the line shape. After the initial Gaussian fit is completed, the next step is to modify the line window and recompute both the moment analysis and the Gaussian fitting. To modify the line window we used the parameters of the line as determined by the Gaussian fit to center the line window on the line center, $v_{\rm Gauss}$, and extend it by the measured linewidth, $\pm 2 \cdot \sigma_{\rm Gauss}$. If either bound of this new line window extends outside of the original, the original bounding velocity is used

for that term. The fit and moments are recomputed but do not yield significant changes for most sources. At this time σ_I (the error on the integrated intensity) is calculated using the final "fit" line window. $\sigma_I = \sigma_T \cdot \sqrt{\delta v_{\rm ch} \cdot (v_u - v_l)}$ where $v_{\rm ch}$ is the channel width ($\delta v_{\rm ch} = 1.1 \; {\rm km \; s^{-1}}$), v_u and v_l are the upper and lower bounds of the line window, and σ_T is the baseline rms. If the line was undetected, flag of 0, the line window used to estimate the error is \sim 6 km s⁻¹, within which more than 95% of all measured FWHMs lie (Figure 7). The Gaussian fits are used to determine the HCO⁺ and N₂H⁺ central velocities and the HCO⁺ linewidths while the zeroth moment is used to calculate the integrated intensity. For N₂H⁺ linewidths, we use an IDL script that deals with the hyperfine lines (assuming a Gaussian shape for each hyperfine line) and uses MPFIT to determine the best-fit line profile. For the rest of the paper, linewidths refer to only the Gaussian-fit, observed HCO+ linewidth. The data from the line analysis of each source is presented in Table 3.

3. DETECTION STATISTICS AND ANALYSIS

In this section, we discuss the statistics of the detected sources in HCO⁺ and N_2H^+ and correlations between integrated intensity for HCO⁺ and N_2H^+ with respect to the two sample groups. We also discuss the determined v_{LSR} and the analysis of the line centroids and linewidths.

3.1. Detection Statistics

Each source has two flags, one for HCO^+ and one for N_2H^+ ; multiple flags are not set for any of the sources/tracer pairs; it is either a detection (1, 2, 4, 5) or a non detection (0). A breakdown of the number of sources with each flag is shown in Figure 8. Out of a total of 1882 sources observed we detect 1444 (76.7%)

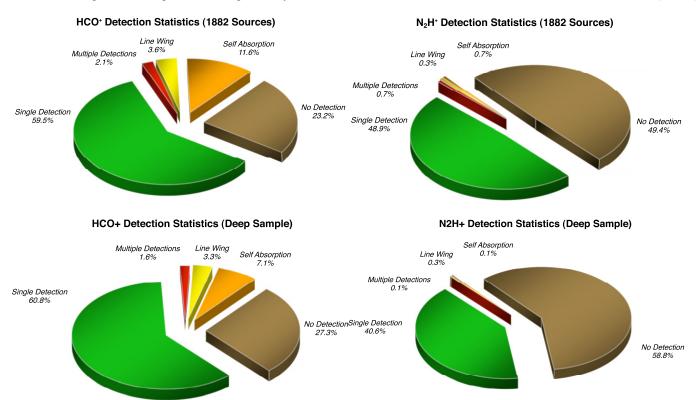


Figure 8. Detection statistics for HCO⁺ and N_2H^+ for all 1882 sources. We detect 76.7% of our sources in HCO⁺ and 50.5% in N_2H^+ at the 3σ level. Out of our "Deep Sample" N = 707, we detect 73.3% of sources in HCO⁺ and 41.2% of sources in N_2H^+ .

(A color version of this figure is available in the online journal.)

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Table 3
Example Data Table

BGPS	R.A.	Decl.	ℓ	b	Offset to	1.1 mm Flux	HCO+	$T_{mb}(HCO^+)$	I(HCO ⁺)	fwhm HCO+	$v_{\rm lsr}$ HCO ⁺	N ₂ H ⁺	$T_{\rm mb}({\rm N_2H^+})$	$I(N_2H^+)$	fwhm N ₂ H ⁺	v _{lsr} N ₂ H ⁺	D_{near}	$D_{ m far}$	Distance
Name	(hh:mm:ss)	(dd:mm:ss)	(°)	(°)	v1.0 (")	(Jy beam ⁻¹)	Flag	(K)	$(K \text{ km s}^{-1})$	$(km s^{-1})$	$(km s^{-1})$	Flag	(K)	$(K \text{ km s}^{-1})$	$(km s^{-1})$	$(km s^{-1})$	(kpc)	(kpc)	Flag
G010.014+00.084	18:07:28.5	-20:14:14.2	10.014	+0.084	5.2	0.246(0.061)	0	(0.069)	(0.324)			0	(0.083)	(0.211)					0
G010.017-00.398	18:09:16.9	-20:28:04.3	10.017	-0.398	137.1	0.102(0.067)	1	0.498(0.077)	1.955(0.447)	3.04	11.40	0	(0.098)	(0.248)			1.91	14.62	0
G010.026-00.356	18:09:08.5	-20:26:24.8	10.026	-0.356	7.8	0.375(0.050)	0	(0.088)	(0.228)			0	(0.103)	(0.260)					0
G010.043-00.424	18:09:26.0	-20:27:29.2	10.043	-0.424	105.6	0.171(0.051)	1	0.488(0.033)	1.521(0.071)	3.57	10.54	0	(0.040)	(0.103)			1.80	14.73	0
G010.051-00.210	18:08:39.0	-20:20:49.9	10.051	-0.210	7.7	0.227(0.049)	0	(0.055)	(0.142)			0	(0.046)	(0.117)					0
G010.068-00.408	18:09:25.3	-20:25:42.6	10.068	-0.408	3	0.441(0.058)	4	1.080(0.070)	4.906(0.349)	3.67	11.44	1	0.441(0.088)	1.362(0.182)	3.94	60.02	1.91	14.62	8
G010.077-00.194	18:08:38.7	-20:19:00.7	10.077	-0.194	2.4	0.439(0.055)	0	(0.091)	(0.480)			1	0.281(0.092)	0.730(0.191)	2.35	77.19			0
G010.084-00.438	18:09:34.0	-20:25:44.6	10.084	-0.438	4.2	0.268(0.058)	0	(0.069)	(0.399)			0	(0.090)	(0.227)					1
G010.087+00.034	18:07:48.9	-20:11:50.5	10.087	+0.034	13.1	0.145(0.051)	0	(0.076)	(0.196)			0	(0.086)	(0.217)					0
G010.104-00.012	18:08:01.2	-20:12:19.2	10.104	-0.012	2	0.315(0.048)	1	0.840(0.084)	3.896(0.442)	4.65	41.58	1	0.719(0.071)	3.595(0.146)	4.30	90.10	4.35	12.18	0
G010.105-00.418	18:09:32.3	-20:24:03.5	10.105	-0.418	4.6	0.454(0.073)	1	1.699(0.064)	7.047(0.340)	3.51	11.32	1	1.154(0.091)	4.465(0.189)	3.56	60.27	1.89	14.64	0
G010.113-00.076	18:08:16.7	-20:13:41.2	10.113	-0.076	7.2	0.216(0.066)	0	(0.065)	(0.167)			0	(0.086)	(0.217)					0
G010.139-00.370	18:09:25.7	-20:20:54.9	10.139	-0.370	27.7	0.720(0.085)	1	1.954(0.052)	7.521(0.136)	4.64	13.83	1	0.472(0.055)	1.526(0.115)	3.58	60.73	2.19	14.34	0
G010.149-00.408	18:09:35.5	-20:21:25.5	10.149	-0.408	2.2	0.662(0.071)	2	(0.043)	(0.144)			1	0.844(0.044)	3.943(0.111)	5.65	59.95			8
G010.164-00.360	18:09:26.6	-20:19:18.4	10.164	-0.360	8	3.717(0.091)	4	4.431(0.050)	20.571(0.131)	6.85	14.01	1	1.295(0.049)	6.322(0.125)	5.17	61.02	2.20	14.32	0
G010.191-00.390	18:09:36.5	-20:18:43.8	10.191	-0.390	4.9	0.598(0.087)	1	1.628(0.044)	6.012(0.093)	4.21	10.89	1	1.774(0.041)	8.501(0.103)	4.87	58.35	1.83	14.70	0
G010.204-00.244	18:09:05.5	-20:13:50.1	10.204	-0.244	10.4	0.207(0.059)	1	0.858(0.072)	2.930(0.418)	2.76	13.16	0	(0.094)	(0.238)			2.10	14.42	0
G010.209+00.048	18:08:01.0	-20:05:02.3	10.209	+0.048	185.9	0.156(0.058)	0	(0.067)	(0.175)			0	(0.073)	(0.184)					0
G010.213-00.324	18:09:24.6	-20:15:39.2	10.213	-0.324	2.9	2.331(0.095)	5	0.983(0.030)	5.151(0.090)	9.07	9.43	5	1.813(0.054)	10.322(0.157)	7.32	59.42	1.64	14.89	8
G010.226-00.209	18:09:00.5	-20:11:40.1	10.226	-0.209	3.8	1.422(0.056)	5	1.293(0.047)	6.012(0.122)	5.26	12.29	1	1.616(0.050)	7.548(0.127)	4.44	59.64	2.00	14.53	8

References. (1) Parallax; (2) IRDC Coincidence; (3) Kolpak et al. 2003; (4) Shirley et al. 2003; (5) Tangent Distance; (6) Outer Galaxy (7) W3/4/5 Region; (8) NGC 7538 Region; (9) Cygnus X Region; (10) Outer Arm (Cyg X;) (11) IC 1396; (12) 3 kpc Arm; (13) Outer Arm.

(This table is available in its entirety in a machine-readable form in the online journal. A portion is shown here for guidance regarding its form and content.)

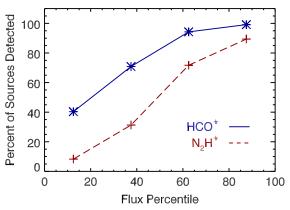


Figure 9. To see how detection statistics change with 1.1 mm flux we plot the percentage of detected sources vs. the percentile of its flux (e.g., the 25% of sources, by number, with the lowest flux, etc.). The highest percentile has a 99% detection rate in HCO $^+$ and a 88% detection rate of N_2H^+ .

in HCO⁺ and 952 (50.5%) in N₂H⁺ at a 3 σ or greater level. Out of 1444 HCO⁺ detections, 1119 (77.49%) are single-velocity component detections, 39 (2.70%) are multiple-velocity component detections, 67 (4.64%) have possible line wings, and 219 (15.17%) have a possible self-absorption profile. For the 952 N₂H⁺ detections, 919 (96.53%) are single-velocity component detections, 14 (1.47%) are multiple-velocity component detections, 6 (0.63%) have possible line wings, and 13 (1.37%) have a possible self-absorption profile. Breaking the sources down into the "Deep Sample" where we observed every source in the BOLOCAT v0.7 in certain ℓ ranges, we find slightly lower detection rates: 72.6% and 41.2% of the N = 707 sources are detected in HCO⁺ and N₂H⁺, respectively (see Figure 8 for a breakdown of the flagging statistics for the "Deep Sample"). Detection statistics versus 1.1 mm dust emission are presented in Figure 9. For sources in the lowest flux percentile, we detect barely 40% in HCO⁺. Sources in the highest flux percentile have a 99% detection rate in HCO⁺ and 88% in N₂H⁺.

We find that nearly all (99.6%) of N_2H^+ detections are associated with an HCO⁺ detection at the $\geqslant 3\sigma$ level. Only four sources that are detected in N_2H^+ do not have a 3σ detection in HCO⁺. These sources are approximately 2σ detections and show a small amount of HCO⁺ emission at the correct velocity to be associated with the N_2H^+ emission. The HCO⁺ line flag statistics change in a fairly interesting way for the sources with detected N_2H^+ . The percentage of sources showing a possible self-absorbed profile increases from 15.17% to 21.10%. The percentage of single line detections drops by a similar amount. About 1% of sources show possible self-absorption in both HCO⁺ and in N_2H^+ . For sources that display self-absorption in N_2H^+ , 11 of 13 also showed self-absorption in HCO⁺.

A recent mapping survey of these two molecular transitions toward a sample of IRDCs has shown that HCO⁺ and N₂H⁺ J = 3–2 emission has a very similar extent and morphology to the 1.1 mm emission (Battersby et al. 2010). To completely understand the physical properties of the gas that is excited in these transitions, we require a detailed source model and radiative transfer modeling of multiple transitions in each species. However, from our astrochemical knowledge of these two species, we can make some general statements about the regions where they are excited. HCO⁺ probes clumps with a wide range of properties. It can exist in warm regions where CO is abundant (e.g., Reiter et al. 2011) and cold regions where CO has frozen out onto dust grains (e.g., Gregersen et al. 2000). It

is possible that HCO⁺ is depleted by freeze-out in some of these clumps with cold (T < 20 K) dense ($n > 10^4 \text{ cm}^{-3}$) gas within the HHT beam (see Tafalla et al. 2006 for examples observed toward low-mass cores), although our observations indicate that this mechanism is unlikely to be dominant in BGPS clumps. $HCO^{+} J = 3-2$ emission likely originates in the dense, warm inner regions of these clumps. In contrast, N₂H⁺ is destroyed by CO in the gas phase, and thus N_2H^+ is most abundant in cold, dense gas where the CO abundance is depleted (Jørgensen et al. 2004). Thus, in star-forming clumps with a strong temperature increase toward the center, N₂H⁺ may only be tracing the outer parts of the clumps where the gas is still relatively dense and cold. This chemical differentiation of N₂H⁺ has been mapped in a few high-mass star-forming regions (Pirogov et al. 2007; Reiter et al. 2011; Busquet et al. 2011), although the differentiation mostly occurs on size scales that are unresolved within our 30" beam.

In nearly 12% of sources, the HCO+ line profiles display apparent self-absorption. For an optically thick line profile, a blue asymmetry (redshifted self-absorption) may be an indication of infalling gas (see Myers et al. 2000); however, the blue asymmetric profile can also be created by rotating and outflowing gas (Redman et al. 2004). For a large sample of sources, it is possible to statistically identify infall in the population by searching for an excess of blue asymmetric profiles. Infall does not create a red asymmetric profile in centrally heated, optically thick gas while rotation and outflow can equally produce both blue and red asymmetric profiles. Surveys of high-mass star-forming regions in HCN J = 3-2 have shown statistical excesses in blue asymmetric profiles (Wu & Evans 2003). In order to calculate the line asymmetry of our subset of sources with self-absorbed profiles, we must obtain observations of an optically thin isotopologue (H¹³CO⁺) to discriminate between self-absorption and a cloud with two closely spaced velocity components along the line of sight. We shall observe this subset of sources in $H^{13}CO^+ J = 3-2$ in a future study.

3.2. Integrated Intensity and Peak Line Temperature Analysis

3.2.1. Comparison of Molecular Emission

Figures 10(a) and (b) show the difference in the distributions of line temperature and integrated intensity for HCO⁺ and N₂H⁺ J = 3-2. The HCO⁺ emission extends to far greater intensities than N₂H⁺, whose distribution seems to be truncated at high intensities. We find, on average, in our Full Sample, HCO⁺ J = 3-2 to be 2.18 times as bright as N_2H^+ J = 3-2 in integrated intensity $I(T_{\rm mb})$ (Figure 11(a)). There are a small number of sources (11.8%, N = 114) detected in both HCO⁺ and N_2H^+ that show stronger N_2H^+ J=3-2 emission than HCO⁺ J = 3-2 emission. For these sources 1/3 are self-absorbed in HCO⁺. The integrated intensity of each species is highly correlated with a Spearman's rank correlation coefficient of $\rho = 0.82$. The slope of a linear regression (MPFIT) is m = 0.82, taking into account errors in the x- and y-directions. The highest intensity points appear to form a tail turning upward on the plot of $I(T_{\rm mb}~{\rm HCO^+})$ versus $I(T_{\rm mb}~{\rm N_2H^+})$. This would be expected for the warmest clumps since the N₂H⁺ abundance is expected to decrease in warmer regions, which should be more prevalent toward brighter 1.1 mm sources (Section 3.2.2).

The peak line temperature tells a story similar to the integrated intensities. The upward curving tail of points at the brightest end of the Full Sample is less noticeable for peak line temperature (Figure 11(b)). The average ratio of peak line temperatures is

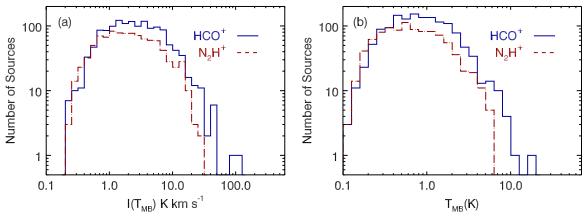


Figure 10. (a) Histogram of integrated intensity of HCO⁺ and N_2H^+ for the "Full Sample" of sources. These histograms are not scaled with respect to each other. They are logarithmically binned. Note the lack of sources with bright N_2H^+ J=3-2 emission and that HCO⁺ sources are on average brighter than the N_2H^+ . The median $3\sigma_{I(HCO^+)}=0.37$ K km s⁻¹ and median $3\sigma_{I(N_2H^+)}=0.41$ K km s⁻¹. (b) A histogram of peak line temperatures of HCO⁺ and N_2H^+ for the "Full Sample" of sources. These histograms are not scaled with respect to each other. They are logarithmically binned. While it is apparent from the T vs. T plots that HCO⁺ has a typically higher line temperature it is clear from these distributions there are two different cutoffs for the peak line temperature of HCO⁺ and N_2H^+ . The average $3\sigma_{T_{DK}(N_2H^+)}=0.16$ K and the average $3\sigma_{T_{DK}(N_2H^+)}=0.17$ K.

 $T_{\rm mb}({\rm HCO^+}~J=3\text{--}2)/T_{\rm mb}({\rm N_2H^+}~J=3\text{--}2)=1.94$ and the correlation coefficient is $\rho=0.79$. The best-fit line has a slope of m=0.83.

It is interesting that HCO⁺ and N_2H^+ J=3-2, with their similar effective densities but different chemistries, are so highly correlated. Their similar effective densities should result in their emission being cospatial; however, their chemical differences should result in differentiation (e.g., Jørgensen et al. 2004; Pirogov et al. 2007). It is likely that any differentiation is unresolved within our beam, which averages over the densities, temperatures, and abundance structure on size scales of a few tenths of a parsec (e.g., Battersby et al. 2010; Reiter et al. 2011).

3.2.2. Comparison with Millimeter Continuum Emission

In Figures 12(a) and (b), we show the integrated intensity of HCO⁺ J=3–2 and N₂H⁺ J=3–2 versus the 1.1 mm flux per beam obtained from the BOLOCAT v0.7 positions on the v1.0 BGPS maps (Rosolowsky et al. 2010). The Spearman's rank coefficient for the two species are $\rho_{\text{HCO}^+}=0.80$ and $\rho_{\text{N}_2\text{H}^+}=0.73$. The slopes are $m_{\text{HCO}^+}=1.15$ and $m_{\text{N}_2\text{H}^+}=1.28$. For HCO⁺, the high 1.1 mm flux points have a tail that continues curving up toward higher HCO⁺ emission with increasing 1.1 mm flux. In contrast, the N₂H⁺ J=3–2 emission for high 1.1 mm fluxes shows a flattening which is again consistent with N₂H⁺ being less abundant in warm sources. The median ratio of integrated intensity to 1.1 mm emission is 6.32 K km s⁻¹ per Jy/beam and 3.27 K km s⁻¹ per Jy/beam for HCO⁺ J=3–2 and N₂H⁺ J=3–2, respectively.

Comparing the peak line temperatures of the molecular emission versus the 1.1 mm dust flux (Figures 12(c) and (d)) leads to similar results as the integrated intensities. The correlations are still significant: $\rho_{\rm HCO^+}=0.75$ and $\rho_{\rm N_2H^+}=0.73$. The slopes are lower than those for integrated intensity: $m_{\rm HCO^+}=0.88$ and $m_{\rm N_2H^+}=0.98$. The median ratio of peak line temperature to 1.1 mm emission is 1.76 K per Jy/beam and 1.06 K per Jy/beam for HCO⁺ J=3–2 and N_2 H⁺ J=3–2, respectively.

We also compare the ratios of the integrated intensities and the peak line temperatures of HCO^+ and N_2H^+ with 1.1 mm flux in Figure 13. Both ratios are uncorrelated with the 1.1 mm dust emission. Surprisingly, there is a wide range in the observed intensity and peak temperature ratios, even for bright sources with fluxes above 1 Jy. Even in these brightest 1.1 mm sources, the $N_2H^+J=3-2$ emission can be strong, indicating significant amounts of unresolved dense, cold (T<20 K) gas within the beam. A summary of the log-fit parameters for each of the correlation plots is presented in Table 4.

3.3. Velocities and Linewidths

We use the Gaussian fit velocity centers of the HCO⁺ and N_2H^+ lines as described in Section 2.5.2 to determine v_{LSR} . We plot v_{LSR} versus Galactic longitude in Figure 14(a). We find that the distribution of v_{LSR} in the dense gas tracers is comparable to that of CO 1–0 (Dame et al. 2001). The spread in dense gas velocities is very similar to the spread in CO emission at each ℓ when our data is overplotted on the Dame et al. (2001) $v-\ell$ map. The v_{LSR} determined for sources detected in both HCO⁺ and N_2H^+ agree very well, see Figure 14 (b). We use only the Gaussian fit HCO⁺ velocities in Section 4 to calculate the kinematic distances of sources.

Figure 14(c) shows the FWHM of our detected HCO⁺ lines versus Galactic longitude. There is no trend with ℓ apparent in the sources we have observed. The few bins where the linewidth seems to vary by an appreciable amount have small numbers of sources in them. There is a moderate relationship in the plot of $\Delta v[\text{HCO}^+]$ versus $I(T_{\text{MB}})[\text{HCO}^+]$, see Figure 15(a). This is expected, as the integrated area of a line is directly related to the peak temperature multiplied by the FWHM. Given the relationship between $\Delta v[\text{HCO}^+]$ and $I(T_{\text{MB}})[\text{HCO}^+]$ and $S_{1.1\text{mm}}$ and $I(T_{\text{MB}})[\text{HCO}^+]$, it is logical to expect a trend of Δv with $S_{1.1\text{mm}}$; Figure 15(b) shows this trend. A moderate correlation also exists between the linewidth and the 1.1 mm dust emission per beam at the BOLOCAT v0.7 positions; however, there is large amount of scatter around this trend.

4. DISCUSSION

4.1. Kinematic Distances

We use the kinematic model of the Galaxy as defined by the parameters determined by Reid et al. (2009a) to calculate the

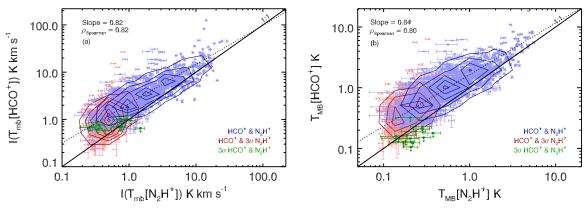


Figure 11. Comparison of the integrated intensities and line temperatures of HCO⁺ and N₂H⁺ for the "Full Sample" of sources. The light blue circles represent the 952 sources that have both an HCO⁺ and N₂H⁺ detection and the blue contours overlaid represent the density of points on the plot. The light red circles are HCO⁺ detections and 3σ N₂H⁺ upper limits. The red contours represent these points. The green circles are detections in N₂H⁺ that do not have a corresponding 3σ HCO⁺ detection and are upper limits for HCO⁺. The solid line plotted is the 1–1 line and the dotted line represents the best fit to the data. (a) A comparison of the integrated intensities (K km s⁻¹) of HCO⁺ and N₂H⁺. The slope of the best-fit line is m = 0.82. (b) A comparison of the peak line temperatures in Kelvin of HCO⁺ and N₂H⁺. The average source has a higher line temperature (T_{mb}) in HCO⁺ than N₂H⁺ by a factor of \sim 2. The slope of the best-fit line is m = 0.83.

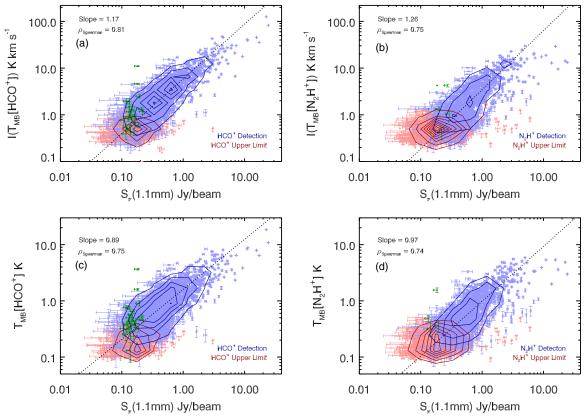


Figure 12. Two top figures, (a) and (b), show the integrated intensity of the molecular line vs. the 1.1 mm flux beam⁻¹ from the BOLOCAT v0.7 positions on the v1.0 maps. The light blue circles are the sources detected in HCO⁺(a), the light red circles are 3σ upper limits to the HCO⁺ line strength. The blue and red contours trace the density of points on the plot. The second panel (b) is the same plot but N_2H^+ integrated intensity is used instead. There is a strong correlation between the molecular emission and the dust emission $ρ_{HCO^+} = 0.80$ and $ρ_{N_2H^+} = 0.73$. The dotted line is the best fit to the blue points. We find the slopes of the two distributions to be $m_{HCO^+} = 1.15$ and $m_{N_2H^+} = 1.28$. The two lower figures, (c) and (d), show the peak line temperature of the molecular line vs. the 1.1 mm flux beam⁻¹ from the Bolocat v0.7 positions on the v1.0 maps. The symbols are the same as in the previous two plots. There is a strong correlation between the line temperature of the molecular emission and the dust emission $ρ_{HCO^+} = 0.75$ and $ρ_{N_2H^+} = 0.73$. We find the slopes of the two distributions to be $m_{HCO^+} = 0.88$ and $m_{N_2H^+} = 0.98$.

near and far distances to BGPS clumps. One thing to note is that the distance determination for Reid et al. (2009a) assumes that all motions are in the azimuthal direction only and does not account for any radial streaming which is known to exist near $\ell \sim 0$. This model sets the distance from the Galactic center to the Sun to be $R_0 = 8.4 \pm 0.6$ kpc and the circular rotation speed

 $\Theta_0=254\pm16~{\rm km~s^{-1}}$ from very long baseline interferometry (VLBI) parallax measurements. We then use these parameters and the kinematic definition of $v_{\rm LSR}$ to compute the distances to all of our sources with single HCO⁺ velocity components.

The distances for all detected sources are plotted versus Galactic longitude in Figure 16. In the first quadrant (0 $^{\circ}$ \leq

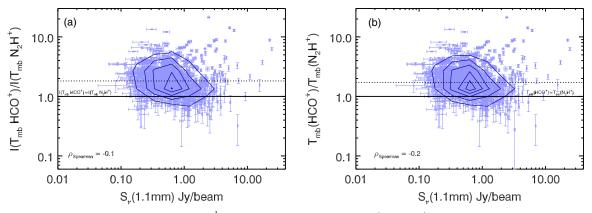


Figure 13. Ratio of molecular emission vs. 1.1 mm flux beam⁻¹ for all sources detected in both HCO⁺ and N_2H^+ . The ratio of integrated intensities (a) and peak line temperatures (b) vs. 1.1 mm emission are presented in these plots. The points in both diagrams are not well correlated with $\rho = -0.1$ for panel (a) and $\rho = -0.2$ for panel (b). The solid lines are where the ratio equals 1.0 and the dotted lines represent the median of the ratios for each panel, (a) 1.81 and (b) 1.69. (A color version of this figure is available in the online journal.)

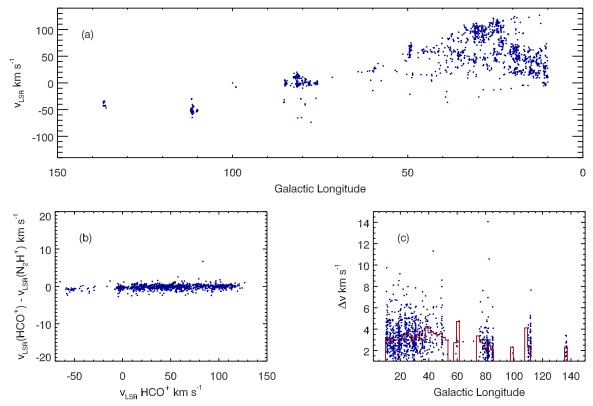


Figure 14. (a) HCO⁺ v_{LSR} determined from the Gaussian fit for each detected source vs. Galactic longitude. The envelope formed by the largest velocity at each ℓ represents the tangent velocity. (b) The comparison of v_{LSR} of HCO⁺ and N_2H^+ . The scatter in the data is 0.71 km s⁻¹ which is smaller than the width of a channel. (c) The HCO⁺ linewidth determined from the Gaussian fit vs. the Galactic longitude of each source. We also plot the median FWHM within bins in ℓ to emphasize any overall trends. There does not appear to be any strong relationship with ℓ .

 Table 4

 Summary of log Fit Parameters

log X-Axis	log Y-Axis	Intercept	Slope	Spearman's Rank (ρ)
I(N ₂ H ⁺) K km s ⁻¹	I(HCO+) K km s ⁻¹	0.33	0.823	0.82
$T_{mb}(N_2H^+) K$	$T_{mb}(\mathrm{HCO^{+}})~\mathrm{K}$	0.21	0.83	0.79
$I(HCO^+) \text{ K km s}^{-1}$	$S_{\nu}(1.1 \text{ mm}) \text{ Jy beam}^{-1}$.78	1.15	0.80
$I(N_2H^+) \text{ K km s}^{-1}$	$S_{\nu}(1.1 \text{ mm}) \text{ Jy beam}^{-1}$	0.55	1.28	0.73
$T_{mb}(HCO^+) K$	$S_{\nu}(1.1 \text{ mm}) \text{ Jy beam}^{-1}$	0.21	0.89	0.75
$T_{mb}(N_2H^+) K$	$S_{\nu}(1.1 \text{ mm}) \text{ Jy beam}^{-1}$	-0.01	0.99	0.73

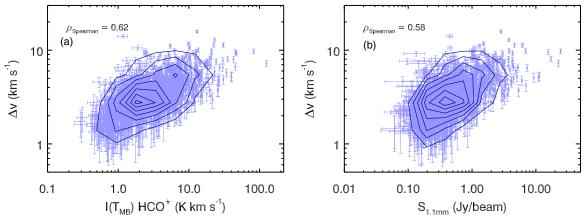


Figure 15. (a) The HCO⁺ linewidth determined from the Gaussian fit vs. the integrated intensity of the HCO⁺ line. There is a moderate correlation, with a Spearman's Rank coefficient of $\rho = 0.60$. (b) The HCO⁺ linewidth determined from the Gaussian fit vs. the 1.1 mm flux per beam from the BOLOCAT v0.7 positions, light blue circles. There is a lot of scatter but there is a moderate correlation between linewidth and 1.1 mm dust emission, $\rho = 0.54$. (A color version of this figure is available in the online journal.)

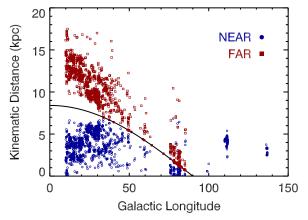


Figure 16. Kinematic distance vs. Galactic longitude for all sources detected and do not have a flag of 2. The near and far distances are shown in blue circles and red boxes, respectively. This version of the plot accentuates the number of sources that lie near the tangent points at each ℓ .

 $\ell < 90^{\circ}$), a velocity will give two distances that are degenerate. Without further information, we cannot tell if a source is on the near side or the far side of the galaxy. For sources that are known to be within a given region, and thus approximately the same distance, we can quantify the velocity spread of the individual sources. For instance, the spread in $v_{\rm LSR}$ for sources in 109° < $\ell < 112^{\circ}$ is 4.9 km s⁻¹. This is one measure of the systematic "random" errors in our v_{LSR} due to intrinsic motion that limits the accuracy of the corresponding distances. Some sources have much larger peculiar motions determined from VBLI parallax, as great as 40 km s⁻¹ (Nagayama et al. 2011), but it is not likely that the majority of sources will be severely discrepant. Some distribution of distances is expected and the spread in velocities for sources nearby makes an accurate kinematic distance determination difficult. In our distance determination, a cloud with a velocity at or greater than the tangent velocity will be placed at the tangent distance. In Section 4.2, we resolve the distance ambiguity for a subsample of our sources.

4.1.1. Galactocentric Distance

The Galactocentric distance is the distance of the source from the Galactic center and is only dependent on velocity and Galactic longitude of a source and therefore does not have a distance ambiguity. We plot a variety of source properties versus their Galactocentric distance in Figure 17. The distribution of sources clearly traces four major spiral arm structures in the Galaxy. The large peak at 4.5 kpc corresponds to the molecular ring and, for sources near $\ell=30^\circ$, the edge of the central bar. The largest concentration of sources is within these two structures. The other structures in order of galactocentric distance are the Sagittarius arm, the local arm, and the Perseus arm

We also plot the observed quantities (linewidth, integrated intensity, and 1.1 mm flux) versus Galactocentric distance. There is a large amount of scatter in each 1.5 kpc bin, and the median values of each quantity are nearly constant except for the bin beyond 10 kpc. The median linewidth, integrated intensity (both HCO⁺ and N₂H⁺), and 1.1 mm flux are systematically lower for sources beyond 10 kpc compared to smaller Galactocentric distances. This could be due to a bias in the original BGPS observing strategy. Sources at Galactocentric distances greater than 10 kpc are predominately in the second quadrant of the Galaxy. Only a few selected regions (e.g., Gem OB1, G111/NGC 7538, IC 1396) were observed by the BGPS in this quadrant. Unlike BGPS observations toward the first quadrant, these second-quadrant heterodyne follow-up observations are not a complete census of sources in the second quadrant and biased toward known star-forming regions. It is possible that the observed regions are not entirely representative of the properties of Galactic sources at this distance biasing our results to sources with stronger HCO⁺ and N₂H⁺ lines. This would make the "true" Galactocentric gradient larger than what we see in Figure 17. Another possibility is that nitrogen and/or carbon metallicity gradients in the Galaxy are becoming important, and that is why HCO+ and N₂H+ are becoming weaker, on average, beyond 10 kpc. There is a decreasing trend for both N and C in OB stars when going from the inner galaxy to the outer galaxy (Daflon & Cunha 2004). This same effect may manifest itself in the dense gas as well; however, more complete sampling is needed to understand these effects.

4.2. Resolving the Distance Ambiguity

We must determine whether or not a source lies on the near or far side of the tangent distance in order to resolve the distance ambiguity (see Figure 16). We use three conservative methods to

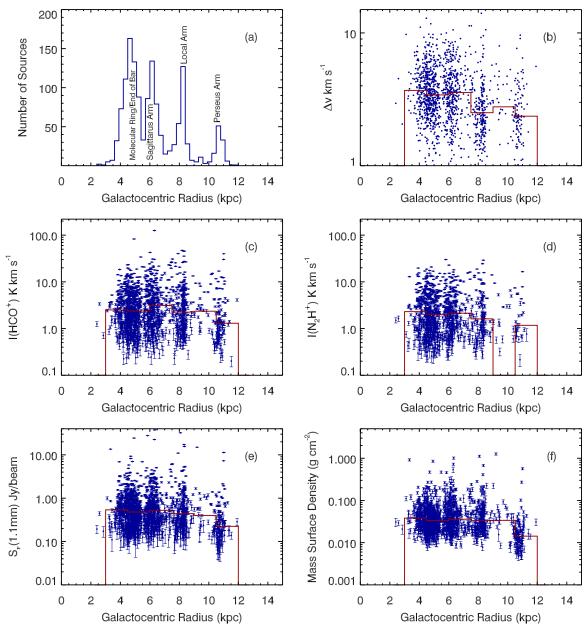


Figure 17. (a) Histogram of Galactocentric distance of all sources with a single HCO⁺ detection. (b) Linewidth vs. Galactocentric distance. (c) $I(T_{\rm MB}, {\rm HCO^+})$ vs. Galactocentric distance. (d) $I(T_{\rm MB}, {\rm N_2H^+})$ vs. Galactocentric distance. (e) 1.1 mm dust emission vs. Galactrocentric distance. (f) Mass Surface Density (Σ) vs. Galactrocentric distance. We overplot the median values the source properties in 1.5 kpc bins to look at trends in the data, only bins with N > 20 sources are plotted. In all cases the sources in the outer galaxy have smaller median values than those in the first quadrant. This is most apparent in panel (f), the Mass Surface Density plot.

break the degeneracy: coincidence with sources with observed maser parallax measurements, coincidence with IRDCs, and correspondence with known kinematic structures in the Galaxy. We then use this subsample of sources where the distance ambiguity has been resolved, the "Known Distance Sample," to study the properties of BGPS objects. A detailed study of the probability that BGPS sources in the first quadrant lie at the near or far distance is currently being made by T. Ellsworth-Bowers et al. (2011, in preparation).

The most accurate distance determination technique is direct parallax measurements of sources by VLBI (e.g., Reid et al. 2009a, 2009b). For a source to be considered associated with a Very Long Baseline Array (VLBA)-determined parallax, we allow for a source position to be different from the VLBA

position by up to 30'' (one beam size). We have four sources that are coincident on the sky with a VLBA source but only three with a single HCO⁺ detection. The distances used to these objects are their parallax distances.

The next selection criterion we used to determine distance is coincidence with an IRDC. IRDCs are clouds of dust that appear dark against the background of mid-infrared Galactic radiation (for example at 8 μ m). Because these objects appear in front of the majority of Galactic emission, they are assumed to be on the near side of the galaxy. Placing an IRDC at the near kinematic distance is a good assumption but disregards the fact that a small number of IRDCs could be at the far distance. IRDCs have been cataloged in the Galactic plane from *Midcourse Space Experiment (MSX)* mid-infrared observations

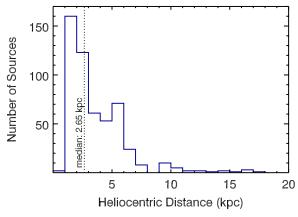


Figure 18. Histogram of heliocentric distance for the Known Distance Sample of sources with the distance ambiguity resolved. The median of the distribution is 2.65 kpc. The spike of sources that lies around 1 kpc are sources that are in the range of $\ell=80^\circ-85^\circ$ and sources in the outer Galaxy. We use other distance measurements for sources in these regions.

(Egan et al. 1999; Simon et al. 2006) and most recently from Spitzer Space Telescope observations (Peretto & Fuller 2009). Peretto & Fuller (2009) developed a catalog of IRDCs and describe each cloud with an ellipse. We first select sources that lie within the ellipse itself. In reality, IRDCs have a wide range of projected geometries and a simple ellipse is not always the best choice to describe more complicated filamentary shapes. Therefore, we also did a by-eye comparison of Spitzer GLIMPSE (Benjamin et al. 2003) images and BGPS images and made a list of BGPS sources that appeared to be coincident with an IRDC. Both the ellipse-coincidence method and the by-eye method suffer from different biases (e.g., the ellipse shape is too simple and the by-eye method is subjective and depends on image display parameters). We conservatively choose sources that are coincident with an IRDC from both methods to be assumed to be at the near distance (N = 192).

We have also included sources in the Known Distance Sample that do not have distance ambiguities, including sources in the Outer Galaxy ($\ell > 90^{\circ}$, N = 89) and sources in the first quadrant that lie at the tangent distance. A caveat is that the method used to compute the distances forces a source to be at the tangent distance if its velocity is larger than allowed in the circular rotation model of the Galaxy. We also include sources that are coincident with the sources in Shirley et al. (2003) and the HII regions in Kolpak et al. (2003). In addition to all of this we use kinematic information from Dame et al. (2001) to include sources near $\ell \sim 80^\circ$ that have the corresponding velocities of the Cygnus-X region. The other sources in this ℓ range have negative velocities, indicating they lie in the outer arms. We do the same analysis and add sources near $20^{\circ} < \ell < 55^{\circ}$ that have velocities corresponding to the Outer Arm. We also add a few sources with $\ell \sim 10$ that correspond to the 3 kpc Arm. All of the 529 sources for which the distance has been determined comprise our Known Distance Sample. For the remainder of the paper, we will only use the Known Distance Sample for our analysis of source properties unless otherwise specified. Resolution of the distance ambiguity for all observed sources is beyond the scope of this paper. In a future paper, we will build probability density functions for the distances to BGPS sources by combining dense gas tracers such as HCO+ and N₂H+ with extant data sets such as the Galactic Ring Survey (13CO (J = 1-0) for diffuse-gas velocity comparison, H_I Galactic

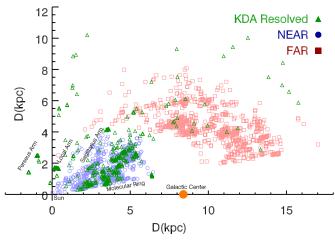


Figure 19. Face-on view of Galactic structure. Using the kinematic distances determined along with the Galactic longitude we make a polar plot presenting the face on view of the Milky Way. Sources in the Known Distance Sample are plotted as green triangles. In the first quadrant of the galaxy, sources with an unresolved distance ambiguity are plotted in blue circles and red boxes for the near and far distances, respectively. These points are plotted twice to represent the distance ambiguity for those not associated with an object that breaks the degeneracy. The large orange circle represents the Galactic Center and the Sun is located at the origin.

(A color version of this figure is available in the online journal.)

Plane Surveys (VGPS, CGPS, SGPS) for H_I self-absoption, models of Galactic molecular gas distribution, and a more refined analysis with IRDCs (T. Ellsworth-Bowers et al. 2011, in preparation).

Figure 18 is a histogram of the heliocentric distances for the Known Distance Sample. These sources include outer Galaxy sources, so the peaks of the distribution do not always correspond to a specific spiral arm. The observed peak of sources at 5 kpc from us does correspond with the Near 3 kpc arm and the edge of the Galactic bar. The median distance of the Known Distance Sample is 2.65 kpc. The large number of sources at a distance of 1–2 kpc comes from sources that are in the range of $\ell=80^{\circ}-85^{\circ}$ and those in the outer galaxy (W3/4/5, NGC 7538). In this area, the intrinsic dispersion of velocities is much larger than the allowable velocities for the kinematic model of the galaxy so we use known average distances to the regions in this ℓ range.

Compiling this distance information together gives us a look at Galactic structure. Figure 19 shows the face-on view of the Milky Way given the kinematic distances we have measured. The sources that lie in the Near Sample are separated from those where we have not resolved the distance ambiguity. The unresolved sources are plotted twice for their near and far distances. Even with the distance ambiguity affecting the majority of our sources one can begin to see strong evidence for Galactic structure including the Near 3 kpc arm, the end of the Galactic bar, as well as the Sagittarius and Perseus Arms. The "molecular ring" is also visible between 3 and 5 kpc from the center of the Galaxy.

4.3. Size-Linewidth Relation

Several physical properties of the clumps may be derived once the distance to the source is determined. The size of BGPS sources was determined from analysis of the flux distribution in 1.1 mm continuum images (Rosolowsky et al. 2010). The physical size of the object is simply $r = \theta \cdot Distance$, where θ is the angular radius of the sources. Figure 20(a) shows

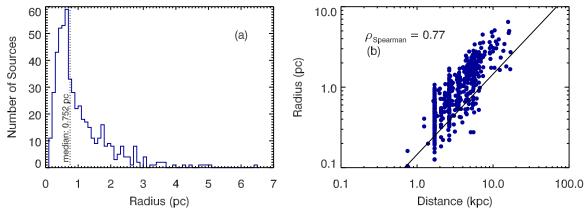


Figure 20. (a) The histogram of the source sizes, in pc, as determined from the distance and the angular size in BOLOCAT v1.0 for the sources in the Known Distance Sample. The median source size is 0.752 pc and is shown by the dotted line. (b) The radius of each source vs. the distance from us. This trend is primarily from the fact the radius is a function of distance for a given source size. The line plotted is the source size that corresponds to our beam size at each distance. (A color version of this figure is available in the online journal.)

histograms of the deconvolved angular source size as measured in the BOLOCAT v1.0. The median source size for the Known Distance Sample is $\sim 60''$ or 0.752 pc. This is a factor of 2.35 larger than the CS J = 5-4 source sizes from Shirley et al. 2003 (0.32 pc median source size) but inline with Wu et al. 2010 who find median sizes of 0.71 pc in HCN J = 1-0.0.77 pc in CS J = 2-1. This indicates that the typical BGPS clump is of lower density and more extended than the sample of water maser selected clumps traced in CS J = 5-4 in the Shirley et al. survey. CS J = 5–4 also has an effective density an order of magnitude higher than HCO⁺ J = 3-2 and is tracing the denser gas toward the center (Reiter et al. 2011). The Shirley et al. (2003) CS J = 5-4 survey was a very heterogeneous sample of sources that spanned a wide range of distances. In comparison to a more homogenous sample at a common distance the continuum survey of the nearby GMC Cygnus X, by Motte et al. (2007), find an average source size of 1.2 mm continuum clumps of 0.1 pc, with an HPBW of 11"; this is a factor of seven times smaller than the median BGPS clumps size.

We plot the clump size against the distance to the source (Figure 20(b)). There is a very strong relationship directly due to the fact that the physical size grows directly proportional to distance for a given angular size. The line indicates the physical size that is equivalent to our beam size at each distance. This shows that 89% of sources are spatially resolved by the BGPS beam. We caution that we are not resolving everything within the source as there is clear evidence of unresolved cores within the larger clump structures. Rather, the large size indicates that BGPS objects are, on average, larger and more diffuse structures than have been systematically studied before in high-mass star formation surveys.

The integrated kinematic motions along the line of sight determine the observed FWHM linewidth of the clumps. Linewidths may be broadened due to thermal motions, unresolved bulk flows of gas across a cloud, small scale (unresolved) turbulence, and optical depth effects. Thermal broadening for our sources is minimal since $\Delta v_{\rm therm}({\rm FWHM}) = 0.612~{\rm km~s^{-1}}$ at $T=20~{\rm K}$. The observed median linewidth of HCO+ for the Known Distance Sample is 2.98 km s⁻¹, which indicates supersonic motions within the 30" beam. The typical linewidth is comparable with the observed linewidths toward high-mass star-forming clumps (e.g., Shirley et al. 2003) and much larger

than the typical linewidths observed toward nearby low-mass star-forming cores (e.g., Rosolowsky et al. 2008). Comparing the distribution of linewidths versus distance shows no trend at all. As a source gets farther away, our beam is averaging over a larger source size; yet, we do not see any systematic increase in linewidth with distance.

Optical depth effects may broaden the observed linewidth. This effect may be especially acute for the HCO⁺ J=3–2 line (e.g., >11% of sources have evidence of possible self-absorption). Equation (10) shows that as the optical depth increases, the linewidth increases:

$$\frac{\Delta v}{\Delta v_o} = \frac{1}{\sqrt{\ln 2}} \sqrt{\ln \left(\frac{\tau}{\ln \left(\frac{2}{1 + e^{-\tau}}\right)}\right)}$$
 (10)

(Phillips et al. 1979). For $\tau=10$, the optically thick linewidth to the optically thin linewidth ratio is larger by a factor of two. For our observed linewidths, which are 10 times the thermal linewidth, even accounting for modest optical depth effects, it is unlikely that optical depth effects can account for the large observed median linewidth. Therefore, we conclude that the dense molecular gas in typical BGPS sources is characterized primarily by supersonic turbulence.

The size and linewidth of the Known Distance Sample clumps are directly compared in Figure 21(a). In contrast to the Larson relationship for molecular clouds (Larson 1981) we do not observe a strong size-linewidth relationship in the dense molecular gas for BGPS clumps: $\rho_{\text{Spearman}} = 0.40$. While there is a very weak trend that generally agrees with Larson's relationship, the scatter in the data erases our ability to say much about it. Traditionally, studies of the size-linewidth relationship in cores find two different slopes depending on the mass of the objects (Caselli & Myers 1995). For instance, the study of Caselli & Myers (1995) find a very shallow slope of $R^{0.21}$ for high-mass cores and a much steeper slope of $R^{0.53}$ for low-mass cores. Combining these two distributions may partially erase the size-linewidth relationship (Shirley et al. 2003); however, the derived power laws from Caselli & Myers (1995) predict significantly smaller linewidths than the sources in the Known Distance Sample. The lack of a correlation between size and linewidth argues against a universal scaling relationship between the amount of supersonic turbulence in dense clumps and their size.

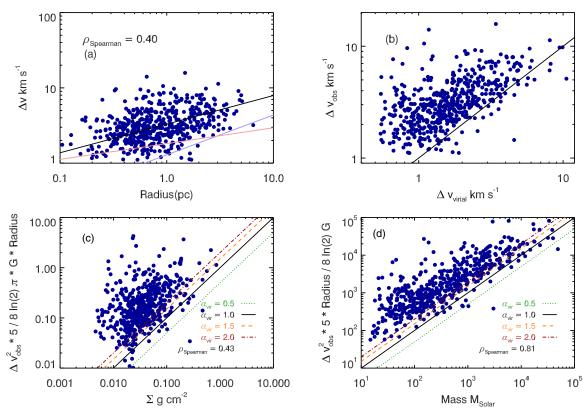


Figure 21. (a) Size linewidth relationship of the 529 sources that have determined distances. Overplotted is the Larson relationship from Larson (1981), black line. While it runs through the middle of our data, there is not enough of a trend to determine anything about it. Also plotted are the two power laws from Caselli & Myers (1995), $R^{.21}$ (light red line) for high mass and $R^{.53}$ (light blue line) for low mass. (b) Virial linewidth vs. observed linewidth shows that our clumps are not dominated by motions due to self-gravity with the majority of sources with observed linewidths larger than the virial linewidth. (c and d) Observed linewidth (1/e-width) vs. surface density/mass compared with the virial parameter α . The colored lines represent different values of the virial parameter. This plot also shows that few of the clumps have a virial parameter less than 1 and are fully gravitationally bound.

4.4. Mass Calculations

The clump mass may be calculated from the total 1.1 mm continuum flux for each source in the Known Distance Sample by

$$M_{\rm H_2} = \frac{S_{1.1} \cdot D^2}{B_{\nu}(T_{\rm dust}) \cdot \kappa_{\rm dust, 1.1} \cdot \frac{1}{100}}$$
(11)

(Hildebrand 1983), where $S_{1.1}$ is the total dust emission from a source, D is the distance to the source, $\kappa_{\rm dust}(1.1\,{\rm mm})=1.14\,{\rm cm}^2\,{\rm g}^{-1}$ is the dust opacity at 1.1 mm (Ossenkopf & Henning 1994), $B_{1.1{\rm mm}}$ is the blackbody intensity at 1.1 mm where we initially assume a temperature of $T_{\rm dust}=20\,{\rm K}$. We also assume a gas-to-dust mass ratio of 100:1 (Hildebrand 1983). Millimeter dust continuum observations are incredibly sensitive to small amounts of mass, as we can detect a 20 K source of $1.1\,M_\odot$ at distances of 1 kpc given an average 3σ flux threshold of 90 mJy at 1.1 mm. Below (Section 4.4.1), we will systematically explore the results of changing the dust temperature distribution of BGPS sources using a Monte Carlo simulation.

Figure 22(a) plots a histogram of the masses of the Known Distance Sample assuming $T_{\rm dust}=20$ K. The median mass of the sample is $320~M_{\odot}$ and the mean is $1648~M_{\odot}$. The BOLOCAT is complete to 98% for sources >0.4 Jy; this gives us a completeness limit for masses of $580~M_{\odot}$ at a distance of 8.5 kpc (most of our sources are at the near distance). The mass versus distance plot, Figure 22(b), shows the expected trend of more

massive sources at the farthest distances due to the D^2 term in the mass calculation. The masses we observed range from $10 M_{\odot}$ to $10^5 M_{\odot}$. Compared to other samples of high-mass clumps, we probe similar mass ranges as the H₂O maser sample of Shirley et al. (2003); although, our observed median mass is smaller. The mass distribution is similar to that observed for the BGPS Galactic Center sample for sources assumed to be at the distance of the Galactic center, 8.5 kpc (Bally et al. 2010). In comparison with sources targeted in regions of known star-formation, such as Orion (Johnstone & Bally 2006) and Cygnus-X (Motte et al. 2007), clumps in those studies probe typical masses of tens to hundreds of M_{\odot} , more analogous to core masses. In comparison to IRDCs, (Rathborne et al. 2005; Peretto & Fuller 2010), we appear to probe the same physical properties on the same scales. IRDC fragments tend to agree with masses of clumps in targeted regions, while the overall IRDC properties agree with those found in this study. For example, in Peretto & Fuller (2010) they find mass ranges of a few tenths of solar masses to nearly $10^5 M_{\odot}$ and are complete to $\sim 800 \, M_{\odot}$. We are sensitive throughout the entire mass range of these other samples, leading us to believe that we are observing objects that span from dense cores to clouds (see Dunham et al. 2010).

Using the dust-determined mass and the source size, we compute the volume-averaged number density given a mean free particle weight, $\mu = 2.37$ (Figure 23(a)), assuming each source is spherical in shape. The median value is $n = 2.5 \times 10^3$ cm⁻³, which is within a factor of three of the masses determined

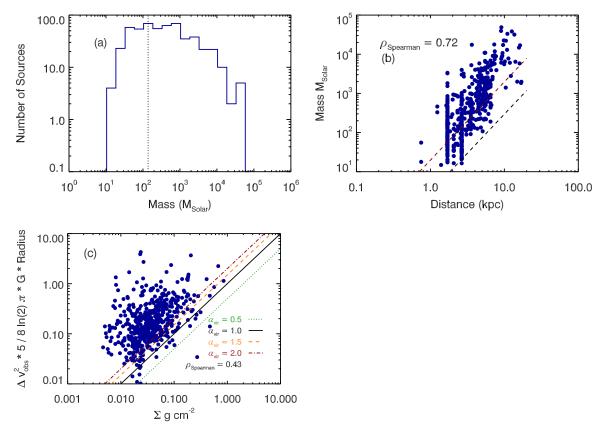


Figure 22. (a) Histogram of observed masses as determined from the 1.1 mm dust emission for the Known Distance Sample. The median of this distribution is $320\,M_\odot$ and the mean is $1272\,M_\odot$. Our completeness limit is $\sim 140\,M_\odot$ shown by the black dotted line based on a source of 1 Jy (above which we observe every object in the BOLOCAT) at our median distance. (b) The distribution of masses vs. the distance from us. The main trend in this plot is due to the distance dependence of the conversion from flux to mass, $M \propto D^2$. The black dotted line represents the mass corresponding to our minimum flux vs. distance. The red dotted line represents a 1 Jy source vs. distance. (c) Differential mass histogram with $d\log M = 0.3$ (bin size) assuming $T_d = 20\,\mathrm{K}$. The black dotted line is our completeness limit, see panel (a). The slope of the line is fit from the largest mass peak of the distribution to the highest masses. The slope determined for this "binned" differential mass histogram is m = -0.70 which is not the slope we determine from the MLE analysis of m = -0.91. This difference is directly caused by the fact that we have binned the data and it will change based on the way one chooses the bin size.

in the NH₃ survey of Gem OB1, where they find a median volume-averaged density of $n = 6.2 \times 10^3 \text{ cm}^{-3}$ (Dunham et al. 2010a). Compared to the IRDC sample of Peretto & Fuller (2010), we probe the same range of volume-averaged number densities from 100 to 10⁴ cm⁻³. This low volume-averaged number density is a result of the large observed source sizes and, therefore, large volume observed toward BGPS clumps. The volume-averaged density is lower than the typical effective excitation density for HCO⁺ and $N_2H^+J = 3-2$ emission. Steep density gradients are known to exist in both low-mass (Shirley et al. 2002) and high-mass (Mueller et al. 2002) star-forming clumps. If we were resolving individual dense knots, we would expect to see a trend of linewidth with volume-averaged density as well (Figure 23(c)). Therefore, BGPS sources tend to be fairly low-density sources with possible compact high-density regions that may be probed with higher angular resolution observations. Some of these clumps of low density gas contain high density regions up to $n = 10^5$ cm⁻³, several orders of magnitude higher than the average source properties (Dunham et al. 2011).

Comparing the timescales of these clumps shows that the free-fall and crossing timescales are similar at a few times 10^5 years. The median free-fall time is 8×10^5 yr; thus, if these clouds were bound, it would take a few hundred thousand years to collapse and begin forming stars. With the masses of

these clumps we also compute the virial linewidth as

$$\Delta v_{\text{virial}}^2 = \frac{8 \ln 2aGM_{\text{virial}}}{5 R}$$

$$\approx \frac{a \cdot \frac{M_{\text{obs}}}{209 M_{\odot}}}{(R/1 \text{ pc})(\Delta v_{\text{obs}}/1 \text{ km s}^{-1})^2} \text{ km s}^{-1} \qquad (12)$$

$$a = \frac{1 - p/3}{1 - 2p/5}; \quad p = 1.5.$$
 (13)

This definition includes the correction factor for a power-law density distribution of p=1.5 (Bertoldi & McKee 1992; Shirley et al. 2003). The virial linewidth represents the velocity dispersion from internal motions due to self-gravity. Figure 21(b) shows that the virial linewidths are smaller on average than the observed linewidths, about 2–3 km s⁻¹ indicating that many of the BGPS clumps are not entirely gravitationally bound. It is likely that there are smaller denser regions within these clumps that are gravitationally bound.

We can also look at the virial parameter in terms of the surface density (see Section 4.4.1) of the clumps given by

$$\alpha_{\text{virial}} = \frac{5\Delta v_{\text{obs}}^2}{8 \ln 2\pi G \Sigma R}.$$
 (14)

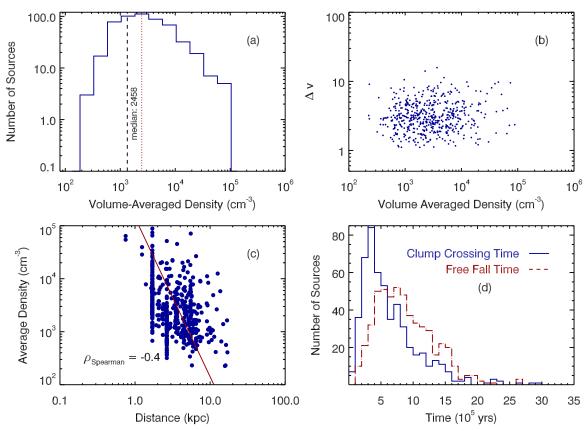


Figure 23. (a) Volume-averaged number density for the Known Distance Sample. The median value is 2.4×10^3 cm⁻³ (red dotted line). We are complete to ~ 1300 cm⁻³ (black dashed line). (b) Δv vs. the average density. (c) The average volume density of a source vs. distance. We are able to measure higher densities for closer sources because source size increases with distance given our finite beam size. Only nearby sources can be fully resolved. The red line indicates our volume-averaged number density completeness vs. distance for a $\sim 140~M_{\odot}$ object, Mass completeness limit, with size equal to the beam size, minimum resolved source size. (d) The clump free-fall timescale and the clump crossing timescales. The median free-fall time is $\sim 8 \times 10^5$ yr. The median crossing time is $\sim 5 \times 10^5$ yr.

This is shown in Figure 21(c). The virial parameter versus mass is also shown in Figure21 (d). This is another way of showing that few of our clouds indicate virialized motion ($\alpha <\sim 1$) and most lie more than a factor of a few above this line. The caveat is we assume that the BGPS traces ALL the mass which may not be entirely true. The BGPS does resolve out diffuse emission and the dense gas tracers are missing the low-density gas traced by CO or H I. It appears that most of the clumps we see are likely not gravitationally bound but do contain dense substructures that likely are. A table of the computed quantities is presented in Table 5.

4.4.1. Differential Mass Histogram

Figure 22(c) shows the differential mass histogram for the number of sources in bins of log(M). In this parameterization, the mass function takes on the form of

$$\frac{dN}{d\log(M)} \sim M^{-(\alpha-1)},\tag{15}$$

where the power-law index is the slope of a line through the histogram. For the observed masses, calculated assuming a dust temperature of 20 K, we find a slope of $\alpha-1=0.91$. This slope is shallower than the slope of the Salpeter stellar initial mass function (IMF) $\alpha-1=1.35$ for $dN/d\log(M)$. Our observed slope is steeper than has been found for the mass distribution of CO clumps $\alpha-1=0.6-0.7$ (e.g., Scoville

et al. 1987). Observations of dense-gas tracers tend to increase the differential mass histogram slope. For instance, Shirley et al. (2003) find a slope of $\alpha-1=0.9$ for their cumulative mass function for cores probed by CS J=5–4. In comparison to IRDCs (Peretto & Fuller 2010), they find a slope of $\alpha-1=.85$ for the total IRDC. This intermediate slope also suggests that we really are looking at the intermediate case of star-forming "clumps" rather than clouds or cores.

There are several sources of uncertainty in determining the slope of the differential mass histogram which we must characterize. The effect of binning has been shown to cause problems in studies of the stellar mass function and thus will also be problematic with the clump mass spectrum (Maíz Apellániz & Úbeda 2005). For instance, the choice of bin size may have a substantial effect on the computed slope of the differential mass histogram. Bins with small numbers of sources dominate the fit if the binwidth is chosen too small, and the number of bins used in a linear regression decreases rapidly if the binwidth is too large. Our data do not span many decades in mass above the estimated completeness limit in the Known Distance Sample, and thus choosing an appropriate binwidth is difficult. We can circumvent this binning problem by using the maximum-likelihood estimator (MLE) to compute the powerlaw slope α (Clauset et al. 2007; Swift & Beaumont 2010). The MLE maximizes the likelihood that the data were drawn from a given model. If the data are drawn from the distribution given by Equation (16), then the maximum likelihood estimate of the

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Table 5Example Table of Computed Quantities^a

BGPS	ℓ	b	1.1mm Flux	Distance	Mass	FHMW HCO+	Virial Parameter	Beam-averaged Density	Volume-averaged Density	Mass Surface Density	Free-fall Time	Clump Crossing Time
Name	(°)	(°)	$(Jy beam^{-1})$	Flag	(M_{\odot})	$({\rm km}~{\rm s}^{-1})$	$lpha_{ m vir}$	$n = \text{cm}^{-3}$	$n = \text{cm}^{-3}$	$(g \text{ cm}^{-2})$	(10^5 yr)	(10^5 yr)
G010.014+00.084	10.014	0.084	6.5	12	790	2.683	3.436	752.6	568.2	0.016	16.78	13.066
G010.068-00.408	10.068	-0.408	1.917	2	249	3.678	10.511	4560.1	1326.8	0.02	10.981	4.889
G010.213-00.324	10.213	-0.324	1.641	2	492	9.071	23.717	28188	6662.8	0.072	4.9	1.452
G010.226-00.209	10.226	-0.209	2	2	695	5.269	8.055	14106.7	3270.1	0.05	6.995	3.557
G010.403-00.202	10.403	-0.202	1.844	2	107	4.975	21.303	4570.7	5260	0.037	5.515	1.725
G010.621-00.441	10.621	-0.441	6.5	12	917	3.345	1.34	1708.2	26650.2	0.224	2.45	3.055
G010.625-00.338	10.625	-0.338	6.5	12	5063	4.725	2.527	5085.7	1037.4	0.045	12.419	11.276
G010.631-00.510	10.631	-0.51	6.5	12	1648	2.975	2.061	1695.1	1123.8	0.033	11.932	11.997
G010.651-00.126	10.651	-0.126	3.468	2	134	6.264	44.083	1112.8	1505.3	0.017	10.31	2.241
G010.665-00.161	10.665	-0.161	3.506	2	132	5.326	26.62	1099	2681.3	0.025	7.725	2.161
G010.671-00.220	10.671	-0.22	3.503	2	552	3.621	5.289	3482.5	1926.3	0.033	9.114	5.721
G010.687-00.308	10.687	-0.308	6.5	2	1709	2.318	1.459	1371.6	658.9	0.023	15.583	18.621
G010.726-00.332	10.726	-0.332	6.5	12	2119	3.176	2.102	2495.4	948.3	0.032	12.989	12.932
G010.743-00.126	10.743	-0.126	3.433	2	571	5.564	13.11	3964.7	1558.3	0.029	10.133	4.04
G010.745-00.295	10.745	-0.295	6.5	12	467	1.176	0.855	497.6	749.7	0.017	14.609	22.81
G010.752-00.200	10.752	-0.2	3.671	2	554	3.082	4.709	2430.5	1033.7	0.022	12.441	8.276
G010.799-00.380	10.799	-0.38	6.5	12	434	2.918	5.589	501.1	723.8	0.016	14.868	9.078
G010.985-00.370	10.985	-0.37	6.5	12	1478	2.945	2.902	1148.6	471.6	0.018	18.42	15.608
G010.989-00.084	10.989	-0.084	3.456	2	992	2.6	1.944	4472.3	1649.3	0.036	9.85	10.197
G011.053-00.040	11.053	-0.04	3.506	2	91	1.733	4.189	903.2	1703	0.017	9.693	6.836
G011.063-00.096	11.063	-0.096	3.427	2	680	3.005	3.621	2925	1293.8	0.027	11.121	8.435

Note. ^a Calculated quantities in this table assume $T_d = 20 \text{ K}$ for all sources.

References. (1) Parallax; (2) IRDC Coincidence; (3) Kolpak et al. 2003; (4) Shirley et al. 2003; (5) Tangent Distance; (6) Outer Galaxy; (7) W3/4/5 Region; (8) NGC 7538 Region; (9) Cygnus X Region; (10) Outer Arm (Cyg X); (11) IC 1396; (12) 3 kpc Arm; (13) Outer Arm.

(This table is available in its entirety in a machine-readable form in the online journal. A portion is shown here for guidance regarding its form and content.)

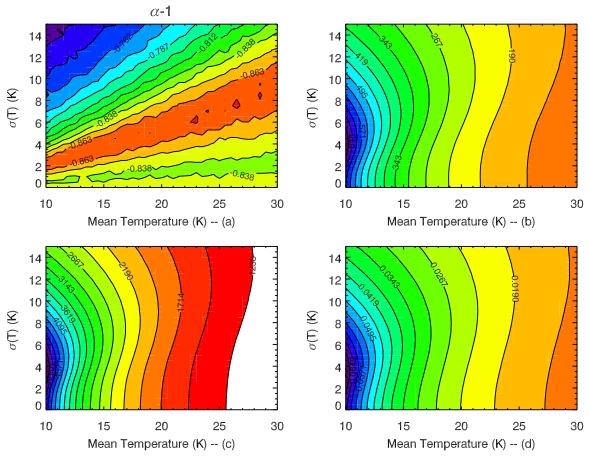


Figure 24. (a) Variation of the power-law index with choice of temperature distribution. (b) A Monte Carlo simulation of the median mass with variations in temperature. The units are in M_{\odot} . (c) A Monte Carlo simulation of the median volume-averaged number density with variations in temperature. The units are in cm⁻³. (d) A Monte Carlo simulation of the median surface density for variations in T_{dust} . The units are g cm⁻².

power-law index is $\hat{\alpha}$ given by Equation (17), where M_{\min} is the lower bound of the power-law behavior and n is the number of sources with mass greater than M_{\min} (Clauset et al. 2007),

$$p(x) = \frac{\alpha - 1}{M_{\min}} \left(\frac{M}{M_{\min}}\right)^{-\alpha} \tag{16}$$

$$\hat{\alpha} = 1 + n \left[\sum_{i=1}^{n} \ln \frac{M_i}{M_{\min}} \right]^{-1}. \tag{17}$$

Another important source of uncertainty is the assumed dust temperature of BGPS sources. We initially assume $T_{\rm dust}=20~{\rm K}$ for every source in the Known Distance Sample to compute our masses (M. Merello et al. 2011, in preparation). In reality, BGPS sources have a range of dust temperatures of an unknown distribution. We perform a Monte Carlo simulation of the differential mass distribution to constrain the range α by assuming that the source temperature distribution is approximated by a Normal distribution, characterized by mean $T_{\rm mean}$ and $\sigma(T)$. We then compute the mass of each source with a random temperature drawn from the temperature distribution and the source flux that has an error term drawn randomly from a Normal distribution added in. For each $T_{\rm mean}$ and $\sigma(T)$, the mass histogram is computed 10^4 times, and we calculate the median value of $\hat{\alpha}$.

The variation of α with the temperature distribution is shown in Figure 24(a). The effect of temperature distribution

is significant but not strong. As part of the MLE procedure we estimate the best value of $M_{\rm min}$, the minimum mass used in the power-law fit for each mass distribution. This is determined by minimizing the Kolmogorov–Smirnov statistic between the best-fit model and $M_{\rm min}$ as a function of $M_{\rm min}$ (Clauset et al. 2007; Swift & Beaumont 2010). The dependence of $M_{\rm min}$ on temperature means that colder temperatures lead to higher masses for a given observed flux. This dependence is also seen in the median of the mass distribution, Figure 24(b), and the median volume-averaged number density, Figure 24(c).

There are several important caveats that must be considered in this analysis. Foremost, the BGPS pipeline reductions will leave artifacts in the data. The process by which the sky variation is removed from the data will also remove some of the diffuse emission, resulting in spatial filtering of the 1.1 mm brightness distributions (Aguirre et al. 2011). Furthermore, the cataloging algorithm is also more sensitive to peaked emission than low levels of diffuse emission (Rosolowsky et al. 2010). This means we are not seeing diffuse sources unless they are very bright. We are missing flux from extended emission surrounding the clumps we do see, thus leaving us with a lower limit on the total mass, and it also affects the derived sizes. This survey is flux-limited, which means we also suffer from Malmquist bias. The BGPS is sensitive to different types of sources (i.e., cores and clumps versus clouds) as the distance increases (see Dunham et al. 2010). The last caveat is that the brightest BGPS clumps (most massive) are associated with HII regions which heat the dust and may contain a significant amount of free-free

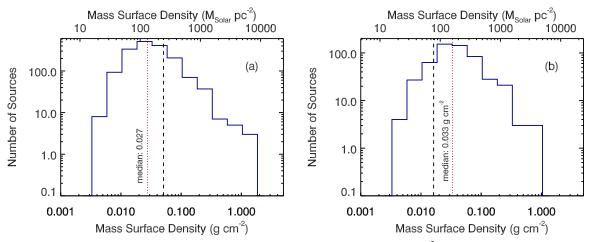


Figure 25. (a) Surface density for the entire sample assuming $T_{\text{dust}} = 20 \text{ K}$. The median value is 0.027 g cm⁻². The completeness limit for the entire sample is 0.051 g cm⁻² which is based on a source of 1 Jy coupled with the beam size (black dashed line). (b) The surface density histogram for the Known Distance Sample. The median value is 0.033 g cm⁻². The completeness limit for the Known Distance Sample is 0.016 g cm⁻² which is based on mass completeness and the median size of a clump (black dashed line).

emission which would most likely lead to a steepening of the mass spectrum. However, we present one of the first differential mass distribution with statistically significant numbers showing that massive clumps appear to have a shallower slope than nearby low-mass cores.

4.4.2. Mass Surface Density

While the derived quantities discussed above depend explicitly on distance, one quantity that is distance independent is mass surface density. We compute the mass surface density while assuming $T_{\rm dust} = 20 {\rm K}$ from

$$\Sigma_{\rm H_2} = \frac{M_{\rm H_2}}{\pi R^2} = \frac{37.2 \cdot S_{\rm Jy}}{\theta_{\rm arcsec}^2} \,\mathrm{g \, cm^{-2}},\tag{18}$$

where Σ only depends on the observed flux, observed source size, and the assumed dust temperature.

Figure 25(a) shows the mass surface density for the all of the BGPS sources we observed with determined fluxes and sizes from the v1.0 catalog (N = 1684). Since dust temperature variations affect the derived mass (Section 4.4.1), we also perform a Monte Carlo simulation to calculate the median mass surface density for distributions with different T_{mean} and T_{σ} . The Monte Carlo simulation includes variations of the fluxes by the Normal distribution corresponding to the flux and error on the flux. Figure 25(b) shows how the median of the surface density distribution changes with temperature. The median of the $T_{\rm dust} = 20 \,\rm K$ distribution is $0.027 \,\rm g \, cm^{-2}$ for the Full Sample and $0.033 \,\rm g \, cm^{-2}$ for the Known Distance Sample, indicating that the properties derived from the Known Distance Sample are likely representative of the total sample. Both values are significantly smaller than the results from Shirley et al. (2003), where they find a median surface density of 0.605 g cm^{-2} . Our median surface density is also much smaller than the $1.0 \,\mathrm{g}\,\mathrm{cm}^{-2}$ threshold that Krumholz & McKee (2008) require for massive star formation (see Fall et al. 2010).

The dependence of the median of surface density distribution on temperature is shown in Figure 24(d). The median mass surface density only increases by up to a factor of 2.5 for distributions with colder dust temperatures but they are still significantly below that of Shirley et al. (2003). The smaller

mass surface density is likely a result of the larger clump sizes measured for BGPS clumps compared to previous surveys. However, our result does not indicate that these BGPS clumps are not capable of forming massive stars. It is likely that observations with higher spatial resolution will reveal the observed mass surface density approaching 1.0 g cm⁻² for cores within BGPS clumps. Indeed, the infrared populations of BGPS clumps have recently been characterized by Dunham et al. (2011) who found that many BGPS clumps are in fact forming high-mass stars. They find that 49% of sources that are in the regions where the BGPS overlaps with other mid-IR Galactic plane surveys contain at least one mid-IR source.

5. CONCLUSIONS

We used the 10 m Heinrich Hertz Telescope to perform spectroscopic follow-up observations of 1882 sources in the BGPS. We simultaneously observed HCO⁺ J=3–2 and N₂H⁺ J=3–2 emission using the dual-polarization, sideband-separating ALMA prototype receiver. Out of the 1882 observed sources, we detect ~77% of the sources in HCO⁺ and over 50% in N₂H⁺. Multiple velocity components along the line of sight to BGPS clumps in these dense molecular gas tracers are rare. Our detection statistics are somewhat biased toward more detections because this sample includes all of the intrinsically brightest sources.

We find a strong correlation between peak temperature and integrated intensity of each dense gas tracer with each other and with the 1.1 mm dust flux. The median ratio of HCO⁺ integrated intensity to 1.1 mm flux is 5.42 K km s⁻¹ per Jy/beam. We find that HCO⁺ is brighter than N_2H^+ for the vast majority of sources, with a subset of only 117 sources (12.6% of sources singly detected in N_2H^+) where N_2H^+ is the brighter of the two dense gas tracers. The ratio of the peak line temperature and integrated intensity of the two molecules does not correlate well with 1.1 mm dust emission.

The observed $v_{\rm LSR}$ appear to follow the same distribution with Galactic longitude as $^{13}{\rm CO}~J=1$ –0 emission observed by Dame et al. (2001). We determine the linewidths from a best-fit Gaussian model and find little change, on average, with Galactic longitude. The median linewidth is 2.98 km s⁻¹, indicating

that BGPS clumps are dominated by supersonic turbulence. Linewidths only modestly correlate with 1.1 mm flux.

We compute kinematic distances for all detected sources and are able to break the distance ambiguity for 529 of our detections in the first and second quadrants using IRDC coincidence, VLBA-determined parallax source coincidence, or proximity to the tangent velocity or known kinematic structures. Using the set of sources of known distance, we compute the radius, mass, and average density of the sources. We find the median source size to be 0.752 pc at a median distance of 2.65 kpc, typically larger than source sizes observed in published surveys of high-mass star-forming clumps and cores. Comparing linewidth to the physical size of the source, we do not find any compelling evidence for a size–linewidth relation in our data. We find our sources lie above the relationships found by Caselli & Myers (1995) and have too small of a correlation to say much about Larson's relationship (Larson 1981).

For an assumed dust temperature of 20K we find a median mass of $\sim 300\,M_\odot$, a low median volume-averaged number density of $2.4\times 10^3~\rm cm^{-3}$, and a median mass surface density of $0.03~\rm g~cm^{-2}$. The similarity of the median mass surface density between the full sample and the Known Distance Sample indicates that the sources in the Known Distance Sample are characteristic of the Full Sample. Compared to published surveys of high mass star formation, BGPS clumps tend to be larger and less dense on average. We also analyzed the variation in median mass and volume density using a Monte Carlo simulation of cores with various dust temperature distributions. From the differential clump mass histogram, we find a power-law slope $(dN/d\log M)$ that is intermediate between the slope derived for diffuse CO clumps and the stellar IMF. Finally, a comparison of the virial linewidth to the observed linewidth indicates that many of the BGPS clumps in this survey have motions consistent with not being gravitationally bound.

In the future, we plan to complete observations of the BGPS catalog for all sources with $\ell \geqslant 10^\circ$ in the dense molecular gas tracers HCO⁺ and N₂H⁺ with the HHT. This will be the largest systematic survey of dense molecular gas in the Milky Way. A series of follow-up observations are currently underway to characterize the physical properties (density, temperature) and evolutionary state of BGPS clumps.

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Facilities: HHT (ALMA Band 6)

APPENDIX

In this appendix, we derive the relationship between σ_T and σ_I for a Gaussian line profile.

Assume that the spectral line is well described by a Gaussian function:

$$T(v) = T_{\text{pk}} \cdot e^{\left(-4\ln(2) \cdot v^2 / \Delta v_{\text{FWHM}}^2\right)},\tag{A1}$$

where $T_{\rm pk}$ is the peak line temperature and $\Delta v_{\rm FWHM}$ is the FWHM linewidth. The integrated intensity of this line is thus defined by the integral of temperature with velocity over the line window:

$$\int T(v) dv = T_{\rm pk} \cdot \Delta v_{\rm FWHM} \cdot \sqrt{\frac{\pi}{4 \ln(2)}}.$$
 (A2)

We may then ask the question, if we have a non-detection in integrated intensity, then how many σ_T (baseline rms) correspond to $3\sigma_I$? Let us rewrite $T_{\rm pk}$ for the undetected Gaussian line as

$$T_{\rm pk} = N \cdot \sigma_T. \tag{A3}$$

The standard formula for the uncertainty of the integrated intensity as given by

$$\sigma_I = \sigma_T \cdot \sqrt{\Delta v_{\rm ch} \cdot \Delta v_{\rm int}},\tag{A4}$$

where $\Delta v_{\rm ch}$ is the velocity resolution of each channel in the spectrum and $\Delta v_{\rm int}$ is the velocity interval integrated over which encompasses the entire line, the line window. We choose a line window that integrates over 99% of the area in the line which is two times the 3σ velocity width of the Gaussian line. The $\frac{1}{e}$ velocity width is related to the FWHM by

$$v\left(\frac{1}{e}\right) = \frac{\Delta v_{\text{FWHM}}}{\sqrt{4 \ln(2)}}.$$
 (A5)

Thus $2 \cdot 3\sigma_v$ (the full width of the line, in both directions) is

$$\Delta v_{\rm int} = 6 \cdot \Delta v_{\rm FWHM} \cdot \sqrt{4 \ln(2)}. \tag{A6}$$

Therefore, the ratio of I to σ_I is

$$\frac{I}{\sigma_I} = \left(\frac{N \cdot \sigma_T \cdot \Delta v_{\text{FWHM}} \sqrt{\frac{\pi}{4 \ln(2)}}}{\sigma_T \cdot \sqrt{\Delta v_{\text{ch}}} \cdot \sqrt{\frac{6 \cdot \Delta v_{\text{FWHM}}}{\sqrt{4 \ln(2)}}}}\right). \tag{A7}$$

Setting the ratio $\frac{I}{\sigma_I}$ equal to 3 and solving for N gives

$$N = 6 \cdot \sqrt{\frac{3 \cdot \sqrt{\ln(2)}}{\pi}} \cdot \sqrt{\frac{\Delta v_{\rm ch}}{\Delta v_{\rm FWHM}}},\tag{A8}$$

which is approximately

$$N \sim 4.88 \cdot \sqrt{\frac{\Delta v_{\rm ch}}{\Delta v_{\rm FWHM}}}.$$
 (A9)

For example, if we have a barely resolved line with $\Delta v_{\rm ch} = 1$ and $\Delta v_{\rm FWHM} = 1$, a 4.88 σ detection in temperature of a Gaussian line would be a 3σ detection in integrated intensity.

REFERENCES

Aguirre, J. E., et al. 2011, ApJS, 192, 4

Bally, J., et al. 2010, ApJ, 721, 137

Battersby, C., Bally, J., Jackson, J. M., Ginsburg, A., Shirley, Y. L., Schlingman, W., & Glenn, J. 2010, ApJ, 721, 222

Benjamin, R. A., et al. 2003, PASP, 115, 953

Bertoldi, F., & McKee, C. F. 1992, ApJ, 395, 140

Bonnell, I. A., & Bate, M. R. 2006, MNRAS, 370, 488

Breen, S. L., Ellingsen, S. P., Caswell, J. L., & Lewis, B. E. 2010, MNRAS, 401, 2219

Busquet, G., Estalella, R., Zhang, Q., Viti, S., Palau, A., Ho, P. T. P., & Sanchez-Monge, A. 2011, A&A, 525, A141

Carey, S. J., et al. 2009, PASP, 121, 76

Caselli, P., & Myers, P. C. 1995, ApJ, 446, 665

Clauset, A., Rohilla Shalizi, C., & Newman, M. E. J. 2007, arXiv:0706.1062

Daflon, S., & Cunha, K. 2004, ApJ, 617, 1115

Dame, T. M., Hartmann, D., & Thaddeus, P. 2001, ApJ, 547, 792

De Buizer, J. M., Radomski, J. T., Telesco, C. M., & Piña, R. K. 2005, ApJS, 156, 179

```
THE ASTROPHYSICAL JOURNAL SUPPLEMENT SERIES, 195:14 (24pp), 2011 August
Dunham, M. K., Robitaille, T. P., Evans, N. J., II, Schlingman, W. M.,
   Cyganowski, C. J., & Urquhart, J. 2011, ApJ, 731, 90
Dunham, M. K., et al. 2010, ApJ, 717, 1157
Egan, M. P., Carey, S. J., Price, S. D., Shipman, R. F., Feldman, P., & Redman, R.
   1999, in The Universe as Seen by ISO, ed. P. Cox & M. F. Kessler (ESA-SP
Ellingsen, S. P., Voronkov, M. A., Cragg, D. M., Sobolev, A. M., Breen, S. L.,
   & Godfrey, P. D. 2007, in IAU Symp. 242, Astrophysical Masers and Their
   Environments, ed. J. M. Chapman & W. A. Baan (Cambridge: Cambridge
   Univ. Press), 213
Evans, N. J., II. 1999, ARA&A, 37, 311
Evans, N. J., et al. 2009, ApJS, 181, 321
Fall, S. M., Krumholz, M. R., & Matzner, C. D. 2010, ApJ, 710, L142
Giovanelli, R., et al. 2005, AJ, 130, 2598
Gregersen, E. M., Evans, N. J., II, Mardones, D., & Myers, P. C. 2000, ApJ,
   533, 440
Hildebrand, R. H. 1983, QJRAS, 24, 267
Jackson, J. M., Finn, S. C., Rathborne, J. M., Chambers, E. T., & Simon, R.
   2008, ApJ, 680, 349
Jackson, J. M., et al. 2006, ApJS, 163, 145
Johnstone, D., & Bally, J. 2006, ApJ, 653, 383
Jørgensen, J. K., Schöier, F. L., & van Dishoeck, E. F. 2004, A&A, 416, 603
Kolpak, M. A., Jackson, J. M., Bania, T. M., Clemens, D. P., & Dickey, J. M.
   2003, ApJ, 582, 756
Krumholz, M. R., & McKee, C. F. 2008, Nature, 451, 1082
Lada, C. J. 1987, in Proc. on Symp. on Star Forming Regions, Vol. 115, ed. M.
   Peimbert & J. Jugaku (Dordrecht: Reidel), 1
Larson, R. B. 1981, MNRAS, 194, 809
Lauria, et al. 2006, ALMA Memo, 553 (http://www.alma.nrao.edu/memos/html-
   memos/alma553/memo553.pdf)
Longmore, S. N., Burton, M. G., Barnes, P. J., Wong, T., Purcell, C. R., & Ott,
                    3, 379, 535
   J. 2007, MNR
Maíz Apellániz, J., & Úbeda, L. 2005, ApJ, 629, 873
Mangum, J. G. 1993, PASP, 105, 117
Markwardt, C. B. 2009, in ASP Conf. Ser. 411, Astronomical Data Analysis
   Software and Systems XVIII, ed. David A. Bohlender, Daniel Durand, &
   Patrick Dowler (San Francisco, CA: ASP), 251
McKee, C. F., & Ostriker, E. C. 2007, ARA&A, 45, 565
Minier, V., Burton, M. G., Hill, T., Pestalozzi, M. R., Purcell, C. R., Garay, G.,
   Walsh, A. J., & Longmore, S. 2005, A&A, 429, 945
Molinari, S., et al. 2010, PASP, 122, 314
```

D. 2007, A&A, 476, 1243

143, 469

Press), 217

```
Ossenkopf, V., & Henning, T. 1994, A&A, 291, 943
                                                                                    Penzias, A. A., & Burrus, C. A. 1973, ARA&A, 11, 51
                                                                                    Peretto, N., & Fuller, G. A. 2009, A&A, 505, 405
                                                                                    Peretto, N., & Fuller, G. A. 2010, ApJ, 723, 555
                                                                                    Phillips, T. G., Huggins, P. J., Wannier, P. G., & Scoville, N. Z. 1979, ApJ, 231,
                                                                                    Pirogov, L., Zinchenko, I., Caselli, P., & Johansson, L. E. B. 2007, A&A, 461,
                                                                                       523
                                                                                    Plume, R., Jaffe, D. T., Evans, N. J., II, Martin-Pintado, J., & Gomez-Gonzalez,
                                                                                       J. 1997, ApJ, 476, 730
                                                                                    Purcell, C. R., Longmore, S. N., Burton, M. G., Walsh, A. J., Minier,
                                                                                       V., Cunningham, M. R., & Balasubramanyam, R. 2009, MNRAS, 394,
                                                                                    Rathborne, J. M., Jackson, J. M., Chambers, E. T., Simon, R., Shipman, R., &
                                                                                       Frieswijk, W. 2005, ApJ, 630, L181
                                                                                    Redman, M. P., Keto, E., Rawlings, J. M. C., & Williams, D. A. 2004, MNRAS,
                                                                                       352, 1365
                                                                                    Reid, M. J., Menten, K. M., Brunthaler, A., Zheng, X. W., Moscadelli, L., &
                                                                                       Xu. Y. 2009a, ApJ, 693, 397
                                                                                    Reid, M. J., et al. 2009b, ApJ, 700, 137
                                                                                    Reiter, M., Shirley, Y. L., Wu, J., Brogan, C., Wootten, A., & Tatematsu, K.
                                                                                       2011, ApJS, 195, 1
                                                                                    Rosolowsky, E., et al. 2010, ApJS, 188, 123
                                                                                    Rosolowsky, E. W., Pineda, J. E., Foster, J. B., Borkin, M. A., Kauffmann, J.,
                                                                                       Caselli, P., Myers, P. C., & Goodman, A. A. 2008, ApJS, 175, 509
                                                                                    Schieder, R., & Kramer, C. 2001, A&A, 373, 746
                                                                                    Schneider, N., Bontemps, S., Simon, R., Jakob, H., Motte, F., Miller, M., Kramer,\\
                                                                                       C., & Stutzki, J. 2006, A&A, 458, 855
                                                                                    Schuller, F., et al. 2009, A&A, 504, 415
                                                                                    Scoville, N. Z., Yun, M. S., Sanders, D. B., Clemens, D. P., & Waller, W. H.
                                                                                       1987, ApJS, 63, 821
                                                                                    Shirley, Y. L., Evans, N. J., II, & Rawlings, J. M. C. 2002, ApJ, 575,
                                                                                    Shirley, Y. L., Evans, N. J., II, Young, K. E., Knez, C., & Jaffe, D. T. 2003, ApJS,
                                                                                       149, 375
                                                                                    Shu, F. H., Adams, F. C., & Lizano, S. 1987, ARA&A, 25, 23
                                                                                    Simon, R., Jackson, J. M., Rathborne, J. M., & Chambers, E. T. 2006, ApJ, 639,
                                                                                    Swift, J. J., & Beaumont, C. N. 2010, PASP, 122, 224
Motte, F., Bontemps, S., Schilke, P., Schneider, N., Menten, K. M., & Broguière,
                                                                                    Tafalla, M., Santiago-García, J., Myers, P. C., Caselli, P., Walmsley, C. M., &
                                                                                       Crapsi, A. 2006, A&A, 455, 577
Mueller, K. E., Shirley, Y. L., Evans, N. J., II, & Jacobson, H. R. 2002, ApJS,
                                                                                    van der Tak, F. F. S., Black, J. H., Schöier, F. L., Jansen, D. J., & van Dishoeck,
                                                                                       E. F. 2007, A&A, 468, 627
Myers, P. C., Evans, N. J., II, & Ohashi, N. 2000, in Protostars and Planets IV,
                                                                                    Wood, D. O. S., & Churchwell, E. 1989, ApJS, 69, 831
   ed. V. Mannings, A. P. Boss, & S. S Russell (Tucson, AZ: Univ. Arizona
                                                                                    Wu, J., & Evans, N. J., II. 2003, ApJ, 592, L79
                                                                                    Wu, J., Evans, N. J., Shirley, Y. L., & Knez, C. 2010, ApJS, 188, 313
```

Nagayama, T., Omodaka, T., Nakagawa, A., Handa, T., Honma, M., Kobayashi,

H., Kawaguchi, N., & Ueno, Y. 2011, arXiv:1104.0363